# Web Information Processing and Applications: Web Mining

## Roadmap



Content Mining

Structure Mining

Web

Mining

Mining

Classification, Clustering

Social network analysis

Recommendation

# What do the following things have in common?

- World economy
- Human cell
- Railroads
- Brain
- Internet
- Friends and Family
- Media & Information
- Society



# The Network!

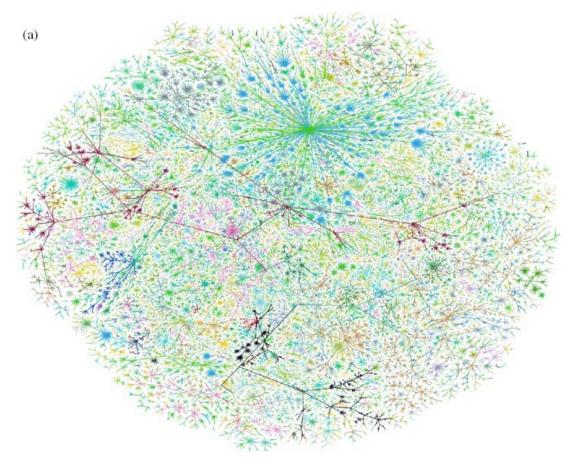
Behind each such system there is an intricate wiring diagram, a network, that defines the interactions between the components

## Networks: Social



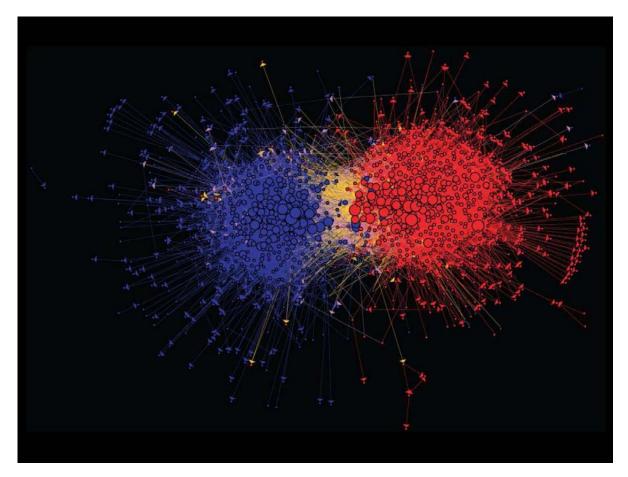
Facebook social graph 4-degrees of separation

## Networks: Communication



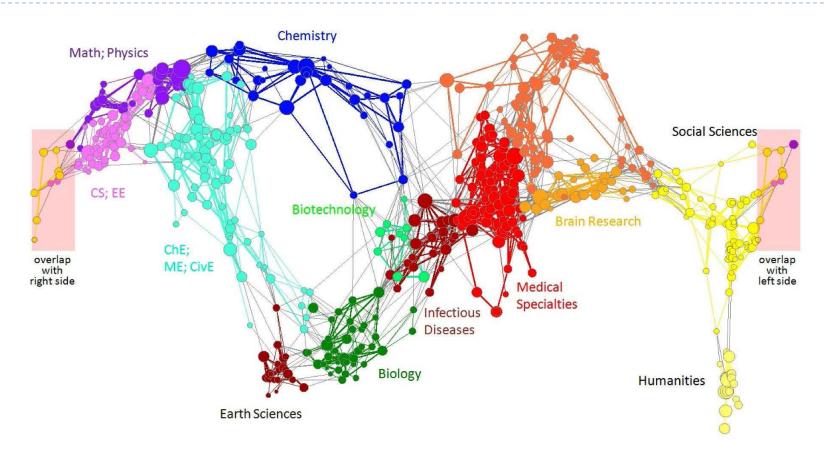
Graph of the Internet (Autonomous Systems)
Power-law degrees

### Networks: Media



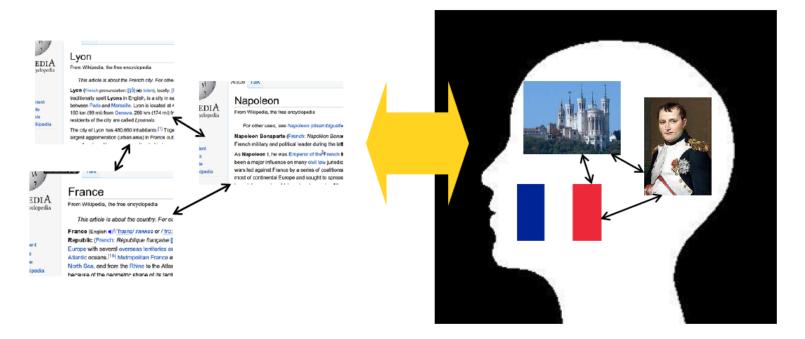
Connections between political blogs Polarization of the network

#### Networks: Information



Citation networks and Maps of science

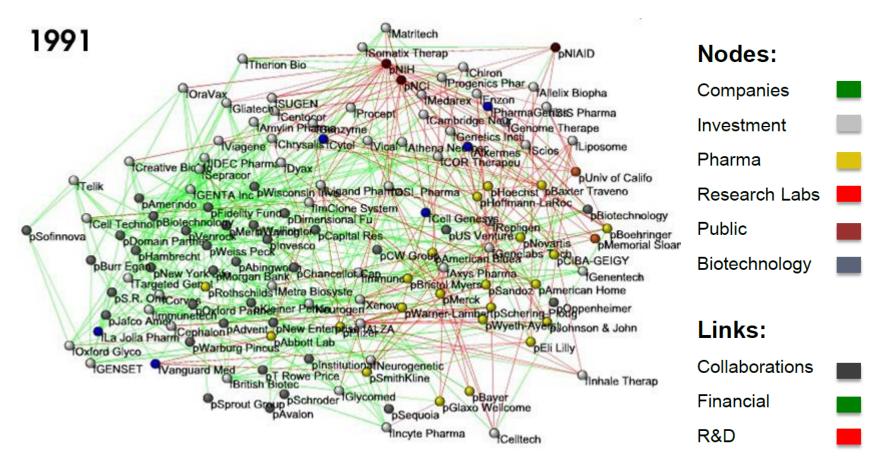
# Networks: Knowledge



Understand how humans navigate Wikipedia

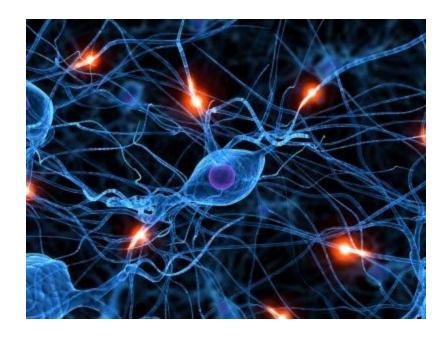
Get an idea of how people connect concepts

# Networks: Economy



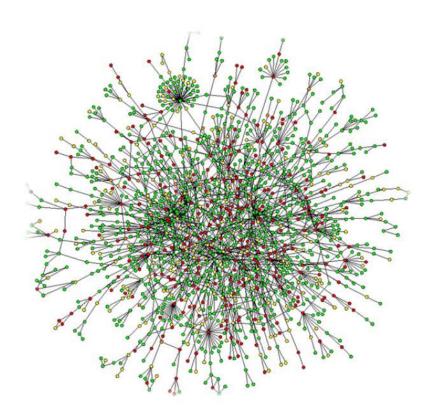
Bio-tech companies

## Networks: Brain



Human brain has between 10-100 billion neurons

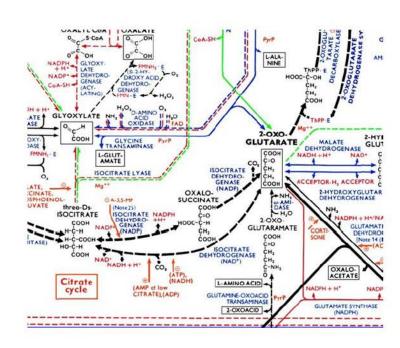
# Networks: Biology



#### Protein-Protein Interaction Networks:

**Nodes: Proteins** 

Edges: 'physical' interactions



#### Metabolic networks:

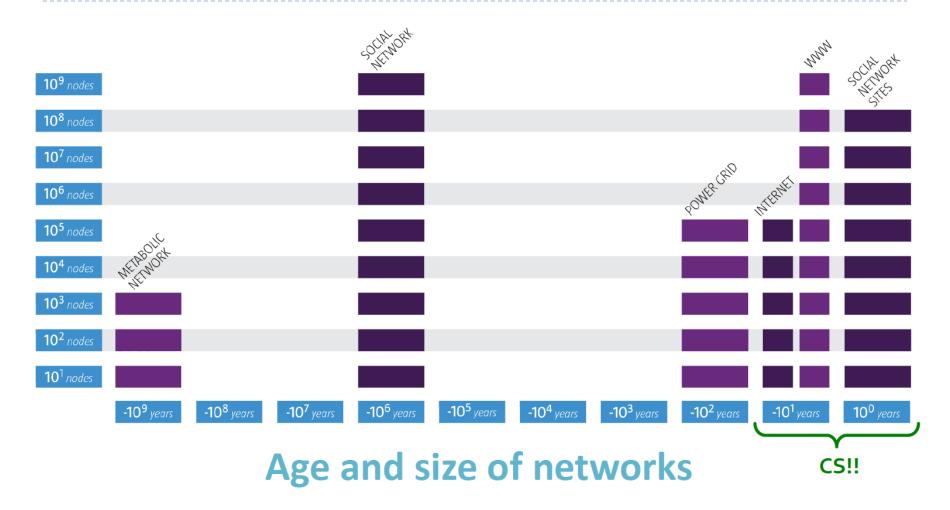
Nodes: Metabolites and enzymes

Edges: Chemical reactions

# Why Networks?

- Universal language for describing complex data
  - Networks from science, nature, and technology are more similar than one would expect
- Shared vocabulary between fields
  - Computer Science, Social Science, Physics, Economics, Statistics, Biology
- Data availability
  - Web/mobile, bio, health, and medical
- Impact!
  - Social networking, social media...

## Networks: Why Now?



#### Networks: Size Matters

#### Network data: Orders of magnitude

- ▶ 436-node network of email exchange at a corporate research lab [Adamic-Adar, SocNets '03]
- ▶ 43,553-node network of email exchange at a university [Kossinets-Watts, Science '06]
- ▶ 4.4-million-node network of declared friendships on a blogging community [Liben-Nowell et al., PNAS '05]
- ▶ 240-million-node network of communication on Microsoft Messenger [Leskovec-Horvitz, WWW '08]
- ▶ 800-million-node Facebook network [Backstrom et al. 'I I]

#### Networks: Online

- Communication networks:
  - ▶ Intrusion (入侵) / fraud (欺诈) detection,

#### Social networks:

- Link prediction, friend recommendation
- Social circle detection, community detection
- Social recommendations
- Identifying influential nodes, Viral marketing

#### Information networks:

Navigational aids

## Networks: Impact



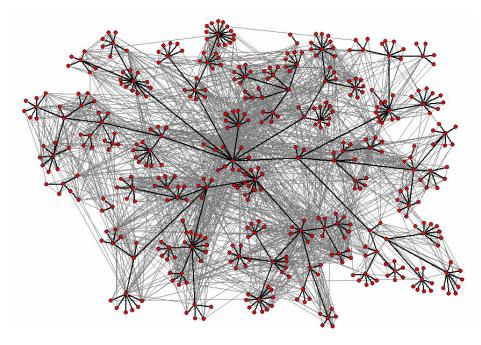






# Web/Networks Structure Mining: Structure of the Web Graph

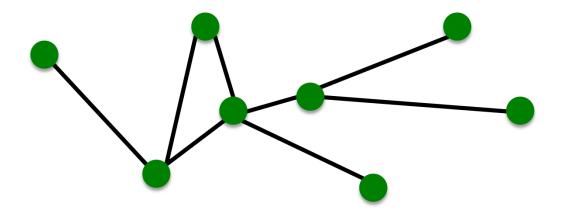
#### Structure of Networks?



Network is a collection of objects where some pairs of objects are connected by links

What is the structure of the network?

## Components of a Network



- ▶ Objects: nodes, vertices
- ► Interactions: links, edges E
- **System:** network, graph G=(V, E)

## Networks or Graphs?

- Network often refers to real systems
  - Web, Social network, Metabolic network

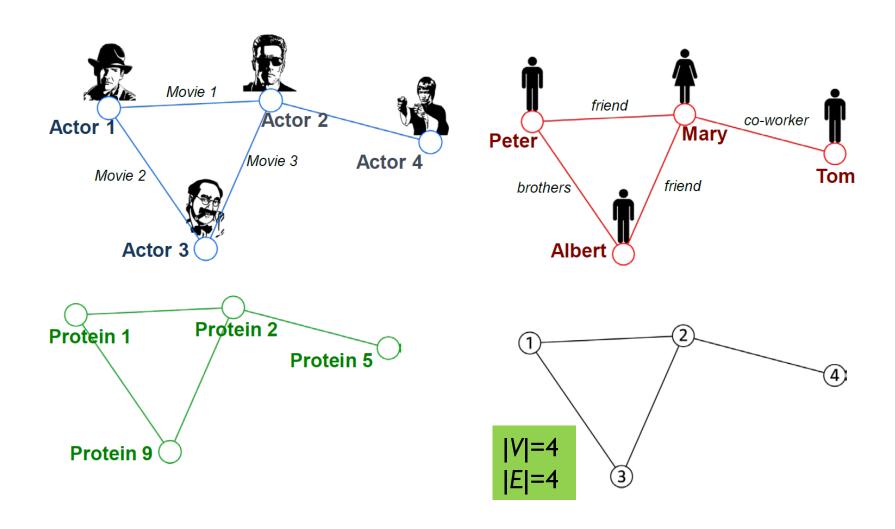
Language: Network, node, link

- ▶ Graph is mathematical representation of a network
  - Web graph, Social graph (a Facebook term)

Language: Graph, vertex, edge

In most cases we will use the two terms interchangeably

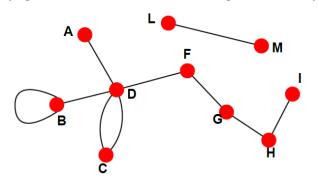
# Networks: Common Language



#### Undirected vs. Directed Networks

#### **Undirected**

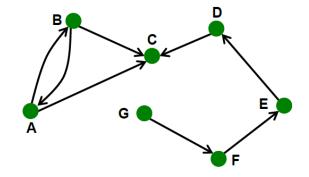
Links: undirected (symmetric, reciprocal)



- Examples:
  - Collaborations
  - Friendship on Facebook

#### **Directed**

Links: directed (arcs)



- Examples:
  - Phone calls
  - Following on Twitter

## Web as a Graph

Q:What does the Web "look like"?



- Here is what we will do next:
  - We will take a real system (i.e., the Web)
  - We will collect lots of Web data
  - We will represent the Web as a graph
  - We will use language of graph theory to reason about the structure of the graph
  - Do a computational experiment on the Web graph
  - Learn something about the structure of the Web!

# Web/Networks Structure Mining: Communities

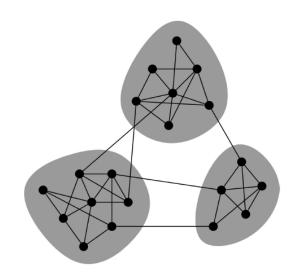
One of the most important structural properties in networks

## Network Communities (社区)

 Granovetter's theory (and common sense) suggest that networks are composed of tightly connected sets of nodes

#### Network communities:

Sets of nodes with lots of connections inside and few to outside (the rest of the network)

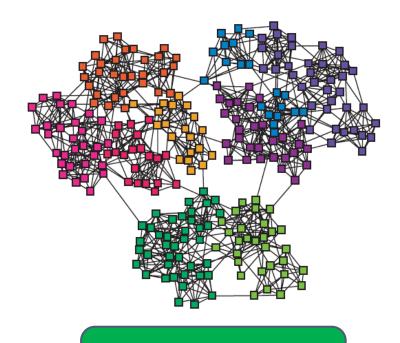


Communities, Clusters, Groups, Modules

# Finding Network Communities

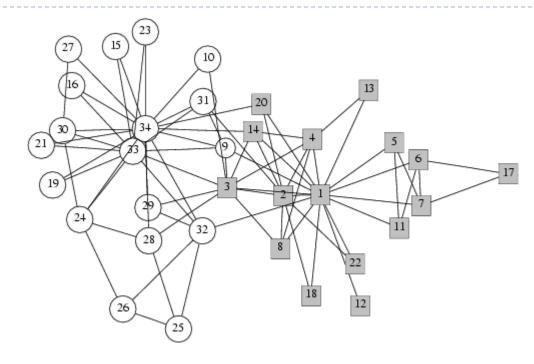
How to automatically find such densely connected groups of nodes?

 Ideally such automatically detected clusters would then correspond to real groups



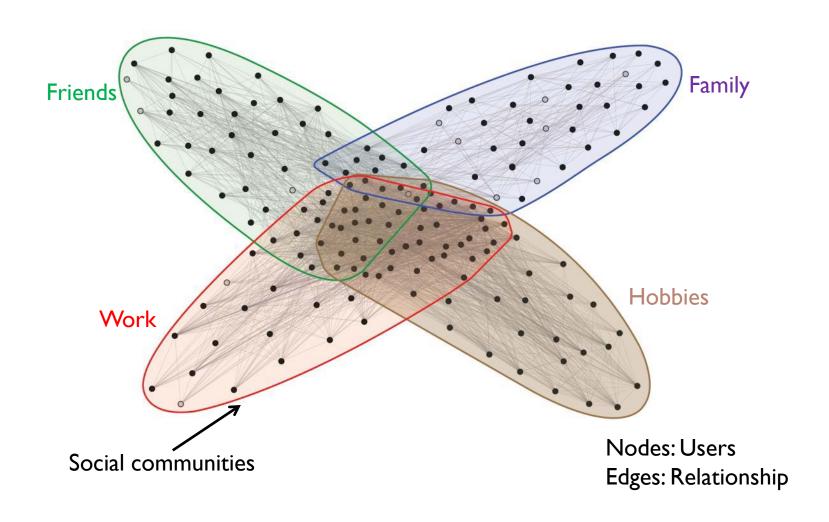
Communities, Clusters, Groups, Modules

# Zachary's Karate Club Network

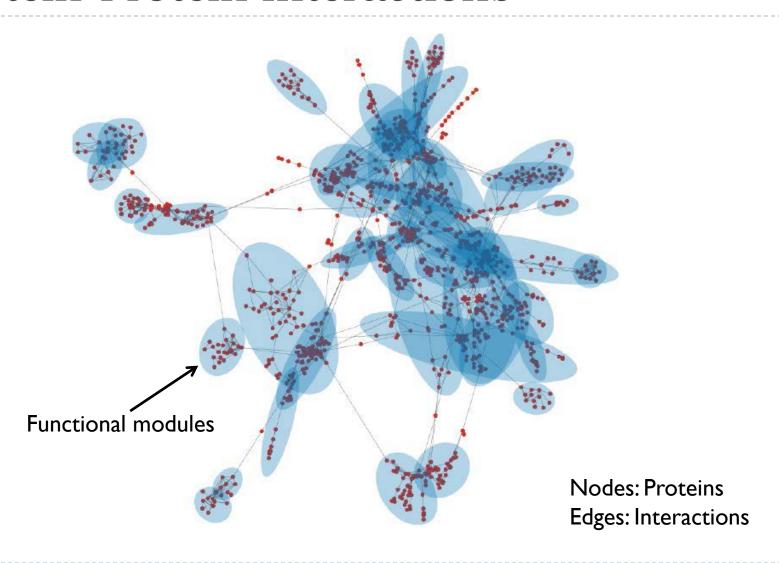


- Social ties and rivalries in a university karate club
- Two conflicting groups
- Split could be explained by a minimum cut in the network

## Social Communities

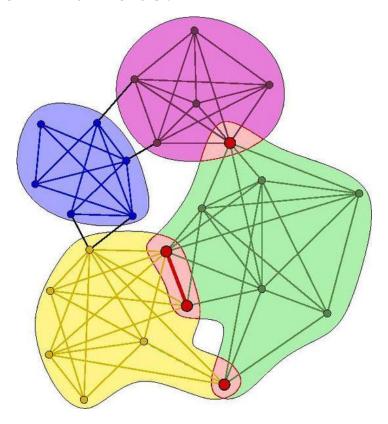


## Protein-Protein Interactions



## Community Detection

▶ How to find communities?



We will work with **undirected** networks

## Community Detection Methods

### Connection between community detection and clustering

- Agglomerative hierarchical clustering
- Partitional clustering
  - ▶ K-means

Based on Structural Similarity

# Vertex Similarity

#### A: adjacency matrix of undirected G

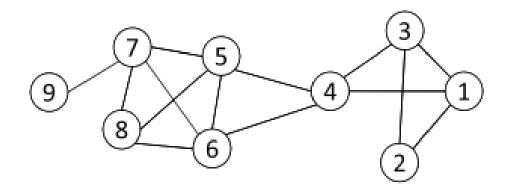
- $A_{ij} = I$  if (i,j) is an edge, else 0
- ullet Structural dissimilarity measure  $d_{ij} = \sqrt{\sum_{k 
  eq i,j} (A_{ik} A_{jk})^2}$
- Jaccard similarity

$$Jaccard(\mathbf{v}_i, \mathbf{v}_j) = \frac{|N_i \cap N_j|}{|N_i \cup N_j|}$$

Cosine similarity

$$cosine(\mathbf{v}_i, \mathbf{v}_j) = \frac{\sum_k A_{ik} A_{jk}}{\sqrt{\sum_s A_{is}^2} \sqrt{\sum_t A_{jt}^2}}$$

# Vertex Similarity



$$Jaccard(4,6) = \frac{|\{5\}|}{|\{1,3,4,5,6,7,8\}|} = \frac{1}{7}$$
$$cosine(4,6) = \frac{1}{\sqrt{4 \cdot 4}} = \frac{1}{4}$$

# Community Detection Methods

#### Connection between community detection and clustering

- Agglomerative hierarchical clustering
- Partitional clustering
  - K-means
- Divisive hierarchical algorithm Girvan and Newman
- Spectral graph cut
- Modularity maximization

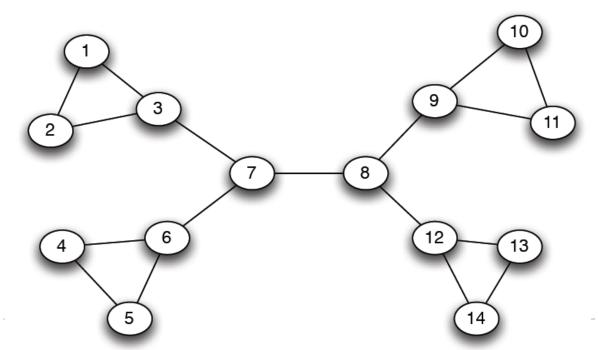
# Divisive Removal of Weak Ties/Bridges

#### Bridges:

Form part of the shortest path between pairs of nodes in different parts of the network

#### Simple idea:

Remove bridges and local bridges

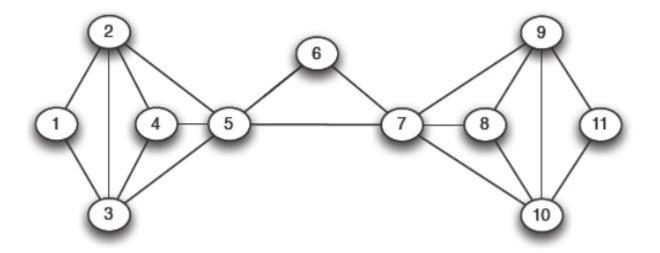


## Generalize the Role of Bridges

- Look for the edges that carry the most of "traffic" in a network
  - Without the edge, paths between many pairs of nodes may have to be "re-routed" a longer way
  - Edges to link different densely-connected regions
  - Good candidates for removal in a divisive method
  - Generalize the (local) bridges

#### Traffic in a Network

- For nodes A and B connected by a path assume I unit of "flow"
  - (If A and B in different connected components, flow = 0)
- Divide flow evenly along all possible shortest paths from A to B
  - if k shortest paths from A and B, then 1/k units of flow pass along each
- ▶ Eg: 2 shortest paths from I to 5, each with I/2 units of flow

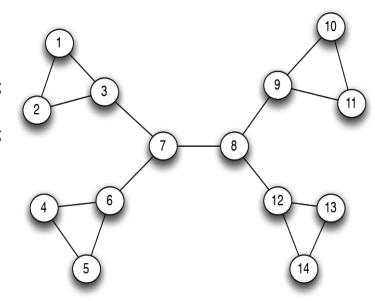


## Edge Betweenness

- Betweenness of an edge: the total amount of flow it carries
  - counting flow between all pairs of nodes using this edge

#### Eg:

- Edge 7-8: each pair of nodes between [1-7] and [8-14]; each pair with traffic = 1; total  $7 \times 7 = 49$
- Edge 3-7: each pair of nodes between [1-3] and [4-14]; each pair with traffic = 1; total 3 x 11 = 33
- Edge I-3: each pair of nodes between [1] and [3-14] (not node 2); each pair with traffic = 1; total 1 x 12 = 12
  - > similar for edges 2-3, 4-6, 5-6, 9-10, 9-11, 12-13, and 12-14
- Edge I-2: each pair of nodes between [I] and [2] (no other); each pair with traffic = I; total I x I = I
  - > similar for edges 4-5, 10-11, and 13-14



#### Girvan-Newman

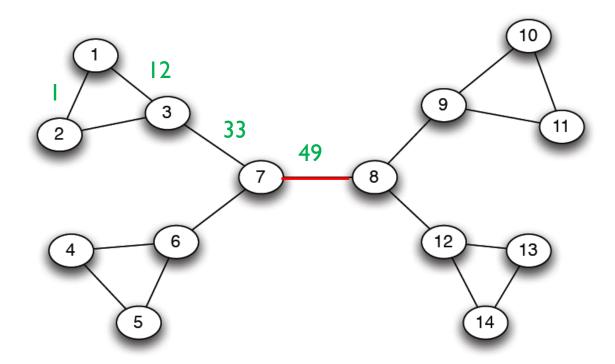
- Divisive hierarchical clustering based on the notion of edge betweenness:
  - Number of shortest paths passing through the edge
- Girvan-Newman Algorithm:
  - Undirected unweighted networks

#### Repeat until no edges are left:

Homework

- Calculate betweenness of edges  $(O(mn), or O(n^2))$  on a sparse graph, with breadth-first-search
- Remove edges with highest betweenness
- Connected components are communities
- Gives a hierarchical decomposition of the network

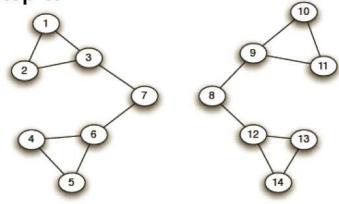
# Girvan-Newman: Example



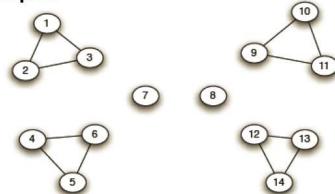
Need to re-compute betweenness at every step

# Girvan-Newman: Example

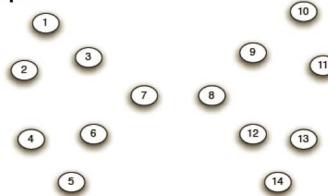
#### Step 1:



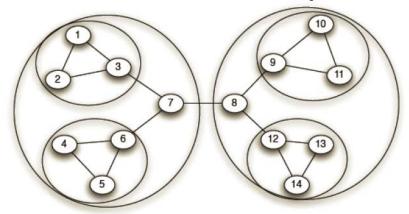
#### Step 2:



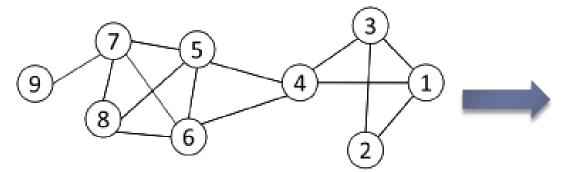
#### Step 3:



#### Hierarchical network decomposition:

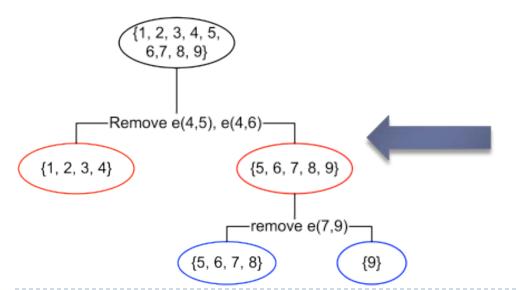


# Divisive clustering based on edge betweenness



#### Initial betweenness value

Table 3.3: Edge Betweenness									
	1	2	3	4	5	6	7	8	9
1	0	4	1	9	0	0	0	0	0
2	4	0	4	0	0	0	0	0	0
3	1	4	0	9	0	0	0	0	0
4	9	0	9	0	10	10	0	0	0
5	0	0	0	10	0	1	6	3	0
6	0	0	0	10	1	0	6	3	0
7	0	0	0	0	6	6	0	2	8
8	0	0	0	0	3	3	2	0	0
9	0	0	0	0	0	0	8	0	0



After remove e(4,5), the betweenness of e(4,6) becomes 20, which is the highest;

After remove e(4,6), the edge e(7,9) has the highest betweenness value 4, and should be removed.

### Girvan-Newman: Results

