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1 Contest Setup

1.1 vimrc

```
set number
                  " Show line numbers
                  " Enable inaction via mouse
  set mouse=a
                      " Highlight matching brace
  set showmatch
                      " Show underline
  set cursorline
  set cursorcolumn
                      " highlight vertical column
  filetype on "enable file detection
  syntax on "syntax highlight
  set autoindent
                      " Auto-indent new lines
  set shiftwidth=4
                      " Number of auto-indent spaces
                      " Enable smart-indent
12 set smartindent
  set smarttab
                      " Enable smart-tabs
set tabstop=4
                 " Number of spaces per Tab
    -----Optional-----
                          " Number of undo levels
set undolevels=10000
19 set scrolloff=5
                      " Auto scroll
21 set hlsearch
                  " Highlight all search results
22 set smartcase
                 " Enable smart-case search
23 set ignorecase " Always case-insensitive
set incsearch " Searches for strings incrementally
highlight Comment ctermfg=cyan
27 set showmode
29 set encoding=utf-8
set fileencoding=utf-8
31 scriptencoding=utf-8
```

1.2 bashrc

```
1 | alias g++="g++ -Wall -Wextra -std=c++11 -02"
```

1.3 Grep Error and Warnings

```
| g++ main.cpp 2>&1 | grep -E 'warning|error'
```

1.4 C++ template

```
#include <bits/stdc++.h>

using namespace std;

typedef long long int ll;
typedef pair<int, int> ii;
```

```
8 | int main()
9 | {
10     return 0;
11 | }
```

1.5 Java template

```
import java.io.*;
  import java.util.*;
  public class Main
       public static void main(String[] args)
           MyScanner sc = new MyScanner();
           out = new PrintWriter(new BufferedOutputStream(System.out));
           // Start writing your solution here.
           // Stop writing your solution here.
           out.close();
14
15
       public static PrintWriter out;
16
       public static class MyScanner
18
19
           BufferedReader br:
20
21
           StringTokenizer st;
23
           public MyScanner()
24
25
               br = new BufferedReader(new InputStreamReader(System.in));
26
28
           boolean hasNext()
29
               while (st == null || !st.hasMoreElements()) {
30
                        st = new StringTokenizer(br.readLine());
                   } catch (Exception e) {
33
                        return false;
35
37
               return true;
39
40
           String next()
41
42
               if (hasNext())
                   return st.nextToken();
43
44
               return null;
45
46
           int nextInt()
47
```

```
return Integer.parseInt(next());
52
           long nextLong()
53
               return Long.parseLong(next());
           double nextDouble()
57
58
               return Double.parseDouble(next());
           String nextLine()
62
63
               String str = "";
                    str = br.readLine();
               } catch (IOException e) {
                    e.printStackTrace();
               return str;
```

1.5.1 Java Issues

- 1. Random Shuffle before sorting: Random rnd = new Random(); rnd.nextInt();
- 2. Use StringBuilder for large output

2 System Testing

- 1. Setup bashrc and vimrc
- 2. Look for compilation parameter and code it into bashrc
- 3. Test if c++ and java templates work properly on local and judge machine
- 4. Test "divide by $0" \to RE/TLE$?
- 5. Test stack size

3 Reminder

- 1. 隊友的建議,要認真聽! 通常隊友的建議都會突破你盲點
- 2. Read the problem statements carefully. Input and output specifications and constraints are crucial!
- 3. Estimate the time complexity and memory complexity carefully.
- 4. Time penalty is 20 minutes per WA, don't rush!
- 5. Sample test cases must all be tested and passed before every submission!
- 6. Test the corner cases, such as 0, 1, -1. Test all edge cases of the input specification.
- 7. Bus error: the code has scanf, fgets but have nothing to read! Check if you have early termination but didn't handle it properly.
- 8. Binary search? 數學算式移項合併後查詢?
- 9. Two Pointer <-> Binary Search
- 10. Directed graph connectivity -> DFS. Undirected graph -> Union Find
- 11. Check connectivity of the graph if the problem statement doesn't say anything
- 12. longlong = int * int won't work!
- 13. Shifting for longlongint should be something like $1LL \ll 35$
- 14. For continuous input problems, be sure to read in all input BEFORE terminating and start processing next the input.
- 15. Don't use anonymous struct

4 Useful code

4.1 Leap year

```
| year % 400 == 0 || (year % 4 == 0 && year % 100 != 0)
```

4.2 Fast Exponentiation O(log(exp))

4.3 GCD O(log(a+b))

注意負數的 case! C++ 是看被除數決定正負號的。

```
1 | 11 gcd(11 a, 11 b)
2 | {
3 | return b == 0 ? a : gcd(b, a % b);
4 | }
```

4.4 Extended Euclidean Algorithm

Bezout identity ax + by = gcd(a, b), where gcd(a, b) is the smallest positive integer that can be written as ax + by, and every integer of the form ax + by is a multiple of gcd(a, b).

4.5 Mod Inverse

Case 1 gcd(a, m) = 1: ax + my = gcd(a, m) = 1 (use ext_gcd) Case 2 m is prime: $a^{m-2} \equiv a^{-1}mod m$ (use Fermat's little theorem)

4.6 Prime Generator

4.7 Binomial Coefficient

```
int binomialCoeff(int n, int k)
{
    int res = 1;

    if ( k > n - k ) // Since C(n, k) = C(n, n-k)
        k = n - k;

    for (int i = 0; i < k; ++i) // n...n-k / 1...k
        res *= (n - i);
        res /= (i + 1);
}

return res;
}</pre>
```

4.8 scanf/printf reference

4.9 STL quick reference

4.9.1 Map

```
map<T1, T2> m; // iterable
void clear();
void erase(T1 key);
it find(T1 key); // <key, val>
void insert(pair<T1, T2> P);
T2 &[](T1 key); // if key not in map, new key will be inserted with default val
it lower_bound(T1 key); // = m.end() if not found, *it = <key, val>
it upper_bound(T1 key); // = m.end() if not found, *it = <key, val>
```

4.9.2 Set

```
set<T> s; // iterable
void clear();
size_t count(T val); // number of val in set
void erase(T val);
it find(T val); // = s.end() if not found
void insert(T val);
it lower_bound(T val); // = s.end() if not found, *it = <key, val>
it upper_bound(T val); // = s.end() if not found, *it = <key, val>
```

4.9.3 Algorithm

```
1 // return if i is smaller than j
  comp = [&](const T &i, const T &j) -> bool;
  vector<T> v:
  bool any of(v.begin(), v.end(), [&](const T &i) -> bool);
  bool all of(v.begin(), v.end(), [&](const T &i) -> bool);
  void copy(inp.begin(), in.end(), out.begin());
  int count(v.begin(), v.end(), int val); // number of val in v
  it unique(v.begin(), v.end());
                                         // it - v.begin() = size
  // after calling, v[nth] will be n-th smallest elem in v
  void nth element(v.begin(), nth it, bin comp);
  void merge(in1.begin(), in1.end(), in2.begin(), in2.end(), out.begin(),
  // include union, intersection, difference, symmetric difference(xor)
  void set union(in1.begin(), in1.end(), in2.begin(), in2.end(), out.
      begin(), comp);
  bool next permutation(v.begin(), v.end());
15 // v1, v2 need sorted already, whether v1 includes v2
bool inclues(v1.begin(), v1.end(), v2.begin(), v2.end());
it find(v.begin(), v.end(), T val); // = v.end() if not found
18 it search(v1.begin(), v1.end(), v2.begin(), v2.end());
it lower bound(v.begin(), v.end(), T val);
it upper bound(v.begin(), v.end(), T val);
21 bool binary search(v.begin(), v.end(), T val); // exist in v?
void sort(v.begin(), v.end(), comp);
void stable sort(v.begin(), v.end(), comp);
```

4.9.4 String

4.9.5 Priority Queue

```
bool cmp(ii a, ii b)
{
    if(a.first == b.first)
        return a.second > b.second;
    return b.first > a.first;
}

priority_queue< ii, vector<ii>, function<bool(ii, ii) > pq(cmp);
```

- 5 Search
- 5.1 Ternary Search
- 5.2 折半完全列舉
- 5.3 Two-pointer 爬行法
- 6 Basic data structure
- 6.1 1D BIT

```
| // BIT is 1-based | const int MAX_N = 20000; //這個記得改! | ll bit[MAX_N + 1]; | int sum(int i) { | int s = 0; | while (i > 0) { | s += bit[i]; | i -= (i & -i); | } | return s; | } | void add(int i, int x) { | while (i <= MAX_N) { | bit[i] += x; | i += (i & -i); | } | } | } | } | | }
```

6.2 2D BIT

6.3 Union Find

```
|| #define N 20000 // 記得改
   struct UFDS {
       int par[N];
       void init() {
           memset(par, -1, sizeof(par));
       int root(int x) {
           return par[x] < 0 ? x : par[x] = root(par[x]);</pre>
       void merge(int x, int y) {
           x = root(x);
           y = root(y);
15
           if (x != y) {
               if (par[x] > par[y])
                   swap(x, y);
20
               par[x] += par[y];
               par[y] = x;
22
           }
24 }
```

6.4 Segment Tree

6.5 Sparse Table

```
struct {
    int sp[MAX_LOG_N][MAX_N]; // MAX_LOG_N = ceil(lg(MAX_N))

void build(int inp[], int n) {
    for (int j = 0; j < n; j++) {
        sp[0][j] = inp[j];
    }

for (int i = 1; (1 << i) <= n; i++)
        for (int j = 0; j + (1 << i) <= n; j++)
        sp[i][j] =
            min(sp[i - 1][j], sp[i - 1][j + (1 << (i - 1))]);

int query(int l, int r) { // [l, r)
    int k = floor(log2(r - 1));

return min(sp[k][l], sp[k][r - (1 << k)]);
}
sptb;</pre>
```

7 Dynamic Programming

- 8 Tree
- 8.1 LCA
- 8.2 Tree Centroid
- 8.3 Treap
- 9 Graph
- 9.1 Articulation point / edge
- 9.2 CC
- 9.2.1 BCC vertex
- 9.2.2 BCC edge
- 9.2.3 SCC
- 9.3 Shortest Path
- 9.3.1 Dijkatra
- 9.3.2 Dijkatra (next-to-shortest path)
- 9.3.3 SPFA
- 9.3.4 Bellman-Ford
- 9.3.5 Floyd-Warshall
- 9.4 MST
- 9.4.1 Kruskal
 - 1. Store the graph by (weight, (from, to))
 - 2. Sort the graph by weight
 - 3. Start from the smallest weight, and keep adding edges that won't form a cycle with the current MST set
 - 4. Early termination condition: n-1 edges has been added, NOT size of the union-find set

- 9.4.2 Prim
- 9.5 Flow
- 9.5.1 Max Flow (Dinic)
- 9.5.2 Min-Cut
- 9.5.3 Min Cost Max Flow
- 9.5.4 Maximum Bipartite Graph

10 String

10.1 Rolling Hash

- 1. Use two rolling hashes if needed.
- 2. The prime for pre-calculation can be 137 and 257, for modulo can be 1e9 + 7 and 0xdefaced

```
#define N 1000100
  #define B 137
  #define M 1000000007
  typedef long long 11;
  char inp[N];
  int len;
  11 p[N], h[N];
  void init()
  { // build polynomial table and hash value
      p[0] = 1; // b to the ith power
      for (int i = 1; i <= len; i++) {
          h[i] = (h[i-1] * B % M + inp[i-1]) % M; // hash value
16
          p[i] = p[i - 1] * B % M;
17
20
  ll get_hash(int l, int r) // [l, r] of the inp string array
21 {
      return ((h[r+1] - (h[1] * p[r-1+1])) % M + M) % M;
23 }
```

10.2 KMP

```
f[i] = j;
16 }
18 int match()
19 {
       int res = 0;
20
       int j = 0, plen = strlen(pat), tlen = strlen(text);
21
23
       for (int i = 0; i < tlen; i++) {
           while (j != 0 && text[i] != pat[j])
24
25
               j = f[j - 1];
26
27
           if (text[i] == pat[j]) {
               if (j == plen - 1) { // find match}
                   res++;
30
                   j = f[j];
31
               } else {
32
                   j++;
33
36
       return res;
```

10.3 Z Algorithm

10.4 Trie

```
1 #define N 600010
 struct node {
       int child[26];
       bool ending;
  } trie[N];
  root is 0
  memset(trie, 0, sizeof(trie));
  || freeNode = 1;
11 */
12 int freeNode;
  void insert(string &str, int pos, int node)
14 {
       if (pos == (int)str.length()) {
           trie[node].ending = true;
       } else { // find which way to go
           int c = str[pos] - 'a';
           if (trie[node].child[c] == 0) // give a new node
19
               trie[node].child[c] = freeNode++;
20
21
           insert(str, pos + 1, trie[node].child[c]);
22
23 }
```

10.5 Suffix Array

11 Geometry

- 1. Keep things in integers as much as possible!
- 2. Try not to divide
- 3. If you have decimals, if they are fixed precision, you can usually just multiply all the input and use integers instead

11.1 EPS

```
a>b\to a-b>0\to a-b>EPS (stands for positive) a\geq b\to a-b\geq 0\to a-b>-EPS (stands for positive or zero)
```

11.2 Template

```
1 // if the points are given in doubles form, change the code accordingly
  typedef long long 11;
  typedef pair<11, 11> pt; // points are stored using long long
  typedef pair<pt, pt> seq; // segments are a pair of points
   #define x first
  #define y second
  #define EPS 1e-9
  pt operator+(pt a, pt b)
       return pt(a.x + b.x, a.y + b.y);
16
  }
  pt operator-(pt a, pt b)
20
       return pt(a.x - b.x, a.y - b.y);
21
22
  pt operator*(pt a, int d)
23
24
       return pt(a.x * d, a.y * d);
26
27
  11 cross(pt a, pt b)
28
29
       return a.x * b.y - a.y * b.x;
32
33
  int ccw(pt a, pt b, pt c)
34
35
      11 \text{ res} = \text{cross}(b - a, c - a);
36
       if (res > 0) // left turn
37
           return 1;
       else if (res == 0) // straight
           return 0;
39
       else // right turn
```

```
return -1;
44 double dist(pt a, pt b)
45 {
       double dx = a.x - b.x;
       double dy = a.y - b.y;
       return sqrt(dx * dx + dy * dy);
49 }
51 bool zero(double x)
52 {
       return fabs(x) <= EPS;</pre>
54 }
56 bool overlap(seg a, seg b)
57 {
58
       return ccw(a.x, a.y, b.x) == 0 && ccw(a.x, a.y, b.y) == 0;
59 }
60
61 bool intersect(seg a, seg b)
62 {
       if (overlap(a, b) == true) { // non-proper intersection
           double d = 0;
           d = max(d, dist(a.x, a.y));
           d = max(d, dist(a.x, b.x));
           d = max(d, dist(a.x, b.y));
           d = max(d, dist(a.y, b.x));
           d = max(d, dist(a.y, b.y));
           d = max(d, dist(b.x, b.y));
           // d > dist(a.x, a.y) + dist(b.x, b.y)
           if (d - (dist(a.x, a.y) + dist(b.x, b.y)) > EPS)
               return false;
           return true;
       // Equal sign for ---- case
       // non qeual sign => proper intersection
       if (ccw(a.x, a.y, b.x) * ccw(a.x, a.y, b.y) \le 0 &&
81
           ccw(b.x, b.y, a.x) * ccw(b.x, b.y, a.y) <= 0)
82
           return true;
       return false;
84 }
86 double area(vector<pt> pts)
87 {
       double res = 0;
       int n = pts.size();
       for (int i = 0; i < n; i++)
           res += (pts[i].y + pts[(i + 1) % n].y) * (pts[(i + 1) % n].x -
       pts[i].x);
       return res / 2.0;
92
93 }
95 vector<pt> halfHull(vector<pt> &points)
```

```
96
97
        vector<pt> res;
98
        for (int i = 0; i < (int)points.size(); i++) {</pre>
99
            while ((int)res.size() >= 2 &&
100
                   ccw(res[res.size() - 2], res[res.size() - 1], points[i])
                res.pop_back(); // res.size() - 2 can't be assign before
        size() >= 2
            // check, bitch
            res.push_back(points[i]);
106
        return res;
109
   vector<pt> convexHull(vector<pt> &points)
       vector<pt> upper, lower;
114
        // make upper hull
       sort(points.begin(), points.end());
       upper = halfHull(points);
        // make lower hull
       reverse(points.begin(), points.end());
        lower = halfHull(points);
        // merge hulls
124
        if ((int)upper.size() > 0) // yes sir~
            upper.pop_back();
126
       if ((int)lower.size() > 0)
127
           lower.pop back();
129
       vector<pt> res(upper.begin(), upper.end());
        res.insert(res.end(), lower.begin(), lower.end());
        return res;
133
   bool completelyInside(vector<pt> &outer, vector<pt> &inner)
136
        int even = 0, odd = 0;
        for (int i = 0; i < (int)inner.size(); i++) {</pre>
            // y = slope * x + offset
            int cntIntersection = 0;
            11 slope = rand() % INT_MAX + 1;
141
            ll offset = inner[i].y - slope * inner[i].x;
142
143
            11 farx = 111111 * (slope >= 0 ? 1 : -1);
145
            11 fary = farx * slope + offset;
            seg a = seg(pt(inner[i].x, inner[i].y), pt(farx, fary));
146
            for (int j = 0; j < (int)outer.size(); j++) {</pre>
147
                seg b = seg(outer[j], outer[(j + 1) % (int)outer.size()]);
```

```
if ((b.x.x * slope + offset == b.x.y) ||
150
                     (b.y.x * slope + offset == b.y.y)) { // on-line}
151
                    break;
154
                if (intersect(a, b) == true)
156
                    cntIntersection++;
157
158
159
            if (cntIntersection % 2 == 0) // outside
160
161
            else
162
163
                odd++;
164
165
        return odd == (int)inner.size();
166
167 }
168
169 // srand(time(NULL))
170 // rand()
```

12 Math

12.1 Euclid's formula

$$a = p^2 - q^2$$

 $b = 2pq$ (always even)
 $c = p^2 + q^2$

12.2 Difference between two consecutive numbers' square is odd

$$(k+1)^2 - k^2 = 2k+1$$

12.3 Summation

$$\sum_{k=1}^{n} 1 = n$$

$$\sum_{k=1}^{n} k = \frac{n(n+1)}{2}$$

$$\sum_{k=1}^{n} k^{2} = \frac{n(n+1)(2n+1)}{6}$$

$$\sum_{k=1}^{n} k^{3} = \frac{n^{2}(n+1)^{2}}{4}$$