

$$\oint_{\text{surface}} \vec{E} \cdot d\vec{A} = Q/\epsilon_0$$

$$\oint_{\text{surface}} \vec{B} \cdot d\vec{A} = 0$$

$$\oint_{\text{loop}} \vec{E} \cdot d\vec{s} = -\frac{d\Phi_B}{dt}$$

$$\oint_{\text{loop}} \vec{B} \cdot d\vec{s} = \mu_0 I_{\text{in}} + \epsilon_0 \mu_0 \frac{d\Phi_E}{dt}$$

$$c = \frac{1}{\sqrt{\epsilon_0 \mu_0}} \quad E = cB \quad \vec{E} \cdot \vec{B} = 0 \quad v = \frac{c}{n}$$

$$\frac{\partial^2 E_x}{\partial x^2} - \frac{1}{c^2} \frac{\partial^2 E_x}{\partial t^2} = 0 \quad \frac{\partial^2 B_z}{\partial x^2} - \frac{1}{c^2} \frac{\partial^2 B_z}{\partial t^2} = 0$$

$$u = \frac{1}{2} \epsilon_0 E^2 + \frac{1}{2\mu_0} B^2 \quad p = \begin{cases} U/c & (\text{absorb}) \\ 2U/c & (\text{reflect}) \end{cases}$$

$$\vec{S} = \frac{1}{\mu_0} \vec{E} \times \vec{B} \quad S = \frac{1}{\mu_0} EB = cu$$

$$I = \langle S \rangle = c\epsilon_0 \langle E^2 \rangle = \frac{1}{2} c\epsilon_0 E^2$$

$$c = f\lambda \quad I = I_1 + I_2 + 2\sqrt{I_1 I_2} \cos \phi \quad I = 4I_0 \cos^2(\phi/2) = 4I_0 \left(\frac{\cos^2 \phi}{4} \right) = I_0 \left(\frac{\sin(N\beta)}{\sin \beta} \right)^2$$

$$\theta_{\text{incident}} = \theta_{\text{reflected}} \quad n_1 \sin \theta_1 = n_2 \sin \theta_2 \quad I = I_0 \left(\frac{\sin(N\beta)}{\sin \beta} \right)^2 \quad \beta = \frac{\pi d \sin \theta}{\lambda}$$

$$t' = t \quad x' = x - ut \quad y' = y \quad z' = z$$

$$t' = \gamma \left(t - \frac{ux}{c^2} \right) \quad x' = \gamma(x - ut) \quad y' = y \quad z' = z$$

$$x'^2 + y'^2 + z'^2 - c^2 t'^2 = x^2 + y^2 + z^2 - c^2 t^2$$

$$f_1 = f_0 \sqrt{\frac{1+u/c}{1-u/c}} \quad (\text{approaching}) \quad v_x = \frac{v'_x + u}{1 + v'_x u/c^2} \quad v_y = \frac{v'_y}{\gamma(1 + v'_x u/c^2)}$$

$$f_1 = f_0 \sqrt{\frac{1-u/c}{1+u/c}} \quad (\text{receding}) \quad p = \gamma m v = \frac{mv}{\sqrt{1-v^2/c^2}} \quad \vec{v} = \frac{c^2 \vec{p}}{E}$$

$$f_1 = f_0 \sqrt{1-u^2/c^2} \quad (\text{transverse}) \quad D = \frac{u}{H} \quad \text{Hubble constant} \quad 50-100 \text{ km/s/Mpc} \quad 1 \text{ pc} = 3.26 \text{ ly}$$

$$\frac{f'}{f} = 1 + \frac{\phi}{c^2} \quad \frac{f'}{f} = \left(1 - \frac{2GM}{Rc^2} \right)^{\frac{1}{2}} \quad R = \frac{2GM}{c^2}$$

$$n(f) = \frac{8\pi}{c^2} f^2 \quad n(\lambda) = \frac{8\pi}{\lambda^4} \quad R = \frac{c}{4} U \quad R = \epsilon_0 T^4 \quad U = \epsilon_0 T^4$$

$$u(f, T) = \frac{8\pi f^2}{c^3} k_B T \quad u(\lambda, T) = \frac{8\pi}{\lambda^4} k_B T$$

$$u(f, T) = \frac{8\pi h}{c^3} \frac{f^3}{e^{\frac{hf}{k_B T}} - 1} \quad u(\lambda, T) = \frac{8\pi hc}{\lambda^5} \frac{1}{e^{\frac{hc}{\lambda k_B T}} - 1}$$

$$U(T) = \int_0^\infty u(\lambda, T) d\lambda = \int_0^\infty u(f, T) df \quad \lambda_{\text{max}} T = 0.2898 \text{ cm} \cdot \text{K}$$

$$L = n\hbar \quad r_n = \frac{n^2}{Z} a_0 \quad a_0 = \frac{\hbar^2}{km_e e^2} = 0.53 \times 10^{-10} \text{ m} \quad E_n = -\frac{Z^2}{n^2} E_0 \quad E_0 = \frac{m_e c^4 k^2}{2\hbar^2} = 13.6 \text{ eV}$$

$$\frac{1}{\lambda} = Z^2 R_\infty \left(\frac{1}{n_1^2} - \frac{1}{n_2^2} \right) \quad R_\infty = \frac{m_e c^4 k^2}{4\pi c \hbar^3} = 1.0974 \times 10^7 \text{ 1/m} \quad hc R_\infty = 13.6 \text{ eV}$$

$$\vec{\mu} = \frac{Q}{2M} \vec{L} \quad |\vec{L}| = \sqrt{\ell(\ell+1)} \hbar \quad L_z = m_\ell \hbar \quad M = \frac{M_1 M_2}{M_1 + M_2} \quad E = \frac{3}{2} k_B T \quad \mu_B = \frac{e\hbar}{2m_e} = 9.27 \times 10^{-24} \text{ J/T}$$

$$U = -\vec{\mu} \cdot \vec{B} \quad F_z = -\frac{dU}{dz} \quad E = -\frac{e^2}{8\pi\epsilon_0 r} \quad \text{spectroscopic notation: } n^{2s+1} L_J$$

$$E = \frac{\hbar^2}{2mL^2} \quad E = \frac{n^2 \hbar^2}{8mb^2} \quad \vec{\mu} = \frac{Q}{2M} \vec{L} \quad \omega_L = \frac{Q}{2M} B \quad E_F = \frac{\hbar^2}{2m} (3\pi^2 n)^{2/3}$$

$$E_n = (n + 1/2) \hbar \omega \quad \vec{\tau} = \vec{\mu} \times \vec{B} \quad \Delta E = \frac{e\hbar}{2m} B \quad E = \frac{3}{5} E_F$$

$$E_{\text{vib}} = n E_0 \sqrt{Z_1 Z_2} \sqrt{\frac{m_e}{M}} \quad E = \frac{\hbar^2}{2I} \quad I = M r_0^2 \quad E = \frac{\hbar^2 \ell(\ell+1)}{2I} \quad E_F = \frac{\pi^2}{3} \hbar c n^{1/3} \text{ for } m=0$$

$$E_{\text{rot}} = \frac{\ell(\ell+1)}{4} E_0 \frac{m_e}{M} \quad p_F = \frac{2}{5} \hbar^2 (3\pi^2)^{1/3} n^{5/3} \quad \text{where } p = -\frac{dE}{dV}$$

$$E = \frac{\hbar^2}{2mL^2} \quad E = \frac{n^2 \hbar^2}{8mb^2} \quad \vec{\mu} = \frac{Q}{2M} \vec{L} \quad \omega_L = \frac{Q}{2M} B \quad E_F = \frac{\hbar^2}{2m} (3\pi^2 n)^{2/3}$$

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$$c = 3.00 \times 10^8 \text{ m/s} \quad h = 6.626 \times 10^{-34} \text{ J} \cdot \text{s} \quad \hbar = \frac{h}{2\pi} \quad \alpha \doteq \frac{1}{137} \quad m_e = 9.11 \times 10^{-31} \text{ kg} \quad m_e c^2 = 0.511 \text{ MeV}$$

$$e = -1.6 \times 10^{-19} \text{ C} \quad \hbar c = 197.33 \text{ MeV} \cdot \text{fm} \quad \pi = 3.1416 \quad m_p = 1.673 \times 10^{-27} \text{ kg} \quad m_p c^2 = 938.3 \text{ MeV}$$

$$k_B = 1.38 \times 10^{-23} \text{ J/K} \quad \hbar c = 12400 \text{ eV} \cdot \text{\AA} \quad e^{-1} = 0.37 \quad \lambda_C = \frac{h}{mc} = 2.4 \times 10^{-12} \text{ m} \quad \frac{m_e}{m_p} \doteq \frac{1}{1836}$$

$$k = \frac{1}{4\pi\epsilon_0} = 9.0 \times 10^9 \frac{\text{N} \cdot \text{m}^2}{\text{C}^2} = 1240 \text{ eV} \cdot \text{nm} = 1240 \text{ MeV} \cdot \text{fm} \quad 2\pi \text{ rad} = 360^\circ \quad 1 \text{ eV} = 1.6 \times 10^{-19} \text{ J} \quad G = 6.67 \times 10^{-11} \frac{\text{N} \cdot \text{m}^2}{\text{kg}^2}$$

$$\epsilon_0 = 8.85 \times 10^{-12} \frac{\text{C}^2}{\text{N} \cdot \text{m}^2} \quad k_B T (20^\circ \text{C}) \doteq \frac{1}{40} \text{ eV} \quad 1 \text{ nm} = 10^{-9} \text{ m} \quad 1 \text{ \AA} = 10^{-10} \text{ m} \quad 1 \text{ fm} = 10^{-15} \text{ m}$$

$$N_0 = 6.02 \times 10^{23} \frac{\text{particles}}{\text{mole}} \quad \text{visible light: } \lambda = 430 \text{ nm} \rightarrow 690 \text{ nm} \quad \text{human eye most sensitive to: } \lambda \doteq 555 \text{ nm}$$

$$\Delta L = n\lambda \quad \sin \theta = \frac{n\lambda}{d} \quad 4nt = (2m-1)\lambda \quad 4nt = 2m\lambda \quad m = 0, \pm 1, \pm 2, \pm 3, \dots$$

$$\Delta L = \left(n + \frac{1}{2} \right) \lambda \quad \sin \theta = \left(n + \frac{1}{2} \right) \frac{\lambda}{d} \quad R = \frac{\lambda}{\Delta \lambda} = mN \quad \frac{\Delta \theta}{\Delta \lambda} = \frac{m}{d \cos \theta}$$

$$n = 0, \pm 1, \pm 2, \pm 3, \dots \quad a \sin \theta = m\lambda \quad m = \pm 1, \pm 2, \pm 3, \dots \quad \theta_{\text{min}} = 1.22 \frac{\lambda}{D} \quad s_{\text{min}} = f \theta_{\text{min}} = f \frac{\lambda}{D}$$

$$I = I_{\text{max}} \left[\frac{\sin(N\beta)}{\sin \beta} \right]^2 \left(\frac{\sin \alpha}{\alpha} \right)^2 \quad \alpha = \frac{\pi a \sin \theta}{\lambda} \quad u = \tanh \eta \quad \cosh \eta = \frac{1}{2} (e^\eta + e^{-\eta})$$

$$\Delta t = \frac{1}{c} \left[2(L_1 - L_2) + \frac{v^2}{c^2} (2L_1 - L_2) \right] = \frac{2L_1 v^2}{c^2} \quad (\text{for } L = L_1 = L_2) \quad \Delta p \Delta x \geq \hbar/2 \quad \Delta E \Delta t \geq \hbar/2 \quad \Delta L \Delta \theta \geq \hbar/2$$

$$\Delta x = x - \bar{x} \quad \bar{x} = 0 \Rightarrow (\Delta x)^2 = \bar{x}^2 \quad \bar{p} = 0 \Rightarrow (\Delta p)^2 = \bar{p}^2 \quad f \simeq \exp \left[-\frac{2}{\hbar} a \sqrt{2m} (\langle U \rangle - E) \right] \rightarrow \text{Tunneling}$$

$$\epsilon = \text{fraction absorbed} = 1 - \text{fraction reflected} \quad \sigma = 5.67 \times 10^{-8} \frac{\text{J}}{\text{s} \cdot \text{m}^2 \cdot \text{K}^4} \quad N = N_0 e^{-t/\tau} \quad \tau = 1/\lambda \quad t_{1/2} = \tau \ln 2$$

$$hf = (K.E.)_e + W \quad \text{Bragg: } 2d \sin \theta = n\lambda \quad \lambda' - \lambda = \frac{h}{mc} (1 - \cos \theta) \quad \text{Compton}$$

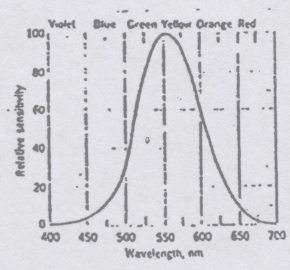
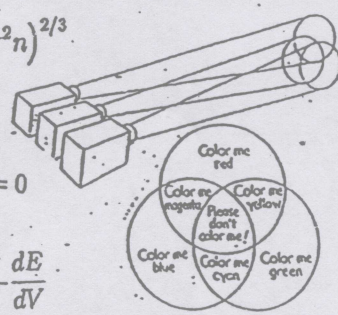
$$hf = E_i - E_f \quad \frac{N_n}{N_0} = \frac{g_n}{g_0} \exp \left(-\frac{E_n - E_0}{k_B T} \right) \quad \mu_B = \frac{e\hbar}{2m_e} = 9.27 \times 10^{-24} \text{ J/T} = 5.79 \times 10^{-9} \text{ eV/Gauss}$$

$$E = \frac{\hbar^2}{2mL^2} \quad E = \frac{n^2 \hbar^2}{8mb^2} \quad \vec{\mu} = \frac{Q}{2M} \vec{L} \quad \omega_L = \frac{Q}{2M} B \quad E_F = \frac{\hbar^2}{2m} (3\pi^2 n)^{2/3}$$

$$E_n = (n + 1/2) \hbar \omega \quad \vec{\tau} = \vec{\mu} \times \vec{B} \quad \Delta E = \frac{e\hbar}{2m} B \quad E = \frac{3}{5} E_F$$

$$E_{\text{vib}} = n E_0 \sqrt{Z_1 Z_2} \sqrt{\frac{m_e}{M}} \quad E = \frac{\hbar^2}{2I} \quad I = M r_0^2 \quad E = \frac{\hbar^2 \ell(\ell+1)}{2I} \quad E_F = \frac{\pi^2}{3} \hbar c n^{1/3} \text{ for } m=0$$

$$E_{\text{rot}} = \frac{\ell(\ell+1)}{4} E_0 \frac{m_e}{M} \quad p_F = \frac{2}{5} \hbar^2 (3\pi^2)^{1/3} n^{5/3} \quad \text{where } p = -\frac{dE}{dV}$$



$$\begin{aligned}
 k &= 9 \times 10^9 \frac{N \cdot m^2}{C^2} = \frac{1}{4\pi\epsilon_0} & 1 \text{ Gauss} &= 10^{-4} T & m_e &= 9.109 \times 10^{-31} \text{ kg} & \pi &\doteq 3.1416 \\
 \epsilon_0 &= 8.85 \times 10^{-12} \frac{C^2}{N \cdot m^2} & e &= -1.6 \times 10^{-19} C & m_p &= 1.673 \times 10^{-27} \text{ kg} & 2\pi \text{ rad} &= 360^\circ \\
 \mu_0 &= 4\pi \times 10^{-7} \frac{Wb}{A \cdot m} & k_B &= 1.38 \times 10^{-23} J/K & m_n &= 1.675 \times 10^{-27} \text{ kg} & e^{-1} &\doteq 0.37 \\
 c &= 3.00 \times 10^8 \text{ m/s} & k_B T(20^\circ) &\simeq \frac{1}{40} eV & 1 eV &= 1.6 \times 10^{-19} J & 1 \text{ nm} &= 10^{-9} \text{ m} \\
 N_0 &= 6.022 \times 10^{23} \frac{\text{particles}}{\text{mole}} & 1 \text{ Wb} &= 1 T \cdot m^2 & 1 kW \cdot hr &= 3.6 \times 10^6 J & 1 \text{ \AA} &= 10^{-10} \text{ m} \\
 & & R &= N_0 k_B & E &= mc^2
 \end{aligned}$$

with no dielectric or magnetic materials

$$\text{Max. 1} \quad \oint_{\text{surface}} \vec{E} \cdot d\vec{A} = q_{\text{in}}/\epsilon_0$$

$$\text{Max. 2} \quad \oint_{\text{surface}} \vec{B} \cdot d\vec{A} = 0$$

$$\text{Max. 3} \quad \oint_{\text{loop}} \vec{E} \cdot d\vec{s} = -\frac{d\Phi_B}{dt}$$

$$\text{Max. 4} \quad \oint_{\text{loop}} \vec{B} \cdot d\vec{s} = \mu_0 I_{\text{in}} + \epsilon_0 \mu_0 \frac{d\Phi_E}{dt}$$

$$c = \frac{1}{\sqrt{\epsilon_0 \mu_0}} \quad I_d = \epsilon_0 \frac{d\Phi_E}{dt} \quad \Phi_E = \int_{\text{surface}} \vec{E} \cdot d\vec{A}$$

$$\vec{F} = m\vec{a} \quad F = \frac{mv^2}{r} \quad \vec{F} = q\vec{E} \quad F = -\frac{dU}{dx} \quad P = \vec{F} \cdot \vec{v}$$

$$\vec{F}_{12} = \frac{kq_1q_2}{r_{12}^2} \hat{r}_{12} \quad \vec{E} = \frac{kq}{r^2} \hat{r} \quad V = \frac{kq}{r} \quad \Delta V = V_b - V_a = -\int_{r_b}^{r_a} \vec{E} \cdot d\vec{s}$$

$$T = \frac{2\pi}{\omega} = \frac{1}{f} \quad E = \frac{\sigma}{2\epsilon_0} \quad V = Ed \quad \vec{E} = -\vec{\nabla}V \quad U = -\vec{p} \cdot \vec{E}$$

$$\vec{\tau} = \vec{r} \times \vec{E} \quad E = \frac{\sigma}{\epsilon_0} \quad C = \frac{Q}{V} \quad C = \frac{\epsilon_0 A}{d} \quad C = \kappa C_0 \quad \epsilon = \kappa \epsilon_0$$

$$U = \frac{Q^2}{2C} = \frac{1}{2} CV^2 = \frac{1}{2} QV \quad \sigma_{\text{ind}} = \sigma(1 - 1/\kappa)$$

$$u_E = \frac{U}{V} = \frac{1}{2} \epsilon_0 E^2 \quad C_{\text{eq}} = C_1 + C_2 + \dots + C_n$$

$$\oint_{\text{surface}} \kappa \vec{E} \cdot d\vec{A} = q_{\text{in}}/\epsilon_0 \quad \frac{1}{C_{\text{eq}}} = \frac{1}{C_1} + \frac{1}{C_2} + \dots + \frac{1}{C_n}$$

$$I = \frac{dQ}{dt} \quad I = \int_{\text{surface}} \vec{J} \cdot d\vec{A} \quad \vec{J} = n_q q \vec{v} \quad \sigma = \frac{1}{\rho} \quad \sum_{\text{node}} I_i = 0 \quad \sum_{\text{loop}} \Delta V_i = 0 \quad \omega = \frac{1}{\sqrt{LC}} \quad I = \frac{\mathcal{E}}{R} (1 - e^{-Rt/L})$$

$$\vec{E} = \rho \vec{J} \quad \vec{J} = \sigma \vec{E} \quad V = IR \quad R = \rho \frac{L}{A}$$

$$P = IV \quad P = I^2 R = V^2/R$$

$$\frac{1}{R_{\text{eq}}} = \frac{1}{R_1} + \frac{1}{R_2} + \dots + \frac{1}{R_n}$$

$$R_{\text{eq}} = R_1 + R_2 + \dots + R_n$$

$$V = \frac{k}{r} \int \rho dV' + \frac{k}{r^2} \int r' \cos \theta \rho dV' + \frac{k}{r^3} \int r'^2 \frac{3 \cos \theta - 1}{2} \rho dV' + \dots$$

$$\vec{p} = \int \vec{r} \rho dV' = \sum_i \vec{r}_i q_i \quad (\text{discrete})$$

$$V = k \frac{\vec{r} \cdot \vec{p}}{r^2}$$

$$\vec{v} = \frac{\vec{E}}{B}$$

$$f = \frac{qB}{2\pi m}$$

$$I = \frac{Bvl}{R}$$

$$\mathcal{E} = Bvl$$

$$B = \frac{\mu_0 NI}{2\pi r}$$

$$B = \mu_0 nI$$

$$B = \frac{\mu_0 IR^2}{2(R^2 + z^2)^{3/2}}$$

$$B = \frac{\mu_0 I}{2R}$$

$$\mu = NIA$$

$$\vec{\tau} = \vec{\mu} \times \vec{B}$$

$$U = -\vec{\mu} \cdot \vec{B}$$

$$\Phi_B = LI$$

$$\mathcal{E} = -\frac{d\Phi_B}{dt} = -L \frac{dI}{dt}$$

$$\mathcal{E}_{12} = -M_{12} \frac{dI_1}{dt}$$

$$M_{21} = M_{12}$$

$$\vec{B} = \vec{B}_0 + \mu_0 \vec{M}$$

$$\vec{B}_0 = \mu_0 \vec{H}$$

$$\vec{H} = \frac{\vec{B}_0}{\mu_0} - \vec{M}$$

$$\vec{B} = \mu_0 \vec{H} + \mu_0 \vec{M}$$

$$\vec{M} = \chi_m \vec{H}$$

$$\vec{B} = \mu \vec{H}$$

$$\vec{M} = C \frac{\vec{B}}{T}$$

$$\mu = \mu_0 (1 + \chi_m)$$

$$U_L = \frac{1}{2} LI^2$$

$$L = \mu_0 A \ln n^2$$

$$L = \frac{\mu_0 \ell}{2\pi} \ln \frac{R_2}{R_1}$$

$$u_B = \frac{U_B}{V} = \frac{1}{2} \mu_0 B^2$$

$$\frac{\mathcal{E}_1}{\mathcal{E}_2} = \frac{N_1}{N_2} = \frac{V_{01}}{V_{02}}$$

$$\mathcal{E} = V_0 \sin(\omega t)$$

$$\vec{\mu}_{\text{orbital}} = -\frac{e}{2m} \vec{L}$$

$$B = \frac{\mu_0 \mu}{2\pi d^3}$$

$$\vec{\tau} = \vec{R} \times \vec{F}$$

$$\vec{L} = \vec{r} \times \vec{p}$$

$$\vec{B} = \frac{\mu_0}{4\pi r^3} [3(\vec{\mu} \cdot \vec{r})\vec{r} - \vec{\mu}]$$

$$PV = nRT = Nk_B T$$

$$\rho = \rho_0 [1 + \alpha(T - T_0)]$$

$$K.E._{\text{ave}} = \frac{3}{2} k_B T$$

$$P_{\text{ave}} = \frac{1}{2} \frac{V_{\text{max}}^2}{R}$$

$$F = \mu \frac{\partial B}{\partial z}$$

$$(1+x)^{-1} = 1 - x + x^2 - x^3 + x^4 - \dots$$

$$(1+x)^{+1/2} = 1 + \frac{1}{2}x - \frac{1}{8}x^2 + \frac{1}{16}x^3 - \dots$$

$$e^x = 1 + x + \frac{1}{2}x^2 + \frac{1}{6}x^3 + \dots$$

$$(1+x)^{-2} = 1 - 2x + 3x^2 - 4x^3 + 5x^4 - \dots$$

$$(1+x)^{-1/2} = 1 - \frac{1}{2}x + \frac{3}{8}x^2 - \frac{5}{16}x^3 + \dots$$

$$\ln(1+x) = x - \frac{1}{2}x^2 + \frac{1}{3}x^3 - \frac{1}{4}x^4 + \dots$$

$$(1+x)^{-3} = 1 - 3x + 6x^2 - 10x^3 + 15x^4 - \dots$$

$$(1+x)^{-1/3} = 1 - \frac{1}{3}x + \frac{2}{9}x^2 - \frac{14}{81}x^3 + \dots$$

$$\sin x = x - \frac{1}{6}x^3 + \frac{1}{120}x^5 - \frac{1}{5040}x^7 + \dots$$

$$\cos x = 1 - \frac{1}{2}x^2 + \frac{1}{24}x^4 - \frac{1}{720}x^6 + \dots$$