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1 Contest Setup

1.1 vimrc

```
set number
                  " Show line numbers
                  " Enable inaction via mouse
  set mouse=a
  set showmatch
                       " Highlight matching brace
                      " Show underline
  set cursorline
  set cursorcolumn
                      " highlight vertical column
  filetype on "enable file detection
  syntax on "syntax highlight
  set autoindent
                       " Auto-indent new lines
  set shiftwidth=4
                      " Number of auto-indent spaces
12 set smartindent
                      " Enable smart-indent
  set smarttab
                      " Enable smart-tabs
14 set tabstop=4
                  " Number of spaces per Tab
    -----Optional-----
                          " Number of undo levels
set undolevels=10000
set scrolloff=5
                      " Auto scroll
21 set hlsearch
                  " Highlight all search results
22 set smartcase
                 " Enable smart-case search
  set ignorecase " Always case-insensitive
24 set incsearch
                 " Searches for strings incrementally
highlight Comment ctermfg=cyan
27 set showmode
29 set encoding=utf-8
30 set fileencoding=utf-8
31 scriptencoding=utf-8
```

1.2 bashrc

```
1 | alias g++="g++ -Wall -Wextra -std=c++11 -02"
```

1.3 C++ template

```
#include <bits/stdc++.h>

using namespace std;

#define x first
#define y second

typedef long long int ll;
typedef pair<int, int> ii;

int main()
{
```

```
13 | return 0;
14 | }
```

1.4 Java template

```
import java.io.*;
   import java.util.*;
  public class Main
       public static void main(String[] args)
           MyScanner sc = new MyScanner();
           out = new PrintWriter(new BufferedOutputStream(System.out));
           // Start writing your solution here.
           // Stop writing your solution here.
           out.close();
13
14
       public static PrintWriter out;
17
       public static class MyScanner
18
19
           BufferedReader br;
20
           StringTokenizer st;
21
22
23
           public MyScanner()
24
25
               br = new BufferedReader(new InputStreamReader(System.in));
26
27
           boolean hasNext()
28
30
               while (st == null || !st.hasMoreElements()) {
                    try {
                        st = new StringTokenizer(br.readLine());
                    } catch (Exception e) {
                        return false;
34
35
36
               return true;
37
39
40
           String next()
41
               if (hasNext())
42
                    return st.nextToken();
                return null;
           }
45
46
47
           int nextInt()
48
49
                return Integer.parseInt(next());
```

```
long nextLong()
52
54
                return Long.parseLong(next());
55
           double nextDouble()
                return Double.parseDouble(next());
60
61
           String nextLine()
63
                String str = "";
64
                try {
                    str = br.readLine();
               } catch (IOException e) {
                    e.printStackTrace();
69
                return str;
```

1.4.1 Java Issues

- 1. Random Shuffle before sorting: $Random \ rnd = new \ Random(); \ rnd.nextInt();$
- 2. Use StringBuilder for large output

2 Reminder

- 1. 隊友的建議, 要認真聽! 通常隊友的建議都會突破你盲點
- Read the problem statements carefully. Input and output specifications and constraints are crucial!
- 3. Estimate the **time complexity** and **memory complexity** carefully.
- 4. Time penalty is 20 minutes per WA, don't rush!
- 5. Sample test cases must all be tested and passed before every submission!
- 6. Test the corner cases, such as 0, 1, -1. Test all edge cases of the input specification.
- 7. Bus error: the code has scanf, fgets but have nothing to read! Check if you have early termination but didn't handle it properly.
- 8. Binary search? 數學算式移項合併後查詢?
- 9. Two Pointer <-> Binary Search
- 10. Directed graph connectivity -> DFS. Undirected graph -> Union Find
- 11. Check connectivity of the graph if the problem statement doesn't say anything
- 12. longlong = int * int won't work!
- 13. Shifting for longlongint should be something like $1LL \ll 35$

3 Useful code

3.1 Grep Error and Warnings

```
| g++ main.cpp 2>&1 | grep -E 'warning|error'
```

3.2 Leap year

```
1 | year % 400 == 0 | | (year % 4 == 0 && year % 100 != 0)
```

3.3 Fast Exponentiation O(log(exp))

3.4 GCD O(log(a+b))

注意負數的 case!

3.5 Extended Euclidean Algorithm

Bezout identity ax + by = gcd(a, b), where gcd(a, b) is the smallest positive integer that can be written as ax + by, and every integer of the form ax + by is a multiple of gcd(a, b).

3.6 Mod Inverse

```
Case 1 gcd(a, m) = 1: ax + my = gcd(a, m) = 1 (use ext\_gcd)
```

Case 2 m is prime: $a^{m-2} \equiv a^{-1} \mod m$ (use Fermat's little theorem)

3.7 Prime Generator

3.8 Binomial Coefficient

```
int binomialCoeff(int n, int k)
{
  int res = 1;

  if ( k > n - k ) // Since C(n, k) = C(n, n-k)
        k = n - k;

  for (int i = 0; i < k; ++i) // n...n-k / 1...k
  {
     res *= (n - i);
     res /= (i + 1);
  }

  return res;
}</pre>
```

3.9 STL quick reference

3.9.1 Map

```
map<T1, T2> m; // iterable
void clear();
void erase(T1 key);
it find(T1 key); // <key, val>
void insert(pair<T1, T2> P);
T2 &[](T1 key); // if key not in map, new key will be inserted with default val
it lower_bound(T1 key); // = m.end() if not found, *it = <key, val>
it upper_bound(T1 key); // = m.end() if not found, *it = <key, val>
```

3.9.2 Set

```
set<T> s; // iterable
void clear();
size_t count(T val); // number of val in set
```

```
void erase(T val);
it find(T val); // = s.end() if not found
void insert(T val);
it lower_bound(T val); // = s.end() if not found, *it = <key, val>
it upper_bound(T val); // = s.end() if not found, *it = <key, val>
```

3.9.3 Algorithm

```
|| / / return if i is smaller than j
  comp = [&](const T &i, const T &j) -> bool;
  vector<T> v;
  bool any of(v.begin(), v.end(), [&](const T &i) -> bool);
  bool all_of(v.begin(), v.end(), [&](const T &i) -> bool);
  void copy(inp.begin(), in.end(), out.begin());
  int count(v.begin(), v.end(), int val); // number of val in v
  it unique(v.begin(), v.end());
                                          // it - v.begin() = size
  // after calling, v[nth] will be n-th smallest elem in v
  void nth element(v.begin(), nth it, bin comp);
  void merge(in1.begin(), in1.end(), in2.begin(), in2.end(), out.begin(),
        comp);
  // include union, intersection, difference, symmetric difference(xor)
  void set union(in1.begin(), in1.end(), in2.begin(), in2.end(), out.
      begin(), comp);
  bool next permutation(v.begin(), v.end());
| // v1, v2 \text{ need sorted already, whether } v1 \text{ includes } v2
  | bool inclues(v1.begin(), v1.end(), v2.begin(), v2.end());
it find(v.begin(), v.end(), T val); // = v.end() if not found
  it search(v1.begin(), v1.end(), v2.begin(), v2.end());
it lower bound(v.begin(), v.end(), T val);
it upper bound(v.begin(), v.end(), T val);
21 bool binary search(v.begin(), v.end(), T val); // exist in v?
void sort(v.begin(), v.end(), comp);
void stable sort(v.begin(), v.end(), comp);
```

3.9.4 String

3.9.5 Priority Queue

```
bool cmp(ii a, ii b)
{
    if(a.first == b.first)
        return a.second > b.second;
    return b.first > a.first;
}

priority_queue< ii, vector<ii>, function<bool(ii, ii)> > pq(cmp);
```

4 Search

- 4.1 Binary Search
- 4.1.1 Find key
- 4.1.2 Upper / lower Bound
- 4.2 Ternary Search
- 4.3 折半完全列舉
- 4.4 Two-pointer 爬行法
- 5 Basic data structure

5.1 1D BIT

5.2 2D BIT

```
for (int j = b; j <= MAX_M; j += (j & -j))
bit[i][j] += x;
| | }
```

5.3 Union Find

```
|| #define N 20000 // 記得改
   struct UFDS {
       int par[N];
       void init() {
           memset(par, -1, sizeof(par));
       int root(int x) {
           return par[x] < 0 ? x : par[x] = root(par[x]);</pre>
       void merge(int x, int y) {
           x = root(x);
15
           y = root(y);
           if (x != y) {
               if (par[x] > par[y])
                   swap(x, y);
               par[x] += par[y];
21
               par[y] = x;
           }
22
24 }
```

5.4 Segment Tree

5.5 Sparse Table

```
1 struct {
       int sp[MAX_LOG_N][MAX_N]; // MAX_LOG_N = ceil(lg(MAX_N))
       void build(int inp[], int n) {
           for (int j = 0; j < n; j++) {
               sp[0][j] = inp[j];
           for (int i = 1; (1 << i) <= n; i++)
               for (int j = 0; j + (1 << i) <= n; j++)
                   sp[i][j] =
                       \min(\text{sp}[i-1][j], \text{sp}[i-1][j+(1 << (i-1))]);
12
13
14
       int query(int 1, int r) { // [1, r)
16
           int k = floor(log2(r - 1));
           return min(sp[k][1], sp[k][r - (1 << k)]);
19
20 } sptb;
```

6 Dynamic Programming

- 7 Tree
- 7.1 LCA
- 8 Graph
- 8.1 Articulation point / edge
- 8.2 CC
- 8.2.1 BCC vertex
- 8.2.2 BCC edge
- 8.2.3 SCC
- 8.3 Shortest Path
- 8.3.1 Dijkatra
- 8.3.2 Dijkatra (next-to-shortest path)
- 8.3.3 SPFA
- 8.3.4 Bellman-Ford
- 8.3.5 Floyd-Warshall
- 8.4 Kruskal MST
- 8.5 Flow
- 8.5.1 Max Flow (Dinic)
- 8.5.2 Min-Cut
- 8.5.3 Min Cost Max Flow
- 8.5.4 Maximum Bipartite Graph

9 String

9.1 Rolling Hash

- 1. Use two rolling hashes if needed.
- 2. The prime for pre-calculation can be 137 and 257, for modulo can be 1e9+7 and 0xdefaced

```
#define N 1000100
#define B 137
#define M 1000000007

typedef long long l1;

char inp[N];
int len;
11 p[N], h[N];
```

```
void init()
{    // build polynomial table and hash value
    p[0] = 1;    // b to the ith power
    for (int i = 1; i <= len; i++) {
        h[i] = (h[i - 1] * B % M + inp[i - 1]) % M;    // hash value
        p[i] = p[i - 1] * B % M;
}

ll get_hash(int 1, int r) // [1, r] of the inp string array
{
    return ((h[r + 1] - (h[1] * p[r - 1 + 1])) % M + M) % M;
}</pre>
```

9.2 KMP

```
void fail()
       int len = strlen(pat);
       f[0] = 0;
       int j = 0;
       for (int i = 1; i < len; i++) {
           while (j != 0 && pat[i] != pat[j])
               j = f[j - 1];
           if (pat[i] == pat[j])
               j++;
13
           f[i] = j;
  int match()
19
       int res = 0;
       int j = 0, plen = strlen(pat), tlen = strlen(text);
23
       for (int i = 0; i < tlen; i++) {</pre>
24
           while (j != 0 && text[i] != pat[j])
25
               j = f[j - 1];
26
27
           if (text[i] == pat[j]) {
               if (j == plen - 1) { // find match
28
29
                   res++;
30
                    j = f[j];
31
               } else {
                    j++;
34
       }
36
37
       return res;
38
```

9.3 Z Algorithm

9.4 Trie

```
| | #define N 600010
  struct node {
      int child[26];
      bool ending;
 } trie[N];
 8 root is 0
 memset(trie, 0, sizeof(trie));
10 freeNode = 1;
11 */
12 int freeNode;
void insert(string &str, int pos, int node)
      if (pos == (int)str.length()) {
15
16
           trie[node].ending = true;
      } else { // find which way to go
17
           int c = str[pos] - 'a';
           if (trie[node].child[c] == 0) // give a new node
               trie[node].child[c] = freeNode++;
20
           insert(str, pos + 1, trie[node].child[c]);
```

9.5 Suffix Array

10 Geometry

10.1 Template

```
#define x first
#define y second

typedef pair <double , double > pt;

struct line {
    double a, b, c;
    // coefficients in general form, compare up to constant factor
}

pt operator-(pt u, pt v) { return pt(u.x-v.x, u.y-v.y); }

pt operator+(pt u, pt v) { return pt(u.x+v.x, u.y+v.y); }

pt operator*(pt u, double d) { return pt(u.x*d, u.y*d); }

double operator*(pt u, pt v) { return u.x*v.x + u.y*v.y); } // dot
    product double operator!(pt p) { return sqrt(p*p); } // norm

double operator^(pt u, pt v) { return u.x*v.y - u.y*v.x; } // cross
    product
```

- 10.1.1 Point / Line
- 10.1.2 Intersection
- 10.2 Half-plane intersection
- 10.3 Convex Hull