

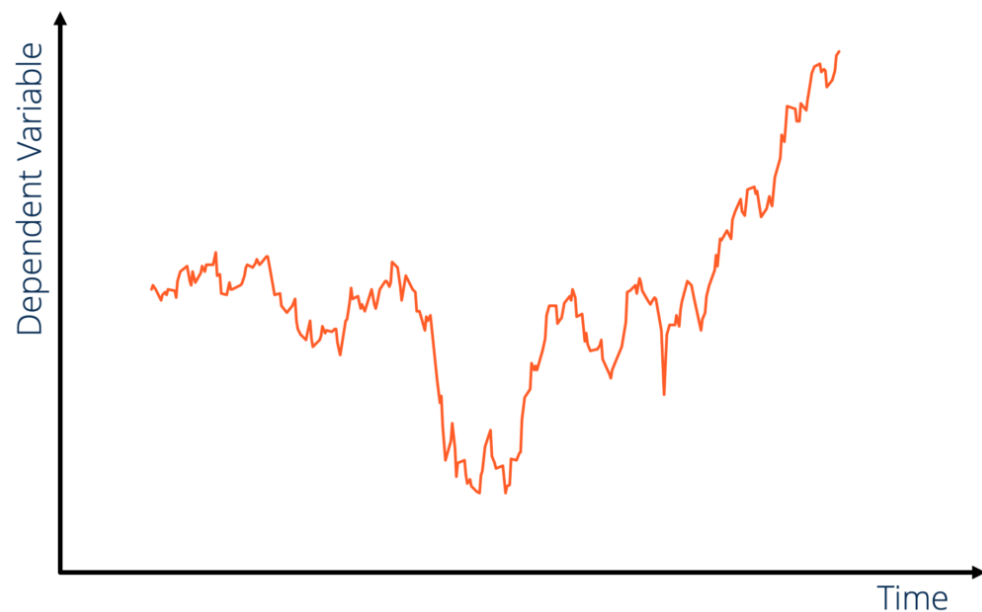
NEURAL NETWORKS AND DEEP LEARNING

神经网络与深度学习

Recurrent Neural Networks
循环神经网络

<https://stanford.edu/~shervine/teaching/cs-230/cheatsheet-recurrent-neural-networks>

Time-Series Analysis



	A	B	C	D	E	F
1	Date	Volume	Open	High	Low	Close
2	1-Apr	423454	12.12	12.89	12	12.18
3	2-Apr	534535	13.12	13.55	12.98	13.2
4	3-Apr	464255	11.16	12.04	11.11	11.3
5	4-Apr	462163	17.12	17.12	17.06	17.1
6	5-Apr	724552	16.24	16.25	15.95	16.24
7	6-Apr	452426	20.28	20.28	19.35	20.28
8	7-Apr	623562	14.12	14.53	13.75	14.2
9	8-Apr	245621	10.89	12.36	10.85	11.3
10	9-Apr	631531	20.1	20.1	18.69	20.04
11	10-Apr	222455	12.11	13.65	11.94	12.3

Lookback
5 days information

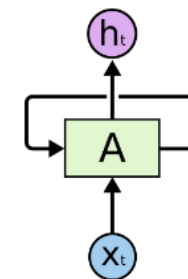
Next day,
Up? Down?

- 传统DNN只能利用当前时刻的信息（i.e., 5-Apr）
- RNN能够回溯更多时间步的信息去改善预测结果

Humans **don't start their thinking from scratch** every second. As you read this essay, you understand each word **based on your understanding of previous words**. You don't throw everything away and start thinking from scratch again.

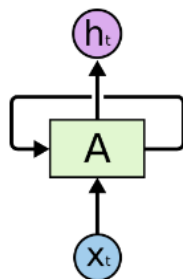
Traditional neural networks can't do this, and it seems like a major shortcoming.

Recurrent neural networks address this issue. They are networks with loops in them, allowing information to persist.



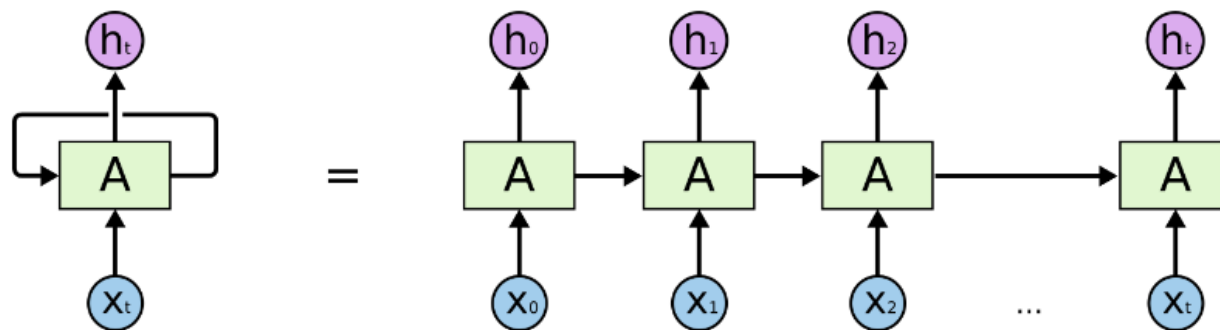
Recurrent Neural Networks have loops.

- h_t, x_t , 具有时间下标, 沿着时间维度信息流动
- A不变 (网络参数), 说明在不同的时间步下是共享参数的, 回顾卷积核



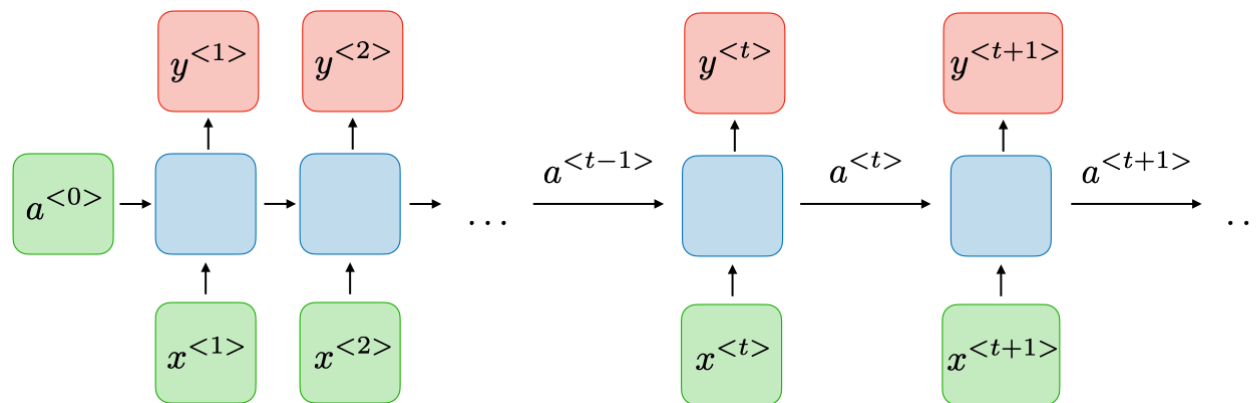
Recurrent Neural Networks have loops.

沿着时间维度（时间步）将RNN展开



An unrolled recurrent neural network.

RNNs, are a class of neural networks that allow previous outputs to be used as inputs while having hidden states.

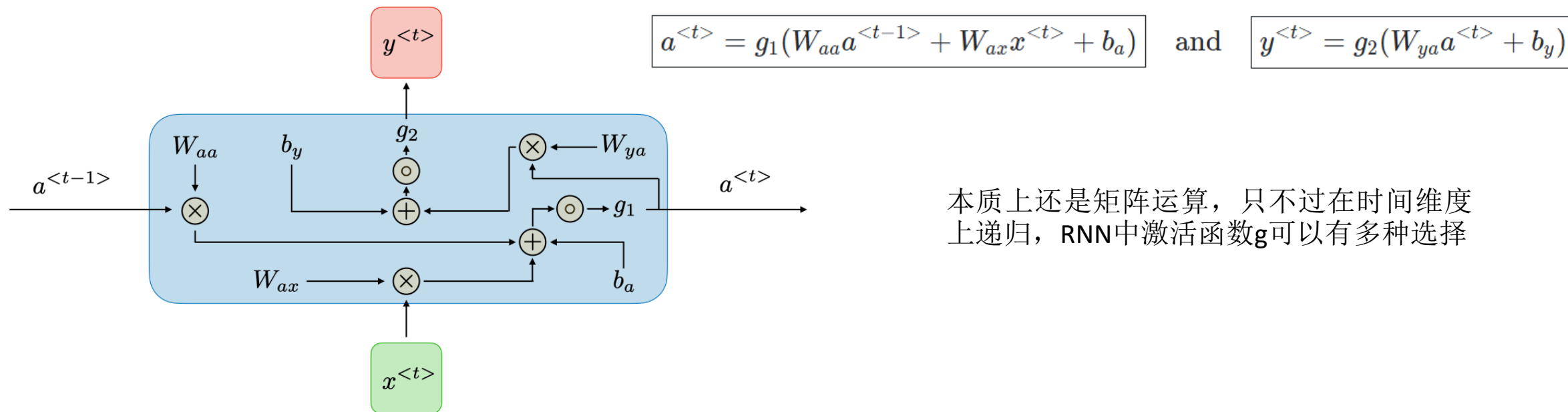


For each timestep t , the activation $a^{<t>}$ and the output $y^{<t>}$ are expressed as follows:

本质上还是矩阵运算，只不过在时间维度上递归

$$a^{<t>} = g_1(W_{aa}a^{<t-1>} + W_{ax}x^{<t>} + b_a) \quad \text{and} \quad y^{<t>} = g_2(W_{ya}a^{<t>} + b_y)$$

where $W_{ax}, W_{aa}, W_{ya}, b_a, b_y$ are coefficients that are shared temporally and g_1, g_2 activation functions.

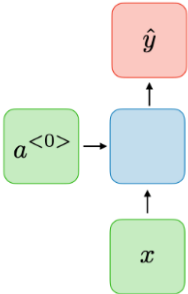
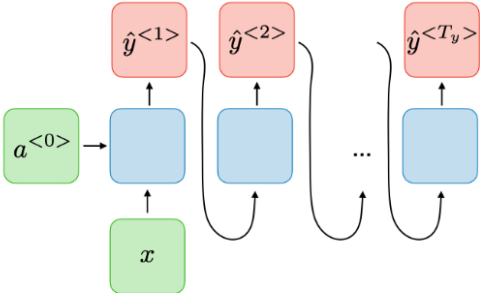
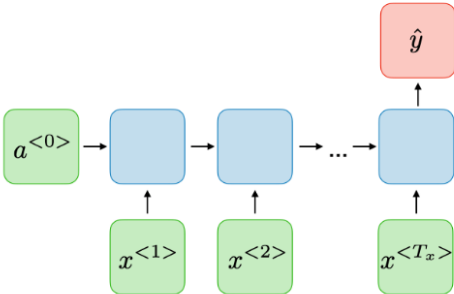


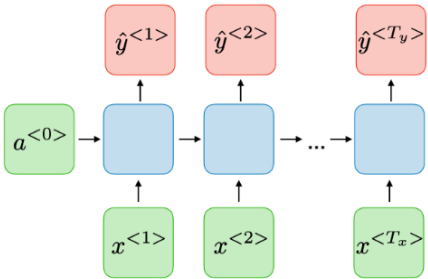
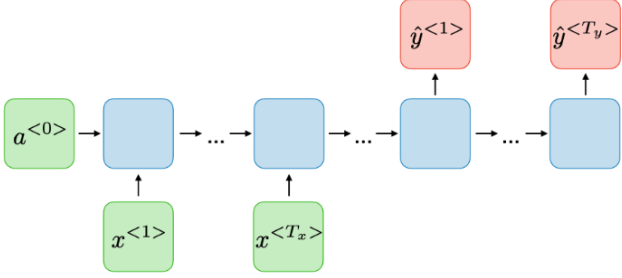
本质上还是矩阵运算，只不过在时间维度上递归，RNN中激活函数 g 可以有多种选择

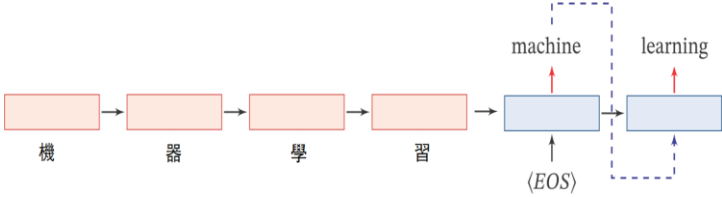
□ **Commonly used activation functions** — The most common activation functions used in RNN modules are described below:

Sigmoid	Tanh	RELU
$g(z) = \frac{1}{1 + e^{-z}}$	$g(z) = \frac{e^z - e^{-z}}{e^z + e^{-z}}$	$g(z) = \max(0, z)$

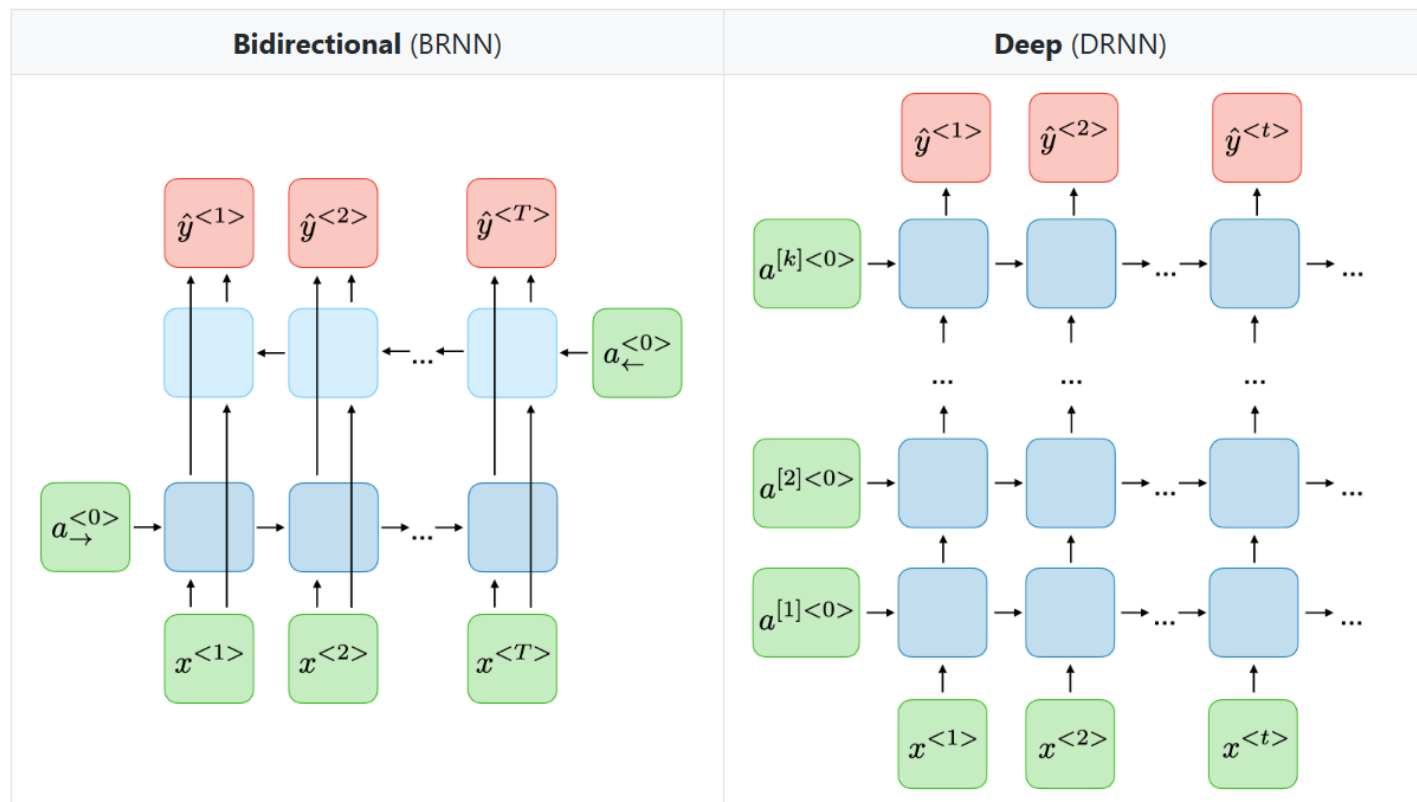
RNN Variants

Type of RNN	Illustration	Example
One-to-one $T_x = T_y = 1$		Traditional neural network
One-to-many $T_x = 1, T_y > 1$		Music generation
Many-to-one $T_x > 1, T_y = 1$		Sentiment classification

Many-to-many $T_x = T_y$		Name entity recognition
Many-to-many $T_x \neq T_y$		Machine translation



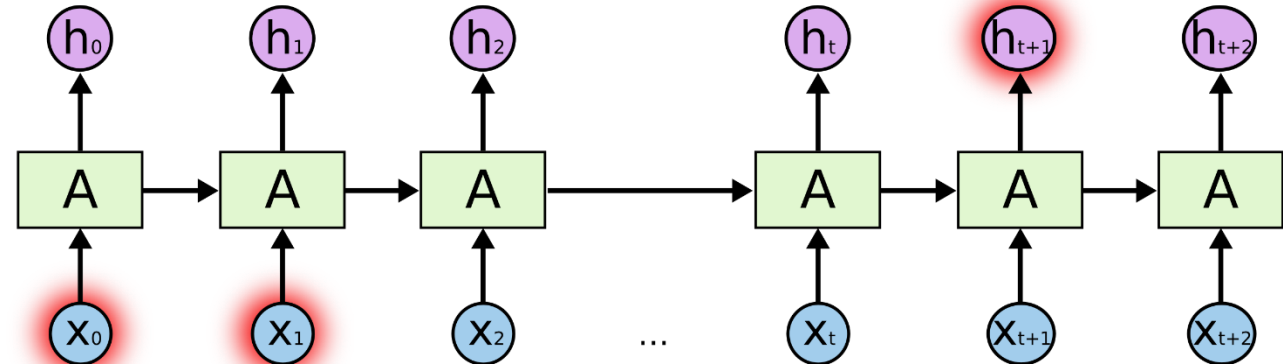
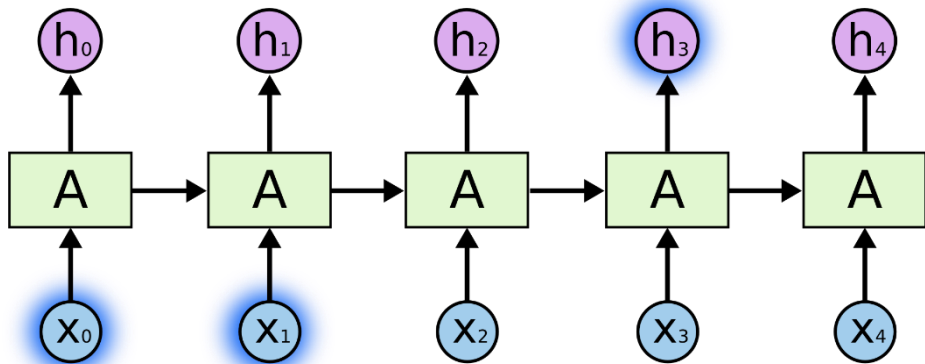
RNN Variants



沿着时间维度正向、反向分别递归更新hidden state

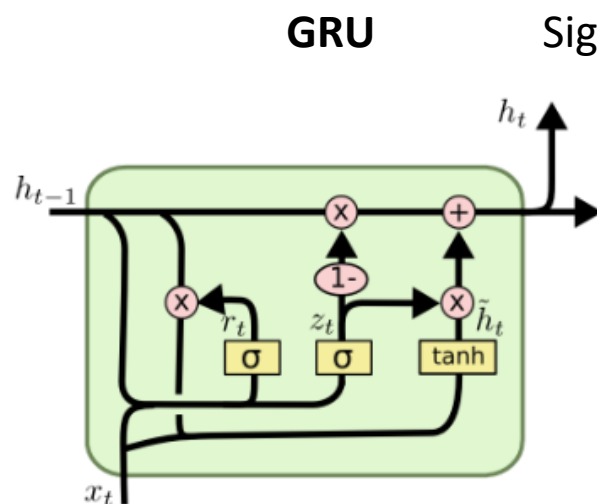
某层（隐藏层）中是沿着时间维度递归更新，可以stack多层RNN

Advantages	Drawbacks
<ul style="list-style-type: none">• Possibility of processing input of any length• Model size not increasing with size of input• Computation takes into account historical information• Weights are shared across time	<ul style="list-style-type: none">• Computation being slow• Difficulty of accessing information from a long time ago• Cannot consider any future input for the current state



RNN Variants

- GRU
- [LSTM](#)
- RNN w/ attention (todo)



$$z_t = \sigma(W_z \cdot [h_{t-1}, x_t])$$

$$r_t = \sigma(W_r \cdot [h_{t-1}, x_t])$$

$$\tilde{h}_t = \tanh(W \cdot [r_t * h_{t-1}, x_t])$$

$$h_t = (1 - z_t) * h_{t-1} + z_t * \tilde{h}_t$$

r_t 控制 h_t 的计算是否/多大程度依赖上一时刻的状态 h_{t-1} 。这允许我们转换当前信息的时候一定程度上遗忘历史信息

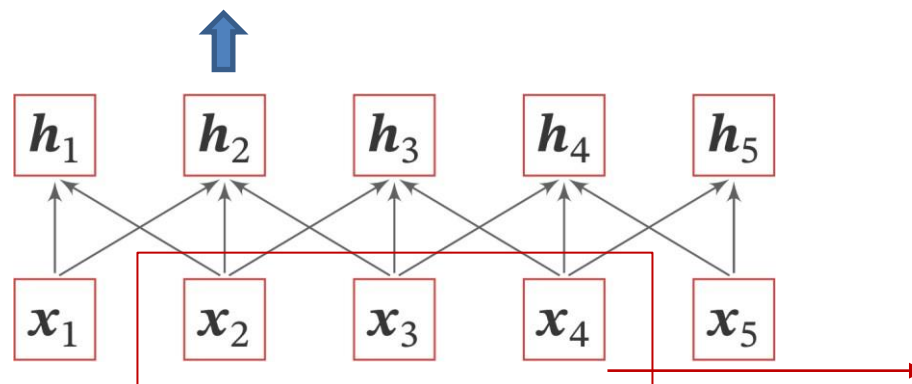
z_t 控制 h_t 的计算是如何融合当前信息与过去信息的。这允许我们在输出信息的时候一定程度上遗忘当前

GRU相比于LSTM去除了output gate, 参数量更少, 运算效率更高

CNN vs RNN

第二个时刻的hidden state不仅和 x_1, x_2 相关，还和 x_3 相关（未来的时间步信息）

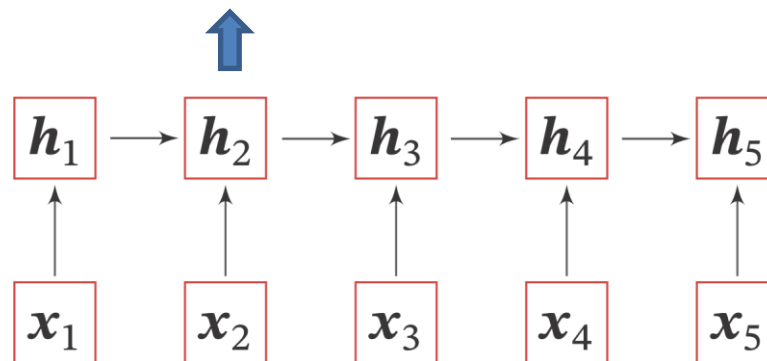
CNN



但是CNN能否对时间序列数据建模？🤔

第二个时刻的hidden state仅和当前及过去时间步的信息相关

RNN



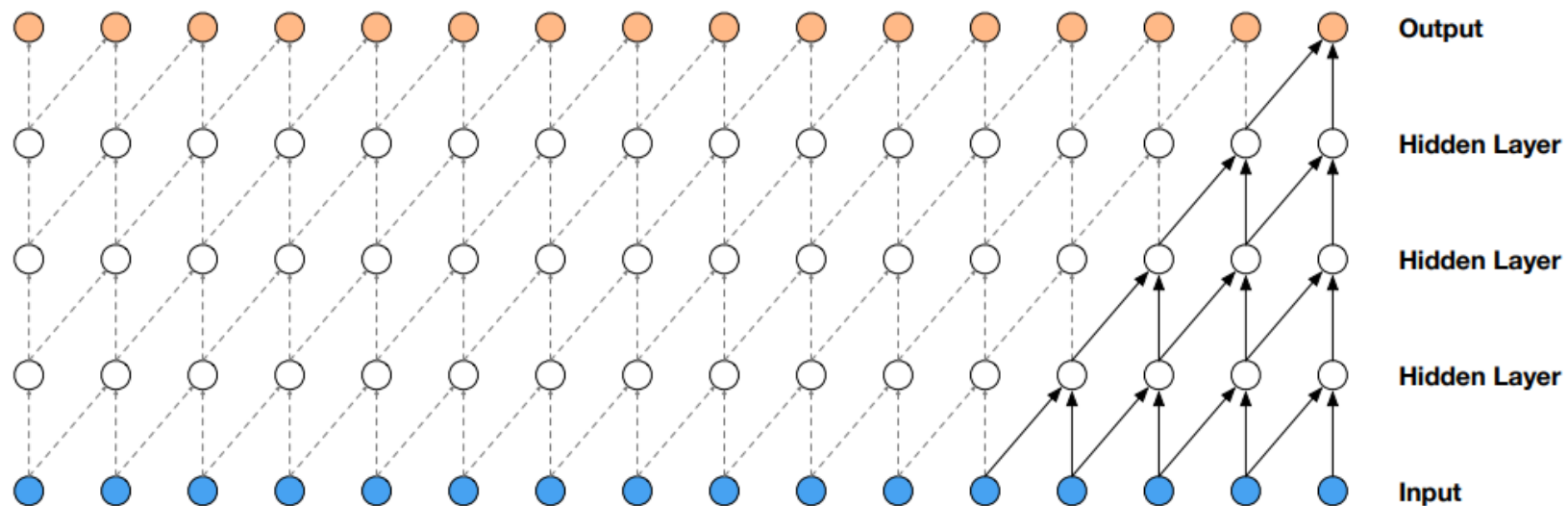
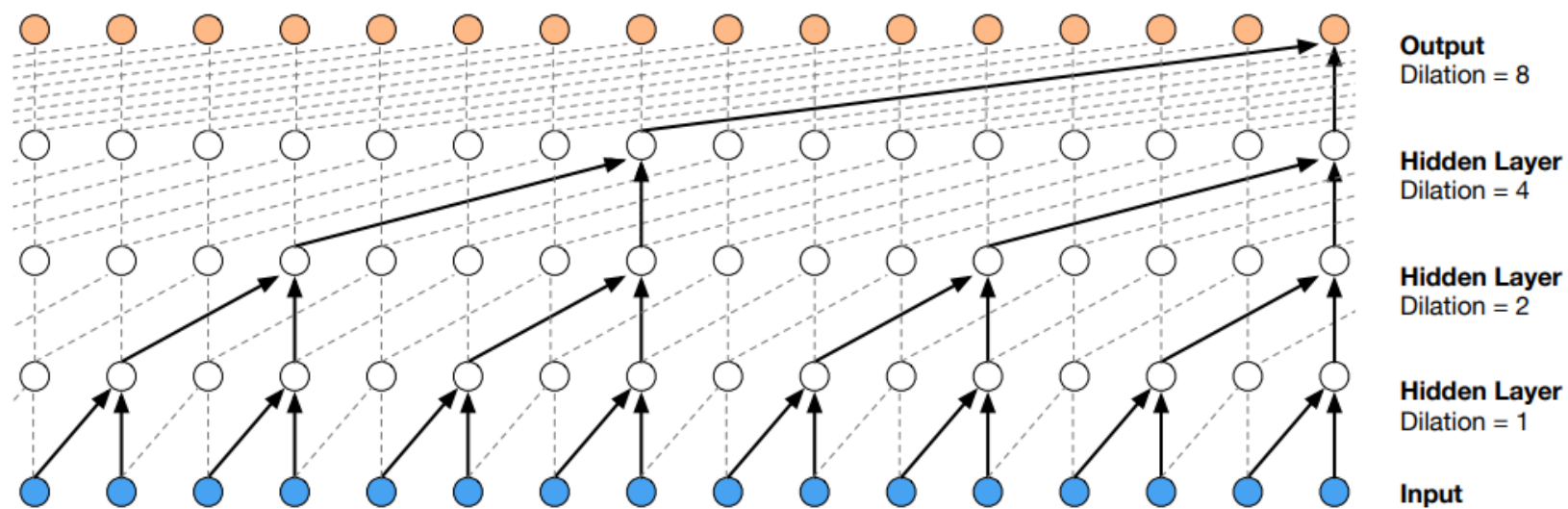


Figure 2: Visualization of a stack of causal convolutional layers.

[WAVENET: A GENERATIVE MODEL FOR RAW AUDIO](#)



Dilated convolution animations

N.B.: Blue maps are inputs, and cyan maps are outputs.

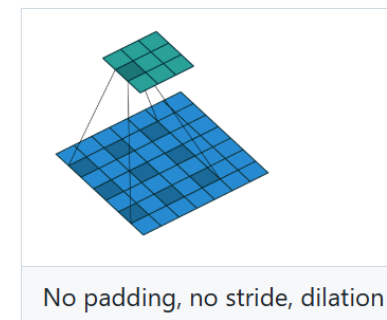


Figure 3: Visualization of a stack of *dilated* causal convolutional layers.

可以在causal convolutional layers里面用空洞卷积（dilated convolution），在不显著增加计算成本的情况下增加网络的感受野范围。以这个layer构建的CNN model for time-series analysis称为Temporal Convolutional Networks (TCN)