Shallow water simulation

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Introduction

The Fifth Dwarf

In an 2006 report on "The Landscape of Parallel Computing", a group of parallel computing researchers at Berkeley suggested that high-performance computing platforms be evaluated with respect to "13 dwarfs" – frequently recurring computational patterns in high-performance scientific code. This assignment represents the fifth dwarf on the list: structured grid computations. We have already seen one example of structured grid computations in class with the Game of Life, but this pattern is common in many areas of physical simulation. It features high spatial locality and allows regular access patterns, and is in principal one of the easier types of computations to parallelize.

Structured grid computations are particularly common in fluid dynamics simulations, and the code that you will tune in this assignment is an example of such a simulation. You will be optimizing and parallelizing a finite volume solver for the shallow water equations, a two-dimensional PDE system that describes waves that are very long compared to the water depth. This is an important system of equations that applies even in situations that you might not initially think of as "shallow"; for example, tsunami waves are long enough that they can be modeled using the shallow water equations even when traveling over mile-deep parts of oceans. There is also a very readable Wikipedia article on the shallow water equations, complete with a little animation similar to the one you will be producing. I was inspired to use this system for our assignment by reading the chapter on shallow water simulation in MATLAB from Cleve Moler's books on "Experiments in MATLAB" and then getting annoyed that he chose a method with a stability problem.

Your mission

You are provided with the following performance-critical C++ files:

- shallow2d.h an implementation of shallow water physics
- minmod.h a (possibly efficient) MinMod limiter
- central2d.h a finite volume solver for 2D hyperbolic PDE

In addition, you are given the following codes for running the simulation and getting pretty pictures out:

- meshio.h I/O routines
- driver.cc a driver file that runs the simuation
- visualizer.py Python visualization script

For this assignment, you should attempt three tasks:

- 1. Profiling: The current code is not particularly tuned, and there are surely some bottlenecks. Profile the computation and determine what parts of the code are slowest. I encourage you to use profiling tools (e.g. VTune Amplifier), but you may also manually instrument the code with timers.
- 2. Parallelization: You should parallelize your code using OpenMP, and study the speedup versus number of processors on both the main cores on the nodes and on the Xeon Phi boards. Set up both strong and weak scaling studies, varying the number of threads you employ. You may start with a naive parallelization (e.g. parallelizing the for loops in the various subroutines), but this is not likely to give you the best possible performance, particularly on the Phi.
- 3. Tuning: You should tune your code in order to get it to run as fast as possible. This may involve a domain decomposition with per-processor ghost cells and batching of time steps between synchronization; it may involve vectorization of the computational kernels; or it may involve eliminating redundant computations in the current implementation.

The primary deliverable for your project is a report that describes your performance experiments and attempts at tuning, along with what you learned about things that did or did not work. Good things for the report include:

- Profiling results
- Speedup plots and scaled speedup plots
- Performance models that predict speedup

In addition, you should also provide the code, and ideally scripts that make it simple to reproduce any performance experiments you've run.

Tuning readings

You are welcome to read about the shallow water equations and about finite volume methods if you would like, and this may help you in understanding what you're seeing. But it is possible to tune your codes without understanding all the physics behind what is going on! I recommend two papers in particular that talk about tuning of finite difference and finite volume codes on accelerators: one on optimizing a 3D finite difference code on the Intel cores and the Xeon Phi, and one on optimizing a shallow water simulator on NVidia GPUs. The GPU architecture is different, but some of the concepts should transfer to thinking about improving performance on the Phis.

Logistical notes

Timeline

As with the previous assignment, this assignment involves two stages. You have just over three weeks, and should work in teams of three. After two weeks (Oct 15), you should submit your initial report (and code) for peer review; reviews are due by Oct 20. Final reports are due one week later (Oct 27). I hope many of you will wrap up before that; the third project should be out by Oct 22.

Peer review logistics

Since the first assignment, GitHub has added a feature to attach PDF files to issues and pull request comments. You should take advantage of this feature to submit your review as a comment on the pull request for the group you are reviewing. You should still look at the codes from the other groups, though!

Notes on the documentation

The documentation for this project is generated automatically from structured comments in the source files using a simple tool called ldoc that I wrote some years ago. You may or may not choose to use ldoc for your version.

Notes on C++ usage

The reference code I've given you is in C++. I wanted to use C, but was persuaded that I could write a clearer, cleaner implementation in C++ and an implementation that will ultimately be easier for you to tune.

While I have tried not to do anything too obscure, this code does use some C++ 11 features (e.g. the constexpr notation used to tell the compiler something is

a compile-time constant). If you want to build on your own machine, you may need to figure out the flag needed to tell your compiler that you are using this C++ dialect.

Shallow water equations

Physics picture

The shallow water equations treat water as incompressible and inviscid, and assume that the horizontal velocity remains constant in any vertical column of water. The unknowns at each point are the water height and the total horizontal momentum in a water column; the equations describe conservation of mass (fluid is neither created nor destroyed) and conservation of linear momentum. We will solve these equations with a numerical method that also exactly conserves mass and momentum (up to rounding error), though it only approximately conserves energy.

The basic variables are water height (h), and the velocity components (u, v). We write the governing equations in the form

$$U_t = F(U)_x + G(U)_y$$

where

$$U = \begin{bmatrix} h \\ hu \\ hv \end{bmatrix}, F = \begin{bmatrix} hu \\ h^2u + gh^2/2 \\ huv \end{bmatrix} G = \begin{bmatrix} hv \\ huv \\ h^2v + gh^2/2 \end{bmatrix}$$

The functions F and G are called *fluxes*, and describe how the conserved quantities (volume and momentum) enter and exit a region of space.

Note that we also need a bound on the characteristic wave speeds for the problem in order to ensure that our method doesn't explode; we use this to control the Courant-Friedrichs-Levy (CFL) number relating wave speeds, time steps, and space steps. For the shallow water equations, the characteristic wave speed is \sqrt{gh} where g is the gravitational constant and h is the height of the water; in addition, we have to take into account the velocity of the underlying flow.

Implementation

Our solver takes advantage of C++ templates to get (potentially) good performance while keeping a clean abstraction between the solver code and the details of the physics. The Shallow2D class specifies the precision of the comptutation (single precision), the data type used to represent vectors of unknowns and fluxes (the C++ std::array). We are really only using the class as name space; we never create an instance of type Shallow2D, and the flux and wave_speed

functions needed by the solver are declared as static (and inline, in the hopes of getting the compiler to optimize for us).

```
struct Shallow2D {
    // Type parameters for solver
    typedef float real;
    typedef std::array<real,3> vec;
    // Gravitational force (compile time constant)
    static constexpr real g = 9.8;
    // Compute shallow water fluxes F(U), G(U)
    static void flux(vec& FU, vec& GU, const vec& U) {
        real h = U[0], hu = U[1], hv = U[2];
        FU[0] = hu;
        FU[1] = hu*hu/h + (0.5*g)*h*h;
        FU[2] = hu*hv/h;
        GU[0] = hv;
        GU[1] = hu*hv/h;
        GU[2] = hv*hv/h + (0.5*g)*h*h;
    }
    // Compute shallow water wave speed
    static void wave_speed(real& cx, real& cy, const vec& U) {
        using namespace std;
        real h = U[0], hu = U[1], hv = U[2];
        real root_gh = sqrt(g * h); // NB: Don't let h go negative!
        cx = abs(hu/h) + root_gh;
        cy = abs(hv/h) + root_gh;
    }
};
```

MinMod limiter

Numerical methods for solving nonlinear wave equations are complicated by the fact that even with smooth initial data, a nonlinear wave can develop discontinuities (shocks) in finite time.

This makes for interesting analysis, since a "strong" solution that satisfies the differential equation no longer makes sense at a shock – instead, we have to come up with some mathematically and physically reasonable definition of a "weak"

solution that satisfies the PDE away from the shock and satisfies some other condition (an entropy condition) at the shock.

The presence of shocks also makes for interesting numerical analysis, because we need to be careful about employing numerical differentiation formulas that sample a discontinuous function at points on different sides of a shock. Using such formulas naively usually causes the numerical method to become unstable. A better method – better even in the absence of shocks! – is to consider multiple numerical differentiation formulas and use the highest order one that "looks reasonable" in the sense that it doesn't predict wildly larger slopes than the others. Because these combined formulas limit the wild behavior of derivative estimates across a shock, we call them limiters. With an appropriate limiter, we can construct methods that have high-order accuracy away from shocks and are at least first-order accurate close to a shock. These are sometimes called high-resolution methods.

The MinMod (minimum modulus) limiter is one example of a limiter. The MinMod limiter estimates the slope through points f_- , f_0 , f_+ (with the step h scaled to 1) by

$$f' = \min ((f_+ - f_-)/2, \theta(f_+ - f_0), \theta(f_0 - f_-))$$

where the minmod function returns the argument with smallest absolute value if all arguments have the same sign, and zero otherwise. Common choices of θ are $\theta = 1.0$ and $\theta = 2.0$.

The minmod limiter *looks* like it should be expensive to computer, since superficially it seems to require a number of branches. We do something a little tricky, getting rid of the condition on the sign of the arguments using the copysign instruction. If the compiler does the "right" thing with max and min for floating point arguments (translating them to branch-free intrinsic operations), this implementation should be relatively fast.

There are many other potential choices of limiters as well. We'll stick with this one for the code, but you should feel free to experiment with others if you know what you're doing and think it will improve performance or accuracy.

Jiang-Tadmor central difference scheme

Jiang and Tadmor proposed a high-resolution finite difference scheme for solving hyperbolic PDE systems in two space dimensions. The method is particularly attractive because, unlike many other methods in this space, it does not require that we write any solvers for problems with special initial data (so-called Riemann problems), nor even that we compute Jacobians of the flux functions.

While this code is based loosely on the Fortran code at the end of Jiang and Tadmor's paper, we've written the current code to be physics-agnostic (rather than hardwiring it to the shallow water equations – or the Euler equations in the Jiang-Tadmor paper). If you're interested in the Euler equations, feel free to add your own physics class to support them!

Staggered grids

The Jiang-Tadmor scheme works by alternating between a main grid and a staggered grid offset by half a step in each direction. Understanding this is important, particularly if you want to apply a domain decomposition method and batch time steps between synchronization barriers in your parallel code!

In even-numbered steps, the entry $\mathtt{u(i,j)}$ in the array of solution values represents the average value of a cell centered at a point (x_i,y_j) . At the following odd-numbered step, the same entry represents values for a cell centered at $(x_i + \Delta x/2, y_j + \Delta y/2)$. However, whenever we run a simulation, we always take an even number of steps, so that outside the solver we can just think about values on the main grid. If **uold** and **unew** represent the information at two successive even time steps (i.e. they represent data on the same grid), then $\mathtt{unew(i,j)}$ depends indirectly on $\mathtt{u(p,q)}$ for $i-3 \le p \le i+3$ and $j-3 \le q \le j+3$.

We currently manage this implicitly: the arrays at even time steps represent cell values on the main grid, and arrays at odd steps represent cell values on the staggered grid. Our main run function always takes an even number of time steps to ensure we end up on the primary grid.

Interface

We want a clean separation between the physics, the solver, and the auxiliary limiter methods used by the solver. At the same time, we don't want to pay the overhead (mostly in terms of lost optimization opportunities) for calling across an abstraction barrier in the inner loops of our solver. We can get around this in C++ by providing the solver with *template arguments*, resolved at compile time, that describe separate classes to implement the physics and the limiter. * The Central2D solver class takes two template arguments: Physics and Limiter. For Physics, we expect the name of a class that defines:

- A type for numerical data (real)
- A type for solution and flux vectors in each cell (vec)
- A flux computation function (flux(vec& F, vec& G, const vec& U))
- A wave speed computation function (wave_speed(real& cx, real& cy, const vec& U)).

The Limiter argument is a type with a static function limdiff with the signature

```
limdiff(fm, f0, fp)
```

The semantics are that fm, f0, and fp are three successive grid points in some direction, and the function returns an approximate (scaled) derivative value from these points.

The solver keeps arrays for the solution, flux values, derivatives of the solution and the fluxes, and the solution at the next time point. We use the C++ vector class to manage storage for these arrays; but since we want to think of them as 2D arrays, we also provide convenience functions to access them with multiple indices (though we maintain C-style 0-based indexing). The internal arrays are padded with ghost cells; the ghost cell in the lower left corner of the domain has index (0,0).

```
dx(w/nx), dy(h/ny),
        cfl(cfl),
       u_ (nx_all * ny_all),
       f_ (nx_all * ny_all),
       g_ (nx_all * ny_all),
       ux_(nx_all * ny_all),
       uy_(nx_all * ny_all),
        fx_(nx_all * ny_all),
        gy_(nx_all * ny_all),
        v_ (nx_all * ny_all) {}
    // Advance from time 0 to time tfinal
    void run(real tfinal);
    // Call f(Uxy, x, y) at each cell center to set initial conditions
    template <typename F>
    void init(F f);
    // Diagnostics
    void solution_check();
    // Array size accessors
    int xsize() const { return nx; }
    int ysize() const { return ny; }
   // Read / write elements of simulation state
               operator()(int i, int j) {
    vec&
       return u_[offset(i+nghost,j+nghost)];
    }
    const vec& operator()(int i, int j) const {
       return u_[offset(i+nghost,j+nghost)];
    }
private:
    static constexpr int nghost = 3;  // Number of ghost cells
                               // Number of (non-ghost) cells in x/y
    const int nx, ny;
    const int nx_all, ny_all; // Total cells in x/y (including ghost)
    const real dx, dy;
                              // Cell size in x/y
    const real cfl;
                              // Allowed CFL number
    std::vector<vec> u ;
                                   // Solution values
                                   // Fluxes in x
    std::vector<vec> f_;
                                   // Fluxes in y
    std::vector<vec> g_;
                                   // x differences of u
    std::vector<vec> ux_;
```

```
std::vector<vec> uy_;
                                    // y differences of u
                                    // x differences of f
    std::vector<vec> fx_;
    std::vector<vec> gy_;
                                    // y differences of g
    std::vector<vec> v_;
                                    // Solution values at next step
    // Array accessor functions
    int offset(int ix, int iy) const { return iy*nx_all+ix; }
    vec& u(int ix, int iy)
                              { return u_[offset(ix,iy)]; }
    vec& v(int ix, int iy)
                              { return v_[offset(ix,iy)]; }
                              { return f_[offset(ix,iy)]; }
    vec& f(int ix, int iy)
    vec& g(int ix, int iy)
                              { return g_[offset(ix,iy)]; }
    vec& ux(int ix, int iy)
                              { return ux_[offset(ix,iy)]; }
                              { return uy [offset(ix,iy)]; }
    vec& uy(int ix, int iy)
    vec& fx(int ix, int iy)
                              { return fx_[offset(ix,iy)]; }
    vec& gy(int ix, int iy)
                              { return gy_[offset(ix,iy)]; }
    // Wrapped accessor (periodic BC)
    int ioffset(int ix, int iy) {
        return offset( (ix+nx-nghost) % nx + nghost,
                       (iy+ny-nghost) % ny + nghost );
    }
    vec& uwrap(int ix, int iy) { return u_[ioffset(ix,iy)]; }
    // Apply limiter to all components in a vector
    static void limdiff(vec& du, const vec& um, const vec& u0, const vec& up) {
        for (int m = 0; m < du.size(); ++m)</pre>
            du[m] = Limiter::limdiff(um[m], u0[m], up[m]);
    }
    // Stages of the main algorithm
    void apply_periodic();
    void compute_fg_speeds(real& cx, real& cy);
    void limited_derivs();
    void compute_step(int io, real dt);
};
```

Initialization

Before starting the simulation, we need to be able to set the initial conditions. The init function does exactly this by running a callback function at the center of each cell in order to initialize the cell U value. For the purposes of this function, cell (i, j) is the subdomain $[i\Delta x, (i+1)\Delta x] \times [j\Delta y, (j+1)\Delta y]$.

```
template <class Physics, class Limiter>
template <typename F>
void Central2D<Physics, Limiter>::init(F f)
{
    for (int iy = 0; iy < ny; ++iy)
        for (int ix = 0; ix < nx; ++ix)
            f(u(nghost+ix,nghost+iy), (ix+0.5)*dx, (iy+0.5)*dy);
}</pre>
```

Time stepper implementation

Boundary conditions

In finite volume methods, boundary conditions are typically applied by setting appropriate values in ghost cells. For our framework, we will apply periodic boundary conditions; that is, waves that exit one side of the domain will enter from the other side.

We apply the conditions by assuming that the cells with coordinates nghost <= ix <= nx+nghost and nghost <= iy <= ny+nghost are "canonical", and setting the values for all other cells (ix,iy) to the corresponding canonical values (ix+p*nx,iy+q*ny) for some integers p and q.

```
template <class Physics, class Limiter>
void Central2D<Physics, Limiter>::apply_periodic()
    // Copy data between right and left boundaries
    for (int iy = 0; iy < ny_all; ++iy)</pre>
        for (int ix = 0; ix < nghost; ++ix) {</pre>
                            iy) = uwrap(ix,
            u(nx+nghost+ix,iy) = uwrap(nx+nghost+ix,iy);
        }
    // Copy data between top and bottom boundaries
    for (int ix = 0; ix < nx_all; ++ix)
        for (int iy = 0; iy < nghost; ++iy) {</pre>
            u(ix,
                            iy) = uwrap(ix,
            u(ix,ny+nghost+iy) = uwrap(ix,ny+nghost+iy);
        }
}
```

Initial flux and speed computations

At the start of each time step, we need the flux values at cell centers (to advance the numerical method) and a bound on the wave speeds in the x and y directions (so that we can choose a time step that respects the specified upper bound on the CFL number).

```
template <class Physics, class Limiter>
void Central2D<Physics, Limiter>::compute_fg_speeds(real& cx_, real& cy_)
{
    using namespace std;
    real cx = 1.0e-15;
    real cy = 1.0e-15;
    for (int iy = 0; iy < ny_all; ++iy)</pre>
        for (int ix = 0; ix < nx_all; ++ix) {</pre>
            real cell_cx, cell_cy;
            Physics::flux(f(ix,iy), g(ix,iy), u(ix,iy));
            Physics::wave_speed(cell_cx, cell_cy, u(ix,iy));
            cx = max(cx, cell_cx);
            cy = max(cy, cell_cy);
    cx_ = cx;
    cy_ = cy;
}
```

Derivatives with limiters

In order to advance the time step, we also need to estimate derivatives of the fluxes and the solution values at each cell. In order to maintain stability, we apply a limiter here.

```
template <class Physics, class Limiter>
void Central2D<Physics, Limiter>::limited_derivs()
{
   for (int iy = 1; iy < ny_all-1; ++iy)
      for (int ix = 1; ix < nx_all-1; ++ix) {
            // x derivs
            limdiff( ux(ix,iy), u(ix-1,iy), u(ix,iy), u(ix+1,iy) );
            limdiff( fx(ix,iy), f(ix-1,iy), f(ix,iy), f(ix+1,iy) );
            // y derivs
            limdiff( uy(ix,iy), u(ix,iy-1), u(ix,iy), u(ix,iy+1) );
            limdiff( gy(ix,iy), g(ix,iy-1), g(ix,iy), g(ix,iy+1) );
        }
}</pre>
```

}

Advancing a time step

Take one step of the numerical scheme. This consists of two pieces: a first-order corrector computed at a half time step, which is used to obtain new F and G values; and a corrector step that computes the solution at the full step. For full details, we refer to the Jiang and Tadmor paper.

The compute_step function takes two arguments: the io flag which is the time step modulo 2 (0 if even, 1 if odd); and the dt flag, which actually determines the time step length. We need to know the even-vs-odd distinction because the Jiang-Tadmor scheme alternates between a primary grid (on even steps) and a staggered grid (on odd steps). This means that the data at (i,j) in an even step and the data at (i,j) in an odd step represent values at different locations in space, offset by half a space step in each direction. Every other step, we shift things back by one mesh cell in each direction, essentially resetting to the primary indexing scheme.

```
template <class Physics, class Limiter>
void Central2D<Physics, Limiter>::compute step(int io, real dt)
{
    real dtcdx2 = 0.5 * dt / dx;
    real dtcdy2 = 0.5 * dt / dy;
    // Predictor (flux values of f and g at half step)
    for (int iy = 1; iy < ny_all-1; ++iy)</pre>
        for (int ix = 1; ix < nx_all-1; ++ix) {
            vec uh = u(ix,iy);
            for (int m = 0; m < uh.size(); ++m) {</pre>
                uh[m] = dtcdx2 * fx(ix,iy)[m];
                uh[m] = dtcdy2 * gy(ix,iy)[m];
            Physics::flux(f(ix,iy), g(ix,iy), uh);
        }
    // Corrector (finish the step)
    for (int iy = nghost-io; iy < ny+nghost-io; ++iy)</pre>
        for (int ix = nghost-io; ix < nx+nghost-io; ++ix) {</pre>
            for (int m = 0; m < v(ix,iy).size(); ++m) {
                v(ix,iy)[m] =
                     0.2500 * (u(ix, iy)[m] + u(ix+1,iy)[m] +
                                u(ix,iy+1)[m] + u(ix+1,iy+1)[m] -
                     0.0625 * (ux(ix+1,iy)[m] - ux(ix,iy)[m] +
                                ux(ix+1,iy+1)[m] - ux(ix,iy+1)[m] +
```

Advance time

The run method advances from time 0 (initial conditions) to time tfinal. Note that run can be called repeatedly; for example, we might want to advance for a period of time, write out a picture, advance more, and write another picture. In this sense, tfinal should be interpreted as an offset from the time represented by the simulator at the start of the call, rather than as an absolute time.

We always take an even number of steps so that the solution at the end lives on the main grid instead of the staggered grid.

```
template <class Physics, class Limiter>
void Central2D<Physics, Limiter>::run(real tfinal)
    bool done = false;
    real t = 0;
    while (!done) {
        real dt;
        for (int io = 0; io < 2; ++io) {
            real cx, cy;
            apply_periodic();
            compute_fg_speeds(cx, cy);
            limited derivs();
            if (io == 0) {
                dt = cfl / std::max(cx/dx, cy/dy);
                if (t + 2*dt >= tfinal) {
                    dt = (tfinal - t)/2;
                    done = true;
```

```
}
compute_step(io, dt);
t += dt;
}
}
```

Diagnostics

The numerical method is supposed to preserve (up to rounding errors) the total volume of water in the domain and the total momentum. Ideally, we should also not see negative water heights, since that will cause the system of equations to blow up. For debugging convenience, we'll plan to periodically print diagnostic information about these conserved quantities (and about the range of water heights).

```
template <class Physics, class Limiter>
void Central2D<Physics, Limiter>::solution check()
    using namespace std;
    real h_sum = 0, hu_sum = 0, hv_sum = 0;
    real hmin = u(nghost,nghost)[0];
    real hmax = hmin;
    for (int j = nghost; j < ny+nghost; ++j)</pre>
        for (int i = nghost; i < nx+nghost; ++i) {</pre>
             vec\& uij = u(i,j);
             real h = uij[0];
            h_sum += h;
            hu_sum += uij[1];
            hv_sum += uij[2];
            hmax = max(h, hmax);
            hmin = min(h, hmin);
             assert(h > 0);
        }
    real cell_area = dx*dy;
    h_sum *= cell_area;
    hu_sum *= cell_area;
    hv_sum *= cell_area;
    \label{lem:continuity} printf("-\n Volume: \g\n Momentum: (\g, \g)\n Range: [\g, \g]\n",
           h_sum, hu_sum, hv_sum, hmin, hmax);
}
```

I/O

After finishing a run (or every several steps), we might want to write out a data file for post processing. One simple approach is to draw a gray scale or color picture showing some scalar quantity at each point. The Portable Gray Map (PGM) format is one of the few graphics formats that can be dumped out in a handful of lines of code without any library calls. The files can be converted to something more modern and snazzy (like a PNG or GIF) later on. Note that we don't actually dump out the state vector for each cell – we need to produce something that is an integer in the range [0,255]. That's what the function **f** is for!

An alternative to writing an image file is to write a data file for further processing by some other program – in this case, a Python visualizer. The visualizer takes the number of pixels in x and y in the first two entries, then raw single-precision raster pictures.

```
template <class Sim>
class SimViz {
  public:

    SimViz(const char* fname, const Sim& sim) : sim(sim) {
        fp = fopen(fname, "w");
        if (fp) {
            float xy[2];
            xy[0] = sim.xsize();
            xy[1] = sim.ysize();
            fwrite(xy, sizeof(float), 2, fp);
        }
    }
    void write_frame() {
```

Driver routines

We use a fairly simple command-line driver to launch this simulation. A better way to do this is to use a scripting language to set up the simulation; Python is a popular choice, though I prefer Lua for many things (not least because it is an easy build). I may add that capability later; for the moment, it's useful to have a simple command-line interface that ought to run most anywhere.

For the driver, we need to put everything together: we're running a Central2D solver for the Shallow2D physics with a MinMod limiter:

```
typedef Central2D< Shallow2D, MinMod<Shallow2D::real> > Sim;
```

Initial states and graphics

• Our default problem is a circular dam break problem; the other interesting problem is the wave problem (a wave on a constant flow, starting off smooth and developing a shock in finite time). The pond and river examples should do nothing interesting at all if the numerical method is coded right.

```
// Circular dam break problem void dam_break(Sim::vec& u, double x, double y) { x -= 1; y -= 1; u[0] = 1.0 + 0.5(xx + y*y < 0.25+1e-5); u[1] = 0; u[2] = 0; } // Still pond (ideally, nothing should move here!) void pond(Sim::vec& u, double x, double y) { u[0] = 1.0; u[1] = 0; u[2] = 0; }
```

```
// River (ideally, the solver shouldn't do much with this, either) void river
(Sim::vec& u, double x, double y) { u[0] = 1.0; u[1] = 1.0; u[2] = 0; } 
// Wave on a river – develops a shock in finite time! void wave
(Sim::vec& u, double x, double y) { using namespace std; u[0] = 1.0 + 0.2 * \sin(M_PI^*x);
u[1] = 1.0; u[2] = 0; }
```

Main driver

Our main driver uses the **getopt** library to parse options, then runs a simulation, writing results to an output file for postprocessing.

```
int main(int argc, char** argv)
{
    const char* fname = "waves.out";
    const char* ic = "dam_break";
           nx = 200;
    double width = 2.0;
    double ftime = 0.01;
    int
           frames = 50;
    int c;
    extern char* optarg;
    while ((c = getopt(argc, argv, "hi:o:n:w:F:f:")) != -1) {
        switch (c) {
        case 'h':
            fprintf(stderr,
                    "%s\n"
                    "\t-h: print this message\n"
                    "\t-i: initial conditions (%s)\n"
                    "\t-o: output file name (%s)\n"
                    "\t-n: number of cells per side (%d)\n"
                    "\t-w: domain width in cells (%g)\n"
                    "\t-f: time between frames (%g)\n"
                    "\t-F: number of frames (%d)\n",
                    argv[0], ic, fname, nx, width, ftime, frames);
            return -1:
        case 'i': ic
                          = strdup(optarg); break;
        case 'o': fname = strdup(optarg); break;
        case 'n': nx
                          = atoi(optarg);
                                              break;
        case 'w': width = atof(optarg);
                                             break;
        case 'f':
                  ftime = atof(optarg);
                                              break;
        case 'F': frames = atoi(optarg);
                                              break;
        default:
            fprintf(stderr, "Unknown option (-%c)\n", c);
```

```
return -1;
        }
    }
    void (*icfun)(Sim::vec& u, double x, double y);
    if (strcmp(ic, "dam_break") == 0) {
        icfun = dam_break;
    } else if (strcmp(ic, "pond") == 0) {
        icfun = pond;
    } else if (strcmp(ic, "river") == 0) {
        icfun = river;
    } else if (strcmp(ic, "wave") == 0) {
        icfun = wave;
    } else {
        fprintf(stderr, "Unknown initial conditions\n");
    }
    Sim sim(width, width, nx,nx);
    SimViz<Sim> viz(fname, sim);
    sim.init(icfun);
    sim.solution_check();
    viz.write_frame();
    for (int i = 0; i < frames; ++i) {</pre>
        sim.run(ftime);
        sim.solution_check();
        viz.write_frame();
    }
}
```