

1 Contest Setup

1.1 Java template

```
import java.io.*;
import java.util.*;
public class Main
   public static void main(String[] args)
        MyScanner sc = new MyScanner();
        out = new PrintWriter(new BufferedOutputStream(System.out));
        // Start writing your solution here.
        // Stop writing your solution here.
        out.close();
    public static PrintWriter out;
    public static class MyScanner
        BufferedReader br:
       StringTokenizer st;
        public MyScanner()
            br = new BufferedReader(new InputStreamReader(System.in));
        boolean hasNext()
            while (st == null || !st.hasMoreElements()) {
                    st = new StringTokenizer(br.readLine());
                } catch (Exception e) {
                    return false;
```

```
return true:
String next()
    if (hasNext())
        return st.nextToken();
    return null;
int nextInt()
    return Integer.parseInt(next());
long nextLong()
    return Long.parseLong(next());
double nextDouble()
    return Double.parseDouble(next());
String nextLine()
    String str = "";
   try {
        str = br.readLine();
    } catch (IOException e) {
        e.printStackTrace();
    return str;
```

1.1.1 Java Issues

- 1. Random Shuffle before sorting:
 Random rnd = new Random(); rnd.nextInt();
- 2. Use StringBuilder for large output
- 3. Java has strict parsing rules. e.g. using sc.nextInt() to read a long will result in RE
- 4. For class sorting, use code implements Comparable<Class name>. Or, use code new Comparator<Interval>() {} atCollections.sort() second argument

2 System Testing

- 1. Setup vimrc and bashrc
- 2. Test g++ and Java 8 compiler
- 3. Look for compilation parameter and code it into bashrc
- 4. Test if c++ and Java templates work properly on local and judge machine (bits, auto, and other c++11 stuff)
- 5. Test "divide by 0" \rightarrow RE/TLE?

- Make a complete graph and run Floyd warshall, to test time complexity upper bound
- 7. Make a linear graph and use DFS to test stack size
- 8. Test output with extra newline and spaces
- 9. Go to Eclipse o preference o Java o Editor o ContentAssist, add .abcdefghijklmnopqrstuvwxyz to auto activation triggers for Java in Eclipse

3 Reminder

- 1. 隊友的建議,要認真聽!要記得心平氣和的小聲討論喔! 通常隊 友的建議都會突破你盲點。
- 2. 每一題都要小心讀, 尤其是 IO 的格式和限制都要看清楚。
- 3. 小心估計時間複雜度和空間複雜度
- 4. Coding 要兩人一組,要相信你的隊友的實力!
- 5. 1WA 罰 20 分鐘! 放輕鬆, 不要急, 多產幾組測資後再丟。
- 6. 範測一定要過! 產個幾組極端測資, 例如 input 下限、特殊 cases 0, 1, -1、空集合等等
- 7. 比賽是連續測資, 一定要全部讀完再開始 solve 喔!
- 8. Bus error: 有scanf, fgets 但是卻沒東西可以讀取了! 可能有 searly termination 但是時機不對。
- 9. 圖論一定要記得檢查連通性。最簡單的做法就是 loop 過所有的 8 點 9
- 10. long long = int * int 會完蛋
- 11. long long int 的位元運算要記得用 1LL << 35
- 12. 記得清理 Global variable
- 13. 建圖時要注意有無重邊!

4 Topic list

- 1. 列舉、窮舉 enumeration
- 2. 貪心 greedy
- 3. 排序 sorting, topological sort
- 4. 二分搜 binary search (數學算式移項合併後查詢)
- 5. 爬行法 (右跑左追) Two Pointer
- 6. 離散化
- 7. Dynamic programming, 矩陣快速幂
- 8. 鴿籠原理 Pigeonhole
- 9. 最近共同祖先 LCA (倍增法, LCA 轉 RMQ)
- 10. 折半完全列舉 (能用 vector 就用 vector)
- 11. 離線查詢 Offline (DFS, LCA)

- 12. 圖的連通性 Directed graph connectivity -> DFS. Undirected graph -> Union Find
- 13. 因式分解
- 14. 從答案推回來
- 15. 寫出數學式,有時就馬上出現答案了!
- 16. 奇偶性質

5 Useful code

5.1 Leap year O(1)

```
(year % 400 == 0 \mid \mid (year % 4 == 0 \&\& year % 100 != 0))
```

5.2 Fast Exponentiation O(log(exp))

```
ll fast_pow(ll a, ll b, ll M) {
    ll ans = 1;
    ll base = a % M;
    while (b) {
        if (b & 1)
            ans = ans * base % M;
        b >>= 1;
    }
    return ans;
}
```

5.3 Mod Inverse O(log n)

```
Case 1: gcd(a, m) = 1: ax + my = gcd(a, m) = 1 (use ext_gcd)
```

Case 2: m is prime: $a^{m-2} \equiv a^{-1} mod m$

5.4 GCD O(log(min(a+b)))

注意負數的 case! C++ 是看被除數決定正負號的。

```
ll gcd(ll a, ll b)
{
    return b == 0 ? a : gcd(b, a % b);
}
```

5.5 Extended Euclidean Algorithm GCD O(log(min(a + b)))

Bezout identity ax + by = gcd(a, b), where $|x| \le \frac{b}{d}$ and $|y| \le \frac{a}{d}$.

```
1 | ll extgcd(ll a, ll b, ll& x, ll&y) {
2     if (b == 0) {
3         x = 1;
```

```
y = 0;
return a;
}
else {
    ll d = extgcd(b, a % b, y, x);
    y -= (a / b) * x;
    return d;
}
```

5.6 Prime Generator O(nloglogn)

5.7 C++ Reference

```
algorithm
        ::find: [it s, it t, val] -> it
        ::count: [it s, it t, val] -> int
        ::unique: [it s, it t] -> it (it = new end)
        ::merge: [it s1, it t1, it s2, it t2, it o] -> void (o allocated)
   string::
        ::replace(idx, len, string) -> void
        ::find (str, pos = \emptyset) -> idx
        ::substr (pos = 0, len = npos) -> string
    string <-> int
        ::stringstream; // remember to clear
12
        ::sscanf(s.c_str(), "%d", &i);
        ::sprintf(result, "%d", i); string s = result;
14
15
   math/cstdlib
        ::atan2(y=0, x=-1) -> pi
17
18
   io printf/scanf
                               "%d"
                                               "%d"
        ::int:
20
        ::double:
                               "%lf", "f"
                                               "%lf"
21
                               "%s"
        ::string:
                                               "%s"
22
                               "%11d"
                                               "%11d"
        ::long long:
23
                               "%Lf"
                                               "%Lf"
24
        ::long double:
                                               "%u"
        ::unsigned int:
                               "%u"
25
        ::unsigned long long: "%ull"
                                               "%ull"
26
```

```
"0%0"
27
        ::oct:
                                   "0x%x"
         ::hex:
28
                                   "%e"
        ::scientific:
29
        ::width:
                                   "%05d"
30
31
        ::precision:
                                   "%.5f"
        ::adjust left:
                                   "%-5d"
32
33
   io cin/cout
34
35
        ::oct:
                                   cout << oct << showbase:
         ::hex:
                                   cout << hex << showbase;</pre>
36
        ::scientific:
                                   cout << scientific;</pre>
37
        ::width:
                                   cout << setw(5);</pre>
38
        ::precision:
                                   cout << fixed << setprecision(5);</pre>
39
                                   cout << setw(5) << left;</pre>
        ::adjust left:
```

6 Search

6.1 Ternary Search O(nlogn)

```
double l = ..., r = ....; // input
for(int i = 0; i < 100; i++) {
   double m1 = l + (r - l) / 3, m2 = r - (r - l) / 3;
   if (f (m1) < f (m2)) // f - convex function
        l = m1;
   else
        r = m2;
}
f(r) - maximum of function</pre>
```

7 Basic data structure

7.1 1D BIT

```
// BIT is 1-based
const int MAX N = 20000; //這個記得改!
ll\ bit[MAX_N + 1];
ll sum(int i) {
    int s = 0:
    while (i > 0) {
        s += bit[i];
        i -= (i \& -i);
    }
    return s;
void add(int i, ll x) {
    while (i <= MAX_N) {
        bit[i] += x;
        i += (i \& -i);
    }
}
```

7.2 2D BIT

```
// BIT is 1-based const int MAX_N = 20000, MAX_M = 20000; //這個記得改! lb bit[MAX_N + 1][MAX_M + 1];
```

```
ll sum(int a, int b) {
    ll s = 0;
    for (int i = a; i > 0; i -= (i & -i))
        for (int j = b; j > 0; j -= (j & -j))
            s += bit[i][j];
    return s;
}

void add(int a, int b, ll x) {
    // MAX_N, MAX_M 須適時調整!
    for (int i = a; i <= MAX_N; i += (i & -i))
            for (int j = b; j <= MAX_M; j += (j & -j))
                 bit[i][j] += x;
}
```

7.3 Union Find

```
const int MAX N = 20000; // 記得改
struct UFDS {
    int par[MAX_N];
    void init(int n) {
        memset(par, -1, sizeof(int) * n);
    int root(int x) {
        return par[x] < 0 ? x : par[x] = root(par[x]);
    void merge(int x, int y) {
        x = root(x);
        y = root(y);
        if (x != y) {
            if (par[x] > par[y])
               swap(x, y);
            par[x] += par[y];
            par[y] = x;
        }
};
```

7.4 Segment Tree

```
typedef long long ll;
   const int MAX N = 1000000;
   const int MAX_NN = (1 << 20); // bigger than MAX_N</pre>
   struct SegTree {
       int NN:
                              // size of tree
        ll dflt;
                             // default val
        ll seg[2 * MAX_NN]; // 0-based index, 2 * MAX_NN - 1 in fact
8
        ll lazy[2 * MAX_NN]; // 0-based index, 2 * MAX NN - 1 in fact
9
        // lazy[u] != 0 <->
10
        // substree of u (u not inclued) is not up-to-date (it's dirty)
11
12
        void init(int n, ll val)
13
14
15
           dflt = val;
            NN = 1;
            while (NN < n)
17
```

```
NN <<= 1:
    fill(seq, seq + 2 * NN, dflt);
    fill(lazy, lazy + 2 * NN, dflt);
void gather(int u, int l, int r)
    seq[u] = seq[u * 2 + 1] + seq[u * 2 + 2];
}
void push(int u, int l, int r)
    if (lazy[u] != 0) {
        int m = (l + r) / 2;
        seg[u * 2 + 1] += (m - 1) * lazy[u];
        seg[u * 2 + 2] += (r - m) * lazy[u];
        lazv[u * 2 + 1] += lazv[u]:
        lazy[u * 2 + 2] += lazy[u];
        lazv[u] = 0;
}
void build(int u, int l, int r)
    if (r - l == 1)
        return;
    int m = (l + r) / 2;
    build(u * 2 + 1, l, m);
    build(u * 2 + 2, m, r);
    gather(u, l, r);
}
ll query(int a, int b, int u, int l, int r)
    if (l >= b || r <= a)
        return dflt;
    if (l >= a && r <= b)
        return sea[u]:
    int m = (l + r) / 2;
    push(u, l, r);
    ll res1 = query(a, b, u * 2 + 1, l, m);
    ll res2 = query(a, b, u * 2 + 2, m, r);
    gather(u, l, r); // data is dirty since previous push
    return res1 + res2;
void update(int a, int b, int x, int u, int l, int r)
    if (l >= b || r <= a)
        return;
    if (l >= a \&\& r <= b) {
        seg[u] += (r - l) * x; // update u and
                               // set subtree u is not up-to-date
        lazv[u] += x;
        return;
```

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73

```
74
           int m = (l + r) / 2;
75
           push(u, l, r);
76
           update(a, b, x, u * 2 + 1, l, m);
77
78
           update(a, b, x, u * 2 + 2, m, r);
           gather(u, l, r); // remember this
79
80
   };
81
  7.5 Sparse Table
   struct Sptb {
       int sp[MAX_LOG_N][MAX_N]; // MAX_LOG_N = ceil(lg(MAX_N))
       void build(int inp[], int n)
```

B Tree

8.1 LCA

```
const int MAX_N = 10000;
   const int MAX LOG N = 14; // (1 << MAX LOG N) > MAX N
   int N;
   int root;
   int dep[MAX_N];
   int par[MAX_LOG_N][MAX_N];
   vector<int> child[MAX_N];
10
   void dfs(int u, int p, int d) {
11
        dep[u] = d;
12
        for (int i = 0; i < int(child[u].size()); i++) {</pre>
13
            int v = child[u][i];
14
            if (v != p) {
15
                dfs(v, u, d + 1);
16
17
18
19 }
```

```
20
   void build() {
21
       // par[0][u] and dep[u]
22
       dfs(root, -1, 0);
23
24
       // par[i][u]
25
26
       for (int i = 0; i + 1 < MAX_LOG_N; i++) {
            for (int u = 0; u < N; u++) {
27
                if (par[i][u] = -1)
28
                    par[i + 1][v] = -1;
29
30
                else
                    par[i + 1][u] = par[i][par[i][u]];
31
            }
32
       }
33
34
35
   int lca(int u, int v) {
       if (dep[u] > dep[v]) swap(u, v); // 讓 v 較深
37
       int diff = dep[v] - dep[u]; // 將 v 上移到與 U 同層
38
       for (int i = 0; i < MAX_LOG_N; i++) {
39
            if (diff & (1 << i)) {
                v = par[i][v];
42
       }
43
44
       if (u == v) return u;
46
       for (int i = MAX_LOG_N - 1; i >= 0; i--) { // 必需倒序
47
            if (par[i][u] != par[i][v]) {
48
                u = par[i][u];
49
                v = par[i][v];
50
51
       }
52
       return par[0][u];
53
54
```

8.2 Tree Center

```
int diameter = 0, radius[N], deg[N]; // deg = in + out degree
   int findRadius()
   {
3
       queue<int> q; // add all leaves in this group
       for (auto i : group)
           if (dea[i] == 1)
               q.push(i);
       int mx = 0;
       while (q.empty() == false) {
           int u = q.front();
           q.pop();
12
13
           for (int v : q[u]) {
14
                dea[v]--:
15
                if(deg[v] == 1) {
16
                    q.push(v);
17
```

```
radius[v] = radius[u] + 1;
18
                    mx = max(mx, radius[v]);
19
                }
20
            }
21
       }
22
23
        int cnt = 0; // crucial for knowing if there are 2 centers or not
24
        for (auto i : group)
25
            if (radius[j] == mx)
26
                cnt++:
27
28
        // add 1 if there are 2 centers (radius, diameter)
29
        diameter = max(diameter, mx * 2 + (cnt == 2));
30
        return mx + (cnt == 2);
31
32
```

9 Graph

9.1 Articulation point / Bridge

const int MAX N = 1111;

```
vector<int> q[MAX_N];
   // for bridge
   typedef pair<int, int> ii;
   vector<ii> ans;
   // for articulation point
   int root;
                            // set it before dfs() call
   bool isCutVertex[MAX_N]; // init to false
   int tt = 0, dfn[MAX_N], low[MAX_N]; // init array to -1
   void dfs(int u, int p)
       dfn[u] = low[u] = tt++;
       // for articulation point, root needs to have >= 2 childrens
17
       int child = 0;
18
       for (auto v : g[u]) {
19
            if (v == p)
20
                continue;
21
22
            child++;
23
            if (dfn[v] == -1) {
24
                dfs(v, u):
25
                low[u] = min(low[u], low[v]);
26
27
                if (low[v] > dfn[u]) // bridge
28
                    ans.push_back(ii(min(u, v), max(u, v)));
29
30
                if (u != root && low[v] >= dfn[u]) { // articulation point
31
                    isCutVertex[u] = true:
32
               } else if (u == root && child >= 2) { // articulation point
33
                    isCutVertex[u] = true;
34
35
```

9.2 2-SAT

```
p \lor (q \land r)
= ((p \land q) \lor (p \land r))
p \oplus q
= \neg((p \land q) \lor (\neg p \land \neg q))
= (\neg p \lor \neg q) \land (p \lor q)
```

9.3 CC

9.3.1 BCC

以 Edge 做分界的話, stack 要裝入 (u - v), 並 pop 終止條件為!= (u - v) 以 Articulation point 做為分界 (code below), 注意有無坑人的重邊

```
int cnt, root, dfsTime[N], dfsLow[N], timer, group[N]; // max N nodes
stack<int> s;
bool in[N];
void dfs(int u, int p)
{
    s.push(u);
    in[u] = true;
    dfsTime[u] = dfsLow[u] = timer++;
}
```

```
int v = q[u][i];
12
13
             if (v == p)
14
                 continue;
15
                                                                                       12
16
                                                                                       13
             if (dfsTime[v] == 0) {
17
                 dfs(v, u):
18
                                                                                       15
                 dfsLow[u] = min(dfsLow[u], dfsLow[v]);
19
                                                                                       16
20
                                                                                       17
                 if (in[u]) // gain speed
21
                                                                                       18
                      dfsLow[u] = min(dfsLow[u], dfsTime[v]);
22
                                                                                       19
             }
23
                                                                                       20
        }
24
                                                                                       21
25
        if (dfsTime[u] == dfsLow[u]) { // dfsLow[u] == dfsTime[u] -> SCC found 23
26
27
28
             while (true) {
                                                                                       25
                 int v = s.top();
29
                                                                                       26
30
                 s.pop();
                                                                                       27
                 in[v] = false;
31
                                                                                       28
                                                                                       29
                 group[v] = cnt;
                                                                                       30
                 if (v == u)
34
                                                                                       31
                      break;
35
                                                                                       32
             }
36
                                                                                       33
37
                                                                                       34
                                                                                       35
                                                                                       36
    // get SCC degree
                                                                                       37
    int deg[n + 1];
                                                                                       38
    memset(deg, 0, sizeof(deg));
                                                                                       39
    for (int i = 1; i \le n; i++)
                                                                                       40
                                                                                       41
        for (int j = 0; j < (int)q[i].size(); <math>j ++) {
                                                                                       42
             int v = g[i][j];
                                                                                       43
             if (group[i] != group[v])
47
                                                                                       44
                 deg[group[i]]++;
48
                                                                                       45
49
                                                                                       46
50
                                                                                       47
  9.3.2 SCC
```

for (int i = 0; $i < (int)q[v].size(); i++) {$

First of all we run DFS on the graph and sort the vertices in decreasing of theirs finishing time (we can use a stack).

Then, we start from the vertex with the greatest finishing time, and for each vertex⁵³ v that is not yet in any SCC, do: for each u that v is reachable by u and u is not yet⁵⁴ in any SCC, put it in the SCC of vertex v. The code is quite simple.

```
const int MAX_V = ...;
const int INF = 0x3f3f3f3f;
int V;
vector<int> g[MAX_V];

int dfn_idx = 0;
int scc_cnt = 0;
```

```
int dfn[MAX_V];
int low[MAX V]:
int belong[MAX_V];
bool in st[MAX V];
vector<int> st;
void scc(int v)
    dfn[v] = low[v] = dfn_idx++;
    st.push_back(v);
    in_st[v] = true;
    for (int i = 0; i < int(g[v].size()); i++) {
        const int u = q[v][i];
        if (dfn[u] = -1) {
            scc(u);
            low[v] = min(low[v], low[u]);
        } else if (in_st[u]) {
            low[v] = min(low[v], dfn[u]);
        }
   }
    if (dfn[v] = low[v]) {
        int k;
        do {
            k = st.back();
            st.pop_back();
            in_st[k] = false;
            belong[k] = scc_cnt;
        } while (k != v);
        scc_cnt++;
    }
}
void tarjan() // scc 建立的順序即為反向的拓璞排序
    st.clear();
    fill(dfn, dfn + V, -1);
    fill(low, low + V, INF);
    dfn_idx = 0;
    scc cnt = 0;
    for (int v = 0; v < V; v++) {
        if (dfn[v] == -1) {
            scc(v);
        }
   }
```

9.4 Shortest Path

Time complexity notations: V = vertex, E = edge Minimax: dp[u][v] = min(dp[u][v], max(dp[u][k], dp[k][v]))

 ∞

9.4.1 Dijkatra (next-to-shortest path) O(VloqE)

```
密集圖別用 priority queue!
```

```
struct Edge {
       int to, cost;
   };
   typedef pair<int, int> P; // <d, v>
   const int INF = 0x3f3f3f3f;
   int N. R:
   vector<Edge> g[5000];
10
   int d[5000];
   int sd[5000];
12
   int solve()
14
   {
15
       fill(d, d + N, INF);
       fill(sd, sd + N, INF);
17
       priority_queue<P, vector<P>, greater<P>> pq;
19
       d[0] = 0:
20
       pq.push(P(0, 0));
       while (!pq.empty()) {
23
24
           P p = pq.top();
           pq.pop();
           int v = p.second;
27
           if (sd[v] < p.first) // 比次短距離還大, 沒用, 跳過
                continue;
           for (size_t i = 0; i < q[v].size(); i++) {
                Edge &e = q[v][i];
               int nd = p.first + e.cost;
33
               if (nd < d[e.to]) { // 更新最短距離
34
                    swap(d[e.to], nd);
35
                    pq.push(P(d[e.to], e.to));
37
               if (d[e.to] < nd && nd < sd[e.to]) { // 更新次短距離
38
                    sd[e.to] = nd:
39
                    pq.push(P(sd[e.to], e.to));
40
41
           }
42
43
44
       return sd[N - 1];
45
   }
```

9.4.2 Bellman-Ford O(VE)

```
struct Edge {
int from, to, cost;
};
```

```
const int MAX_V = ...;
    const int MAX E = ...;
   const int INF = 0x3f3f3f3f;
   int V, E;
   Edge edges[MAX_E];
   int d[MAX V];
   bool bellman_ford()
13
        fill(d, d + V, INF);
14
15
       d[0] = 0;
        for (int i = 0; i < V; i++) {
17
            for (int j = 0; j < E; j++) {
18
                Edge &e = edges[j];
19
                if (d[e.to] > d[e.from] + e.cost) {
20
                    d[e.to] = d[e.from] + e.cost;
21
22
                    if (i == V - 1) // negative cycle
23
                         return true;
24
                }
25
26
            }
       }
27
28
        return false;
29
30
```

9.4.3 Floyd-Warshall $O(V^3)$

The graph is stored using adjacency matrix. The initial state is diagnal=0 and others=INF. (If INF is int, use long long for the matrix) If diagonal numbers are negative \leftarrow cycle .

```
for(int k = 0; k < N; k++)
  for(int i = 0; i < N; i++)
    for(int j = 0; j < N; j++)
        dp[i][j] = min(dp[i][j], dp[i][k] + dp[k][j]);</pre>
```

9.5 MST

9.5.1 Kruskal

- 1. Store the graph by (weight, (from, to))
- 2. Sort the graph by weight
- 3. Start from the smallest weight, and keep adding edges that won't form a cycle with the current MST set
- 4. Early termination condition: n-1 edges has been added, NOT size of the union-find set

10 Flow

10.1 Max Flow (Dinic)

```
struct Edge {
       int to, cap, rev;
2
       Edge(int a, int b, int c) {
           to = a:
            cap = b;
5
            rev = c;
6
7
   };
   const int INF = 0x3f3f3f3f;
   const int MAX V = 20000 + 10;
   // vector<Edge> g[MAX_V];
   vector< vector<Edge> > g(MAX_V);
   int level[MAX V];
   int iter[MAX_V];
   inline void add edge(int u, int v, int cap) {
       g[u].push_back((Edge){v, cap, (int)g[v].size()});
18
       g[v].push_back((Edge){u, 0, (int)g[u].size() - 1});
21
   void bfs(int s) {
       memset(level, -1, sizeof(level)); // 用 fill
       queue<int> q;
       level[s] = 0;
       q.push(s);
       while (!q.empty()) {
           int v = q.front(); q.pop();
            for (int i = 0; i < int(g[v].size()); i++) {
                const Edge& e = g[v][i];
                if (e.cap > 0 && level[e.to] < 0) {
                    level[e.to] = level[v] + 1;
34
                    q.push(e.to);
35
               }
36
            }
37
       }
38
39
   int dfs(int v, int t, int f) {
       if (v == t) return f;
42
       for (int& i = iter[v]; i < int(g[v].size()); i++) { // & 很重要
43
            Edge& e = a[v][i]:
44
            if (e.cap > 0 && level[v] < level[e.to]) {</pre>
45
                int d = dfs(e.to, t, min(f, e.cap));
46
                if (d > 0) {
47
                    e.cap -= d;
48
                    g[e.to][e.rev].cap += d;
49
50
                    return d:
51
            }
52
```

```
53
        return 0;
   }
55
56
57
   int max_flow(int s, int t) { // dinic
        int flow = 0;
58
        for (;;) {
59
            bfs(s);
60
            if (level[t] < 0) return flow;</pre>
61
            memset(iter, 0, sizeof(iter));
62
63
            int f;
            while ((f = dfs(s, t, INF)) > 0) {
64
                 flow += f:
65
66
        }
67
68
```

10.2 Min Cost Flow

```
#define st first
   #define nd second
   typedef pair <double, int> pii; // 改成用 int
   const double INF = 1e10;
   struct Edge {
       int to, cap;
       double cost;
       int rev:
   };
11
   const int MAX_V = 2 * 100 + 10;
   int V;
14
   vector<Edge> g[MAX_V];
   double h[MAX V]:
   double d[MAX_V];
   int prevv[MAX V];
   int preve[MAX_V];
   // int match[MAX V]:
20
21
   void add edge(int u, int v, int cap, double cost) {
22
       q[u].push_back((Edge){v, cap, cost, (int)q[v].size()});
23
       g[v].push_back((Edge){u, 0, -cost, (int)g[u].size() - 1});
24
25
26
27
   double min_cost_flow(int s, int t, int f) {
       double res = 0;
28
       fill(h, h + V, 0);
29
       fill(match, match + V, -1);
30
       while (f > \emptyset) {
31
            // dijkstra 找最小成本增廣路徑
32
            // without h will reduce to SPFA = O(V*E)
33
            fill(d, d + V, INF);
34
            priority_queue< pii, vector<pii>, greater<pii> > pq;
35
36
            d[s] = 0:
37
```

```
pq.push(pii(d[s], s));
38
39
           while (!pq.empty()) {
40
                pii p = pq.top(); pq.pop();
41
                int v = p.nd;
42
               if (d[v] < p.st) continue;
43
                for (size_t i = 0; i < q[v].size(); i++) {
44
                    const Edge& e = q[v][i];
45
                    if (e.cap > 0 \&\& d[e.to] > d[v] + e.cost + h[v] -
46
        h[e.to]) {
                        d[e.to] = d[v] + e.cost + h[v] - h[e.to];
47
                        prevv[e.to] = v;
48
                        preve[e.to] = i;
49
                        pq.push(pii(d[e.to], e.to));
50
                    }
51
52
           }
53
54
55
           // 找不到增庸路徑
           if (d[t] == INF) return -1; // double 時不能這樣判
           // 維護 h[v]
           for (int v = 0; v < V; v++)
               h[v] += d[v];
           // 找瓶頸
           int bn = f:
           for (int v = t; v != s; v = prevv[v])
                bn = min(bn, g[prevv[v]][preve[v]].cap);
           // // find match
           // for (int v = prevv[t]; v != s; v = prevv[prevv[v]]) {
                  int u = prevv[v]:
                  match[v] = u;
           //
           //
                  match[u] = v;
           // }
73
           // 更新剩餘圖
74
           f -= bn:
75
           res += bn * h[t]; // SPFA: res += bn * d[t]
           for (int v = t; v != s; v = prevv[v]) {
77
                Edge& e = q[prevv[v]][preve[v]];
78
                e.cap -= bn:
79
                g[v][e.rev].cap += bn;
80
           }
81
82
83
       return res;
84
```

10.3 Bipartite Matching, Unweighted

```
const int MAX_V = ...;
int V;
vector<int> g[MAX_V];
int match[MAX_V];
bool used[MAX_V];
```

```
void add edge(int u, int v) {
       g[u].push_back(v);
       g[v].push back(u);
   // 回傳有無找到從 V 出發的增廣路徑
   // (首尾都為未匹配點的交錯路徑)
   // [待確認] 每次遞迴都找一個末匹配點 V 及匹配點 U
   bool dfs(int v) {
       used[v] = true:
       for (size t i = 0; i < q[v].size(); i++) {
           int u = g[v][i], w = match[u];
18
           // 尚未配對或可從 W 找到增廣路徑 (即路徑繼續增長)
19
           if (w < 0 \mid | (!used[w] \&\& dfs(w)))  {
20
               // 交錯配對
21
               match[v] = u;
22
               match[u] = v:
23
               return true;
24
           }
25
       }
26
       return false;
27
28
29
   int bipartite_matching() { // 匈牙利演算法
30
       int res = 0;
31
       memset(match, -1, sizeof(match));
32
       for (int v = 0; v < V; v++) {
33
           if (match[v] = -1) {
34
               memset(used, false, sizeof(used));
               if (dfs(v)) {
37
                   res++;
               }
38
           }
39
       }
40
       return res;
41
  }
```

11 String

11.1 Rolling Hash

- 1. Use two rolling hashes if needed.
- 2. The prime for pre-calculation can be 137 and 257, for modulo can be 1e9+7 and 0xdefaced

```
#define N 1000100
#define B 137
#define M 1000000007

typedef long long ll;

char inp[N];
int len;
```

```
ll p[N], h[N];
   void init()
   { // build polynomial table and hash value
12
       p[0] = 1; // b to the ith power
13
       for (int i = 1; i \le len; i++) {
14
           h[i] = (h[i - 1] * B % M + inp[i - 1]) % M; // hash value
           p[i] = p[i - 1] * B % M;
16
       }
17
   }
18
19
   ll get_hash(int l, int r) // [l, r] of the inp string array
21
       return ((h[r + 1] - (h[l] * p[r - l + 1])) % M + M) % M;
22
23
  11.2 KMP
1 | void fail()
   {
2
       int len = strlen(pat);
3
```

```
f[0] = 0;
        int j = 0;
        for (int i = 1; i < len; i++) {
            while (j != 0 && pat[i] != pat[j])
                j = f[j - 1];
            if (pat[i] == pat[i])
                j++;
            f[i] = i;
        }
    }
    int match()
    {
19
        int res = 0:
20
        int j = 0, plen = strlen(pat), tlen = strlen(text);
21
22
        for (int i = 0; i < tlen; i++) {
23
            while (j != 0 && text[i] != pat[j])
24
                j = f[j - 1];
25
26
            if (text[i] == pat[i]) {
27
                if (j = plen - 1) \{ // find match \}
28
                    res++;
29
                    j = f[j];
30
                } else {
31
32
                    j++;
                }
33
            }
34
35
36
        return res;
37
38 | }
```

11.3 Z Algorithm

```
int len = strlen(inp), z[len];
   z[0] = 0; // initial
   int l = 0, r = 0; // z box bound [1, r]
   for (int i = 1; i < len; i++)
       if (i > r) { // i not in z box
            l = r = i; // z box contains itself only
            while (r < len \&\& inp[r - l] == inp[r])
                r++;
            z[i] = r - l;
11
            r--:
12
       } else { // i in z box
13
            if (z[i - l] + i < r) // over shoot R bound
14
                z[i] = z[i - l];
15
            else {
16
                l = i;
17
                while (r < len \&\& inp[r - l] == inp[r])
18
19
                    r++;
                z[i] = r - l;
20
21
                r--;
            }
22
23
       }
  }
24
```

12 Matrix

12.1 Gauss Jordan Elimination

```
typedef long long ll:
   typedef vector<ll> vec;
   typedef vector<vec> mat;
   vec gauss jordan(mat A) {
       int n = A.size(), m = A[0].size(); // 增廣矩陣
       for (int i = 0; i < n; i++) {
            // float: find j s.t. A[j][i] is max
            // mod: find min j s.t. A[j][i] is not 0
           int pivot = i:
            for (int j = i; j < n; j++) {
                // if (fabs(A[j][i]) > fabs(A[pivot])) {
12
                //
                       pivot = j;
13
                // }
14
                if (A[pivot][i] != 0) {
15
                    pivot = j;
16
                    break;
17
                }
18
           }
19
20
            swap(A[i], A[pivot]);
21
            if (A[i][i] = 0) \{ // \text{ if } (fabs(A[i][i]) < eps) \}
22
```

```
23
                // 無解或無限多組解
                // 可改成 continue, 全部做完後再判
24
                return vec();
25
            }
26
27
            ll divi = inv(A[i][i]);
28
            for (int j = i; j < m; j++) {
29
                // A[i][j] /= A[i][i];
30
                A[i][j] = (A[i][j] * divi) % MOD;
31
            }
32
33
            for (int j = 0; j < n; j++) {
34
                if (j != i) {
35
                    for (int k = i + 1; k < m; k++) {
36
                        // A[j][k] -= A[j][i] * A[i][k];
37
                        ll p = (A[i][i] * A[i][k]) % MOD;
38
                        A[j][k] = (A[j][k] - p + MOD) % MOD;
40
                    }
                }
41
42
           }
       }
43
45
       vec x(n);
        for (int i = 0; i < n; i++)
            x[i] = A[i][m - 1];
47
        return x;
48
49 | }
```

12.2 Determinant

整數版本

```
typedef long long ll;
   typedef vector<ll> vec;
   typedef vector<vec> mat;
   ll determinant(mat m) { // square matrix
       const int n = m.size();
       ll det = 1;
        for (int i = 0; i < n; i++) {
            for (int j = i + 1; j < n; j++) {
                int a = i, b = j;
10
                while (m[b][i]) {
11
                    ll q = m[a][i] / m[b][i];
12
                    for (int k = 0: k < n: k++)
13
                        m[a][k] = m[a][k] - m[b][k] * q;
14
                    swap(a, b);
15
                }
16
17
                if (a != i) {
18
                    swap(m[i], m[j]);
19
                    det = -det;
20
21
            }
22
23
           if (m[i][i] == 0)
24
```

13 Geometry

- 1. Keep things in integers as much as possible!
- 2. Try not to divide
- 3. If you have decimals, if they are fixed precision, you can usually just multiply all the input and use integers instead

13.1 EPS

```
= 0: fabs \le eps
< 0: < -eps
> 0: > +eps
```

13.2 Template

```
// if the points are given in doubles form, change the code accordingly
   typedef long long ll;
   typedef pair<ll, ll> pt; // points are stored using long long
    typedef pair<pt, pt> seg; // segments are a pair of points
    #define x first
    #define y second
   #define EPS 1e-9
12
   pt operator+(pt a, pt b)
13
14
        return pt(a.x + b.x, a.y + b.y);
15
16
17
   pt operator-(pt a, pt b)
18
19
        return pt(a.x - b.x, a.y - b.y);
20
21
22
   pt operator*(pt a, int d)
23
24
        return pt(a.x * d, a.v * d);
25
26
27
   ll cross(pt a, pt b)
28
   {
29
30
        return a.x * b.y - a.y * b.x;
31
32
```

```
{
34
35
        ll res = cross(b - a, c - a);
       if (res > 0) // left turn
36
37
           return 1:
        else if (res = 0) // straight
38
            return 0;
        else // right turn
40
41
            return -1:
42
43
   double dist(pt a, pt b)
45
        double dx = a.x - b.x;
46
        double dv = a.v - b.v:
47
        return sqrt(dx * dx + dy * dy);
48
49
50
   bool zero(double x)
51
        return fabs(x) <= EPS;
   bool overlap(seq a, seq b)
        return ccw(a.x, a.y, b.x) = 0 && ccw(a.x, a.y, b.y) = 0;
   bool intersect(seg a, seg b)
        if (overlap(a, b) == true) { // non-proper intersection
           double d = 0:
            d = max(d, dist(a.x, a.y));
           d = max(d, dist(a.x, b.x));
           d = max(d, dist(a.x, b.y));
            d = max(d, dist(a.y, b.x));
            d = max(d, dist(a.y, b.y));
           d = max(d, dist(b.x, b.y));
71
            // d > dist(a.x, a.y) + dist(b.x, b.y)
72
            if (d - (dist(a.x, a.y) + dist(b.x, b.y)) > EPS)
73
                return false;
74
75
            return true;
       }
76
77
       // Equal sign for ---- case
78
        // non geual sign => proper intersection
79
        if (ccw(a.x, a.y, b.x) * ccw(a.x, a.y, b.y) <= 0 &&
80
            ccw(b.x, b.y, a.x) * ccw(b.x, b.y, a.y) <= 0
81
            return true:
82
        return false;
83
   }
84
85
   double area(vector<pt> pts)
86
87
        double res = 0;
```

int ccw(pt a, pt b, pt c)

```
int n = pts.size();
89
        for (int i = 0; i < n; i++)
             res += (pts[i].y + pts[(i + 1) % n].y) * (pts[(i + 1) % n].x -
91
     \rightarrow pts[i].x);
        return res / 2.0;
92
93
94
    vector<pt> halfHull(vector<pt> &points)
95
96
        vector<pt> res;
97
98
        for (int i = 0; i < (int)points.size(); i++) {
99
             while ((int)res.size() >= 2 &&
100
                    ccw(res[res.size() - 2], res[res.size() - 1], points[i]) <</pre>
101

→ ∅)

                 res.pop back(); // res.size() - 2 can't be assign before
102
     \rightarrow size() >= 2
             // check, bitch
103
104
             res.push_back(points[i]);
105
106
107
        return res;
108
    }
109
110
111
    vector<pt> convexHull(vector<pt> &points)
112
        vector<pt> upper, lower;
113
114
        // make upper hull
115
        sort(points.begin(), points.end());
116
117
        upper = halfHull(points);
118
        // make lower hull
119
        reverse(points.begin(), points.end());
120
        lower = halfHull(points):
121
122
        // merae hulls
123
        if ((int)upper.size() > 0) // yes sir~
124
             upper.pop back();
125
        if ((int)lower.size() > 0)
126
             lower.pop back();
127
128
        vector<pt> res(upper.begin(), upper.end());
129
        res.insert(res.end(), lower.begin(), lower.end());
130
131
132
        return res;
133
```

14 Math

14.1 Euclid's formula (Pythagorean Triples)

$$a = p^2 - q^2$$

```
b=2pq (always even) c=p^2+q^2
```

14.2 Difference between two consecutive numbers' square is 16 odd 16

```
(k+1)^2 - k^2 = 2k+1
```

14.3 Summation

```
\begin{split} \sum_{k=1}^{n} 1 &= n \\ \sum_{k=1}^{n} k &= \frac{n(n+1)}{2} \\ \sum_{k=1}^{n} k^2 &= \frac{n(n+1)(2n+1)}{6} \\ \sum_{k=1}^{n} k^3 &= \frac{n^2(n+1)^2}{4} \end{split}
```

14.4 Combination

14.4.1 Pascal triangle

```
#define N 210
ll C[N][N];

void Combination() {
    for(ll i=0; i<N; i++) {
        C[i][0] = 1;
        C[i][i] = 1;
    }

    for(ll i=2; i<N; i++) {
        for(ll j=1; j<=i; j++) {
              C[i][j] = (C[i-1][j] + C[i-1][j-1])%M; // if needed, mod it
        }
    }
}</pre>
```

14.4.2 Lucus

```
\binom{n}{m}\equiv\prod_{i=0}^k\binom{n_i}{m_i}\pmod{p} where n=n_kp^k+n_{k-1}p^{k-1}+\cdots+n_1p+n_0, m=m_kp^k+m_{k-1}p^{k-1}+\cdots+m_1p+m_0 p is prime c
```

```
typedef long long ll;

typedef long long ll;

ll fast_pow(ll a, ll b, ll p) {
    ll ans = 1;
    ll base = a % p;
    b = b % (p - 1); // Fermat's little theorem
    while (b) {
        if (b & 1) {
            ans = (ans * base) % p;
    }
}
```

```
10
            base = (base * base) % p;
11
12
            b >>= 1;
        return ans;
   ll inv(ll a, ll p) {
17
18
        return fast_pow(a, p - 2, p);
19
20
   ll C(ll n, ll m, ll p) {
21
       if (n < m) return 0;
22
        m = min(m, n - m);
23
       ll nom = 1, den = 1;
24
        for (ll i = 1; i \le m; i++) {
25
            nom = (nom * (n - i + 1)) % p;
26
27
            den = (den * i) % p;
28
29
        return (nom * inv(den, p)) % p;
30
31
    // To make C(n, m) % p computed in O(log(p, n) * p) instead of O(m)
32
33
    // https://en.wikipedia.org/wiki/Lucas's_theorem
   ll lucas(ll n, ll m, ll p) {
       if (m == 0) return 1;
35
        return C(n % p, m % p, p) * lucas(n / p, m / p, p) % p;
36
  14.4.3 線性
```

```
ll binomialCoeff(ll n, ll k)
{
    ll res = 1;
    if ( k > n - k ) // Since C(n, k) = C(n, n-k)
        k = n - k;

    for (int i = 0; i < k; ++i) // n...n-k / 1...k
        res *= (n - i);
        res /= (i + 1);
    }

    return res;</pre>
```

14.5 Chinese remainder theorem

```
typedef long long ll;

struct Item {
    ll m, r;
};

Item extcrt(const vector<Item> &v)
{
    ll m1 = v[0].m, r1 = v[0].r, x, y;
```

```
10
        for (int i = 1; i < int(v.size()); i++) {
11
            ll m2 = v[i].m, r2 = v[i].r;
12
            ll g = extgcd(m1, m2, x, y); // now x = (m/g)^(-1)
13
14
            if ((r2 - r1) \% q != 0)
15
                return {-1, -1};
17
            ll k = (r2 - r1) / g * x % (m2 / g);
18
           k = (k + m2 / q) \% (m2 / q); // for the case k is negative
19
20
           ll m = m1 * m2 / q;
21
            ll r = (m1 * k + r1) % m:
22
23
24
            m1 = m:
            r1 = (r + m) \% m; // for the case r is negative
25
27
        return (Item) {
28
29
            m1, r1
       };
```

14.6 2-Circle relations

```
d = 圓心距, R, r 為半徑 (R \ge r) 内切: d = R - r 外切: d = R + r 内離: d < R - r 外離: d > R + r 相交: d < R + r 且 d > R - r
```

14.7 Fun Facts

1. 如果 $\frac{b}{a}$ 是最簡分數,則 $1-\frac{b}{a}$ 也是

15 Dynamic Programming - Problems collection

```
# 零一背包 (poj 1276)
fill(dp, dp + W + 1, 0);
for (int i = 0; i < N; i++)
    for (int j = W; j >= items[i].w; j--)
        dp[j] = max(dp[j], dp[j - w[i]] + v[i]);
return dp[W];

# 多重背包二進位拆解 (poj 1276)
for_each(ll v, w, num) {
    for (ll k = 1; k <= num; k *= 2) {
        items.push_back((Item) {k * v, k * w});
        num -= k;
    }
    if (num > 0)
        items.push_back((Item) {num * v, num * w});
}

# 完全背包
dp[i][j] = 前 i + 1 個物品, 在重量 j 下所能組出的最大價值
```

```
第 i 個物品,不放或至少放一個
dp[i][j] = max(dp[i - 1][j], dp[i][j - w[i]] + v[i])
fill(dp, dp + W + 1, 0);
for (int i = 0; i < N; i++)
   for (int j = w[i]; j \leftarrow W; j++)
       dp[j] = max(dp[j], dp[j - w[i]] + v[i]);
return dp[W]:
# Coin Change (2015 桂冠賽 E)
dp[i][j] = 前 i + 1 個物品, 組出 j 元的方法數
第 i 個物品,不用或用至少一個
dp[i][j] = dp[i - 1][j] + dp[i][j - coin[i]]
# Cutting Sticks (2015 桂冠賽 F)
補上二個切點在最左與最右
dp[i][j] = 使(i, j) 區間中的所有切點都被切的最小成本
dp[i][j] = min(dp[i][c] + dp[c][j] + (p[j] - p[i]) for i < c < j
dp[i][i + 1] = 0
ans = dp[0][N + 1]
# Throwing a Party (itsa dp 06)
給定一棵有根樹、代表公司職位層級圖、每個人有其權重、現從中選一個點集合出來、
且一個人不能與其上司一都在集合中,並最大化集合的權重和,輸出該總和。
dp[u][0/1] = u 在或不在集合中,以 u 為根的子樹最大權重和
dp[u][0] = max(max(dp[c][0], dp[c][1]) for children c of u) + val[u]
dp[u][1] = max(dp[c][0]  for children c of u)
bottom up dp
# LIS (0(N^2))
dp[i] = 以 i 為結尾的 LIS 的長度
dp[i] = max(dp[j] \text{ for } 0 \iff j \iff i) + 1
ans = max(dp)
# LIS (0(nlgn)), poj 1631
dp[i] = 長度為 i + 1 的 LIS 的最後一項的最小值,不存在時為 INF
fill(dp, dp + N, INF);
for (int i = 0; i < N; i++)
   *lower bound(dp, dp + N, A[i]) = A[i];
ans = lower_bound(dp, dp + N, INF) - dp;
# Maximum Subarray
# Not equal on a Segment (cf edu7 C)
給定長度為 n 的陣列 a[] 與 m 個詢問。
針對每個詢問 l, r, x 請輸出 a[l, r] 中不等於 x 的任一位置。
dp[i] = max j such that j < i and a[j] != a[i]
dp[i] = dp[i - 1] if a[i] == a[i - 1] else i - 1
針對每筆詢問 l, r, x
1. a[r] != x
2. a[r] = x & dp[r] >= l -> 輸出 dp[r]
3. a[r] = x && dp[r] < l -> 輸出 -1
# bitmask dp, poj 2686
給定一個無向帶權圖, 代表 M 個城市之間的路, 與 N 張車票,
每張車票有一個數值 t[i]、若欲使用車票 t[i] 從城市 U 經由路徑 d[u][v] 走到城市 V、
所花的時間為 d[u][v] / t[i]。請問, 從城市 A 走到城市 B 最快要多久?
dp[S][v] = 從城市 A 到城市 v 的最少時間, 其中 S 為用過的車票的集合
考慮前一個城市 U 是誰,使用哪個車票 t[i] 而來,可以得到轉移方程式:
dp[S][v] = min([
   dp[S - {v}][u] + d[u][v] / t[i]
   for all city u has edge to v, for all ticket in S
# Tug of War
N 個人參加拔河比賽, 每個人有其重量 W[i], 欲使二隊的人數最多只差一, 雙方的重量和越接近越好
```

```
請問二隊的重量和分別是多少?
dp[i][j][k] = 只考慮前 i+1 個人, 可不可以使左堆的重量為 j, 且左堆的人數為 k dp[i][j][k] = dp[i-1][j-w[i][k-1] or dp[i-1][j][k]
dp[i][j] = (dp[i - 1][j - w[i]] << 1) | (dp[i - 1][j])
# Modulo Sum (cf 319 B)
給定長度為 N 的序列 A 與一正整數 M, 請問該序列中有無一個子序列, 子序列的總合是 M 的倍數
若 N > M, 則根據鴿籠原理, 必有至少兩個前綴和的值 mod M 為相同值, 解必定存在
dp[i][j] = 前 i + 1 個數可否組出 mod m = j 的數
dp[i][j] = true if
   dp[i-1][(j-(a[i] \text{ mod m})) \text{ mod m}] \text{ or } dp[i-1][j] \text{ or }
   i = a[i] \% m
# P01 2229
給定正整數 N, 請問將 N 拆成一堆 2^x 之和的方法數
dp[i] = 拆解 N 的方法數
dp[i] = dp[i / 2] if i is odd
     = dp[i - 1] + dp[i / 2] if i is even
# P0J 3616
給定 N 個區間 [S, t)、每個區間有權重 W[i]、從中選出一些不相交的區間、使權重和最大
dp[i] = 考慮前 i + 1 個區間, 且必選第 i 個區間的最大權重和
dp[i] = max(dp[j] \mid 0 \le j \le i) + w[i]
ans = max(dp)
# P0J 2184
N 隻牛每隻牛有權重 <s, f>, 從中選出一些牛的集合,
使得 sum(s) + sum(f) 最大, 且 sum(s) > 0, sum(f) > 0。
枚舉 SUM(S) ,將 SUM(S) 視為重量對 f 做零一背包。
# P0J 3666
給定長度為 N 的序列,請問最少要加多少值,使得序列單調遞增
dp[i][j] = 使序列前 i+1 項變為單調, 且將 A[i] 變為「第 j 小的數」的最小成本
dp[i][j] = min(dp[i - 1][k] \mid 0 \leftarrow k \leftarrow j) + abs(S[j] - A[i])
min(dp[i - 1][k] | 0 <= k <= j) 動態維護
for (int j = 0; j < N; j++)
    dp[0][i] = abs(S[i] - A[0]);
for (int i = 1; i < N; i++) {
    int pre_min_cost = dp[i][0];
    for (int j = 0; j < N; j++) {
```

```
pre_min_cost = min(pre_min_cost, dp[i-1][j]);
       dp[i][i] = pre min cost + abs(S[i] - A[i]);
   }
ans = min(dp[N - 1])
# P0J 3734
N 個 blocks 上色, R, G, Y, B, 上完色後紅色的數量與綠色的數量都要是偶數。請問方法數。
dp[i][0/1/2/3] = 前 i 個 blocks 上完色, 紅色數量為奇數/偶數, 綠色數量為數/偶數
用遞推, 考慮第 i+1 個 block 的顏色, 找出個狀態的轉移, 整理可發現 dp[i+1][0] = dp[i][2] + dp[i][1] + 2 * dp[i][0]
dp[i + 1][1] = dp[i][3] + dp[i][0] + 2 * dp[i][1]
dp[i + 1][2] = dp[i][0] + dp[i][3] + 2 * dp[i][2]
dp[i + 1][3] = dp[i][1] + dp[i][2] + 2 * dp[i][3]
矩陣快速幂加速求 dp[N - 1][0][0]
# P01 3171
數線上、給定 N 個區間 [s[i], t[i]]、每個區間有其代價、求覆蓋區間 [M, E] 的最小代價。
dp[i][j] = 最多使用前 i + 1 個區間, 使 [M, j] 被覆蓋的最小代價
考慮第 1 個區間用或不用,可得:
dp[i][i] =
   1. \min(dp[i-1][k] \text{ for } k \text{ in } [s[i]-1, t[i]]) + cost[i] \text{ if } i=t[i]
   2. dp[i - 1][j] if j \neq t[i]
壓空間,使用線段樹加速。
dp[t[i]] = min(dp[t[i]],
   min(dp[i - 1][k] for k in [s[i] - 1, t[i]]) + cost[i]
fill(dp, dp + E + 1, INF);
seg.init(E + 1, INF);
int idx = 0;
while (idx < N && A[idx].s == 0) {
   dp[A[idx].t] = min(dp[A[idx].t], A[idx].cost);
    seg.update(A[idx].t, A[idx].cost);
   idx++:
for (int i = idx; i < N; i++) {
   ll v = min(dp[A[i].t], seq.query(A[i].s - 1, A[i].t + 1) + A[i].cost);
   dp[A[i].t] = v;
    seg.update(A[i].t, v);
```