

**TUGAS MINGGU KE-12**  
**STATISTIKA DESKRIPTIF**



**NAMA : MUKHAMAD IKHSANUDIN**

**NIM : 082011633086**

**PROGRAM STUDI S1 SISTEM INFORMASI**

**FAKULTAS SAINS DAN TEKNOLOGI**

**UNIVERSITAS AIRLANGGA**

**2021**

Tugas pertemuan 24 → dikumpulkan hari ini, tgl. 04-06-2021 jam 23.59 → di upload ke Aula dan kirim ke email eto-w@fst.unair .ac.id dengan subject : PCA

Code dan outputnya jadikan satu di notebook R-nya

Gunakan prcomp() and princomp() functions untuk masing-masing soal berikut :

1. Carilah data yang sesuai untuk PCA dengan covarians
  - a. Tampilkan eigenvalue-nya (variansnya) → table dan grafik
  - b. Tampilkan matriks PC-nya
  - c. Plot di 2-dimensi untuk individunya
  - d. Plot di 2-dimensi untuk variabelnya
  - e. Bi-Plot di 2-dimensi untuk individu dan variabelnya
  - f. Plot PC di 3-dimensi
  - g. Interpretasikan point c s.d f
2. Carilah data yang sesuai untuk PCA dengan correlation
  - a. Tampilkan eigenvalue-nya (variansnya) → table dan grafik
  - b. Tampilkan matriks PC-nya
  - c. Plot di 2-dimensi untuk individunya
  - d. Plot di 2-dimensi untuk variabelnya
  - e. Bi-Plot di 2-dimensi untuk individu dan variabelnya
  - f. Plot PC di 3-dimensi
  - g. Interpretasikan point c s.d f

=====

Code ditaruh diantara tanda berikut :

```
```{R}
```

Syntax di sini

```
```
```

1. Carilah data yang sesuai untuk PCA dengan covarians

```
```{r}
#No 1
library(dplyr)
PCA_Data <- select(mtcars, c(1:7, 10:11))
head(PCA_Data[, -9])
```
```

| Description: df[,8] [6 x 8] |              |              |               |             |               |             |               |               |
|-----------------------------|--------------|--------------|---------------|-------------|---------------|-------------|---------------|---------------|
|                             | mpg<br><dbl> | cyl<br><dbl> | disp<br><dbl> | hp<br><dbl> | drat<br><dbl> | wt<br><dbl> | qsec<br><dbl> | gear<br><dbl> |
| Mazda RX4                   | 21.0         | 6            | 160           | 110         | 3.90          | 2.620       | 16.46         | 4             |
| Mazda RX4 Wag               | 21.0         | 6            | 160           | 110         | 3.90          | 2.875       | 17.02         | 4             |
| Datsun 710                  | 22.8         | 4            | 108           | 93          | 3.85          | 2.320       | 18.61         | 4             |
| Hornet 4 Drive              | 21.4         | 6            | 258           | 110         | 3.08          | 3.215       | 19.44         | 3             |
| Hornet Sportabout           | 18.7         | 8            | 360           | 175         | 3.15          | 3.440       | 17.02         | 3             |
| Valiant                     | 18.1         | 6            | 225           | 105         | 2.76          | 3.460       | 20.22         | 3             |

6 rows

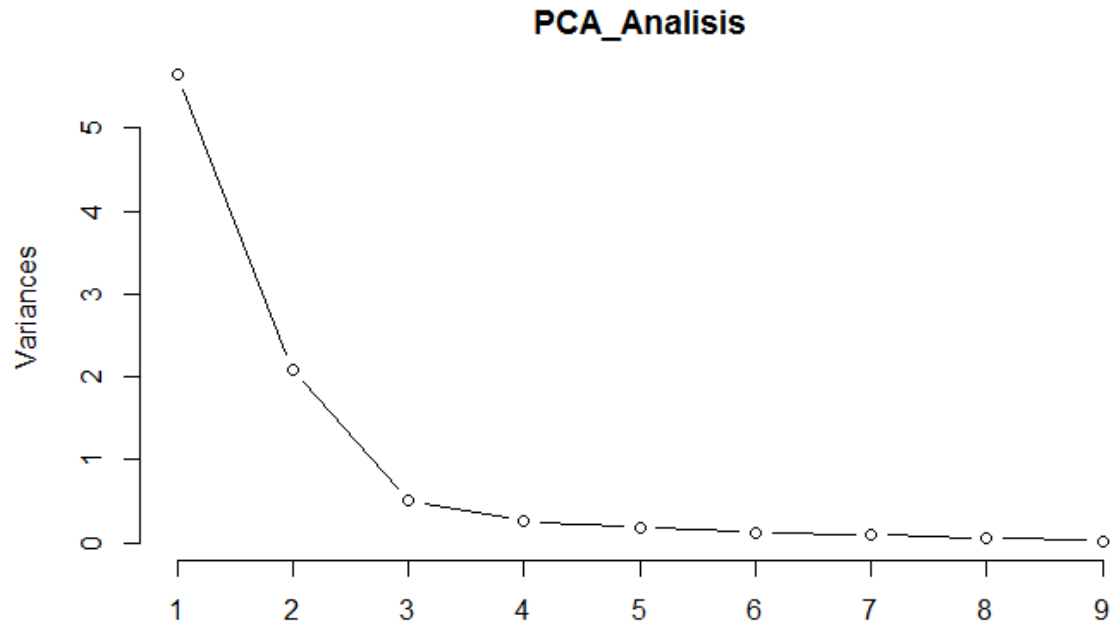
a. Tampilkan eigenvalue-nya (variansnya) → table dan grafik

```
```{r}
#a. Tampilkan eigen valuenya (variansnya)
PCA_Standardized <- scale(x = PCA_Data)
Covarian_Matrix <- cov(PCA_Standardized)
Nilai_Eigen <- eigen(Covarian_Matrix)
Nilai_Eigen
PCA_Analisis <- prcomp(x = PCA_Data, scale. = TRUE, center = TRUE)
PCA_Analisis
plot(PCA_Analisis, type = "l")
```
```

```
eigen() decomposition
$values
[1] 5.65593947 2.08210029 0.50421482 0.26502753 0.18315864 0.12379319 0.10506192 0.05851375
[9] 0.02219038

$vectors
      [,1]      [,2]      [,3]      [,4]      [,5]      [,6]      [,7]
[1,] 0.3931477 -0.02753861 -0.22119309 -0.006126378 -0.3207620 0.72015586 0.38138068
[2,] -0.4025537 -0.01570975 -0.25231615 0.040700251 0.1171397 0.22432550 0.15893251
[3,] -0.3973528 0.08888469 -0.07825139 0.339493732 -0.4867849 -0.01967516 0.18233095
[4,] -0.3670814 -0.26941371 -0.01721159 0.068300993 -0.2947317 0.35394225 -0.69620751
[5,] 0.3118165 -0.34165268 0.14995507 0.845658485 0.1619259 -0.01536794 -0.04767957
[6,] -0.3734771 0.17194306 0.45373418 0.191260029 -0.1874822 -0.08377237 0.42777608
[7,] 0.2243508 0.48404435 0.62812782 -0.030329127 -0.1482495 0.25752940 -0.27622581
[8,] 0.2094749 -0.55078264 0.20658376 -0.282381831 -0.5624860 -0.32298239 0.08555707
[9,] -0.2445807 -0.48431310 0.46412069 -0.214492216 0.3997820 0.35706914 0.20604210

      [,8]      [,9]
[1,] 0.12465987 -0.11492862
[2,] -0.81032177 -0.16266295
[3,] 0.06416707 0.66190812
[4,] 0.16573993 -0.25177306
[5,] -0.13505066 -0.03809096
[6,] 0.19839375 -0.56918844
[7,] -0.35613350 0.16873731
[8,] -0.31636479 -0.04719694
[9,] 0.10832772 0.32045892
```



b. Tampilkan matriks PC-nya

```
```{r}
#b. tampilkan matriks PC nya
PCA_Analisis_New <- princomp(x = PCA_Data)
PCA_Analisis_New
Covarian_Matrix <- cov(PCA_Standardized)
Covarian_Matrix
```
```

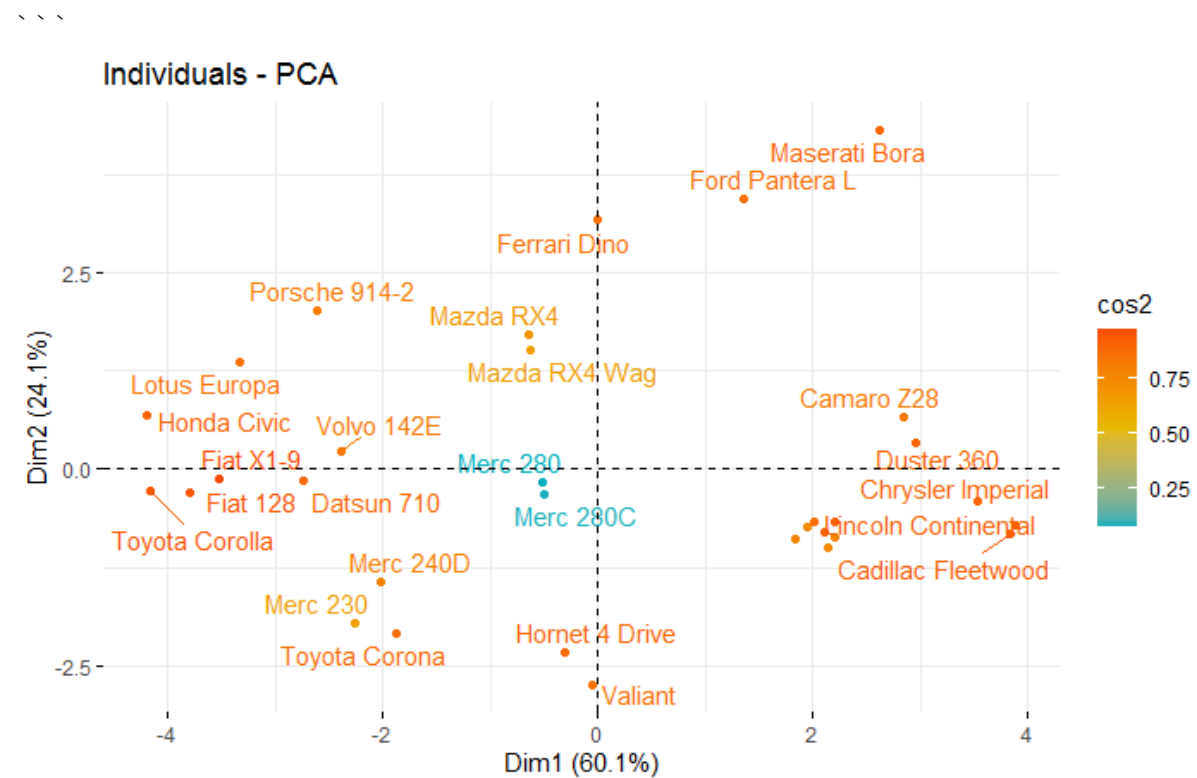
```
call:
princomp(x = PCA_Data)

Standard deviations:
  Comp.1    Comp.2    Comp.3    Comp.4    Comp.5    Comp.6    Comp.7    Comp.8
134.3820274  37.5465620   3.0181296   1.2548450   0.8904901   0.6371404   0.3006062   0.2814188
  Comp.9
   0.2124807

9 variables and 32 observations.
      mpg      cyl      disp      hp      drat      wt      qsec      gear
mpg  1.0000000 -0.8521620 -0.8475514 -0.7761684  0.68117191 -0.8676594  0.41868403  0.4802848
cyl -0.8521620  1.0000000  0.9020329  0.8324475 -0.69993811  0.7824958 -0.59124207 -0.4926866
disp -0.8475514  0.9020329  1.0000000  0.7909486 -0.71021393  0.8879799 -0.43369788 -0.5555692
hp  -0.7761684  0.8324475  0.7909486  1.0000000 -0.44875912  0.6587479 -0.70822339 -0.1257043
drat  0.6811719 -0.6999381 -0.7102139 -0.4487591  1.00000000 -0.7124406  0.09120476  0.6996101
wt  -0.8676594  0.7824958  0.8879799  0.6587479 -0.71244065  1.0000000 -0.17471588 -0.5832870
qsec  0.4186840 -0.5912421 -0.4336979 -0.7082234  0.09120476 -0.1747159  1.00000000 -0.2126822
gear  0.4802848 -0.4926866 -0.5555692 -0.1257043  0.69961013 -0.5832870 -0.21268223  1.0000000
carb -0.5509251  0.5269883  0.3949769  0.7498125 -0.09078980  0.4276059 -0.65624923  0.2740728
carb
mpg -0.5509251
cyl  0.5269883
disp  0.3949769
hp   0.7498125
drat -0.0907898
wt   0.4276059
qsec -0.6562492
gear  0.2740728
carb  1.0000000
```

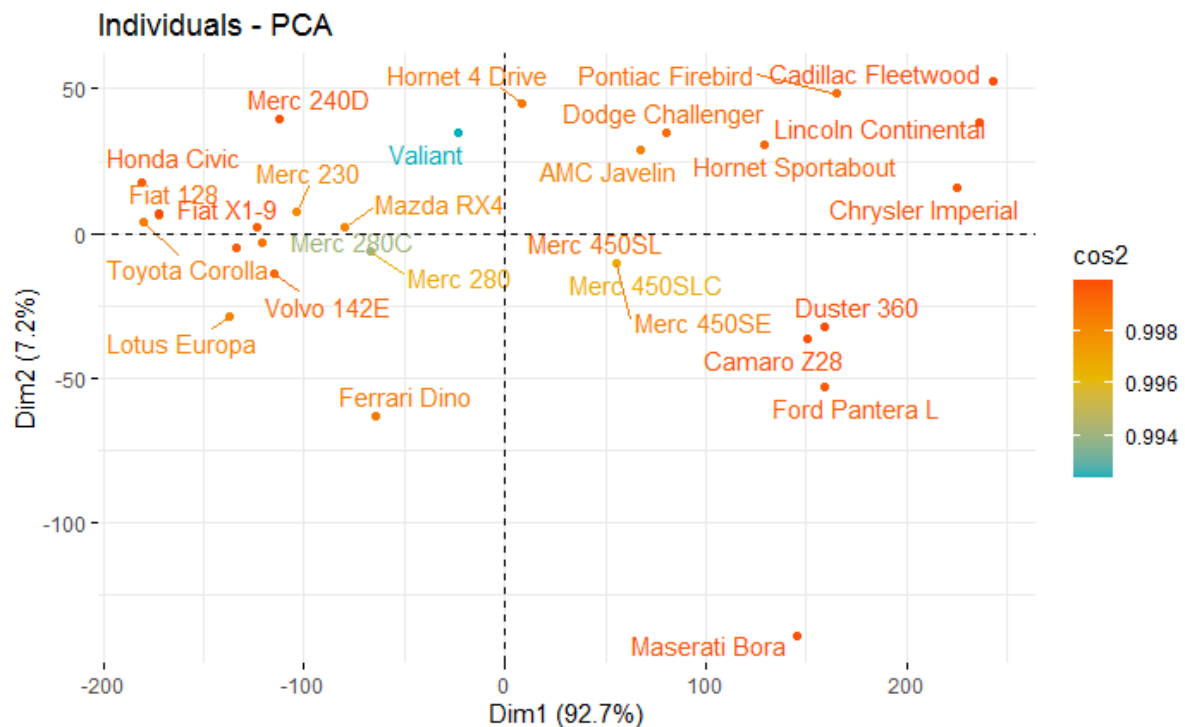
c. Plot di 2-dimensi untuk individunya

```
```{r}
#c. Plot di 2-dimensi untuk individunya
library(factoextra)
Visual_PCA_Cor <- prcomp(mtcars, scale = TRUE)
fviz_pca_ind(Visual_PCA_Cor, col.ind = "cos2", gradient.cols =
c("#00AFBB", "#E7B800", "#FC4E07"), repel = TRUE)
```



```
```{r}
library(factoextra)
Visual_PCA_Cov <- prcomp(mtcars, scale = FALSE)
fviz_pca_ind(Visual_PCA_Cov, col.ind = "cos2", gradient.cols =
c("#00AFBB", "#E7B800", "#FC4E07"), repel = TRUE)
```

```
```
```

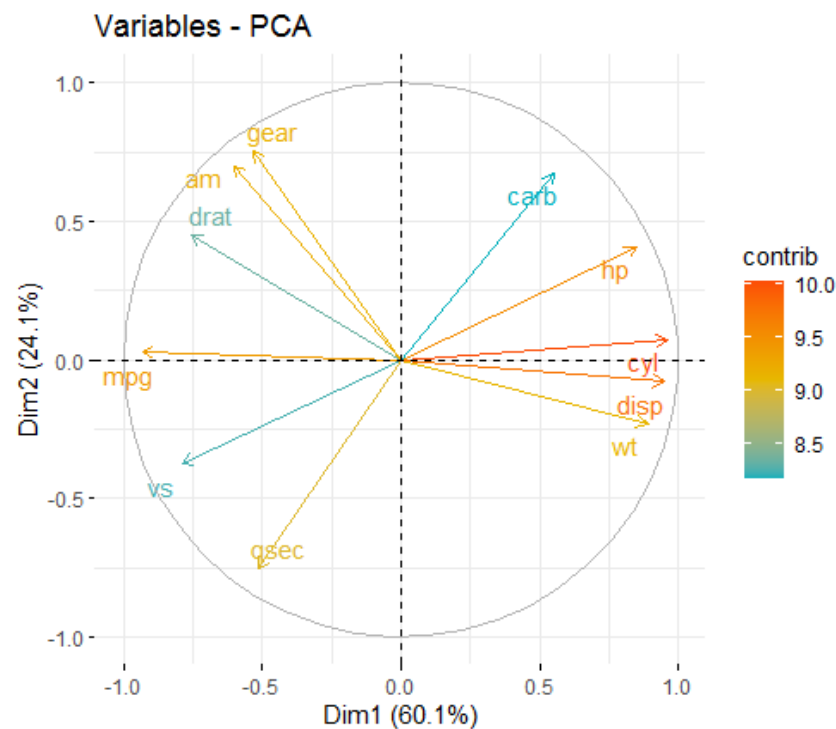


d. Plot di 2-dimensi untuk variabelnya

```

```{R}
#d Plot di 2-dimensi untuk variabelnya
fviz_pca_var(Visual_PCA_Cor, col.var = "contrib",
gradient.cols = c("#00AFBB", "#E7B800", "#FC4E07"), repel =
TRUE)
```

```



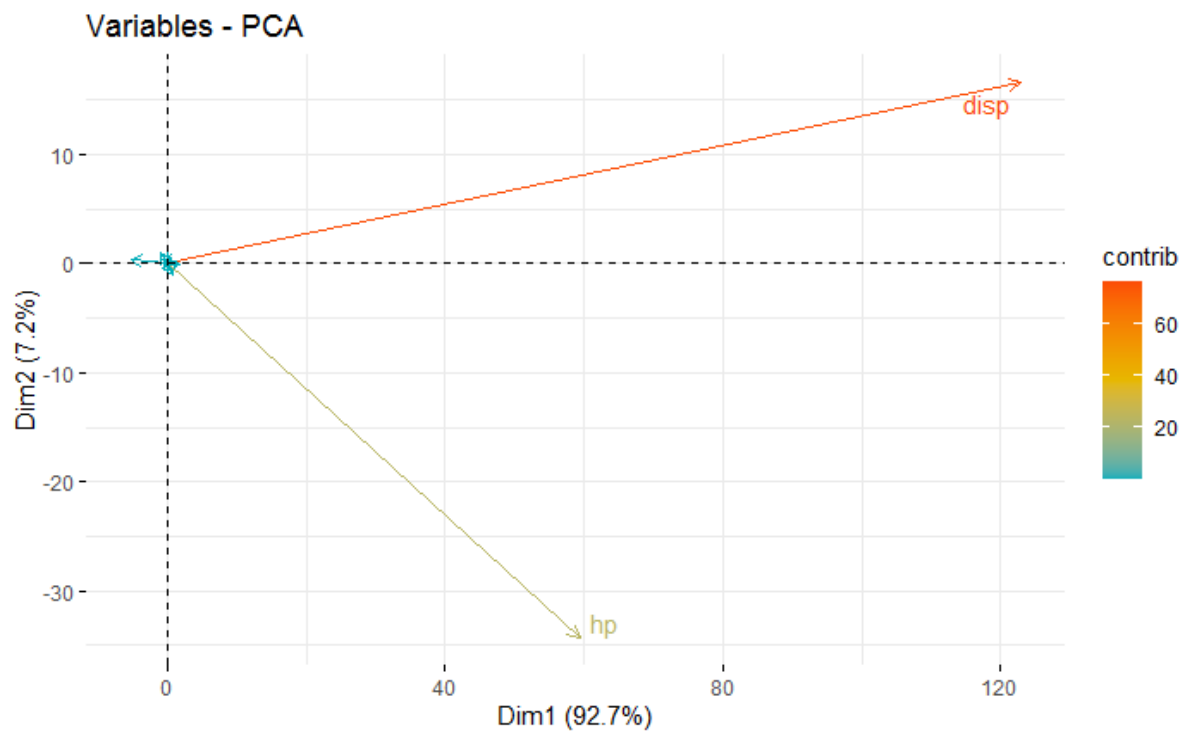
```

```{R}

```

```
fviz_pca_var(Visual_PCA_Cov, col.var = "contrib",
gradient.cols = c("#00AFBB", "#E7B800", "#FC4E07"), repel =
TRUE)
```

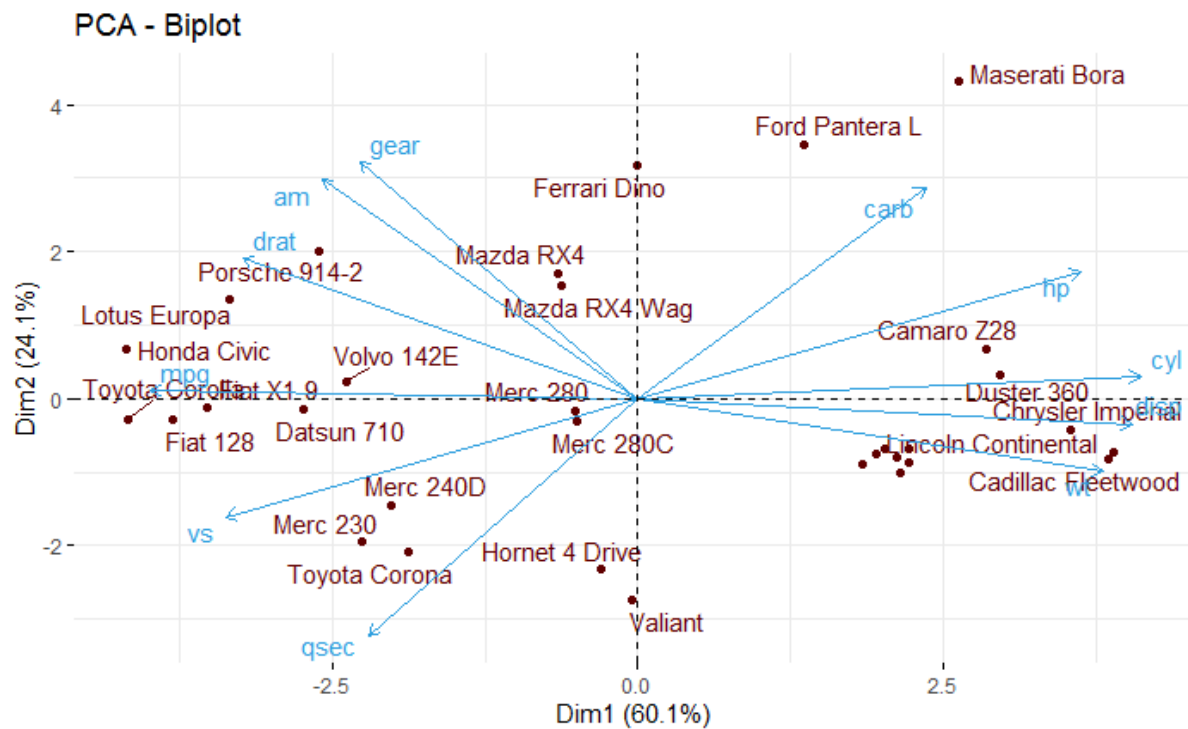
```



e. Bi-Plot di 2-dimensi untuk individu dan variabelnya

```
```{R}
#e. Bi-Plot di 2-dimensi untuk individu dan variabelnya
fviz_pca_biplot(Visual_PCA_Cor, repel = TRUE, col.var =
"#2E9FDF", col.ind = "#600000")
```

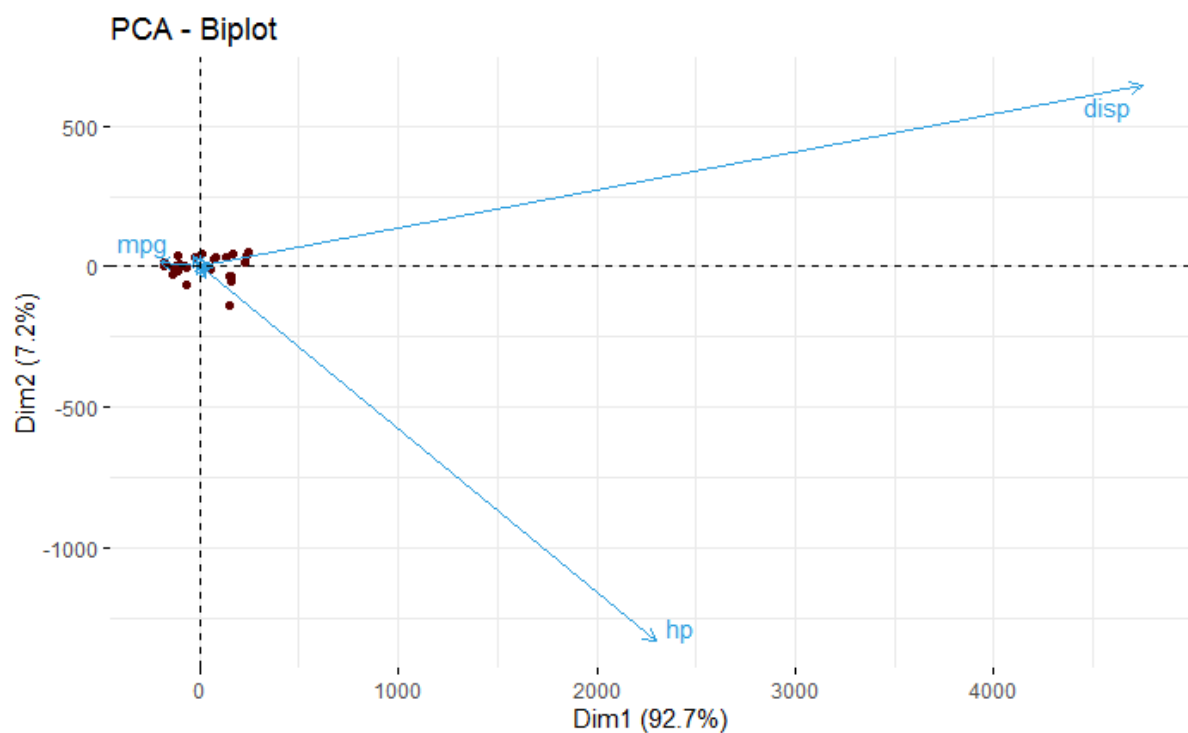
```



```

```{R}
fviz_pca_biplot(Visual_PCA_Cov, repel = TRUE, col.var =
"#2E9FDF", col.ind = "#600000")
```

```



f. Plot PC di 3-dimensi

```

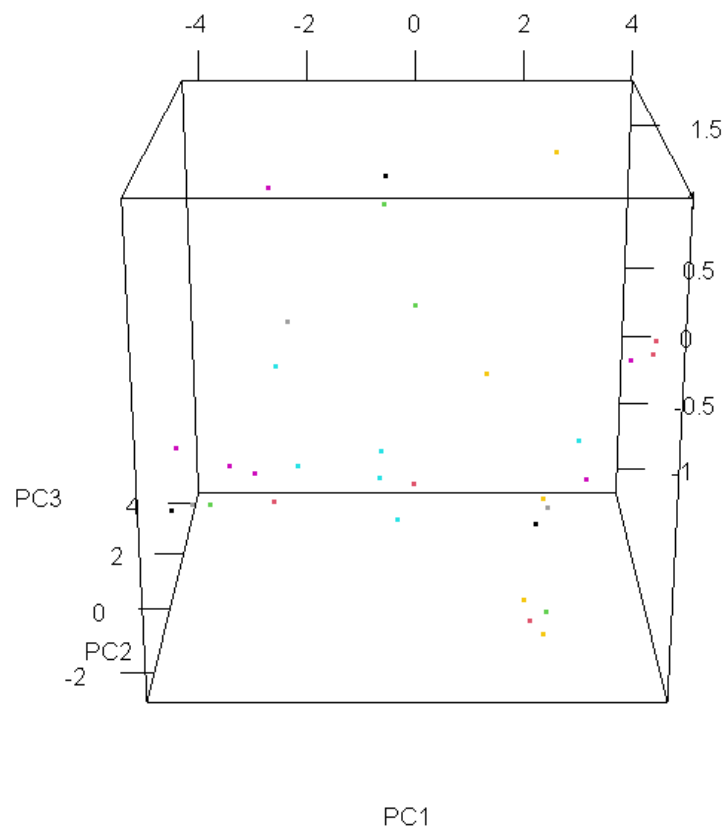
```{R}
#f. Plot PC di 3-dimensi
library(rgl)

```



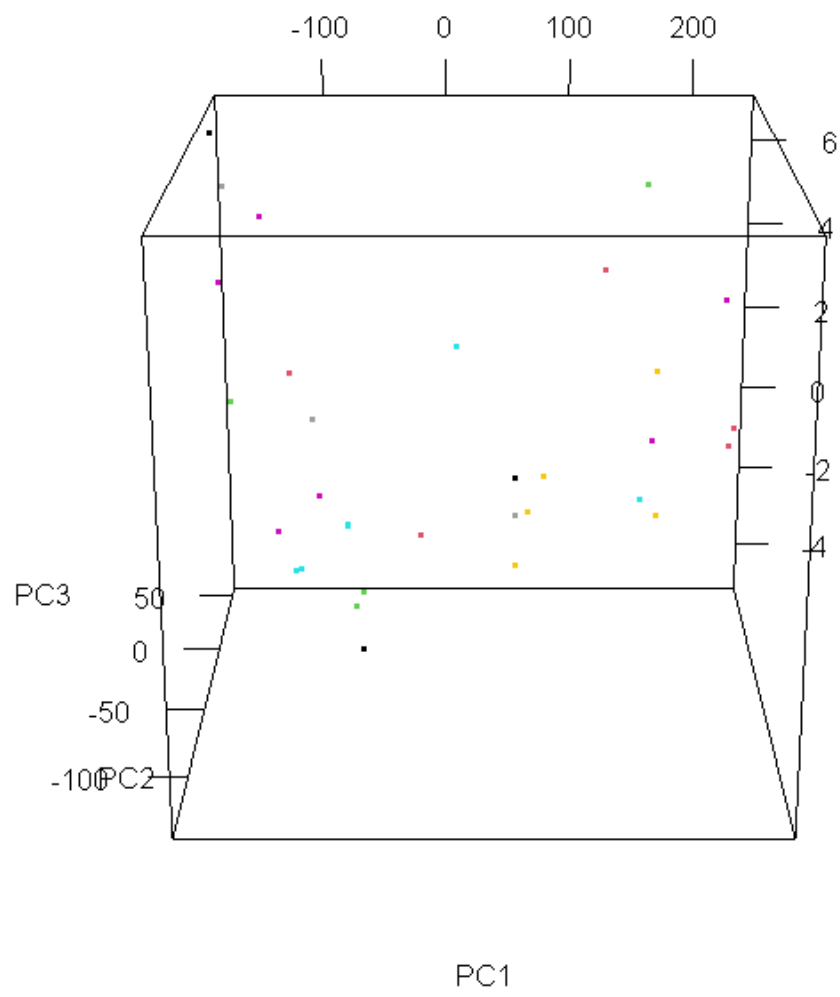
```
plot3d(Visual_PCA_Cor$x, col = PCA_Data$mpg)
```

```



```
```{R}
library(rgl)
plot3d(Visual_PCA_Cov$x, col = PCA_Data$mpg)
```

```



2. Carilah data yang sesuai untuk PCA dengan correlation

```
```{R}
#No 2
PCA_Standardized <- scale(x = PCA_Data)
Correlation_Matrix <- cor(PCA_Standardized)
Nilai_Eigen_Cor <- eigen(Correlation_Matrix)
Nilai_Eigen_Cor
PCA_Analisis_Cor <- prcomp(x = PCA_Data, scale. = TRUE, center
= TRUE)
PCA_Analisis_Cor
```
```

Description: df[,8] [6 x 8]

|                   | mpg<br><dbl> | cyl<br><dbl> | disp<br><dbl> | hp<br><dbl> | drat<br><dbl> | wt<br><dbl> | qsec<br><dbl> | gear<br><dbl> |
|-------------------|--------------|--------------|---------------|-------------|---------------|-------------|---------------|---------------|
| Mazda RX4         | 21.0         | 6            | 160           | 110         | 3.90          | 2.620       | 16.46         | 4             |
| Mazda RX4 Wag     | 21.0         | 6            | 160           | 110         | 3.90          | 2.875       | 17.02         | 4             |
| Datsun 710        | 22.8         | 4            | 108           | 93          | 3.85          | 2.320       | 18.61         | 4             |
| Hornet 4 Drive    | 21.4         | 6            | 258           | 110         | 3.08          | 3.215       | 19.44         | 3             |
| Hornet Sportabout | 18.7         | 8            | 360           | 175         | 3.15          | 3.440       | 17.02         | 3             |
| Valiant           | 18.1         | 6            | 225           | 105         | 2.76          | 3.460       | 20.22         | 3             |

6 rows

a. Tampilkan eigenvalue-nya (variannya) → table dan grafik

```
```{R}
#a. Tampilkan eigenvalue-nya (variannya)
Nilai_Eigen_Cor <- eigen(Correlation_Matrix)
Nilai_Eigen_Cor
```
```

```
eigen() decomposition
$values
[1] 5.65593947 2.08210029 0.50421482 0.26502753 0.18315864 0.12379319 0.10506192 0.05851375
[9] 0.02219038

$vectors
      [,1]      [,2]      [,3]      [,4]      [,5]      [,6]      [,7]
[1,] 0.3931477 -0.02753861 -0.22119309 -0.006126378 0.3207620 -0.72015586 0.38138068
[2,] -0.4025537 -0.01570975 -0.25231615 0.040700251 -0.1171397 -0.22432550 0.15893251
[3,] -0.3973528 0.08888469 -0.07825139 0.339493732 0.4867849 0.01967516 0.18233095
[4,] -0.3670814 -0.26941371 -0.01721159 0.068300993 0.2947317 -0.35394225 -0.69620751
[5,] 0.3118165 -0.34165268 0.14995507 0.845658485 -0.1619259 0.01536794 -0.04767957
[6,] -0.3734771 0.17194306 0.45373418 0.191260029 0.1874822 0.08377237 0.42777608
[7,] 0.2243508 0.48404435 0.62812782 -0.030329127 0.1482495 -0.25752940 -0.27622581
[8,] 0.2094749 -0.55078264 0.20658376 -0.282381831 0.5624860 0.32298239 0.08555707
[9,] -0.2445807 -0.48431310 0.46412069 -0.214492216 -0.3997820 -0.35706914 0.20604210

      [,8]      [,9]
[1,] 0.12465987 -0.11492862
[2,] -0.81032177 -0.16266295
[3,] 0.06416707 0.66190812
[4,] 0.16573993 -0.25177306
[5,] -0.13505066 -0.03809096
[6,] 0.19839375 -0.56918844
[7,] -0.35613350 0.16873731
[8,] -0.31636479 -0.04719694
[9,] 0.10832772 0.32045892
```

b. Tampilkan matriks PC-nya

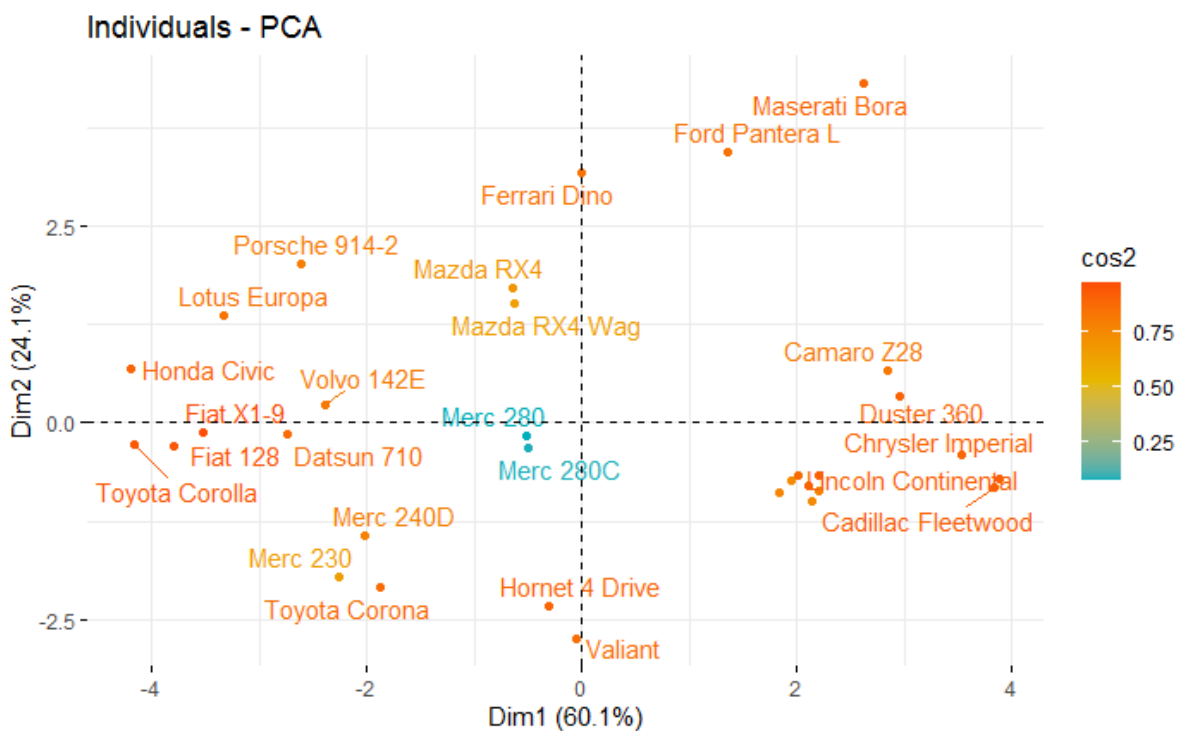
```
```{R}
#b. Tampilkan matriks PC-nya
```

```
Correlation_Matrix <- cor(PCA_Standardized)
Correlation_Matrix
```
```

|      | mpg        | cyl        | disp       | hp         | drat        | wt         | qsec        | gear       |
|------|------------|------------|------------|------------|-------------|------------|-------------|------------|
| mpg  | 1.0000000  | -0.8521620 | -0.8475514 | -0.7761684 | 0.68117191  | -0.8676594 | 0.41868403  | 0.4802848  |
| cyl  | -0.8521620 | 1.0000000  | 0.9020329  | 0.8324475  | -0.69993811 | 0.7824958  | -0.59124207 | -0.4926866 |
| disp | -0.8475514 | 0.9020329  | 1.0000000  | 0.7909486  | -0.71021393 | 0.8879799  | -0.43369788 | -0.5555692 |
| hp   | -0.7761684 | 0.8324475  | 0.7909486  | 1.0000000  | -0.44875912 | 0.6587479  | -0.70822339 | -0.1257043 |
| drat | 0.6811719  | -0.6999381 | -0.7102139 | -0.4487591 | 1.00000000  | -0.7124406 | 0.09120476  | 0.6996101  |
| wt   | -0.8676594 | 0.7824958  | 0.8879799  | 0.6587479  | -0.71244065 | 1.0000000  | -0.17471588 | -0.5832870 |
| qsec | 0.4186840  | -0.5912421 | -0.4336979 | -0.7082234 | 0.09120476  | -0.1747159 | 1.00000000  | -0.2126822 |
| gear | 0.4802848  | -0.4926866 | -0.5555692 | -0.1257043 | 0.69961013  | -0.5832870 | -0.21268223 | 1.0000000  |
| carb | -0.5509251 | 0.5269883  | 0.3949769  | 0.7498125  | -0.09078980 | 0.4276059  | -0.65624923 | 0.2740728  |
| carb |            |            |            |            |             |            |             |            |
| mpg  | -0.5509251 |            |            |            |             |            |             |            |
| cyl  | 0.5269883  |            |            |            |             |            |             |            |
| disp | 0.3949769  |            |            |            |             |            |             |            |
| hp   | 0.7498125  |            |            |            |             |            |             |            |
| drat | -0.0907898 |            |            |            |             |            |             |            |
| wt   | 0.4276059  |            |            |            |             |            |             |            |
| qsec | -0.6562492 |            |            |            |             |            |             |            |
| gear | 0.2740728  |            |            |            |             |            |             |            |
| carb | 1.0000000  |            |            |            |             |            |             |            |

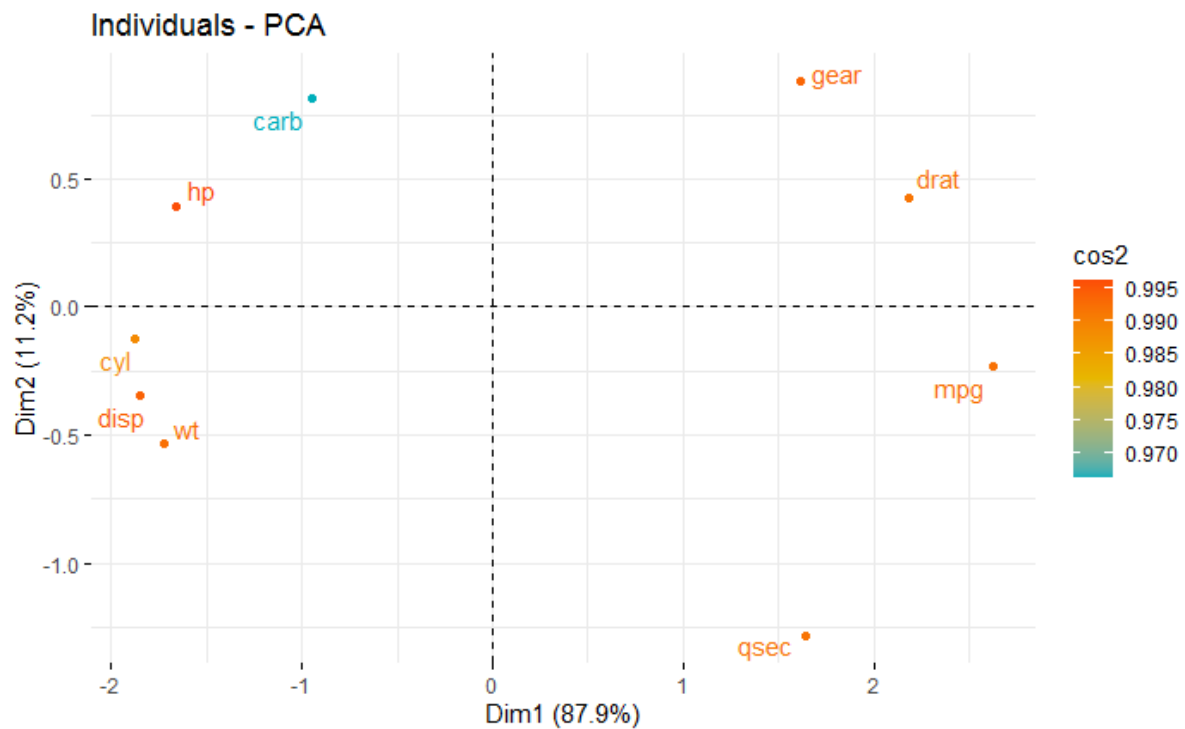
c. Plot di 2-dimensi untuk individunya

```
```{R}
#c. Plot di 2-dimensi untuk individunya
library(factoextra)
Visual_PCA_Cor <- prcomp(Correlation_Matrix, scale = TRUE)
fviz_pca_ind(visual.pca.cor, col.ind = "cos2", gradient.cols =
c("#00AFBB", "#E7B800", "#FC4E07"), repel = TRUE)
```
```

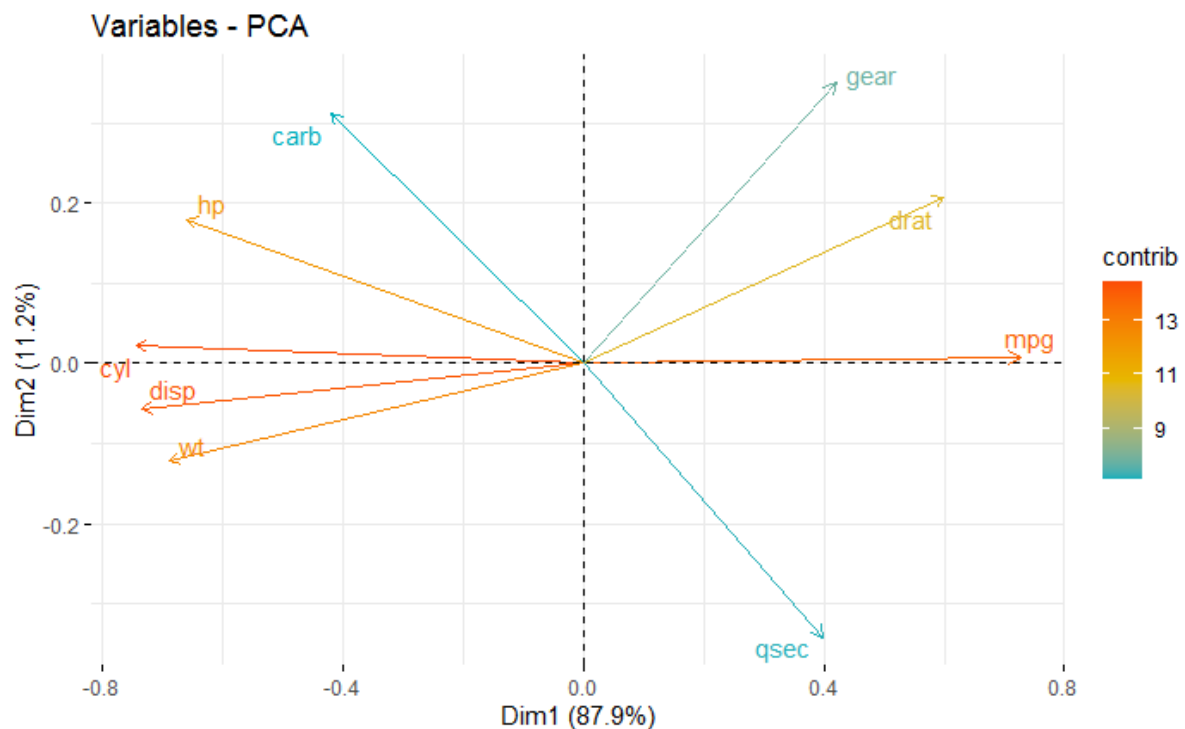


```
```{R}
library(factoextra)
Visual_PCA_Cor <- princomp(Correlation_Matrix, scale = TRUE)
```

```
fviz_pca_ind(Visual_PCA_Cor, col.ind = "cos2", gradient.cols =
c("#00AFBB", "#E7B800", "#FC4E07"), repel = TRUE)
````
```



```
````{R}
fviz_pca_var(Visual_PCA_Cor, col.var = "contrib",
gradient.cols = c("#00AFBB", "#E7B800", "#FC4E07"), repel =
TRUE)
````
```

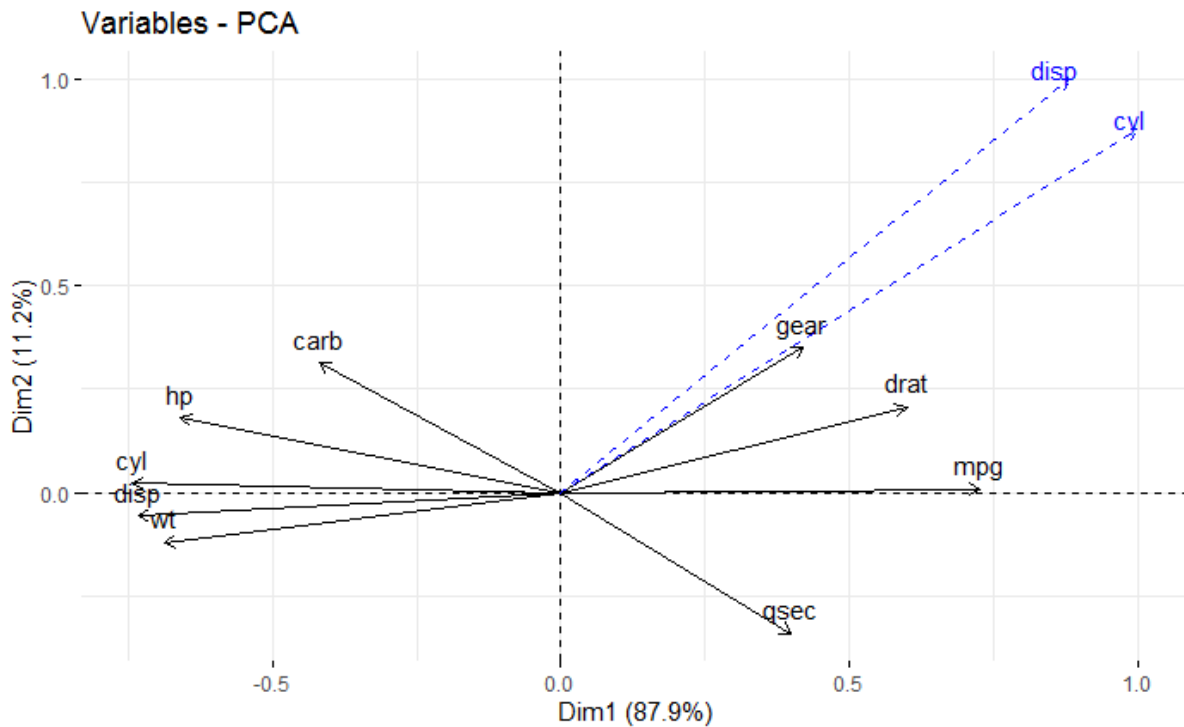


d. Plot di 2-dimensi untuk variabelnya

```

```{R}
#d. Plot di 2-dimensi untuk variabelnya
PCA_Cor <- PCA_Data[1:23, 2:3, drop = FALSE]
PCA_Cor_New <- cor(PCA_Cor)
Correlation <- fviz_pca_var(Visual_PCA_Cor)
fviz_add(Correlation, PCA_Cor_New, color = "blue", geom =
"arrow")
```

```

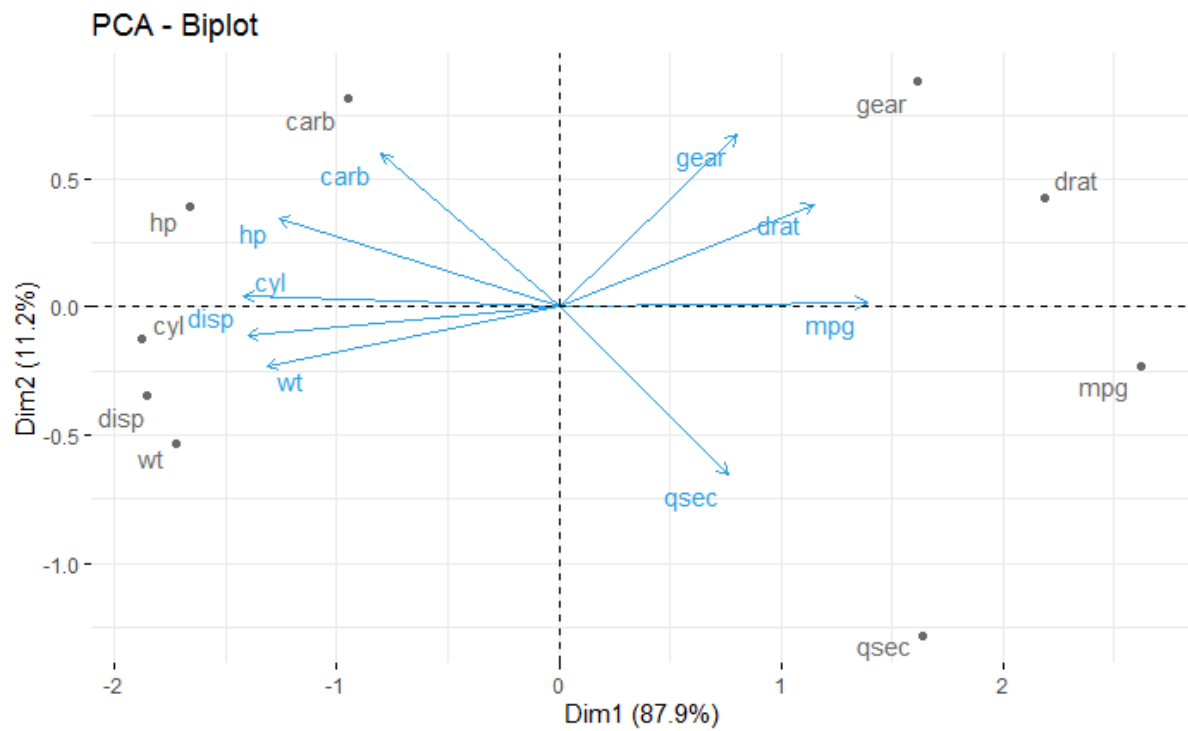


e. Bi-Plot di 2-dimensi untuk individu dan variabelnya

```

```{R}
#e. Bi-Plot di 2-dimensi untuk individu dan variabelnya
fviz_pca_biplot(Visual_PCA_Cor, repel = TRUE, col.var =
"#2E9FDF", col.ind = "#696969")
```

```



f. Plot PC di 3-dimensi

```

```{R}
#f. Plot PC di 3-dimensi
library(rgl)
plot3d(Visual_PCA_Cor$x, col = PCA_Data$gear)
```

```

