

The Open Source CFD Toolbox

Programmer's Guide

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Contents

C	opyri	ght Notice	P-2
G	1. A 2. V 3. C 4. M 5. C 6. C 7. A 8. T 9. T	Free Documentation Licence PPLICABILITY AND DEFINITIONS ERBATIM COPYING OPYING IN QUANTITY ODIFICATIONS OMBINING DOCUMENTS OLLECTIONS OF DOCUMENTS GGREGATION WITH INDEPENDENT WORKS PRANSLATION ERMINATION FUTURE REVISIONS OF THIS LICENSE	P-3 P-3 P-4 P-4 P-5 P-6 P-7 P-7 P-7
Tr	ader	narks	P-9
C	onter	nts	P-11
1	Ten 1.1 1.2 1.3	Coordinate system Tensors 1.2.1 Tensor notation Algebraic tensor operations 1.3.1 The inner product 1.3.2 The double inner product of two tensors 1.3.3 The triple inner product of two third rank tensors 1.3.4 The outer product 1.3.5 The cross product of two vectors 1.3.6 Other general tensor operations 1.3.7 Geometric transformation and the identity tensor 1.3.8 Useful tensor identities 1.3.9 Operations exclusive to tensors of rank 2 1.3.10 Operations exclusive to scalars	P-15 P-15 P-17 P-17 P-17 P-18 P-19 P-19 P-19 P-20 P-20 P-21 P-21 P-22
	1.4	OpenFOAM tensor classes	P-23 P-23 P-25
2	Disc 2.1	Cretisation procedures Differential operators	P-27 P-27 P-27

P-12 Contents

		2.1.3	Curl
		2.1.4	Laplacian
		2.1.5	Temporal derivative
	2.2	Overvi	iew of discretisation
		2.2.1	OpenFOAM lists and fields
	2.3	Discre	tisation of the solution domain
		2.3.1	Defining a mesh in OpenFOAM
		2.3.2	Defining a geometricField in OpenFOAM
	2.4	Equati	ion discretisation
		2.4.1	The Laplacian term
		2.4.2	The convection term
		2.4.3	First time derivative
		2.4.4	Second time derivative
		2.4.5	Divergence
		2.4.6	Gradient
		2.4.7	Grad-grad squared
		2.4.8	Curl
		2.4.9	Source terms
			Other explicit discretisation schemes
	2.5		oral discretisation
	2.0	2.5.1	
	2.6		lary Conditions
	2.0	2.6.1	Physical boundary conditions
		2.0.1	Triplical boundary conditions
3	Exa	mples	of the use of OpenFOAM
	3.1	Flow a	around a cylinder
		3.1.1	Problem specification
		3.1.2	Note on potentialFoam
		3.1.3	Mesh generation
		3.1.4	Boundary conditions and initial fields
		3.1.5	Running the case
	3.2		y turbulent flow over a backward-facing step
	0.2	3.2.1	Problem specification
		3.2.2	Mesh generation
		3.2.3	Boundary conditions and initial fields
		3.2.4	Case control
		3.2.4	Running the case and post-processing
	3.3		sonic flow over a forward-facing step
	5.0	3.3.1	Problem specification
		3.3.2	Mesh generation
		3.3.2	Running the case
	9 4	3.3.4	Exercise
	3.4		pression of a tank internally pressurised with water
		3.4.1	Problem specification
		3.4.2	Mesh Generation
		3.4.3	Preparing the Run
		3.4.4	Running the case
		3.4.5	Improving the solution by refining the mesh
	3.5	_	etohydrodynamic flow of a liquid
		3.5.1	Problem specification
		3.5.2	Mesh generation

Contents			P-13
	3.5.3	Running the case	P-70
Index			P-73

P-14 Contents

Chapter 1

Tensor mathematics

This Chapter describes tensors and their algebraic operations and how they are represented in mathematical text in this book. It then explains how tensors and tensor algebra are programmed in OpenFOAM.

1.1 Coordinate system

OpenFOAM is primarily designed to solve problems in continuum mechanics, *i.e.* the branch of mechanics concerned with the stresses in solids, liquids and gases and the deformation or flow of these materials. OpenFOAM is therefore based in 3 dimensional space and time and deals with physical entities described by tensors. The coordinate system used by OpenFOAM is the right-handed rectangular Cartesian axes as shown in Figure 1.1. This system of axes is constructed by defining an origin O from which three lines are drawn at right angles to each other, termed the Ox, Oy, Oz axes. A right-handed set of axes is defined such that to an observer looking down the Oz axis (with O nearest them), the arc from a point on the Ox axis to a point on the Oy axis is in a clockwise sense.

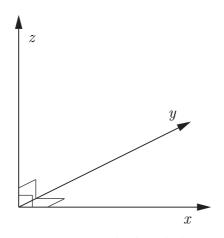


Figure 1.1: Right handed axes

1.2 Tensors

The term tensor describes an entity that belongs to a particular space and obeys certain mathematical rules. Briefly, tensors are represented by a set of *component values* relating to a set of unit base vectors; in OpenFOAM the unit base vectors \mathbf{i}_x , \mathbf{i}_y and \mathbf{i}_z are

P-16 Tensor mathematics

aligned with the right-handed rectangular Cartesian axes x, y and z respectively. The base vectors are therefore orthogonal, i.e. at right-angles to one another. Every tensor has the following attributes:

Dimension d of the particular space to which they belong, *i.e.* d = 3 in OpenFOAM;

Rank An integer $r \geq 0$, such that the number of component values $= d^r$.

While OpenFOAM 1.x is set to 3 dimensions, it offers tensors of ranks 0 to 3 as standard while being written in such a way to allow this basic set of ranks to be extended indefinitely. Tensors of rank 0 and 1, better known as scalars and vectors, should be familiar to readers; tensors of rank 2 and 3 may not be so familiar. For completeness all ranks of tensor offered as standard in OpenFOAM 1.x are reviewed below.

- Rank 0 'scalar' Any property which can be represented by a single real number, denoted by characters in italics, e.g. mass m, volume V, pressure p and viscosity μ .
- **Rank 1 'vector'** An entity which can be represented physically by both magnitude and direction. In component form, the vector $\mathbf{a} = (a_1, a_2, a_3)$ relates to a set of Cartesian axes x, y, z respectively. The *index notation* presents the same vector as a_i , i = 1, 2, 3, although the list of indices i = 1, 2, 3 will be omitted in this book, as it is intuitive since we are always dealing with 3 dimensions.
- Rank 2 'tensor' or second rank tensor, T has 9 components which can be expressed in array notation as:

$$\mathbf{T} = T_{ij} = \begin{pmatrix} T_{11} & T_{12} & T_{13} \\ T_{21} & T_{22} & T_{23} \\ T_{31} & T_{32} & T_{33} \end{pmatrix}$$
(1.1)

The components T_{ij} are now represented using 2 indices since r=2 and the list of indices i, j=1,2,3 is omitted as before. The components for which i=j are referred to as the diagonal components, and those for which $i \neq j$ are referred to as the off-diagonal components. The *transpose* of **T** is produced by exchanging components across the diagonal such that

$$\mathbf{T}^{\mathrm{T}} = T_{ji} = \begin{pmatrix} T_{11} & T_{21} & T_{31} \\ T_{12} & T_{22} & T_{32} \\ T_{13} & T_{23} & T_{33} \end{pmatrix}$$
(1.2)

Note: a rank 2 tensor is often colloquially termed 'tensor' since the occurrence of higher order tensors is fairly rare.

- **Symmetric rank 2** The term 'symmetric' refers to components being symmetric about the diagonal, *i.e.* $T_{ij} = T_{ji}$. In this case, there are only 6 independent components since $T_{12} = T_{21}$, $T_{13} = T_{31}$ and $T_{23} = T_{32}$. OpenFOAM distinguishes between symmetric and non-symmetric tensors to save memory by storing 6 components rather than 9 if the tensor is symmetric. Most tensors encountered in continuum mechanics are symmetric.
- **Rank 3** has 27 components and is represented in index notation as P_{ijk} which is too long to represent in array notation as in Equation 1.1.
- **Symmetric rank 3** Symmetry of a rank 3 tensor is defined in OpenFOAM to mean that $P_{ijk} = P_{ikj} = P_{jik} = P_{jki} = P_{kij} = P_{kji}$ and therefore has 10 independent components. More specifically, it is formed by the outer product of 3 identical vectors, where the outer product operation is described in Section 1.3.4.

1.2.1 Tensor notation

This is a book on computational continuum mechanics that deals with problems involving complex PDEs in 3 spatial dimensions and in time. It is vital from the beginning to adopt a notation for the equations which is compact yet unambiguous. To make the equations easy to follow, we must use a notation that encapsulates the idea of a tensor as an entity in the own right, rather than a list of scalar components. Additionally, any tensor operation should be perceived as an operation on the entire tensor entity rather than a series of operations on its components.

Consequently, in this book the *tensor notation* is preferred in which any tensor of rank 1 and above, *i.e.* all tensors other than scalars, are represented by letters in bold face, *e.g.* a. This actively promotes the concept of a tensor as a entity in its own right since it is denoted by a single symbol, and it is also extremely compact. The potential drawback is that the rank of a bold face symbol is not immediately apparent, although it is clearly not zero. However, in practice this presents no real problem since we are aware of the property each symbol represents and therefore intuitively know its rank, *e.g.* we know velocity **U** is a tensor of rank 1.

A further, more fundamental idea regarding the choice of notation is that the mathematical representation of a tensor should not change depending on our coordinate system, *i.e.* the vector **a**is the same vector irrespective of where we view it from. The tensor notation supports this concept as it implies nothing about the coordinate system. However, other notations, *e.g.* a_i , expose the individual components of the tensor which naturally implies the choice of coordinate system. The unsatisfactory consequence of this is that the tensor is then represented by a set of values which are not unique — they depend on the coordinate system.

That said, the index notation, introduced in Section 1.2, is adopted from time to time in this book mainly to expand tensor operations into the constituent components. When using the index notation, we adopt the *summation convention* which states that whenever the same letter subscript occurs twice in a term, the that subscript is to be given all values, *i.e.* 1, 2, 3, and the results added together, *e.g.*

$$a_i b_i = \sum_{i=1}^3 a_i b_i = a_1 b_1 + a_2 b_2 + a_3 b_3 \tag{1.3}$$

In the remainder of the book the symbol \sum is omitted since the repeated subscript indicates the summation.

1.3 Algebraic tensor operations

This section describes all the algebraic operations for tensors that are available in Open-FOAM. Let us first review the most simple tensor operations: addition, subtraction, and scalar multiplication and division. Addition and subtraction are both commutative and associative and are only valid between tensors of the same rank. The operations are performed by addition/subtraction of respective components of the tensors, e.g. the subtraction of two vectors \mathbf{a} and \mathbf{b} is

$$\mathbf{a} - \mathbf{b} = a_i - b_i = (a_1 - b_1, a_2 - b_2, a_3 - b_3) \tag{1.4}$$

Multiplication of any tensor \mathbf{a} by a scalar s is also commutative and associative and is performed by multiplying all the tensor components by the scalar. For example,

$$s\mathbf{a} = sa_i = (sa_1, sa_2, sa_3)$$
 (1.5)

P-18 Tensor mathematics

Division between a tensor \mathbf{a} and a scalar is only relevant when the scalar is the second argument of the operation, *i.e.*

$$\mathbf{a}/s = a_i/s = (a_1/s, a_2/s, a_3/s) \tag{1.6}$$

Following these operations are a set of more complex products between tensors of rank 1 and above, described in the following Sections.

1.3.1 The inner product

The inner product operates on any two tensors of rank r_1 and r_2 such that the rank of the result $r = r_1 + r_2 - 2$. Inner product operations with tensors up to rank 3 are described below:

• The inner product of two vectors **a** and **b** is commutative and produces a scalar $s = \mathbf{a} \cdot \mathbf{b}$ where

$$s = a_i b_i = a_1 b_1 + a_2 b_2 + a_3 b_3 \tag{1.7}$$

• The inner product of a tensor \mathbf{T} and vector \mathbf{a} produces a vector $\mathbf{b} = \mathbf{T} \cdot \mathbf{a}$, represented below as a column array for convenience

$$b_{i} = T_{ij}a_{j} = \begin{pmatrix} T_{11}a_{1} + T_{12}a_{2} + T_{13}a_{3} \\ T_{21}a_{1} + T_{22}a_{2} + T_{23}a_{3} \\ T_{31}a_{1} + T_{32}a_{2} + T_{33}a_{3} \end{pmatrix}$$

$$(1.8)$$

It is non-commutative if **T** is non-symmetric such that $\mathbf{b} = \mathbf{a} \cdot \mathbf{T} = \mathbf{T}^{\mathrm{T}} \cdot \mathbf{a}$ is

$$b_{i} = a_{j}T_{ji} = \begin{pmatrix} a_{1}T_{11} + a_{2}T_{21} + a_{3}T_{31} \\ a_{1}T_{12} + a_{2}T_{22} + a_{3}T_{32} \\ a_{1}T_{13} + a_{2}T_{23} + a_{3}T_{33} \end{pmatrix}$$

$$(1.9)$$

ullet The inner product of two tensors ${f T}$ and ${f S}$ produces a tensor ${f P}={f T}ullet {f S}$ whose components are evaluated as:

$$P_{ij} = T_{ik} S_{kj} (1.10)$$

It is non-commutative such that $\mathbf{T} \cdot \mathbf{S} = (\mathbf{S}^T \cdot \mathbf{T}^T)^T$

• The inner product of a vector \mathbf{a} and third rank tensor \mathbf{P} produces a second rank tensor $\mathbf{T} = \mathbf{a} \cdot \mathbf{P}$ whose components are

$$T_{ij} = a_k P_{kij} (1.11)$$

Again this is non-commutative so that $\mathbf{T} = \mathbf{P} \cdot \mathbf{a}$ is

$$T_{ij} = P_{ijk}a_k \tag{1.12}$$

• The inner product of a second rank tensor T and third rank tensor P produces a third rank tensor $Q = T \cdot P$ whose components are

$$Q_{ijk} = T_{il}P_{ljk} \tag{1.13}$$

Again this is non-commutative so that $\mathbf{Q} = \mathbf{P} \cdot \mathbf{T}$ is

$$Q_{ijk} = P_{ijl}T_{lk} \tag{1.14}$$

1.3.2 The double inner product of two tensors

The double inner product of two second-rank tensors T and S produces a scalar s = T : S which can be evaluated as the sum of the 9 products of the tensor components

$$s = T_{ij}S_{ij} = T_{11}S_{11} + T_{12}S_{12} + T_{13}S_{13} + T_{21}S_{21} + T_{22}S_{22} + T_{23}S_{23} + T_{31}S_{31} + T_{32}S_{32} + T_{33}S_{33}$$

$$(1.15)$$

The double inner product between a second rank tensor T and third rank tensor P produces a vector $\mathbf{a} = T \ P$ with components

$$a_i = T_{jk} P_{jki} \tag{1.16}$$

This is non-commutative so that $\mathbf{a} = \mathbf{P} \cdot \mathbf{T}$ is

$$a_i = P_{ijk}T_{jk} (1.17)$$

1.3.3 The triple inner product of two third rank tensors

The triple inner product of two third rank tensors \mathbf{P} and \mathbf{Q} produces a scalar $s = \mathbf{P} \ \mathbf{Q}$ which can be evaluated as the sum of the 27 products of the tensor components

$$s = P_{ijk}Q_{ijk} \tag{1.18}$$

1.3.4 The outer product

The outer product operates between vectors and tensors as follows:

• The outer product of two vectors \mathbf{a} and \mathbf{b} is non-commutative and produces a tensor $\mathbf{T} = \mathbf{a}\mathbf{b} = (\mathbf{b}\mathbf{a})^{\mathrm{T}}$ whose components are evaluated as:

$$T_{ij} = a_i b_j = \begin{pmatrix} a_1 b_1 & a_1 b_2 & a_1 b_3 \\ a_2 b_1 & a_2 b_2 & a_2 b_3 \\ a_3 b_1 & a_3 b_2 & a_3 b_3 \end{pmatrix}$$

$$(1.19)$$

• An outer product of a vector \mathbf{a} and second rank tensor \mathbf{T} produces a third rank tensor $\mathbf{P} = \mathbf{a}\mathbf{T}$ whose components are

$$P_{ijk} = a_i T_{jk} (1.20)$$

This is non-commutative so that P = Ta produces

$$P_{ijk} = T_{ij}a_k \tag{1.21}$$

1.3.5 The cross product of two vectors

The cross product operation is exclusive to vectors only. For two vectors \mathbf{a} with \mathbf{b} , it produces a vector $\mathbf{c} = \mathbf{a} \times \mathbf{b}$ whose components are

$$c_i = e_{ijk}a_ib_k = (a_2b_3 - a_3b_2, a_3b_1 - a_1b_3, a_1b_2 - a_2b_1)$$

$$(1.22)$$

where the *permutation symbol* is defined by

$$e_{ijk} = \begin{cases} 0 & \text{when any two indices are equal} \\ +1 & \text{when } i,j,k \text{ are an even permutation of } 1,2,3 \\ -1 & \text{when } i,j,k \text{ are an odd permutation of } 1,2,3 \end{cases}$$

$$(1.23)$$

in which the even permutations are 123, 231 and 312 and the odd permutations are 132, 213 and 321.

P-20 Tensor mathematics

1.3.6 Other general tensor operations

Some less common tensor operations and terminology used by OpenFOAM are described below.

Square of a tensor is defined as the outer product of the tensor with itself, e.g. for a vector \mathbf{a} , the square $\mathbf{a}^2 = \mathbf{a}\mathbf{a}$.

nth power of a tensor is evaluated by n outer products of the tensor, e.g. for a vector \mathbf{a} , the 3rd power $\mathbf{a}^3 = \mathbf{a}\mathbf{a}\mathbf{a}$.

Magnitude squared of a tensor is the rth inner product of the tensor of rank r with itself, to produce a scalar. For example, for a second rank tensor \mathbf{T} , $|\mathbf{T}|^2 = \mathbf{T} \cdot \mathbf{T}$.

Magnitude is the square root of the magnitude squared, e.g. for a tensor \mathbf{T} , $|\mathbf{T}| = \sqrt{\mathbf{T} \cdot \mathbf{T}}$. Vectors of unit magnitude are referred to as unit vectors.

Component maximum is the component of the tensor with greatest value, inclusive of sign, *i.e.* not the largest magnitude.

Component minimum is the component of the tensor with smallest value.

Component average is the mean of all components of a tensor.

Scale As the name suggests, the scale function is a tool for scaling the components of one tensor by the components of another tensor of the same rank. It is evaluated as the product of corresponding components of 2 tensors, *e.g.*, scaling vector **a** by vector **b** would produce vector **c** whose components are

$$c_i = \text{scale}(\mathbf{a}, \mathbf{b}) = (a_1 b_1, a_2 b_2, a_3 b_3)$$
 (1.24)

1.3.7 Geometric transformation and the identity tensor

A second rank tensor \mathbf{T} is strictly defined as a linear vector function, i.e. it is a function which associates an argument vector \mathbf{a} to another vector \mathbf{b} by the inner product $\mathbf{b} = \mathbf{T} \cdot \mathbf{a}$. The components of \mathbf{T} can be chosen to perform a specific geometric transformation of a tensor from the x, y, z coordinate system to a new coordinate system x^*, y^*, z^* ; \mathbf{T} is then referred to as the transformation tensor. While a scalar remains unchanged under a transformation, the vector \mathbf{a} is transformed to \mathbf{a}^* by

$$\mathbf{a}^* = \mathbf{T} \cdot \mathbf{a} \tag{1.25}$$

A second rank tensor S is transformed to S^* according to

$$\mathbf{S}^* = \mathbf{T} \cdot \mathbf{S} \cdot \mathbf{T}^{\mathrm{T}} \tag{1.26}$$

The *identity tensor* \mathbf{I} is defined by the requirement that it transforms another tensor onto itself. For all vectors \mathbf{a}

$$\mathbf{a} = \mathbf{I} \cdot \mathbf{a} \tag{1.27}$$

and therefore

$$\mathbf{I} = \delta_{ij} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix} \tag{1.28}$$

where δ_{ij} is known as the Kronecker delta symbol.

1.3.8 Useful tensor identities

Several identities are listed below which can be verified by under the assumption that all the relevant derivatives exist and are continuous. The identities are expressed for scalar s and vector \mathbf{a} .

$$\nabla \cdot (\nabla \times \mathbf{a}) \equiv 0$$

$$\nabla \times (\nabla s) \equiv \mathbf{0}$$

$$\nabla \cdot (s\mathbf{a}) \equiv s \nabla \cdot \mathbf{a} + \mathbf{a} \cdot \nabla s$$

$$\nabla \times (s\mathbf{a}) \equiv s \nabla \times \mathbf{a} + \nabla s \times \mathbf{a}$$

$$\nabla (\mathbf{a} \cdot \mathbf{b}) \equiv \mathbf{a} \times (\nabla \times \mathbf{b}) + \mathbf{b} \times (\nabla \times \mathbf{a}) + (\mathbf{a} \cdot \nabla) \mathbf{b} + (\mathbf{b} \cdot \nabla) \mathbf{a}$$

$$\nabla \cdot (\mathbf{a} \times \mathbf{b}) \equiv \mathbf{b} \cdot (\nabla \times \mathbf{a}) - \mathbf{a} \cdot (\nabla \times \mathbf{b})$$

$$\nabla \times (\mathbf{a} \times \mathbf{b}) \equiv \mathbf{a} (\nabla \cdot \mathbf{b}) - \mathbf{b} (\nabla \cdot \mathbf{a}) + (\mathbf{b} \cdot \nabla) \mathbf{a} - (\mathbf{a} \cdot \nabla) \mathbf{b}$$

$$\nabla \times (\nabla \times \mathbf{a}) \equiv \nabla (\nabla \cdot \mathbf{a}) - \nabla^2 \mathbf{a}$$

$$(\nabla \times \mathbf{a}) \times \mathbf{a} \equiv \mathbf{a} \cdot (\nabla \mathbf{a}) - \nabla (\mathbf{a} \cdot \mathbf{a})$$

It is sometimes useful to know the $e-\delta$ identity to help to manipulate equations in index notation:

$$e_{ijk}e_{irs} = \delta_{jr}\delta_{ks} - \delta_{js}\delta_{kr} \tag{1.30}$$

1.3.9 Operations exclusive to tensors of rank 2

There are several operations that manipulate the components of tensors of rank 2 that are listed below:

Transpose of a tensor $T = T_{ij}$ is $T^T = T_{ji}$ as described in Equation 1.2.

Symmetric and skew (antisymmetric) tensors As discussed in section 1.2, a tensor is said to be symmetric if its components are symmetric about the diagonal, i.e. $\mathbf{T} = \mathbf{T}^{\mathrm{T}}$. A skew or antisymmetric tensor has $\mathbf{T} = -\mathbf{T}^{\mathrm{T}}$ which intuitively implies that $T_{11} = T_{22} = T_{33} = 0$. Every second order tensor can be decomposed into symmetric and skew parts by

$$\mathbf{T} = \underbrace{\frac{1}{2}(\mathbf{T} + \mathbf{T}^{\mathrm{T}})}_{symmetric} + \underbrace{\frac{1}{2}(\mathbf{T} - \mathbf{T}^{\mathrm{T}})}_{skew} = \operatorname{symm} \mathbf{T} + \operatorname{skew} \mathbf{T}$$
(1.31)

Trace The trace of a tensor **T** is a scalar, evaluated by summing the diagonal components

$$\operatorname{tr} \mathbf{T} = T_{11} + T_{22} + T_{33} \tag{1.32}$$

 ${f Diagonal}$ returns a vector whose components are the diagonal components of the second rank tensor ${f T}$

$$\operatorname{diag} \mathbf{T} = (T_{11}, T_{22}, T_{33}) \tag{1.33}$$

Deviatoric and hydrostatic tensors Every second rank tensor \mathbf{T} can be decomposed into a deviatoric component, for which $\operatorname{tr} \mathbf{T} = 0$ and a hydrostatic component of the form $\mathbf{T} = s\mathbf{I}$ where s is a scalar. Every second rank tensor can be decomposed into deviatoric and hydrostatic parts as follows:

$$\mathbf{T} = \underbrace{\mathbf{T} - \frac{1}{3} (\operatorname{tr} \mathbf{T}) \mathbf{I}}_{deviatoric} + \underbrace{\frac{1}{3} (\operatorname{tr} \mathbf{T}) \mathbf{I}}_{hydrostatic} = \operatorname{dev} \mathbf{T} + \operatorname{hyd} \mathbf{T}$$
(1.34)

P-22 Tensor mathematics

Determinant The determinant of a second rank tensor is evaluated by

$$\det \mathbf{T} = \begin{vmatrix} T_{11} & T_{12} & T_{13} \\ T_{21} & T_{22} & T_{23} \\ T_{31} & T_{32} & T_{33} \end{vmatrix} = T_{11}(T_{22}T_{33} - T_{23}T_{32}) - T_{12}(T_{21}T_{33} - T_{23}T_{31}) + T_{13}(T_{21}T_{32} - T_{22}T_{31})$$

$$= \frac{1}{6}e_{ijk}e_{pqr}T_{ip}T_{jq}T_{kr}$$
(1.35)

Cofactors The *minors* of a tensor are evaluated for each component by deleting the row and column in which the component is situated and evaluating the resulting entries as a 2×2 determinant. For example, the minor of T_{12} is

$$\begin{vmatrix} T_{11} & T_{12} & T_{13} \\ T_{21} & T_{22} & T_{23} \\ T_{31} & T_{32} & T_{33} \end{vmatrix} = \begin{vmatrix} T_{21} & T_{23} \\ T_{31} & T_{33} \end{vmatrix} = T_{21}T_{33} - T_{23}T_{31}$$

$$(1.36)$$

The cofactors are *signed minors* where each minor is component is given a sign based on the rule

+ve if
$$i + j$$
 is even
-ve if $i + j$ is odd (1.37)

The cofactors of T can be evaluated as

$$\operatorname{cof} \mathbf{T} = \frac{1}{2} e_{jkr} e_{ist} T_{sk} T_{tr} \tag{1.38}$$

Inverse The inverse of a tensor can be evaluated as

$$\operatorname{inv} \mathbf{T} = \frac{\operatorname{cof} \mathbf{T}^{\mathrm{T}}}{\det \mathbf{T}} \tag{1.39}$$

Hodge dual of a tensor is a vector whose components are

$$*\mathbf{T} = (T_{23}, -T_{13}, T_{12}) \tag{1.40}$$

1.3.10 Operations exclusive to scalars

OpenFOAM supports most of the well known functions that operate on scalars, e.g. square root, exponential, logarithm, sine, cosine etc.., a list of which can be found in Table 1.2. There are 3 additional functions defined within OpenFOAM that are described below:

Sign of a scalar s is

$$\operatorname{sgn}(s) = \begin{cases} 1 & \text{if } s \ge 0, \\ -1 & \text{if } s < 0. \end{cases}$$
 (1.41)

Positive of a scalar s is

$$pos(s) = \begin{cases} 1 & \text{if } s \ge 0, \\ 0 & \text{if } s < 0. \end{cases}$$
 (1.42)

Limit of a scalar s by the scalar n

$$\lim_{n \to \infty} \lim_{n \to \infty} f(s, n) = \begin{cases} s & \text{if } s < n, \\ 0 & \text{if } s \ge n. \end{cases} \tag{1.43}$$

1.4 OpenFOAM tensor classes

OpenFOAM contains a C++ class library primitive that contains the classes for the tensor mathematics described so far. The basic tensor classes that are available as standard in OpenFOAM are listed in Table 1.1. The Table also lists the functions that allow the user to access individual components of a tensor, known as access functions.

Rank	Common name	Basic class	Access functions
0	Scalar	scalar	
1	Vector	vector	x(), y(), z()
2	Tensor	tensor	xx(), xy(), xz()

Table 1.1: Basic tensor classes in OpenFOAM

We can declare the tensor

$$\mathbf{T} = \begin{pmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 7 & 8 & 9 \end{pmatrix} \tag{1.44}$$

in OpenFOAM by the line:

We can then access the component T_{13} , or T_{xz} using the xz() access function. For instance the code

Info <<
$$``Txz = '' << T.xz() << endl;$$

outputs to the screen:

Txz = 3

1.4.1 Algebraic tensor operations in OpenFOAM

The algebraic operations described in Section 1.3 are all available to the OpenFOAM tensor classes using syntax which closely mimics the notation used in written mathematics. Some functions are represented solely by descriptive functions, e.g.symm(), but others can also be executed using symbolic operators, e.g.*. All functions are listed in Table 1.2.

Operation	Comment	Mathematical	Description
		Description	in OpenFOAM
Addition		a + b	a + b
Subtraction		a - b	a - b
Scalar multiplication		$s\mathbf{a}$	s * a
Scalar division		\mathbf{a}/s	a / s
Outer product	$rank \mathbf{a}, \mathbf{b} >= 1$	ab	a * b
Inner product	$rank \mathbf{a}, \mathbf{b} >= 1$	a•b	a & b
Double inner product	$rank \mathbf{a}, \mathbf{b} >= 2$	a:b	a && b
Cross product	$rank \ \mathbf{a}, \mathbf{b} = 1$	$\mathbf{a} \times \mathbf{b}$	a ^ b
Square		\mathbf{a}^2	sqr(a)
		Cox	ntinued on next page

P-24 Tensor mathematics

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Operation	Comment	Mathematical	Description
		Description	in OpenFOAM
Magnitude squared		$ \mathbf{a} ^2$	magSqr(a)
Magnitude		$ \mathbf{a} $	mag(a)
Power	n = 0, 1,, 4	\mathbf{a}^n	pow(a,n)
Component average	i = 1,, N	$\overline{a_i}$	cmptAv(a)
Component maximum	i = 1,, N	$\max(a_i)$	max(a)
Component minimum	i = 1,, N	$\min(a_i)$	min(a)
Scale		$scale(\mathbf{a}, \mathbf{b})$	scale(a,b)
Geometric transformation	transforms a u	sing tensor T	<pre>transform(T,a)</pre>
Operations evaluaive to ten	gong of monte ?		
Operations exclusive to tens	sors of rank 2	T^{T}	T.T()
Transpose		_	
Diagonal Trace		$\operatorname{diag}\mathbf{T}$	diag(T)
		tr T	tr(T)
Deviatoric component		$\operatorname{dev}\mathbf{T}$	dev(T)
Symmetric component		$\operatorname{symm} \mathbf{T}$	symm(T)
Skew-symmetric component		$\operatorname{skew} \mathbf{T}$	skew(T)
Determinant		$\det \mathbf{T}$	det(T)
Cofactors		$\operatorname{cof}\mathbf{T}$	cof(T)
Inverse		$\operatorname{inv} \mathbf{T}$	inv(T)
Hodge dual		$*\mathbf{T}$	*T
Operations exclusive to scal	ars		
Sign (boolean)	iai b	sgn(s)	sign(s)
Positive (boolean)		s >= 0	pos(s)
Negative (boolean)		s < 0	neg(s)
Limit	n scalar	limit(s, n)	limit(s,n)
Square root	n scarar	\sqrt{s}	sqrt(s)
Exponential			exp(s)
Natural logarithm		$\exp s$ $\ln s$	log(s)
<u> </u>			•
Base 10 logarithm		$\log_{10} s$	log10(s)
Sine		$\sin s$	sin(s)
Cosine		$\cos s$	cos(s)
Tangent		$ \tan s $	tan(s)
Arc sine		$a\sin s$	asin(s)
Arc cosine		$a\cos s$	acos(s)
Arc tangent		a tan s	atan(s)
Hyperbolic sine		$\sinh s$	sinh(s)
Hyperbolic cosine		$\cosh s$	cosh(s)
Hyperbolic tangent		$\tanh s$	tanh(s)
Hyperbolic arc sine		a s inh s	asinh(s)
Hyperbolic arc cosine		$\operatorname{acosh} s$	acosh(s)
Hyperbolic arc tangent		$\operatorname{atanh} s$	atanh(s)
Error function		$\operatorname{erf} s$	erf(s)
Complement error function		$\operatorname{erfc} s$	erfc(s)
Logarithm gamma function		$\ln \Gamma s$	lgamma(s)
Type 1 Bessel function of order	0	$J_0 s$	j0(s)
Type 1 Bessel function of order		$\operatorname{J}_1 s$	j1(s)
Type I Desser rancolon of order	-		tinued on next page
		Con	made on none page

1.5 Dimensional units P-25

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Operation	Comment	Mathematical	Description
		Description	in OpenFOAM
Type 2 Bessel function of order	0 0	$Y_0 s$	y0(s)
Type 2 Bessel function of order	r 1	$Y_1 s$	y1(s)

a, b are tensors of arbitrary rank unless otherwise stated

Table 1.2: Algebraic tensor operations in OpenFOAM

1.5 Dimensional units

In continuum mechanics, properties are represented in some chosen units, e.g. mass in kilograms (kg), volume in cubic metres (m³), pressure in Pascals (kg m s⁻²). Algebraic operations must be performed on these properties using consistent units of measurement; in particular, addition, subtraction and equality are only physically meaningful for properties of the same dimensional units. As a safeguard against implementing a meaningless operation, OpenFOAM encourages the user to attach dimensional units to any tensor and will then perform dimension checking of any tensor operation.

Units are defined using the dimensionSet class, e.g.

dimensionSet pressureDims(1, -1, -2, 0, 0, 0, 0);

No.	Property	Unit	Symbol
1	Mass	kilogram	k
2	Length	metre	m
3	Time	second	S
4	Temperature	Kelvin	K
5	Quantity	moles	mol
6	Current	ampere	A
7	Luminous intensity	candela	cd

Table 1.3: S.I. base units of measurement

where each of the values corresponds to the power of each of the S.I. base units of measurement listed in Table 1.3. The line of code declares pressureDims to be the dimensionSet for pressure kg m s⁻² since the first entry in the pressureDims array, 1, corresponds to k¹, the second entry, -1, corresponds to m⁻¹ etc.. A tensor with units is defined using the dimensioned<Type> template class, the <Type> being scalar, vector, tensor, etc.. The dimensioned<Type> stores a variable name of class word, the value <Type> and a dimensionSet

```
dimensionedTensor sigma
    (
          "sigma",
           dimensionSet(1, -1, -2, 0, 0, 0, 0),
           tensor(1e6,0,0,0,1e6,0,0,0,1e6),
    );
```

s is a scalar, N is the number of tensor components

P-26 Tensor mathematics

creates a tensor with correct dimensions of pressure, or stress

$$\sigma = \begin{pmatrix} 10^6 & 0 & 0 \\ 0 & 10^6 & 0 \\ 0 & 0 & 10^6 \end{pmatrix} \tag{1.45}$$

Chapter 2

Discretisation procedures

So far we have dealt with algebra of tensors at a point. The PDEs we wish to solve involve derivatives of tensors with respect to time and space. We therefore need to extend our description to a tensor field, i.e. a tensor that varies across time and spatial domains. In this Chapter we will first present a mathematical description of all the differential operators we may encounter. We will then show how a tensor field is constructed in OpenFOAM and how the derivatives of these fields are discretised into a set of algebraic equations.

2.1 Differential operators

Before defining the spatial derivatives we first introduce the nabla vector operator ∇ , represented in index notation as ∂_i :

$$\nabla \equiv \partial_i \equiv \frac{\partial}{\partial x_i} \equiv \left(\frac{\partial}{\partial x_1}, \frac{\partial}{\partial x_2}, \frac{\partial}{\partial x_3}\right) \tag{2.1}$$

The nabla operator is a useful notation that obeys the following rules:

- it operates on the tensors to its right and the conventional rules of a derivative of a product, e.g. $\partial_i ab = (\partial_i a) b + a (\partial_i b)$;
- otherwise the nabla operator behaves like any other vector in an algebraic operation.

2.1.1 Gradient

If a scalar field s is defined and continuously differentiable then the gradient of s, ∇s is a vector field

$$\nabla s = \partial_i s = \left(\frac{\partial s}{\partial x_1}, \frac{\partial s}{\partial x_2}, \frac{\partial s}{\partial x_3}\right) \tag{2.2}$$

The gradient can operate on any tensor field to produce a tensor field that is one rank higher. For example, the gradient of a vector field **a** is a second rank tensor field

$$\nabla \mathbf{a} = \partial_i a_j = \begin{pmatrix} \partial a_1 / \partial x_1 & \partial a_2 / \partial x_1 & \partial a_3 / \partial x_1 \\ \partial a_1 / \partial x_2 & \partial a_2 / \partial x_2 & \partial a_3 / \partial x_2 \\ \partial a_1 / \partial x_3 & \partial a_2 / \partial x_3 & \partial a_3 / \partial x_3 \end{pmatrix}$$
(2.3)

2.1.2 Divergence

If a vector field \mathbf{a} is defined and continuously differentiable then the divergence of \mathbf{a} is a scalar field

$$\nabla \cdot \mathbf{a} = \partial_i a_i = \frac{\partial a_1}{\partial x_1} + \frac{\partial a_2}{\partial x_2} + \frac{\partial a_3}{\partial x_3}$$
 (2.4)

The divergence can operate on any tensor field of rank 1 and above to produce a tensor that is one rank lower. For example the divergence of a second rank tensor field **T** is a vector field (expanding the vector as a column array for convenience)

$$\nabla \cdot \mathbf{T} = \partial_i T_{ij} = \begin{pmatrix} \partial T_{11}/\partial x_1 + \partial T_{12}/\partial x_1 + \partial T_{13}/\partial x_1 \\ \partial T_{21}/\partial x_2 + \partial T_{22}/\partial x_2 + \partial T_{23}/\partial x_2 \\ \partial T_{31}/\partial x_3 + \partial T_{32}/\partial x_3 + \partial T_{33}/\partial x_3 \end{pmatrix}$$
(2.5)

2.1.3 Curl

If a vector field **a** is defined and continuously differentiable then the curl of **a**, $\nabla \times \mathbf{a}$ is a vector field

$$\nabla \times \mathbf{a} = e_{ijk} \partial_j a_k = \left(\frac{\partial a_3}{\partial x_2} - \frac{\partial a_2}{\partial x_3}, \frac{\partial a_1}{\partial x_3} - \frac{\partial a_3}{\partial x_1}, \frac{\partial a_2}{\partial x_1} - \frac{\partial a_1}{\partial x_2} \right)$$
(2.6)

The curl is related to the gradient by

$$\nabla \times \mathbf{a} = 2 \,(* \,\mathrm{skew} \,\nabla \mathbf{a}) \tag{2.7}$$

2.1.4 Laplacian

The Laplacian is an operation that can be defined mathematically by a combination of the divergence and gradient operators by $\nabla^2 \equiv \nabla \cdot \nabla$. However, the Laplacian should be considered as a single operation that transforms a tensor field into another tensor field of the same rank, rather than a combination of two operations, one which raises the rank by 1 and one which reduces the rank by 1.

In fact, the Laplacian is best defined as a *scalar operator*, just as we defined nabla as a vector operator, by

$$\nabla^2 \equiv \partial^2 \equiv \frac{\partial^2}{\partial x_1^2} + \frac{\partial^2}{\partial x_2^2} + \frac{\partial^2}{\partial x_3^2} \tag{2.8}$$

For example, the Laplacian of a scalar field s is the scalar field

$$\nabla^2 s = \partial^2 s = \frac{\partial^2 s}{\partial x_1^2} + \frac{\partial^2 s}{\partial x_2^2} + \frac{\partial^2 s}{\partial x_3^2}$$
 (2.9)

2.1.5 Temporal derivative

There is more than one definition of temporal, or time, derivative of a tensor. To describe the temporal derivatives we must first recall that the tensor relates to a property of a volume of material that may be moving. If we track an infinitesimally small volume of material, or particle, as it moves and observe the change in the tensorial property ϕ in time, we have the *total*, or *material* time derivative denoted by

$$\frac{D\phi}{Dt} = \lim_{\Delta t \to 0} \frac{\Delta\phi}{\Delta t} \tag{2.10}$$

However in continuum mechanics, particularly fluid mechanics, we often observe the change of a ϕ in time at a fixed point in space as different particles move across that point. This change at a point in space is termed the *spatial* time derivative which is denoted by $\partial/\partial t$ and is related to the material derivative by:

$$\frac{D\phi}{Dt} = \frac{\partial\phi}{\partial t} + \mathbf{U} \cdot \nabla\phi \tag{2.11}$$

where **U** is the velocity field of property ϕ . The second term on the right is known as the convective rate of change of ϕ .

2.2 Overview of discretisation

The term discretisation means approximation of a problem into discrete quantities. The FV method and others, such as the finite element and finite difference methods, all discretise the problem as follows:

Spatial discretisation Defining the solution domain by a set of points that fill and bound a region of space when connected;

Temporal discretisation (For transient problems) dividing the time domain into into a finite number of time intervals, or steps;

Equation discretisation Generating a system of algebraic equations in terms of discrete quantities defined at specific locations in the domain, from the PDEs that characterise the problem.

2.2.1 OpenFOAM lists and fields

OpenFOAM frequently needs to store sets of data and perform functions, such as mathematical operations, on the data. OpenFOAM therefore provides an array template class List<Type>, making it possible to create a list of any object of class Type that inherits the functions of the Type. For example a List of vector is List<vector>.

Lists of the tensor classes are defined as standard in OpenFOAM by the template class Field<Type>. For better code legibility, all instances of Field<Type>, e.g.Field<vector>, are renamed using typedef declarations as scalarField, vectorField, tensorField, symmTensor-Field, tensorThirdField and symmTensorThirdField. Algebraic operations can be performed between Fields subject to obvious restrictions such as the fields having the same number of elements. OpenFOAM also supports operations between a field and single tensor, e.g. all values of a Field U can be multiplied by the scalar 2 with the operation U = 2.0 * U.

2.3 Discretisation of the solution domain

Discretisation of the solution domain is shown in Figure 2.1. The space domain is discretised into computational mesh on which the PDEs are subsequently discretised. Discretisation of time, if required, is simple: it is broken into a set of time steps Δt that may change during a numerical simulation, perhaps depending on some condition calculated during the simulation.

On a more detailed level, discretisation of space requires the subdivision of the domain into a number of cells, or control volumes. The cells are contiguous, i.e. they do not overlap one another and completely fill the domain. A typical cell is shown in Figure 2.2.

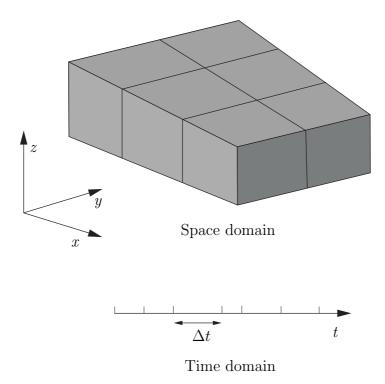


Figure 2.1: Discretisation of the solution domain

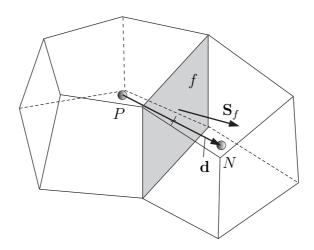


Figure 2.2: Parameters in finite volume discretisation

Dependent variables and other properties are principally stored at the cell centroid P although they may be stored on faces or vertices. The cell is bounded by a set of flat faces, given the generic label f. In OpenFOAM there is no limitation on the number of faces bounding each cell, nor any restriction on the alignment of each face. This kind of mesh is often referred to as "arbitrarily unstructured" to differentiate it from meshes in which the cell faces have a prescribed alignment, typically with the coordinate axes. Codes with arbitrarily unstructured meshes offer greater freedom in mesh generation and manipulation in particular when the geometry of the domain is complex or changes over time.

Whilst most properties are defined at the cell centroids, some are defined at cell faces. There are two types of cell face.

Internal faces Those faces that connect two cells (and it can never be more than two). For each internal face, OpenFOAM designates one adjoining cell to be the face owner and the other to be the neighbour;

Boundary faces Those belonging to one cell since they coincide with the boundary of the domain. These faces simply have an owner cell.

2.3.1 Defining a mesh in OpenFOAM

There are different levels of mesh description in OpenFOAM, beginning with the most basic mesh class, named polyMesh since it is based on polyhedra. A polyMesh is constructed using the minimum information required to define the mesh geometry described below and presented in Figure 2.3:

Points A list of cell vertex point coordinate vectors, *i.e.* a vectorField, that is renamed pointField using a typedef declaration;

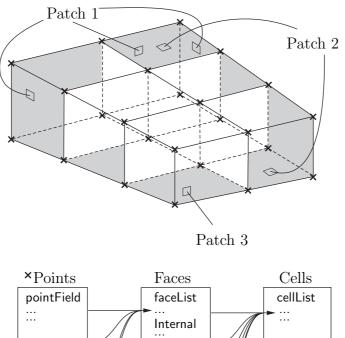
Faces A list of cell faces List<face>, or faceList, where the face class is defined by a list of vertex numbers, corresponding to the pointField;

Cells a list of cells List<cell>, or cellList, where the cell class is defined by a list of face numbers, corresponding to the faceList described previously.

Boundary a polyBoundaryMesh decomposed into a list of patches, polyPatchList representing different regions of the boundary. The boundary is subdivided in this manner to allow different boundary conditions to be specified on different patches during a solution. All the faces of any polyPatch are stored as a single block of the faceList, so that its faces can be easily accessed using the slice class which stores references to the first and last face of the block. Each polyPatch is then constructed from

- a slice;
- a word to assign it a name.

FV discretisation uses specific data that is derived from the mesh geometry stored in polyMesh. OpenFOAM therefore extends the polyMesh class to fvMesh which stores the additional data needed for FV discretisation. fvMesh is constructed from polyMesh and stores the data in Table 2.1 which can be updated during runtime in cases where the mesh moves, is refined *etc.*.



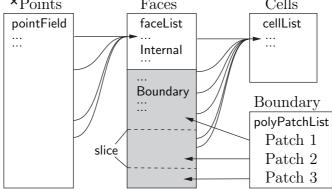


Figure 2.3: Schematic of the basic mesh description used in OpenFOAM

2.3.2 Defining a geometricField in OpenFOAM

So far we can define a field, *i.e.* a list of tensors, and a mesh. These can be combined to define a tensor field relating to discrete points in our domain, specified in OpenFOAM by the template class geometricField<Type>. The Field values are separated into those defined within the internal region of the domain, *e.g.* at the cell centres, and those defined on the domain boundary, *e.g.* on the boundary faces. The geometricField<Type> stores the following information:

Internal field This is simply a Field<Type>, described in Section 2.2.1;

BoundaryField This is a GeometricBoundaryField, in which a Field is defined for the faces of each patch and a Field is defined for the patches of the boundary. This is then a field of fields, stored within an object of the FieldField<Type> class. A reference to the fvBoundaryMesh is also stored [**].

Mesh A reference to an fvMesh, with some additional detail as to the whether the field is defined at cell centres, faces, etc..

Dimensions A dimensionSet, described in Section 4.2.6.

Old values Discretisation of time derivatives requires field data from previous time steps. The geometricField<Type> will store references to stored fields from the previous, or old, time step and its previous, or old-old, time step where necessary.

Class	Description	Symbol	Access function
volScalarField	Cell volumes	V	V()
surfaceVectorField	Face area vectors	\mathbf{S}_f	Sf()
surfaceScalarField	Face area magnitudes	$ \mathbf{S}_f $	magSf()
volVectorField	Cell centres	\mathbf{C}	C()
surfaceVectorField	Face centres	\mathbf{C}_f	Cf()
surfaceScalarField	Face motion fluxes **	ϕ_g	phi()

Table 2.1: fvMesh stored data.

Previous iteration values The iterative solution procedures can use under-relaxation which requires access to data from the previous iteration. Again, if required, geometricField<Type> stores a reference to the data from the previous iteration.

As discussed in Section 2.3, we principally define a property at the cell centres but quite often it is stored at the cell faces and on occasion it is defined on cell vertices. The geometricField<Type> is renamed using typedef declarations to indicate where the field variable is defined as follows:

volField<Type> A field defined at cell centres;

surfaceField<Type> A field defined on cell faces;

pointField<Type> A field defined on cell vertices.

These typedef field classes of geometricField<Type>are illustrated in Figure 2.4. A geometricField<Type> inherits all the tensor algebra of Field<Type> and has all operations subjected to dimension checking using the dimensionSet. It can also be subjected to the FV discretisation procedures described in the following Section. The class structure used to build geometricField<Type> is shown in Figure 2.5¹.

2.4 Equation discretisation

Equation discretisation converts the PDEs into a set of algebraic equations that are commonly expressed in matrix form as:

$$[A][x] = [b] \tag{2.12}$$

where [A] is a square matrix, [x] is the column vector of dependent variable and [b] is the source vector. The description of [x] and [b] as 'vectors' comes from matrix terminology rather than being a precise description of what they truly are: a list of values defined at locations in the geometry, i.e. a geometricField<Type>, or more specifically a volField<Type> when using FV discretisation.

[A] is a list of coefficients of a set of algebraic equations, and cannot be described as a geometricField<Type>. It is therefore given a class of its own: fvMatrix. fvMatrix<Type> is created through discretisation of a geometric<Type>Field and therefore inherits the <Type>. It supports many of the standard algebraic matrix operations of addition +, subtraction - and multiplication *.

Each term in a PDE is represented individually in OpenFOAM code using the classes of static functions finiteVolumeMethod and finiteVolumeCalculus, abbreviated by a typedef

¹The diagram is not an exact description of the class hierarchy, rather a representation of the general structure leading from some primitive classes to geometric<Type>Field.

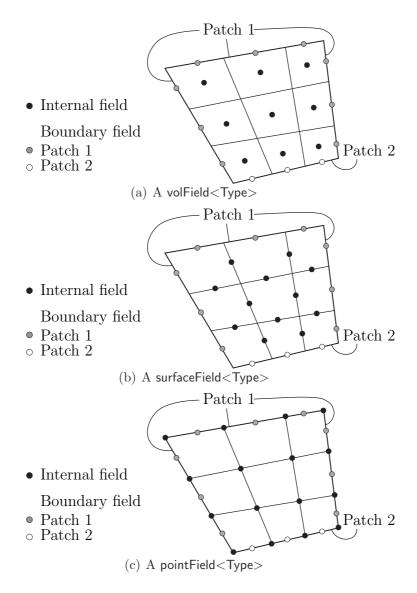


Figure 2.4: Types of geometricField<Type> defined on a mesh with 2 boundary patches (in 2 dimensions for simplicity)

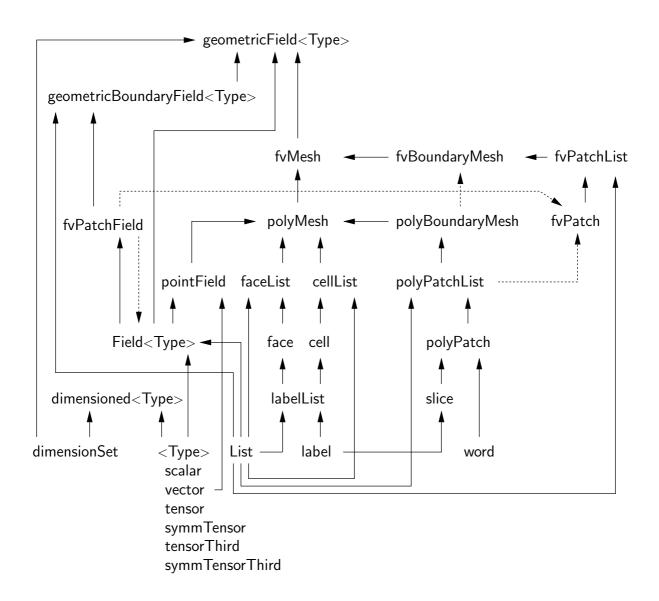


Figure 2.5: Basic class structure leading to geometricField<Type>

to fvm and fvc respectively. fvm and fvc contain static functions, representing differential operators, e.g. ∇^2 , $\nabla \cdot$ and $\partial/\partial t$, that discretise geometricField<Type>s. The purpose of defining these functions within two classes, fvm and fvc, rather than one, is to distinguish:

- functions of fvm that calculate implicit derivatives of and return an fvMatrix<Type>
- some functions of fvc that calculate explicit derivatives and other explicit calculations, returning a geometricField<Type>.

Figure 2.6 shows a geometricField<Type> defined on a mesh with 2 boundary patches and illustrates the explicit operations merely transform one field to another and drawn in 2D for simplicity.

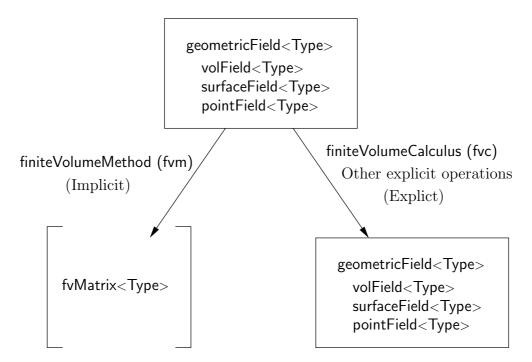


Figure 2.6: A geometricField<Type> and its operators

Table 2.2 lists the main functions that are available in fvm and fvc to discretise terms that may be found in a PDE. FV discretisation of each term is formulated by first integrating the term over a cell volume V. Most spatial derivative terms are then converted to integrals over the cell surface S bounding the volume using Gauss's theorem

$$\int_{V} \nabla \star \phi \ dV = \int_{S} d\mathbf{S} \star \phi \tag{2.13}$$

where **S** is the surface area vector, ϕ can represent any tensor field and the star notation \star is used to represent any tensor product, *i.e.* inner, outer and cross and the respective derivatives: divergence $\nabla \cdot \phi$, gradient $\nabla \phi$ and $\nabla \times \phi$. Volume and surface integrals are then linearised using appropriate schemes which are described for each term in the following Sections. Some terms are always discretised using one scheme, a selection of schemes is offered in OpenFOAM for the discretisation of other terms. The choice of scheme is either made by a direct specification within the code or it can be read from an input file at job run-time and stored within an fvSchemes class object.

Term description	Implicit /	Text	fvm::/fvc:: functions
	Explicit	expression	·
Laplacian	Imp/Exp	$ abla^2 \phi$	laplacian(phi)
		$\nabla \cdot \Gamma \nabla \phi$	laplacian(Gamma, phi)
Time derivative	Imp/Exp	$\frac{\partial \phi}{\partial t}$	ddt(phi)
		$\frac{\partial \rho \phi}{\partial t}$	ddt(rho,phi)
Second time derivative	Imp/Exp	$\frac{\partial}{\partial t} \left(\rho \frac{\partial \phi}{\partial t} \right)$	d2dt2(rho, phi)
Convection	Imp/Exp	$\nabla \cdot (\psi)$	div(psi,scheme)*
		$\nabla \cdot (\psi \phi)$	div(psi, phi, word)*
			div(psi, phi)
Divergence	Exp	$\nabla \cdot \chi$	div(chi)
Gradient	Exp	$\nabla \chi$	grad(chi)
		$ abla \phi$	gGrad(phi)
			lsGrad(phi)
			<pre>snGrad(phi)</pre>
			<pre>snGradCorrection(phi)</pre>
Grad-grad squared	Exp	$ \nabla\nabla\phi ^2$	sqrGradGrad(phi)
Curl	Exp	$\nabla \times \phi$	curl(phi)
Source	Imp	$ ho\phi$	Sp(rho,phi)
±c	Imp/Exp†	11.11	SuSp(rho,phi)

†fvm::SuSp source is discretised implicit or explicit depending on the sign of rho. †An explicit source can be introduced simply as a vol<Type>Field, e.g.rho*phi. Function arguments can be of the following classes:

phi: vol<Type>Field

Gamma: scalar volScalarField, surfaceScalarField, volTensorField, surfaceTensorField.

rho: scalar, volScalarField psi: surfaceScalarField.

 ${\tt chi: surface < Type > Field, vol < Type > Field.}$

Table 2.2: Discretisation of PDE terms in OpenFOAM

2.4.1 The Laplacian term

The Laplacian term is integrated over a control volume and linearised as follows:

$$\int_{V} \nabla \cdot (\Gamma \nabla \phi) \ dV = \int_{S} d\mathbf{S} \cdot (\Gamma \nabla \phi) = \sum_{f} \Gamma_{f} \mathbf{S}_{f} \cdot (\nabla \phi)_{f}$$
(2.14)

The face gradient discretisation is implicit when the length vector \mathbf{d} between the centre of the cell of interest P and the centre of a neighbouring cell N is orthogonal to the face plane, *i.e.* parallel to \mathbf{S}_f :

$$\mathbf{S}_f \bullet (\nabla \phi)_f = |S_f| \frac{\phi_N - \phi_P}{|\mathbf{d}|} \tag{2.15}$$

In the case of non-orthogonal meshes, an additional explicit term is introduced which is evaluated by interpolating cell centre gradients, themselves calculated by central differencing cell centre values.

2.4.2 The convection term

The convection term is integrated over a control volume and linearised as follows:

$$\int_{V} \nabla \cdot (\rho \mathbf{U}\phi) \ dV = \int_{S} d\mathbf{S} \cdot (\rho \mathbf{U}\phi) = \sum_{f} \mathbf{S}_{f} \cdot (\rho \mathbf{U})_{f} \phi_{f} = \sum_{f} F \phi_{f}$$
 (2.16)

The face field ϕ_f can be evaluated using a variety of schemes:

Central differencing (CD) is second-order accurate but unbounded

$$\phi_f = f_x \phi_P + (1 - f_x)\phi_N \tag{2.17}$$

where $f_x \equiv \overline{fN}/\overline{PN}$ where \overline{fN} is the distance between f and cell centre N and \overline{PN} is the distance between cell centres P and N.

Upwind differencing (UD) determines ϕ_f from the direction of flow and is bounded at the expense of accuracy

$$\phi_f = \begin{cases} \phi_P & \text{for } F \ge 0\\ \phi_N & \text{for } F < 0 \end{cases}$$
 (2.18)

Blended differencing (BD) schemes combine UD and CD in an attempt to preserve boundedness with reasonable accuracy,

$$\phi_f = (1 - \gamma) (\phi_f)_{UD} + \gamma (\phi_f)_{CD}$$

$$(2.19)$$

OpenFOAM has several implementations of the Gamma differencing—scheme to select the blending coefficient γ but it offers other well-known schemes such as van Leer, SUPERBEE, MINMOD etc..

2.4.3 First time derivative

The first time derivative $\partial/\partial t$ is integrated over a control volume as follows:

$$\frac{\partial}{\partial t} \int_{V} \rho \phi \ dV \tag{2.20}$$

The term is discretised by simple differencing in time using:

new values $\phi^n \equiv \phi(t + \Delta t)$ at the time step we are solving for;

old values $\phi^o \equiv \phi(t)$ that were stored from the previous time step;

old-old values $\phi^{oo} \equiv \phi(t - \Delta t)$ stored from a time step previous to the last.

One of two discretisation schemes can be declared using the timeScheme keyword in the appropriate input file, described in detail in section 4.4 of the User Guide.

Euler implicit scheme, timeScheme EulerImplicit, that is first order accurate in time:

$$\frac{\partial}{\partial t} \int_{V} \rho \phi \ dV = \frac{(\rho_P \phi_P V)^n - (\rho_P \phi_P V)^o}{\Delta t}$$
 (2.21)

Backward differencing scheme, timeScheme BackwardDifferencing, that is second order accurate in time by storing the old-old values and therefore with a larger overhead in data storage than EulerImplicit:

$$\frac{\partial}{\partial t} \int_{V} \rho \phi \ dV = \frac{3 \left(\rho_P \phi_P V\right)^n - 4 \left(\rho_P \phi_P V\right)^o + \left(\rho_P \phi_P V\right)^{oo}}{2\Delta t} \tag{2.22}$$

2.4.4 Second time derivative

The second time derivative is integrated over a control volume and linearised as follows:

$$\frac{\partial}{\partial t} \int_{V} \rho \frac{\partial \phi}{\partial t} dV = \frac{(\rho_P \phi_P V)^n - 2(\rho_P \phi_P V)^o + (\rho_P \phi_P V)^{oo}}{\Delta t^2}$$
(2.23)

It is first order accurate in time.

2.4.5 Divergence

The divergence term described in this Section is strictly an explicit term that is distinguished from the convection term of Section 2.4.2, *i.e.* in that it is not the divergence of the product of a velocity and dependent variable. The term is integrated over a control volume and linearised as follows:

$$\int_{V} \nabla \cdot \phi \ dV = \int_{S} d\mathbf{S} \cdot \phi = \sum_{f} \mathbf{S}_{f} \cdot \phi_{f}$$
(2.24)

The fvc::div function can take as its argument either a surface<Type>Field, in which case ϕ_f is specified directly, or a vol<Type>Field which is interpolated to the face by central differencing as described in Section 2.4.10:

2.4.6 Gradient

The gradient term is an explicit term that can be evaluated in a variety of ways. The scheme can be evaluated either by selecting the particular grad function relevant to the discretisation scheme, e.g.fvc::gGrad, fvc::lsGrad etc., or by using the fvc::grad function combined with the appropriate timeScheme keyword in an input file

Gauss integration is invoked using the fvc::grad function with timeScheme Gauss or directly using the fvc::gGrad function. The discretisation is performed using the standard method of applying Gauss's theorem to the volume integral:

$$\int_{V} \nabla \phi \ dV = \int_{S} d\mathbf{S} \, \phi = \sum_{f} \mathbf{S}_{f} \phi_{f} \tag{2.25}$$

As with the fvc::div function, the Gaussian integration fvc::grad function can take either a surfaceField<Type> or a volField<Type> as an argument.

Least squares method is based on the following idea:

- 1. a value at point P can be extrapolated to neighbouring point N using the gradient at P;
- 2. the extrapolated value at N can be compared to the actual value at N, the difference being the error;
- 3. if we now minimise the sum of the square of weighted errors at all neighbours of P with the respect to the gradient, then the gradient should be a good approximation.

Least squares is invoked using the fvc::grad function with timeScheme leastSquares or directly using the fvc::lsGrad function. The discretisation is performed as by first calculating the tensor G at every point P by summing over neighbours N:

$$\mathbf{G} = \sum_{N} w_{N}^{2} \mathbf{dd} \tag{2.26}$$

where **d** is the vector from P to N and the weighting function $w_N = 1/|\mathbf{d}|$. The gradient is then evaluated as:

$$(\nabla \phi)_P = \sum_N w_N^2 \mathbf{G}^{-1} \cdot \mathbf{d} (\phi_N - \phi_P)$$
 (2.27)

Surface normal gradient The gradient normal to a surface $\mathbf{n}_f \cdot (\nabla \phi)_f$ can be evaluated at cell faces using the scheme

$$(\nabla \phi)_f = \frac{\phi_N - \phi_P}{|\mathbf{d}|} \tag{2.28}$$

This gradient is called by the function fvc::snGrad and returns a surfaceField<Type>. The scheme is directly analogous to that evaluated for the Laplacian discretisation scheme in Section 2.4.1, and in the same manner, a correction can be introduced to improve the accuracy of this face gradient in the case of non-orthogonal meshes. This correction is called using the function fvc::snGradCorrection [Check**].

2.4.7 Grad-grad squared

The grad-grad squared term is evaluated by: taking the gradient of the field; taking the gradient of the resulting gradient field; and then calculating the magnitude squared of the result. The mathematical expression for grad-grad squared of ϕ is $|\nabla (\nabla \phi)|^2$.

2.4.8 Curl

The curl is evaluated from the gradient term described in Section 2.4.6. First, the gradient is discretised and then the curl is evaluated using the relationship from Equation 2.7, repeated here for convenience

$$\nabla \times \phi = 2 * (\text{skew } \nabla \phi)$$

2.4.9 Source terms

Source terms can be specified in 3 ways

Explicit Every explicit term is a volField<Type>. Hence, an explicit source term can be incorporated into an equation simply as a field of values. For example if we wished to solve Poisson's equation $\nabla^2 \phi = f$, we would define phi and f as volScalarField and then do

Implicit An implicit source term is integrated over a control volume and linearised by

$$\int_{V} \rho \phi \ dV = \rho_P V_P \phi_P \tag{2.29}$$

Implicit/Explicit The implicit source term changes the coefficient of the diagonal of the matrix. Depending on the sign of the coefficient and matrix terms, this will either increase or decrease diagonal dominance of the matrix. Decreasing the diagonal dominance could cause instability during iterative solution of the matrix equation. Therefore OpenFOAM provides a mixed source discretisation procedure that is implicit when the coefficients that are greater than zero, and explicit for the coefficients less than zero. In mathematical terms the matrix coefficient for node P is $V_P \max(\rho_P, 0)$ and the source term is $V_P \phi_P \min(\rho_P, 0)$.

2.4.10 Other explicit discretisation schemes

There are some other discretisation procedures that convert volField<Type>s into surface<Type>Fields and visa versa.

Surface integral fvc::surfaceIntegrate performs a summation of surface<Type>Field face values bounding each cell and dividing by the cell volume, i.e. $(\sum_f \phi_f)/V_P$. It returns a volField<Type>.

Surface sum fvc::surfaceSum performs a summation of surface<Type>Field face values bounding each cell, i.e. $\sum_f \phi_f$ returning a volField<Type>.

Average fvc::average produces an area weighted average of surface<Type>Field face values, i.e. $(\sum_f S_f \phi_f) / \sum_f S_f$, and returns a volField<Type>.

Reconstruct

Face interpolate The geometric<Type>Field function faceInterpolate() interpolates volField<Type> cell centre values to cell faces using central differencing, returning a surface<Type>Field.

2.5 Temporal discretisation

Although we have described the discretisation of temporal derivatives in Sections 2.4.3 and 2.4.4, we need to consider how to treat the spatial derivatives in a transient problem. If we denote all the spatial terms as $\mathcal{A}\phi$ where \mathcal{A} is any spatial operator, e.g. Laplacian, then we can express a transient PDE in integral form as

$$\int_{t}^{t+\Delta t} \left[\frac{\partial}{\partial t} \int_{V} \rho \phi \ dV + \int_{V} \mathcal{A}\phi \ dV \right] \ dt = 0$$
 (2.30)

Using the Euler implicit method of Equation 2.21, the first term can be expressed as

$$\int_{t}^{t+\Delta t} \left[\frac{\partial}{\partial t} \int_{V} \rho \phi \ dV \right] dt = \int_{t}^{t+\Delta t} \frac{(\rho_{P} \phi_{P} V)^{n} - (\rho_{P} \phi_{P} V)^{o}}{\Delta t} dt$$

$$= \frac{(\rho_{P} \phi_{P} V)^{n} - (\rho_{P} \phi_{P} V)^{o}}{\Delta t} \Delta t \tag{2.31}$$

The second term can be expressed as

$$\int_{t}^{t+\Delta t} \left[\int_{V} \mathcal{A}\phi \ dV \right] \ dt = \int_{t}^{t+\Delta t} \mathcal{A}^{*}\phi \ dt \tag{2.32}$$

where \mathcal{A}^* represents the spatial discretisation of \mathcal{A} . The time integral can be discretised in three ways:

Euler implicit uses implicit discretisation of the spatial terms, thereby taking current values ϕ^n .

$$\int_{t}^{t+\Delta t} \mathcal{A}^* \phi \ dt = \mathcal{A}^* \phi^n \Delta t \tag{2.33}$$

It is first order accurate in time, guarantees boundedness and is unconditionally stable.

Explicit uses explicit discretisation of the spatial terms, thereby taking old values ϕ^o .

$$\int_{t}^{t+\Delta t} \mathcal{A}^* \phi \ dt = \mathcal{A}^* \phi^o \Delta t \tag{2.34}$$

It is first order accurate in time and is unstable if the Courant number Co is greater than 1. The Courant number is defined as

$$Co = \frac{\mathbf{U}_f \cdot \mathbf{d}}{|\mathbf{d}|^2 \Delta t} \tag{2.35}$$

where \mathbf{U}_f is a characteristic velocity, e.g. velocity of a wave front, velocity of flow.

Crank Nicholson uses the trapezoid rule to discretise the spatial terms, thereby taking a mean of current values ϕ^n and old values ϕ^o .

$$\int_{t}^{t+\Delta t} \mathcal{A}^* \phi \ dt = \mathcal{A}^* \left(\frac{\phi^n + \phi^o}{2} \right) \Delta t \tag{2.36}$$

It is second order accurate in time, is unconditionally stable but does not guarantee boundedness.

2.5.1 Treatment of temporal discretisation in OpenFOAM

At present the treatment of the temporal discretisation is controlled by the implementation of the spatial derivatives in the PDE we wish to solve. For example, let us say we wish to solve a transient diffusion equation

$$\frac{\partial \phi}{\partial t} = \kappa \nabla^2 \phi \tag{2.37}$$

An Euler implicit implementation of this would read

```
solve(fvm::ddt(phi) == kappa*fvm::laplacian(phi))
```

where we use the fvm class to discretise the Laplacian term implicitly. An explicit implementation would read

```
solve(fvm::ddt(phi) == kappa*fvc::laplacian(phi))
```

where we now use the fvc class to discretise the Laplacian term explicitly. The Crank Nicholson scheme can be implemented by the mean of implicit and explicit terms:

```
solve
   (
   fvm::ddt(phi)
   ==
   kappa*0.5*(fvm::laplacian(phi) + fvc::laplacian(phi))
)
```

2.6 Boundary Conditions

Boundary conditions are required to complete the problem we wish to solve. We therefore need to specify boundary conditions on all our boundary faces. Boundary conditions can be divided into 2 types:

Dirichlet prescribes the value of the dependent variable on the boundary and is therefore termed 'fixed value' in this guide;

Neumann prescribes the gradient of the variable normal to the boundary and is therefore termed 'fixed gradient' in this guide.

When we perform discretisation of terms that include the sum over faces \sum_f , we need to consider what happens when one of the faces is a boundary face.

Fixed value We specify a fixed value at the boundary ϕ_b

- We can simply substitute ϕ_b in cases where the discretisation requires the value on a boundary face ϕ_f , e.g. in the convection term in Equation 2.16.
- In terms where the face gradient $(\nabla \phi)_f$ is required, e.g. Laplacian, it is calculated using the boundary face value and cell centre value,

$$\mathbf{S}_f \bullet (\nabla \phi)_f = |S_f| \frac{\phi_b - \phi_P}{|\mathbf{d}|} \tag{2.38}$$

Fixed gradient The fixed gradient boundary condition g_b is a specification on inner product of the gradient and unit normal to the boundary, or

$$g_b = \left(\frac{\mathbf{S}}{|\mathbf{S}|} \bullet \nabla \phi\right)_f \tag{2.39}$$

• When discretisation requires the value on a boundary face ϕ_f we must interpolate the cell centre value to the boundary by

$$\phi_f = \phi_P + \mathbf{d} \cdot (\nabla \phi)_f$$

$$= \phi_P + |\mathbf{d}| q_h$$
(2.40)

• ϕ_b can be directly substituted in cases where the discretisation requires the face gradient to be evaluated,

$$\mathbf{S}_f \bullet (\nabla \phi)_f = |S_f| \, g_b \tag{2.41}$$

2.6.1 Physical boundary conditions

The specification of boundary conditions is usually an engineer's interpretation of the true behaviour. Real boundary conditions are generally defined by some physical attributes rather than the numerical description as described of the previous Section. In incompressible fluid flow there are the following physical boundaries

Inlet The velocity field at the inlet is supplied and, for consistency, the boundary condition on pressure is zero gradient.

Outlet The pressure field at the outlet is supplied and a zero gradient boundary condition on velocity is specified.

No-slip impermeable wall The velocity of the fluid is equal to that of the wall itself, *i.e.* a fixed value condition can be specified. The pressure is specified zero gradient since the flux through the wall is zero.

In a problem whose solution domain and boundary conditions are symmetric about a plane, we only need to model half the domain to one side of the symmetry plane. The boundary condition on the plane must be specified according to

Symmetry plane The symmetry plane condition specifies the component of the gradient normal to the plane should be zero. [Check**]

Chapter 3

Examples of the use of OpenFOAM

In this section we shall describe several test cases supplied with the OpenFOAM distribution. The intention is to provide example cases, including those in the tutorials in chapter 2 of the User Guide, for every standard solver. The examples are designed to introduce certain tools and features of OpenFOAM, e.g. within pre-/post-processing, numerical schemes, algorithms. They also provide a means for validation of solvers although that is not their principal function.

Each example contains a description of the problem: the geometry, initial and boundary conditions, a brief description of the equations being solved, models used, and physical properties required. The solution domain is selected which may be a portion of the original geometry, e.g. if we introduce symmetry planes. The method of meshing, usually blockMesh, is specified; of course the user can simply view the mesh since every example is distributed with the polyMesh directory containing the data files that describe the mesh.

The examples coexist with the tutorials in the *tutorials* subdirectory of the OpenFOAM installation. They are organised into a set of subdirectories by solver, *e.g.* all the icoFoam cases are stored within a subdirectory *icoFoam*. Before running a particular example, the user is urged to copy it into their user account. We recommend that the user stores all OpenFOAM cases in a directory we recommend that the tutorials are copied into a directory *\$FOAM_RUN*. If this directory structure has not yet been created in the user's account, it can be created with

```
mkdir -p $FOAM_RUN
```

The tutorials can then be copied into this directory with

```
cp -r $FOAM_TUTORIALS/* $FOAM_RUN
```

3.1 Flow around a cylinder

In this example we shall investigate potential flow around a cylinder using potentialFoam. This example introduces the following OpenFOAM features:

- non-orthogonal meshes;
- generating an analytical solution to a problem in OpenFOAM.

3.1.1 Problem specification

The problem is defined as follows:

Solution domain The domain is 2 dimensional and consists of a square domain with a cylinder collocated with the centre of the square as shown in Figure 3.1.

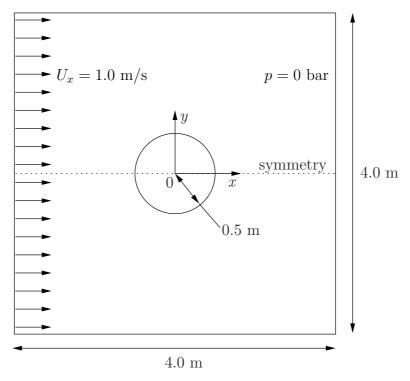


Figure 3.1: Geometry of flow round a cylinder

Governing equations

• Mass continuity for an incompressible fluid

$$\nabla \cdot \mathbf{U} = 0 \tag{3.1}$$

• Pressure equation for an incompressible, irrotational fluid assuming steadystate conditions

$$\nabla^2 p = 0 \tag{3.2}$$

Boundary conditions

- Inlet (left) with fixed velocity U = (1, 0, 0) m/s.
- Outlet (right) with a fixed pressure p = 0 Pa.
- No-slip wall (bottom);
- Symmetry plane (top).

Initial conditions U = 0 m/s, p = 0 Pa — required in OpenFOAM input files but not necessary for the solution since the problem is steady-state.

Solver name potentialFoam: a potential flow code, *i.e.* assumes the flow is incompressible, steady, irrotational, inviscid and it ignores gravity.

Case name cylinder case located in the \$FOAM_TUTORIALS/potentialFoam directory.

3.1.2 Note on potentialFoam

potentialFoam is a useful solver to validate OpenFOAM since the assumptions of potential flow are such that an analytical solution exists for cases whose geometries are relatively simple. In this example of flow around a cylinder an analytical solution exists with which we can compare our numerical solution. potentialFoam can also be run more like a utility to provide a (reasonably) conservative initial U field for a problem. When running certain cases, this can useful for avoiding instabilities due to the initial field being unstable. In short, potentialFoam creates a conservative field from a non-conservative initial field supplied by the user.

3.1.3 Mesh generation

Mesh generation using blockMesh has been described in tutorials in the User Guide. In this case, the mesh consists of 10 blocks as shown in Figure 3.2. Remember that all

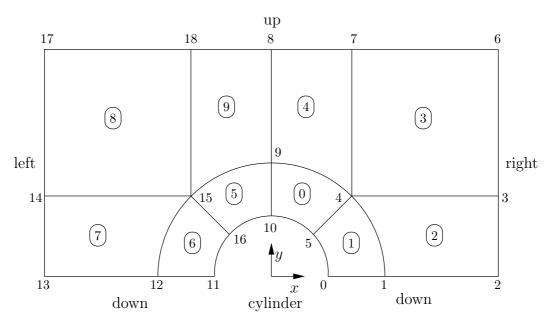


Figure 3.2: Blocks in cylinder geometry

meshes are treated as 3 dimensional in OpenFOAM. If we wish to solve a 2 dimensional problem, we must describe a 3 dimensional mesh that is only one cell thick in the third direction that is not solved. In Figure 3.2 we show only the back plane of the geometry, along z = -0.5, in which the vertex numbers are numbered 0-18. The other 19 vertices in the front plane, z = +0.5, are numbered in the same order as the back plane, as shown in the mesh description file below:

```
2
                                      OpenFOAM: The Open Source CFD Toolbox
                    ield
3
                   O peration
                                      Version:
                                                 2.1.0
                                                 www.OpenFOAM.org
5
                   A nd
                                      Web:
                   M anipulation
6
    FoamFile
                      2.0;
         version
         format
                      ascii;
11
                      dictionary
         class
                      blockMeshDict
13
         object
14
15
16
    convertToMeters 1;
```

```
18
    vertices #codeStream
19
20
         codeInclude
21
         #{
22
              #include "pointField.H"
23
24
         #};
25
         code
26
27
              pointField points(19);
28
              points[0]
                          = point(0.5, 0, -0.5);
29
                           = point(1, 0, -0.5);
              points[1]
30
              points[2]
                          = point(2, 0, -0.5);
                          = point(2, 0.707107, -0.5);
              points[3]
32
                           = point(0.707107, 0.707107, -0.5);
              points[4]
33
                           = point(0.353553, 0.353553, -0.5);
34
              points[5]
              points[6]
                           = point(2, 2, -0.5);
35
              points[7]
                           = point(0.707107, 2, -0.5);
                          = point(0, 2, -0.5);
= point(0, 1, -0.5);
              points[8]
37
              points[9]
38
              points[10]
                          = point(0, 0.5, -0.5)
              points[11] = point(-0.5, 0, -0.5);
40
              points[12] = point(-1, 0, -0.5);
41
              points[13] = point(-2, 0, -0.5);
42
              points[14] = point(-2, 0.707107,
                                                    -0.5);
43
                          = point(-0.707107, 0.707107, -0.5);
              points[15]
              points[16] = point(-0.353553, 0.353553, -0.5);
45
              points[17] = point(-2, 2, -0.5);
46
              points[18] = point(-0.707107, 2, -0.5);
47
              // Duplicate z points
49
              label sz = points.size();
50
              points.setSize(2*sz);
              for (label i = 0; i < sz; i++)
52
53
                   const point& pt = points[i];
54
                   points[i+sz] = point(pt.x(), pt.y(), -pt.z());
55
              }
57
              os
                  << points;
         #};
59
    };
60
61
62
    blocks
63
64
         hex (5 4 9 10 24 23 28 29) (10 10 1) simpleGrading (1 1 1)
65
         hex (0 1 4 5 19 20 23 24) (10 10 1) simpleGrading (1 1 1)
66
         hex (1 2 3 4 20 21 22 23) (20 10 1) simpleGrading (1 1 1)
67
         hex (4 3 6 7 23 22 25 26) (20 20 1) simpleGrading (1 1 1)
68
         hex (9 4 7 8 28 23 26 27) (10 20 1) simpleGrading (1 1 1)
69
         hex (15 16 10 9 34 35 29 28) (10 10 1) simpleGrading (1 1 1)
70
         hex (12 11 16 15 31 30 35 34) (10 10 1) simpleGrading (1 1 1)
71
         hex (13 12 15 14 32 31 34 33) (20 10 1) simpleGrading (1 1 1)
72
         hex (14 15 18 17 33 34 37 36) (20 20 1) simpleGrading (1 1 1)
         hex (15 9 8 18 34 28 27 37) (10 20 1) simpleGrading (1 1 1)
74
    );
75
76
    edges
77
78
         arc 0 5 (0.469846 0.17101 -0.5)
         arc 5 10 (0.17101 0.469846 -0.5)
arc 1 4 (0.939693 0.34202 -0.5)
arc 4 9 (0.34202 0.939693 -0.5)
         arc 19 24 (0.469846 0.17101 0.5)
arc 24 29 (0.17101 0.469846 0.5)
                      (0.469846 0.17101 0.5)
84
         arc 20 23
arc 23 28
                     (0.939693 0.34202 0.5)
(0.34202 0.939693 0.5)
(-0.469846 0.17101 -0.5)
(-0.17101 0.469846 -0.5)
         arc 11 16
88
         arc 16 10
                    (-0.939693 0.34202 -0.5)
(-0.34202 0.939693 -0.5)
         arc 12
89
                 15
         arc 15 9
90
         arc 30 35
arc 35 29
                     (-0.469846 0.17101 0.5)
                     (-0.17101 0.469846 0.5)
92
                     (-0.939693 0.34202
             31
                 34
93
         arc
         arc 34 28
                    (-0.34202 0.939693 0.5)
94
    );
95
96
```

```
boundary
98
           down
99
100
                 type symmetryPlane;
101
                 faces
102
103
                      (0 1 20 19)
(1 2 21 20)
(12 11 30 31)
(13 12 31 32)
104
105
106
107
                 );
108
109
           right
110
111
112
                 type patch;
                 faces
113
114
115
116
                 );
117
118
119
           up
120
                 type symmetryPlane;
121
122
123
                      (7 8 27 26)
(6 7 26 25)
(8 18 37 27)
(18 17 36 37)
124
125
126
127
                 );
           }
left
129
130
132
                 type patch;
133
134
                      (14 13 32 33)
(17 14 33 36)
136
137
           cylinder
139
140
                 type symmetryPlane;
141
                 faces
142
143
                       (10 5 24 29)
144
                      (5 0 19 24)
(16 10 29 35)
(11 16 35 30)
145
146
147
                 );
148
           }
149
150
151
      mergePatchPairs
152
153
154
155
```

3.1.4 Boundary conditions and initial fields

Using FoamX or editing case files by hand, set the boundary conditions in accordance with the problem description in Figure 3.1, i.e. the left boundary should be an Inlet, the right boundary should be an Outlet and the down and cylinder boundaries should be symmetryPlane. The top boundary conditions is chosen so that we can make the most genuine comparison with our analytical solution which uses the assumption that the domain is infinite in the y direction. The result is that the normal gradient of U is small along a plane coinciding with our boundary. We therefore impose the condition that the normal component is zero, i.e. specify the boundary as a symmetryPlane, thereby ensuring that the comparison with the analytical is reasonable.

3.1.5 Running the case

No fluid properties need be specified in this problem since the flow is assumed to be incompressible and inviscid. In the *system* subdirectory, the *controlDict* specifies the control parameters for the run. Note that since we assume steady flow, we only run for 1 time step:

```
---*- C++ -*---
2
                   F ield
                                       OpenFOAM: The Open Source CFD Toolbox
3
4
                   O peration
                                       Version:
                                                  2.1.0
5
                   A nd
                                       Web:
                                                   www.OpenFOAM.org
                   {\tt M} anipulation
6
    FoamFile
10
         version
                       2.0;
11
         format
                       ascii;
                       dictionary;
"system";
         class
         location
         object
14
                       controlDict;
15
                      * * * * * * *
16
17
    application
                       potentialFoam;
18
19
    startFrom
                       startTime;
20
21
    startTime
                       0;
22
23
    stopAt
                       endTime;
24
25
    endTime
                       1;
26
27
    deltaT
                       1;
28
29
    writeControl
                       timeStep;
30
31
    writeInterval
                       1;
32
33
    purgeWrite
34
35
    writeFormat
                       ascii;
36
37
38
    writePrecision 6;
39
    writeCompression off;
40
41
42
    timeFormat
                       general;
43
    timePrecision
44
46
    runTimeModifiable true;
47
    functions
48
         difference
              // Load the library containing the 'coded' functionObject
52
             functionObjectLibs ("libutilityFunctionObjects.so");
53
              type coded;
54
             // Name of on-the-fly generated functionObject
redirectType error;
55
56
              code
                  // Lookup U
                  Info<< "Looking up field U\n" << endl;
60
                  const volVectorField& U = mesh().lookupObject<volVectorField>("U");
61
62
                  Info<< "Reading inlet velocity uInfX\n" << endl;</pre>
63
64
                  scalar ULeft = 0.0;
label leftI = mesh().boundaryMesh().findPatchID("left");
65
66
                  const fvPatchVectorField& fvp = U.boundaryField()[leftI];
67
                  if (fvp.size())
68
                  {
                       ULeft = fvp[0].x();
70
71
                  reduce(ULeft, maxOp<scalar>());
72
73
                  dimensionedScalar uInfX
74
```

```
(
                      "uInfx"
76
                      dimensionSet(0, 1, -1, 0, 0),
77
78
                      ULeft.
                  );
79
80
                  Info << "U at inlet = " << uInfX.value() << " m/s" << endl;</pre>
81
82
83
                  scalar magCylinder = 0.0;
84
                  label cylI = mesh().boundaryMesh().findPatchID("cylinder");
85
                  const fvPatchVectorField& cylFvp = mesh().C().boundaryField()[cylI];
86
                  if (cylFvp.size())
87
89
                      magCylinder = mag(cylFvp[0]);
90
                  reduce(magCylinder, maxOp<scalar>());
91
92
                  dimensionedScalar radius
93
94
                      "radius"
95
                      dimensionSet(0, 1, 0, 0, 0),
96
                      magCylinder
97
98
                  );
99
                  Info << "Cylinder radius = " << radius.value() << " m" << endl;</pre>
100
101
                  volVectorField UA
103
                      IOobject
104
105
                          "UA"
106
                          mesh().time().timeName(),
U.mesh(),
IOobject::NO_READ,
107
108
109
                          IOobject::AUTO_WRÍTE
110
111
                      )
U
112
                  );
113
114
                  Info<< "\nEvaluating analytical solution" << endl;</pre>
115
                  const volVectorField& centres = UA.mesh().C();
117
                  volScalarField magCentres(mag(centres));
118
                  volScalarField theta(acos((centres & vector(1,0,0))/magCentres));
119
120
                  volVectorField cs2theta
121
122
                      cos(2*theta)*vector(1,0,0)
123
                     sin(2*theta)*vector(0,1,0)
124
125
126
                  UA = uInfX*(dimensionedVector(vector(1,0,0))
127
                    - pow((radius/magCentres),2)*cs2theta);
128
129
                  // Force writing of UA (since time has not changed)
130
132
                  volScalarField error("error", mag(U-UA)/mag(UA));
133
134
                  Info<<"Writing relative error in U to " << error.objectPath()</pre>
                      << endl;
137
                  error.write();
138
             #};
139
         }
140
141
142
143
```

potentialFoam executes an iterative loop around the pressure equation which it solves in order that explicit terms relating to non-orthogonal correction in the Laplacian term may be updated in successive iterations. The number of iterations around the pressure equation is controlled by the nNonOrthogonalCorrectors keyword in *controlDict*. In the first instance we can set nNonOrthogonalCorrectors to 0 so that no loops are performed, *i.e.* the pressure equation is solved once, and there is no non-orthogonal correction. The solution is shown in Figure 3.3(a) (at t = 1, when the steady-state simulation is complete). We expect the solution to show smooth streamlines passing across the domain

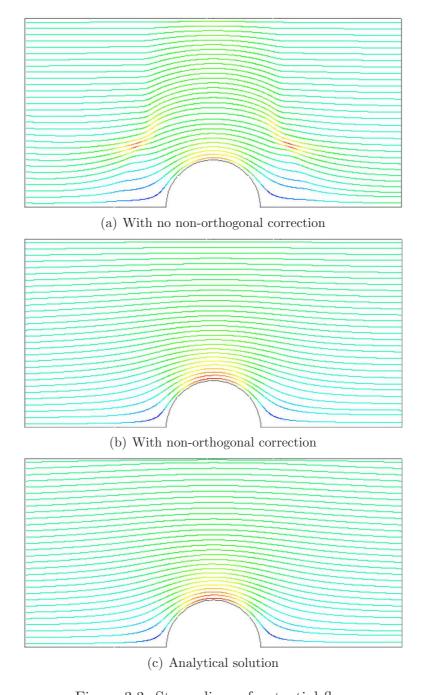


Figure 3.3: Streamlines of potential flow

as in the analytical solution in Figure 3.3(c), yet there is clearly some error in the regions where there is high non-orthogonality in the mesh, e.g. at the join of blocks 0, 1 and 3. The case can be run a second time with some non-orthogonal correction by setting nNonOrthogonalCorrectors to 3. The solution shows smooth streamlines with no significant error due to non-orthogonality as shown in Figure 3.3(b).

3.2 Steady turbulent flow over a backward-facing step

In this example we shall investigate steady turbulent flow over a backward-facing step. The problem description is taken from one used by Pitz and Daily in an experimental investigation [**] against which the computed solution can be compared. This example introduces the following OpenFOAM features for the first time:

- generation of a mesh using blockMesh using full mesh grading capability;
- steady turbulent flow.

3.2.1 Problem specification

The problem is defined as follows:

Solution domain The domain is 2 dimensional, consisting of a short inlet, a backward-facing step and converging nozzle at outlet as shown in Figure 3.4.

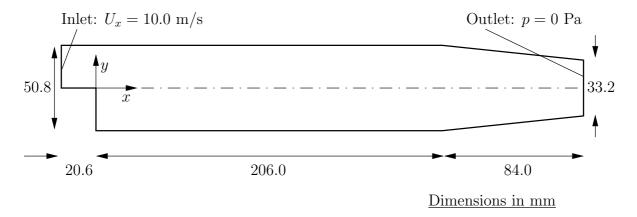


Figure 3.4: Geometry of backward-facing step

Governing equations

• Mass continuity for incompressible flow

$$\nabla \cdot \mathbf{U} = 0 \tag{3.3}$$

• Steady flow momentum equation

$$\nabla \cdot (\mathbf{U}\mathbf{U}) + \nabla \cdot \mathbf{R} = -\nabla p \tag{3.4}$$

where p is kinematic pressure and (in slightly over-simplistic terms) $\mathbf{R} = \nu_{eff} \nabla \mathbf{U}$ is the viscous stress term with an effective kinematic viscosity ν_{eff} , calculated from selected transport and turbulence models.

Initial conditions U = 0 m/s, p = 0 Pa — required in OpenFOAM input files but not necessary for the solution since the problem is steady-state.

Boundary conditions

- Inlet (left) with fixed velocity U = (10, 0, 0) m/s;
- Outlet (right) with fixed pressure p = 0 Pa;
- No-slip walls on other boundaries.

Transport properties

• Kinematic viscosity of air $\nu = \mu/\rho = 18.1 \times 10^{-6}/1.293 = 14.0 \ \mu m^2/s$

$Turbulence\ model$

- Standard $k \epsilon$;
- Coefficients: $C_{\mu} = 0.09$; $C_1 = 1.44$; $C_2 = 1.92$; $\alpha_k = 1$; $\alpha_{\epsilon} = 0.76923$.

Solver name simpleFoam: an implementation for steady incompressible flow.

Case name pitzDaily, located in the \$FOAM_TUTORIALS/simpleFoam directory.

The problem is solved using simpleFoam, so-called as it is an implementation for steady flow using the SIMPLE algorithm [**]. The solver has full access to all the turbulence models in the incompressibleTurbulenceModels library and the non-Newtonian models incompressibleTransportModels library of the standard OpenFOAM release.

3.2.2 Mesh generation

We expect that the flow in this problem is reasonably complex and an optimum solution will require grading of the mesh. In general, the regions of highest shear are particularly critical, requiring a finer mesh than in the regions of low shear. We can anticipate where high shear will occur by considering what the solution might be in advance of any calculation. At the inlet we have strong uniform flow in the x direction and, as it passes over the step, it generates shear on the fluid below, generating a vortex in the bottom half of the domain. The regions of high shear will therefore be close to the centreline of the domain and close to the walls.

The domain is subdivided into 12 blocks as shown in Figure 3.5.

The mesh is 3 dimensional, as always in OpenFOAM, so in Figure 3.5 we are viewing the back plane along z = -0.5. The full set of vertices and blocks are given in the mesh description file below:

```
2
                   F ield
                                       OpenFOAM: The Open Source CFD Toolbox
3
                                       Version: 2.1.0
4
                   O peration
                                                  www.OpenFOAM.org
5
                   A nd
                                       Web:
                   M anipulation
6
    FoamFile
         version
                       2.0;
         format
                       ascii;
                       dictionary;
blockMeshDict;
14
15
16
    convertToMeters 0.001:
17
18
```

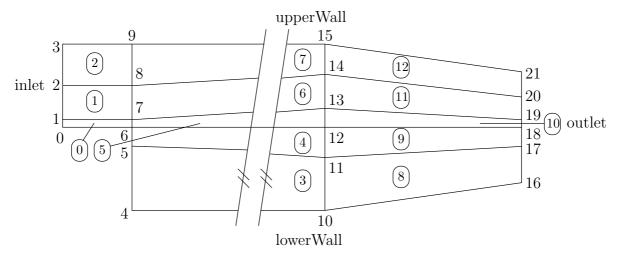


Figure 3.5: Blocks in backward-facing step

```
vertices
19
20
                (-20.6 0 -0.5)
(-20.6 3 -0.5)
(-20.6 12.7 -0.5)
(-20.6 25.4 -0.5)
(0 -25.4 -0.5)
(0 -5 -0.5)
2.1
22
23
24
25
26
                (0 -5 -0.5)

(0 0 -0.5)

(0 3 -0.5)

(0 12.7 -0.5)

(0 25.4 -0.5)

(206 -25.4 -0.5)

(206 -8.5 -0.5)

(206 6 5 -0.5)
27
28
29
30
31
32
33
                (206 6.5 -0.5)
(206 17 -0.5)
(206 25.4 -0.5)
34
35
36
                (290 -16.6 -0.5)
(290 -6.3 -0.5)
(290 0 -0.5)
(290 4.5 -0.5)
37
38
39
40
                (290 11 -0.5)
(290 16.6 -0.5)
41
               (290 11 -0.5)

(290 16.6 -0.5)

(-20.6 0 0.5)

(-20.6 3 0.5)

(-20.6 12.7 0.5)

(-20.6 25.4 0.5)

(0 -25.4 0.5)

(0 0 0.5)

(0 3 0.5)

(0 12.7 0.5)

(0 25.4 0.5)

(0 25.4 0.5)

(206 -25.4 0.5)

(206 -25.4 0.5)

(206 6.5 0.5)

(206 0 0.5)

(206 17 0.5)

(206 25.4 0.5)

(206 25.4 0.5)

(206 17 0.5)

(206 25.4 0.5)

(206 17 0.5)

(206 25.4 0.5)

(209 -16.6 0.5)

(290 -6.3 0.5)

(290 4.5 0.5)

(290 11 0.5)

(290 16.6 0.5)
43
44
^{45}
46
47
49
51
53
55
57
59
60
61
62
63
64
        );
65
66
        blocks
67
68
               hex (0 6 7 1 22 28 29 23) (18 7 1) simpleGrading (0.5 1.8 1)
69
70
               hex (1 7 8 2 23 29 30 24) (18 10 1) simpleGrading (0.5 4 1)
               hex (2 8 9 3 24 30 31 25) (18 13 1) simpleGrading (0.5 0.25 1)
71
               hex (4 10 11 5 26 32 33 27) (180 18 1) simpleGrading (4 1 1)
72
               hex (5 11 12 6 27 33 34 28)
                                                                     (180 9 1) edgeGrading (4 4 4 4 0.5 1 1 0.5 1 1 1 1)
73
               hex (6 12 13 7 28 34 35 29) (180 7 1) edgeGrading (4 4 4 4 1.8 1 1 1.8 1 1 1)
74
               hex (7 13 14 8 29 35 36 30) (180 10 1) edgeGrading (4 4 4 4 4 1 1 4 1 1 1 1)
75
               hex (8 14 15 9 30 36 37 31) (180 13 1) simpleGrading (4 0.25 1)
76
               hex (10 16 17 11 32 38 39 33) (25 18 1) simpleGrading (2.5 1 1)
77
```

```
hex (11 17 18 12 33 39 40 34) (25 9 1) simpleGrading (2.5 1 1)
 78
                hex (12 18 19 13 34 40 41 35) (25 7 1) simpleGrading (2.5 1 1)
 79
                 hex (13 19 20 14 35 41 42 36) (25 10 1) simpleGrading (2.5 1 1)
 80
                 hex (14 20 21 15 36 42 43 37) (25 13 1) simpleGrading (2.5 0.25 1)
 81
 82
 83
         edges
 84
 85
 86
 87
         boundary
 88
 89
                inlet {
 90
 91
                         type patch;
faces
 92
 93
 94
                                 (0 22 23 1)
(1 23 24 2)
(2 24 25 3)
 95
 96
 97
                         );
 98
 99
                outlet {
100
101
                         type patch;
102
                         faces
103
104
                                        17 39 38)
105
                                 (16
                                 (17 18 40 39)
(18 19 41 40)
(19 20 42 41)
(20 21 43 42)
106
107
109
110
                        );
111
                 upperWall
112
113
                         type wall;
114
                         faces
115
116
                                 (3 25 31 9)
(9 31 37 15)
(15 37 43 21)
117
118
119
                        );
120
121
                 lowerWall
122
123
                         type wall;
faces
124
125
126
                                 (0 6 28 22)
(6 5 27 28)
(5 4 26 27)
(4 10 32 26)
127
128
129
130
                                 (10 16 38 32)
131
                         );
132
133
                 frontAndBack
134
135
                         type empty;
136
137
                         faces
                                (22 28 29 23)

(23 29 30 24)

(24 30 31 25)

(26 32 33 27)

(27 33 34 28)

(28 34 35 29)

(29 35 36 30)

(30 36 37 31)

(32 38 39 33)

(33 39 40 34)

(34 40 41 35)

(35 41 42 36)

(36 42 43 37)

(0 1 7 6)

(1 2 8 7)

(2 3 9 8)

(4 5 11 10)

(5 6 12 11)

(6 7 13 12)

(7 8 14 13)

(8 9 15 14)

(10 11 17 16)

(11 12 18 17)

(12 13 19 18)
138
139
141
142
145
149
150
151
152
153
154
155
156
157
158
159
160
161
162
```

A major feature of this problem is the use of the full mesh grading capability of blockMesh that is described in section 5.3.1 of the User Guide. The user can see that blocks 4,5 and 6 use the full list of 12 expansion ratios. The expansion ratios correspond to each edge of the block, the first 4 to the edges aligned in the local x_1 direction, the second 4 to the edges in the local x_2 direction and the last 4 to the edges in the local x_3 direction. In blocks 4, 5, and 6, the ratios are equal for all edges in the local x_1 and x_3 directions but not for the edges in the x_2 direction that corresponds in all blocks to the global y. If we consider the ratios used in relation to the block definition in section 5.3.1 of the User Guide, we realize that different gradings have been prescribed along the left and right edges in blocks 4,5 and 6 in Figure 3.5. The purpose of this differential grading is to generate a fine mesh close to the most critical region of flow, the corner of the step, and allow it to expand into the rest of the domain.

The mesh can be generated using blockMesh from the command line or from within FoamX and viewed as described in previous examples.

3.2.3 Boundary conditions and initial fields

The case files can be viewed, or edited from within FoamX or by hand. In this case, we are required to set the initial and boundary fields for velocity \mathbf{U} , pressure p, turbulent kinetic energy k and dissipation rate ε . The boundary conditions can be specified by setting the physical patch types in FoamX: the upper and lower walls are set to Wall, the left patch to Inlet and the right patch to Outlet. These physical boundary conditions require us to specify a fixedValue at the inlet on \mathbf{U} , k and ε . \mathbf{U} is given in the problem specification, but the values of k and ϵ must be chosen by the user in a similar manner to that described in section 2.1.8.1 of the User Guide. We assume that the inlet turbulence is isotropic and estimate the fluctuations to be 5% of \mathbf{U} at the inlet. We have

$$U'_x = U'_y = U'_z = \frac{5}{100} 10 = 0.5 \text{ m/s}$$
 (3.5)

and

$$k = \frac{3}{2}(0.5)^2 = 0.375 \text{ m}^2/\text{s}^2$$
 (3.6)

If we estimate the turbulent length scale l to be 10% of the width of the inlet then

$$\varepsilon = \frac{C_{\mu}^{0.75} k^{1.5}}{l} = \frac{0.09^{0.75} 0.375^{1.5}}{0.1 \times 25.4 \times 10^{-3}} = 14.855 \,\mathrm{m}^2/\mathrm{s}^3$$
(3.7)

At the outlet we need only specify the pressure p = 0Pa.

3.2.4 Case control

The choices of *fvSchemes* are as follows: the timeScheme should be SteadyState; the gradScheme and laplacianScheme should be set as default to Gauss; and, the divScheme should be set to UD to ensure boundedness.

Special attention should be paid to the settings of *fvTolerances*. Although the top level simpleFoam code contains only equations for p and \mathbf{U} , the turbulent model solves equations for k, ε and \mathbf{R} , and tolerance settings are required for all 5 equations. A solverTolerance of 10^{-5} and solverRelativeTolerance of 0.1 are acceptable for all variables with the exception of p when 10^{-6} and 0.01 are recommended. Under-relaxation of the solution is required since the problem is steady. A relaxationFactor of 0.7 is acceptable for \mathbf{U} , k, ε and \mathbf{R} but 0.3 is required for p to avoid numerical instability.

Finally, in *controlDict*, the time step deltaT should be set to 1 since in steady state cases such as this is effectively an iteration counter. With benefit of hindsight we know that the solution requires 1000 iterations reach reasonable convergence, hence endTime is set to 1000. Ensure that the writeFrequency is sufficiently high, e.g. 50, that you will not fill the hard disk with data during run time.

3.2.5 Running the case and post-processing

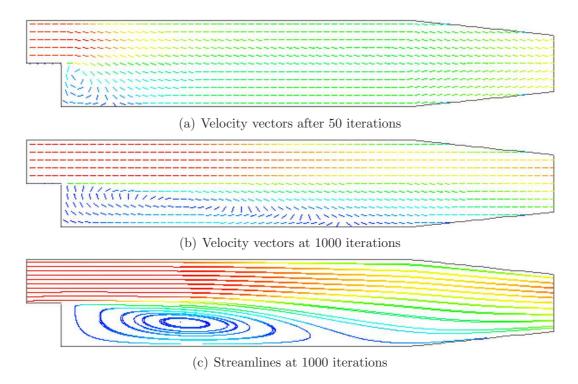


Figure 3.6: Development of a vortex in the backward-facing step.

Run the case and post-process the results. After a few iterations, e.g. 50, a vortex develops beneath the corner of the step that is the height of the step but narrow in the x-direction as shown by the vector plot of velocities is shown Figure 3.6(a). Over several iterations the vortex stretches in the x-direction from the step to the outlet until at 1000 iterations the system reaches a steady-state in which the vortex is fully developed as shown in Figure 3.6(b-c).

3.3 Supersonic flow over a forward-facing step

In this example we shall investigate supersonic flow over a forward-facing step. The problem description involves a flow of Mach 3 at an inlet to a rectangular geometry with a step near the inlet region that generates shock waves.

This example introduces the following OpenFOAM features for the first time:

• supersonic flow;

3.3.1 Problem specification

The problem is defined as follows:

Solution domain The domain is 2 dimensional and consists of a short inlet section followed by a forward-facing step of 20% the height of the section as shown in Figure 3.7

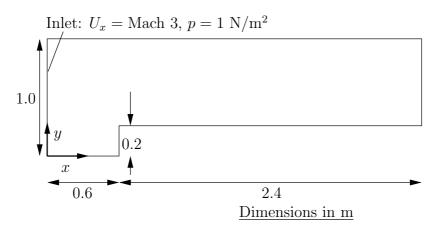


Figure 3.7: Geometry of the forward step geometry

Governing equations

• Mass continuity

$$\frac{\partial \rho}{\partial t} + \nabla \cdot (\rho \mathbf{U}) = 0 \tag{3.8}$$

• Ideal gas

$$p = \rho RT \tag{3.9}$$

• Momentum equation for Newtonian fluid

$$\frac{\partial \rho \mathbf{U}}{\partial t} + \nabla \cdot (\rho \mathbf{U} \mathbf{U}) - \nabla \cdot \mu \nabla \mathbf{U} = -\nabla p \tag{3.10}$$

• Energy equation for fluid (ignoring some viscous terms), $e = C_v T$, with Fourier's Law $\mathbf{q} = -k \nabla T$

$$\frac{\partial \rho e}{\partial t} + \nabla \cdot (\rho \mathbf{U} e) - \nabla \cdot \left(\frac{k}{C_v}\right) \nabla e = p \nabla \cdot \mathbf{U}$$
(3.11)

Initial conditions U = 0 m/s, p = 1 Pa, T = 1 K.

Boundary conditions

- Inlet (left) with fixedValue for velocity U = 3 m/s = Mach 3, pressure p = 1 Pa and temperature T = 1 K;
- Outlet (right) with zeroGradient on U, p and T;
- No-slip adiabatic wall (bottom);

• Symmetry plane (top).

Transport properties

• Dynamic viscosity of air $\mu = 18.1 \mu Pa s$

Thermodynamic properties

- Specific heat at constant volume $C_v = 1.78571 \text{ J/kg K}$
- Gas constant R = 0.714286 J/kg K
- Conductivity $k = 32.3 \, \mu \text{W/m K}$

Case name forwardStep case located in the \$FOAM_TUTORIALS/sonicFoam directory.

Solver name sonicFoam: an implementation for compressible trans-sonic/supersonic laminar gas flow.

The case is designed such that the speed of sound of the gas $c = \sqrt{\gamma RT} = 1$ m/s, the consequence being that the velocities are directly equivalent to the Mach number, e.g. the inlet velocity of 3 m/s is equivalent to Mach 3. This speed of sound calculation can be verified using the relationship for a perfect gas, $C_p - Cv = R$, i.e. the ratio of specific heats

$$\gamma = C_p/C_v = \frac{R}{C_v} + 1 \tag{3.12}$$

3.3.2 Mesh generation

The mesh used in this case is relatively simple, specified with uniform rectangular cells of length 0.06 m in the x direction and 0.05 m in the y direction. The geometry can simply be divided into 3 blocks, one below the top of the step, and two above the step, one either side of the step front. The full set of vertices and blocks are given in the mesh description file below:

```
---*- C++ -*---
2
                                              OpenFOAM: The Open Source CFD Toolbox
3
                         ield
                                              Version: 2.1.0
                       O peration
4
                       A nd
                                                            www.OpenFOAM.org
                       M anipulation
6
7
     FoamFile
8
9
                           2.0;
           version
10
           format
11
           class
                           dictionary
12
13
14
15
16
     convertToMeters 1;
17
18
19
     vertices
20
           (0 0 -0.05)
(0.6 0 -0.05)
(0 0.2 -0.05)
(0.6 0.2 -0.05)
21
22
23
24
25
26
27
28
29
30
              0.2 0.05)
.6 0.2 0.0
31
                      0.05)
32
33
```

```
(0 1 0.05)
(0.6 1 0.05)
(3 1 0.05)
35
36
     );
37
38
     blocks
39
40
          hex (0 1 3 2 8 9 11 10) (25 10 1) simpleGrading (1 1 1)
41
          hex (2 3 6 5 10 11 14 13) (25 40 1) simpleGrading (1 1 1)
42
43
          hex (3 4 7 6 11 12 15 14) (100 40 1) simpleGrading (1 1 1)
     );
44
45
     edges
46
     );
48
49
50
     boundary
51
          inlet {
52
53
               type patch;
54
               faces
55
56
                     (0 \ 8 \ 10 \ 2)
57
                     (2 10 13 5)
58
59
60
          outlet {
61
62
               type patch;
63
               faces
64
65
                     (471512)
66
67
68
          bottom
69
70
71
               type symmetryPlane;
72
73
                     (0 1 9 8)
74
               );
75
          }
76
          top
77
78
               type symmetryPlane;
79
80
81
                       13 14 6)
14 15 7)
82
83
84
85
          obstacle
86
87
               type patch;
88
               faces
89
90
                     (1 \ 3 \ 11 \ 9)
91
                     (3 \ 4 \ 12 \ 11)
92
93
94
     );
95
96
    mergePatchPairs
97
```

3.3.3 Running the case

The case approaches a steady-state at some time after 5 s. The results for pressure at 10 s are shown in Figure 3.8. The results clearly show discontinuities in pressure, *i.e.* shock waves, emanating from ahead of the base of the step.

3.3.4 Exercise

The user can examine the effect on the solution of increasing the inlet velocity.

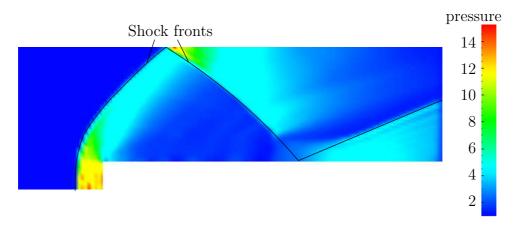


Figure 3.8: Shock fronts in the forward step problem

3.4 Decompression of a tank internally pressurised with water

In this example we shall investigate a problem of rapid opening of a pipe valve close to a pressurised liquid-filled tank. The prominent feature of the result in such cases is the propagation of pressure waves which must therefore be modelled as a compressible liquid.

This tutorial introduces the following OpenFOAM features for the first time:

- Mesh refinement
- Pressure waves in liquids

3.4.1 Problem specification

Solution domain The domain is 2 dimensional and consists of a tank with a small outflow pipe as shown in Figure 3.9

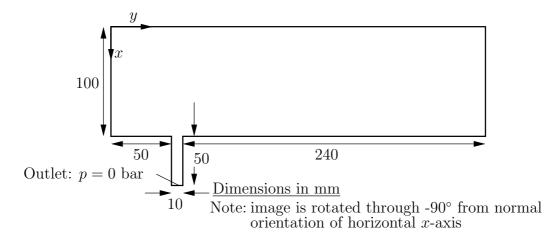


Figure 3.9: Geometry of a tank with outflow pipe

Governing equations This problem requires a model for compressibility ψ in the fluid in order to be able to resolve waves propagating at a finite speed. A barotropic relationship is used to relate density ρ and pressure p are related to ψ .

• Mass continuity

$$\frac{\partial \rho}{\partial t} + \nabla \cdot (\rho \mathbf{U}) = 0 \tag{3.13}$$

• The barotropic relationship

$$\frac{\partial \rho}{\partial p} = \frac{\rho}{K} = \psi \tag{3.14}$$

where K is the bulk modulus

• Equation 3.14 is linearised as

$$\rho \approx \rho_0 + \psi \left(p - p_0 \right) \tag{3.15}$$

where ρ_0 and p_0 are the reference density and pressure respectively such that $\rho(p_0) = \rho_0$.

• Momentum equation for Newtonian fluid

$$\frac{\partial \rho \mathbf{U}}{\partial t} + \nabla \cdot (\rho \mathbf{U} \mathbf{U}) - \nabla \cdot \mu \nabla \mathbf{U} = -\nabla p \tag{3.16}$$

Boundary conditions Using FoamX the following physical boundary conditions can be set:

- outerWall is specified the wall condition;
- axis is specified as the symmetryPlane;
- nozzle is specified as a pressureOutlet where p = 0 bar.
- front and back boundaries are specified as empty.

Initial conditions U = 0 m/s, p = 100 bar.

Transport properties

• Dynamic viscosity of water $\mu = 1.0 \text{ mPa s}$

Thermodynamic properties

- Density of water $\rho = 1000 \text{ kg/m}^3$
- Reference pressure $p_0 = 1$ bar
- Compressibility of water $\psi = 4.54 \times 10^{-7} \text{ s}^2/\text{m}^2$

Solver name sonicLiquidFoam: a compressible sonic laminar liquid flow code.

Case name decompressionTank case located in the \$FOAM_TUTORIALS/sonicLiquidFoam directory.

3.4.2 Mesh Generation

The full geometry is modelled in this case; the set of vertices and blocks are given in the mesh description file below:

```
11
                format
                                       ascii;
                                      dictionary;
blockMeshDict;
12
                class
13
                object
14
15
16
        convertToMeters 0.1;
17
18
        vertices
19
                (0 0 -0.1)

(1 0 -0.1)

(0 0.5 -0.1)

(1 0.5 -0.1)

(1 0.5 -0.1)

(1 0.6 -0.1)

(1 0.6 -0.1)

(1 0.6 -0.1)

(1 0.0 0.1)

(1 0 0.1)

(1 0.5 0.1)

(1 0.5 0.1)

(1 0.5 0.1)

(1 0.6 0.1)

(1 0.6 0.1)

(1 0.6 0.1)

(1 0.6 0.1)

(1 0.5 0.1)

(1 0.6 0.1)

(1 0.6 0.1)

(1 0.5 0.1)

(1 0.6 0.1)

(1 0.6 0.1)

(1 0.5 0.1)

(1 0.6 0.1)

(1 0.5 0.1)

(1 0.6 0.1)

(1 0.5 0.1)
20
21
22
23
24
25
26
27
28
31
32
37
39
40
        );
41
42
        blocks
43
44
                hex (0 1 3 2 10 11 13 12) (30 20 1) simpleGrading (1 1 1)
45
               hex (2 3 6 5 12 13 16 15) (30 5 1) simpleGrading (1 1 1)
46
                hex (3 4 7 6 13 14 17 16) (25 5 1) simpleGrading (1 1 1)
47
               hex (5 6 9 8 15 16 19 18) (30 95 1) simpleGrading (1 1 1)
48
49
50
        edges
51
        ();
52
53
54
55
        boundary
56
        (
               outerWall {
57
58
                        type wall;
59
                        faces
60
61
                               (0 1 11 10)
(1 3 13 11)
(3 4 14 13)
(7 6 16 17)
(6 9 19 16)
(9 8 18 19)
62
63
64
65
66
67
                       );
68
                }
69
                axis
70
71
                        type symmetryPlane;
                       faces
74
                                    10 12 2)
12 15 5)
15 18 8)
                               (0
(2
(5
75
                       );
79
                }
80
                nozzle
82
                        type patch;
                       faces
83
84
                                (471714)
85
                       );
86
                }
back
87
88
89
90
                       type empty;
                       faces
91
92
                               (0 2 3
(2 5 6
(3 6 7
                                            1)
3)
4)
93
94
95
```

```
(5896)
97
98
99
100
101
             type empty;
102
103
                 (10 11 13 12)
(12 13 16 15)
(13 14 17 16)
104
105
106
107
108
109
110
111
    mergePatchPairs
112
113
114
```

In order to improve the numerical accuracy, we shall use the reference level of 1 bar for the pressure field. Note that both the internal field level and the boundary conditions are offset by the reference level.

3.4.3 Preparing the Run

Before we commence the setup of the calculation, we need to consider the characteristic velocity of the phenomenon we are trying to capture. In the case under consideration, the fluid velocity will be very small, but the pressure wave will propagate with the speed of sound in water. The speed of sound is calculated as:

$$c = \sqrt{\frac{1}{\psi}} = \sqrt{\frac{1}{4.54 \times 10^{-7}}} = 1483.2 \text{m/s}.$$
 (3.17)

For the mesh described above, the characteristic mesh size is approximately 2 mm (note the scaling factor of 0.1 in the *blockMeshDict* file). Using

$$Co = \frac{U\,\Delta t}{\Delta x}\tag{3.18}$$

a reasonable time step is around $\Delta t = 5 \times 10^{-7} \text{s}$, giving the Co number of 0.35, based on the speed of sound. Also, note that the reported Co number by the code (associated with the convective velocity) will be two orders of magnitude smaller. As we are interested in the pressure wave propagation, we shall set the simulation time to 0.25 ms. For reference, the *controlDict* file is quoted below.

```
2
                    ield
                                      OpenFOAM: The Open Source CFD Toolbox
3
                                                 2.1.0
                   O peration
                                      Version:
                   A nd
                                      Web:
                                                 www.OpenFOAM.org
                   M anipulation
6
    FoamFile
10
         version
                      2.0;
                      ascii;
11
         format
                      dictionary;
         location
                      "system"
13
                      controlDict;
         object
15
16
17
                      sonicLiquidFoam;
    application
18
19
    startFrom
                      startTime:
20
```

```
startTime
                       0;
22
23
    stopAt
                       endTime;
24
25
    endTime
                       0.0001;
26
27
    deltaT
                       5e-07;
28
29
    writeControl
                       timeStep;
30
31
    writeInterval
                       20;
32
33
    purgeWrite
                       0;
34
35
                       ascii;
    writeFormat
36
37
    writePrecision
38
39
    writeCompression off;
40
41
    timeFormat
                       general;
42
43
    timePrecision
44
45
    runTimeModifiable true;
46
47
48
```

3.4.4 Running the case

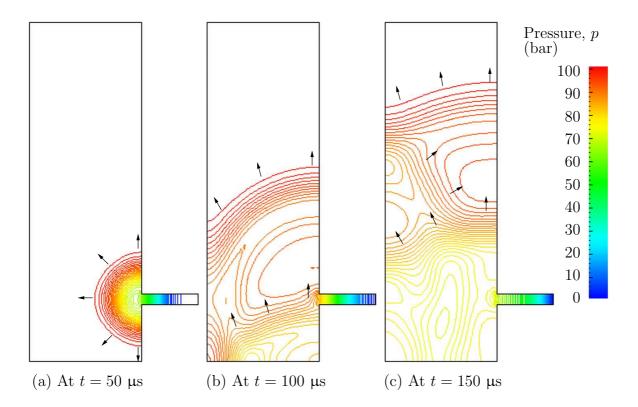


Figure 3.10: Propagation of pressure waves

The user can run the case and view results in dxFoam. The liquid flows out through the nozzle causing a wave to move along the nozzle. As it reaches the inlet to the tank, some of the wave is transmitted into the tank and some of it is reflected. While a wave is reflected up and down the inlet pipe, the waves transmitted into the tank expand and propagate through the tank. In Figure 3.10, the pressures are shown as contours so that the wave fronts are more clearly defined than if plotted as a normal isoline plot.

If the simulation is run for a long enough time for the reflected wave to return to the pipe, we can see that negative absolute pressure is detected. The modelling permits this and has some physical basis since liquids can support tension, *i.e.* negative pressures. In reality, however, impurities or dissolved gases in liquids act as sites for cavitation, or vapourisation/boiling, of the liquid due to the low pressure. Therefore in practical situations, we generally do not observe pressures falling below the vapourisation pressure of the liquid; not at least for longer than it takes for the cavitation process to occur.

3.4.5 Improving the solution by refining the mesh

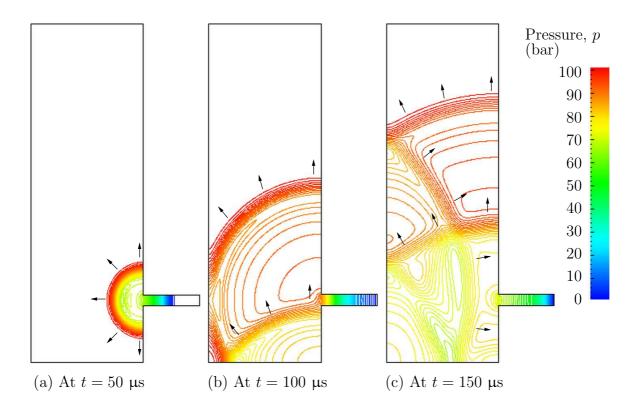


Figure 3.11: Propagation of pressure waves with refined mesh

Looking at the evolution of the resulting pressure field in time, we can clearly see the propagation of the pressure wave into the tank and numerous reflections from the inside walls. It is also obvious that the pressure wave is smeared over a number of cells. We shall now refine the mesh and reduce the time step to obtain a sharper front resolution. Simply edit the *blockMeshDict* and increase the number of cells by a factor of 4 in the x and y directions, *i.e.* block 0 becomes (120 80 1) from (30 20 1) and so on. Run blockMesh on this file. In addition, in order to maintain a Courant number below 1, the time step must be reduced accordingly to $\Delta t = 10^{-7}$ s. The second simulation gives considerably better resolution of the pressure waves as shown in Figure 3.11.

3.5 Magnetohydrodynamic flow of a liquid

In this example we shall investigate an flow of an electrically-conducting liquid through a magnetic field. The problem is one belonging to the branch of fluid dynamics known as magnetohydrodynamics (MHD) that uses mhdFoam.

3.5.1 Problem specification

The problem is known as the Hartmann problem, chosen as it contains an analytical solution with which mhdFoam can be validated. It is defined as follows:

Solution domain The domain is 2 dimensional and consists of flow along two parallel plates as shown in Fig. 3.12.

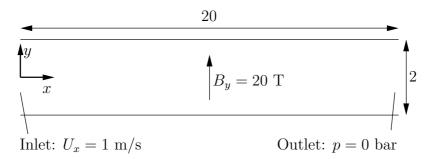


Figure 3.12: Geometry of the Hartmann problem

Governing equations

• Mass continuity for incompressible fluid

$$\nabla \cdot \mathbf{U} = 0 \tag{3.19}$$

• Momentum equation for incompressible fluid

$$\frac{\partial \mathbf{U}}{\partial t} + \nabla \cdot (\mathbf{U}\mathbf{U}) + \nabla \cdot (2\mathbf{B}\Gamma_{\mathbf{B}\mathbf{U}}\mathbf{B}) + \nabla \cdot (\nu \mathbf{U}) + \nabla (\Gamma_{\mathbf{B}\mathbf{U}}\mathbf{B} \cdot \mathbf{B}) = -\nabla p \ (3.20)$$

where **B** is the magnetic flux density, $\Gamma_{\mathbf{B}\mathbf{U}} = (2\mu\rho)^{-1}$.

• Maxwell's equations

$$\nabla \times \mathbf{E} = -\frac{\partial \mathbf{B}}{\partial t} \tag{3.21}$$

where **E** is the electric field strength.

$$\nabla \cdot \mathbf{B} = 0 \tag{3.22}$$

$$\nabla \times \mathbf{H} = \mathbf{J} + \frac{\partial \mathbf{D}}{\partial t} = \mathbf{J} \tag{3.23}$$

assuming $\partial \mathbf{D}/\partial t \ll \mathbf{J}$. Here, **H** is the magnetic field strength, **J** is the current density and **D** is the electric flux density.

• Charge continuity

$$\nabla \cdot \mathbf{J} = 0 \tag{3.24}$$

• Constitutive law

$$\mathbf{B} = \mu \mathbf{H} \tag{3.25}$$

• Ohm's law

$$\mathbf{J} = \sigma \left(\mathbf{E} + \mathbf{U} \times \mathbf{B} \right) \tag{3.26}$$

• Combining Equation 3.21, Equation 3.23, Equation 3.26, and taking the curl

$$\frac{\partial \mathbf{B}}{\partial t} + \nabla \cdot (\mathbf{U}\mathbf{B}) - \nabla \cdot (\phi_{\mathbf{B}}\mathbf{U}) - \nabla \cdot (\Gamma_{\mathbf{B}}\mathbf{B}) = 0$$
(3.27)

Boundary conditions

- inlet is specified the inlet condition with fixed velocity U = (1, 0, 0) m/s;
- outlet is specified as the outlet with with fixed pressure p = 0 Pa;
- upperWall is specified as a wall where $\mathbf{B} = (0, 20, 0) \mathrm{T}$.
- lowerWall is specified as a wall where $\mathbf{B} = (0, 20, 0) \mathrm{T}$.
- front and back boundaries are specified as empty.

Initial conditions U = 0 m/s, p = 100 Pa, B = (0, 20, 0) T.

Transport properties

- Kinematic viscosity $\nu = 1 \text{ Pas}$
- Density $\rho = 1 \text{ kg m/s}$
- Electrical conductivity $\sigma = 1 \ (\Omega \, \text{m})^{-1}$
- Permeability $\mu = 1 \text{ H/m}$

Solver name mhdFoam: an incompressible laminar magneto-hydrodynamics code.

Case name hartmann case located in the \$FOAM_TUTORIALS/mhdFoam directory.

3.5.2 Mesh generation

The geometry is simply modelled with 100 cells in the x-direction and 40 cells in the y-direction; the set of vertices and blocks are given in the mesh description file below:

```
----*- C++ -*-----
1
2
                    ield
                                      OpenFOAM: The Open Source CFD Toolbox
3
                                     Version:
                                                 2.1.0
4
                  O peration
                   A nd
                                                 www.OpenFOAM.org
                                      Web:
5
                  {\tt M} anipulation
    FoamFile
9
                      2.0;
ascii;
         version
10
11
         format
                      dictionary;
blockMeshDict;
12
         class
13
14
15
16
    convertToMeters 1;
17
18
    vertices
19
20
         (0 -1 0)
         (20 -1 0)
22
          20 1 0)
24
            -1 0.1)
             -1 0.1)
         (20\ 1\ 0.1)
         (0\ 1\ 0.1)
28
    );
30
    blocks
        hex (0 1 2 3 4 5 6 7) (100 40 1) simpleGrading (1 1 1)
    );
34
```

```
edges
36
37
     ();
38
39
     boundary
40
           inlet
43
44
                 type patch;
45
46
                      (0 4 7 3)
48
49
           outlet
50
51
                type patch;
52
54
                      (2651)
55
56
57
           ĺowerWall
58
59
                type patch;
faces
60
61
62
                      (1540)
63
64
65
           upperWall
66
67
                type patch;
                      (3762)
           frontAndBack
                type empty;
                      (0 \ 3 \ 2 \ 1)
(4 \ 5 \ 6 \ 7)
80
81
           }
82
     );
84
     mergePatchPairs
86
87
```

3.5.3 Running the case

The user can run the case and view results in dxFoam. It is also useful at this stage to run the Ucomponents utility to convert the U vector field into individual scalar components. MHD flow is governed by, amongst other things, the Hartmann number which is a measure of the ratio of electromagnetic body force to viscous force

$$M = BL\sqrt{\frac{\sigma}{\rho\nu}} \tag{3.28}$$

where L is the characteristic length scale. In this case with $B_y=20$ T, M=20 and the electromagnetic body forces dominate the viscous forces. Consequently with the flow fairly steady at t=2 s the velocity profile is almost planar, viewed at a cross section midway along the domain x=10 m. The user can plot a graph of the profile of U_x in dxFoam. Now the user should reduce the magnetic flux density **B** to 1 Tand re-run the code and Ucomponents. In this case, M=1 and the electromagnetic body forces no longer dominate. The velocity profile consequently takes on the parabolic form, characteristic

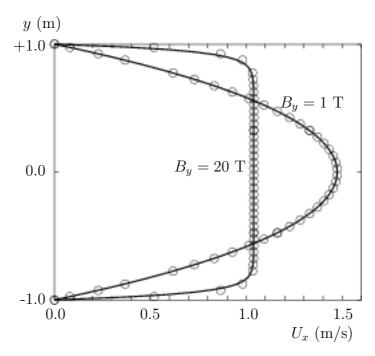


Figure 3.13: Velocity profile in the Hartmann problem for $B_y=1~\mathrm{T}$ and $B_y=20~\mathrm{T}$.

of Poiseuille flow as shown in Figure 3.13. To validate the code the analytical solution for the velocity profile U_x is superimposed in Figure 3.13, given by:

$$\frac{U_x(y)}{U_x(0)} = \frac{\cosh M - \cosh M(y/L)}{\cosh M - 1} \tag{3.29}$$

where the characteristic length L is half the width of the domain, *i.e.* 1 m.

Index

Symbols Numbers A B C D E F G H I J K L M N O P Q R S T U V W X Z

Symbols	algorithms tools, U-96
*	alphaContactAngle
tensor member function, P-25	boundary condition, U-59
+	analytical solution, P-45
tensor member function, P-25	Animations window panel, U-168
-	anisotropicFilter model, U-101
tensor member function, P-25	Annotation window panel, U-26, U-167
/	ansysToFoam utility, U-90
tensor member function, P-25	APIfunctions model, U-100
/**/	applications, U-69
C++ syntax, U-78	Apply button, U-164, U-168
//	applyBoundaryLayer utility, U-90
C++ syntax, U-78	applyWallFunctionBoundaryConditions utility,
OpenFOAM file syntax, U-104	U-90
# include	arbitrarily unstructured, P-31
C++ syntax, U-72, U-78	arc
&	keyword entry, U-139
tensor member function, P-25	arc keyword, U-138
&&	As keyword, U-182
tensor member function, P-25	ascii
	keyword entry, U-112
tensor member function, P-25	attachMesh utility, U-91
<pre><lesmodel>Coeffs keyword, U-184</lesmodel></pre>	Auto Accept button, U-168
<rasmodel>Coeffs keyword, U-183</rasmodel>	autoMesh
<pre><delta>Coeffs keyword, U-184</delta></pre>	library, U-97
0.000000e+00 directory, U-104	autoPatch utility, U-91
1-dimensional mesh, U-130	autoRefineMesh utility, U-92
1D mesh, U-130	axes
2-dimensional mesh, U-130	right-handed, U-136
2D mesh, U-130	right-handed rectangular Cartesian, P-15,
Numbers	U-20
0 directory, U-104	axi-symmetric cases, U-135, U-144
· ·	axi-symmetric mesh, U-130
${f A}$.
access functions, P-23	${f B}$
addLayersControls keyword, U-146	background
adiabaticFlameT utility, U-96	process, U-26, U-81
adjointShapeOptimizationFoam $solver, U-85$	backward
adjustableRunTime	keyword entry, U-119
keyword entry, U-62, U-111	Backward differencing, P-39
adjustTimeStep keyword, U-62	bar otropic Compressibility Models
agglomerator keyword, U-122	library, U-99

P-74 Index

basicMultiComponentMixture model, U-99,	supersonicFreeStream, U-137
U-180	surfaceNormalFixedValue, U-137
basicSolidThermo	symmetryPlane, P-63, U-135
library, U-100	totalPressure, U-137
basicThermophysicalModels	turbulentInlet, U-137
library, U-98	wall, U-42
binary	wall, P-63, P-69, U-59, U-135
keyword entry, U-112	wallBuoyantPressure, U-137
BirdCarreau model, U-102	wedge, U-130, U-135, U-144
blended differencing, P-38	zeroGradient, U-136
block	boundary conditions, P-43
expansion ratio, U-140	Dirichlet, P-43
block keyword, U-138	inlet, P-44
blocking	Neumann, P-43
keyword entry, U-80	no-slip impermeable wall, P-44
blockMesh	outlet, P-44
library, U-97	physical, P-44
blockMesh solver, P-47	
blockMesh utility, U-38, U-90, U-136	symmetry plane, P-44
blockMesh executable	boundaryField keyword, U-23, U-108
	boundaryFoam solver, U-85
vertex numbering, U-140 blockMeshDict	bounded II 117 II 110
	keyword entry, U-117, U-118
dictionary, U-20, U-22, U-37, U-50, U-136, U-144	
	boxTurb utility, U-90
blocks keyword, U-22, U-32, U-140	breaking of a dam, U-57
boundaries, U-132	bubbleFoam solver, U-87
boundary, U-132	buoyantBaffleSimpleFoam solver, U-88
boundary	buoyantBoussinesqPimpleFoam solver, U-88
dictionary, U-129, U-136	buoyantBoussinesqSimpleFoam solver, U-88
boundary keyword, U-141	buoyantPimpleFoam solver, U-88
boundary condition	buoyantSimpleFoam solver, U-88
alphaContactAngle, U-59	buoyantSimpleRadiationFoam solver, U-88
calculated, U-136	button
cyclic, U-135, U-142	Apply, $U-164$, $U-168$
directionMixed, U-136	Auto Accept, U-168
empty, P-63, P-69, U-20, U-130, U-135	Choose Preset, U-166
fixedGradient, U-136	Delete, U-164
fixedValue, U-136	Edit Color Map, U-165
fluxCorrectedVelocity, U-137	Enable Line Series, U-36
inlet, P-69	Orientation Axes, U-26, U-167
inletOutlet, U-137	Refresh Times, U-27
mixed, U-136	Rescale to Data Range, U-27
moving Wall Velocity, $U-137$	Reset, U-164
outlet, P-69	Set Ambient Color, U-166
outletInlet, U-137	Update GUI, U-165
partialSlip, $U-137$	Use Parallel Projection, U-26
patch, U - 135	Use parallel projection, U-167
pressure Directed Inlet Velocity, $U-137$	
pressureInletVelocity, U-137	\mathbf{C}
pressureOutlet, P-63	C++ syntax
pressure Transmissive, $U-137$	/**/, U-78
processor, U-135	//, U-78
setup, U-22	# include, U-72, U-78
slip, U-137	cacheAgglomeration keyword, U-123

calculated	pointField, $P-31$
boundary condition, U-136	polyBoundaryMesh, P-31
cAlpha keyword, U-63	polyMesh, P-31, U-127, U-129
cases, U-103	polyPatchList, P-31
castellatedMesh keyword, U-146	polyPatch, P-31
castellatedMeshControls	scalarField, P-29
dictionary, U-147–U-149	scalar, P-23
castellatedMeshControls keyword, U-146	slice, P-31
cavitatingFoam solver, U-87	symmTensorField, P-29
cavity flow, U-19	symmTensorThirdField, P-29
CELARCH	tensorField, P-29
environment variable, U-173	tensorThirdField, P-29
CEI_HOME	tensor, P-23
environment variable, U-173	vectorField, P-29
cell	vector, P-23, U-107
expansion ratio, U-140	word, P-25, P-31
cell class, P-31	class keyword, U-105
cell	clockTime
keyword entry, U-174	keyword entry, U-111
cellLimited	cloud keyword, U-175
keyword entry, U-117	cmptAv
cellPoint	tensor member function, P-25
keyword entry, U-174	Co utility, U-93
cellPointFace	coalChemistryFoam solver, U-88
keyword entry, U-174	coalCombustion
cells	library, U-98
dictionary, U-136	cofactors
central differencing, P-38	tensor member function, P-25
cfdTools tools, U-97	coldEngineFoam solver, U-88
cfx4ToFoam utility, U-90, U-154	collapseEdges utility, $U-92$
changeDictionary utility, U-90	Color By menu, U-166
channelFoam solver, U-85	Color Legend window, U-29
Charts window panel, U-168	Color Legend window panel, U-166
checkMesh utility, U-91, U-155	Color Scale window panel, U-166
chemFoam solver, U-88	Colors window panel, U-168
chemistryModel	combinePatchFaces utility, U-92
library, U-100	comments, U-78
chemistryModel model, U-100	commsType keyword, U-80
chemistrySolver model, U-100	compressed
chemkinToFoam utility, U-96	keyword entry, U-112
Choose Preset button, U-166	compressibleInterFoam solver, U-87
chtMultiRegionFoam solver, U-88	compressibleLESModels
Chung	library, U-102
library, U-99	compressible RAS Models
class	library, U-101
cell, P-31	constant directory, U-104, U-179
dimensionSet, P-25, P-32, P-33	constLaminarFlameSpeed model, U-99
face, P-31	constTransport model, U-100, U-180
finiteVolumeCalculus, P-33	containers tools, U-96
finiteVolumeMethod, P-33	continuum
fvMesh, P-31	mechanics, P-15
fvSchemes, P-36	control
fvc, P-36	of time, U-111
fvm, P-36	controlDict

P-76 Index

dictionary, P-65, U-23, U-32, U-43, U-52,	ddt
U-62, U-104, U-160	fvc member function, P-37
controlDict file, P-50	fvm member function, P-37
convection, see divergence, P-38	DeardorffDiffStress model, U-102
convergence, U-40	debug keyword, U-146
conversion	decomposePar utility, U-81, U-82, U-95
library, U-98	decomposeParDict
convertToMeters keyword, U-138	dictionary, U-81
coordinate	decomposition
system, P-15	of field, U-81
coordinate system, U-20	of mesh, U-81
corrected	decompositionMethods
keyword entry, U-117, U-118	library, U-98
Courant number, P-42, U-24	decompression of a tank, P-62
Cp keyword, U-181	defaultFieldValues keyword, U-60
cpuTime	deformedGeom utility, U-91
keyword entry, U-111	Delete button, U-164
Crank Nicholson	delta keyword, U-83, U-184
	deltaT keyword, U-111
temporal discretisation, P-42 CrankNicholson	dependencies, U-72
keyword entry, U-119	dependency lists, U-72
createBaffles utility, U-91	det
createPatch utility, U-91	tensor member function, P-25
createTurbulenceFields utility, U-93	determinant, see tensor, determinant
cross product, see tensor, vector cross product	
CrossPowerLaw	tensor member function, P-25
keyword entry, U-61	diag
CrossPowerLaw model, U-102	tensor member function, P-25
cubeRootVolDelta model, U-101	diagonal
cubicCorrected	keyword entry, U-121, U-122
keyword entry, U-119	DIC
cubicCorrection	keyword entry, U-122
keyword entry, U-116	DICGaussSeidel
curl, P-37	keyword entry, U-122
curl	dictionary
fvc member function, P-37	LESProperties, U-183
Current Time Controls menu, U-27, U-165	PISO, U-25
curve keyword, U-175	blockMeshDict, U-20, U-22, U-37, U-50,
Cv keyword, U-181	U-136, U-144
cyclic	boundary, $U-129$, $U-136$
boundary condition, U-135, U-142	$\it castellated Mesh Controls, U-147-U-149$
cyclic	cells, U-136
keyword entry, U-134	controlDict, P-65, U-23, U-32, U-43, U-52,
cylinder	U-62, U-104, U-160
flow around a, P-45	decomposeParDict, U-81
	faces, U-129, U-136
D	fvSchemes, U-62, U-63, U-104, U-113
d2dt2	fvSolution, U-104, U-120
fvc member function, P-37	mechanicalProperties, U-51
fvm member function, P-37	neighbour, U-129
dam	owner, U-129
breaking of a, U-57	points, U-129, U-136
datToFoam utility, U-90	thermalProperties, U-52
db tools, U-96	thermophysicalProperties, U-179

transportProperties, U-23, U-40, U-43 turbulenceProperties, U-42, U-61, U-183	divSchemes keyword, U-114 dnsFoam solver, U-87
dieselEngineFoam solver, U-88	doLayers keyword, U-146
dieselFoam solver, U-88	double inner product, see tensor, double inner
dieselMixture model, U-99, U-180	product
dieselSpray	dsmc
library, U-98	library, U-98
differencing	dsmcFieldsCalc utility, U-94
Backward, P-39	dsmcFoam solver, U-89
blended, P-38	dsmcInitialise utility, U-90
central, P-38	dx
Euler implicit, P-39	keyword entry, U-174
Gamma, P-38	dynamicFvMesh
MINMOD, P-38	-
SUPERBEE, P-38	library, U-97
· · · · · · · · · · · · · · · · · · ·	dynamicMesh
upwind, P-38	library, U-97
van Leer, P-38	dynLagrangian model, U-101
DILU	dynMixedSmagorinsky model, U-101
keyword entry, U-122	dynOneEqEddy model, U-101, U-102
dimension	dynSmagorinsky model, U-101
checking in OpenFOAM, P-25, U-107	${f E}$
dimensional units, U-107	
dimensioned <type> template class, P-25</type>	eConstThermo model, U-100, U-179
dimensionedTypes tools, U-97	edgeGrading keyword, U-140
dimensions keyword, U-22, U-108	edgeMesh
dimensionSet class, P-25, P-32, P-33	library, U-97
dimensionSet tools, U-97	edges keyword, U-138
directionMixed	Edit menu, U-167, U-168
boundary condition, U-136	Edit Color Map button, U-165
directory	egrMixture model, U-99, U-180
0.000000e+00, U-104	electrostaticFoam solver, U-89
<i>0</i> , U-104	empty
Make, U-73	boundary condition, P-63, P-69, U-20,
constant, U-104, U-179	U-130, U-135
fluentInterface, U-170	empty
polyMesh, U-104, U-129	keyword entry, U-134
processorN, U-82	Enable Line Series button, U-36
run, U-103	endTime keyword, U-24, U-111
system, P-50, U-104	engine
tutorials, P-45, U-19	library, U-98
discretisation	engineCompRatio utility, U-94
equation, P-33	engineFoam solver, U-88
± '	engineSwirl utility, U-90
U-164, U-165	ensight74FoamExec utility, U-172
distance	ENSIGHT7_INPUT
keyword entry, U-149, U-175	environment variable, U-173
distributed model, U-98	ENSIGHT7_READER
distributed keyword, U-83, U-84	environment variable, U-173
distributionModels	ensightFoamReader utility, U-92
	enstrophy utility, U-93
library, U-98	environment variable
div	CEL_ARCH, U-173
fvc member function, P-37	,
fvm member function, P-37	CELHOME, U-173
divergence, P-37, P-39	ENSIGHT7_INPUT, U-173

P-78 Index

ENSIGHT7_READER, U-173	keyword entry, U-122
FOAM_RUN, U-103	featureAngle keyword, U-152
WM_ARCH_OPTION, U-76	features keyword, U-147, U-148
WM_ARCH, U-76	field
WM_COMPILER_BIN, U-76	U, U-24
WM_COMPILER_DIR, U-76	p, U-24
WM_COMPILER_LIB, U-76	decomposition, U-81
WM_COMPILER, U-76	FieldField <type> template class, P-32</type>
WM_COMPILE_OPTION, U-76	fieldFunctionObjects
WM_DIR, U-76	library, U-97
WM_MPLIB, U-76	fields, P-29
WM_OPTIONS, U-76	mapping, U-160
WM_PRECISION_OPTION, U-76	fields tools, U-97
WM_PROJECT_DIR, U-76	fields keyword, U-174
WM_PROJECT_DIR, U-76	Field <type> template class, P-29</type>
WM_PROJECT_USER_DIR, U-76	fieldValues keyword, U-60
,	fieldview9Reader utility, U-92
WM_PROJECT_VERSION, U-76	file
WM_PROJECT, U-76	Make/files, U-74
wmake, U-75	controlDict, P-50
ePsiThermo model, U-98, U-180	•
equilibriumCO utility, U-96	files, U-73
equilibriumFlameT utility, U-96	g, U-61
errorReduction keyword, U-153	options, U-73
Euler	snappyHexMeshDict, U-145
keyword entry, U-119	transportProperties, U-61
Euler implicit	file format, U-104
differencing, P-39	fileFormats
temporal discretisation, P-42	library, U-98
examples	fileModificationChecking keyword, U-80
decompression of a tank, P-62	fileModificationSkew keyword, U-80
flow around a cylinder, P-45	files file, U-73
flow over backward step, P-53	filteredLinear2
Hartmann problem, P-67	keyword entry, U-116
supersonic flow over forward step, P-58	finalLayerRatio keyword, U-152
execFlowFunctionObjects utility, U-94	financialFoam solver, U-89
expandDictionary utility, U-96	finite volume
expansionRatio keyword, U-152	discretisation, P-27
explicit	mesh, P-31
temporal discretisation, P-42	finiteVolume
extrude2DMesh utility, U-90	library, U-97
extrudeMesh utility, U-90	finiteVolume tools, U-97
extrudeToRegionMesh utility, U-90	finiteVolumeCalculus class, P-33
T.	finiteVolumeMethod class, P-33
\mathbf{F}	fireFoam solver, U-88
face class, P-31	firstTime keyword, U-111
face keyword, U-175	fixed
faceAgglomerate utility, U-90	keyword entry, U-112
faceAreaPair	fixedGradient
keyword entry, U-122	boundary condition, U-136
faceLimited	fixedValue
keyword entry, U-117	boundary condition, U-136
faces	flattenMesh utility, U-91
dictionary, U-129, U-136	floatTransfer keyword, U-80
FDIC	flow

free surface, U-57	d2dt2, P-37
laminar, U-19	ddt, P-37
steady, turbulent, P-53	div, P-37
supersonic, P-59	gGrad, P-37
turbulent, U-19	grad, P-37
flow around a cylinder, P-45	laplacian, P-37
flow over backward step, P-53	lsGrad, P-37
flowType utility, U-93	snGrad, P-37
fluent3DMeshToFoam utility, U-90	snGradCorrection, P-37
fluentInterface directory, U-170	sqrGradGrad, P-37
fluentMeshToFoam utility, U-90, U-154	fvDOM
fluxCorrectedVelocity	library, U-99
boundary condition, U-137	fvm class, P-36
fluxRequired keyword, U-114	fvm member function
OpenFOAM	d2dt2, P-37
cases, U-103	ddt, P-37
FOAM_RUN	div, P-37
environment variable, U-103	laplacian, P-37
foamCalc utility, U-34, U-94	Su, P-37
foamCalcFunctions	SuSp, P-37
library, U-97	fvMatrices tools, U-97
foamCorrectVrt script/alias, U-158	fvMatrix template class, P-33
foamDataToFluent utility, U-92, U-170	fvMesh class, P-31
foamDebugSwitches utility, U-96	fvMesh tools, U-97
FoamFile keyword, U-105	fvMotionSolvers
foamFile	library, U-97
keyword entry, U-174	fvSchemes
foamFormatConvert utility, U-96	dictionary, U-62, U-63, U-104, U-113
foamInfoExec utility, U-96	fvSchemes class, P-36
foamJob script/alias, U-177	fvSchemes
foamListTimes utility, U-94	menu entry, U-53
foamLog script/alias, U-177	fvSolution
foamMeshToFluent utility, U-90, U-170	dictionary, U-104, U-120
foamToEnsight utility, U-92	
foamToEnsightParts utility, U-92	${f G}$
foamToFieldview9 utility, U-92	g file, U-61
foamToGMV utility, U-92	gambitToFoam utility, U-91, U-154
foamToStarMesh utility, U-90	GAMG
foamToSurface utility, U-91	keyword entry, U-54, U-121, U-122
foamToTecplot360 utility, U-92	Gamma
foamToVTK utility, U-92	keyword entry, U-116
foamUpgradeCyclics utility, U-90	Gamma differencing, P-38
foamUpgradeFvSolution utility, U-90	Gauss
forces	keyword entry, U-117
library, U-97	Gauss's theorem, P-36
foreground	GaussSeidel
process, U-26	keyword entry, U-122
format keyword, U-105	General window panel, U-167, U-168
fourth	general
keyword entry, U-117, U-118	keyword entry, U-112
functions keyword, U-112	genericFvPatchField
fvc class, P-36	library, U-98
fvc member function	geometric-algebraic multi-grid, $U-122$
curl, P-37	GeometricBoundaryField template class, P-32

P-80 Index

<pre>geometricField<type> template class, P-32 geometry keyword, U-146 gGrad</type></pre>	identities, see tensor, identities identity, see tensor, identity incompressibleLESModels
fvc member function, P-37	library, U-101
global tools, U-97	incompressibleRASModels
gmshToFoam utility, U-91	library, U-100
gnuplot	incompressibleTransportModels
keyword entry, U-112, U-174	library, P-54, U-102
,	incompressibleTurbulenceModels
grad	-
fvc member function, P-37	library, P-54
(Grad Grad) squared, P-37	index
gradient, P-37, P-40	notation, P-16, P-17
Gauss scheme, P-40	Information window panel, U-164
Gauss's theorem, U-53	inhomogeneousMixture model, U-99, U-180
least square fit, U-53	inlet
least squares method, P-40, U-53	boundary condition, P-69
surface normal, P-40	inletOutlet
gradSchemes keyword, U-114	boundary condition, U-137
graph tools, U-97	inner product, see tensor, inner product
graphFormat keyword, U-112	inotify
GuldersEGRLaminarFlameSpeed model, U-99	keyword entry, U-80
GuldersLaminarFlameSpeed model, U-99	inotifyMaster
	keyword entry, U-80
\mathbf{H}	inside
hConstThermo model, U-100, U-179	keyword entry, U-149
Help menu, U-167	insideCells utility, U-91
HerschelBulkley model, U-102	interDyMFoam solver, U-87
Hf keyword, U-181	interfaceProperties
hhuMixtureThermo model, U-99, U-180	library, U-102
hierarchical	interfaceProperties model, U-102
keyword entry, U-82, U-83	interFoam solver, U-87
highCpCoeffs keyword, U-182	interMixingFoam solver, U-87
homogenousDynSmagorinsky model, U-101	internalField keyword, U-23, U-108
homogeneousMixture model, U-99, U-180	, ,
hPolynomialThermo model, U-100, U-179	interPhaseChangeFoam solver, U-87
hPsiMixtureThermo model, U-99, U-180	interpolation tools, U-97
hPsiThermo model, U-98, U-180	interpolationScheme keyword, U-174
hRhoMixtureThermo model, U-99, U-180	interpolations tools, U-97
· · · · · · · · · · · · · · · · · · ·	interpolationSchemes keyword, U-114
hRhoThermo model, U-98, U-180	inv
hsPsiMixtureThermo model, U-99, U-180	tensor member function, P-25
hsPsiThermo model, U-98, U-180	iterations
hsRhoMixtureThermo model, U-99, U-180	maximum, U-121
hsRhoThermo model, U-98, U-180	т
I	J
I	janafThermo model, U-100, U-179
	jobControl
tensor member function, P-25	library, U-97
icoFoam solver, U-19, U-23, U-24, U-26, U-85	jplot
icoPolynomial model, U-100, U-179	keyword entry, U-112, U-174
icoUncoupled Kinematic Parcel DyMFoam solver,	T/
U-88	K
icoUncoupledKinematicParcelFoam solver, U-88	kEpsilon model, U-100, U-101
ideasToFoam utility, U-154	keyword
ideas InvToFoam utility II-91	As II-189

- II 101	TT 110
Cp, U-181	functions, U-112
Cv, U-181	geometry, U-146
FoamFile, U-105	gradSchemes, U-114
Hf, U-181	graphFormat, U-112
LESModel, U-184	highCpCoeffs, U-182
Pr, U-182	internalField, U-23, U-108
RASModel, U-183	interpolationSchemes, U-114
Tcommon, U-182	interpolationScheme, U-174
Thigh, U-182	laplacianSchemes, U-114
Tlow, U-182	latestTime, U-40
Ts, U-182	layers, U-152
addLayersControls, U-146	leastSquares, U-53
adjustTimeStep, U-62	levels, U-150
agglomerator, U-122	libs, U-80, U-112
arc, U-138	locationInMesh, U-148, U-149
blocks, U-22, U-32, U-140	location, $U-105$
block, U-138	${\tt lowCpCoeffs}, U\text{-}182$
boundaryField, $U-23$, $U-108$	manualCoeffs, U-83
boundary, U-141	$ exttt{maxAlphaCo}, exttt{U-62}$
boxToCell, U-60	maxBoundarySkewness, $ ext{U-}153$
cAlpha, U-63	$ exttt{maxConcave}, exttt{U-}153$
$ ext{cacheAgglomeration}, ext{U-}123$	$\mathtt{maxCo}, \mathrm{U} ext{-}62$
castellatedMeshControls, U-146	maxDeltaT, U - 62
castellatedMesh, U-146	maxFaceThicknessRatio, U -152
class, U -105	maxGlobalCells, U-148
cloud, U-175	maxInternalSkewness, U - 153
${\tt commsType}, \ {\tt U-80}$	$ exttt{maxIter}, ext{U-}121$
convertToMeters, U-138	$ exttt{maxLocalCells}, exttt{U-}148$
curve, U-175	$ exttt{maxNonOrtho}, exttt{U-153}$
debug, U-146	maxThicknessToMedialRatio, $ ext{U-}152$
$ ext{defaultFieldValues}, ext{U-}60$	mergeLevels, $U ext{-}123$
deltaT, U-111	$ exttt{mergePatchPairs}, exttt{U-}138$
delta, U-83, U-184	mergeTolerance, $ ext{U-}146$
dimensions, U-22, U-108	meshQualityControls, U -146
distributed, U-83, U-84	method, U - 83
divSchemes, U-114	$\verb midPointAndFace , U-175 $
doLayers, U -146	${\tt midPoint}, U\text{-}175$
edgeGrading, U-140	$\mathtt{minArea},\ \mathrm{U\text{-}}153$
edges, U -138	$\verb minDeterminant , U-153 $
$\mathtt{endTime},\ \mathrm{U\text{-}}24,\ \mathrm{U\text{-}}111$	$\verb minFaceWeight , U-153 $
errorReduction, U-153	$\verb minFlatness , U-153 $
expansionRatio, U-152	$\verb minMedianAxisAngle , U-152 $
face, U-175	minRefinementCells, U-148
${\tt featureAngle, U-152}$	minThickness, $U ext{-}152$
features, U-147, U-148	$\verb minTriangleTwist , U-153 $
fieldValues, U-60	$\mathtt{minTwist}, \text{U-}153$
fields, U-174	$\verb minVolRatio , U-153 $
fileModificationChecking, U-80	$\mathtt{minVol},\ \mathrm{U}\text{-}153$
${\tt fileModificationSkew},\ U\textrm{-}80$	mode, U-149
$ ext{finalLayerRatio}, ext{U-152}$	${\tt molWeight}, U\text{-}181$
firstTime, U-111	mu, U-182
floatTransfer, U-80	<code>nAlphaSubCycles</code> , $U ext{-}63$
fluxRequired, U-114	nBufferCellsNoExtrude, $U ext{-}152$
format, U-105	nCellsBetweenLevels, U-148

P-82

II 190	II 101
nFaces, U-130	specie, U-181
nFinestSweeps, U-123	spline, U-138
nGrow, U-152	startFace, U-130
nLayerIter, U-152	startFrom, U-24, U-111
nMoles, U-181	startTime, U-24, U-111
nPostSweeps, U-123	stopAt, U-111
nPreSweeps, U-123	strategy, U-82, U-83
nRelaxIter, U-150, U-152	surfaceFormat, U-174
nRelaxedIter, U-152	surfaces, U-174
nSmoothNormals, U-152	thermoType, U-179
nSmoothPatch, U-150	thermodynamics, U-181
nSmoothScale, U-153	timeFormat, U-112
nSmoothSurfaceNormals, U-152	timePrecision, U-112
nSmoothThickness, U-152	timeScheme, U-114
nSolveIter, U-150	tolerance, U-54, U-121, U-150
neighbourPatch, U-142	topoSetSource, U-60
numberOfSubdomains, U-83	traction, U-51
n, U-83	transport, U-181
object, U-105	turbulence, U-183
order, U-83	type, U-132, U-133
pRefCell, U-25, U-125	uniform, U-175
pRefValue, U-25, U-125	valueFraction, U-136
p_rhgRefCell, U-125	value, U-23, U-136
p_rhgRefValue, U-125	version, U-105
patchMap, U-160	vertices, U-22, U-138, U-139
patches, U-138	writeCompression, U-112
preconditioner, U-121, U-122	writeControl, U-24, U-62, U-111
pressure, U-51	writeFormat, U-56, U-112
printCoeffs, U-43, U-183	writeInterval, U-24, U-33, U-111
processorWeights, U-82	writePrecision, U-112
processorWeights, U-83	<pre><lesmodel>Coeffs, U-184</lesmodel></pre>
purgeWrite, U-112	<pre><rasmodel>Coeffs, U-183</rasmodel></pre>
refGradient, U-136	<pre><delta>Coeffs, U-184</delta></pre>
refinementRegions, U-148, U-150	keyword entry
refinementSurfaces, U-148	CrankNicholson, U-119
refinementRegions, U-149	CrossPowerLaw, U-61
regions, U-60	DICGaussSeidel, U-122
relTol, U-54, U-121	DIC, U-122 DILU, U-122
relativeSizes, U-152 relaxed, U-153	Euler, U-119
resolveFeatureAngle, U-148	FDIC, U-122
roots, U-83, U-84	GAMG, U-54, U-121, U-122
	Gama, U-116
runTimeModifiable, U-112	,
scotchCoeffs, U-83	GaussSeidel, U-122
setFormat, U-174	Gauss, U-117
sets, U-174	LESModel, U-42, U-183 MGridGen, U-123
simpleGrading, U-140	*
simulationType, U-42, U-61, U-183 smoother, U-123	MUSCL, U-116
•	Newtonian, U-61
snGradSchemes, U-114 snapControls, U-146	PBiCG, U-121 PCG, U-121
snap. U-146	•
snap, 0-140 solvers, U-120	QUICK, U-119 RASModel, U-42, U-183
solvers, U-120 solver, U-54, U-121	SFCD, U-116, U-119
551751, 6 64, 6-121	51 55, 6 110, 6-115

UMIST, $U-115$	outside, $ ext{U-}149$
$\verb"adjustableRunTime", U-62, U-111"$	$\mathtt{patch},\ U\text{-}134,\ U\text{-}176$
arc, U-139	$\mathtt{polyLine},\ U\text{-}139$
ascii, U - 112	${ t polySpline,\ U-139}$
backward, U - 119	processor, $U-134$
binary, $U-112$	${\tt raw}, { m U-}112, { m U-}174$
blocking, U-80	$\mathtt{runTime},\ U\text{-}33,\ U\text{-}111$
bounded, U-117, U-118	scheduled, $U ext{-}80$
cellLimited, U-117	scientific, U - 112
cellPointFace, U-174	scotch, U-82, U-83
cellPoint, U-174	simpleSpline, U-139
cell, U-174	simple, U-82, U-83
clockTime, U-111	skewLinear, U-116, U-119
compressed, U-112	smoothSolver, U-121
corrected, U-117, U-118	$\mathtt{startTime}, \ \mathtt{U-24}, \ \mathtt{U-111}$
cpuTime, U-111	steadyState, U-119
cubicCorrected, U-119	stl, U-174
cubicCorrection, U-116	symmetryPlane, U-134
cyclic, U-134	timeStampMaster, U-80
diagonal, U-121, U-122	timeStamp, U-80
distance, U-149, U-175	timeStep, U-24, U-33, U-111
dx, U-174	uncompressed, U-112
empty, U-134	uncorrected, U-117, U-118
faceAreaPair, U-122	upwind, U-116, U-119
faceLimited, U-117	vanLeer, U-116
filteredLinear2, U-116	valideer, 0-110 vtk, U-174
fixed, U-112	•
foamFile, U-174	wall, U-134
fourth, U-117, U-118	wedge, U-134
general, U-112	writeControl, U-111
gnuplot, U-112, U-174	writeNow, U-111
hierarchical, U-82, U-83	xmgr, U-112, U-174
inotifyMaster, U-80	xyz, U-175
,	x, U-175
inotify, U-80	y, U-175
inside, U-149	z, U-175
jplot, U-112, U-174	kivaToFoam utility, U-91
laminar, U-42, U-183	kOmega model, U-100
latestTime, U-111	kOmegaSST model, U-100, U-101
leastSquares, U-117	kOmegaSSTSAS model, U-101
limitedCubic, U-116	Kronecker delta, P-20
limitedLinear, U-116	${f L}$
limited, U-117, U-118	
linearUpwind, U-116, U-119	lagrangian
linear, U-116, U-119	library, U-98
line, U-139	lagrangianIntermediate
localEuler, U-119	library, U-98
$\mathtt{manual},\ \mathrm{U}\text{-}82,\ \mathrm{U}\text{-}83$	Lambda2 utility, U-93
metis, U-83	LamBremhorstKE model, U-101
midPoint, U-116	laminar model, U-100, U-101
$\mathtt{nextWrite}, \mathrm{U}\text{-}111$	laminar
${\tt noWriteNow},\ U\text{-}111$	keyword entry, U-42, U-183
nonBlocking, U-80	laminar Flame Speed Models
none, U-115, U-122	library, U-99
null, U-174	laplaceFilter $model, U-101$

P-84 Index

Laplacian, P-38	dynamicFvMesh, U -97
laplacian, P-37	dynamicMesh, U-97
- /	- /
laplacian	edgeMesh, U-97
fvc member function, P-37	engine, U-98
fvm member function, P-37	fieldFunctionObjects, U-97
laplacianFoam solver, U-85	fileFormats, U-98
laplacianSchemes keyword, U-114	finiteVolume, U-97
latestTime	foamCalcFunctions, U-97
keyword entry, U-111	forces, U-97
latestTime keyword, U-40	fvDOM, U-99
LaunderGibsonRSTM model, U-101	fvMotionSolvers, U-97
LaunderSharmaKE model, U-101	genericFvPatchField, U -98
layers keyword, U-152	incompressible LESM odels, $U-101$
leastSquares	incompressibleRASModels, U-100
keyword entry, U-117	incompressible Transport Models, $P-54$, $U-102$
leastSquares keyword, U-53	incompressibleTurbulenceModels, P-54
LESdeltas	interfaceProperties, U-102
library, U-101	jobControl, U-97
LESfilters	lagrangianIntermediate, U-98
library, U-101	lagrangian, U-98
LESModel	laminarFlameSpeedModels, $U-99$
keyword entry, U-42, U-183	linear, U-99
LESModel keyword, U-184	liquidMixtureProperties, U-100
LESProperties	liquidProperties, U-100
dictionary, U-183	meshTools, U-97
levels keyword, U-150	molecular Measurements, U-98
libraries, U-69	molecule, U-98
library	pairPatchAgglomeration, U-98
Chung, U-99	postCalc, U-97
LESdeltas, U-101	potential, U-98
LESfilters, U-101	primitive, P-23
MGridGenGAMGAgglomeration, U-98	radiationModels, U-99
ODE, U-97	randomProcesses, U-98
OSspecific, U-98	reactionThermophysicalModels, U-99
OpenFOAM, U-96	sampling, U-97
P1, U-99	solidMixtureProperties, U-100
PV3FoamReader, U-163	solidParticle, U-98
PVFoamReader, U-163	solidProperties, U-100
•	•
SLGThermo, U-100	solid, U-100
Wallis, U-99	specie, U-100
autoMesh, U-97	surfMesh, U-97
barotropicCompressibilityModels, U-99	surfaceFilmModels, U-102
basicSolidThermo, U-100	systemCall, U-97
basicThermophysicalModels, U-98	thermalPorousZone, U-100
blockMesh, U-97	thermophysicalFunctions, U-100
chemistryModel, U-100	thermophysical, U-179
coalCombustion, U-98	topoChangerFvMesh, U-98
compressibleLESModels, U-102	triSurface, U-97
compressible RAS Models, $U-101$	twoPhaseInterfaceProperties, U-102
conversion, U-98	utilityFunctionObjects, U-97
decomposition Methods, $U-98$	viewFactor, U-99
diesel $Spray,\ U\text{-}98$	vtkFoam, U - 163
distributionModels, U-98	vtkPV3Foam, $U-163$
dsmc, U-98	libs keyword, U-80, U-112

lid-driven cavity flow, U-19	keyword entry, U-82, U-83
LienCubicKE model, U-101	manualCoeffs keyword, U-83
LienCubicKELowRe model, U-101	mapFields utility, U-32, U-39, U-43, U-56, U-90,
LienLeschzinerLowRe model, U-101	U-160
Lights window panel, U-167	mapping
limited	fields, U-160
keyword entry, U-117, U-118	Marker Style menu, U-36
limitedCubic	matrices tools, U-97
keyword entry, U-116	max
limitedLinear	tensor member function, P-25
keyword entry, U-116	maxAlphaCo keyword, U-62
line	maxBoundarySkewness keyword, U-153
keyword entry, U-139	maxCo keyword, U-62
Line Style menu, U-36	maxConcave keyword, U-153
linear	maxDeltaT keyword, U-62
library, U-99	maxDeltaxyz model, U-101
linear	maxFaceThicknessRatio keyword, U-152
keyword entry, U-116, U-119	maxGlobalCells keyword, U-148
linearUpwind	maximum iterations, U-121
keyword entry, U-116, U-119	maxInternalSkewness keyword, U-153
liquid	maxIter keyword, U-121
electrically-conducting, P-67	maxLocalCells keyword, U-148
liquidMixtureProperties	maxNonOrtho keyword, U-153
library, U-100	maxThicknessToMedialRatio keyword, U-152
liquidProperties	mdEquilibrationFoam solver, U-89
library, U-100	mdFoam solver, U-89
lists, P-29	mdInitialise utility, U-90
•	mechanicalProperties
List <type> template class, P-29 localEuler</type>	dictionary, U-51
	memory tools, U-97
keyword entry, U-119	menu
location keyword, U-105	Color By, U-166
locationInMesh keyword, U-148, U-149	Current Time Controls, U-27, U-165
locDynOneEqEddy model, U-101	Edit, U-167, U-168
lowCpCoeffs keyword, U-182	Help, U-167
lowReOneEqEddy model, U-102	<u>-</u> ·
LRDDiffStress model, U-102	Line Style, U-36
LRR model, U-101	Marker Style, U-36
lsGrad	VCR Controls, U-27, U-165 View, U-167
fvc member function, P-37	,
LTSInterFoam solver, U-87	menu entry
LTSReactingParcelFoam solver, U-88	Plot Over Line, U-35
${f M}$	Save Animation, U-169
Mach utility, U-93	Save Screenshot, U-169
	Settings, U-168
mag	Show Color Legend, U-27
tensor member function, P-25	Solid Color, U-166
magneticFoam solver, U-89	Toolbars, U-167
magnetohydrodynamics, P-67	View Settings, U-26
magSqr	View Settings, U-26, U-167
tensor member function, P-25	Wireframe, U-166
Make directory, U-73	fvSchemes, U-53
make script/alias, U-71	mergeLevels keyword, U-123
Make/files file, U-74	mergeMeshes utility, U-91
manual	mergeOrSplitBaffles utility, U-91

P-86 Index

mergePatchPairs keyword, U-138	minTwist keyword, U-153
mergeTolerance keyword, U-146	minVol keyword, U-153
mesh	minVolRatio keyword, U-153
1-dimensional, U-130	mirrorMesh utility, U-91
1D, U-130	mixed
2-dimensional, U-130	boundary condition, U-136
2D, U-130	mixed $Smagorinsky\ \mathrm{model},\ U\text{-}101$
axi-symmetric, U-130	mixtureAdiabaticFlameT utility, $U-96$
basic, P-31	mode keyword, U-149
block structured, U-136	model
decomposition, U-81	APIfunctions, U-100
description, U-127	BirdCarreau, U-102
finite volume, P-31	CrossPowerLaw, U-102
generation, U-136, U-145	DeardorffDiffStress, U-102
grading, U-136, U-140	${\sf GuldersEGRLaminarFlameSpeed},\ {\sf U-99}$
grading, example of, P-53	${\sf GuldersLaminarFlameSpeed},\ {\hbox{U-}99}$
non-orthogonal, P-45	HerschelBulkley, $U-102$
refinement, P-62	LRDDiffStress, U-102
resolution, U-32	LRR, U-101
specification, U-127	${\sf LamBremhorstKE},\ U\text{-}101$
split-hex, U-145	Launder Gibson RSTM, $U-101$
Stereolithography (STL), U-145	LaunderSharmaKE, U - 101
surface, U-145	LienCubicKELowRe, U-101
validity constraints, U-127	LienCubicKE, U-101
Mesh Parts window panel, U-25	LienLeschzinerLowRe, U-101
meshes tools, U-97	NSRDSfunctions, U-100
meshQualityControls keyword, U-146	Newtonian, U-102
meshTools	Nonlinear KEShih, $U-101$
library, U-97	${\sf PrandtlDelta}, {\color{red}{\rm U-101}}$
message passing interface	RNGkEpsilon, U-101
openMPI, U-82	Smagorinsky2, U-101
method keyword, U-83	Smagorinsky, U- 101 , U- 102
metis	${\sf SpalartAllmarasDDES},\ {\sf U-102}$
keyword entry, U-83	SpalartAllmarasIDDES, $U-102$
MGridGenGAMGAgg lomeration	SpalartAllmaras, $U-101$, $U-102$
library, U-98	anisotropic Filter, $U-101$
MGridGen	${\it basicMultiComponentMixture},\ U\text{-}99,\ U\text{-}180$
keyword entry, U-123	chemistry Model, $U-100$
mhdFoam solver, P-69, U-89	chemistrySolver, U-100
midPoint	${\sf constLaminarFlameSpeed},\ U\text{-}99$
keyword entry, U-116	constTransport, $U-100$, $U-180$
midPoint keyword, U-175	cubeRootVolDelta, U - 101
midPointAndFace keyword, U-175	dieselMixture, U-99, U-180
min	distributed, U-98
tensor member function, P-25	dynLagrangian, U - 101
minArea keyword, U-153	dynMixedSmagorinsky, U - 101
minDeterminant keyword, U-153	dynOneEqEddy, U- 101 , U- 102
minFaceWeight keyword, U-153	dyn $Smagorinsky,\ U ext{-}101$
minFlatness keyword, U-153	eConstThermo, $U-100$, $U-179$
minMedianAxisAngle keyword, U-152	ePsiThermo, U-98, U-180
MINMOD differencing, P-38	egrMixture, U-99, U-180
minRefinementCells keyword, U-148	hConstThermo, U-100, U-179
minThickness keyword, U-152	hPolynomialThermo, U-100, U-179
minTriangleTwist keyword, U-153	hPsiMixtureThermo, U-99, U-180

hPsiThermo, U-98, U-180	MPI
hRhoMixtureThermo, U-99, U-180	openMPI, U-82
hRhoThermo, U-98, U-180	MRFInterFoam solver, U-87
hhuMixtureThermo, U-99, U-180	MRFMultiphaseInterFoam solver, U-87
homogenousDynSmagorinsky, U-101	MRFSimpleFoam solver, U-85
homogeneousMixture, U-99, U-180	mshToFoam utility, U-91
hsPsiMixtureThermo, U-99, U-180	mu keyword, U-182
hsPsiThermo, U-98, U-180	multiComponentMixture model, U-99, U-180
hsRhoMixtureThermo, U-99, U-180	multigrid
hsRhoThermo, U-98, U-180	geometric-algebraic, U-122
icoPolynomial, U-100, U-179	multiphaseInterFoam solver, U-87
inhomogeneousMixture, U-99, U-180	MUSCL
interfaceProperties, U-102	keyword entry, U-116
janafThermo, U-100, U-179	key word entry, 0-110
kEpsilon, U-100, U-101	$\mathbf N$
kOmegaSSTSAS, U-101	n keyword, U-83
kOmegaSST, U-100, U-101	nabla
kOmega, U-100	operator, P-27
laminar, U-100, U-101	nAlphaSubCycles keyword, U-63
	nBufferCellsNoExtrude keyword, U-152
laplaceFilter, U-101	nCellsBetweenLevels keyword, U-148
locDynOneEqEddy, U-101	neighbour
lowReOneEqEddy, U-102	dictionary, U-129
maxDeltaxyz, U-101	neighbourPatch keyword, U-142
mixedSmagorinsky, U-101	netgenNeutralToFoam utility, U-91
multiComponentMixture, U-99, U-180	Newtonian
oneEqEddy, U-101, U-102	
perfectGas, U-100, U-179	keyword entry, U-61
polynomialTransport, U-100, U-180	Newtonian model, U-102
powerLaw, U-102	nextWrite
ptsotchDecomp, U-98	keyword entry, U-111
pureMixture, U-99, U-180	nFaces keyword, U-130
qZeta, U-101	nFinestSweeps keyword, U-123
reactingMixture, U-99, U-180	nGrow keyword, U-152
realizableKE, U-101	nLayerIter keyword, U-152
reconstruct, U-98	nMoles keyword, U-181
scaleSimilarity, U-101	non-orthogonal mesh, P-45
scotchDecomp, U-98	nonBlocking
simpleFilter, U-101	keyword entry, U-80
smoothDelta, U - 101	none
specieThermo, U-100, U-180	keyword entry, U-115, U-122
spectEddyVisc, U-102	NonlinearKEShih model, U-101
sutherland Transport, $U-100$, $U-180$	nonNewtonianIcoFoam solver, U-86
veryInhomogeneousMixture, U-99, U-180	noWriteNow
modifyMesh utility, U-92	keyword entry, U-111
molecularMeasurements	nPostSweeps keyword, U-123
library, U-98	nPreSweeps keyword, U-123
molecule	nRelaxedIter keyword, U-152
library, U-98	nRelaxIter keyword, U-150, U-152
molWeight keyword, U-181	nSmoothNormals keyword, U-152
moveDynamicMesh utility, U-91	${\tt nSmoothPatch}\ {\tt keyword},\ {\tt U-150}$
moveEngineMesh utility, U-91	nSmoothScale keyword, U-153
moveMesh utility, U-91	${\tt nSmoothSurfaceNormals}\ {\tt keyword},\ {\tt U-152}$
movingWallVelocity	nSmoothThickness keyword, U-152
boundary condition, U-137	nSolveIter keyword, U-150

P-88

NSRDSfunctions model, U-100	boundary condition, U-137
null	particleTracks utility, U-94
keyword entry, U-174	patch
numberOfSubdomains keyword, U-83	boundary condition, U-135
	patch
O	keyword entry, U-134, U-176
object keyword, U-105	patchAverage utility, U-93
objToVTK utility, U-91	patches keyword, U-138
ODE	patchIntegrate utility, U-94
library, U-97	patchMap keyword, U-160
oneEqEddy model, U-101, U-102	patchSummary utility, U-96
Opacity text box, U-167	
OpenFOAM	PBiCG
applications, U-69	keyword entry, U-121
file format, U-104	PCG
,	keyword entry, U-121
libraries, U-69	pdfPlot utility, U-94
OpenFOAM	PDRFoam solver, U-88
library, U-96	PDRMesh utility, U-92
OpenFOAM file syntax	Pe utility, U-93
//, U-104	perfectGas model, U-100, U-179
openMPI	permutation symbol, P-19
message passing interface, U-82	pimpleDyMFoam solver, U-86
MPI, U-82	pimpleFoam solver, U-86
operator	Pipeline Browser window, U-25, U-164
scalar, P-28	PISO
vector, P-27	dictionary, U-25
Options window, U-168	pisoFoam solver, U-19, U-86
options file, U-73	Plot Over Line
order keyword, U-83	menu entry, U-35
Orientation Axes button, U-26, U-167	plot3dToFoam utility, U-91
OSspecific 25, 5 25, 5 25,	pointField class, P-31
library, U-98	pointField <type> template class, P-33</type>
outer product, see tensor, outer product	points
outlet	dictionary, U-129, U-136
	polyBoundaryMesh class, P-31
boundary condition, P-69	polyDualMesh utility, U-91
outletInlet	• •
boundary condition, U-137	polyLine
outside	keyword entry, U-139
keyword entry, U-149	polyMesh directory, U-104, U-129
owner	polyMesh class, P-31, U-127, U-129
dictionary, U-129	polynomialTransport model, U-100, U-180
P	polyPatch class, P-31
_	polyPatchList class, P-31
p field, U-24	polySpline
P1	keyword entry, U-139
library, U-99	$porous Explicit Source Reacting Parcel Foam \ solver$
p_rhgRefCell keyword, U-125	U-89
p_rhgRefValue keyword, U-125	porousInterFoam solver, U-87
pairPatchAgglomeration	porousSimpleFoam solver, U-86
library, U-98	post-processing, U-163
paraFoam, U-25, U-163	post-processing
parallel	paraFoam, U-163
running, U-81	postCalc
partialSlip	library, U-97

postChannel utility, U-94	${f R}$
potential	R utility, U-93
library, U-98	radiationModels
potentialFoam solver, P-46, U-85	library, U-99
pow	randomProcesses
tensor member function, P-25	library, U-98
powerLaw model, U-102	RASModel
pPrime2 utility, U-93	keyword entry, U-42, U-183
Pr keyword, U-182	RASModel keyword, U-183
PrandtlDelta model, U-101	raw
preconditioner keyword, U-121, U-122	keyword entry, U-112, U-174
pRefCell keyword, U-25, U-125	reactingFoam solver, U-88
pRefValue keyword, U-25, U-125	reactingMixture model, U-99, U-180
pressure keyword, U-51	reactingParcelFilmFoam solver, U-89
pressure waves	reactingParcelFoam solver, U-89
in liquids, P-62	reaction Thermophysical Models
pressureDirectedInletVelocity	library, U-99
boundary condition, U-137	realizableKE model, U-101
pressureInletVelocity	reconstruct model, U-98
boundary condition, U-137	reconstructPar utility, U-85, U-95
pressureOutlet	reconstructParMesh utility, U-95
boundary condition, P-63	redistributeMeshPar utility, U-96
pressureTransmissive	refGradient keyword, U-136
boundary condition, U-137	refineHexMesh utility, U-92
primitive	refinementRegions keyword, U-149
library, P-23	refinementLevel utility, U-92
primitives tools, U-97	refinementRegions keyword, U-148, U-150
printCoeffs keyword, U-43, U-183	refinementSurfaces keyword, U-148
processorWeights keyword, U-82	refineMesh utility, U-91
probeLocations utility, U-94	refineWallLayer utility, U-92
process	Refresh Times button, U-27
background, U-26, U-81	regions keyword, U-60
foreground, U-26	relative tolerance, U-121
processor	relativeSizes keyword, U-152
boundary condition, U-135	relaxed keyword, U-153
processor	relTol keyword, U-54, U-121
keyword entry, U-134	removeFaces utility, U-92
processorN directory, U-82	Render View window, U-168
processorWeights keyword, U-83	Render View window panel, U-168
Properties window panel, U-27, U-164	renumberMesh utility, U-91
ptot utility, U-94	Rescale to Data Range button, U-27
ptsotchDecomp model, U-98	Reset button, U-164
pureMixture model, U-99, U-180	resolveFeatureAngle keyword, U-148
purgeWrite keyword, U-112	restart, U-40
PV3FoamReader	Reynolds number, U-19, U-23
library, U-163	rhoPorousMRFLTSPimpleFoam solver, U-86
PVFoamReader	rhoPorousMRFPimpleFoam solver, U-86
library, U-163	rhoPorousMRFSimpleFoam solver, U-86
	rhoCentralDyMFoam solver, U-86
\mathbf{Q}	rhoCentralFoam solver, U-86
Q utility, U-93	rhoPimpleFoam solver, U-86
QUICK	rhoReactingFoam solver, U-88
keyword entry, U-119	rhoSimpleFoam solver, U-86
qZeta model, U-101	rhoSimplecFoam solver, U-86

P-90 Index

rmdepall script/alias, U-76	Settings
RNGkEpsilon model, U-101	menu entry, U-168
roots keyword, U-83, U-84	settlingFoam solver, U-87
rotateMesh utility, U-91	SFCD
run	keyword entry, U-116, U-119
parallel, U-81	shallowWaterFoam solver, U-86
run directory, U-103	shape, U-140
runTime	Show Color Legend
keyword entry, U-33, U-111	menu entry, U-27
runTimeModifiable keyword, U-112	SI units, U-107
Tunitimonatification neg word, 6 112	simple
${f S}$	keyword entry, U-82, U-83
sammToFoam utility, U-91	simpleFilter model, U-101
sample utility, U-94, U-173	simpleFoam solver, P-54, U-86
sampling	simpleGrading keyword, U-140
library, U-97	simpleSpline
Save Animation	keyword entry, U-139
menu entry, U-169	, , , , , , , , , , , , , , , , , , ,
Save Screenshot	simulationType keyword, U-42, U-61, U-183
menu entry, U-169	singleCellMesh utility, U-92
scalar, P-16	skew
operator, P-28	tensor member function, P-25
scalar class, P-23	skewLinear
scalarField class, P-29	keyword entry, U-116, U-119
•	SLGThermo
scalarTransportFoam solver, U-85	library, U-100
scale	slice class, P-31
tensor member function, P-25	slip
scalePoints utility, U-157	boundary condition, U-137
scaleSimilarity model, U-101	Smagorinsky model, U-101, U-102
scheduled	Smagorinsky2 model, U-101
keyword entry, U-80	smapToFoam utility, $U-93$
scientific	smoothDelta model, U-101
keyword entry, U-112	smoother keyword, U-123
scotch	smoothSolver
keyword entry, U-82, U-83	keyword entry, U-121
scotchCoeffs keyword, U-83	snap keyword, U-146
scotchDecomp model, U-98	snapControls keyword, U-146
script/alias	snappyHexMesh utility
foamCorrectVrt, $U-158$	background mesh, U-146
foamJob, $U-177$	cell removal, U-149
foamLog, $U-177$	cell splitting, U-147
make, $U-71$	mesh layers, U-150
rmdepall, U - 76	meshing process, U-145
wclean, U-75	snapping to surfaces, U-150
wmake, U-71	snappyHexMesh utility, U-90, U-145
second time derivative, P-37	snappyHexMeshDict file, U-145
Seed window, U-169	snGrad
selectCells utility, U-92	fvc member function, P-37
Set Ambient Color button, U-166	snGradCorrection
setFields utility, U-60, U-90	fvc member function, P-37
setFormat keyword, U-174	snGradSchemes keyword, U-114
sets keyword, U-174	solid
setSet utility, U-91	library, U-100
setsToZones utility, U-92	Solid Color

menu entry, U-166	mdEquilibrationFoam, U-89
solidDisplacementFoam solver, U-89	mdFoam, U-89
solidDisplacementFoam solver, U-52	mhdFoam, P-69, U-89
solidEquilibriumDisplacementFoam solver, U-89	multiphaseInterFoam, U-87
solidMixtureProperties	nonNewtonianIcoFoam, U-86
library, U-100	pimpleDyMFoam, U-86
solidParticle	pimpleFoam, U-86
library, U-98	pisoFoam, U-19, U-86
solidProperties	porousExplicitSourceReactingParcelFoam,
library, U-100	U-89
solver	porousInterFoam, U-87
LTSInterFoam, U-87	porousSimpleFoam, U-86
LTSReactingParcelFoam, U-88	potentialFoam, P-46, U-85
MRFInterFoam, U-87	reactingFoam, U-88
MRFMultiphaseInterFoam, U-87	reactingParcelFilmFoam, U-89
MRFSimpleFoam, U-85	reactingParcelFoam, U-89
PDRFoam, U-88	rhoCentralDyMFoam, U-86
SRFSimpleFoam, U-86	rhoCentralFoam, U-86
XiFoam, U-88	rhoPimpleFoam, U-86
adjointShapeOptimizationFoam, U-85	rhoReactingFoam, U-88
blockMesh, P-47	rhoSimpleFoam, U-86
boundaryFoam, U-85	rhoSimpler Gain, U-86
bubbleFoam, U-87	rhoPorousMRFLTSPimpleFoam, U-86
buoyantBaffleSimpleFoam, U-88	rhoPorousMRFPimpleFoam, U-86
buoyantBoussinesqPimpleFoam, U-88	rhoPorousMRFSimpleFoam, U-86
buoyantBoussinesqSimpleFoam, U-88	scalarTransportFoam, U-85
buoyantPimpleFoam, U-88	settlingFoam, U-87
buoyantSimpleFoam, U-88	shallowWaterFoam, U-86
buoyantSimpleRadiationFoam, U-88	simpleFoam, P-54, U-86
cavitatingFoam, U-87	solidDisplacementFoam, U-89
channelFoam, U-85	solidDisplacementFoam, U-52
chemFoam, U-88	solidEquilibriumDisplacementFoam, U-89
chtMultiRegionFoam, U-88	sonicDyMFoam, U-86
coalChemistryFoam, U-88	,
coldEngineFoam, U-88	sonicFoam, P-60, U-86 sonicLiquidFoam, P-63, U-86
,	. , , ,
compressibleInterFoam, U-87 dieselEngineFoam, U-88	twoLiquidMixingFoam, U-87
,	twoPhaseEulerFoam, U-87
dieselFoam, U-88	uncoupledKinematicParcelFoam, U-89 windSimpleFoam, U-86
dnsFoam, U-87	• /
dsmcFoam, U-89	solver keyword, U-54, U-121
electrostaticFoam, U-89	solver relative tolerance, U-121
engineFoam, U-88	solver tolerance, U-121
financialFoam, U-89	solvers keyword, U-120
fireFoam, U-88	sonicDyMFoam solver, U-86
icoFoam, U-19, U-23, U-24, U-26, U-85	sonicFoam solver, P-60, U-86
icoUncoupledKinematicParcelDyMFoam,	sonicLiquidFoam solver, P-63, U-86
U-88	source, P-37
icoUncoupledKinematicParcelFoam, U-88	SpalartAllmaras model, U-101, U-102
interDyMFoam, U-87	SpalartAllmarasDDES model, U-102
interFoam, U-87	SpalartAllmarasIDDES model, U-102
interMixingFoam, U-87	specie
interPhaseChangeFoam, U-87	library, U-100
laplacianFoam, U-85	specie keyword, U-181
magneticFoam, $ ext{U-89}$	specieThermo model, U-100, U-180

P-92 Index

spectEddyVisc model, U-102	surfaceFind utility, U-94
spline keyword, U-138	surfaceFormat keyword, U-174
splitCells utility, U-92	surfaceInertia utility, U-95
splitMesh utility, U-92	surfaceMesh tools, U-97
splitMeshRegions utility, U-92	surfaceMeshConvert utility, U-95
sqr	surfaceMeshConvertTesting utility, U-95
tensor member function, P-25	surfaceMeshExport utility, U-95
sqrGradGrad	surfaceMeshImport utility, U-95
fvc member function, P-37	surfaceMeshInfo utility, U-95
SRFSimpleFoam solver, U-86	surfaceMeshTriangulate utility, U-95
star3ToFoam utility, U-91	surfaceNormalFixedValue
star4ToFoam utility, U-91	boundary condition, U-137
startFace keyword, U-130	surfaceOrient utility, U-95
startFrom keyword, U-24, U-111	surfacePointMerge utility, U-95
starToFoam utility, U-154	surfaceRedistributePar utility, U-95
startTime	surfaceRefineRedGreen utility, U-95
keyword entry, U-24, U-111	surfaces keyword, U-174
startTime keyword, U-24, U-111	surfaceSmooth utility, U-95
steady flow	surfaceSplitByPatch utility, U-95
turbulent, P-53	surfaceSplitNonManifolds utility, U-95
steadyParticleTracks utility, U-94	surfaceSubset utility, U-95
steadyState	surfaceToPatch utility, U-95
keyword entry, U-119	surfaceTransformPoints utility, U-95
Stereolithography (STL), U-145	surfMesh
stitchMesh utility, U-92	library, U-97
stl	SuSp
keyword entry, U-174	fvm member function, P-37
stopAt keyword, U-111	sutherlandTransport model, U-100, U-180
strategy keyword, U-82, U-83	symm
streamFunction utility, U-93	tensor member function, P-25
stress analysis of plate with hole, U-47	symmetryPlane
stressComponents utility, U-93	boundary condition, P-63, U-135
Style window panel, U-25, U-166	symmetryPlane
Su	keyword entry, U-134
fvm member function, P-37	symmTensorField class, P-29
subsetMesh utility, U-92	symmTensorThirdField class, P-29
summation convention, P-17	system directory, P-50, U-104
SUPERBEE differencing, P-38	systemCall
supersonic flow, P-59	library, U-97
supersonic flow over forward step, P-58	
supersonicFreeStream	${f T}$
boundary condition, U-137	T()
surface mesh, U-145	tensor member function, P-25
surfaceAdd utility, U-94	Tcommon keyword, U-182
surfaceAutoPatch utility, U-94	template class
surfaceCheck utility, U-94	GeometricBoundaryField, P-32
surfaceClean utility, U-94	fvMatrix, P-33
surfaceCoarsen utility, U-94	dimensioned <type>, P-25</type>
surfaceConvert utility, U-94	FieldField <type>, P-32</type>
surfaceFeatureConvert utility, U-94	Field <type>, P-29</type>
surfaceFeatureExtract utility, U-94, U-148	geometricField <type>, P-32</type>
surfaceField <type> template class, P-33</type>	List <type>, P-29</type>
surfaceFilmModels	pointField <type>, P-33</type>
library, U-102	surfaceField <type>, P-33</type>

volField <type>, P-33</type>	*, P-25
temporal discretisation, P-42	+, P-25
Crank Nicholson, P-42	-, P-25
Euler implicit, P-42	/, P-25
explicit, P-42	&, P-25
in OpenFOAM, P-43	&&, P-25
tensor, P-15	^, P-25
addition, P-17	cmptAv, P-25
algebraic operations, P-17	cofactors, P-25
algebraic operations in OpenFOAM, P-23	det, P-25
antisymmetric, see tensor, skew	dev, P-25
calculus, P-27	diag, P-25
classes in OpenFOAM, P-23	I, P-25
cofactors, P-22	inv, P-25
component average, P-20	mag, P-25
component average, 1-20 component maximum, P-20	C ,
- · · · · · · · · · · · · · · · · · · ·	magSqr, P-25
component minimum, P-20	max, P-25
determinant, P-22	min, P-25
deviatoric, P-21	pow, P-25
diagonal, P-21	scale, P-25
dimension, P-16	skew, P-25
double inner product, P-19	sqr, P-25
geometric transformation, P-20	symm, P-25
Hodge dual, P-22	T(), P-25
hydrostatic, P-21	tr, P-25
identities, P-21	transform, P-25
identity, P-20	tensorField class, P-29
inner product, P-18	tensorThirdField class, P-29
inverse, P-22	tetgenToFoam utility, U-91
magnitude, P-20	text box
magnitude squared, P-20	Opacity, U-167
mathematics, P-15	thermal Porous Zone
notation, P-17	library, U-100
nth power, P-20	thermalProperties
outer product, P-19	dictionary, $U-52$
rank, P-16	thermodynamics keyword, U-181
rank 3, P-16	thermophysical
scalar division, P-18	library, U-179
scalar multiplication, P-17	thermophysicalFunctions
scale function, P-20	library, U-100
second rank, P-16	thermophysicalProperties
skew, P-21	dictionary, U-179
square of, P-20	thermoType keyword, U-179
subtraction, P-17	Thigh keyword, U-182
symmetric, P-21	time
symmetric rank 2, P-16	control, U-111
symmetric rank 3, P-16	time derivative, P-37
trace, P-21	first, P-39
transformation, P-20	second, P-37, P-39
transpose, P-16, P-21	time step, U-24
triple inner product, P-19	timeFormat keyword, U-112
vector cross product, P-19	timePrecision keyword, U-112
	,
tensor class, P-23	timeScheme keyword, U-114
tensor member function	timeStamp

P-94 Index

keyword entry, U-80	turbulence
timeStampMaster	dissipation, U-41
keyword entry, U-80	kinetic energy, U-41
timeStep	length scale, U-42
keyword entry, U-24, U-33, U-111	turbulence keyword, U-183
Tlow keyword, U-182	turbulence model
tolerance	RAS, U-41
solver, U-121	turbulenceProperties
solver relative, U-121	dictionary, U-42, U-61, U-183
tolerance keyword, U-54, U-121, U-150	turbulent flow
Toolbars	steady, P-53
menu entry, U-167	turbulentInlet
tools	boundary condition, U-137
algorithms, U-96	tutorials
cfdTools, U-97	breaking of a dam, U-57
containers, U-96	lid-driven cavity flow, U-19
db, U-96	stress analysis of plate with hole, U-47
dimensionSet, U-97	tutorials directory, P-45, U-19
dimensioned Types, U-97	twoLiquidMixingFoam solver, U-87
fields, U-97	twoPhaseEulerFoam solver, U-87
finiteVolume, U-97	twoPhaseInterfaceProperties
fvMatrices, U-97	library, U-102
fvMesh, U-97	type keyword, U-132, U-133
global, U-97	type keyword, 0 152, 0 150
graph, U-97	\mathbf{U}
interpolations, U-97	U field, U-24
interpolation, U-97	Ucomponents utility, P-70
matrices, U-97	UMIST
memory, U-97	keyword entry, U-115
meshes, U-97	uncompressed
primitives, U-97	keyword entry, U-112
surfaceMesh, U-97	uncorrected
volMesh, U-97	keyword entry, U-117, U-118
topoChangerFvMesh	uncoupledKinematicParcelFoam solver, U-89
library, U-98	uniform keyword, U-175
topoSet utility, U-92	units
topoSetSource keyword, U-60	base, U-107
totalPressure	of measurement, P-25, U-107
boundary condition, U-137	S.I. base, P-25
tr	SI, U-107
tensor member function, P-25	Système International, U-107
trace, see tensor, trace	United States Customary System, U-107
traction keyword, U-51	USCS, U-107
transform	Update GUI button, U-165
tensor member function, P-25	uprime utility, U-93
transformPoints utility, U-92	upwind
transport keyword, U-181	keyword entry, U-116, U-119
transportProperties	upwind differencing, P-38, U-62
dictionary, U-23, U-40, U-43	USCS units, U-107
transportProperties file, U-61	Use Parallel Projection button, U-26
triple inner product, P-19	Use parallel projection button, U-167
triSurface	utility
library, U-97	Co, U-93
Ts keyword, U-182	Lambda2, U-93

Mach, U-93	foamMeshToFluent, U-90, U-170
PDRMesh, U-92	foamToEnsightParts, U-92
Pe, U-93	foamToEnsight, U-92
Q, U-93	foamToFieldview9, U-92
R, U-93	foamToGMV, U-92
Ucomponents, P-70	foamToStarMesh, U-90
adiabaticFlameT, U-96	foamToSurface, U-91
ansysToFoam, U-90	foamToTecplot360, U-92
applyBoundaryLayer, U-90	foamToVTK, U-92
applyWallFunctionBoundaryConditions,	foamUpgradeCyclics, U-90
U-90	foamUpgradeEvSolution, U-90
attachMesh, U-91	gambitToFoam, U-91, U-154
autoPatch, U-91	gmshToFoam, U-91
autoRefineMesh, U-92	ideasToFoam, U-154
blockMesh, U-38, U-90, U-136	ideasUnvToFoam, U-91
boxTurb, U-90	insideCells, U-91
cfx4ToFoam, U-90, U-154	kivaToFoam, U-91
	•
changeDictionary, U-90	mapFields, U-32, U-39, U-43, U-56, U-90,
checkMesh, U-91, U-155	U-160
chemkinToFoam, U-96	mdInitialise, U-90
collapseEdges, U-92	mergeMeshes, U-91
combinePatchFaces, U-92	mergeOrSplitBaffles, U-91
createBaffles, U-91	mirrorMesh, U-91
createPatch, U-91	mixtureAdiabaticFlameT, U-96
createTurbulenceFields, U-93	modifyMesh, U-92
datToFoam, U-90	moveDynamicMesh, U-91
decomposePar, U-81, U-82, U-95	moveEngineMesh, U-91
deformedGeom, U-91	moveMesh, U-91
dsmcFieldsCalc, U-94	mshToFoam, U-91
dsmcInitialise, U-90	${\sf netgenNeutralToFoam}, \hbox{U-}91$
engineCompRatio, U-94	objToVTK, U-91
engineSwirl, U-90	pPrime2, U-93
ensight74FoamExec, U-172	particleTracks, $U-94$
ensightFoamReader, U -92	patchAverage, U - 93
enstrophy, $U-93$	patchIntegrate, U - 94
equilibriumCO, U-96	patchSummary, $U-96$
equilibriumFlameT, U-96	pdfPlot, U-94
execFlowFunctionObjects, U-94	plot $3dToFoam, U-91$
expandDictionary, U-96	polyDualMesh, U - 91
extrude2DMesh, U -90	postChannel, U -94
extrudeMesh, U -90	probeLocations, U-94
extrudeToRegionMesh, U-90	ptot, U-94
faceAgglomerate, U - 90	reconstructParMesh, $U-95$
fieldview9Reader, U-92	reconstructPar, U-85, U-95
flattenMesh, U-91	redistributeMeshPar, $U-96$
flowType, U-93	refineHexMesh, U-92
fluent3DMeshToFoam, U-90	refineMesh, U-91
fluentMeshToFoam, U-90, U-154	refineWallLayer, U-92
foamCalc, U-34, U-94	refinementLevel, U-92
foamDataToFluent, U-92, U-170	removeFaces, U-92
foamDebugSwitches, U-96	renumberMesh, U-91
foamFormatConvert, U-96	rotateMesh, U-91
foamInfoExec, U-96	sammToFoam, U-91
foamListTimes, U-94	sample, U-94, U-173
· · · · · · · · · · · · · · · · · · ·	• • •

P-96 Index

scalePoints, U-157	wallShearStress, $U-93$
selectCells, U-92	wdot, U-94
setFields, U-60, U-90	writeCellCentres, U-94
setSet, U-91	writeMeshObj, U-91
setsToZones, U-92	yPlusLES, U-93
singleCellMesh, U-92	yPlusRAS, U-93
smapToFoam, U-93	zipUpMesh, U-92
snappyHexMesh, U-90, U-145	utilityFunctionObjects
splitCells, U-92	library, U-97
splitMeshRegions, U-92	•
splitMesh, U-92	\mathbf{V}
star3ToFoam, U-91	value keyword, U-23, U-136
star4ToFoam, U-91	valueFraction keyword, U-136
starToFoam, U-154	van Leer differencing, P-38
steadyParticleTracks, U-94	vanLeer
stitchMesh, U-92	keyword entry, U-116
streamFunction, U-93	VCR Controls menu, U-27, U-165
stressComponents, U-93	vector, P-16
subsetMesh, U-92	operator, P-27
surfaceAdd, U-94	unit, P-20
surfaceAutoPatch, U-94	vector class, P-23, U-107
surfaceCheck, U-94	vector product, see tensor, vector cross product
surfaceClean, U-94	vectorField class, P-29
surfaceCoarsen, U-94	version keyword, U-105
surfaceConvert, U-94	vertices keyword, U-22, U-138, U-139
surfaceFeatureConvert, U-94	veryInhomogeneousMixture model, U-99, U-180
surfaceFeatureExtract, U-94, U-148	View menu, U-167
surfaceFind, U-94	View Settings
surfaceInertia, U-95	menu entry, U-26, U-167
surfaceMeshConvertTesting, U-95	View Settings (Render View) window, U-167
surfaceMeshConvert, U-95	View Settings
surfaceMeshExport, U-95	menu entry, U-26
surfaceMeshImport, U-95	viewFactor
surfaceMeshInfo, U-95	library, U-99
surfaceMeshTriangulate, U-95	viewFactorGen utility, U-90
surfaceOrient, U-95	viscosity
surfacePointMerge, U-95	kinematic, U-23, U-43
surfaceRedistributePar, U-95	volField <type> template class, P-33</type>
surfaceRefineRedGreen, U-95	volMesh tools, U-97
surfaceSmooth, U-95	vorticity utility, U-93
surfaceSplitByPatch, U-95	vtk
surfaceSplitNonManifolds, U-95	keyword entry, U-174
surfaceSubset, U-95	vtkFoam
surfaceToPatch, U-95	library, U-163
surfaceTransformPoints, U-95	vtkPV3Foam
tetgenToFoam, U-91	library, U-163
topoSet, U-92	norary, 0-100
transformPoints, U-92	\mathbf{W}
uprime, U-93	wall
viewFactorGen, U-90	boundary condition, P-63, P-69, U-59.
vorticity, U-93	U-135
wallFunctionTable, U-90	wall
wallGradU, U-93	keyword entry, U-134
wallHeatFlux, U-93	wallBuoyantPressure
,	-

boundary condition, U-137	environment variable, U-76
wallFunctionTable utility, $U-90$	WM_MPLIB
wall $GradU$ utility, $U\text{-}93$	environment variable, U-76
wallHeatFlux utility, U-93	WM_OPTIONS
Wallis	environment variable, U-76
library, U-99	WM_PRECISION_OPTION
wallShearStress utility, U-93	environment variable, U-76
wclean script/alias, U-75	WM_PROJECT
wdot utility, U-94	environment variable, U-76
wedge	WM_PROJECT_DIR
boundary condition, U-130, U-135, U-144	environment variable, U-76
wedge	WM_PROJECT_INST_DIR
keyword entry, U-134	environment variable, U-76
window	WM_PROJECT_USER_DIR
Color Legend, U-29	environment variable, U-76
Options, U-168	WM_PROJECT_VERSION
Pipeline Browser, U-25, U-164	environment variable, U-76
Render View, U-168	wmake
Seed, U-169	platforms, U-72
View Settings (Render View), U-167	wmake script/alias, U-71
window panel	word class, P-25, P-31
Animations, U-168	writeCellCentres utility, U-94
Annotation, U-26, U-167	${\tt writeCompression} \ {\rm keyword}, \ {\rm U\text{-}112}$
Charts, U-168	writeControl
Color Legend, U-166	keyword entry, U-111
Color Scale, U-166	writeControl keyword, U-24, U-62, U-111
Colors, U-168	writeFormat keyword, U-56, U-112
Display, U-25, U-27, U-164, U-165	writeInterval keyword, U-24, U-33, U-111
General, U-167, U-168	writeMeshObj utility, U-91
Information, U-164	writeNow
Lights, U-167	keyword entry, U-111
Mesh Parts, U-25	writePrecision keyword, U-112
Properties, U-27, U-164	\mathbf{X}
Render View, U-168	X X
Style, U-25, U-166	keyword entry, U-175
windSimpleFoam solver, U-86	XiFoam solver, U-88
Wireframe	xmgr
menu entry, U-166	keyword entry, U-112, U-174
WM_ARCH	xyz
environment variable, U-76	keyword entry, U-175
WM_ARCH_OPTION	key word energy, o 170
environment variable, U-76	Y
WM_COMPILE_OPTION	у
environment variable, U-76	keyword entry, U-175
WM_COMPILER	yPlusLES utility, U-93
environment variable, U-76	yPlusRAS utility, U-93
WM_COMPILER_BIN	
environment variable, U-76	${f Z}$
WM_COMPILER_DIR	z
environment variable, U-76	keyword entry, U-175
WM_COMPILER_LIB	zeroGradient
environment variable, U-76	boundary condition, U-136
WM_DIR	zipUpMesh utility, U-92