

# Getting started with CGAL Polyhedron

## the example of subdivision surfaces

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### Abstract

This document is a tutorial on how to get started with the halfedge data structure provided by CGAL, the Computational Geometry Algorithm Library. Assuming the reader to be familiar with the C++ template mechanisms and the key concepts of the STL (Standard Template Library), we describe three different approaches with increasing level of sophistication for implementing mesh subdivision schemes. The simplest approach uses simple Euler operators to implement the  $\sqrt{3}$  subdivision scheme applicable to triangle meshes. A second approach overloads the incremental builder already provided by CGAL to implement the quad-triangle subdivision scheme applicable to polygon meshes. The third approach is generic and offers a convenient way to design its own subdivision scheme through the definition of rule templates. Catmull-Clark, Loop and Doo-Sabin schemes are illustrated using the latter approach. Two companion applications, one developed on Windows with MS .NET, MFC and OpenGL, and the other developed for both Linux and Windows with Qt and OpenGL, implement the subdivision schemes listed above, as well as several functionalities for interaction, visualization and raster/vectorial output.

**Keywords:** CGAL library, tutorial, halfedge data structure, polygon surface mesh, subdivision surfaces, quad-triangle,  $\sqrt{3}$ , Loop, Doo-Sabin, Catmull-Clark, OpenGL.

## 1 Introduction

The CGAL library is a joint effort between nine European institutes [FGK<sup>+</sup>00]. The goal of CGAL is to make available to users in industry and academia some efficient solutions to basic geometric problems developed in the area of computational geometry in a C++ software library.

CGAL features a 3D polygon surface mesh data structure based on the concept of halfedge data structure [Ket99], which has been very successful for the design of general algorithms on meshes. In this document we provide a tutorial to get started with CGAL Polyhedron data structure through the example of subdivision surfaces. We also offer an application both under windows and linux, featuring an OpenGL-based viewer, an arcball for interaction and two ways (raster and vectorial) to produce pictures and illustrations.

The main targeted audience is a master or a Ph.D. student in computer graphics or computational geometry, aiming at doing some research on mesh processing algorithms. We hope this tutorial will convince the reader :

- not reinventing the wheel. Taking some time choosing the “right tool” is often worth it. This may be true, even for a short project;

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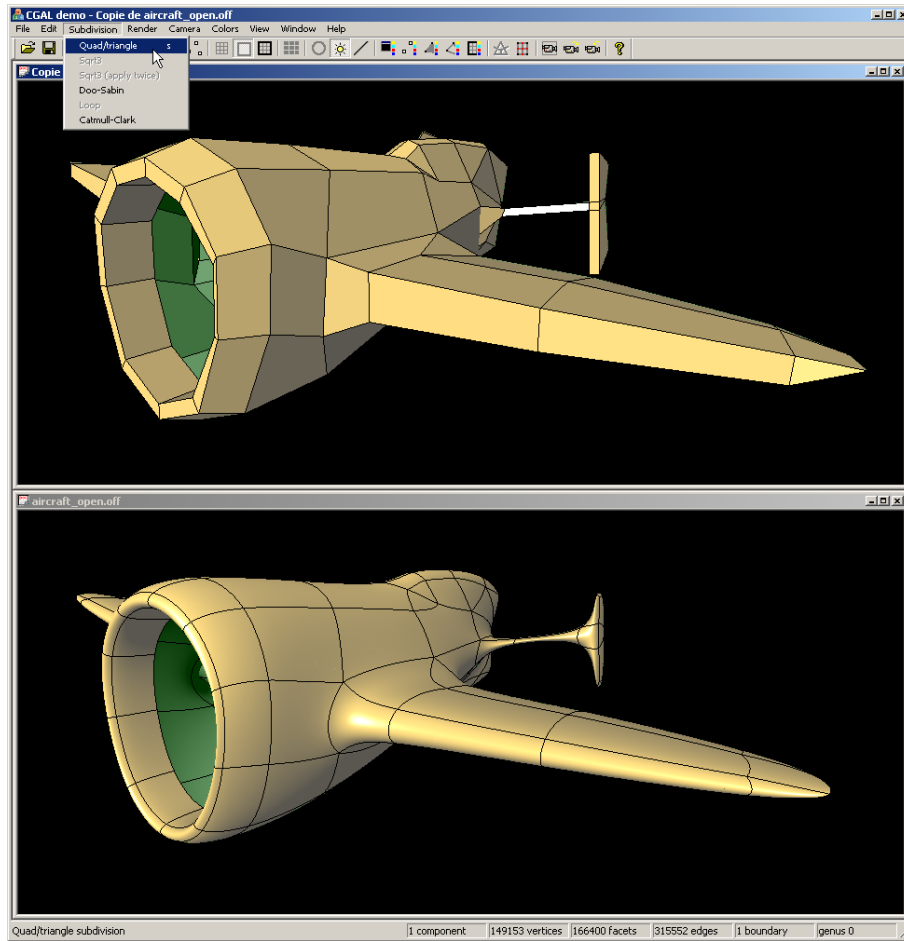


Figure 1 – Snapshot taken from the tutorial application running on Windows. A polygon mesh is subdivided using the quad-triangle subdivision scheme [SL02].

- using an optimized and robust library to ease the implementation and obtain fast and robust results. This allows focusing on the elaborated algorithm, not on the underlying data structure;
- using generic programming to reuse existing data structures and algorithms;
- using a standard library in order to benefit from existing support and discussion groups<sup>1</sup>.

## 2 Prerequisites

Before using CGAL, it is mandatory to be familiar with C++ and the *generic programming paradigm*. The latter features the notion of C++ class templates and function templates, which is at the corner stone of all features provided by CGAL.

<sup>1</sup>see the cgal discuss list: [http://www.cgal.org/user\\_support.html](http://www.cgal.org/user_support.html).

An example illustrating generic programming is the Standard Template Library (STL) [MS96]. Generality and flexibility is achieved with a set of *concepts*, where a concept is a well defined set of requirements. One of them is the *iterator* concept, which allows both referring to an item and traversing a sequence of items. Those items are stored in a data structure called *container* in STL. Another concept, so-called *circulator*, allows traversing some circular sequences. They share most of the requirements with iterators, except the lack of past-the-end position in the sequence. Since CGAL is strongly inspired from the genericity of STL, it is important to become familiar with its concepts before starting using it.

## 2.1 Subdivision Surfaces

Since this tutorial is centered at the design and implementation of subdivision surfaces, a short non-theoretic introduction of subdivision surfaces is given in this section. We are going to focus on the various refinement schemes and the connectivity properties. A complete review on subdivisions can be found at [?].

A subdivision surface is the limit surface resulted from the application of a subdivision algorithm to a control mesh (Figure 1). The subdivision algorithm recursively *refine* (subdivide) the control mesh and *modify* (smooth) the geometry. A subdivision algorithm can be characterized by a *refinement operator* and a *modification operator*.

Refinement operators edit the connectivity and create a uniformly refined mesh from the source mesh. These operators can be classified according to the refinement patterns. Figure ?? shows four major patterns employed in subdivision algorithms. Examples are Catmull-Clark subdivision (PQQ) [?], Loop subdivision (PTQ) [?], Doo-Sabin subdivision (DQQ) [?] and  $\sqrt{3}$  subdivision [?]. Subdivisions may employ a combination of two patterns. Examples are Stam QT subdivision [?] and 4-3 subdivision [?] (PQQ and PTQ).

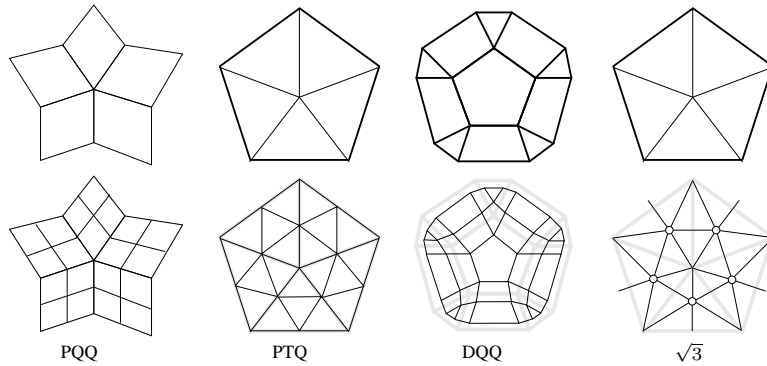


Figure 2 – Refinement schemes: primal quadrilateral quadrisection (PQQ), primal triangle quadrisection (PTQ), dual quadrilateral quadrisection (DQQ) and  $\sqrt{3}$  refinement.

Modification operators collect a submesh of the source mesh and applied a stencil on the submesh to generate the corresponding vertex of the refined mesh. Figure 3 demonstrates the examples of the correspondence between a source submesh and its target vertices.

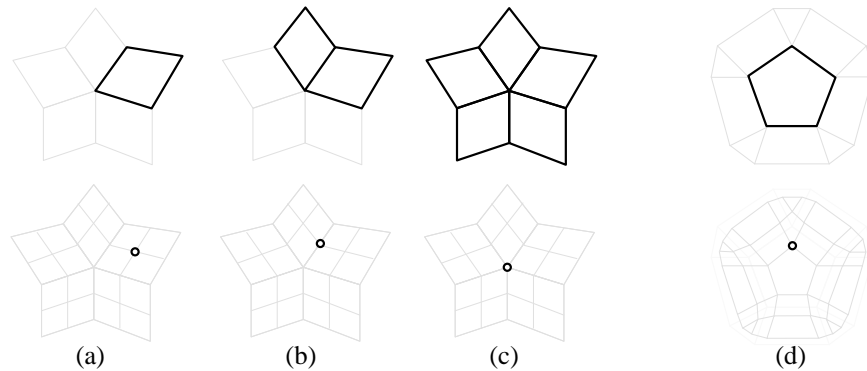


Figure 3 – The correspondence of the source submesh and the target vertex in the Catmull-Clark subdivision (a-c) and Doo-Sabin subdivision (d).

## 3 Polyhedron Data Structure: Fundamentals

### 3.1 Halfedge data structure

The specification of a polygon surface mesh consists of combinatorial entities: vertices, edges, and faces, and numerical quantities: attributes such as vertex positions, vertex normals, texture coordinates, face colors, etc. The *connectivity* describes the incidences between elements and is implied by the topology of the mesh. For example, two vertices or two faces are adjacent if there exists an edge incident to both.

A *halfedge data structure* is an edge-centered data structure capable of maintaining incidence informations of vertices, edges and faces, for example for planar maps, polyhedra, or other orientable, two-dimensional surfaces embedded in arbitrary dimension. Each edge is decomposed into two halfedges with opposite orientations. One incident face and one incident vertex are stored in each halfedge. For each face and each vertex, one incident halfedge is stored (see Fig.4).

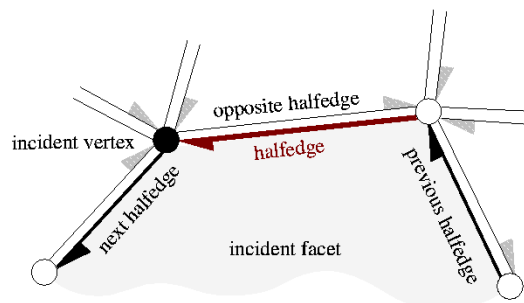


Figure 4 – One halfedge and its incident primitives.

Notice that the halfedge data structure is only a combinatorial data structure, geometric interpretation being added by classes built on top of the halfedge data structure. On example is the class `CGAL::Polyhedron_3` used in this tutorial. The halfedge data structure has been very successful for the design of algorithms on meshes for several reasons:

- an edge-based data structure leads to a constant size structure, contrary to face-based data structures with inevitable variable topological structure when dealing with arbitrary vertex valence and face degrees.

- a halfedge encodes the orientation of an edge, facilitating the mesh traversal.
- navigation around each vertex by visiting all surrounding edges or faces is made easy.
- each halfedge can be associated with a unique corner, that is a couple {face,vertex}. The storage of attributes such as normals or texture coordinates per corner (instead of per vertex) is thus allowed.

## 3.2 Polyhedron Data Structure

The class `Polyhedron_3` can represent polygon meshes<sup>2</sup>. Its underlying combinatorial component is based on the halfedge data structure. As all CGAL geometric entities, its geometric component is templated by the *kernel*<sup>3</sup>.

### 3.2.1 Declaration

The simplest declaration of the polyhedron (without extended primitives) consists of templating with a cartesian kernel and double number precision:

```
// instantiation of a polyhedron

#include <CGAL/Cartesian.h>
#include <CGAL/Polyhedron_3.h>

typedef CGAL::Cartesian<double>    kernel;
typedef CGAL::Polyhedron_3<kernel> Polyhedron;

Polyhedron p;
```

### 3.2.2 Extending primitives

The polyhedron can be parameterized by a *traits* class in order to extend the vertex, halfedge and facet primitives. In this tutorial all primitives (facets, halfedges and vertices) are extended. The facet is extended with a normal and with a general-purpose integer tag:

```
template <class Refs, class T, class P, class Norm>
class Enriched_facet :
    public CGAL::HalfedgeDS_face_base<Refs, T>
{
    // tag
    int m_tag;

    // normal
    Norm m_normal;

public:

    // no constructors to repeat, since only
    // default constructor mandatory
    Enriched_facet()
    {
    }

    // tag
    const int& tag() { return m_tag; }
    void tag(const int& t) { m_tag = t; }

    // normal
    typedef Norm Normal_3;
    Normal_3& normal() { return m_normal; }
    const Normal_3& normal() const { return m_normal; }
};
```

---

<sup>2</sup><http://www.cgal.org>

<sup>3</sup>CGAL kernel

The halfedge is extended with a general-purpose tag and a binary tag to indicate whether it belongs to the control mesh or not. The latter tag is used to superimpose the control mesh as shown in Fig.1.

```
template <class Refs, class Tprev, class Tvertex,
          class Tface, class Norm>
class Enriched_halfedge : public
    CGAL::HalfedgeDS_halfedge_base<Refs,Tprev,Tvertex,Tface>
{
private:

    // tag
    int m_tag;

    // option for control edge superimposing
    bool m_control_edge;

public:

    // life cycle
    Enriched_halfedge()
    {
        m_control_edge = true;
    }

    // tag
    const int& tag() const { return m_tag; }
    int& tag() { return m_tag; }
    void tag(const int& t) { m_tag = t; }

    // control edge
    bool& control_edge() { return m_control_edge; }
    const bool& control_edge() const { return m_control_edge; }
    void control_edge(const bool& flag) { m_control_edge = flag; }
};
```

The vertex is extended with a normal and a general-purpose integer tag:

```
template <class Refs, class T, class P, class Norm>
class Enriched_vertex :
    public CGAL::HalfedgeDS_vertex_base<Refs, T, P>
{
    // tag
    int m_tag;

    // normal
    Norm m_normal;

public:
    // life cycle
    Enriched_vertex() {}
    // repeat mandatory constructors
    Enriched_vertex(const P& pt)
        : CGAL::HalfedgeDS_vertex_base<Refs, T, P>(pt)
    {
    }

    // normal
    typedef Norm Normal_3;
    Normal_3& normal() { return m_normal; }
    const Normal_3& normal() const { return m_normal; }

    // tag
    int& tag() { return m_tag; }
    const int& tag() const { return m_tag; }
    void tag(const int& t) { m_tag = t; }
};
```

A redefined items class for the polyhedron uses the class wrapper mechanism to embed all three extended primitives within one unique class.

```
struct Enriched_items : public CGAL::Polyhedron_items_3
{
    // wrap vertex
    template <class Refs, class Traits>
    struct Vertex_wrapper
    {
        typedef typename Traits::Point_3 Point;
        typedef typename Traits::Vector_3 Normal;
        typedef Enriched_vertex<Refs,
                               CGAL::Tag_true,
                               Point,
                               Normal> Vertex;

    };

    // wrap face
    template <class Refs, class Traits>
    struct Face_wrapper
    {
        typedef typename Traits::Point_3 Point;
        typedef typename Traits::Vector_3 Normal;
        typedef Enriched_facet<Refs,
                               CGAL::Tag_true,
                               Point,
                               Normal> Face;

    };

    // wrap halfedge
    template <class Refs, class Traits>
    struct Halfedge_wrapper
    {
        typedef typename Traits::Vector_3 Normal;
        typedef Enriched_halfedge<Refs,
                                   CGAL::Tag_true,
                                   CGAL::Tag_true,
                                   CGAL::Tag_true,
                                   Normal> Halfedge;

    };
};
```

The trait class is then used for templating a polyhedron *Enriched\_polyhedron*:

```
template <class kernel, class items>
class Enriched_polyhedron :
    public CGAL::Polyhedron_3<kernel,items>
{
    //...
};
```

The corresponding instantiation of an enriched polyhedron follows:

```
#include <CGAL/Simple_cartesian.h>
#include "enriched_polyhedron.h"

typedef double number_type;
typedef CGAL::Simple_cartesian<number_type> kernel;

Enriched_polyhedron<kernel,Enriched_items> polyhedron;
```

### 3.2.3 Iteration and Circulation

The *iterator* STL concept allows traversing a sequence of items. This concept is applied to the primitives of a mesh, be they halfedges, edges, vertices, facets or points. Notice that the order of iteration is not dictated by any incidence relationship, contrary to the circulator. The following example shows how to iterate on the mesh vertices.

```

Vertex_iterator iter;
for(iter = polyhedron.vertices_begin();
    iter != polyhedron.vertices_end();
    iter++)
{
    Vertex_handle hVertex = iter;
    // do something with hVertex
}

```

The *circulator* STL concept allows traversing a circular sequence of items. This concept is applied both inside facets and around vertices.

**Circulating around a facet** The facets being defined by the circular sequence of halfedges along their boundary, this calls for a circulator around a facet. The convention is that the halfedges are oriented counterclockwise around facets as seen from the outside of the polyhedron (see Fig.5, left).

```

// circulate around hFacet
Halfedge_around_facet_circulator circ = hFacet->facet_begin();
Halfedge_around_facet_circulator end = circ;
CGAL_For_all(circ,end)
{
    Halfedge_handle hHalfedge = circ;
    // do something with hHalfedge
}

```

**Circulating around a vertex** The convention being that the halfedges are oriented counterclockwise around facets as seen from the outside of the polyhedron, this implies that the halfedges are oriented clockwise around the vertices (see Fig.5, right).

```

// circulate around hVertex
Halfedge_around_vertex_circulator circ = hVertex->vertex_begin();
Halfedge_around_vertex_circulator end = circ;
CGAL_For_all(circ,end)
{
    Halfedge_handle hHalfedge = circ;
    // do something with hHalfedge
}

```

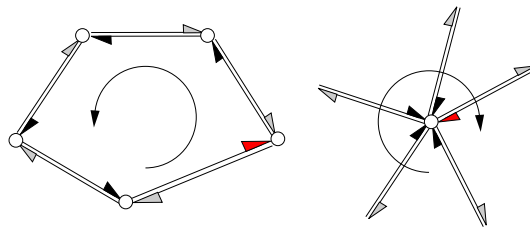


Figure 5 – Left: circulation around a facet (ccw). Right: circulation around a vertex (cw).

### 3.3 Connectivity Editing

#### 3.3.1 Connectivity Operators

The polyhedron provides a series of atomic operators to modify the connectivity of the polyhedral surface:

- split or join of two facets,
- split or join of two vertices,
- split or join of two loops,



- split of an edge.

Furthermore, more operators are provided to work with surfaces with boundaries, to create or delete holes, add a facet to the border, etc. We refer to the references manual for precise definitions and illustrative figures<sup>4</sup>.

### 3.3.2 Incremental Builder

The utility class `Polyhedron_incremental_builder_3` helps in creating polyhedral surfaces from a list of points followed by a list of facets that are represented as indices into the point list. This is particularly useful for implementing file reader for common file formats. In Section 4.2, we use the incremental builder to implement the quad-triangle subdivision scheme.

In the following example, the incremental builder is used to create a simple triangle. `Build_triangle` is such a function object derived from `Modifier_base<HalfedgeDS>`. The `delegate()` member function of the polyhedron accepts this function object and calls its `operator()` with a reference to its internally used halfedge data structure. Thus, this member function in `Build_triangle` can create the triangle in the halfedge data structure.

```
// examples/Polyhedron/polyhedron_prog_incr_builder.C

#include <CGAL/Cartesian.h>
#include <CGAL/Polyhedron_incremental_builder_3.h>
#include <CGAL/Polyhedron_3.h>

// A modifier creating a triangle with
// the incremental builder.

template <class HDS>
class Build_triangle
: public CGAL::Modifier_base<HDS>
{
public:
    Build_triangle() {}

    void operator()(HDS& hds)
    {
        // Postcondition: 'hds' is a valid polyhedral surface.
        CGAL::Polyhedron_incremental_builder_3<HDS> B(hds, true);
        B.begin_surface(3, 1, 6);
        typedef typename HDS::Vertex    Vertex;
        typedef typename Vertex::Point Point;
        B.add_vertex(Point(0, 0, 0));
        B.add_vertex(Point(1, 0, 0));
        B.add_vertex(Point(0, 1, 0));
        B.begin_facet();
        B.add_vertex_to_facet(0);
        B.add_vertex_to_facet(1);
        B.add_vertex_to_facet(2);
        B.end_facet();
        B.end_surface();
    }
};

typedef CGAL::Cartesian<double>      Kernel;
typedef CGAL::Polyhedron_3<Kernel>   Polyhedron;
typedef Polyhedron::HalfedgeDS       HalfedgeDS;

Polyhedron P;
Build_triangle<HalfedgeDS> triangle;
P.delegate(triangle);
CGAL_assertion(P.is_triangle(P.halfedges_begin()));
```

---

<sup>4</sup>See [Euler operators](#)

## 4 Design and Implementation of Subdivisions

### 4.1 $\sqrt{3}$ -Subdivision using Euler Operators

The  $\sqrt{3}$  subdivision scheme was introduced by Kobbelt [Kob00]. It takes as input a triangle mesh and subdivides each facet into three triangles by splitting it at its centroid. Next, all edges of the initial mesh are flipped so that they join two adjacent centroids. Finally, each initial vertex is replaced by a barycentric combination of its neighbors. An example of one step of the  $\sqrt{3}$  subdivision scheme is shown in Fig.6, and an example of several steps is shown in Fig.7.

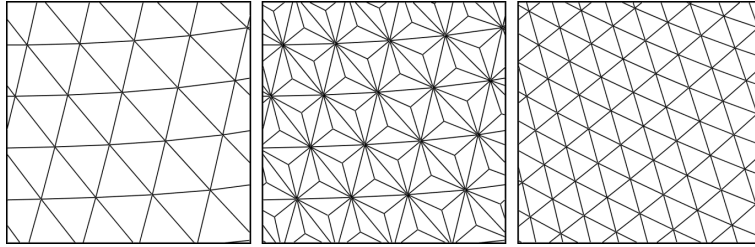


Figure 6 – The  $\sqrt{3}$ -Subdivision scheme is decomposed as a set of Euler operators: face splits and edge flips.

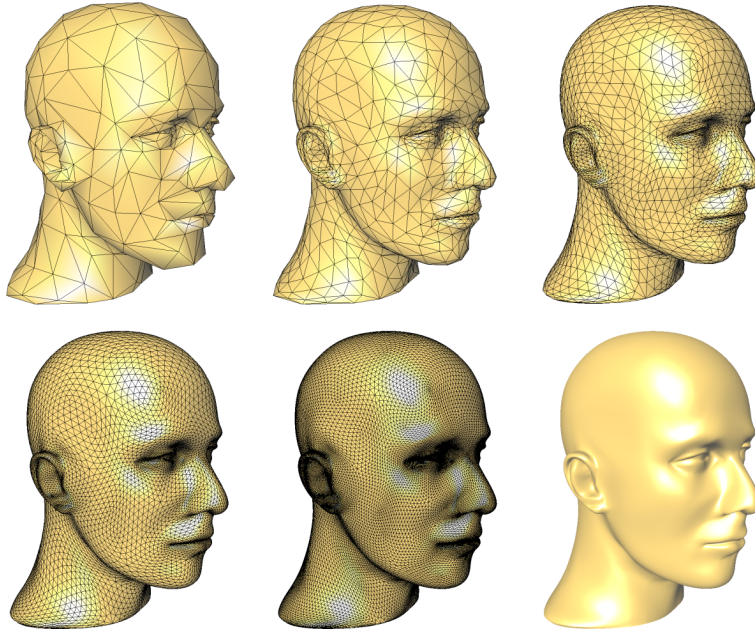


Figure 7 –  $\sqrt{3}$ -Subdivision of the mannequin mesh.

## 4.2 Quad-triangle Subdivision using Incremental Builder

The quad-triangle subdivision scheme was introduced by Levin [Lev03], then Stam and Loop [SL02]. It applies to polygon meshes and basically features Loop subdivision on triangles and Catmull-Clark subdivision on polygons of the control mesh (see Fig.8). After one iteration of subdivision the subdivided model is only composed of triangles and quads. A simple solution for implementing such a scheme is to use the *incremental builder* concept featured by CGAL Polyhedron (see Section 3.3.2).

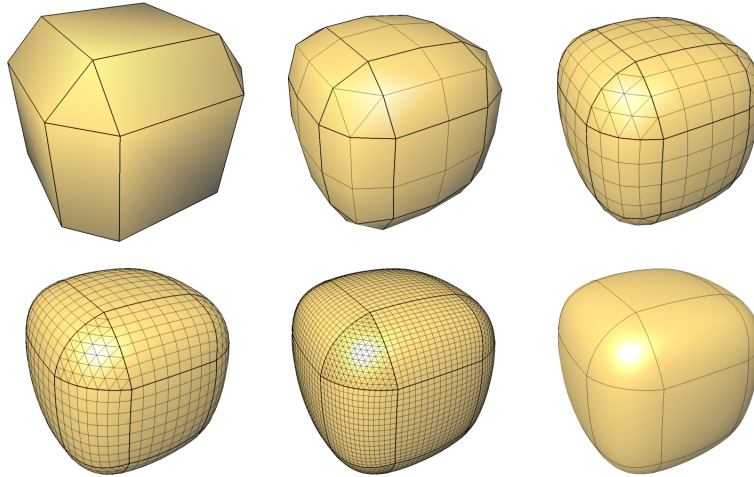


Figure 8 – *Quad-triangle subdivision scheme.*

### Subdivision engine

```
#include "enriched_polyhedron.h"
#include "builder.h"

template <class HDS, class Polyhedron, class kernel>
class CModifierQuadTriangle : public CGAL::Modifier_base<HDS>
{
private:
    typedef ...

    Polyhedron *m_pMesh;

public:
    // life cycle
    CModifierQuadTriangle(Polyhedron *pMesh)
    {
        CGAL_assertion(pMesh != NULL);
        m_pMesh = pMesh;
    }
    ~CModifierQuadTriangle() {}

    // subdivision
    void operator()( HDS& hds)
    {
        builder B(hds, true);
        B.begin_surface(3, 1, 6);
        add_vertices(B);
        add_facets(B);
        B.end_surface();
    }
}
```

```

private:

    // ...
    // for the complete implementation of the subdivision,
    // readers should refer to the accompanied source codes of
    // this tutorial.

};

template <class Polyhedron, class kernel>
class CSubdivider_quad_triangle
{
public:
    typedef typename Polyhedron::HalfedgeDS HalfedgeDS;

public:
    // life cycle
    CSubdivider_quad_triangle() {}
    ~CSubdivider_quad_triangle() {}

public:
    void subdivide(Polyhedron &OriginalMesh,
                  Polyhedron &NewMesh,
                  bool smooth_boundary = true)
    {
        CModifierQuadTriangle<HalfedgeDS, Polyhedron, kernel>
            builder(&OriginalMesh);

        // delegate construction
        NewMesh.delegate(builder);

        // smooth
        builder.smooth(&NewMesh, smooth_boundary);
    }
};

```

### 4.3 Subdivision using a rule template

We use Catmull-Clark (CC) subdivision as our first example (see Figure 9). CC subdivision can be defined as the combination of the primal quadrilateral quadrisection (PQQ) scheme and the Catmull-Clark geometry rules.

```

template <class Polyhedron, template <class> Rule>
void PrimalQuadQuadralize(Polyhedron& p, Rule<Polyhedron>& r) { ...}

template <class Polyhedron>
void CCSubdivision(Polyhedron& p) {
    PrimalQuadQuadralize(p, CatmullClarkRule<Polyhedron>());
}

```

For meshes based on PQQ scheme, the footprints of the range vertices each corresponds to a topology primitive, i.e. vertex, edge or facet, in the domain (see Figure. ??). The policy class hence needs to provide the policy functions in each case.

```

template <class P> class CatmullClarkRule
{
public:
    typedef P Polyhedron;
    typedef typename Polyhedron::Vertex_handle Vertex_handle;
    typedef typename Polyhedron::Halfedge_handle Halfedge_handle;
    typedef typename Polyhedron::Facet_handle Facet_handle;

    void face_vertex_rule(Facet_handle domain_f, Vertex_handle range_v);
    void edge_vertex_rule(Halfedge_handle domain_e, Vertex_handle range_v);
    void vertex_vertex_rule(Vertex_handle domain_v, Vertex_handle range_v);
};

```

Each policy function has two input parameters: the domain primitive and the range vertex. The footprint, defined as the vertices set of the 1-distance neighbors of the corresponding domain primitive, is passed as

the handle of the primitive. Employing the incidental function of the halfedge data structure, the policy designer works on the simple view of the *local* mesh corresponding to the footprint. Following codes demonstrate the facet-vertex case.

```
void facet_vertex_rule(Facet_handle domain_f, Vertex_handle& range_v)
{
    typedef typename Polyhedron::Point_3 Point;

    Halfedge_around_facet_circulator hcir = domain_f->facet_begin();
    Halfedge_around_facet_circulator hcir_end = hcir;
    range_v->point() = Point(0,0,0);
    do
        range_v->point() += hcir->vertex()->point();
    while (++hcir != hcir_end);

    range_v->point() /= circulator_size(hcir);
}
```

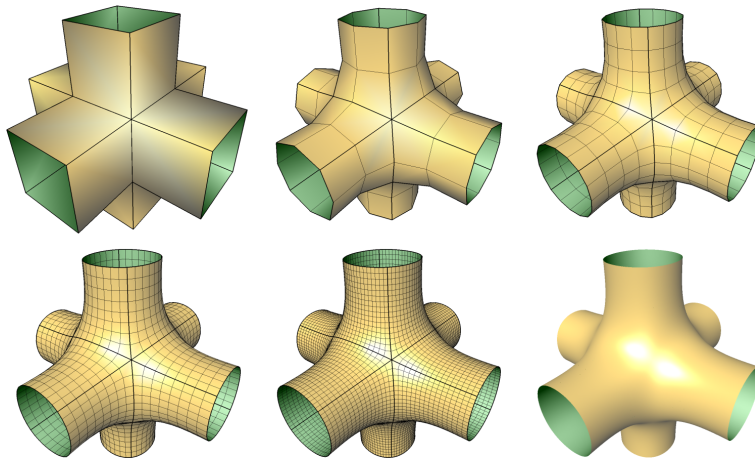


Figure 9 – Catmull-Clark subdivision of a quadrilateral control mesh.

Loop subdivision uses similar refinement scheme to PQQ scheme except that it works on the triangle mesh. Hence the footprints of Loop scheme are same as the CC scheme but without the facet-vertex case.

```
PrimalTriangleQuadralize(p, LoopRule<Polyhedron>());

template <class Polyhedron>
void LoopSubdivision(Polyhedron& p)
{
    PrimalTriangleQuadralize(p, LoopRule<Polyhedron>());
}

template <class P> class LoopRule
{
public:
    typedef ...

    void edge_vertex_rule(Halfedge_handle domain_e, Vertex_handle range_v);
    void vertex_vertex_rule(Vertex_handle domain_v, Vertex_handle range_v);
};
```

Doo-Sabin (DS) subdivision is fundamentally different from the primal subdivision schemes in the aspect of the footprints. As showed in Figure ??, each range vertex corresponds to a *corner* in the domain mesh. The footprint of the range vertex is the facet containing the corner.

```
DualQuadQuadralize(p, DooSabinRule<Polyhedron>());
```

```

template <class Polyhedron>
void DSSubdivision(Polyhedron& p)
{
    DualQuadQuadralize(p, DooSabinRule<Polyhedron>());
}

template <class P> class DooSabinRule
{
public:
    typedef ...

    void corner_vertex_rule(Halfedge_handle domain_e, Vertex_handle range_v);
};

```

The only policy function for the DS subdivision has the halfedge pointing to the corner as the domain parameter. A demo of policy function for the regular facet, i.e. the quadrilateral facet, is listed in the following codes.

```

void corner_vertex__rule(Halfedge_handle domain_e, Vertex_handle range_v)
{
    range_v->point() = Point(0,0,0);

    range_v->point() = domain_e->vertex()->point() * 9 +
        (domain_e->next()->vertex()->point() +
         domain_e->pre()->vertex()->point()) * 3 +
        domain_e->next()->next()->vertex()->point();

    range_v->point() /= 16.0;
}

```

For the complete implementation of the subdivision, readers should refer to the accompanied source codes of this tutorial.

## 5 Application demo

The application demo runs on windows and features:

- A standard document-view architecture. Accepted file formats are ASCII off and obj (1-based vertex indices for the latter).
- An OpenGL-based viewer.
- An arcball for interaction.
- One menu dedicated to subdivision algorithms (shortcut 's' for quad-triangle scheme).
- Some rendering options accesible through the menu render or through the shortcut 'r'. Note that superimposing the control edges during subdivision is only available for the quad-triangle subdivision scheme.
- A 24-bits raster image output to the clipboard (short-cut ctrl+c),
- A vectorial output to an .eps file (menu file/dump to eps), editable with *e.g.*, Adobe Illustrator.
- One functionality to display two models with the same viewpoint (copy and paste viewpoint).

### 5.1 Compiling on Windows

The application has been compiled on MS .NET 2003 using CGAL 3.0, OpenGL and MFC. The following steps are necessary to compile:

- Install CGAL 3.0.
- Define an environment variable CGAL3 with the path to the CGAL-3.0 folder.

- Compile the CGAL library in multithread mode and name the output libraries resp. `cgal_mt_debug.lib` and `cgal_mt_release.lib` for resp. the debug and the release mode.
- Check your path to the library in the MS .NET project properties.
- Rebuild all.

## References

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