# BIG DATA ANALYTICS Advertising on the Web



## Outline

Web Advertising

The Adwords Problem

# On-line advertising

- Web applications support themselves through advertising
- The most lucrative venue for on-line advertising: search
- The "adwords" model of matching search queries to advertisements
- The algorithms: greedy and "on-line"

# Online Advertising

- Banner ads: Initial form of web advertising
- On-line stores: to maximize the probability that the customer will be interested in the product
- Search ads are placed among the results of a search query:
  - Advertisers bid for the right to have their ad shown in response to certain queries
  - They pay only if the ad is clicked on

# Display Ads

- ullet  $\sim$  advertising in traditional media
- The fee is typically a fraction of a cent per impression



# Specialized Display Ads

- Traditional media: newspapers or magazines for special interests
- many specialized, low-circulation magazines
- An ad for golf clubs on sports.yahoo.com/golf has much more value per impression

### Content Personalization

- Use information about the user
- E.g. Sally likes golf  $\implies$  show her an ad for golf clubs
  - She may belong to a golf-related group on Facebook
  - She may mention "golf" frequently in emails posted on her gmail account
  - She may spend a lot of time on the Yahoo! golf page
  - She may issue search queries with golf-related terms frequently
  - She may bookmark the Web sites of one or more golf courses.

# Privacy issues

- People like the free services that are usually advertisingsupported
- These services depend on advertising being much more effective than conventional ads
- Better to see things you might actually use
- Potential for misuse if the information.

# Search Advertising

- Introduced by Overture around 2000
  - Advertisers bid on keywords
  - When someone searched fors that keyword, the highest bidders' ads are shown
  - Advertiser is charged only if the ad is clicked on
- Similar system adopted by Google around 2002: Adwords

# Challenges for the Search Advertising (1)

- Ads are displayed in response to query terms:
  - inverted index of words
  - the advertiser specifies parameters of the ad
- How to rank ads?
- "Most-recent first":
  - advertisers post small variations of their ads at frequent intervals
  - ⇒ discover ads that are too similar

# Challenges for the Search Advertising (2)

- Measure the attractiveness of an ad:
  - Attractive ads will be clicked on more frequently
  - The position of the ad has great influence is clicked
  - Attractiveness may depends on the query terms
  - All ads deserve the opportunity to be shown until their click probability can be approximated closely

## Web 2.0

- Performance-based advertising works!
  - Multi-billion-dollar industry
- Interesting problem: what ads to show for a given query?
  - Today's lecture
- If I am an advertiser, which search terms should I bid on and how much should I bid?

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# The Adwords system

- Only a limited number of ads with each query
- Users: a budget for all clicks on their ads in a month
- Ordering ads: by the amount they expected to receive for display of each ad
  - The click-through rate based on the history of displays
  - The value of an  $ad = the bid \times the click-through rate.$

## Adwords Problem

#### Given:

- 1. A set of bids by advertisers for search queries.
- 2. A click-through rate for each advertiser-query pair.
- 3. A budget for each advertiser.
- 4. A limit on the number of ads to be displayed with each search query.
- Respond to each search query with a set of advertisers such that:
  - 1. The size of the set is no larger than the limit on the number of ads per query.
  - 2. Each advertiser has bid on the search guery.
  - 3. Each advertiser has enough budget left to pay for the ad if it is clicked upon.

## **Adwords Problem**

- A stream of queries arrives at the search engine:  $q_1, q_2, \dots$
- Several advertisers bid on each query
- When query  $q_i$  arrives, search engine must pick a subset of advertisers whose ads are shown
- Goal: Maximize search engine's revenues
- Simple solution: Instead of raw bids, use the "expected revenue per click" (i.e., Bid×CTR)
- We need an online algorithm!

# Online algorithms

#### Classic model of algorithms:

- You get to see the entire input, then compute some function of it
- In this context, "offline algorithm"

#### • Online Algorithms:

- You get to see the input one piece at a time, and need to make irrevocable decisions along the way
- Optimizing the output

## The Adwords Innovation

Advertiser	Bid	CTR	$Bid{ imes}CTR$
А	\$1	1%	1 cent
В	\$0.75	2%	1.5 cent
С	\$0.5	2.5%	1.125 cent

## Complications: Budget

- Two complications:
  - Budget
  - CTR of an ad is unknown
- Each advertiser has a limited budget:
  - Search engine guarantees that the advertiser will not be charged more than their daily budget

# Complications: CTR

- CTR: Each ad has a different likelihood of being clicked
  - Advertiser 1 bids \$2, click probability = 0.1
  - Advertiser 2 bids \$1, click probability = 0.5
- Clickthrough rate (CTR) is measured historically
- Very hard problem: Exploration vs. exploitation
- Exploit: Should we keep showing an ad for which we have good estimates of click-through rate
- OR Explore: Shall we show a brand new ad to get a better sense of its click-through rate

# Greedy Algorithm

- Our setting: Simplified environment:
  - There is 1 ad shown for each query
  - All advertisers have the same budget B
  - All ads are equally likely to be clicked
  - Value of each ad is the same (=1)
- Simplest algorithm is greedy:
  - For a query pick any advertiser who has bid 1 for that query

# Bad scenario for Greedy

- Two advertisers A and B:
  - ullet A bids on query x, B bids on x and y
  - Both have budgets of \$4
- Query stream: xxxxyyyy
  - Worst case greedy choice: BBBB\_\_\_\_\_
  - Optimal: AAAABBBB
  - Competitive ratio = 1/2
- Note: Greedy algorithm is deterministic it always resolves draws in the same way

# BALANCE algorithm

- BALANCE Algorithm by Mehta, Saberi, Vazirani, and Vazirani
  - For each query, pick the advertiser with the largest unspent budget
  - Break ties arbitrarily (but in a deterministic way)

# Example: BALANCE

- Two advertisers A and B:
  - ullet A bids on query x, B bids on x and y
  - Both have budgets of \$4
- Query stream: xxxxyyyy
- BALANCE choice: ABABBB\_\_\_
  - Optimal: A A A A B B B B
  - Greedy:  $BBBB_{---}$
- Competitive ratio = 3/4

## General Version of the Problem

- Arbitrary bids and arbitrary budgets!
- ullet Consider we have 1 query q, advertiser i
  - Bid =  $x_i$
  - Budget =  $b_i$
- In a general setting BALANCE can be terrible
  - Consider two advertisers  $A_1$  and  $A_2$
  - $A_1: x_1 = 1, b_1 = 110$
  - $A_2: x_2 = 10, b_2 = 100$
  - Consider we see 10 instances of q
  - BALANCE always selects  $A_1$  and earns 10
  - Optimal earns 100

## Generalized BALANCED

- ullet Arbitrary bids: consider query q, bidder i
  - Bid =  $x_i$
  - Budget=  $b_i$
  - Amount spent so far  $= m_i$
  - Fraction of budget left over  $f_i = 1 m_i/b_i$
  - Define  $\psi_i(q) = x_i(1 e^{-f_i})$
- Allocate query q to bidder i with largest value of  $\psi_i(q)$
- Competitive ratio (1-1/e)

## Generalized BALANCED

- The click-through rate differs for different ads
- ullet multiply the bid by the click-through rate when computing the  $\psi_i(q)$ 's
- maximize the expected revenue

# Matching Bids and Search Queries

- Simplified model: advertisers bid on sets of words
- "Broad matching":
  - ad is eligible also for search queries that are inexact matches of the bid keywords
  - E.g., subset of keywords/ queries with very similar meanings
- Need to take into account how closely related the search query is to the advertiser's bid

# Charging Advertisers for Clicks

- Simplified model:
  - A first-price auction
- A second-price auction:
  - advertiser pays approximately the bid of the advertiser placed immediately behind them in the auction
  - less susceptible to being gamed by advertisers than first-price auctions
  - higher revenues for the search engine

## References

 J. Leskovec, A. Rajaraman and J. D. Ullman Mining of Massive Datasets (2014), Chapter 8