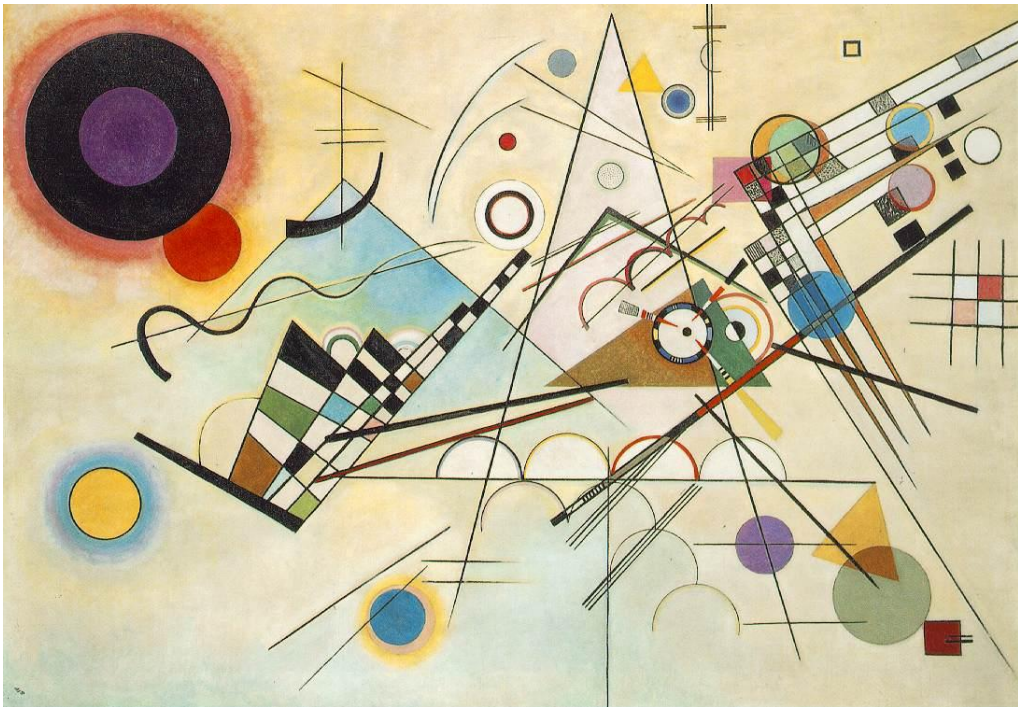


INTENSIONAL SEMANTICS



KAI VON FINTEL IRENE HEIM

1997 – ∞

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About these lecture notes

These lecture notes have been evolving for years now, starting with some old notes from the early 1990s by Angelika Kratzer, Irene Heim, and Kai von Fintel, which have since been modified and expanded many times by Irene and/or Kai.

We encourage the use of these notes in courses at other institutions. Of course, you need to give full credit to the authors and you may not use the notes for any commercial purposes. If you use the notes, we would like to be notified and we would very much appreciate any comments, criticism, and advice on these materials.

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Link to the latest full version (not necessarily up-to-date):

<http://kvf.me/intensional>

GitHub repository with the current & up-to-date development version:

<https://github.com/fintelkai/fintel-heim-intensional-notes>

Most recent homepage of the class these notes are designed for:

<http://kvf.me/advsem>

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Some advice

1. These notes presuppose familiarity with the material, concepts, and notation of the Heim & Kratzer textbook.
2. There are numerous exercises throughout the notes. It is highly recommended to do all of them and it is certainly necessary to do so if you at all anticipate doing semantics-related work in the future.
3. The notes are designed to go along with explanatory lectures. You should ask questions and make comments as you work through the notes.
4. Students with semantic ambitions should also at an early point start reading supplementary material (as for example listed at the end of each chapter of these notes).
5. Prospective semanticists may start thinking about how *they* would teach this material.
6. For more advice along these lines, see <http://kaivonfintel.org/prerequisites/>.

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PART I

INTENSIONALITY: CONDITIONALS, ATTITUDES, MODALS

CHAPTER ONE

BEGINNINGS

Language is the main
instrument of man's refusal
to accept the world as it is.

George Steiner, *After Babel*,
p. 228

We introduce the idea of extension vs. intension and its main use: taking us from the actual here and now to past, future, possible, counterfactual situations. We develop a compositional framework for intensional semantics.

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I.1 Displacement

Hockett (1960) in a famous article (and a follow-up, Hockett & Altmann (1968)) presented a list of DESIGN FEATURES OF HUMAN LANGUAGE. This list continues to

Charles F. Hockett. 1960.
The origin of speech. *Scientific American* 203. 89–96

play a role in current discussions of animal communication. One of the design features is **DISPLACEMENT**. Human language is not restricted to discourse about the *actual here and now*.¹

How does natural language untie us from the actual here and now? One degree of freedom is given by the ability to name entities and refer to them even if they are not where we are when we speak:

- (1) Thomas is in Hamburg.

This kind of displacement is not something we will explore here. We'll take it for granted.

Consider a sentence with no names of absent entities in it:

- (2) It is snowing (in Cambridge).

On its own, (2) makes a claim about what is happening right now here in Cambridge. But there are devices at our disposal that can be added to (2), resulting in claims about snow in displaced situations. Displacement can occur in the **TEMPORAL** dimension and/or in what might be called the **MODAL** dimension. Here's an example of temporal displacement:

- (3) At noon yesterday, it was snowing in Cambridge.

This sentence makes a claim not about snow now but about snow at noon yesterday, a different time from now.

Here's an example of modal displacement:

- (4) If the storm system hadn't been deflected by the jet stream, it would have been snowing in Cambridge.

This sentence makes a claim not about snow in the actual world but about snow in the world as it would have been if the storm system hadn't been deflected by the jet stream, a world distinct from the actual one (where the system did not hit us), a merely **POSSIBLE WORLD**.

Natural language abounds in modal constructions. (4) is a so-called **COUNTERFACTUAL CONDITIONAL**. Here are some other examples:

- (5) **MODAL AUXILIARIES**
It may be snowing in Cambridge.
- (6) **MODAL ADVERBS**
Possibly, it will snow in Cambridge tomorrow.

The terms **MODAL** and **MODALITY** descend from the Latin *modus*, "way", and are ancient terms pertaining to the way a proposition holds, necessarily, contingently, etc.

See Kratzer (1981, 1991) for more examples of modal constructions.

¹ Steiner (1998: 226) writes: "Hypotheticals, 'imaginaries', conditionals, the syntax of counterfactuality and contingency may well be the generative centres of human speech".

- (7) PROPOSITIONAL ATTITUDES
Jens believes that it is snowing in Cambridge.
- (8) HABITUALS
Jane smokes.
- (9) GENERICS
Bears like honey.

In this chapter, we will put in place the basic framework of INTENSIONAL SEMANTICS, the kind of semantics that models displacement of the point of evaluation in temporal and modal dimensions. To do this, we will start with one rather special example of modal displacement:

- (10) In the world of Sherlock Holmes, a detective lives at 221B Baker Street.

(10) doesn't claim that a detective lives at 221B Baker Street in the actual world (presumably a false claim), but that in the world as it is described in the Sherlock Holmes stories of Sir Arthur Conan Doyle, a detective lives at 221B Baker Street (a true claim, of course). We choose this example rather than one of the more run-of-the-mill displacement constructions because we want to focus on conceptual and technical matters before we do serious empirical work.

The questions we want to answer are: How does natural language achieve this feat of modal displacement? How do we manage to make claims about other possible worlds? And why would we want to?

To make displacement possible and compositionally tractable, we need meanings of natural language expressions, and of sentences in particular, to be displaceable in the first place. They need to be “portable”, so to speak, able to make claims about more than just the actual here and now. And need we need other natural language expressions that take that portable meaning and apply it to some situation other than the actual here and now. That is what intensionality is all about.

The basic idea of the account we'll develop is this:

- expressions are assigned their semantic values relative to a possible world;
- in particular, sentences have truth-values in possible worlds;
- in the absence of modal displacement, we evaluate sentences with respect to the “actual” world, the world in which we are speaking;
- modal displacement changes the world of evaluation;
- displacement is effected by special operators, whose semantics is our primary concern here.

A terminological note: we will call the sister of the intensional operator its PREJACENT, a useful term introduced by our medieval colleagues.



https://en.wikipedia.org/wiki/Sherlock_Holmes

1.2 An Intensional Semantics in 10 Easy Steps

1.2.1 Laying the Foundations

STEP 1: POSSIBLE WORLDS. Our first step is to introduce possible worlds. This is not the place to discuss the metaphysics of possible worlds in any depth. Instead, we will just start working with them and see what they can do for us. Basically, a possible world is a way that things might have been. In the actual world, there are two coffee mugs on my desk, but there could have been more or less. So, there is a possible world — albeit a rather bizarre one — where there are 17 coffee mugs on my desk. We join Heim & Kratzer in adducing this quote from [D. Lewis \(1986: 1f.\)](#):



David Lewis

The world we live in is a very inclusive thing. Every stick and every stone you have ever seen is part of it. And so are you and I. And so are the planet Earth, the solar system, the entire Milky Way, the remote galaxies we see through telescopes, and (if there are such things) all the bits of empty space between the stars and galaxies. There is nothing so far away from us as not to be part of our world. Anything at any distance at all is to be included. Likewise the world is inclusive in time. No long-gone ancient Romans, no long-gone pterodactyls, no long-gone primordial clouds of plasma are too far in the past, nor are the dead dark stars too far in the future, to be part of the same world. . . .

The way things are, at its most inclusive, means the way the entire world is. But things might have been different, in ever so many ways. This book of mine might have been finished on schedule. Or, had I not been such a commonsensical chap, I might be defending not only a plurality of possible worlds, but also a plurality of impossible worlds, whereof you speak truly by contradicting yourself. Or I might not have existed at all — neither myself, nor any counterparts of me. Or there might never have been any people. Or the physical constants might have had somewhat different values, incompatible with the emergence of life. Or there might have been altogether different laws of nature; and instead of electrons and quarks, there might have been alien particles, without charge or mass or spin but with alien physical properties that nothing in this world shares. There are ever so many ways that a world might be: and one of these many ways is the way that this world is.

Previously, our “metaphysical inventory” included a domain of entities and a set of two truth-values and increasingly complex functions between entities, truth-values, and functions thereof. Now, we will add possible worlds to the inventory. Let’s assume we are given a set W , the set of all possible worlds, which

is a vast space since there are so many ways that things might have been different from the way they are. Each world has as among its parts entities like you and me and these coffee mugs. Some of them may not exist in other possible worlds. So, strictly speaking each possible worlds has its own, possibly distinctive, domain of entities. What we will use in our system, however, will be the grand union of all these world-specific domains of entities. We will use D to stand for the set of all possible individuals.

Among the many possible worlds that there are — according to Lewis, there is a veritable plenitude of them — is the world as it is described in the Sherlock Holmes stories by Sir Arthur Conan Doyle. In that world, there is a famous detective Sherlock Holmes, who lives at 221B Baker Street in London and has a trusted sidekick named Dr. Watson. Our sentence *In the world of Sherlock Holmes, a detective lives at 221B Baker Street* displaces the claim that a famous detective lives at 221B Baker Street from the actual world to the world as described in the Sherlock Holmes stories. In other words, the following holds:²

- (11) The sentence *In the world of Sherlock Holmes, a detective lives at 221B Baker Street* is true in a world w iff the sentence *a detective lives at 221B Baker Street* is true in the world as it is described in the Sherlock Holmes stories.

What this suggests is that we need to make space in our system for having devices that control in what world a claim is evaluated. This is what we will do now.

STEP 2: THE EVALUATION WORLD PARAMETER. Recall from H&K that we were working with a semantic interpretation function that was relativized to an assignment function g , which was needed to take care of pronouns, traces, variables, etc. From now on, we will relativize the semantic values in our system to possible worlds as well. What this means is that from now on, our interpretation function will have two superscripts: a world w and an assignment g : $\llbracket \cdot \rrbracket^{w,g}$.

So, the prejacent embedded in (10) will have its truth-conditions described as follows:³

- (12) $\llbracket \text{a famous detective lives at 221B Baker Street} \rrbracket^{w,g} = 1$
iff a famous detective lives at 221B Baker Street in world w .

It is customary to refer to the world for which we are calculating the extension of a given expression as the EVALUATION WORLD. In the absence of any shifting devices, we would normally evaluate a sentence in the actual world. But then

² We will see in Section (1.3.2) that this is not quite right. It'll do for now.

³ Recall from H&K, pp.22f, that what's inside the interpretation brackets is a mention of an object language expression. They make this clear by bold-facing all object language expressions inside interpretation brackets. In these notes, we will follow common practice in the field and not use a special typographic distinction, but let it be understood that what is interpreted are object language expressions.

there are shifting devices such as our *in the world of Sherlock Holmes*. We will soon see how they work. But first some more pedestrian steps: adding lexical entries and composition principles that are formulated relative to a possible world. This will allow us to derive the truth-conditions as stated in (12) in a compositional manner.

STEP 3: LEXICAL ENTRIES. Among our lexical items, we can distinguish between items which have a WORLD-DEPENDENT semantic value and those that are world-independent. Predicates are typically world-dependent. Here are some sample entries.

(13) For any $w \in W$ and any assignment function g :

- a. $\llbracket \text{famous} \rrbracket^{w,g} = \lambda x \in D. x \text{ is famous in } w.$ ^{4,5}
- b. $\llbracket \text{detective} \rrbracket^{w,g} = \lambda x \in D. x \text{ is a detective in } w.$
- c. $\llbracket \text{lives-at} \rrbracket^{w,g} = \lambda x \in D. \lambda y \in D. y \text{ lives-at } x \text{ in } w.$

The set of detectives will obviously differ from world to world, and so will the set of famous individuals and the set of pairs where the first element lives at the second element.

Other items have semantic values which do not differ from world to world. The most important such items are certain “logical” expressions, such as truth-functional connectives and determiners:

- (14) a. $\llbracket \text{and} \rrbracket^{w,g} = \lambda u \in D_t. \lambda v \in D_t. u = v = \mathbf{I}.$
 b. $\llbracket \text{the} \rrbracket^{w,g} = \lambda f \in D_{\langle e,t \rangle} : \exists! x [f(x) = \mathbf{I}]. \text{ the } y \text{ such that } f(y) = \mathbf{I}.$
 c. $\llbracket \text{every} \rrbracket^{w,g} = \lambda f_{\langle e,t \rangle}. \lambda h_{\langle e,t \rangle}. \forall x_e : f(x) = \mathbf{I} \rightarrow h(x) = \mathbf{I}.$
 d. $\llbracket \text{a/some} \rrbracket^{w,g} = \lambda f_{\langle e,t \rangle}. \lambda h_{\langle e,t \rangle}. \exists x_e : f(x) = \mathbf{I} \ \& \ h(x) = \mathbf{I}.$

Note that there is no occurrence of w on the right-hand side of the entries in (14). That’s the tell-tale sign of the world-independence of the semantics of these items.

We will also assume that proper names have world-independent semantic values, that is, they refer to the same individual in any possible world.

Note the ruthless condensation of the notation in (c) and (d): variables are subscripted with the type of the domain that their values are constrained to come from.

4 Of course, “ $\lambda x \in D. \dots$ ” is short for “ $\lambda x : x \in D. \dots$ ”. Get used to semanticists condensing their notation whenever convenient! A further step of condensation is taken below: “ $\lambda x : x \in D_e. \dots$ ” becomes “ $\lambda x_e. \dots$ ”.

5 Always make sure that you actually understand what the notation means. Here, for example, we are saying that the semantic value of the word *famous* with respect to a given possible world w and a variable assignment g is that function that is defined for an argument x only if x is a member of the domain of individuals and that, if it is defined, yields the truth-value \mathbf{I} if and only if x is famous in w . (12)[a] does *not* mean that the function maps x to “ x is famous in w ”, which would be very weird: mapping an individual to a meta-language statement!

- (15) a. $\llbracket \text{Noam Chomsky} \rrbracket^{w,g} = \text{Noam Chomsky}.$
 b. $\llbracket \text{Sherlock Holmes} \rrbracket^{w,g} = \text{Sherlock Holmes}.$
 c. $\llbracket \text{221B Baker Street} \rrbracket^{w,g} = \text{221B Baker Street}.$

STEP 4: COMPOSITION PRINCIPLES. The old rules of Functional Application, Predicate Modification, and λ -Abstraction can be retained almost intact. We just need to modify them by adding world-superscripts to the interpretation function. For example:

- (16) FUNCTIONAL APPLICATION (FA)
 If α is a branching node and $\{\beta, \gamma\}$ the set of its daughters, then, for any world w and assignment g : if $\llbracket \beta \rrbracket^{w,g}$ is a function whose domain contains $\llbracket \gamma \rrbracket^{w,g}$, then $\llbracket \alpha \rrbracket^{w,g} = \llbracket \beta \rrbracket^{w,g}(\llbracket \gamma \rrbracket^{w,g})$.

The rule simply passes the world parameter down.

STEP 5: TRUTH. Lastly, we will want to connect our semantic system to the notion of the TRUTH OF AN UTTERANCE. We first adopt the “Appropriateness Condition” from Heim & Kratzer (p.243):

- (17) APPROPRIATENESS CONDITION
 A context c is *appropriate* for an LF ϕ only if c determines a variable assignment g_c whose domain includes every index which has a free occurrence in ϕ .

We then intensionalize Heim & Kratzer’s definition of truth and falsity of utterances:

- (18) TRUTH AND FALSITY CONDITIONS FOR UTTERANCES
 An utterance of a sentence ϕ in a context c in a possible world w is *true* iff $\llbracket \phi \rrbracket^{w,g_c} = \mathbf{1}$ and *false* if $\llbracket \phi \rrbracket^{w,g_c} = \mathbf{0}$.

EXERCISE 1.1: Compute under what conditions an utterance in possible world w_7 (which may or may not be the one we are all living in) of the sentence *a famous detective lives at 221B Baker Street* is true. [Since this is the first exercise in this framework, please do this in excruciating detail, not skipping any steps.] \square

1.2.2 Intensional Operators

So far we have merely “redecorated” the system inherited from Heim & Kratzer. We have introduced possible worlds into our inventory, our lexical entries and our old composition principles. But with the tools we have now, all we can do so far is to keep track of the world in which we evaluate the semantic value of an expression, complex or lexical. We will get real mileage once we introduce INTENSIONAL OPERATORS which are capable of shifting the world parameter.

We mentioned that there are a number of devices for modal displacement. As advertised, for now, we will just focus on a very particular one: the expression *in the world of Sherlock Holmes*. We will assume, as seems reasonable, that this expression is a sentence-modifier both syntactically and semantically.

STEP 6: A SYNCATEGOREMATIC ENTRY. We begin with a heuristic step. We want to derive something like the following truth-conditions for our sentence:

- (19) $\llbracket \text{in the world of Sherlock Holmes, a famous detective lives at 221B Baker Street} \rrbracket^{w,g} = 1$
 iff the world w' as it is described in the Sherlock Holmes stories is such that there exists a famous detective in w' who lives at 221B Baker Street in w' .

We would get this if in general we had this rule for *in the world of Sherlock Holmes*:

- (20) For any sentence ϕ , any world w , and any assignment g :
 $\llbracket \text{in the world of Sherlock Holmes } \phi \rrbracket^{w,g} = 1$
 iff the world w' as it is described in the Sherlock Holmes stories is such that $\llbracket \phi \rrbracket^{w',g} = 1$.

This is a so-called SYNCATEGOREMATIC treatment of the meaning of this expression. Instead of giving an explicit semantic value to the expression, we specify what effect it has on the meaning of a complex expression that contains it. In (20), we do not compute the meaning for *in the world of Sherlock Holmes*, ϕ from the combination of the meanings of its parts, since *in the world of Sherlock Holmes* is not given a separate meaning, but in effect triggers a special composition principle. This format is very common in modal logic systems, which usually give a syncategorematic semantics for the two modal operators (the necessity operator \Box and the possibility operator \Diamond). When one only has a few closed class expressions to deal with that may shift the world parameter, employing syncategorematic entries is a reasonable strategy. But we are facing a multitude of displacement devices. So, we will need to make our system more modular.

So, we want to give *in the world of Sherlock Holmes* its own meaning and combine that meaning with that of its prejacent by a general composition principle. The Fregean slogan we adopted says that all composition is function application (modulo the need for λ -abstraction and the possible need for predicate modification).⁶ So, what we will want to do is to make 19 be the result of functional application. But we can immediately see that it cannot be the result of our usual rule of functional application, since that would feed to *in the world of Sherlock*

The diamond \Diamond symbol for possibility is due to C.I. Lewis, first introduced in C. I. Lewis & Langford (1932), but he made no use of a symbol for the dual combination $\neg\Diamond\neg$. The dual symbol \Box was later devised by F.B. Fitch and first appeared in print in 1946 in a paper by his doctoral student Barcan (1946). See footnote 425 of Hughes & Cresswell (1968). Another notation one finds is L for necessity and M for possibility, the latter from the German *möglich* 'possible'.

6 See Heim & Kratzer, Section 4.3, pp. 63–72 for a reminder about the status of predicate modification.

Holmes the semantic value of *a famous detective lives in 221B Baker Street* in w , which would be a particular truth-value, 1 if a famous detective lives at 221B Baker Street in w and 0 if there doesn't. And whatever the semantics of *in the world of Sherlock Holmes* is, it is certainly *not* a truth-functional operator.

So, we need to feed something else to *in the world of Sherlock Holmes*. At the same time, we want the operator to be able to shift the evaluation world of its prejacent. Can we do this?

EXERCISE 1.2: How would you show that *in the world of Sherlock Holmes* is not a truth-functional operator? \square

STEP 7: INTENSIONS. We will define a richer notion of semantic value, the INTENSION of an expression. This will be a function from possible worlds to the extension of the expression in that world. The intension of a sentence can be applied to any world and give the truth-value of the sentence in that world. Intensional operators take the intension of their prejacent as their argument, that is we will feed the intension of the embedded sentence to the shifting operator. The operator will use that intension and apply it to the world it wants the evaluation to happen in. Voilà.

Now let's spell that account out. Our system actually provides us with two kinds of meanings. For any expression α , we have $\llbracket \alpha \rrbracket^{w,g}$, the semantic value of α in w , also known as the EXTENSION of α in w . But we can also calculate $\lambda w. \llbracket \alpha \rrbracket^{w,g}$, the function that assigns to any world w the extension of α in that world. This is usually called the INTENSION of α . We will sometimes use an abbreviatory notation⁷ for the intension of α :

$$(21) \quad \llbracket \alpha \rrbracket_{\text{c}}^g := \lambda w. \llbracket \alpha \rrbracket^{w,g}.$$

It should be immediately obvious that since the definition of intension abstracts over the evaluation world, intensions are not world-dependent.^{8,9}

Note that strictly speaking, it now makes no sense anymore to speak of “*the* semantic value” of an expression α . What we have is a semantic system that allows us to calculate extensions (for a given possible world w) as well as intensions for all (interpretable) expressions. We will see that when α occurs in a

As before in H&K, we make no claim that the semantic values that are attributed to expressions in our framework fully capture what is informally meant by “meaning”. But certainly, intensions come closer to “meaning” than extensions.

⁷ The notation with the subscripted cent-sign comes from Montague Grammar. See e.g. Dowty, Wall & Peters (1991: 147).

⁸ Since intensions are by definition not dependent on the choice of a particular world, it makes no sense to put a world-superscript on the intension-brackets. So don't ever write “ $\llbracket \dots \rrbracket_{\text{c}}^{w,g}$ ”; we'll treat that as undefined nonsense.

⁹ The definition here is simplified, in that it glosses over the fact that some expressions, in particular those that contain PRESUPPOSITION TRIGGERS, may fail to have an extension in certain worlds. In such a case, the intension has no extension to map such a world to. Therefore, the intension will have to be a partial function. So, the official, more “pedantic”, definition will have to be as follows: $\llbracket \alpha \rrbracket_{\text{c}}^g := \lambda w: \alpha \in \text{dom}(\llbracket \dots \rrbracket^{w,g}). \llbracket \alpha \rrbracket^{w,g}$.

particular bigger tree, it will always be determinate which of the two “semantic values” of α is the one that enters into the compositional semantics. So, that one — whichever one it is, the extension or the intension of α — might then be called “*the* semantic value of α in the tree β ”.

It should be noted that the terminology of EXTENSION vs. INTENSION is time-honored but that the possible worlds interpretation thereof is more recent. The technical notion we are using is certainly less rich a notion of meaning than traditionally assumed.¹⁰

STEP 8: SEMANTIC TYPES AND SEMANTIC DOMAINS. If we want to be able to feed the intensions to lexical items like *in the world of Sherlock Holmes*, we need to have the appropriate types in our system.

Recall that W is the set of all possible worlds. And recall that D is the set of all POSSIBLE INDIVIDUALS and thus contains all individuals existing in the actual world *plus* all individuals existing in any of the merely possible worlds.

We now expand the set of semantic types, to add intensions. Intensions are functions from possible worlds to all kinds of extensions. So, basically we want to add for any kind of extension we have in our system, a corresponding kind of intension, a function from possible worlds to that kind of extension.

We add a new clause, (22c), to the definition of semantic types:

- (22) SEMANTIC TYPES
- a. e and t are semantic types.
 - b. If σ and τ are semantic types, then $\langle \sigma, \tau \rangle$ is a semantic type.
 - c. If σ is a semantic type, then $\langle s, \sigma \rangle$ is a semantic type.
 - d. Nothing else is a semantic type.

We also add a fourth clause to the previous definition of semantic domains:

- (23) SEMANTIC DOMAINS
- a. $D_e = D$, the set of all possible individuals
 - b. $D_t = \{0, 1\}$, the set of truth-values
 - c. If σ and τ are semantic types, then $D_{\langle \sigma, \tau \rangle}$ is the set of all functions from D_σ to D_τ .
 - d. INTENSIONS: If σ is a type, then $D_{\langle s, \sigma \rangle}$ is the set of all functions from W to D_σ .

Clause (d) is the addition to our previous system of types. The functions of the schematic type $\langle s, \dots \rangle$ are intensions.¹¹ Here are some examples of intensions:

¹⁰ For example, Frege’s “modes of presentation” are not obviously captured by this possible worlds implementation of extension/intension.

¹¹ Note a curious feature of this set-up: there is no type s and no associated domain. This corresponds to the assumption that there are no expressions of English that take as their extension

The Port-Royal logicians distinguished EXTENSION from COMPREHENSION. Leibniz preferred the term INTENSION rather than COMPREHENSION. The notion probably goes back even further. See [Spencer \(1971\)](#) for some notes on this. The possible worlds interpretation is due to [Carnap \(1947\)](#).

- The intensions of sentences are of type $\langle s, t \rangle$, functions from possible worlds to truth values. These are usually called PROPOSITIONS. Note that if the function is total, then we can see the sentence as picking out a set of possible worlds, those in which the sentence is true. More often than not, however, propositions will be PARTIAL functions from worlds to truth-values, that is functions that fail to map certain possible worlds into either truth-value. This will be the case when the sentence contains a presupposition trigger, such as *the*. The famous sentence *The King of France is bald* has an intension that (at least in the analysis sketched in Heim & Kratzer) is undefined for any world where there fails to be a unique King of France.
- The intensions of one-place predicates are of type $\langle s, \langle e, t \rangle \rangle$, functions from worlds to set of individuals. These are usually called PROPERTIES.
- The intensions of expressions of type e are of type $\langle s, e \rangle$, functions from worlds to individuals. These are usually called INDIVIDUAL CONCEPTS.

STEP 9: A LEXICAL ENTRY FOR A SHIFTER. We are ready to formulate the lexical entry for *in the world of Sherlock Holmes*.¹²

- (24) $\llbracket \text{in the world of Sherlock Holmes} \rrbracket^{w,g} =$
 $\lambda p_{\langle s, t \rangle}. \text{the world } w' \text{ as it is described in the Sherlock Holmes stories}$
 $\text{is such that } p(w') = 1.$

That is, *in the world of Sherlock Holmes* expects as its argument a function of type $\langle s, t \rangle$, a proposition. It yields the truth-value 1 iff the proposition is true in the world as it is described in the Sherlock Holmes stories.

All that's left to do now is to provide *in the world of Sherlock Holmes* with a proposition as its argument. This is the job of a new composition principle.

STEP 10: INTENSIONAL FUNCTIONAL APPLICATION. We add the new rule of Intensional Functional Application.

- (25) INTENSIONAL FUNCTIONAL APPLICATION (IFA)
 If α is a branching node and $\{\beta, \gamma\}$ the set of its daughters, then, for any world w and assignment g : if $\llbracket \beta \rrbracket^{w,g}$ is a function whose domain contains $\llbracket \gamma \rrbracket_c^g$, then $\llbracket \alpha \rrbracket^{w,g} = \llbracket \beta \rrbracket^{w,g}(\llbracket \gamma \rrbracket_c^g).$

a possible world, that is, there are no pronouns or names referring to possible worlds. We will actually question this assumption in a later chapter. For now, we will stay with this more conventional set-up.

12 This is not yet the final semantics, see Section (1.3) for complications. One complication we will not even start to discuss is that obviously it is not a necessity that there are Sherlock Holmes stories in the first place and that the use of this operator *presupposes* that they exist; so a more fully explicit semantics would need to build in that presuppositional component. Also, note again the condensed notation: “ $\lambda p_{\langle s, t \rangle}. \dots$ ” stands for the fully official “ $\lambda p: p \in D_{\langle s, t \rangle}. \dots$ ”.

This is the crucial move. It makes space for expressions that want to take the intension of their sister as their argument and do stuff to it. Now, everything is in place. Given 24, the semantic argument of *in the world of Sherlock Holmes* will not be a truth-value but a proposition. And thus, *in the world of Sherlock Holmes* will be able to check the truth-value of its prejacent in various possible worlds. To see in practice that we have all we need, please do the following exercise.

EXERCISE 1.3: Calculate the conditions under which an utterance in a given possible world w_7 of the sentence *in the world of the Sherlock Holmes stories, a famous detective lives at 221B Baker Street* is true. \square

EXERCISE 1.4: What in our system prevents us from computing the extension of *Watson is slow*, for example, by applying the intension of *slow* to the extension of *Watson*? What in our system prevents us from computing the extension of *Watson is slow* by applying the intension of *slow* to the intension of *Watson*? \square

Please think about this exercise before looking at Section (1.4), which explores this issue.

EXERCISE 1.5: What is wrong with the following equation:

$$(26) \quad (\lambda x. x \text{ is slow in } w) (\text{Watson}) = \text{Watson is slow in } w.$$

[Hint: there is nothing wrong with the following:

$$(27) \quad . (\lambda x. x \text{ is slow in } w) (\text{Watson}) = 1 \text{ iff Watson is slow in } w.]$$

\square

1.3 Comments and Complications

1.3.1 Intensions All the Way?

We have seen that to adequately deal with expressions like *in the world of Sherlock Holmes*, we need an intensional semantics, one that gives us access to the extensions of expressions across the multitude of possible worlds. At the same time, we have kept the semantics for items like *and*, *every*, and *a* unchanged and extensional. This is not the only way one can set up an intensional semantics. The following exercise demonstrates this.

EXERCISE 1.6: Consider the following “intensional” meaning for *and*:

$$(28) \quad \llbracket \text{and} \rrbracket^{w,g} = \lambda p_{\langle s,t \rangle}. \lambda q_{\langle s,t \rangle}. p(w) = q(w) = 1.$$

With this semantics, *and* would operate on the intensions of the two conjoined sentences. In any possible world w , the complex sentence will be true iff the component propositions are both true of that world.

Compute the truth-conditions of the sentence *In the world of Sherlock Holmes, Holmes is quick and Watson is slow* both with the extensional meaning for *and*

given earlier and the intensional meaning given here. Is there any difference in the results? □

There are then at least two ways one could develop an intensional system.

- (i) We could “generalize to the worst case” and make the semantics deliver intensions as *the* semantic value of an expression. Such systems are common in the literature (see [D. Lewis 1970](#), [Cresswell 1973](#)).
- (ii) We could maintain much of the extensional semantics we have developed so far and extend it conservatively so as to account for non-extensional contexts.

We have chosen to pursue (ii) over (i), because it allows us to keep the semantics of extensional expressions simpler. The philosophy we follow is that we will only move to the intensional sub-machinery when triggered by an expression that creates a non-extensional context. As the exercise just showed, this is more a matter of taste than a deep scientific decision.

1.3.2 Why Talk about Other Worlds?

Why would natural language bother having such elaborate mechanisms to talk about other possible worlds? While having devices for spatial and temporal displacement (talking about Hamburg or what happened yesterday) seems eminently reasonable, talking about worlds other than the actual world seems only suitable for poets and the like. So, why?

The solution to this puzzle lies in a fact that our current semantics of the shifter *in the world of Sherlock Holmes* does not yet accurately capture: modal sentences have empirical content, they make CONTINGENT claims, claims that are true or false depending on the circumstances in the actual world.

Our example sentence *In the world of Sherlock Holmes, a famous detective lives at 221B Baker Street* is true in this world but it could easily have been false. There is no reason why Sir Arthur Conan Doyle could not have decided to locate Holmes’ abode on Abbey Road.

To see that our semantics does not yet capture this fact, notice that in the semantics we gave for *in the world of Sherlock Holmes*:

- (29) $\llbracket \text{in the world of Sherlock Holmes} \rrbracket^{w,g} =$
 $\lambda p_{\langle s,t \rangle}. \text{the world } w' \text{ as it is described in the Sherlock Holmes stories}$
 $\text{is such that } p(w') = 1.$

there is no occurrence of w on the right hand side. This means that the truth-conditions for sentences with this shifter are world-independent. In other words, they are predicted to make non-contingent claims that are either true no-matter-what or false no-matter-what. This needs to be fixed.

The fix is obvious: what matters to the truth of our sentence is the content of the Sherlock Holmes stories as they are in the evaluation world. So, we need the following semantics for our shifter:

- (30) $\llbracket \text{in the world of Sherlock Holmes} \rrbracket^{w,g} =$
 $\lambda p_{\langle s,t \rangle}. \text{the world } w' \text{ as it is described in the Sherlock Holmes stories}$
in w is such that $p(w') = 1$.

We see now that sentences with this shifter do make a claim about the evaluation world: namely, that the Sherlock Holmes stories as they are in the evaluation world describe a world in which such-and-such is true. So, what is happening is that although it appears at first as if modal statements concern other possible worlds and thus couldn't really be very informative, they actually only talk about certain possible worlds, those that stand in some relation to what is going on at the ground level in the actual world. As a crude analogy, consider:

- (31) My grandmother is sick.

At one level this is a claim about my grandmother. But it is also a claim about me: namely that I have a grandmother who is sick. Thus it is with modal statements. They talk about possible worlds that stand in a certain relation to the actual world and thus they make claims about the actual world, albeit slightly indirectly.

1.3.3 The Worlds of Sherlock Holmes

So far, we have played along with colloquial usage in talking of *the* world of Sherlock Holmes. But it is important to realize that this is sloppy talk. D. Lewis (1978) writes:

[I]t will not do to follow ordinary language to the extent of supposing that we can somehow single out a single one of the worlds [as the one described by the stories]. Is the world of Sherlock Holmes a world where Holmes has an even or an odd number of hairs on his head at the moment when he first meets Watson? What is Inspector Lestrade's blood type? It is absurd to suppose that these questions about the world of Sherlock Holmes have answers. The best explanation of that is that the worlds of Sherlock Holmes are plural, and the questions have different answers at different ones.

The usual move at this point is to talk about the set of worlds "COMPATIBLE WITH the (content of) Sherlock Holmes stories in w ". We imagine that we ask of each possible world whether what is going on in it is compatible with the stories as they were written in our world. Worlds where Holmes lives on Abbey Road are not compatible. Some worlds where he lives at 221B Baker Street are compatible (again not all, because in some such worlds he is not a famous detective but

an obscure violinist). Among the worlds compatible with the stories are ones where he has an even number of hairs on his head at the moment when he first meets Watson and there are others where he has an odd number of hairs at that moment.

What the operator *in the world of Sherlock Holmes* expresses is that its complement is true throughout the worlds compatible with the stories. In other words, the operator *universally quantifies* over the compatible worlds. Our next iteration of the semantics for the operator is therefore this:

- (32) $\llbracket \text{in the world of Sherlock Holmes} \rrbracket^{w,g} =$
 $\lambda p_{\langle s,t \rangle}. \forall w' \text{ compatible with the Sherlock Holmes stories in } w:$
 $p(w') = 1.$

At a very abstract level, the way we parse sentences of the form *in the world of Sherlock Holmes*, ϕ is that both components, the *in*-phrase and the prejacent, determine sets of possible worlds and that the set of possible worlds representing the content of the fiction mentioned in the *in*-phrase is a subset of the set of possible worlds determined by the prejacent. We will see the same rough structure of relating sets of possible worlds in other intensional constructions.

This is where we will leave things. There is more to be said about fiction operators like *in the world of Sherlock Holmes*, but we will just refer to you to the relevant literature. In particular, one might want to make sense of Lewis' idea that a special treatment is needed for cases where the sentence makes a claim about things that are left open by the fiction (no truth-value, perhaps?). One also needs to figure out how to deal with cases where the fiction is internally inconsistent. In any case, for our purposes we're done with this kind of operator.

1.3.4 What's next

With the basic framework of intensional semantics in place, we can now look at a succession of intensional operators. In particular, we will explore the semantics of propositional attitude predicates such as *believe* or *want*, modal auxiliaries such as *must* or *might*, and conditional sentences. In each case, we will see that they shift the evaluation of their prejacent to a certain set of possible worlds and that which worlds we are taken to depends on certain facts about the original evaluation world. We will look at the non-trivial issues that arise when several intensional operators interact (modals under attitudes, modals in the consequent of a conditional, etc.). We will also see that constituents of the prejacent can sometimes be evaluated with respect to a world that is not the world that the intensional operator is taking us to (so-called *de re* readings). Further, we will move from worlds to times and explore the semantics of tense and aspect. And, for the intrepid, this can all come together by exploring how tense and aspect interact with attitudes, modality, and conditionals.

1.4 *Issues with an informal meta-language

Starred sections are optional on a first pass.

Exercise (1.5) asks what is wrong with writing something like¹³

$$(33) \quad (\lambda x. x \text{ is slow in } w) (\text{Watson}) = \text{Watson is slow in } w.$$

Think about it. On the left hand side of the “=” sign is a meta-language expression consisting of a λ -expression (so some kind of function) applied to an individual (contributed by the meta-language name “Watson”). The function is a function from individuals to truth-values that will deliver the truth-value 1 if the individual is slow in world w . So, what we have on the left hand side is the result of a function from individuals to truth-values applied to an individual. In other words, on the left hand side we have a truth-value, namely the truth-value 1 if Watson is slow in w and the truth-value 0 if Watson is not slow in w .

Now, what do we have on the right hand side of the “=”? We have the meta-language sentence “Watson is slow in w ”. That is not nor does it contribute a truth-value. It is a statement of fact. Truth-values are not the same as statements of fact.

The proper thing to do is to write

$$(34) \quad (\lambda x. x \text{ is slow in } w) (\text{Watson}) = 1 \text{ iff Watson is slow in } w.$$

There are actually two ways to parse the statement in (34), both legitimate it appears.

On one parse, the major connective is the meta-language expression “iff”. On its left hand side is a meta-language statement (that applying the function to the individual Watson gives the truth-value 1) and on the right hand side of the “iff” we have another meta-language statement (that Watson is slow in w). So, the whole thing says that these two statements are equivalent: (i) that function applied to that individual gives us the truth-value 1, and (ii) that Watson is slow in w .

The other parse is perhaps more conspicuously represented as follows:

$$(35) \quad (\lambda x. x \text{ is slow in } w) (\text{Watson}) = \begin{cases} 1 & \text{if Watson is slow in } w \\ 0 & \text{if Watson is not slow in } w \end{cases}$$

Here, the “=” sign is the major connective. The left hand side is a meta-language expression that resolves to a truth-value and the right hand side as well contributes a truth-value: 1 if such and such and 0 if such and such.

H&K, of course, introduced a convention that allowed meta-language statements to be used in a place where a truth-value was expected (p.37, (9)):

Read “[$\lambda\alpha: \phi. \gamma$]” as either (i) or (ii), whichever makes sense.

(i) “the function which maps every α such that ϕ to γ ”

Is this weird? It turns out that natural language, not just our semi-formal meta-language, has conditionals that seem very similar: *I fear [the consequences if we fail]*. See Lasersohn 1996 for some discussion.

¹³ Thanks to Magda Kaufmann, Angelika Kratzer, and Ede Zimmermann for discussion on the issues explored in this section.

- (ii) “the function which maps every α such that γ to 1, if γ , and to 0 otherwise”

Since it never makes sense to map anything to a meta-language statement, no ambiguity will ever arise.

So, one might want to extend this leeway and use it in the case of (33) as well. We could say that in general, meta-language statements supply truth-values wherever that makes sense. In that case, (33) is just shorthand for (34).

This is the approach of von Stechow 1991.

Alternatively, one can introduce a new notation that indicates that a meta-language statement is being used to contribute a truth-value:

This is the approach Ede Zimmermann (pc) advocates and has been using in his classes.

$$(36) \quad \vdash \alpha \dashv = \begin{cases} 1 & \text{if } \alpha \\ 0 & \text{if otherwise} \end{cases}$$

Lastly, one could abandon the H & K informal meta-language approach altogether and introduce a rigidly formalized meta-language.

These lecture notes will proceed to follow H & K's approach and will not introduce any further innovations. So, (33) is illicit and only (34) is acceptable.

1.5 Supplemental Readings

There is considerable overlap between this chapter and Chapter 12 of Heim & Kratzer's textbook:

Irene Heim & Angelika Kratzer. 1998. *Semantics in generative grammar*. Oxford: Blackwell.

Here, we approach intensional semantics from a different angle. It would probably be beneficial if you read H & K's Chapter 12 in addition to this chapter and if you did the exercises in there.

Come to think of it, some other ancillary reading is also recommended. You may want to look at relevant chapters in other textbooks:

David R. Dowty, Robert Wall & Stanley Peters. 1981. *Introduction to Montague semantics*. Kluwer. [Chapters 5 & 6].

L. T. F. Gamut. 1991. *Logic, language, and meaning*. Chicago University Press. [Volume II: Intensional Logic and Logical Grammar].

Gennaro Chierchia & Sally McConnell-Ginet. 2000. *Meaning and grammar: An introduction to semantics (2nd edition)*. MIT Press. [Chapter 5: Intensionality].

Thomas Ede Zimmermann & Wolfgang Sternefeld. 2013. *Introduction to semantics: An essential guide to the composition of meaning*. de Gruyter Mouton.

The *Stanford encyclopedia of philosophy* is always a good resource. Here's the entry on possible worlds:

Christopher Menzel. 2016. Possible worlds. In Edward N. Zalta (ed.), *The Stanford encyclopedia of philosophy*, Spring 2016. <http://plato.stanford.edu/entries/possible-worlds/>.

A couple of influential philosophical works on the metaphysics and uses of possible worlds:

Saul Kripke. 1980. *Naming and necessity*. Oxford: Blackwell.

David Lewis. 1986. *On the plurality of worlds*. Oxford: Blackwell.

An interesting paper on the origins of the modern possible worlds semantics for modal logic:

B. Jack Copeland. 2002. The genesis of possible worlds semantics. *Journal of Philosophical Logic* 31(2). 99–137. <http://dx.doi.org/10.1023/A:1015273407895>.

A personal history of formal semantics:

Barbara H. Partee. 2005. Reflections of a formal semanticist as of Feb 2005. ms. (longer version of introductory essay in 2004 book). http://people.umass.edu/partee/docs/BHP_Essay_Feb05.pdf.

A must read for students who plan to go on to becoming specialists in semantics, together with a handbook article putting it in perspective:

Richard Montague. 1973. The proper treatment of quantification in ordinary English. In Jaako Hintikka, Julius Moravcsik & Patrick Suppes (eds.), *Approaches to natural language*, 221–242. Reprinted in Portner & Partee (2002), pp. 17–34. Dordrecht: Reidel. http://www.blackwellpublishing.com/content/BPL/Images/Content_store/Sample_chapter/9780631215417/Portner.pdf.

Barbara H. Partee & Herman L.W. Hendriks. 1997. Montague grammar. In Johan van Benthem & Alice ter Meulen (eds.), *Handbook of logic and language*, 5–91. Elsevier.

To learn more about discourse about fiction, read Lewis:

David Lewis. 1978. Truth in fiction. *American Philosophical Quarterly* 15(1). Reprinted with postscripts in D. Lewis (1983), pp. 261–280, 37–46. <http://www.jstor.org/stable/20009693>.

Recent reconsiderations:

Andrea Bonomi & Sandro Zucchi. 2003. A pragmatic framework for truth in fiction. *Dialectica* 57(2). Preprint <http://filosofia.dipafilo.unimi.it/~bonomi/Pragmatic.pdf>, 103–120. <http://dx.doi.org/10.1111/j.1746-8361.2003.tb00259.x>.

Richard Hanley. 2004. As good as it gets: Lewis on truth in fiction. *Australasian Journal of Philosophy* 82(1). 112–128. <http://dx.doi.org/10.1080/713659790>.

Diane Proudfoot. 2006. Possible worlds semantics and fiction. *Journal of Philosophical Logic* 35(1). 9–40. <http://dx.doi.org/10.1007/s10992-005-9005-8>.

Inconsistencies in fictions and elsewhere are discussed in:

Achille Varzi. 1997. Inconsistency without contradiction. *Notre Dame Journal of Formal Logic* 38(4). 621–638. <http://dx.doi.org/10.1305/ndjfl/1039540773>.

David Lewis. 1982. Logic for equivocators. *Noûs* 16(3). Reprinted in D. Lewis (1998: pp. 97–110), 431–441. <http://dx.doi.org/10.2307/2216219>.

Some other interesting work on stories and pictures and their content:

Jeff Ross. 1997. *The semantics of media* (Studies in Linguistics and Philosophy (SLAP) 64). Dordrecht: Kluwer.

Sandro Zucchi. 2001. Tense in fiction. In Carlo Cecchetto, Gennaro Chierchia & Maria Teresa Guasti (eds.), *Semantic interfaces: Reference, anaphora and aspect*, 320–355. CSLI Publications. <http://tinyurl.com/5ulwxwg>.

Ben Blumson. 2009. Pictures, perspective and possibility. *Philosophical Studies*. <http://dx.doi.org/10.1007/s11098-009-9337-2>.

Astonishingly, Lewis’ doctrine of the reality of the plurality of possible worlds is being paralleled (pun absolutely intended) by theoretical physicists in a number of ways. There is a controversial “many worlds” interpretation of quantum mechanics, for example. Other terms found are the “multiverse” and “parallel universes”. See for starters, Kai’s blog entry on a popular book on the issue, <http://kaivonfintel.org/many-worlds/>, MIT physics professor Max Tegmark’s page on the topic, <http://space.mit.edu/home/tegmark/crazy.html>, and a Fresh Air interview with physicist Brian Greene, who just wrote a book called *The Hidden Reality: Parallel Universes and the Deep Laws of the Cosmos*: <http://www.npr.org/2011/01/24/132932268/a-physicist-explains-why-parallel-universes-may-exist>.

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CHAPTER TWO

CONDITIONALS

The word “if”, just two tiny letters
Says so much for something so small
The biggest little word in existence;
Never answers, just questions us all

If regrets were gold, I’d be rich as a queen
If teardrops were diamonds, how my face would gleam
If I’d loved you better, I wouldn’t be lonely
If only, if only, if only

Dolly Parton, *If Only*

We develop a possible worlds semantics for conditionals that treats the if-clause as an intensional operator, with a bit of context-dependency thrown in.

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2.1 *If* ... the biggest little word

In many ways, conditionals are the archetypal construction of displacement: the consequent is evaluated not against the actual here and now but against the scenario conjured up by the antecedent. Consider a few conditional sentences:

- (1) a. If Kim left before 6am, she got here in time.
b. If there’s an earthquake tomorrow, this house will collapse.
c. If there had been a massive snowstorm last night, Kai would have stayed home.

These represent the three main subtypes of conditionals (there are more): (1a) is an “indicative” conditional about the past, (1b) is an indicative conditional about the future, and (1c) is a “subjunctive” conditional. For the moment, the differences will be left aside.

The basic idea of how conditionals work is this: the *if*-clause takes us to a particular possible world (or maybe a set thereof) and the consequent clause is asserted to be true of that world (or those worlds). But what world(s) are we being taken to? The most obvious requirement is that the antecedent of the conditional needs to be true of the world(s). But there’s more.

Given our discussion of how the semantics of fiction operators anchors them in facts about the actual world (the content of the relevant body of fiction), it shouldn’t come as a surprise that conditionals are similarly anchored. So, look at the examples in (1): what in the actual world are they about?

Here’s a sketch: (1a) is about the local transportation system, the weather, the traffic, and so on. (1b) is about the sturdiness of this house, facts of geology, laws of physics, and so on. (1c) is about Kai’s proclivities (such as avoiding traffic snarls), the local climate, and so on. Since the conditionals are anchored in real world facts, they are no mere flights of fancy and whether they are true depends on those facts. If today’s traffic was particularly bad, it may be false that Kim’s leaving before 6am would have got her here in time. If the architects went to great lengths to make the house earthquake-safe, (1b) may well be false. And if there was an attendance-mandatory faculty meeting, Kai may well have come in in spite of a massive snowstorm.

So, the outlines of the semantics of conditionals are clear: *if* takes us to worlds where the antecedent is true but that match the actual world in certain relevant features. And the consequent then is evaluated in those worlds. There are many details to work out and we’ll return to that task in Part III of these notes. But for now, we put forward a placeholder analysis.

2.2 The Restricted Strict Implication Analysis

We will treat *if* as a higher-order operator that together with the antecedent creates an intensional operator with a semantics very similar to the final analysis we gave to *in the world of Sherlock Holmes* in the previous chapter. But where the fiction operator directly encoded what features of the actual world it’s sensitive to (the Sherlock Holmes fiction), conditionals rely on context for this job. Here’s the proposal:

$$(2) \quad \llbracket \text{if} \rrbracket^{w,g} = \lambda p \in D_{\langle s,t \rangle}. \lambda q \in D_{\langle s,t \rangle}. \\ \forall w': p(w') = 1 \ \& \ w' \text{ is relevantly like } w \rightarrow q(w') = 1.$$

The contextual anchoring to features of the evaluation world w is here effected by the placeholder “relevantly like w ”. This is crucial because otherwise the

It is perhaps unfortunate that David Lewis used a rather whimsical example to start off his seminal book on counterfactuals (“If kangaroos had not tails, they would topple over”). Or consider this scene from the TV show “Big Bang Theory”: <https://www.youtube.com/watch?v=olpYoKt4bn8>. As the examples in the text make clear, conditionals can be very down-to-earth.

conditional would talk about any world whatsoever where the antecedent is true. This would make the truth-conditions not just not contingent on the actual world but also far too strong to allow most sensible conditionals to be true ever.

Think about the earthquake conditional (1b): we would derive the absurdly strong truth-conditions that the conditional is true iff *all* of the worlds where there is a major earthquake in Cambridge tomorrow are worlds where my house collapses.

There are some obvious and immediate problems with this analysis. For one, while it's easy to imagine circumstances where the conditional (1b) is judged to be true, there surely are possible worlds where there's an earthquake but my house does not collapse: perhaps, the builders in that world used all the recommended best practices to make the building earthquake-safe, perhaps it's a world where I'm simply unreasonably lucky, or the house is immediately adjacent to much sturdier neighboring buildings which keep it propped up, or Harry Potter flies by and protects the house at the last minute (he owes me a favor, after all). This problem (that the house doesn't in fact collapse in *all* possible worlds where there's an earthquake but that the conditional can still be judged true in some worlds) is accompanied with another problem: whether the conditional is true depends on what the world is like. Was the house built to exacting standards? Is it propped up by its neighbors? Does Harry Potter owe me a favor? That is the problem solved by restricting the quantifier over worlds to world “relevantly like *w*”.

Obviously, this is a semantics with a “placeholder”, because what does “relevantly like” mean precisely? Now, just because the semantics is therefore rather vague and context-dependent doesn't mean it is wrong. As D. Lewis (1973) writes:

Counterfactuals are notoriously vague. That does not mean that we cannot give a clear account of their truth conditions. It does mean that such an account must either be stated in vague terms — which does not mean ill-understood terms — or be made relative to some parameter that is fixed only within rough limits on any given occasion of language use.

In a later chapter, we will revisit the formulation in (2) and fill it out more explicitly. Before we go on to consider other intensional constructions, we'll briefly talk about the astonishingly silly idea that conditionals are not intensional constructions.

2.3 A red herring: Material implication

Consider the following example:

- (3) If I am healthy, I will come to class.

The simplest analysis of such conditional constructions is the so-called MATERIAL IMPLICATION analysis,¹ which treats *if* as contributing a truth-function operating on the truth-values of the two component sentences (which are called the ANTECEDENT and CONSEQUENT — from Latin — or PROTASIS and APODOSIS — from Greek). The lexical entry for *if* would look as follows:

$$(4) \quad \llbracket \text{if} \rrbracket = \lambda u \in D_t. \lambda v \in D_t. u = 0 \text{ or } v = 1.$$

Note that as a truth-functional connective, this *if* does not vary its denotation depending on the evaluation world. It's its arguments that vary with the evaluation world.

Applied to example in (3), this semantics would predict that the example is false just in case the antecedent is true, I am healthy, but the consequent false, I do not come to class. Otherwise, the sentence is true. We will see that there is much to complain about here. But one should realize that under the assumption that *if* denotes a truth-function, *this one* is the most plausible candidate.

Suber (1997) does a good job of persuading (or at least trying to persuade) recalcitrant logic students:

After saying all this, it is important to note that material implication does conform to some of our ordinary intuitions about implication. For example, take the conditional statement, *If I am healthy, I will come to class*. We can symbolize it: $H \supset C$.²

The question is: when is this statement false? When will I have broken my promise? There are only four possibilities:

H	C	$H \supset C$
T	T	?
T	F	?
F	T	?
F	F	?

- In case #1, I am healthy and I come to class. I have clearly kept my promise; the conditional is true.
- In case #2, I am healthy, but I have decided to stay home and read magazines. I have broken my promise; the conditional is false.
- In case #3, I am not healthy, but I have come to class anyway. I am sneezing all over you, and you're not happy about it, but I did not violate my promise; the conditional is true.

¹ Quoth the Stoic philosopher Philo of Megara: “a true conditional is one which does not have a true antecedent and a false consequent” (according to Empiricus (c. 200: II, 110–112)).

² The symbol \supset which Suber uses here is called the “horseshoe”. We have been using the right arrow \rightarrow as the symbol for implication. We think that this is much preferable to the confusing horseshoe symbol. There is an intimate connection between universal quantification, material implication, and the subset relation, usually symbolized as \subset , which is the other way round from the horseshoe. The horseshoe can be traced back to the notation introduced by Peano (1889), a capital C standing for ‘consequenza’ facing backwards. The C facing in the other (more “logical”) direction was actually introduced first by Gergonne (1817), but didn't catch on.

- In case #4, I am not healthy, and I did not come to class. I did not violate my promise; the conditional is true.

But this is exactly the outcome required by the material implication. The compound is only false when the antecedent is true and the consequence is false (case #2); it is true every other time.

Despite the initial plausibility of the analysis, it cannot be maintained. Consider again our earthquake example:

- (1b) If there is a major earthquake in Cambridge tomorrow, my house will collapse.

If we adopt the material implication analysis, we predict that (1b) will be false just in case there is indeed a major earthquake in Cambridge tomorrow but my house fails to collapse. This makes a direct prediction about when the negation of (1b) should be true. A false prediction, if ever there was one:

- (5) a. It's not true that if there is a major earthquake in Cambridge tomorrow, my house will collapse.
 b. \neq There will be a major earthquake in Cambridge tomorrow, and my house will fail to collapse.

Clearly, one might think that (5a) is true without at all being committed to what the material implication analysis predicts to be the equivalent statement in (5b). This is one of the inadequacies of the material implication analysis.

These inadequacies are sometimes referred to as the “paradoxes of material implication”. But that is misleading. As far as logic is concerned, there is nothing wrong with the truth-function of material implication. It is well-behaved and quite useful in logical systems. What is arguable is that it is not to be used as a reconstruction of what conditionals mean in natural language.

EXERCISE 2.1: What prediction does the restricted strict implication analysis in (2) make about the negated conditional in (5a)? □

EXERCISE 2.2: Under the assumption that *if* has the meaning in (4), calculate the truth-conditions predicted for (6):

- (6) a. No student will succeed if he goofs off.
 b. No student λx (if x goofs off, x will succeed)

State the predicted truth-conditions in words and evaluate whether they correspond to the actual meaning of (6). □

2.4 Supplemental Readings

We'll come back to conditionals soon enough, but here are two introductory readings:

Kai von Fintel. 2011. Conditionals. In Claudia Maienborn, Klaus von Heusinger & Paul Portner (eds.), *Semantics: An international handbook of meaning*, vol. 2, 1515–1538. de Gruyter. <http://dx.doi.org/10.1515/9783110255072.1515>. <http://mit.edu/fintel/fintel-2011-hsk-conditionals.pdf>.

Kai von Fintel. 2012. Subjunctive conditionals. In Gillian Russell & Delia Graff Fara (eds.), *The Routledge companion to philosophy of language*, 466–477. New York: Routledge. <http://dx.doi.org/1721.1/95784>. <http://mit.edu/fintel/fintel-2012-subjunctives.pdf>.

Here is a not so introductory reading:

Anthony S. Gillies. 2016. Conditionals. To appear in: Bob Hale, Alex Miller, and Crispin Wright, eds. *Blackwell Companion to the Philosophy of Language*, Blackwell. Pre-final draft. <http://semanticsarchive.net/Archive/TAYOTArY/gillies-conditionals-blackwell.pdf>.

A couple of defenses of the material conditional:

Barbara Abbott. 2010. Conditionals in English and FOPL. In Dingfang Shu & Ken Turner (eds.), *Contrasting meanings in languages of the East and West*. Peter Lang. <http://semanticsarchive.net/Archive/jUoM2ZmZ>.

Adam Rieger. 2015. Defending a simple theory of conditionals. *American Philosophical Quarterly* 52(3). 253–260. <http://apq.press.illinois.edu/52/3/rieger.html>.

CHAPTER THREE

PROPOSITIONAL ATTITUDES

We start with the basic possible worlds semantics for propositional attitude ascriptions. We talk briefly about the formal properties of accessibility relations.

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3.1 Hintikka's Idea

Expressions like *believe*, *know*, *doubt*, *expect*, *regret*, and so on are usually said to describe PROPOSITIONAL ATTITUDES, expressing relations between individuals (the attitude holder) and propositions (intensions of sentences).

The simple idea is that *George believes that Henry is a spy* claims that George believes of the proposition that Henry is a spy that it is true. Note that for the attitude ascription to be true it does not have to hold that Henry is actually a spy. But where—in which world(s)—does Henry have to be a spy for it be true that George believes that Henry is a spy? We might want to be inspired by the colloquial phrase “in the world according to George” and say that *George believes that Henry is a spy* is true iff in the world according to George's beliefs, Henry is a spy. We immediately recall from Chapter 1 that we need to fix this idea up by making space for multiple worlds compatible with George's beliefs and by tying the truth-conditions to contingent facts about the evaluation world. That is, what George believes is different in different possible worlds.

According to [Hintikka \(1969\)](#), the term PROPOSITIONAL ATTITUDE goes back to [Russell \(1940\)](#).

Of course, the possible worlds semantics for propositional attitudes was in place long before the extension to fiction contexts was proposed. Our discussion here has inverted the historical sequence for pedagogical purposes.

The following lexical entry thus offers itself:

$$(I) \quad \llbracket \text{believe} \rrbracket^{w,g} = \lambda p_{\langle s,t \rangle} . \lambda x . \forall w' \text{ compatible with } x\text{'s beliefs in } w : p(w') = 1.$$

It is important to realize the modesty of this semantics: we are not trying to figure out what belief systems are and particularly not what their internal workings are. That is the job of psychologists (and philosophers of mind, perhaps). For our semantics, we treat the belief system as a black box that determines for each possible world whether it considers it possible that it is the world it is located in.

What is going on in this semantics? We conceive of George's beliefs as a state of his mind about whose internal structure we will remain agnostic, a matter left to other cognitive scientists. What we require of it is that it embody opinions about what the world he is located in looks like. In other words, if his beliefs are confronted with a particular possible world w' , they will determine whether that world may or may not be the world as they think it is. What we are asking of George's mental state is whether any state of affairs, any event, anything in w' is in contradiction with anything that George believes. If not, then w' is compatible with George's beliefs. For all George believes, w' may well be the world where he lives. Many worlds will pass this criterion, just consider as one factor that George is unlikely to have any precise opinions about the number of leaves on the tree in front of my house. George's belief system determines a set of worlds compatible with his beliefs: those worlds that are viable candidates for being the actual world, as far as his belief system is concerned.

Now, George believes a proposition iff that proposition is true in all of the worlds compatible with his beliefs. If there is just one world compatible with his beliefs where the proposition is not true, that means that he considers it possible that the proposition is not true. In such a case, we can't say that he believes the proposition. Here is the same story in the words of [Hintikka \(1969\)](#), the source for this semantics for propositional attitudes:



Jaakko Hintikka

My basic assumption (slightly simplified) is that an attribution of any propositional attitude to the person in question involves a division of all the possible worlds (...) into two classes: into those possible worlds which are in accordance with the attitude in question and into those which are incompatible with it. The meaning of the division in the case of such attitudes as knowledge, belief, memory, perception, hope, wish, striving, desire, etc. is clear enough. For instance, if what we are speaking of are (say) a 's memories, then these possible worlds are all the possible worlds compatible with everything he remembers. [...]

How are these informal observations to be incorporated into a more explicit semantical theory? According to what I have said, understanding attributions of the propositional attitude in question (...) means being able to make a distinction between two kinds of possible worlds, according to whether they are compatible with the relevant attitudes of the person in question. The semantical counterpart to this is of course a function which to a given individual person assigns a set of possible worlds.

However, a minor complication is in order here. Of course, the person in question may himself have different attitudes in the different worlds we are considering. Hence this function in effect becomes a relation which to a given individual and to a given possible world μ associates a number of possible worlds which we shall call the *ALTERNATIVES* to μ . The relation will be called the *alternativeness* relation. (For different propositional attitudes, we have to consider different alternativeness relations.)

EXERCISE 3.1: Let's adopt Hintikka's idea that we can use a function that maps x and w into the set of worlds w' compatible with what x believes in w . Call this function \mathcal{B} . That is,

$$(2) \quad \mathcal{B} = \lambda x. \lambda w. \{w' : w' \text{ is compatible with what } x \text{ believes in } w\}.$$

Using this notation, our lexical entry for *believe* would look as follows:

$$(3) \quad \llbracket \text{believe} \rrbracket^{w,g} = \lambda p_{\langle s,t \rangle}. \lambda x. \mathcal{B}(x)(w) \subseteq p.$$

We are here indulging in the usual sloppiness in treating p both as a function from worlds to truth-values and as the set characterized by that function.

Here now are two “alternatives” for the semantics of *believe*:

$$(4) \quad \text{ATTEMPT 1 (VERY WRONG)}$$

$$\llbracket \text{believe} \rrbracket^{w,g} = \lambda p \in D_{\langle s,t \rangle}. [\lambda x \in D. p = \mathcal{B}(x)(w)].$$

$$(5) \quad \text{ATTEMPT 2 (ALSO VERY WRONG)}$$

$$\llbracket \text{believe} \rrbracket^{w,g} = \lambda p \in D_{\langle s,t \rangle}. [\lambda x \in D. p \cap \mathcal{B}(x)(w) \neq \emptyset].$$

Explain why these do not adequately capture the meaning of *believe*. \square

EXERCISE 3.2: Follow-up: The semantics in (5) would have made *believe* into an existential quantifier of sorts: it would say that *some* of the worlds compatible with what the subject believes are such-and-such. You have argued (successfully, of course) that such an analysis is wrong for *believe*. But *are* there attitude predicates with such an “existential” meaning? Discuss some candidates. If you can't find any candidates that survive scrutiny, can you speculate why there might be no existential attitude predicates? [Warning: this is underexplored territory!]

\square

\mathcal{BS} is meant to stand for ‘belief state’, not for what you might have thought!

We can also think of belief states as being represented by a function \mathcal{BS} , which maps an individual and a world into a set of propositions: those that the individual believes. From there, we could calculate the set of worlds compatible with an individual x ’s beliefs in world w by retrieving the set of those possible worlds in which all of the propositions in $\mathcal{BS}(x)(w)$ are true: $\{w' : \forall p \in \mathcal{BS}(x)(w) : p(w') = 1\}$, which in set talk is simply the big intersection of all the propositions in the set: $\cap \mathcal{BS}(x)(w)$. Our lexical entry then would be:

$$(6) \quad \llbracket \text{believe} \rrbracket^{w,g} = \lambda p_{\langle s,t \rangle} . \lambda x . \cap \mathcal{BS}(x)(w) \subseteq p.$$

EXERCISE 3.3: Imagine that our individual x forms a new opinion. Imagine that we model this by adding a new proposition p to the pool of opinions. So, $\mathcal{BS}(x)(w)$ now contains one further element. There are now more opinions. What happens to the set of worlds compatible with x ’s beliefs? Does it get bigger or smaller? Is the new set a subset or superset of the previous set of compatible worlds? \square

3.2 Accessibility Relations

Another way of reformulating Hintikka’s semantics for propositional attitudes is via the notion of an ACCESSIBILITY RELATION. We talk of a world w' being accessible from w . Each attitude can be associated with such an accessibility relation. For example, we can introduce the relation $w\mathcal{R}_\alpha^B w'$ which holds iff w' is compatible with α ’s belief state in w . We have then yet another equivalent way of specifying the lexical entry for *believe*:

$$(7) \quad \llbracket \text{believe} \rrbracket^{w,g} = \lambda p_{\langle s,t \rangle} . \lambda x . \forall w' : w\mathcal{R}_x^B w' \rightarrow p(w') = 1.$$

It is profitable to think of different attitudes (belief, knowledge, hope, regret, memory, ...) as corresponding to different accessibility relations. Recall now that the linguistic study of determiners benefitted quite a bit from an investigation of the formal properties of the relations between sets of individuals that determiners express. We can do the same thing here and ask about the formal properties of the accessibility relation associated with belief versus the one associated with knowledge, etc. The obvious properties to think about are reflexivity, transitivity, and symmetry.

3.2.1 Reflexivity

A relation is reflexive iff for any object in the domain of the relation we know that the relation holds between that object and itself. Which accessibility relations are reflexive? Take knowledge:

Kirill Shkolovsky (in class) asked why we call reflexivity, transitivity, and symmetry “formal” properties of relations. The idea is that certain properties are “formal” or “logical”, while others are more substantial. So, the fact that the relation “have the same birthday as” is symmetric seems a more formal fact about it than the fact that the relation holds between my daughter and my brother-in-law. Nevertheless, one of the most common ways of characterizing formal/logical notions (permutation-invariance, if you’re curious) does not in fact make symmetry etc. a formal/logical notion. So, while intuitively these do seem to be formal/logical properties, we do not know how to substantiate that intuition. See MacFarlane (2005) for discussion.

(8) $w\mathcal{R}_x^{\mathcal{K}}w'$ iff w' is compatible with what x knows in w .

We are asking whether for any given possible world w , we know that $\mathcal{R}_x^{\mathcal{K}}$ holds between w and w itself. It will hold if w is a world that is compatible with what we know in w . And clearly that must be so. Take our body of knowledge in w . The concept of knowledge crucially contains the concept of truth: what we know must be true. So if in w we know that something is the case then it must be the case in w . So, w must be compatible with all we know in w . $\mathcal{R}_x^{\mathcal{K}}$ is reflexive.

We talk here about knowledge entailing (or even presupposing) truth but we do not mean to say that knowledge simply equals true belief. Professors Socrates and Gettier and their exegetes have further considerations.

Now, if an attitude X corresponds to a reflexive accessibility relation, then we can conclude from a X s *that* p being true in w that p is true in w . This property of an attitude predicate is often called VERIDICALITY. It is to be distinguished from FACTIVITY, which is a property of attitudes which *presuppose* – rather than (merely) entail – the truth of their complement.

In modal logic notation: $\Box p \rightarrow p$. This pattern is sometimes called T or M, as is the corresponding system of modal logic.

If we consider the relation $\mathcal{R}_x^{\mathcal{B}}$ pairing with a world w those worlds w' which are compatible with what x *believes* in w , we no longer have reflexivity: belief is not a veridical attitude. It is easy to have false beliefs, which means that the actual world is not in fact compatible with one's beliefs, which contradicts reflexivity. And many other attitudes as well do not involve veridicality/reflexivity: what we hope may not come true, what we remember may not be what actually happened, etc.

The difference between *believe* and *know* in natural discourse is quite delicate, especially when one considers first person uses (*I believe the earth is flat* vs. *I know the earth is flat*).

In modal logic, the correspondence between formal properties of the accessibility relation and the validity of inference patterns is well-studied. What we have just seen is that reflexivity of the accessibility relation corresponds to the validity of $\Box p \rightarrow p$. Other properties correspond to other characteristic patterns. Let's see this for transitivity and symmetry.

3.2.2 *Transitivity

Transitivity of the accessibility relation corresponds to the inference $\Box p \rightarrow \Box \Box p$. The pattern seems not obviously wrong for knowledge: if one knows that p , doesn't one thereby know that one knows that p ? But before we comment on that, let's establish the formal correspondence between transitivity and that inference pattern. This needs to go in both directions.

What does it take for the pattern to be valid? Assume that $\Box p$ holds for an arbitrary world w , i.e. that p is true in all worlds w' accessible from w . Now, the inference is to the fact that p again holds in any world w'' accessible from any of those worlds w' accessible from w . But what would prevent p from being false in some w'' accessible from some w' accessible from w ? That could only be prevented from happening if we knew that w'' itself is accessible from w as well, because then we would know from the premiss that p is true in it (since p is true in *all* worlds accessible from w). Ah, but w'' (some world accessible from a world w' accessible from w) is only guaranteed to be accessible from

In the literature on epistemic modal logic, the pattern is known as the KK THESIS or POSITIVE INTROSPECTION. In general modal logic, it is the characteristic axiom 4 of the modal logic system S4, which is a system that adds 4 to the previous axiom M/T. Thus, S4 is the logic of accessibility relations that are both reflexive and transitive.

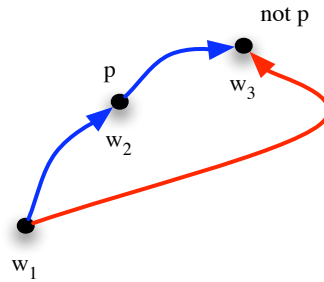


Figure 3.1: Transitivity

w if the accessibility relation is transitive (if w' is accessible from w and w'' is accessible from w' , then transitivity ensures that w'' is accessible from w). This reasoning has shown that validity of the pattern requires transitivity. The other half of proving the correspondence is to show that transitivity entails that the pattern is valid.

The proof proceeds by *reductio*. Assume that the accessibility relation is transitive. Assume that (i) $\Box p$ holds for some world w but that (ii) $\Box\Box p$ doesn't hold in w . We will show that this situation cannot obtain. By (i), p is true in all worlds w' accessible from w . By (ii), there is some non- p world w'' accessible from some world w' accessible from w . But by transitivity of the accessibility relation, that non- p world w'' must be accessible from w . And since *all* worlds accessible from w are p worlds, w'' must be a p world, in contradiction to (ii). So, as soon as we assume transitivity, there is no way for the inference not to go through.

Now, do any of the attitudes have the transitivity property? It seems rather obvious that as soon as you believe something, you thereby believe that you believe it (and so it seems that belief involves a transitive accessibility relation). And in fact, as soon as you believe something, you believe that you *know* it. But one might shy away from saying that knowing something automatically amounts to knowing that you know it. For example, many are attracted to the idea that to know something requires that (i) that it is true, (ii) that you believe it, and (iii) that you are justified in believing it: the justified true belief analysis of knowledge. So, now couldn't it be that you know something, and thus (?) that you believe you know it, and thus that you believe that you are justified in believing it, but that you are not justified in believing that you are *justified* in believing it? After all, one's source of knowledge, one's reliable means of acquiring knowledge, might be a mechanism that one has no insight into. So, while one can implicitly trust (believe) in its reliability, and while it is in fact reliable, one might not have any means to have trustworthy beliefs about it. [Further worries about the KK Thesis are discussed by [Williamson \(2000\)](#).]

3.2.3 *Symmetry

What would the consequences be if the accessibility relation were symmetric? Symmetry of the accessibility relation \mathcal{R} corresponds to the validity of the following principle:

(9) Brouwer's Axiom :

$$\forall p \forall w : w \in p \rightarrow \left[\forall w' [w \mathcal{R} w' \rightarrow \exists w'' [w' \mathcal{R} w'' \& w'' \in p]] \right]$$

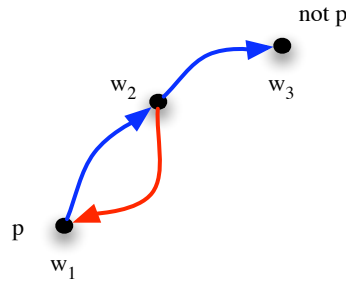


Figure 3.2: Symmetry

Here's the reasoning: Assume that \mathcal{R} is in fact symmetric. Pick a world w in which p is true. Now, could it be that the right hand side of the inference fails to hold in w ? Assume that it does fail. Then, there must be some world w' accessible from w in which $\Diamond p$ is false. In other words, from that world w' there is no accessible world w'' in which p is true. But since \mathcal{R} is assumed to be symmetric, one of the worlds accessible from w' is w and in w , p is true, which contradicts the assumption that the inference doesn't go through. So, symmetry ensures the validity of the inference.

The other way (validity of the inference requires symmetry): the inference says that from any p world we only have worlds accessible from which there is at least one accessible p world. But imagine that p is true in w but not true in any other world. So, the only way for the conclusion of the inference to hold automatically is to have a guarantee that w (the only p world) is accessible from any world accessible from it. That is, we need to have symmetry. QED.

To see whether a particular kind of attitude is based on a symmetric accessibility relation, we can ask whether Brouwer's Axiom is intuitively valid with respect to this attitude. If it is not valid, this shows that the accessibility relation can't be symmetric. In the case of a knowledge-based accessibility relation (epistemic accessibility), one can argue that *symmetry does not hold*:¹

The symmetry condition would imply that if something happens to be true in the actual world, then you know that it is compatible

In modal logic notation: $p \rightarrow \Box \Diamond p$, known simply as B in modal logic. The system that combines T/M with B is often called Brouwer's System (B), after the mathematician L.E.J. Brouwer, not because he proposed it but because it was thought that it had some connections to his doctrines.



L.E.J. Brouwer

¹ Thanks to Bob Stalnaker (pc to Kai von Fintel) for help with the following reasoning.

with your knowledge (Brouwer's Axiom). This will be violated by any case in which your beliefs are consistent, but mistaken. Suppose that while p is in fact true, you feel certain that it is false, and so think that you know that it is false. Since you think you know this, it is compatible with your knowledge that you know it. (Since we are assuming you are consistent, you can't both believe that you know it, and know that you do not). So it is compatible with your knowledge that you know that *not* p . Equivalently²: you don't know that you don't know that *not* p . Equivalently: you don't know that it's compatible with your knowledge that p . But by Brouwer's Axiom, since p is true, you would have to know that it's compatible with your knowledge that p . So if Brouwer's Axiom held, there would be a contradiction. So Brouwer's Axiom doesn't hold here, which shows that epistemic accessibility is not symmetric.

Game theorists and theoretical computer scientists who traffic in logics of knowledge often assume that the accessibility relation for knowledge is an equivalence relation (reflexive, symmetric, and transitive). But this is appropriate only if one abstracts away from any error, in effect assuming that belief and knowledge coincide. One striking consequence of working with an equivalence relation as the accessibility relation for knowledge is that one predicts the principle of NEGATIVE INTROSPECTION to hold:

- (IO) NEGATIVE INTROSPECTION (NI)
 If one doesn't know that p , then one knows that one doesn't know that p .
 $(\neg \Box p \rightarrow \Box \neg \Box p)$.

This surely seems rather dubious: imagine that one strongly believes that p but that nevertheless p is false, then one doesn't know that p , but one doesn't seem to believe that one doesn't know that p , in fact one believes that one does know that p .

3.3 Supplemental Readings

A recent survey on attitudes:

Eric Swanson. 2011. Propositional attitudes. In Klaus von Heusinger, Claudia Maienborn & Paul Portner (eds.), *Semantics: An international handbook of meaning*, vol. 2 (Handbücher zur Sprach- und Kommunikationswissenschaft 33.2), chap. 60, 1538–1561. Berlin/Boston: de Gruyter Mouton. <http://dx.doi.org/10.1515/9783110255072.1538>. <http://tinyurl.com/swanson-hsk>.

² This and the following step rely on the duality of necessity and possibility: q is compatible with your knowledge iff you don't know that *not* q .

All one really needs to make NI valid is to have a EUCLIDEAN accessibility relation: any two worlds accessible from the same world are accessible from each other. It is a nice little exercise to prove this, if you have become interested in this sort of thing. Note that all reflexive and Euclidean accessibility relations are transitive and symmetric as well — another nice little thing to prove.

Further connections between mathematical properties of accessibility relations and logical properties of various notions of necessity and possibility are studied extensively in modal logic:

G.E. Hughes & Max Cresswell. 1996. *A new introduction to modal logic*. London: Routledge.

James Garson. 2008. Modal logic. In Edward N. Zalta (ed.), *The Stanford encyclopedia of philosophy*. <http://plato.stanford.edu/entries/logic-modal/>, especially section 7 and 8, “Modal Axioms and Conditions on Frames”, “Map of the Relationships between Modal Logics”.

A thorough discussion of the possible worlds theory of attitudes, and some of its potential shortcomings, can be found in Bob Stalnaker’s work:

Robert Stalnaker. 1984. *Inquiry*. MIT Press.

Robert Stalnaker. 1999. *Context and content*. Oxford: Oxford University Press.

A quick and informative surveys about the notion of knowledge:

Matthias Steup. 2008. The analysis of knowledge. In Edward N. Zalta (ed.), *The Stanford encyclopedia of philosophy*, Fall 2008. <http://plato.stanford.edu/archives/fall2008/entries/knowledge-analysis/>.

Linguistic work on attitudes has often been concerned with various co-occurrence patterns, particularly which moods (indicative or subjunctive or infinitive) occur in the complement and whether negative polarity items are licensed in the complement.

Mood licensing:

Paul Portner. 1997. The semantics of mood, complementation, and conversational force. *Natural Language Semantics* 5(2). 167–212. <http://dx.doi.org/10.1023/A:1008280630142>.

NPI-Licensing:

Nirit Kadmon & Fred Landman. 1993. *Any*. *Linguistics and Philosophy* 16(4). 353–422. <http://dx.doi.org/10.1007/BF00985272>.

Kai von Stechow. 1999. NPI licensing, Strawson entailment, and context dependency. *Journal of Semantics* 16(2). 97–148. <http://dx.doi.org/10.1093/jos/16.2.97>.

Anastasia Giannakidou. 1999. Affective dependencies. *Linguistics and Philosophy* 22(4). 367–421. <http://dx.doi.org/10.1023/A:1005492130684>.

There is some interesting work out of Amherst rethinking the way attitude predicates take their complements:

Angelika Kratzer. 2006. Decomposing attitude verbs. Handout from a talk honoring Anita Mittwoch on her 80th birthday at the Hebrew University of Jerusalem July 4, 2006. <http://semanticsarchive.net/Archive/DcwY2JkM/attitude-verbs2006.pdf>.

Keir Moulton. 2008. Clausal complementation and the *Wager*-class. *North East Linguistics Society (NELS)* 38. <http://sites.google.com/site/keirmoulton/Moultonnels2008wager.pdf>. <http://people.umass.edu/keir/Wager.pdf>.

Keir Moulton. 2009. *Natural selection and the syntax of clausal complementation*. University of Massachusetts at Amherst dissertation. http://scholarworks.umass.edu/open_access_dissertations/99/.

Tamina Stephenson in her MIT dissertation and related work explores the way attitude predicates interact with epistemic modals and taste predicates in their complements:

Tamina Stephenson. 2007a. Judge dependence, epistemic modals, and predicates of personal taste. *Linguistics and Philosophy* 30(4). 487–525. <http://dx.doi.org/10.1007/s10988-008-9023-4>.

Tamina Stephenson. 2007b. *Towards a theory of subjective meaning*. Massachusetts Institute of Technology dissertation. <http://semanticsarchive.net/Archive/2QxMjkoO/Stephenson-2007-thesis.pdf>.

Jon Gajewski in his MIT dissertation and subsequent work explores the distribution of the NEG-RAISING property among attitude predicates and traces it back to presuppositional components of the meaning of the predicates:

Jon Gajewski. 2005. *Neg-raising: Polarity and presupposition*. Massachusetts Institute of Technology dissertation. <http://dx.doi.org/10.1007/s10988-007-9020-z>.

Jon Gajewski. 2007. Neg-raising and polarity. *Linguistics and Philosophy*. <http://dx.doi.org/10.1007/s10988-007-9020-z>.

Interesting work has also been done on presupposition projection in attitude contexts:

Nicholas Asher. 1987. A typology for attitude verbs and their anaphoric properties. *Linguistics and Philosophy* 10(2). 125–197. <http://dx.doi.org/10.1007/BF00584317>.

Irene Heim. 1992. Presupposition projection and the semantics of attitude verbs. *Journal of Semantics* 9(3). 183–221. <http://dx.doi.org/10.1093/jos/9.3.183>.

Bart Geurts. 1998. Presuppositions and anaphors in attitude contexts. *Linguistics and Philosophy* 21(6). 545–601. <http://dx.doi.org/10.1023/A:1005481821597>.

CHAPTER FOUR

MODALITY

We turn to modal auxiliaries and related constructions. We see more context-dependency. We still quantify over possible worlds.

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4.1 The Quantificational Theory of Modality

We will now be looking at modal auxiliaries like *may*, *must*, *can*, *have to*, etc. Most of what we say here should carry over straightforwardly to modal adverbs like *maybe*, *possibly*, *certainly*, etc. We will make certain syntactic assumptions, which make our work easier but which leave aside many questions that at some point deserve to be addressed.

4.1.1 Syntactic Assumptions

We will assume, at least for the time being, that a modal like *may* is a RAISING predicate (rather than a CONTROL predicate), i.e., its subject is not its own argument, but has been moved from the subject-position of its infinitival complement. So, we are dealing with the following kind of structure:

- (1) a. Ann may be smart.
 b. [Ann [λ_t [may [t_t be smart]]]]

Actually, we will be working here with the even simpler structure below, in which the subject has been reconstructed to its lowest trace position. (E.g., these could be generated by deleting all but the lowest copy in the movement chain.) We will be able to prove that movement of a name or pronoun never affects truth-conditions, so at any rate the interpretation of the structure in (1b) would be the same as that of (2). As a matter of convenience, then, we will take the reconstructed structures, which allow us to abstract away from the (here irrelevant) mechanics of variable binding.

- (2) may [Ann be smart]

So, for now at least, we are assuming that modals are expressions that take a full sentence as their semantic argument.¹ Now then, what do modals mean?

4.1.2 Quantification over Possible Worlds

The basic idea of the possible worlds semantics for modal expressions is that they are quantifiers over possible worlds. Toy lexical entries for *must* and *may*, for example, would look like this:

- (3) $\llbracket \text{must} \rrbracket^{w,g} = \lambda p_{\langle s,t \rangle}. \forall w': p(w') = 1.$
 (4) $\llbracket \text{may} \rrbracket^{w,g} = \lambda p_{\langle s,t \rangle}. \exists w': p(w') = 1.$

This analysis is too crude (in particular, notice that it would make modal sentences non-contingent — there is no occurrence of the evaluation world on the right hand side!). But it does already have some desirable consequences that we will seek to preserve through all subsequent refinements. It correctly predicts a number of intuitive judgments about the logical relations between *must* and *may* and among various combinations of these items and negations. To start with some elementary facts, we feel that *must* ϕ entails *may* ϕ , but not vice versa:

¹ We will assume that even though *Ann be smart* is a non-finite sentence, this will not have any effect on its semantic type, which is that of a sentence, which in turn means that its semantic value is a truth-value. This is hopefully independent of the (interesting) fact that *Ann be smart* on its own cannot be used to make a truth-evaluable assertion.

The issue of raising vs. control will probably be taken up later. If you are eager to get started on it and other questions of the morphosyntax of modals, read the handout from an LSA class Sabine and Kai taught a few years ago: <http://web.mit.edu/fintel/lsa220-class-2-handout.pdf>.

We will talk about reconstruction in more detail later.

This idea goes back a long time. It was famously held by Leibniz, but there are precedents in the medieval literature; see Knuuttila (2015). See Copeland (2002) for the modern history of the possible worlds analysis of modal expressions.

(5) You must stay.
Therefore, you may stay. VALID

(6) You may stay.
Therefore, you must stay. INVALID

(7) a. You may stay, but it is not the case that you must stay.²
b. You may stay, but you don't have to stay. CONSISTENT

We judge *must* ϕ incompatible with its "inner negation" *must* [*not* ϕ], but find *may* ϕ and *may* [*not* ϕ] entirely compatible:

(8) You must stay, and/but also, you must leave. (leave = not stay).
CONTRADICTORY

(9) You may stay, but also, you may leave.
CONSISTENT

We also judge that in each pair below, the (a)-sentence and the (b)-sentences say the same thing.

(10) a. You must stay.
b. It is not the case that you may leave.
You aren't allowed to leave.
(You may not leave.)³
(You can't leave.)

(11) a. You may stay.
b. It is not the case that you must leave.
You don't have to leave.
You don't need to leave.
(You needn't leave.)

² The somewhat stilted *it is not the case*-construction is used in (a) to make certain that negation takes scope over *must*. When modal auxiliaries and negation are together in the auxiliary complex of the same clause, their relative scope seems not to be transparently encoded in the surface order; specifically, the scope order is not reliably negation \succ modal. (Think about examples with *mustn't*, *can't*, *shouldn't*, *may not* etc. What's going on here? This is an interesting topic which we must set aside for now. See the references at the end of the chapter for relevant work.) With modal *main* verbs (such as *have to*), this complication doesn't arise; they are consistently inside the scope of clause-mate auxiliary negation. Therefore we can use (b) to (unambiguously) express the same scope order as (a), without having to resort to a biclausal structure.

³ The parenthesized variants of the (b)-sentences are pertinent here only to the extent that we can be certain that negation scopes over the modal. In these examples, apparently it does, but as we remarked above, this cannot be taken for granted in all structures of this form.

Given that *stay* and *leave* are each other's negations (i.e. $\llbracket \text{leave} \rrbracket^{w,g} = \llbracket \text{not stay} \rrbracket^{w,g}$, and $\llbracket \text{stay} \rrbracket^{w,g} = \llbracket \text{not leave} \rrbracket^{w,g}$), the LF-structures of these equivalent pairs of sentences can be seen to instantiate the following schemata:⁴

- (I2) a. $\text{must } \phi \equiv \text{not } [\text{may } [\text{not } \phi]]$
 b. $\text{must } [\text{not } \psi] \equiv \text{not } [\text{may } \psi]$
- (I3) a. $\text{may } \phi \equiv \text{not } [\text{must } [\text{not } \phi]]$
 b. $\text{may } [\text{not } \psi] \equiv \text{not } [\text{must } \psi]$

Our present analysis of *must*, *have-to*, ... as universal quantifiers and of *may*, *can*, ... as existential quantifiers straightforwardly predicts all of the above judgments, as you can easily prove.

- (I4) a. $\forall x \phi \equiv \neg \exists x \neg \phi$
 b. $\forall x \neg \phi \equiv \neg \exists x \phi$
- (I5) a. $\exists x \phi \equiv \neg \forall x \neg \phi$
 b. $\exists x \neg \phi \equiv \neg \forall x \phi$

More linguistic data regarding the “parallel logic” of modals and quantifiers can be found in Larry Horn’s dissertation (Horn 1972).

4.2 Flavors of Modality

4.2.1 Contingency

We already said that the semantics we started with is too simple-minded. In particular, we have no dependency on the evaluation world, which would make modal statements non-contingent. This is not correct.

If one says *It may be snowing in Cambridge*, that may well be part of useful, practical advice about what to wear on your upcoming trip to Cambridge. It may be true or it may be false. The sentence seems true if said in the dead of winter when we have already heard about a Nor’Easter that is sweeping across New England. The sentence seems false if said by a clueless Australian acquaintance of ours in July.

The contingency of modal claims is not captured by our current semantics. All the *may*-sentence would claim under that semantics is that there is some possible world where it is snowing in Cambridge. And surely, once you have read Lewis’ quote in Chapter 1, where he asserts the existence of possible worlds with different physical constants than we enjoy here, you must admit that there have to be such worlds even if it is July. The problem is that in our semantics, repeated here

4 In logicians’ jargon, *must* and *may* behave as DUALS of each other. For definitions of “dual”, see Barwise & Cooper (1981: 197) or Gamut (1991: vol.2,238).

$$(16) \quad \llbracket \text{may} \rrbracket^{w,g} = \lambda p_{\langle s,t \rangle}. \exists w': p(w') = 1.$$

there is no occurrence of w on the right hand side. This means that the truth-conditions for *may*-sentences are world-independent. In other words, they make non-contingent claims that are either true whatever or false whatever, and because of the plenitude of possible worlds they are more likely to be true than false. This needs to be fixed. But how?

Conversely, the plenitude of possible worlds would make *must*-claims very likely false if they are not reigned in or anchored somehow.

Well, what makes *it may be snowing in Cambridge* seem true when we know about a Nor'Easter over New England? What makes it seem false when we know that it is summer in New England? The idea is that we only consider possible worlds COMPATIBLE WITH THE EVIDENCE AVAILABLE TO US. And since what evidence is available to us differs from world to world, so will the truth of a *may*-statement.

$$(17) \quad \llbracket \text{may} \rrbracket^{w,g} = \lambda p. \exists w' \text{ compatible with the evidence in } w: p(w') = 1.^5$$

$$(18) \quad \llbracket \text{must} \rrbracket^{w,g} = \lambda p. \forall w' \text{ compatible with the evidence in } w: p(w') = 1.$$

Let us consider a different example:

$$(19) \quad \text{You have to be quiet.}$$

Imagine this sentence being said based on the house rules of the particular dormitory you live in. Again, this is a sentence that could be true or could be false. Why do we feel that this is a contingent assertion? Well, the house rules can be different from one world to the next, and so we might be unsure or mistaken about what they are. In one possible world, they say that all noise must stop at 11pm, in another world they say that all noise must stop at 10pm. Suppose we know that it is 10:30 now, and that the dorm we are in has either one or the other of these two rules, but we have forgotten which. Then, for all we know, *you have to be quiet* may be true or it may be false. This suggests a lexical entry along these lines:

$$(20) \quad \llbracket \text{have-to} \rrbracket^{w,g} = \lambda p. \forall w' \text{ compatible with the rules in } w: p(w') = 1.$$

Again, we are tying the modal statement about other worlds down to certain worlds that stand in a certain relation to actual world: those worlds where the rules as they are here are obeyed.

A note of caution: it is very important to realize that the worlds compatible with the rules as they are in w are those worlds where nothing happens that violates any of the w -rules. This is not at all the same as saying that the worlds compatible with the rules in w are those worlds where the same rules are in force. Usually, the rules do not care what the rules are, unless the rules contain

⁵ From now on, we will leave off type-specifications such as that p has to be of type $\langle s, t \rangle$, whenever it is obvious what they should be and when saving space is aesthetically called for.

some kind of meta-statement to the effect that the rules have to be the way they are, i.e. that the rules cannot be changed. So, in fact, a world w' in which nothing happens that violates the rules as they are in w but where the rules are quite different and in fact what happens violates the rules as they are in w' is nevertheless a world compatible with the rules in w . For example, imagine that the only relevant rule in w is that students go to bed before midnight. Take a world w' where a particular student goes to bed at 11:30 pm but where the rules are different and say that students have to go to bed before 11 pm. Such a world w' is compatible with the rules in w (but of course not with the rules in w').

Apparently, there are different flavors of modality, varying in what kind of facts in the evaluation world they are sensitive to. The semantics we gave for *must* and *may* above makes them talk about evidence, while the semantics we gave for *have-to* made it talk about rules. But that was just because the examples were hand-picked. In fact, in the dorm scenario we could just as well have said *You must be quiet*. And, vice versa, there is nothing wrong with using *it has to be snowing in Cambridge* based on the evidence we have. In fact, many modal expressions seem to be multiply ambiguous.

Traditional descriptions of modals often distinguish a number of “readings”: EPISTEMIC, DEONTIC, ABILITY, CIRCUMSTANTIAL, DYNAMIC, . . . (Beyond “epistemic” and “deontic,” there is a great deal of terminological variety. Sometimes all non-epistemic readings are grouped together under the term ROOT MODALITY.) Here are some initial illustrations.

(21) EPISTEMIC MODALITY

A: Where is John?
B: I don't know. He *may* be at home.

(22) DEONTIC MODALITY

A: Am I allowed to stay over at Janet's house?
B: No, but you *may* bring her here for dinner.

(23) CIRCUMSTANTIAL/DYNAMIC MODALITY

A: I will plant the rhododendron here.
B: That's not a good idea. It *can* grow very tall.

How are *may* and *can* interpreted in each of these examples? What do the interpretations have in common, and where do they differ?

In all three examples, the modal makes an existentially quantified claim about possible worlds. This is usually called the MODAL FORCE of the claim. What differs is what worlds are quantified over. In EPISTEMIC modal sentences, we quantify over worlds compatible with the available evidence. In DEONTIC modal sentences, we quantify over worlds compatible with the rules and/or regulations.

And in the CIRCUMSTANTIAL modal sentence, we quantify over the set of worlds which conform to the laws of nature (in particular, plant biology). What speaker B in (23) is saying, then, is that there are some worlds conforming to the laws of nature in which this rhododendron grows very tall. (Or is this another instance of an epistemic reading? See below for discussion of the distinction between circumstantial readings and epistemic ones.)

How can we account for this variety of readings? One way would be to write a host of lexical entries, basically treating this as a kind of (more or less principled) ambiguity. Another way, which is preferred by many people, is to treat this as a case of context-dependency, as argued in seminal work by Kratzer (1977, 1978, 1981, 1991).

According to Kratzer, what a modal brings with it intrinsically is just a modal force, that is, whether it is an existential (possibility) modal or a universal (necessity) modal. What worlds it quantifies over is determined by context. In essence, the context has to supply a restriction to the quantifier. How can we implement this idea?

We encountered context-dependency before when we talked about pronouns and their referential (and E-Type) readings (H&K, chapters 9–11). We treated referential pronouns as free variables, appealing to a general principle that free variables in an LF need to be supplied with values from the utterance context. If we want to describe the context-dependency of modals in a technically analogous fashion, we can think of their LF-representations as incorporating or subcategorizing for a kind of invisible pronoun, a free variable that stands for a set of possible worlds. So we posit LF-structures like this:

$$(24) \quad [I' [I \text{ must } p_{\langle n, \langle s, t \rangle \rangle}] [VP \text{ you quiet}]]$$

$p_{\langle n, \langle s, t \rangle \rangle}$ here is a variable over (characteristic functions of) sets of worlds, which — like all free variables — needs to receive a value from the utterance context. Possible values include: the set of worlds compatible with the speaker's current knowledge; the set of worlds in which everyone obeys all the house rules of a certain dormitory; and many others. The denotation of the modal itself now has to be of type $\langle st, \langle st, t \rangle \rangle$ rather than $\langle st, t \rangle$, thus it will be more like a quantificational determiner rather than a complete generalized quantifier. Only after the modal has been combined with its covert restrictor do we obtain a value of type $\langle st, t \rangle$.

$$(25) \quad \begin{aligned} \text{a. } & \llbracket \text{must} \rrbracket^{w,g} = \llbracket \text{have-to} \rrbracket^{w,g} = \llbracket \text{need-to} \rrbracket^{w,g} = \dots = \\ & \lambda p \in D_{\langle s, t \rangle}. \lambda q \in D_{\langle s, t \rangle}. \forall w \in W [p(w) = 1 \rightarrow q(w) = 1] \\ \text{b. } & \llbracket \text{may} \rrbracket^{w,g} = \llbracket \text{can} \rrbracket^{w,g} = \llbracket \text{be-allowed-to} \rrbracket^{w,g} = \dots = \\ & \lambda p \in D_{\langle s, t \rangle}. \lambda q \in D_{\langle s, t \rangle}. \exists w \in W [p(w) = 1 \ \& \ q(w) = 1] \end{aligned}$$

On this approach, the epistemic, deontic, etc. “readings” of individual occurrences of modal verbs come about by a combination of two separate things.



Angelika Kratzer

It is well-known that natural language quantification is in general subject to contextual restriction. See Stanley & Szabó (2000) for a recent discussion.

Warning: This account is problematic and will be refined soon.

We are using the notation for variables of types other than e introduced by Heim & Kratzer.

See p. 213. An index on a variable now is an ordered pair of a natural number and a type.

Q: Can you think of overt anaphoric expressions that are arguably of the type $\langle s, t \rangle$, a proposition?

in set talk: $p \subseteq q$

in set talk: $p \cap q \neq \emptyset$

The lexical semantics of the modal itself encodes just a quantificational force, a *relation* between sets of worlds. This is either the subset-relation (universal quantification; necessity) or the relation of non-disjointness (existential quantification; possibility). The covert variable next to the modal picks up a contextually salient set of worlds, and this functions as the quantifier's restrictor. The labels "epistemic", "deontic", "circumstantial" etc. group together certain conceptually natural classes of possible values for this covert restrictor.

Notice that, strictly speaking, there is not just one deontic reading (for example), but many. A speaker who utters

(26) You have to be quiet.

might mean: 'I want you to be quiet,' (i.e., you are quiet in all those worlds that conform to my preferences). Or she might mean: 'unless you are quiet, you won't succeed in what you are trying to do,' (i.e., you are quiet in all those worlds in which you succeed at your current task). Or she might mean: 'the house rules of this dormitory here demand that you be quiet,' (i.e., you are quiet in all those worlds in which the house rules aren't violated). And so on. So the label "deontic" appears to cover a whole open-ended set of imaginable "readings", and which one is intended and understood on a particular utterance occasion may depend on all sorts of things in the interlocutors' previous conversation and tacit shared assumptions. (And the same goes for the other traditional labels.)

4.2.2 Epistemic vs. Circumstantial Modality

Is it all context-dependency? Or do flavors of modality correspond to some sorts of signals in the structure of sentences? Read the following famous passage from Kratzer and think about how the two sentences with their very different modal meanings differ in structure:

Quoted from Kratzer (1991). In Kratzer (1981), the hydrangeas were *Zwetschenbäume* 'plum trees'. The German word *Zwetschge*, by the way, is etymologically derived from the name of the city Damascus (Syria), the center of the ancient plum trade.

Consider sentences (27) and (28):

- (27) Hydrangeas can grow here.
- (28) There might be hydrangeas growing here.

The two sentences differ in meaning in a way which is illustrated by the following scenario.

"Hydrangeas"

Suppose I acquire a piece of land in a far away country and discover that soil and climate are very much like at home, where hydrangeas prosper everywhere. Since hydrangeas are my favorite plants, I wonder whether they would grow in this place and inquire about it. The answer is (27). In such a situation, the proposition expressed by (27) is true. It is true regardless of whether it is or

isn't likely that there are already hydrangeas in the country we are considering. All that matters is climate, soil, the special properties of hydrangeas, and the like. Suppose now that the country we are in has never had any contacts whatsoever with Asia or America, and the vegetation is altogether different from ours. Given this evidence, my utterance of (28) would express a false proposition. What counts here is the complete evidence available. And this evidence is not compatible with the existence of hydrangeas.

(27) together with our scenario illustrates the pure CIRCUMSTANTIAL reading of the modal *can*. [...]. (28) together with our scenario illustrates the epistemic reading of modals. [...] circumstantial and epistemic conversational backgrounds involve different kinds of facts. In using an epistemic modal, we are interested in what else may or must be the case in our world given all the evidence available. Using a circumstantial modal, we are interested in the necessities implied by or the possibilities opened up by certain sorts of facts. Epistemic modality is the modality of curious people like historians, detectives, and futurologists. Circumstantial modality is the modality of rational agents like gardeners, architects, and engineers. A historian asks what might have been the case, given all the available facts. An engineer asks what can be done given certain relevant facts.

Consider also the very different prominent meanings of the following two sentences, taken from Kratzer as well:

- (29) a. Cathy can make a pound of cheese out of this can of milk.
b. Cathy might make a pound of cheese out of this can of milk.

EXERCISE 4.1: Come up with examples of epistemic, deontic, and circumstantial uses of the necessity verb *have to*. Describe the set of worlds that constitutes the understood restrictor in each of your examples. □

4.2.3 Contingency Again

We messed up. If you inspect the context-dependent meanings we have on the table now for our modals, you will see that the right hand sides again do not mention the evaluation world *w*. Therefore, we will again have the problem of not making contingent claims, indirectly about the actual world. This needs to be fixed. We need a semantics that is both context-dependent and contingent.

The problem, it turns out, is with the idea that the utterance context supplies a *determinate set of worlds* as the restrictor. When I understand that you meant your use of *must*, in *you must be quiet*, to quantify over the set of worlds in which the house rules of our dorm are obeyed, this does not imply that you and I have

to know or agree on which set exactly this is. That depends on what the house rules in our world actually happen to say, and this may be an open question at the current stage of our conversation. What we do agree on, if I have understood your use of *must* in the way that you intended it, is just that it quantifies over *whatever set of worlds it may be* that the house rules pick out.

The technical implementation of this insight requires that we think of the context's contribution not as a set of worlds, but rather as a function which for each world it applies to picks out such a set. For example, it may be the function which, for any world w , yields the set $\{w' : \text{the house rules that are in force in } w \text{ are obeyed in } w'\}$. If we apply this function to a world w_1 , in which the house rules read “no noise after 10 pm”, it will yield a set of worlds in which nobody makes noise after 10 pm. If we apply the same function to a world w_2 , in which the house rules read “no noise after 11 pm”, it will yield a set of worlds in which nobody makes noise after 11 pm.

Suppose, then, that the covert restrictor of a modal predicate denotes such a function, i.e., its value is of type $\langle s, st \rangle$.

(30) [I' [I must $R_{\langle n, \langle s, st \rangle \rangle}$] [VP you quiet]]

And the new lexical entries for *must* and *may* that will fit this new structure are these:

- (31) a. $\llbracket \text{must} \rrbracket^{w,g} = \llbracket \text{have-to} \rrbracket^{w,g} = \llbracket \text{need-to} \rrbracket^{w,g} = \dots =$
 $\lambda R \in D_{\langle s, st \rangle} \cdot \lambda q \in D_{\langle s, t \rangle} \cdot \forall w' \in W [R(w)(w') = 1 \rightarrow q(w') = 1]$
 b. $\llbracket \text{may} \rrbracket^{w,g} = \llbracket \text{can} \rrbracket^{w,g} = \llbracket \text{be-allowed-to} \rrbracket^{w,g} = \dots =$
 $\lambda R \in D_{\langle s, st \rangle} \cdot \lambda q \in D_{\langle s, t \rangle} \cdot \exists w' \in W [R(w)(w') = 1 \ \& \ q(w') = 1]$

in set talk: $R(w) \subseteq q$

in set talk: $R(w) \cap q \neq \emptyset$

Let us see now how this solves the contingency problem.

- (32) Let w be a world, and assume that the context supplies an assignment g such that $g(R_{\langle 17, \langle s, st \rangle \rangle}) = \lambda w. \lambda w'$. the house rules in force in w are obeyed in w'

$$\begin{aligned}
 & \llbracket \text{must } R_{\langle 17, \langle s, st \rangle \rangle} \text{ you quiet} \rrbracket^{w,g} = & (\text{IFA}) \\
 & \llbracket \text{must } R_{\langle 17, \langle s, st \rangle \rangle} \rrbracket^{w,g} (\lambda w' \llbracket \text{you quiet} \rrbracket^{w'}) = & (\text{FA}) \\
 & \llbracket \text{must} \rrbracket^{w,g} (\llbracket R_{\langle 17, \langle s, st \rangle \rangle} \rrbracket^{w,g} (\lambda w' \llbracket \text{you quiet} \rrbracket^{w'})) = & (\text{lex. entries } \textit{you}, \textit{quiet}) \\
 & \llbracket \text{must} \rrbracket^{w,g} (\llbracket R_{\langle 17, \langle s, st \rangle \rangle} \rrbracket^{w,g} (\lambda w'. \text{you are quiet in } w')) = & (\text{lex. entry } \textit{must}) \\
 & \forall w' \in W: \llbracket R_{\langle 17, \langle s, st \rangle \rangle} \rrbracket^{w,g}(w)(w') = 1 \rightarrow \text{you are quiet in } w' = & (\text{pronoun rule}) \\
 & \forall w' \in W: g(R_{\langle 17, \langle s, st \rangle \rangle})(w)(w') = 1 \rightarrow \text{you are quiet in } w' = & (\text{def. of } g) \\
 & \forall w' \in W [\text{the house rules in force in } w \text{ are obeyed in } w' & \\
 & \quad \rightarrow \text{you are quiet in } w']
 \end{aligned}$$

As we see in the last line of (32), the truth-value of 30 depends on the evaluation world w .

EXERCISE 4.2: Describe two worlds w_1 and w_2 so that

$\llbracket \text{must } R_{\langle 17, \langle s, st \rangle \rangle} \text{ you quiet} \rrbracket^{w_1, g} = 1$ and $\llbracket \text{must } R_{\langle 17, \langle s, st \rangle \rangle} \text{ you quiet} \rrbracket^{w_2, g} = 0$. \square

EXERCISE 4.3: In analogy to the deontic relation $g(R_{\langle 17, \langle s, st \rangle \rangle})$ defined in (32), define an appropriate relation that yields an epistemic reading for a sentence like *You may be quiet*. \square

4.2.4 Iteration

Consider the following example:

(33) You might have to leave.

What does this mean? Under one natural interpretation, we learn that the speaker considers it possible that the addressee is under the obligation to leave. This seems to involve one modal embedded under a higher modal. It appears that this sentence should be true in a world w iff some world w' compatible with what the speaker knows in w is such that every world w'' in which the rules as they are in w' are followed is such that you leave in w'' .

Assume the following LF:

(34) $[I' [\text{might } R_{\langle 1, \langle s, st \rangle \rangle}] [VP [\text{have-to } R_{\langle 2, \langle s, st \rangle \rangle}] [IP \text{ you leave}]]]$

Suppose w is the world for which we calculate the truth-value of the whole sentence, and the context maps R_1 to the function which maps w to the set of all those worlds compatible with what is known in w . *might* says that some of those worlds are worlds w' that make the tree below *might* true. Now assume further that the context maps R_2 to the function which assigns to any such world w' the set of all those worlds in which the rules as they are in w' are followed. *have to* says that all of those worlds are worlds w'' in which you leave.

In other words, while it is not known to be the case that you have to leave, for all the speaker knows it might be the case.

EXERCISE 4.4: Describe values for the covert $\langle s, st \rangle$ -variable that are intuitively suitable for the interpretation of the modals in the following sentences:

(35) As far as John's preferences are concerned, you *may* stay with us.

(36) According to the guidelines of the graduate school, every PhD candidate *must* take 9 credit hours outside his/her department.

(37) John *can* run a mile in 5 minutes.

(38) This *has* to be the White House.

There is more to be said about which modals can embed under which other modals. See for some discussion the handout mentioned earlier: <http://web.mit.edu/fintel/lsa220-class-2-handout.pdf>.

From now on, we will omit the type-designation of variables whenever we feel confident that their type is easy to figure out from the context.

- (39) This elevator *can* carry up to 3000 pounds.

For some of the sentences, different interpretations are conceivable depending on the circumstances in which they are uttered. You may therefore have to sketch the utterance context you have in mind before describing the accessibility relation. □

EXERCISE 4.5: Collect two naturally occurring examples of modalized sentences (e.g., sentences that you overhear in conversation, or read in a newspaper or novel – not ones that are being used as examples in a linguistics or philosophy paper!), and give definitions of values for the covert $\langle s, st \rangle$ -variable which account for the way in which you actually understood these sentences when you encountered them. (If the appropriate interpretation is not salient for the sentence out of context, include information about the relevant preceding text or non-linguistic background.) □

4.3 Supplemental Readings

The most important background readings for this chapter are the following two papers by Kratzer:

Angelika Kratzer. 1981. The notional category of modality. In Hans-Jürgen Eikmeyer & Hannes Rieser (eds.), *Words, worlds, and contexts: New approaches in word semantics* (Research in Text Theory 6), 38–74. Berlin: de Gruyter.

Angelika Kratzer. 1991. Modality. In Arnim von Stechow & Dieter Wunderlich (eds.), *Semantics: An international handbook of contemporary research*, 639–650. Berlin: de Gruyter. <https://udrive.oit.umass.edu/kratzer/kratzer-modality.pdf>.

There are updated versions of Kratzer's classic papers in her volume "Modals and conditionals" (<https://doi.org/10.1093/acprof:oso/9780199234684.001.0001>).

A major new resource on modality is Paul Portner's book:

Paul Portner. 2009. *Modality*. Oxford University Press.

You might also profit from other survey-ish type papers:

Kai von Fintel. 2005. Modality and language. In Donald M. Borchert (ed.), *Encyclopedia of philosophy – second edition*. MacMillan. <http://mit.edu/fintel/fintel-2005-modality.pdf>.

Kai von Fintel & Anthony S. Gillies. 2007. An opinionated guide to epistemic modality. In Tamar Szabó Gendler & John Hawthorne (eds.), *Oxford studies in epistemology: Volume 2*, 32–62. Oxford University Press. <http://mit.edu/fintel/fintel-gillies-2007-ose2.pdf>.

Eric Swanson. 2008. Modality in language. *Philosophy Compass* 3(6). 1193–1207. <http://dx.doi.org/10.1111/j.1747-9991.2008.00177.x>.

Valentine Hacquard. 2009. Modality. ms, prepared for *Semantics: An international handbook of meaning*, edited by Klaus von Heusinger, Claudia Maienborn, and Paul Portner. http://ling.umd.edu/~hacquard/papers/HoS_Modality_Hacquard.pdf.

On the syntax of modals, there are only a few papers of uneven quality. Some of the more recent work is listed here. Follow up on older references from the bibliographies in these papers.

Rajesh Bhatt. 1997. Obligation and possession. In Heidi Harley (ed.), *Papers from the UPenn/MIT Roundtable on Argument Structure and Aspect* (MIT Working Papers in Linguistics 32), 21–40. <http://people.umass.edu/bhatt/papers/bhatt-haveto.pdf>.

Susi Wurmbrand. 1999. Modal verbs must be raising verbs. *West Coast Conference on Formal Linguistics (WCCFL)* 18. 599–612. <http://citeseerx.ist.psu.edu/viewdoc/download?doi=10.1.1.35.7442&rep=rep1&type=pdf>.

Annabel Cormack & Neil Smith. 2002. Modals and negation in English. In Sjef Barbiers, Frits Beukema & Wim van der Wurff (eds.), *Modality and its interaction with the verbal system*, 133–163. Benjamins.

Jonny Butler. 2003. A minimalist treatment of modality. *Lingua* 113(10). 967–996. [http://dx.doi.org/10.1016/S0024-3841\(02\)00146-8](http://dx.doi.org/10.1016/S0024-3841(02)00146-8).

The following paper explores some issues in the LF-syntax of epistemic modals:

Kai von Stechow & Sabine Iatridou. 2003. Epistemic containment. *Linguistic Inquiry* 34(2). 173–198. <http://dx.doi.org/10.1162/002438903321663370>.

Valentine Hacquard's MIT dissertation is a rich source of cross-linguistic issues in modality, as is Fabrice Nauze's Amsterdam dissertation:

Valentine Hacquard. 2006. *Aspects of modality*. Massachusetts Institute of Technology dissertation. http://ling.umd.edu/~hacquard/papers/hacquard_thesis.pdf.

Fabrice Nauze. 2008. *Modality in typological perspective*. Universiteit van Amsterdam dissertation. <http://www.illc.uva.nl/Publications/Dissertations/DS-2008-08.text.pdf>.

Some more recent work by Hacquard deals with deriving and correlating modal flavors with syntactic position of the modal auxiliaries:

Valentine Hacquard. 2010. On the event relativity of modal auxiliaries. *Natural Language Semantics* 18(1). 79–114. <http://dx.doi.org/10.1007/s11050-010-9056-4>.

Valentine Hacquard. 2013. The grammatical category of modality. *Proceedings of the 19th Amsterdam Colloquium*. http://www.illc.uva.nl/AC/AC2013/uploaded_files/inlineitem/o3_Hacquard.pdf.

A recent handbook article by Hacquard on actuality entailments (involving the interaction of modality with aspect; we'll discuss aspect later in these notes):

Valentine Hacquard. 2016. Actuality entailments. to appear in L. Matthewson, C. Meier, H. Rullmann, T. E. Zimmermann (eds.) *Companion to Semantics*. Wiley. http://ling.umd.edu/~hacquard/papers/Hacquard_Actuality%20Entailments_July%202016.pdf.

The semantics of epistemic modals has become a hot topic recently. Here are some of the main references:

Ian Hacking. 1967. Possibility. *The Philosophical Review* 76(2). 143–168. <http://dx.doi.org/10.2307/2183640>. <http://www.jstor.org/stable/2183640>.

Paul Teller. 1972. Epistemic possibility. *Philosophia* 2(4). 302–320. <http://dx.doi.org/10.1007/BF02381591>.

Keith DeRose. 1991. Epistemic possibilities. *The Philosophical Review* 100(4). 581–605. <http://dx.doi.org/10.2307/2185175>.

Andy Egan, John Hawthorne & Brian Weatherson. 2005. Epistemic modals in context. In Gerhard Preyer & Georg Peter (eds.), *Contextualism in philosophy: Knowledge, meaning, and truth*, 131–170. Oxford: Oxford University Press.

Andy Egan. 2007. Epistemic modals, relativism, and assertion. *Philosophical Studies* 133(1). 1–22. <http://dx.doi.org/10.1007/s11098-006-9003-x>.

John MacFarlane. 2006. Epistemic modals are assessment-sensitive. ms, University of California, Berkeley, forthcoming in an OUP volume on epistemic modals, edited by Brian Weatherson and Andy Egan. <http://sophos.berkeley.edu/macfarlane/epistmod.pdf>.

Tamina Stephenson. 2007a. Judge dependence, epistemic modals, and predicates of personal taste. *Linguistics and Philosophy* 30(4). 487–525. <http://dx.doi.org/10.1007/s10988-008-9023-4>.

John Hawthorne. 2007. Eavesdroppers and epistemic modals. ms, Rutgers University, to appear in the proceedings of the 2007 Sofia Conference in Mexico, in a supplement to *Noûs*.

Kai von Fintel & Anthony S. Gillies. 2008a. CIA leaks. *The Philosophical Review* 117(1). 77–98. <http://dx.doi.org/10.1215/00318108-2007-025>.

Kai von Fintel & Anthony S. Gillies. 2008b. *Might* made right. To appear in a volume on epistemic modality, edited by Andy Egan and Brian Weatherson, Oxford University Press. <http://mit.edu/fintel/fintel-gillies-2008-mm.pdf>.

A paper by Pranav Anand and Valentine Hacquard tackles what happens to epistemic modals under attitude predicates:

Pranav Anand & Valentine Hacquard. 2013. Epistemics and attitudes. *Semantics and Pragmatics* 6(8). 1–59. <http://dx.doi.org/10.3765/sp.6.8>.

Evidentiality is a topic closely related to epistemic modality. Some references:

Thomas Willett. 1988. A cross-linguistic survey of the grammaticalization of evidentiality. *Studies in Language* 12(1). 51–97.

Alexandra Y. Aikhenvald. 2004. *Evidentiality*. Oxford: Oxford University Press.

Hans Bernhard Drubig. 2001. On the syntactic form of epistemic modality. ms, Universität Tübingen. <http://www.sfb441.uni-tuebingen.de/b2/papers/DrubigModality.pdf>.

Eleanor M. Blain & Rose-Marie Déchaine. 2007. Evidential types: Evidence from Cree dialects. *International Journal of American Linguistics* 73(3). 257–291. <http://dx.doi.org/10.1086/521728>.

Eric McCready & Norry Ogata. 2007. Evidentiality, modality and probability. *Linguistics and Philosophy* 30(2). 147–206. <http://dx.doi.org/10.1007/s10988-007-9017-7>.

Peggy Speas. 2008. On the syntax and semantics of evidentials. *Language and Linguistics Compass* 2(5). 940–965. <http://dx.doi.org/10.1111/j.1749-818X.2008.00069.x>.

Kai von Fintel & Anthony S. Gillies. 2010. *Must* ... stay ... strong! *Natural Language Semantics* 18(4). 351–383. <http://dx.doi.org/10.1007/s11050-010-9058-2>.

Modals interact with disjunction and indefinites to generate so-called FREE CHOICE-readings, which are a perennial puzzle. Here is just a very small set of initial references:

Hans Kamp. 1973. Free choice permission. *Proceedings of the Aristotelian Society, New Series* 74. 57–74. <http://www.jstor.org/stable/4544849>.

Thomas Ede Zimmermann. 2000. Free choice disjunction and epistemic possibility. *Natural Language Semantics* 8(4). 255–290. <http://dx.doi.org/10.1023/A:1011255819284>.

Katrin Schulz. 2005. A pragmatic solution for the paradox of free choice permission. *Synthese* 147(2). 343–377. <http://dx.doi.org/10.1007/s11229-005-1353-y>.

- Maria Aloni. 2007. Free choice, modals, and imperatives. *Natural Language Semantics* 15(1). 65–94. <http://dx.doi.org/10.1007/s11050-007-9010-2>.
- Luis Alonso-Ovalle. 2006. *Disjunction in alternative semantics*. University of Massachusetts at Amherst dissertation. http://alonso-ovalle.net/index.php?page_id=28.
- Danny Fox. 2007. Free choice and the theory of scalar implicatures. In Uli Sauerland & Penka Stateva (eds.), *Presupposition and implicature in compositional semantics*, 537–586. New York: Palgrave Macmillan. http://web.mit.edu/linguistics/people/faculty/fox/free_choice.pdf.
- Robert van Rooij. 2006. Free choice counterfactual donkeys. *Journal of Semantics* 23(4). 383–402. <http://dx.doi.org/10.1093/jos/ffl004>.

PART II

DPS IN INTENSIONAL CONTEXTS

CHAPTER FIVE

SPECIFICITY AND TRANSPARENCY

We discuss two important aspects of the interpretation of DPs in intensional contexts: the scope of their quantificational force, if any, and the world with respect to which their predicate is evaluated.

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5.1 Predictions of our framework

When a DP occurs in the scope of an intensional operator, our framework makes clear predictions. Consider, for example:

- (1) Chris wanted Dana to buy a book about soccer.

Imagine that we give the following meaning to *want*:

- (2) $\llbracket \text{want} \rrbracket^{w,g} = \lambda p_{\langle s,t \rangle} . \lambda x_e . \forall w' \text{ such that } x \text{'s wants in } w \text{ are satisfied in } w': p(w') = 1.$

In other words, x *wants* p is true iff p is true in all worlds where x 's wants are satisfied. Further, assume that the DP *a book about soccer* is interpreted within the embedded clause. Then, we claim, (1) will be true iff in all of the worlds that satisfy all of Chris' wants, there is a book about soccer that Dana buys. (You prove this claim in the following exercise.)

EXERCISE 5.1: Draw the obvious, if simplified, LF for (1) and calculate its truth-conditions. \square

Now, consider what happens if the object of the lower verb QRs and adjoins to the matrix clause:

- (3) [a book about soccer] (I [Chris wanted Dana to buy t_I])

When you calculate the truth-conditions of (3) [please do so], you will get a result that is very different from the previous exercise. Now what is claimed is that there is a book about soccer, call it x , such that in all of the worlds satisfying all of Chris' wants Dana buys x .

There are two important differences between the truth-conditions that our framework assigns to these two LFs.

Quantifier scope: Since *want* is a universal quantifier over worlds and *a book about soccer* is an existential quantifier over individuals, there's a question about the relative scope of the two quantifiers. In the first truth-conditions we sketched, the existential quantifier scopes under the universal quantifier: for every world there is an individual such that bla-bla. In the second LF, the existential quantifier scopes over the universal one: there is an individual such that in every world yadda-yadda. The most common terminology for this difference involves the pair *specific/non-specific*: the sentence (or the object DP) is interpreted specifically if the DP takes scope over the intensional operator, and it is interpreted non-specifically if the DP takes scope under the intensional operator.

Predicate evaluation: When the existential quantifier scopes over the intensional operator, this also has the effect that the predicate contained in it, *book about soccer*, is evaluated in the matrix evaluation world. And when the quantifier takes lower scope, its predicate is evaluated in the worlds that the intensional operator shifts to. One evocative terminology for whether the predicate is evaluated with respect to the matrix evaluation world or the worlds shifted to by the intensional operator is *transparent/opaque*. A predicate evaluated relative to the matrix world is called *transparent*. A predicate evaluated in the worlds shifted to by an intensional operator is receiving an *opaque* interpretation.

There's another terminological pair that is very common: *de re/de dicto*. One way to conceive of that distinction in our framework is that it stands for a particular combination of the two distinctions we just introduced: *de re* means specific and transparent, and *de dicto* means non-specific and opaque.

Caution about terminology: terminological confusion and exuberance is rampant in this area (and many others). In a way, terminology is just a shorthand way to pick out salient properties of LFs (or their denotation). It's the latter that truly matters. One particular problematic aspect of the terminology is its binary nature, while the relevant distinctions are actually more complex, especially as soon as we are dealing with nested intensionality.

EXERCISE 5.2: Consider the sentence *Chris must want Dana to buy a book about soccer*. One can imagine using this to describe a scenario where we are seeing Dana enter a bookstore known to cater to soccer aficionados. For some reason

we won't go into, we come to the conclusion that there is a specific book about soccer that Chris must have asked Dana to buy. But at the same time, we have no idea what that book might be, so there's not a specific book about which we made our deduction. This suggests that we may want to give the object DP intermediate scope. So, draw an LF that corresponds to this idea and calculate its truth-conditions. □

The notion of *specificity* is particularly laden with complexity. We use it here to indicate the scope of a DP with respect to an intensional operator. There are quite a few other conceptions, usefully surveyed by [von Heusinger 2011](#). One that is very common is the notion that specific DPs indicate that the speaker has a referent or referents “in mind”, something that may even be relevant in the absence of intensional operators. Consider:

- (4) A man is knocking on the door.

The speaker might base such a claim on circumstantial evidence (hearing a particularly masculine knock on the door?) or on clear visual evidence (seeing the man through the window). In the second case, we're tempted to say that the speaker has a specific referent “in mind” while in the first case there is non-specific existential quantification. Whether this is merely a pragmatic distinction about what is grounding the speaker's claim or whether the LF reflects this difference in “specificity” is a debatable issue. If one adopted the idea that all matrix sentences contain an epistemic operator, such as Marie-Christine Meyer's “Matrix K” operator ([Meyer 2013](#)), then we would have a genuine LF ambiguity if DPs such as *a man* could take scope over or under that operator.

For discussion, see for example [Ludlow & Neale 1991](#).

Our recommendation is to use the terms *specific/non-specific*, *transparent/opaque*, *de re/de dicto* only with extreme caution. They are sometimes useful shorthands, but unless it is crystal-clear what properties of LFs/denotations you are using them to pick out, they are more likely to be a source of obfuscation and confusion.

Let's look at some more examples of the ambiguity predicted by our framework as soon as we allow for the possibility of an embedded DP to take scope either under or over a relevant intensional operator. A classic kind of example is (5), which contains the DP *a plumber* inside the infinitive complement of *want*.

- (5) John wants to marry a plumber.

According to the non-specific reading, every possible world in which John gets what he wants is a world in which there is a plumber whom he marries. According to the specific reading, there is a plumber in the actual world whom John marries in every world in which he gets what he wants. We can imagine situations in which one of the readings is true and the other one false.

For example, suppose John thinks that plumbers make ideal spouses, because they can fix things around the house. He has never met one so far, but he

definitely wants to marry one. In this scenario, the non-specific reading is true, but the specific reading is false. What all of John's desire-worlds have in common is that they have a plumber getting married to John in them. But it's not the same plumber in all those worlds. In fact, there is no particular individual (actual plumber or other) whom he marries in every one of those worlds.

For a different scenario, suppose that John has fallen in love with Robin and wants to marry Robin. Robin happens to be a plumber, but John doesn't know this; in fact, he wouldn't like it and might even call off the engagement if he found out. Here the specific reading is true, because there is an actual plumber, viz. Robin, who gets married to John in every world in which he gets what he wants. The non-specific reading is false, however, because the worlds which conform to John's wishes actually do not have him marrying a plumber in them. In his favorite worlds, he marries Robin, who is not a plumber in those worlds.

When confronted with this second scenario, you might, with equal justification, say 'John wants to marry a plumber', or 'John *doesn't* want to marry a plumber'. Each can be taken in a way that makes it a true description of the facts — although, of course, you cannot assert both in the same breath. This intuition fits well with the idea that we are dealing with a genuine ambiguity.

Let's look at another example:

- (6) John believes that your abstract will be accepted.

Here the relevant DP in the complement clause of the verb *believe* is *your abstract*. Again, we detect an ambiguity, which is brought to light by constructing different scenarios.

- (i) John's belief may be about an abstract that he reviewed, but since the abstract is anonymous, he doesn't know who wrote it. He told me that there was a wonderful abstract about subjacency in Hindi that is sure to be accepted. I know that it was your abstract and inform you of John's opinion by saying (6). This is the specific reading. In the same situation, the non-specific reading is false: Among John's belief worlds, there are many worlds in which *your abstract will be accepted* is not true or even false. For all he knows, you might have written, for instance, that terrible abstract about Antecedent-Contained Deletion, which he also reviewed and is positive will be rejected.
- (ii) For the other scenario, imagine that you are a famous linguist, and John doesn't have a very high opinion about the fairness of the abstract selection process. He thinks that famous people never get rejected, however the anonymous reviewers judge their submissions. He believes (correctly or incorrectly — this doesn't matter here) that you submitted a (unique) abstract. He has no specific information or opinion about the abstract's content and quality, but given his general beliefs and his knowledge that you are famous, he nevertheless believes that your abstract will be accepted.

Actually, *why* wouldn't one be able to assert both sentences in the same breath, if both have a true reading?

This is the non-specific reading. Here it is true in all of John's belief worlds that you submitted a (unique) abstract and it will be accepted. The specific reading of (6), though, may well be false in this scenario. Suppose — to flesh it out further — the abstract you actually submitted is that terrible one about ACD. That one surely doesn't get accepted in every one of John's belief worlds. There may be some where it gets in (unless John is certain it can't be by anyone famous, he has to allow at least the possibility that it will get in despite its low quality). But there are definitely also belief-worlds of his in which it doesn't get accepted.

We have taken care here to construct scenarios that make one of the readings true and the other false. This establishes the existence of two distinct readings. We should note, however, that there are also many possible and natural scenarios that simultaneously support the truth of *both* readings. Consider, for instance, the following third scenario for sentence (6).

- (iii) John is your adviser and is fully convinced that your abstract will be accepted, since he knows it and in fact helped you when you were writing it. This is the sort of situation in which both the non-specific and the specific reading are true. It is true, on the one hand, that the sentence *your abstract will be accepted* is true in every one of John's belief worlds (non-specific reading). And on the other hand, if we ask whether the abstract which you actually wrote will get accepted in each of John's belief worlds, that is likewise true (specific reading).

In fact, this kind of “doubly verifying” scenario is very common when we look at actual uses of attitude sentences in ordinary conversation. There may even be many cases where communication proceeds smoothly without either the speaker or the hearer making up their minds as to which of the two readings they intend or understand. It doesn't matter, since the possible circumstances in which their truth-values would differ are unlikely and ignorable anyway. Still, we *can* conjure up scenarios in which the two readings come apart, and our intuitions about those scenarios do support the existence of a semantic ambiguity.

EXERCISE 5.3: For the two examples just discussed, we can explain their non-specific (and opaque) interpretation via LFs where the relevant DP remains inside the scope of the intensional operator at LF:

(7) John wants [[a plumber]₁ [PRO₂ to marry t₁]]

(8) John believes [the abstract-by-you will-be-accepted]

To obtain the specific (and transparent) readings, we apparently have to QR the DP to a position above the intensional predicate, minimally the VP headed by *want* or *believe*.

(9) [a plumber]_I [John wants [PRO₂ to marry t_I]]

(10) [the abstract-by-you]_I [John believes t_I will-be-accepted]

Calculate the interpretations of the four structures in (7) — (10), and determine their predicted truth-values in each of the (types of) possible worlds that we described above in our introduction to the ambiguity.

Some assumptions to make the job easier: (i) Assume that (7) and (9) are evaluated with respect to a variable assignment that assigns John to the number 2. This assumption takes the place of a worked out theory of how controlled PRO is interpreted. (ii) Assume that *abstract-by-you* is an unanalyzed one-place predicate. This takes the place of a worked out theory of how genitives with a non-possessive meaning are to be analyzed. □

5.2 Raised subjects

In the examples of ambiguities that we have looked at so far, the surface position of the DP in question was inside the modal predicate's clausal or VP-complement. We saw that if it stays there at LF, a non-specific opaque reading results, and if it covertly moves up above the modal operator, we get a specific transparent reading. In the present section, we will look at cases in which a DP that is superficially *higher* than a modal operator can still be read non-specifically. In these cases, it is the specific reading which we obtain if the LF looks essentially like the surface structure, and it is the non-specific reading for which we apparently have to posit a non-trivial covert derivation.

5.2.1 Non-specific readings for raised subjects

Suppose I come to my office one morning and find the papers and books on my desk in different locations than I remember leaving them the night before. I say:

(11) Somebody must have been here (since last night).

On the assumptions we have been making, *somebody* is base-generated as the subject of the VP *be here* and then moved to its surface position above the modal. So (11) has the following S-structure, which is also an interpretable LF.

(12) somebody [2 [[must R] [t₂ have-been-here]]]

What does (12) mean? The appropriate reading for *must* here is epistemic, so suppose the variable R is mapped to the relation $[\lambda w. \lambda w'. w' \text{ is compatible with what I believe in } w]$. Let w_o be the utterance world. Then the truth-condition calculated by our rules is as follows.

- (13) $\exists x[x \text{ is a person in } w_o \ \& \ \forall w'[w' \text{ is compatible with what I believe in } w_o \rightarrow x \text{ was here in } w']]$

But this is not the intended meaning. For (13) to be true, there has to be a person who in every world compatible with what I believe was in my office. In other words, all my belief-worlds have to have one and the same person coming to my office. But this is not what you intuitively understood me to be saying about my belief-state when I said (11). The context we described suggests that I do not know (nor have any opinion about) which person it was that was in my office. For all I know, it might have been John, or it might have been Mary, or it might have been this stranger here, or that stranger there. In each of my belief-worlds, somebody or other was in my office, but no one person was there in all of them. I do not believe of anyone in particular that he or she was there, and you did not understand me to be saying so when I uttered (11). What you did understand me to be claiming, apparently, was not (13) but (14).

- (14) $\forall w'[w' \text{ is compatible with what I believe in } w_o \rightarrow \exists x [x \text{ is a person in } w' \ \& \ x \text{ was here in } w']]$

In other words — to use the terminology we introduced in the last section — the DP *somebody* in (11) appears to have a non-specific reading.

How can sentence (11) have the meaning in (14)? The LF in (12), as we saw, means something else; it expresses a specific reading, which typically is false when (11) is uttered sincerely. So there must be another LF. What does it look like and how is it derived? One way to capture the intended reading, it seems, would be to generate an LF that's essentially the same as the underlying structure we posited for (11), i.e., the structure *before* the subject has raised:

- (15) $[_{IP} \in [_I' \text{ [must R] [somebody have-been-here]}]]$

(15) means precisely (14) (assuming that the unfilled Spec-of-IP position is semantically vacuous), as you can verify by calculating its interpretation by our rules. So is (15) (one of) the LF(s) for (11), and what assumption about syntax allow it to be generated? Or are there other — perhaps less obvious, but easier to generate — candidates for the non-specific LF-structure of (11)?

Before we get into these questions, let's look at a few more examples. Each of the following sentences, we claim, has a non-specific reading for the subject, as given in the accompanying formula. The modal operators in the examples are of a variety of syntactic types, including modal auxiliaries, main verbs, adjectives, and adverbs.

- (16) Everyone in the class may have received an A.
 $\exists w'[w' \text{ conforms to what I believe in } w \ \& \ \forall x[x \text{ is in this class in } w' \rightarrow x \text{ received an A in } w']]$.

- (17) At least two semanticists have to be invited.
 $\forall w'[w' \text{ conforms to what is desirable in } w]$
 $\rightarrow \exists_2 x [x \text{ is a semanticist in } w' \ \& \ x \text{ is invited in } w']]$.
- (18) Somebody from New York is expected to win the lottery.
 $\forall w'[w' \text{ conforms to what is expected in } w]$
 $\rightarrow \exists x [x \text{ is a person from NY in } w' \ \& \ x \text{ wins the lottery in } w']]$
- (19) Somebody from New York is likely to win the lottery.
 $\forall w'[w' \text{ is as likely as any other world, given what I know in } w]$
 $\rightarrow \exists x [x \text{ is a person from NY in } w' \ \& \ x \text{ wins the lottery in } w']]$ ¹
- (20) One of these two people is probably infected.
 $\forall w'[w' \text{ is as likely as any other world, given what I know in } w]$
 $\rightarrow \exists x [x \text{ is one of these two people} \ \& \ x \text{ is infected in } w']]$

To bring out the intended non-specific reading of the last example (to pick just one) imagine this scenario: We are tracking a dangerous virus infection and

1 Hopefully the exact analysis of the modal operators *likely* and *probably* is not too crucial for the present discussion, but you may still be wondering about it. As you see in our formula, we are thinking of *likely* (*probably*) as a kind of epistemic necessity operator, i.e., a universal quantifier over a set of worlds that is somehow determined by the speaker's knowledge. (We are focussing on the "subjective probability" sense of these words. Perhaps there is also an "objective probability" reading that is circumstantial rather than epistemic.) What is the difference then between *likely* and e.g. epistemic *must* (or *necessary* or *I believe that*)? Intuitively, 'it is likely that p' makes a weaker claim than 'it must be the case that p'. If both are universal quantifiers, then, it appears that *likely* is quantifying over a smaller set than *must*, i.e., over only a proper subset of the worlds that are compatible with what I believe. The difference concerns those worlds that I cannot strictly rule out but regard as remote possibilities. These worlds are included in the domain for *must*, but not in the one for *likely*. For example, if there was a race between John and Mary, and I am willing to bet that Mary won but am not completely sure she did, then those worlds where John won are remote possibilities for me. They are included in the domain of *must*, and so I will not say that Mary *must* have won, but they are not in the domain quantified over by *likely*, so I do say that Mary is *likely* to have won.

This is only a very crude approximation, of course. For one thing, probability is a gradable notion. Some things are more probable than others, and where we draw the line between what's probable and what isn't is a vague or context-dependent matter. Even *must*, *necessary* etc. arguably don't really express complete certainty (because in practice there is hardly anything we are completely certain of), but rather just a very high degree of probability. For more discussion of *likely*, *necessary*, and other graded modal concepts in a possible worlds semantics, see e.g. Kratzer 1981, 1991.

A different approach may be that *likely* quantifies over the same set of worlds as *must*, but with a weaker, less than universal, quantificational force. I.e., 'it is likely that p' means something like p is true in *most* of the worlds conforming to what I know. A *prima facie* problem with this idea is that presumably every proposition is true in infinitely many possible worlds, so how can we make sense of cardinal notions like 'more' and 'most' here? But perhaps this can be worked out somehow.

have sampled blood from two particular patients. Unfortunately, we were sloppy and the blood samples ended up all mixed up in one container. The virus count is high enough to make it quite probable that one of the patients is infected but because of the mix-up we have no evidence about which one of them it may be. In this scenario, (20) appears to be true. It would not be true under a specific reading, because neither one of the two people is infected in every one of the likely worlds.

A word of clarification about our empirical claim: We have been concentrating on the observation that non-specific readings are *available*, but have not addressed the question whether they are the *only* available readings or coexist with equally possible specific readings. Indeed, some of the sentences in our list appear to be ambiguous: For example, it seems that (18) could also be understood to claim that there is a particular New Yorker who is likely to win (e.g., because he has bribed everybody). Others arguably are not ambiguous and can only be read non-specific. This is what von Stechow & Sichel (2003) claim about sentences like (16). They note that if (16) also allowed a specific reading, it should be possible to make coherent sense of (21).

(21) Everyone in the class may have received an A. But not everybody did.

In fact, (21) sounds contradictory, which they show is explained if only the non-specific reading is permitted by the grammar. They conjecture that this is a systematic property of epistemic modal operators (as opposed to deontic and other types of modalities). Epistemic operators always have widest scope in their sentence.

So there are really two challenges here for our current theory. We need to account for the existence of non-specific readings, and also for the absence, in at least some of our examples, of specific readings. We will be concerned here exclusively with the first challenge and will set the second aside. We will aim, in effect, to set up the system so that all sentences of this type are in principle ambiguous, hoping that additional constraints that we are not investigating here will kick in to exclude the specific readings where they are missing.

To complicate the empirical picture further, there are also examples where raised subjects are unambiguously specific. Such cases have been around in the syntactic literature for a while, and they have received renewed attention in the work of Lasnik and others. To illustrate just one of the systematic restrictions, negative quantifiers like *nobody* seem to permit only surface scope (i.e., wide scope) with respect to a modal verb or adjective they have raised over.

(22) Nobody from New York is likely to win the lottery.

(22) does not have a non-specific reading parallel to the one for (19) above, i.e., it cannot mean that it is likely that nobody from NY will win. It can only mean that there is nobody from NY who is likely to win. This too is an issue that we set aside.

For a thorough investigation of low scope readings of negative DPs, see Iatridou & Sichel 2011.

In the next couple of sections, all that we are trying to do is find and justify a mechanism by which the grammar is able to generate both specific and non-specific readings for subjects that have raised over modal operators. It is quite conceivable, of course, that the nature of the additional constraints which often exclude one reading or the other is ultimately relevant to this discussion and that a better understanding of them may undermine our conclusions. But this is something we must leave for further research.

5.2.2 Syntactic “Reconstruction”

Given that the non-specific reading of (11) we are aiming to generate is equivalent to the formula in (14), an obvious idea is that there is an LF which is essentially the pre-movement structure of this sentence, i.e., the structure prior to the raising of the subject above the operator. There are a number of ways to make such an LF available.

One option, most defended in [Sauerland & Elbourne \(2002\)](#), is to assume that the raising of the subject can happen in a part of the derivation which only feeds PF, not LF. In that case, the subject simply stays in its underlying VP-internal position throughout the derivation from DS to LF. (Recall that quantifiers are interpretable there, as they generally are in subject positions.)

Another option is a version of the so-called Copy Theory of movement introduced in [Chomsky \(1993\)](#). This assumes that movement generally proceeds in two separate steps, rather than as a single complex operation as we have assumed so far. Recall that in H&K, it was stipulated that every movement effects the following four changes:

- (i) a phrase α is deleted,
- (ii) an index i is attached to the resulting empty node (making it a so-called trace, which the semantic rule for “Pronouns and Traces” recognizes as a variable),
- (iii) a new copy of α is created somewhere else in the tree (at the “landing site”), and
- (iv) the sister-constituent of this new copy gets another instance of the index i adjoined to it (which the semantic rule of Predicate Abstraction recognizes as a binder index).

If we adopt the Copy Theory, we assume instead that there are three distinct operations:

“**Copy**”: Create a new copy of α somewhere in the tree, attach an index i to the original α , and adjoin another instance of i to the sister of the new copy of α . (= steps (ii), (iii), and (iv) above)

“**Delete Lower Copy**”: Delete the original α . (= step (i) above)

“**Delete Upper Copy**”: Delete the new copy of α and both instances of i .

The Copy operation is part of every movement operation, and can happen anywhere in the syntactic derivation. The Delete operations happen at the end of the LF derivation and at the end of the PF deletion. We have a choice of applying either Delete Lower Copy or Delete Upper Copy to each pair of copies, and we can make this choice independently at LF and at PF. (E.g., we can do Copy in the common part of the derivation and then Delete Lower Copy at LF and Delete Upper Copy at PF.) If we always choose Delete Lower Copy at LF, this system generates exactly the same structures and interpretations as the one from H&K. But if we exercise the Delete Upper Copy option at LF, we are effectively undoing previous movements, and this gives us LFs with potentially new interpretations. In the application we are interested in here, we would apply the Copy step of subject raising before the derivation branches, and then choose Delete Lower Copy at PF but Delete Upper Copy at LF. The LF will thus look as if the raising never happened, and it will straightforwardly get the desired non-specific reading.

If the choice between the two Delete operations is generally optional, we in principle predict ambiguity wherever there has been movement. Notice, however, first, that the two structures will often be truth-conditionally equivalent (e.g. when the moved phrase is a name), and second, that they will not always be both interpretable. (E.g., if we chose Delete Upper Copy after QRing a quantifier from object position, we'd get an uninterpretable structure, and so this option is automatically ruled out.) Even so, we predict lots of ambiguity. Specifically, since raised subjects are always interpretable in both their underlying and raised locations, we predict all raising structures where a quantificational DP has raised over a modal operator (or over negation or a temporal operator) to be ambiguous. As we have already mentioned, this is not factually correct, and so there must be various further constraints that somehow restrict the choices. (Similar comments apply, of course, to the option we mentioned first, of applying raising only on the PF-branch.)

Yet another solution was first proposed by May (1977): May assumed that QR could in principle apply in a “downward” fashion, i.e., it could adjoin the moved phrase to a node that doesn't contain its trace. Exercising this option with a raised subject would let us produce the following structure, where the subject has first raised over the modal and then QRed below it.

(23) $t_j \lambda_i [\text{must-R} [\text{someone } \lambda_j [t_i \text{ have been here}]]]$

As it stands, this structure contains at least one free variable (the trace t_j) and can therefore not possibly represent any actual reading of this sentence. May further assumes that traces can in principle be deleted, when their presence is not required for interpretability. This is not yet quite enough, though to make (23) interpretable, at least not within our framework of assumptions, for (24) is still not a candidate for an actual reading of (II).

(24) λ_i [must-R [someone λ_j [t_i have been here]]]

We would need to assume further that the topmost binder index could be deleted along with the unbound trace, and also that the indices i and j can be the same, so that the raising trace t_j is bound by the binding-index created by QR. If these things can be properly worked out somehow, then this is another way to generate the non-specific reading. Notice that the LF is not exactly the same as on the previous two approaches, since the subject ends up in an adjoined position rather than in its original argument position, but this difference is obviously without semantic import.

What all of these approaches have in common is that they place the burden of generating the non-specific reading for raised subjects on the syntactic derivation. Somehow or other, they all wind up with structures in which the subject is lower than it is on the surface and thereby falls within the scope of the modal operator. They also have in common that they take the modal operator (here the auxiliary, in other cases a main predicate or an adverb) to be staying put. I.e., they assume that the non-specific readings are not due to the modal operator being covertly higher than it seems to be, but to the subject being lower. Approaches with these features will be said to appeal to “syntactic reconstruction” of the subject.²

5.2.3 Some Alternatives to Syntactic Reconstruction

Besides (some version of) syntactic reconstruction, there are many other ways in which one try to generate non-specific readings for raised subjects. Here are some other possibilities that have been suggested and/or readily come to mind. We will see that some of them yield exactly the non-specific reading as we have been describing it so far, whereas others yield a reading that is very similar but not quite the same. We will confine ourselves to analyses which involve no or only minor changes to our system of syntactic and semantic assumptions. Obviously, if one departed from these further, there would be even more different options, but even so, there seem to be quite a few.

1. RAISING THE MODAL OPERATOR, VARIANT I: NO TRACE Conceivably, an LF for the non-specific reading of (11) might be derived from the S-structure (= (12)) by covertly moving *must* (and its covert *R*-argument) up above the subject. This would have to be a movement which leaves no (semantically non-vacuous) trace. Given our inventory of composition rules, the only type that the trace could have to make the structure containing it interpretable would be the type of the

2. This is a very broad notion of “reconstruction”, where basically any mechanism which puts a phrase at LF in a location nearer to its underlying site than its surface site is called “reconstruction”. In some of the literature, the term is used more narrowly. For example, May’s downward QR is sometimes explicitly contrasted with genuine reconstruction, since it places the quantifier somewhere else than exactly where it has moved from.

moved operator itself (i.e. $\langle st, t \rangle$). If it had that type, however, the movement would be semantically inconsequential, i.e., the structure would mean exactly the same as (12). So this would not be a way to provide an LF for the non-specific reading. If there was no trace left however (and also no binder index introduced), we indeed would obtain the non-specific reading.

EXERCISE 5.4: Prove the claims we just made in the previous paragraph. Why is no type for the trace other than $\langle st, t \rangle$ possible? Why is the movement semantically inert when this type is chosen? How does the correct intended meaning arise if there is no trace and binder index? \square

2. RAISING THE MODAL OPERATOR, VARIANT 2: TRACE OF TYPE S [Requires slightly modified inventory of composition rules. Derives an interpretation that is not quite the same as the non-specific opaque reading we have assumed so far. Rather, it is the non-specific transparent “third” reading discussed in the next chapter.]

3. HIGHER TYPE FOR TRACE OF RAISING, VARIANT 1: TYPE $\langle et, t \rangle$ [Before reading this section, read and do the exercise on p.212/3 in $H\mathcal{C}K$]

So far in our discussion, we have taken for granted that the LF which corresponds to the surface structure, viz. (12), gives us the specific reading. This, however, is correct only on the tacit assumption that the trace of raising is a variable of type e . If it is part of our general theory that all variables, or at least all interpretable binder indices (hence all bound variables), in our LFs are of type e , then there is nothing more here to say. But it is not *prima facie* obvious that we must or should make this general assumption, and if we don't, then the tree in (12) is not really one single LF, but the common structure for many different ones, which differ in the type chosen for the trace. Most of the infinitely many semantic types we might assign to this trace will lead to uninterpretable structures, but there turns out to be one other choice besides e that works, namely $\langle et, t \rangle$:

(25) somebody $\lambda_{2, \langle et, t \rangle}$ [[must R] [$t_{2, \langle et, t \rangle}$ have-been-here]]

(25) is interpretable in our system, but again, as in the previous approach, the predicted interpretation is not exactly the non-specific reading as we have been describing it so far, but the non-specific transparent third reading.

EXERCISE 5.5: Using higher-type traces to “reverse” syntactic scope-relations is a trick which can be used quite generally. It is useful to look at a non-intensional example as a first illustration. (26) contains a universal quantifier and a negation, and it is scopally ambiguous between the readings in (a) and (b).

(26) Everything that glitters is not gold.

a. $\forall x[x \text{ glitters} \rightarrow \neg x \text{ is gold}]$

“surface scope”

b. $\neg \forall x[x \text{ glitters} \rightarrow x \text{ is gold}]$

“inverse scope”

That a trace of type $\langle et, t \rangle$ does not in fact yield the targeted non-specific opaque reading had not been noticed until we bothered to calculate the meaning of (25). For example, Fox 2000, which derives from a dissertation supervised by us, is unaware of the fact that a high-type but extensional trace gives a scope-reconstructed but transparent reading.

We could derive the inverse scope reading for (26) by generating an LF (e.g. by some version of syntactic reconstruction") in which the *every*-DP is below *not*. Interestingly, however, we can also derive this reading if the *every*-DP is in its raised position above *not* but its trace has the type $\langle\langle e, t \rangle, t\rangle$.

Spell out this analysis. (I.e., draw the LF and show how the inverse-scope interpretation is calculated by our semantic rules.) \square

EXERCISE 5.6: Convince yourself that there are no other types for the raising trace besides e and $\langle et, t \rangle$ that would make the structure in (12) interpretable. (At least not if we stick exactly to our current composition rules.) \square

4. HIGHER TYPE FOR TRACE OF RAISING, VARIANT 2: TYPE $\langle s, \langle et, t \rangle \rangle$ If we want to get *exactly* the non-specific reading that results from syntactic reconstruction out of a surface-like LF of the form (12), we must use an even higher type for the raising trace, namely $\langle s, \langle\langle e, t \rangle, t \rangle \rangle$, the type of the intension of a quantifier. As you just proved in the exercise, this is not possible if we stick to exactly the composition rules that we have currently available. The problem is in the VP: the trace in subject position is of type $\langle s, \langle\langle e, t \rangle, t \rangle \rangle$ and its sister is of type $\langle e, t \rangle$. These two cannot combine by either FA or IFA, but it works if we employ another variant of functional application.³

(27) *Extensionalizing Functional Application* (EFA)

If α is a branching node and $\{\beta, \gamma\}$ the set of its daughters, then, for any world w and assignment g :

if $\llbracket \beta \rrbracket^{w,g}$ is a function whose domain contains $\llbracket \gamma \rrbracket^{w,g}$,

then $\llbracket \alpha \rrbracket^{w,g} = \llbracket \beta \rrbracket^{w,g}(\llbracket \gamma \rrbracket^{w,g})$.

EXERCISE 5.7: Calculate the truth-conditions of (12) under the assumption that the trace of the subject quantifier is of type $\langle s, \langle\langle e, t \rangle, t \rangle \rangle$. \square

CAN WE CHOOSE BETWEEN ALL THESE OPTIONS? Two of the methods we tried derived readings in which the raised subject's *quantificational determiner* took scope below the world-quantifier in the modal operator, but the raised subject's

3 Notice that the problem here is kind of the mirror image of the problem that led to the introduction of "Intensional Functional Application" in H&K, ch. 12. There, we had a function looking for an argument of type $\langle s, t \rangle$, but the sister node had an extension of type t . IFA allowed us to, in effect, construct an argument with an added "s" in its type. This time around, we have to get rid of an "s" rather than adding one; and this is what EFA accomplishes.

So we now have three different "functional application"-type rules altogether in our system: ordinary FA simply applies $\llbracket \beta \rrbracket^w$ to $\llbracket \gamma \rrbracket^w$; IFA applies $\llbracket \beta \rrbracket^w$ to $\lambda w'. \llbracket \gamma \rrbracket^{w'}$; and EFA applies $\llbracket \beta \rrbracket^w(w)$ to $\llbracket \gamma \rrbracket^w$. At most one of them will be applicable to each given branching node, depending on the type of $\llbracket \gamma \rrbracket^w$.

Think about the situation. Might there be other variant functional application rules?

restricting NP still was evaluated in the utterance world (or the evaluation world for the larger sentence, whichever that may be), in other words: a non-specific but transparent interpretation. It is difficult to assess whether such readings are actually available for the particular sentences under consideration, and we will postpone this question to the next chapter. We would like to argue here, however, that even if these readings are available, they cannot be the *only* readings that are available for raised subjects besides their wide-scope readings. In other words, even if we allowed one of the mechanisms that generated these sort of hybrid readings, we would still need another mechanism that gives us, for at least some examples, the “real” non-specific opaque readings that we obtain e.g. by syntactic reconstruction. The relevant examples that show this most clearly involve DPs with more descriptive content than *somebody* and whose NPs express clearly contingent properties.

(28) A neat-freak must have been here.

If I say this instead of our original (11) when I come to my office in the morning and interpret the clues on my desk, I am saying that every world compatible with my beliefs is such that someone who is a neat-freak *in that world* was here in that world. Suppose there is a guy, Bill, whom I know slightly but not well enough to have an opinion on whether or not he is neat. He may or not be, for all I know. So there are worlds among my belief worlds where he is a neat-freak and worlds where he is not. I also don't have an opinion on whether he was or wasn't the one who came into my office last night. He did in some of my belief worlds and he didn't in others. I am implying with (28), however, that if Bill isn't a neat-freak, then it wasn't him in my office. I.e., (28) *is* telling you that, even if I have belief-worlds in which Bill is a slob and I have belief-worlds in which (only) he was in my office, I do not have any belief-worlds in which Bill is a slob *and* the only person who was in my office. This is correctly predicted if (28) expresses the “genuine” non-specific reading in (29), but not if it expresses the “hybrid” reading in (30).

(29) $\forall w' [w' \text{ is compatible with what I believe in } w_o \rightarrow$
 $\exists x [x \text{ is a neatfreak in } w' \text{ and } x \text{ was here in } w']]$

(30) $\forall w' [w' \text{ is compatible with what I believe in } w_o \rightarrow$
 $\exists x [x \text{ is a neatfreak in } w_o \text{ and } x \text{ was here in } w']]$

We therefore conclude the mechanisms 2 and 3 considered above (whatever their merits otherwise) cannot supplant syntactic reconstruction or some other mechanism that yields readings like (29).

This leaves only the first and fourth options that we looked at as potential competitors to syntactic reconstruction, and we will focus the rest of the discussion on how we might be able to tease apart the predictions that these mechanisms imply from the ones of a syntactic reconstruction approach.

As for moving the modal operator, there are no direct bad predictions that we are aware of with this. But it leads us to expect that we might find not only scope ambiguities involving a modal operator and a DP, but also scope ambiguities between two modal operators, since one of them might covertly move over the other. It seems that this never happens. Sentences with stacked modal verbs seem to be unambiguous and show only those readings where the scopes of the operators reflect their surface hierarchy.

- (3I) a. I have to be allowed to graduate.
b. #I am allowed to have to graduate.

See [Lechner 2007](#) for an early discussion of semantic effects of head movement. See [McCloskey 2016](#) for a recent re-assessment.

Of course, this might be explained by appropriate constraints on the movement of modal operators, and such constraints may even come for free in a the right syntactic theory. Also, we should have a much more comprehensive investigation of the empirical facts before we reach any verdict. If it is true, however, that modal operators only engage in scope interaction with DPs and never with each other, then a theory which does not allow any movement of modals at all could claim the advantage of having a simple and principled explanation for this fact.

What about the “semantic reconstruction” option, where raised subjects can leave traces of type $\langle s, \langle et, t \rangle \rangle$ and thus get narrow scope semantically without ending up low syntactically? This type of approach has been explored quite thoroughly and defended with great sophistication. The main consideration against semantic reconstruction and in favor of syntactic reconstruction comes from binding theoretic concerns. We give some crucial examples from Fox 2000 here.

SCOPE RECONSTRUCTION AND CONDITION C. Consider:

- (32) a. [A first year student] seems to David *t* to be at the party.
b. [Someone from NY] is very likely *t* to win the lottery.

These examples are a reminder that we can get non-specific readings of raised subjects. Fox argues that Binding Theory Condition C can be used to distinguish syntactic and semantic reconstruction. Assuming that Condition C applies at LF, syntactic reconstruction (where the full DP is interpreted in a lower position) predicts that an R-expression in that DP should not be allowed if there's a higher coreferential pronoun. The semantic reconstruction account has no simple way of making the same prediction.

Here are the crucial tests:

- (33) a. [A student of his_I] seems to David_I to be at the party.
 OK_{specific}, OK_{non-specific}
 b. [A student of David's_I] seems to him_I to be at the party.
 OK_{specific}, *non-specific

- (34) a. [Someone from his_i city] seems to David_i t to be likely to win the lottery.
 O^K_{specific}, O^K_{non-specific}
- b. [Someone from David_i's city] seems to him_i t to be likely to win the lottery.
 O^K_{specific}, *non-specific

Fox claims that the (b) cases do not have a non-specific reading. If syntactic reconstruction is the mechanism that gives us non-specific readings of A-moved subjects, the explanation is straightforward.

EXERCISE 5.8: Use the following observations to bolster Fox's argument.

- (35) a. The cat seems to be out of the bag.
b. Advantage might have been taken of them.
- (36) a. For these issues to be clarified, many new papers about his_i philosophy seem to Quine t to be needed.
b. #For these issues to be clarified, many new papers about Quine's_i philosophy seem to him t to be needed. □

If Fox's argument is correct, then (some form of) syntactic reconstruction is the mechanism by which we get non-specific readings of A-movement subjects. This means that syntactic reconstruction is possible, but it also means that semantic reconstruction must not be available. Otherwise, there would be a way of getting non-specific readings that would not be sensitive to Condition C. So, the question arises *why* semantic reconstruction is unavailable. Fox (2000: p. 171, fn. 41) discusses two ways of ruling out the high type traces that would give rise to semantic reconstruction:

- (i) “traces, like pronouns, are always interpreted as variables that range over individuals (type *e*)”,
- (ii) “the semantic type of a trace is determined to be the lowest type compatible with the syntactic environment (as suggested in Beck 1996)”.

We will return to this issue in a later chapter when we can raise it again in a slightly different framework.

5.3 Supplemental readings

In addition to the references about reconstruction in the text, you might want to look at:

Cedric Boeckx. 2001. Scope reconstruction and A-movement. *Natural Language and Linguistic Theory* 19(3). 503–548. <http://dx.doi.org/10.1023/a:1010646425448>.

Mark Baltin. 2010. The copy theory of movement and the binding-theoretic status of A-traces: You can't get there from here. http://linguistics.as.nyu.edu/docs/IO/2637/baltin_copytheoryofmovement.pdf.

CHAPTER SIX

THE ARGUMENT STRUCTURE OF MODALS

Are modals really raising predicates? Are they at least sometimes control predicates? If they are “raising” predicates, is that syntactic raising or some kind of “semantic” raising?

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6.1 Raising vs. Control

In lieu of lecture notes, a part of a handout from a class on “Morphology, syntax, and semantics of modals” taught by Kai von Stechow and Sabine at the 2009 LSA Summer Institute at the University of California at Berkeley.

- (13) O Yanis boruse na kolimbisi apenandi (ala dhen to ekane) (Greek)
 John could-IMP swim across (but didn't do it)

However, when the perfective is used, we get what Bhatt called an “actuality entailment”:

- (14) O Yanis borese na kolimbisi apenandi (ala dhen to ekane)
 John could-PRF swim across (#but didn't do it)

The obvious question is what the effect of the perfective is on the modal. While we have some understanding of these facts due to the aforementioned authors, the phenomenon still remains largely unsolved.

Syntax-related Issues that have received some attention in the literature:

I. Raising versus Control

(and addressing the issue of where modals appear in the tree and where they are interpreted:)

II. The Relative Ordering of Modals

III. Negation and Modals

I. Raising versus control

In a tradition going back to Jackendoff (1972), it has been widely assumed that deontic and epistemic modals differ in certain basic syntactic properties.

One should keep in mind that this is an important issue, especially if one wants to adopt or develop a system like Kratzer's (1978, 1981, 1991), in which modals differ only in contextual parameters. Under an idealized such account, there should be no syntactic differences between epistemic and deontic modals, for example.

Specifically, the idea is/was that deontics are instances of a control structure, while epistemics are raising predicates:

- (15) a. John must be there at 5pm **(Deontic)**
 b. [John must [PRO be there at 5pm]]

- (16) John must be there already (Epistemic)
 [ec must [John be there already]]
 [John_k must [t_k be there already]]

The idea behind this intuition was pretty straightforward: Deontics assert that the subject has a certain property, namely the property of having a particular obligation (or permission). Therefore, the modal assigns a theta-role to the subject. The lower thematic subject, of course, also exists; in the absence of Case, it is instantiated as PRO¹.

Epistemics, on the other hand, are propositional predicates. They say nothing about the subject or any particular argument inside the clause. At most, they mediate a relationship between a proposition and the belief system of an individual (the speaker). Therefore, the subject does not receive a theta-role from the epistemic modal. Rather, the modal has a thematic relationship with the entire CP/IP.

Linguists subsequently further refined their understanding of deontics, taking from the philosophers the distinction between *ought to do* and *ought to be* deontic modality. Brennan (1993), probably the first linguist to make this connection, based an interesting syntactic proposal on this distinction².

The idea here is that in *ought-to-do* modality, a particular individual has a certain obligation. For Brennan, *ought-to-do* modals are control predicates, as they assign a theta-role to their subject (and are infinitive-embedding).

- (17) Ought-to-do:
 John ought to/ has to/should hand this in before 5pm.
 John should PRO hand this in before 5pm.

On the other hand, *ought-to-be* modality does not assert obligation of any particular person.

For Brennan, *ought-to-be* modals are raising predicates, as evidenced also by the fact that

¹ Alternatively, in a theory without PRO, (15b) would be as follows:
 (15) b'. [John must [be there at 5pm]]

² Brennan (1993) cites Feldman (1986) as having influenced her work but the idea started earlier. However, Castañeda (1970) gives an early description of the notion, citing even earlier sources:

“Deontic concepts like ought, right, obligation, forbidden, and permissible have benefited from the philosophically exciting work in the semantics of modal concepts done by Kanger, Hintikka, Kripke, Montague and others. Their semantics illuminates both the topic and the contribution of the standard axiomatic approach to deontic logic: the topic is what philosophers used to call the Ought-to-be. On the other hand, the non-standard approach represented by early axiomatic deontic systems of ours deals with the Ought-to-do.”

they can support expletive subjects.

- (18) Ought-to-be:
There ought to/have to/should be laws against things like this.

In short, for Brennan, epistemic modals are raising predicates but deontic modals come in two varieties: Control (17) and Raising (18).

In effect, the difference between *ought-to-do* and *ought-to-be* modals is whether the obligation is understood to be borne by somebody. The idea was that when there is a bearer of the obligation, and hence an *ought-to-do* modal, the carrier of the obligation would be the thematic subject of the *ought-to-do* modal. With *ought-to-do* modality, there is no bearer of obligation. In other words, either the bearer of obligation is the theta-marked subject, or there is no bearer of obligation.

However, it turns out that there are deontic sentences that have a bearer of obligation that is not the syntactic subject.

From Bhatt (1998):

- (19) John has to eat an apple today.
(said as an instruction to John's caretaker at the day-care, who is therefore the carrier of the obligation)
- (20) Bill has to be consulted by John on every decision.
(*John* is the bearer of the obligation)

From Wurmbrand (1999):

- (21) The traitor must die.
(22) The old man must fall down the stairs and it must look like an accident.

From Claire Halpert (p.c.):

- (23) The security guard must not see you as you break into the museum.

Given such data, the idea that the bearer of the obligation is a theta-role assigned under structural conditions to the subject becomes difficult to maintain. An overt non-subject can be the bearer of the obligation, as in (20) (argument of by-phrase) and (23) (object of the verb). In addition, the bearer of the obligation can also be absent syntactically, as in (19), (21), and (22).

Furthermore, as Bhatt points out, (24) is structurally like an example of Brennan's *ought-to-be* modality and thus is not expected to have a carrier of the obligation at all. However, when said to the caterer, it becomes an *ought-to-do* modality, with the caterer being the carrier of the obligation.

- (24) We are expecting fifty guests tonight. There have to be 50 chairs in the living room room by 5p.m.

What both Bhatt and Wurmbrand conclude is that there is no structurally assigned theta-role 'carrier of the obligation'. It is claimed that there are no syntactic differences in the representations of *ought-to-do* and *ought-to-be* deontic modals; all deontic modals are raising constructions. That is, deontic modals never come with a theta-role of obligation (or permission). However, there is an inference mechanism that can identify the carrier of the obligation, who can appear in various syntactic positions (see (20) and (23)), or absent altogether, as in (19), (21-22) and (24).

In addition, both Bhatt and Wurmbrand bring to the fore several syntactic arguments that deontic modals pattern like raising predicates and not like control.

One of their arguments comes from Case. Bhatt discusses Hindi, but the argument there is a bit more complicated than we can do justice here. Wurmbrand's argument from Icelandic Case is easier to convey in a few words.

In Icelandic, while most verbs take nominative subjects, there are verbs that take accusative subjects (the verb meaning 'lack') and verbs that take dative subjects (the verb meaning 'like'). When these verbs are embedded under a control predicate, the higher subject gets the Case associated with the higher verb. When they are embedded under a raising predicate, the subject appears in the Case associated with the embedded predicate:

- (25) NP_{nom} V_{Control Pred} PRO lack/like DP
 (26) NP_{acc/dat} V_{Raising Pred} t lack/like DP

When verbs with quirky subjects are embedded under a modal, the case of the subject of the modal depends on the embedded predicate.³

- (27) NP_{acc/dat} Modal lack/like DP

Here are Wurmbrand's actual Icelandic data:

³ Unlike Thráinsson and Vikner (1995), who say that such sentences receive epistemic readings, Wurmbrand says that deontic modals have the same pattern.

- (28) a. Harald / *Haraldur vantar peninga.
Harold-ACC / *Harold-NOM lacks money
'Harold lacks money'
- b. Haraldi / *Haraldur líkar vel í Stuttgart.
Harold-DAT / *Harold-NOM likes well in Stuttgart
'Harold likes it in Stuttgart'
- (29) a. Haraldur / *Harald vonast til að vanta ekki peninga.
Harold-NOM / *Harold-ACC hopes for to lack not money
'Harold hopes not to lack money'
- b. Haraldur / *Haraldi vonast til að líka vel í Stuttgart.
Harold-NOM / *Harold-DAT hopes for to like well in Stuttg.
'Harold hopes to like it in Stuttgart'
- c. Harald virðist vanta ekki peninga.
Harold-ACC seems lack not money
'Harold seems not to lack money'
- (30) a. Haraldi / *Haraldur verour að líka hamborgarar.
Harold-DAT / *Harold-NOM must to like hamburgers
'Harold must like hamburgers' (in order to be accepted by his
new American in-laws)
- b. Umsækjandann veraur að vanta peninga.
The-applicant-ACC must to lack money
'The applicant must lack money' (in order to apply for this grant)

Note that the fact that nominative is impossible shows that raising is not just an option with these Icelandic modals, but is the only choice.

These and other syntactic arguments convinced a fair amount of people that all deontic modals are raising predicates, just like epistemic modals⁴.

This conclusion also fits Kratzer's proposal, since a common syntactic representation is more easily compatible with the view that epistemics and deontics differ only in conversational backgrounds and ordering source.

However, the conclusion that deontic modals are uniformly raising predicates may be too

⁴ Though we do not have time to go into this issue here, the same question arises for other modals, e.g, dynamic and ability ones. For these, see Hacquard (2006) and Hackl (1998).

strong for the general case. Bhatt and Wurmbrand have shown for sure that some deontic modals must be raising predicates. However, there is no apparent conceptual reason why there couldn't be deontic modals that are control predicates.

Recently, Nauze (2008) revives the position that English deontic modals are control predicates. However, his position is that the syntactic and semantic properties of modals differ significantly crosslinguistically. (Interestingly, this is in combination with a rejection of Kratzer's proposal that deontic/epistemic, etc., distinctions among modals are only contextually determined.)

Nauze puts faith in what he considers Brennan's strongest argument for the status of English deontic modals as theta-role assigners⁵ (Nauze p. 148, (16a,b), repeated below as (31)).

Sentences (31a) and (31b) are equivalent:

- (31) a. The president shook hands with John.
b. John shook hands with the president.

Epistemic predicates, which are propositional arguments for Brennan, retain this equivalence:

- (32) a. The president may/must have shaken hands with John.
b. John may/must have shaken hands with the president.

However, deontics do not (Nauze 149, (20a,b)):

- (33) a. The president must shake hands with John.
b. John must shake hands with the president.

Brennan/Nauze say that as *ought-to-be* modality (e.g. as said to the president's campaign director or John's secretary) the two sentences are equivalent. However, as *ought-to-do* modality (33a,b) are not equivalent. For Brennan and Nauze this is the result of the deontic modal assigning a theta-role to 'the president' in (a) but to 'John' in (b).

Is this a necessary conclusion? Once we have our inference mechanism (which we need anyway for sentences like (19-24), we can use it to choose either 'the president' or 'John' as the bearer of the obligation to shake hands with the other. Nothing would have to follow about the syntax of the two modals⁶.

⁵ He does not provide arguments against the position that all English deontics are raising predicates but does acknowledge the existence of that position in fn 78 on page 126, where he cites Wurmbrand (1999) and Barbiers (2006).

⁶ To be fair to Nauze, he does seem to acknowledge a path to this possibility in fn 27 on p. 149:

However, as we said earlier, even if we manage to show that all deontic modals in English and in Icelandic are raising predicates, there is no conceptual reason given as to why deontics could only be raising –unlike epistemics, whose status as propositional predicates seems quite clear.

To conclude this section:

- There has been a debate about the syntactic status of deontic and epistemic modals: do they assign a theta-role to their syntactic subjects (making them control predicates) or do they not (making them raising predicates)? Epistemics are uncontroversially taken to be raising predicates. The actual debate mostly centers on deontics. While there may be reason to expect that all epistemics will be raising predicates crosslinguistically, it may well turn out to be the case that deontics can go either way.
 - These questions should be extended to other modals (ability, dynamic etc), as well as to other languages.
 - In addition, one should keep in mind that if one wants a theory like Kratzer's, where modals differ only in contextual parameters, possible syntactic differences like raising versus control will have to be addressed seriously.
-

II. The relative ordering of modals

There has been a lot of work on the relative ordering of (functional) categories. The same question has been asked about modals: **if there is more than one modal in a tree, what order do the modals come in?**

There are two aspects of the question to address here:

- What are the facts?
- Why are the facts the way they are?

So what are the facts?

An early conclusion, and one that seems still fairly widely accepted, is that epistemics are

“Notice that in Kratzer's theory, this analysis of ought-to-do/ought-to-be deontic modals in terms of VP/S-operators can be accounted for by different conversational backgrounds: one expressing the president's duties, the other expressing the secretary's duties, respectively” This might mean that Nauze might accept as additional conversational background one expressing John's duties. In that case, we would have again no basis for a syntactic distinction.

6.2 “Semantic” Raising

Unedited lecture notes from 2002.

5. Modal predicates and argument structure

The modal operators we have considered so far have been of two semantic types: (i) type $\langle st, t \rangle$, which we assumed for modal auxiliaries, main modal verbs like **need to**, **have to**, and adjectives like **likely**^{1,2}; and (ii) type $\langle st, et \rangle$, the type of attitude verbs like **believe** and **want**. The syntactic properties of the lexical items of each of these semantic types are diverse:

- (175) for semantic type $\langle st, et \rangle$:
- (a) verbs (adjectives) with **that**-clause and **for**-clause complements:
V, subcategorizes for CP with **that** or **for**
believe (that), say, prefer (for), ... (aware, eager, ...)
 - (b) exceptional case-marking (ECM) verbs:
V, subcategorizes for IP
believe, ...
- (176) for semantic type $\langle st, t \rangle$:
- (c) modal auxiliaries:
Infl, subcategorizes for VP
must, may, ...
 - (d) raising verbs (and adjectives):
V(or A), subcategorizes for IP
have (to), need (to), ... (likely (to), ...)
 - (e) verbs (and adjectives) with expletive subjects:
V (or A), subcategorizes for CP with **that** or **for**
seem, ... (possible, ...)

In groups (d) and (e) we can also include the passives (without by-phrase) of verbs in (b) and (a). (E.g. **There are allowed to be cars on the beach; It is known that ...**). The syntactic concepts used in this classification are open to revision, of course. Also the list is not meant to be exhaustive.

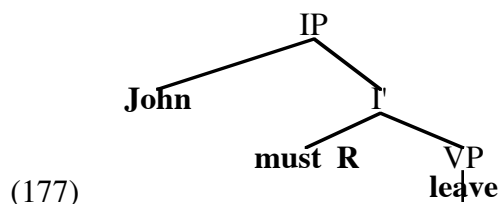
What additional semantic types do we find in lexical items that create intensional contexts? If we consider verbs like **tell** (in **John told Mary that ...**), we presumably need a type with a second type- e argument, i.e. $\langle st, \langle e, et \rangle \rangle$. What about the type of the intensional argument; does this always have to be a proposition ($\langle s, t \rangle$)? In particular, could it also be $\langle s, et \rangle$, i.e. a 1-place

¹In this section, we concentrate on modal operators that are syntactic heads, i.e. verbs (and adjectives). We will completely disregard adverbs (like 'possibly', 'necessarily').

²Actually, our type for the modals themselves is not $\langle st, t \rangle$, but rather $\langle \langle s, st \rangle, \langle st, t \rangle \rangle$. $\langle st, t \rangle$ is really the type of the constituent which already includes the modal and its covert restrictor. In this section, we will consistently talk as if the covert restrictors were already included in the lexical items which require them. So strictly speaking, when we talk about the type of a modal verb, we really mean the type of the node dominating the verb and the R-variable.

property? What might be examples (or candidates for examples) of predicates whose extensions are of, say, types $\langle\langle s, et \rangle, t \rangle$, $\langle\langle s, et \rangle, et \rangle$, or $\langle\langle s, et \rangle, \langle e, et \rangle \rangle$? [hint: see H&K ch. 12]

If we were not assuming the VP-internal subject hypothesis, then our first guess about the semantic type of modal auxiliaries would probably have been $\langle\langle s, et \rangle, et \rangle$.³ This would be the type to make them straightforwardly interpretable in syntactic structures like (177).

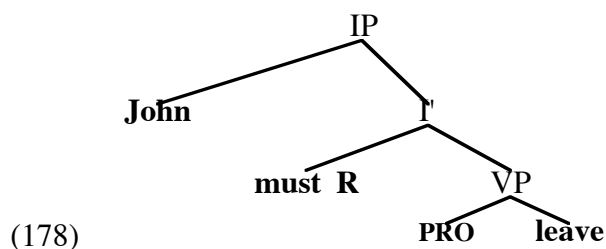


When we adopted the raising analysis of modal auxiliaries (and verbs like **have to**, **need to**), we did so without explicit motivation and discussion of alternatives. In this section, we are trying to fill this gap. We will compare the empirical predictions of the raising analysis (type $\langle st, t \rangle$) with the predictions of at least one kind of non-raising analysis. We will find that the behavior of the modal auxiliaries and of many modal main verbs (including **have to** and **need to**) is indeed accounted for more successfully by the raising analysis than by that alternative. We will also ask whether any lexical items in natural languages behave as predicted by the alternative analysis, and we will conclude with some speculations about universal constraints on possible lexical items.

5.1 A type- $\langle\langle s, et \rangle, et \rangle$ analysis for modals?

Suppose we adopted a syntactic representation as in (177). Here the modal (including its restrictor) combines first with a complement whose intension is a 1-place property, and then with an external argument which denotes an individual. Therefore, the denotation of the modal+restrictor will have to be of type $\langle et, et \rangle$ (if we are going to apply plain FA) or type $\langle\langle s, et \rangle, et \rangle$ (if we are going to use IFA). Can we write suitable lexical entries with at least one of

³ Even if we do stick to the VP-internal subject hypothesis, the raising analysis of modals that we have so far taken for granted is not our only option. The subject internal to the VP could be a PRO, as in (178), and it then depends on how we treat PRO.



If PRO is semantically vacuous as suggested in H&K, ch. 8, (178) is the same as (177) in its implications for the semantic type of **must-R**. If PRO is a pronoun that needs to be bound (hence treated as a variable of type e), the modal's type would need to be $\langle st, et \rangle$. We will disregard these options for the moment, but see below.

these types? Here is a proposal.

(179) For any $w \in W$:

- (a) $[[\mathbf{must}]]^w = \lambda R_{\langle s, st \rangle}. \lambda P_{\langle s, et \rangle}. \lambda x_e. \forall w' [w' \in R(w) \rightarrow P(w')(x) = 1]$
- (b) $[[\mathbf{may}]]^w = \lambda R_{\langle s, st \rangle}. \lambda P_{\langle s, et \rangle}. \lambda x_e. \exists w' [w' \in R(w) \& P(w')(x) = 1]$

So for the modal+restrictor node, we will have (180). Compare this with (181), which is what we had for the same node on the raising analysis.

$$(180) \quad [[\mathbf{must}]]^{w, [R \rightarrow R]} = \lambda P_{\langle s, et \rangle}. \lambda x_e. \forall w' [w' \in R(w) \rightarrow P(w')(x) = 1] \quad (= G)$$

$$(181) \quad [[\mathbf{must}]]^{w, [R \rightarrow R]} = \lambda p_{\langle s, t \rangle}. \forall w' [w' \in R(w) \rightarrow p(w') = 1] \quad (= F)$$

The function defined in (181) – let's call it F – takes a proposition; the function defined in (180), G , instead takes first a property and then an individual. Apart from this difference, these two functions perform similar jobs, as we can see when we define one in terms of the other:

$$(182) \quad G = \lambda P_{\langle s, et \rangle}. \lambda x_e. F(\lambda w. P(w)(x))$$

(182) is a recipe for constructing G , given F . What (182) says intuitively is this: if you want to know what value G yields when applied to P and x , construct the proposition that x has property P , and then apply F to that proposition.

Given that the new type- $\langle s, et \rangle$ meaning of the modal is constructed in this way from the old type- $\langle st, t \rangle$ meaning, the predicted truth-conditions for the new structures in (177) will be systematically the same as for the old raising structures. In the raising analysis, **John** and **leave** formed a syntactic unit⁴, therefore the composition rule applying to this unit determined that we should calculate the proposition that John leaves. The modal then applied to that proposition. In the new analysis, **John** and **leave** are separate pieces, so we don't know from the composition rules alone that we should put them together into the proposition that John leaves. But the new lexical entry of the modal, which takes both of these pieces as arguments, has it written into it that we are supposed to construct this proposition. The division of labor between composition rules and lexical meanings is different, but the net result of the calculation is the same.

So far, our type- $\langle s, et \rangle$ analysis predicts the same truth-conditions as the old raising (type- $\langle st, t \rangle$) analysis. However, we will see now that this is no longer true when we move beyond examples with referential (e.g., proper name) subjects.

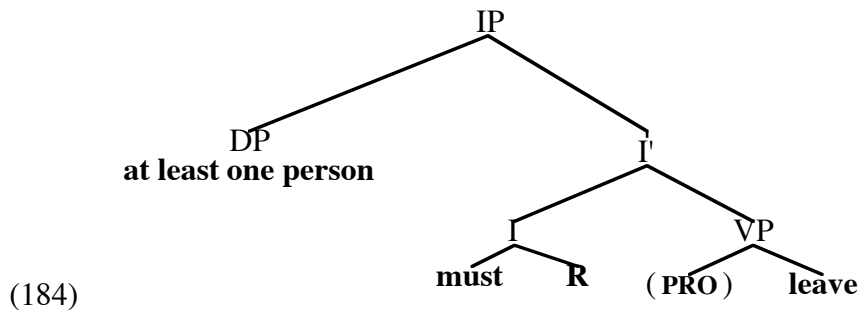
Suppose the subject is a quantificational DP, as in (183).

(183) **At least one person must leave.**

The syntactic structure at both S-structure and LF on the current analysis will have to be (184).⁵

⁴We are assuming here that we have raising followed by "reconstruction" (deletion of upper copy and coindexing). Without reconstruction, the relevant syntactic unit consists of **leave** and a variable. But after the variable is bound by Predicate Abstraction and the predicate abstract is predicated of **John**, the result still is the same.

⁵Ignore the parenthesized PRO. (See fn. 3)



This structure is interpretable by means of our new lexical entry in (181), and it expresses the *de re* reading. (Exercise: Verify this.) But what about the *de dicto* reading? Can we derive another LF which expresses that?

If reconstruction is the operation of deleting the upper copy (and coindexing link) of a movement chain, then of course, this operation is not applicable in a non-movement structure like (184). But the problem runs deeper than this. Even if we did allow some syntactic operation or other by which the DP **at least one person** got lowered past the modal (e.g., to substitute into the slot of the PRO, or to adjoin to the VP), that wouldn't help. It would not give us a representation of the *de dicto* reading, but only an uninterpretable structure. The sister node of **must-R** would now have a proposition as its intension (viz., the proposition $\lambda w'. \exists x[x \text{ is a person in } w' \ \& \ x \text{ leaves in } w']$). But a proposition is not a suitable argument; as we see in (180), **must-R** needs a property. Nor would it help to allow a syntactic operation that would raise the modal above the subject. The obstacle to generating the *de dicto* reading is not in the syntax, but in the semantic type of the modal. As long as **must-R** has a denotation of type $\langle\langle s,et \rangle, et \rangle$, *de dicto* readings are predicted impossible.

It is fair to conclude, then, that our original raising analysis was superior. The existence of *de dicto* readings for subjects provides an empirical argument in its favor.⁶

⁶ A note of caution: We have not shown that the raising analysis is superior to any non-raising analysis, only that it is superior to the particular non-raising analysis we considered – part of which was the assumption that the modal's outer argument is of type e. The situation changes if we consider other (fancier) choices of semantic type. Those authors who have actually defended non-raising analyses of modals in the literature have proposed instead that the modal's type is $\langle\langle s,et \rangle, \langle\langle s, \langle et, t \rangle \rangle, t \rangle \rangle$. Where we had e in (179), this has the type of the intension of a generalized quantifier. (It is not clear exactly who should be credited with this idea. D. Dowty ('Governed transformations as lexical rules in a Montague Grammar,' LI 1978) has an analogous entry for ECM ("raising-to-object") verbs, but his entry for raising-to-subject verbs has the simpler type in (179). Maybe the earliest published application to modal auxiliaries and raising-to-subject verbs is in E. Klein & I. Sag (1982) "Semantic Type and Control," in M. Barlow et al. (eds.) Developments in Generalized Phrase Structure Grammar, Bloomington: Indiana Linguistics Club. Anyway, the idea was widely familiar by the early 1980s. See e.g. the discussion in ch. IV, sec. 9, of Chierchia's thesis (G. Chierchia, Topics in the Syntax and Semantics of Infinitives and Gerunds, UMass Amherst Ph.D. thesis, GLSA 1984), and in D. Dowty (1985) 'On recent analyses of the semantics of control,' L&P 8.)

I leave it as an exercise to show that this fancier type accommodates *de dicto* readings without raising or reconstruction. A *prima facie* problem that arises in exchange is that only *de dicto* readings are generated. A follow-up exercise is to solve this problem. See the references cited above.

5.2 Reminder: standard tests for control and raising

In introductory syntax texts, the distinction between Raising predicates and Control predicates is often motivated by a battery of "tests":

	<i>raising</i>	<i>control</i>
<i>selectional restrictions</i>	imposed by lower verb only	imposed by both verbs
<i>passivization</i>	preserves truth-conditions	changes truth-conditions
<i>expletive subjects</i>	okay	impossible
<i>de dicto subjects</i>	possible	impossible

See e.g. Radford (1988).⁷ Here are some examples to remind you of the data that the table above is intended to summarize.

Selectional restrictions:

- (192) (a) **John likes physics.**
 (b) **#This number likes physics.**
 (c) **This number is divisible by 5.**
 (d) **#John is divisible by 5.**
- (193) (a) **John seems to like physics.**
 (b) **#This number seems to like physics.**
 (c) **This number seems to be divisible by 5.**
 (d) **#John seems to be divisible by 5.**
- (194) (a) **John tries to like physics.**
 (b) **#This number tries to like physics.**
 (c) **#This number tries to be divisible by 5.**
 (d) **#John tries to be divisible by 5.**

Passivization:

- (195) **Mary is likely to hire John.**
John is likely to be hired by Mary.
 (equivalent)

⁷To be more accurate, only the first three of these tests are found in Radford and other books on that level. The '*de dicto* subjects' test is normally omitted, since it would be harder to explain to readers with no knowledge of semantics. But it is found in the original literature on which these textbooks draw (see for example May (1977)).

- (196) **Mary is eager to hire John.**
 John is eager to be hired by Mary.
 (not equivalent)

Expletives and idiom chunks:

- (197) (a) **There seem to be two people in the booth.**
 (b) **The cat seems to be out of the bag.**
- (198) (a) ***There tried to be two people in the booth.**
 (b) **The cat tried to be out of the bag.** (only non-idiomatic)

De dicto readings:

- (199) **Several accomplices appeared to be involved.**
 (But in reality, there weren't any accomplices.)
- (200) **Several accomplices wanted to be involved.**
 (#But in reality, there weren't any accomplices.)

Exercise: How does the raising analysis that we have favored account for the behavior of raising predicates under the first three of these tests? (We have already answered the question for test number four.) Where necessary, state appropriate auxiliary assumptions about what it means to be an "expletive" or an "idiom chunk".

What about a non-raising analysis along the lines of (179) (adapted here to *seem*, *appear*, *be likely* etc., but crucially keeping the semantic type the same, i.e., $\langle\langle s, et \rangle, et \rangle$)? We have already seen that this fails to capture the existence of *de dicto* readings. What about the behavior of raising verbs under the other three tests?

5.3 Raising, control, and constraints on the lexicon

We have seen that a non-raising analysis using type $\langle\langle s, et \rangle, et \rangle$ is not empirically adequate for the modals and other raising verbs that we have looked at. It fails to account for *de dicto* readings and expletive subjects. So as far as accounting for the data of English (at least as far as we have looked at them) we can just forget about it. But there is a different and deeper question to consider. As linguists we are not merely concerned with finding the right analysis to predict the behavior of a given set of lexical items. We also aim to make predictions about the range of possible lexical items allowed by Universal Grammar. So, for example, we must look again at the already discarded type- $\langle\langle s, et \rangle, et \rangle$ entry for **must** and ask ourselves: Granted that this isn't the meaning of **must** – could it still be the meaning of some verb or adjective, in English or in some other natural language? Are there any words out there that do behave in precisely the way that **must** would have had to for us to maintain this entry for it? And if not, why not?

So suppose there were a verb **xxx** with just the lexical entry we entertained in section 5.1 for **must**, repeated here from (179):

$$(216) \quad [[\mathbf{xxx}]]^{w,[R \rightarrow R]} = \lambda P_{\langle s,et \rangle}. \lambda x_e. \forall w' [w' \in R(w) \rightarrow P(w')(x) = 1]$$

How would this verb behave in regard to the tests that are commonly employed to distinguish so-called "raising" verbs from so-called "control" verbs? We already saw in section 5.1 that it would never allow *de dicto* readings for its subject, and in this respect it would look like a "control" verb. What about the other tests?

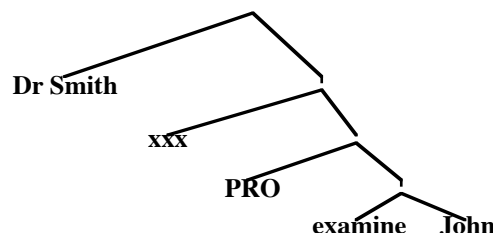
Another characteristic of "control" verbs is that active-passive pairs like the one in (217) are truth-conditionally non-equivalent (in contrast with analogous pairs with "raising" predicates like (218), which are always equivalent).

- (217) (a) Doctor Smith hopes to examine John.
(b) John hopes to be examined by doctor Smith.

- (218) (a) Doctor Smith is likely to examine John.
(b) John is likely to be examined by doctor Smith.

How will our hypothetical verb **xxx** behave in this regard? The two LFs for the active-passive pair will look as follows:⁸

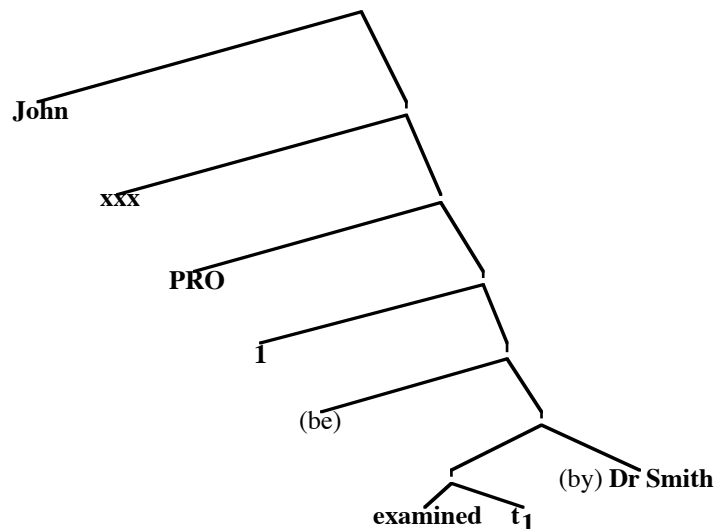
(219)



⁸We are assuming a movement analysis of the passive here, on which the passive morphology is semantically vacuous. An alternative would be a lexical analysis, which treats the passive morpheme as a relation-changing operation ($\lambda f_{\langle e,et \rangle}. \lambda x. \lambda y. f(y)(x)$) and base-generates the two argument DPs in their surface hierarchical order. This would not make any difference to the discussion in this section.

Notice, by the way, that if we did not have a PRO-subject in the complement of **xxx** (but no subject at all, not even a semantically vacuous one), then the movement analysis would be unavailable to us here and we would be forced to choose the lexical analysis of passives. This is the reason why many authors conclude that a non-raising analysis of "raising" verbs is incompatible with a movement analysis of passive. The conclusion may hold on their assumptions, but not in the context of the H&K treatment of PRO (where PRO itself is vacuous, but capable of leaving a non-vacuous trace when moving).

(220)



Calculating the interpretation up to the step that depends on the lexical entry for **xxx**, we know that (219) is true in w iff $[[\mathbf{xxx}]]^w.[\mathbf{R} \rightarrow \mathbf{R}](\lambda w'. \lambda x. x \text{ examines John in } w')(Smith) = 1$, and that (220) is true in w iff $[[\mathbf{xxx}]]^w.[\mathbf{R} \rightarrow \mathbf{R}](\lambda w'. \lambda x. Smith \text{ examines } x \text{ in } w')(John) = 1$. Given the entry for **xxx** in (1), and given that, for all w' , $[\lambda x. x \text{ examines John in } w'](Smith) = [\lambda x. Smith \text{ examines } x \text{ in } w'](John)$, it follows that $[[\mathbf{xxx}]]^w.[\mathbf{R} \rightarrow \mathbf{R}] = [[\mathbf{xxx}]]^w.[\mathbf{R} \rightarrow \mathbf{R}]$. So the truth-conditions of the two structures (in a given utterance context) are identical. In the passive test, then, our hypothetical verb **xxx** is predicted to act like a "raising" verb.

A caveat is in order here: The prediction that (219) and (220) are equivalent means only that their truth-conditions will coincide if they are evaluated w.r.t. to the same contextually supplied accessibility relation. If (219) were used in a context which supplies one accessibility relation R_1 , and (220) in a context which supplies a different one, R_2 , then of course they could well differ in truth-value. For example, it may happen that the active sentence (219) is uttered with the tacit understanding that we are quantifying over those possible worlds in which Dr Smith fulfills his duties, and that the passive sentence (220) is uttered with the understanding that we are talking about those worlds in which John fulfills his duties. Then these two utterances will express different propositions, and maybe one of them is true and the other false.

This implies that we will have to be very careful when we evaluate speaker's judgments as to whether a given verb does or doesn't pass the equivalence-under-passivization test. If there is (suspected) context-dependency of the accessibility relation, we'll have to make sure that people are really resolving it in the same way for the two sentences. If we just present the sentences out of context, this should not be taken for granted. People will then have to exercise their imagination to fill in a natural context, and in doing so they may well be influenced in a roundabout way by the very fact that one sentence is in the active voice and the other one in the passive. Passivization, even though it doesn't affect truth-conditions (in simple sentences), does have some effect on non-truth-conditional aspects of meaning or discourse-coherence. These effects are not well understood, but there is, speaking very roughly and vaguely, a *ceteris paribus* tendency for the surface subject to denote the topic of the discourse. This might indirectly affect the relative salience of different competing candidates for the accessibility relation. In other

words, if Dr Smith is referred to with the subject of the sentence, and therefore is perceived as the discourse topic, then the accessibility relation which is defined in terms of Dr Smith's duties is *ceteris paribus* more salient than the one defined in terms of John's duties. So a verb with the semantics defined in (216) may appear to fail the equivalence-under-passivization test, due to an indirect chain of connections between the discourse function of passivization and the strategies for the resolution of context-dependence. (And, for the same reason, even a verb with the simpler type <st,t> entry that is our official proposal for **must-R** may appear to fail it!)

However, even if this effect is quite strong and systematic, we can still tell the difference between a verb like **xxx**, which guarantees equivalence under passivization in a fixed context, and a verb whose meaning is defined in such a way that it "hard-wires" a distinctive contribution of the subject to the truth-conditions. The difference will be that we can, in principle, give independent contextual clues about the intended accessibility relation and thereby counteract and override the effect of the active/passive choice.⁹

Let us return now to the main thread of our discussion. What do we learn from our investigation of the predicted behavior of our hypothetical verb **xxx** w.r.t. to standard diagnostics for "control" and "raising"? We could continue to proceed through the whole list of tests, but already we have seen enough to conclude that **xxx** displays a mixed pattern of behavior w.r.t. these standard diagnostics: On at least one test (availability of *de dicto* readings), it acts "control"-like, and on at least one other one (equivalence under passivization), it acts "raising"-like. This is interesting, because it makes **xxx** a counterexample to an assumption which is widely shared (though often left implicit) in the syntactic literature, namely the assumption that the characteristics targeted by the standard tests "cluster together"; in other words, any given lexical item will either act "raising"-like on all test, or else act "control"-like on all tests.¹⁰ Let us call this the "Clustering Assumption". More precisely, **xxx** is relevant to this assumption in the following way: First of all, the very fact that we were able to write down an explicit and coherent lexical entry like the one for **xxx** in (216) shows that the Clustering Assumption is not conceptually necessary, but rather constitutes a substantive empirical generalization. Given this, we now are motivated to look for real counterexamples in the vocabularies of the world's languages, and the hypothetical

⁹See Bhatt 1998 (Rajesh Bhatt, "Obligation and Possession," in H. Harley (ed.) MITWPL 32: *Papers from the UPenn/MIT Roundtable on Argument Structure and Aspect*, pp. 21 - 40. [esp. section 4]) for related discussion. Giving proper attention to the complexities of strategies for the resolution of context-dependence may also help us make some sense of the inconclusive evidence presented by Jackendoff (1972; pp. 104f.). See also Brennan 1993 (Virginia Brennan, *Root and Epistemic Modal Auxiliary Verbs*. Ph.D. Dissertation, University of Massachusetts at Amherst. [Chapters 1 and 2 on the argument structure of various kinds of modal auxiliaries]).

¹⁰This is not meant to exclude the possibility that a given word may be ambiguous between raising and control meanings. (Many authors in fact have posited pervasive systematic ambiguity of this sort; see e.g. Brennan 1993 and references cited there for modal auxiliaries, and Jacobson 1992 and references cited there for main verbs like 'promise,' 'permit', etc.) The assumption stated says that such an ambiguous word will act consistently raising-like on one of its readings, and consistently control-like on the other reading. This is not the same as displaying control behavior as well as raising behavior on one given reading. (Though admittedly the difference will not be easy to detect in practice.)

example of **xxx** gives us some concrete idea of what we should be looking for. And if this search turns out to be unsuccessful (i.e., we don't find real counterexamples), then the example of **xxx** will give us some guidance in our endeavor to identify the principle(s) of Universal Grammar from which the Clustering Assumption follows.

Let us skip here over the survey of known data and the many non-trivial problems in the interpretation of that data, and let us proceed on the assumption that the Clustering Assumption is empirically correct. This means that **xxx**, as interpreted in (216) above, is not a possible word in natural language. Why not?

Two kinds of answers come to mind. One conceptually attractive hypothesis is that there are simply no lexical items of type $\langle\langle s, et \rangle, et \rangle$ – perhaps more generally no lexical items with any arguments of types other than e or $\langle s, t \rangle$. This has been proposed (most recently, to my knowledge by Larson, den Dikken & Ludlow¹¹), but rejected by many because it rules out a widely favored analysis of control verbs (most prominently defended in Chierchia 1984). Another answer is that, even though $\langle\langle s, et \rangle, et \rangle$ is a possible lexical type, there is a relevant universal constraint against meanings of this type with a certain formal property ...

¹¹ see <http://semlab5.sbs.sunysb.edu/~rlarson/larson-papers.html>, listed under "in progress, 1997"

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CHAPTER SEVEN

THE THIRD READING

In this chapter, we will see that quantificational noun phrases in the scope of a modal operator can receive a reading where their restrictive predicate is not interpreted in the worlds introduced by the modal operator (which is what happens in specific readings as well) while at the same time their quantificational force takes scope below the modal operator (which is what happens in non-specific readings as well). This seemingly paradoxical situation might force whole-sale revisions to our architecture. We discuss the standard solution (which involves supplying predicates with world-arguments).

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7.1 A Problem

Janet Dean Fodor discussed examples like (1) in her dissertation (1970).

(1) Mary wanted to buy a hat just like mine.

Fodor observes that (1) has three readings, which she labels “specific transparent,” “non-specific transparent,” and “non-specific opaque.”

- (i) On the “specific transparent” reading, the sentence says that there is a particular hat which is just like mine such that Mary has a desire to buy it. Say, I am walking along Newbury Street with Mary. Mary sees a hat in a display window and wants to buy *it*. She tells me so. I don’t reveal that I have one just like it. But later I tell *you* by uttering (1).

- (ii) On the “non-specific opaque” reading, the sentence says that Mary’s desire was to buy some hat or other which fulfills the description that it is just like mine. She is a copycat.
- (iii) On the “non-specific transparent” reading, finally, the sentence will be true, e.g., in the following situation: Mary’s desire is to buy some hat or other, and the only important thing is that it be a Red Sox cap. Unbeknownst to her, my hat is one of those as well.

The existence of three different readings appears to be problematic for the scopal account of specific/non-specific ambiguities that we have been assuming. It seems that our analysis allows just two semantically distinct types of LFs: Either the DP *a hat just like mine* takes scope below *want*, as in (2), or it takes scope above *want*, as in (3).

(2) Mary wanted [[a hat-just-like-mine]_i [PRO to buy t_i]]

(3) [a hat-just-like-mine]_i [Mary wanted [PRO to buy t_i]]

In the system we have developed so far, (2) says that in every world *w'* in which Mary gets what she wants, there is something that she buys in *w'* that’s a hat in *w'* and like my hat in *w'*. This is Fodor’s “non-specific opaque” reading. (3), on the other hand, says that there is some thing *x* which is a hat in the actual world and like my hat in the actual world, and Mary buys *x* in every one of her desire worlds. That is Fodor’s “specific transparent.” But what about the “non-specific transparent” reading? To obtain this reading, it seems that we would have to evaluate the predicate *hat just like mine* in the actual world, so as to obtain its actual extension (in the scenario we have sketched, the set of all Red Sox caps). But the existential quantifier expressed by the indefinite article in the *hat*-DP should not take scope over the modal operator *want*, but below it, so that we can account for the fact that in different desire-worlds of Mary’s, she buys possibly different hats.

There is a tension here: one aspect of the truth-conditions of this reading suggests that the DP *a hat just like mine* should be *outside* of the scope of *want*, but another aspect of these truth-conditions compels us to place it *inside* the scope of *want*. We can’t have it both ways, it would seem, which is why this has been called a “scope paradox”

Another example of this sort, due to [Bäuerle \(1983\)](#), is (4):

- (4) Georg believes that a woman from Stuttgart loves every member of the VfB team.

Bäuerle describes the following scenario: Georg has seen a group of men on the bus. This group happens to be the VfB team (Stuttgart’s soccer team), but Georg does not know this. Georg also believes (Bäuerle doesn’t spell out on what grounds) that there is some woman from Stuttgart who loves every one of these men. There is no particular woman of whom he believes that, so there

are different such women in his different belief-worlds. Bäuerle notes that (4) can be understood as true in this scenario. But there is a problem in finding an appropriate LF that will predict its truth here. First, since there are different women in different belief-worlds of Georg's, the existential quantifier *a woman from Stuttgart* must be inside the scope of *believe*. Second, since (in each belief world) there aren't different women that love each of the men, but one that loves them all, the *a*-DP should take scope over the *every*-DP. If the *every*-DP is in the scope of the *a*-DP, and the *a*-DP is in the scope of *believe*, then it follows that the *every*-DP is in the scope of *believe*. But on the other hand, if we want to capture the fact that the men in question need not be VfB-members in Georg's belief-worlds, the predicate *member of the VfB team* needs to be outside of the scope of *believe*. Again, we have a "scope paradox".

Before we turn to possible solutions for this problem, let's have one more example:

- (5) Mary hopes that a friend of mine will win the race.

This again seems to have three readings. In Fodor's terminology, the DP *a friend of mine* can be "non-specific opaque," in which case (5) is true iff in every world where Mary's hopes come true, there is somebody who is my friend and wins. It can also have a "specific transparent" reading: Mary wants John to win, she doesn't know John is my friend, but I can still report her hope as in (5). But there is a third option, the "non-specific transparent" reading. To bring out this rather exotic reading, imagine this: Mary looks at the ten contestants and says *I hope one of the three on the right wins - they are so shaggy - I like shaggy people*. She doesn't know that those are my friends. But I could still report her hope as in (5).

7.2 The Standard Solution: Overt World Variables

The scope paradoxes we have encountered can be traced back to a basic design feature of our system of intensional semantics: the relevant "evaluation world" for each predicate in a sentence is strictly determined by its LF-position. All predicates that occur in the (immediate) scope of the same modal operator must be evaluated in the same possible worlds. E.g. if the scope of *want* consists of the clause *a friend of mine (to) win*, then every desire-world w' will be required to contain an individual that wins in w' and is also my friend *in* w' . If we want to quantify over individuals that are my friends in the actual world (and not necessarily in all the subject's desire worlds), we have no choice but to place *friend of mine* outside of the scope of *want*. And if we want to accomplish this by means of QR, we must move the entire DP *a friend of mine*.

Not every kind of intensional semantics constrains our options in this way. One way to visualize what we might want is to write down an LF that looks promising:

(6) Mary wanted_{w_o}[$\lambda w'$ [a hat-just-like-mine _{w_o}] λx_1 [PRO to buy_{w'}x₁]]

We have annotated each predicate with the world in which we wish to evaluate it. w_o is the evaluation world for the entire sentence and it is the world in which we evaluate the predicates *want* and *hat-just-like-mine*. The embedded sentence contributes a function from worlds to truth-values and we insert an explicit λ -operator binding the world where the predicate *buy* is evaluated. The crucial aspect of (6) is that the world in which *hat-just-like-mine* is evaluated is the matrix evaluation world and not the same world in which its clause-mate predicate *buy* is evaluated. This LF thus looks like it might faithfully capture Fodor's third reading.

Logical forms with overt world variables such as (6) are in fact the standard solution to the problem presented by the third reading. Let us spell out some of the technicalities. Later, we will consider a couple of alternatives.

We return to the basic system used in Heim & Kratzer up to chapter II. The interpretation function is relativized only to an assignment function, not to any other evaluation parameters such as a world, a time, or an index. The semantic rules are Functional Application, Predicate Abstraction, and Predicate Modification, in their formulations from the earlier part of H&K. There is no rule of Intensional Functional Application. The only ingredient of intensional semantics that we do retain is the expanded type system and ontology. We have a third basic type besides e and t , the type s . D_s is the set of all indices, for now possible worlds (later: world-time pairs).

There are a number of innovations in the lexicon and in the syntax. As for the lexicon, the main change concerns the treatment of predicates (verbs, nouns, adjectives). They now all get an additional argument, of type s .

The decision to make the world-argument the predicate's first (lowest) argument is arbitrary, and nothing hinges on it. For all we know, it could be the highest argument, or somewhere in between.

- (7) a. $\llbracket \text{smart} \rrbracket = \lambda w \in D_s. \lambda x \in D_e. x \text{ is smart in } w$
 b. $\llbracket \text{likes} \rrbracket = \lambda w \in D_s. \lambda x \in D_e. \lambda y \in D_e. y \text{ likes } x \text{ in } w$
 c. $\llbracket \text{teacher} \rrbracket = \lambda w \in D_s. \lambda x \in D_e. x \text{ is a teacher in } w$
 d. $\llbracket \text{friend} \rrbracket = \lambda w \in D_s. \lambda x \in D_e. \lambda y \in D_e. y \text{ is } x\text{'s friend in } w$

This also applies to attitude predicates, modals, and tenses. We illustrate with *believe* and *must*:

- (8) a. $\llbracket \text{believe} \rrbracket = \lambda w \in D_s. \lambda p \in D_{\langle s, t \rangle}. \lambda x \in D.$
 $\quad \forall w' [w' \text{ conforms to what } x \text{ believes in } w \rightarrow p(w') = 1]$
 b. $\llbracket \text{must} \rrbracket = \lambda w \in D_s. \lambda R \in D_{\langle s, st \rangle}. \lambda p \in D_{\langle s, t \rangle}.$
 $\quad \forall w' [R(w)(w') = 1 \rightarrow p(w') = 1]$

Note that predicates (ordinary ones and modal ones), like the ones in (7) and (8) now have as their semantic values what used to be their *intensions*.

There is no change to the entries of proper names, determiners, or truth-functional connectives; these keep their purely extensional (“s-free”) types and meanings:

- (9) a. $\llbracket \text{Ann} \rrbracket = \text{Ann}$
 b. $\llbracket \text{and} \rrbracket = \lambda u \in D_t. [\lambda v \in D_t. u = v = 1]$
 c. $\llbracket \text{the} \rrbracket = \lambda f \in D_{\langle e, t \rangle} : \exists! x. f(x) = 1. \text{ the } y \text{ such that } f(y) = 1.$
 d. $\llbracket \text{every} \rrbracket = \lambda f \in D_{\langle e, t \rangle}. \lambda g \in D_{\langle e, t \rangle}. \forall x [f(x) = 1 \rightarrow g(x) = 1]$

So, let’s start analyzing a simple sentence.

- (10) $[_{VP} \text{ John leaves}]$

The verb’s type is $\langle s, et \rangle$, so it’s looking for a sister node which denotes a *world*. *John*, which denotes an individual, is not a suitable argument.

We get out of this problem by adding a couple of items to our lexicon, which are abstract (unpronounced) morphemes. One is a series of pronouns of type s (“index pronouns” or, for now, “world pronouns”). In this chapter, we will write them as w_n , with a numerical subscript n , or even as w, w', w'' . (Later, we sometimes might write them as *pro* _{n} and rely on context to make clear we are not referring to an individual.) Their semantics is what you expect: they get values from the assignment function.

We will stipulate that a complete (matrix) sentence must not contain any free variables of type s and must receive a denotation of type $\langle s, t \rangle$.¹ This means that we need binders of world pronouns. Many proposals in this line of thought help themselves to freely inserted covert binders. We will follow H&K in not doing that. Instead we posit one more lexical item, analogous to the covert vacuous operator *PRO* of type e in H&K (pp.227–228): a semantically vacuous operator, *OP*, which moves and leaves a trace of type s . Its syntactic properties are such that it must end up in *C* or right below a functional head in the “clausal spine” between *C* and *V*, and it must get there by a very short movement, a kind of “head movement”. We are leaving this rather vague.

So, our sentence *John leaves* contains *OP*, generated as the first sister of the verb and then moved to the “top” of the sentence:

¹ In the 2016 edition of this class, Suzana Fong noted that this stipulation is *prima facie* less appealing than the alternative assumption that type- s pronouns are exactly like type- e pronoun in every respect, including the ability to remain free and get values from a contextually supplied assignment. Irene tried to sketch some principled reason why it might not be possible to refer to a specific world other than the world one is in. But as Mitya Privoznov pointed out, a similar idea is not plausible for times, given the existence of temporal deictics like *then*. So at best there might be a principled reason why the world-coordinate of a free index-pronoun would always have to be w_u . Irene had to concede therefore that the ban against free index-pronouns was just a stipulation. We want to think more about (a) whether we really need it, and (b) if we do, what might explain it.

we leave off most of the bracketing and start writing the world arguments as subscripts to the predicates):

- (16) a. non-specific opaque:
 $OP\ 1\ Mary\ wants_{w_1}\ [\ OP\ 2\ a\ friend-of-mine_{w_2}\ leave_{w_2}]$
- b. specific transparent:
 $OP\ 1\ a\ friend-of-mine_{w_1}\ 3\ Mary\ wants_{w_1}\ [\ OP\ 2\ t_3\ leave_{w_2}]$
- c. non-specific transparent:
 $OP\ 1\ Mary\ wants_{w_1}\ [\ OP\ 2\ a\ friend-of-mine_{w_1}\ leave_{w_2}]$

So, instead of writing t_1
 for a trace of type s that
 serves as the first argument of
leaves, say, we write “ $leaves_{w_1}$ ”

Notice that the third reading is minimally different from the first reading: all that happened is the choice to co-index the world argument of *friend of mine* with the matrix *OP*.

In this new framework, then, we have a way of resolving the apparent “scope paradoxes” and of acknowledging Fodor’s point that there are two separate distinctions to be made when DPs interact with modal operators. First, there is the scopal relation between the DP and the operator; the DP may take wider scope (Fodor’s “specific” reading) or narrower scope (“non-specific” reading) than the operator. Second, there is the choice of binder for the world-argument of the DP’s restricting predicate; this may be cobound with the world-argument of the embedded predicate (Fodor “opaque”) or with the modal operator’s own world-argument (“transparent”). So the transparent/opaque distinction in the sense of Fodor is not *per se* a distinction of scope; but it has a principled connection with scope in one direction: Unless the DP is within the modal operator’s scope, the opaque option (= co-binding the world-pronoun with the embedded predicate’s world-argument) is in principle unavailable. (Hence “specific” implies “transparent”, and “opaque” implies “non-specific”.) But there is no implication in the other direction: if the DP has narrow scope w.r.t. to the modal operator, either the local or the long-distance binding option for its world-pronoun is in principle available. Hence “non-specific” readings may be either “transparent” or “opaque”.

EXERCISE 7.2: For DPs with extensions of type e (specifically, DPs headed by the definite article), there is a truth-conditionally manifest transparent/opaque distinction, but no truth-conditionally detectable specific/non-specific distinction. In other words, if we construct LFs analogous to (16)[a-c] above for an example with a definite DP, we can always prove that the first option (wide scope DP) and the third option (narrow scope DP with distantly bound world-pronoun) denote identical propositions. In this exercise, you are asked to show this for the example in (17).

- (17) John believes that your abstract will be accepted. \square

7.3 The third reading with conditionals and modals

So, far our examples of the third reading have all been with attitude predicates but the phenomenon can also be observed in conditionals and with modals. A famous example is due to [Abusch 1994](#):

- (18) Things would be different if every senator had grown up to be a rancher instead.

What makes conditionals different is that the *if*-clause is a scope island for quantifiers so that *every senator* cannot QR scope out of the *if*-clause in (18). But the question of whether its predicate, *senator*, is interpreted in the matrix evaluation world (“transparent”) or in the worlds that *if* takes us to (“opaque”) remains open. Abusch’s example is constructed to heavily favor the transparent reading.

[Percus 2000](#) provides a clever minimal pair that shows the expected ambiguity:

- (19) a. If every semanticist owned a villa in Tuscany, there would be no field at all.
 b. If I were a syntactician and if every semanticist owned a villa in Tuscany, I would be quite envious.

We can also see the ambiguities at work in modal sentences:

- (20) a. It could have been that everyone inside was outside.
 b. Everyone inside is permitted to be outside.

These latter examples are from [Yalcin 2015](#), who proceeds to discuss the very puzzling fact that transparent readings do not seem to be available in certain “epistemic” contexts, neither with indicative conditionals nor modals.

7.4 Binding Theory for World Variables

One could in principle imagine some indexings of our LFs that we have not considered so far. In a system (unlike ours) where one freely inserts “ λw ” operators on top of every clause, one could generate the following LF, which indexes the predicate of the complement clause to the matrix λ -operator rather than to the one on top of its own clause.

- (21) λw_o John wants _{w_o} [λw_i PRO leave _{w_o}]

Of course, the resulting semantics would be pathological: what John would be claimed to stand in the wanting relation to is a set of worlds that is either the entire set W of possible worlds (if the evaluation world is one in which John leaves) or the empty set (if the evaluation world is one in which John doesn't leave). Clearly, the sentence has no such meaning. Would we need to restrict our system to not generate such an LF? Perhaps not, if the meaning is so absurd that the LF would be filtered out by some overarching rules distinguishing sense from nonsense. Nevertheless, it is gratifying to note that this kind of LF is unavailable in our system: the only place where the lower world-binder OP could originate is as a sister to *leave* and moving it to the lower CP (where we need a proposition to feed to *want*) would by necessity make it bind the world argument of *leave*.

But there are real problems when we look at more complex examples. Here is one discussed by Percus in important work (Percus 2000):

(22) Mary thinks that my brother is Canadian.

Since the subject of the lower clause is a type e expression, we expect at least two readings: opaque and transparent, cf. Exercise 7.2. The two LFs are as follows:

- (23) a. opaque
 $OP \circ \text{Mary thinks}_{w_o} [(\text{that}) OP \text{I my brother}_{w_i} (\text{is}) \text{Canadian}_{w_i}]$
 b. transparent
 $OP \circ \text{Mary thinks}_{w_o} [(\text{that}) OP \text{I my brother}_{w_o} (\text{is}) \text{Canadian}_{w_i}]$

But as Percus points out, there is another indexing that might be generated:

(24) $OP \circ \text{Mary thinks}_{w_o} [(\text{that}) OP \text{I my brother}_{w_i} (\text{is}) \text{Canadian}_{w_o}]$

In (24), we have co-indexed the main predicate of the lower clause with the matrix λ -operator and co-indexed the nominal predicate *brother* with the embedded λ -operator. That is, in comparison with the transparent reading in (23b), we have just switched around the indices on the two predicates in the lower clause.

Note that this LF will not lead to a pathological reading. So, is the predicted reading one that the sentence actually has? No. For the transparent reading, we can easily convince ourselves that the sentence does have that reading. Here is Percus' scenario: "My brother's name is Allon. Suppose Mary thinks Allon is not my brother but she also thinks that Allon is Canadian." In such a scenario, our sentence can be judged as true, as predicted if it can have the LF in (23b). But when we try to find evidence that (24) is a possible LF for our sentence, we fail. Here is Percus:

If the sentence permitted a structure with this indexing, we would take the sentence to be true whenever there is some *actual* Canadian who *Mary thinks* is my brother — even when this person is not my brother in actuality, and *even when Mary mistakenly thinks that he is not Canadian*. For instance, we would take the sentence to be true

when Mary thinks that Pierre (the Canadian) is my brother and naturally concludes — since she knows that *I* am American — that Pierre too is American. But in fact we judge the sentence to be *false* on this scenario, and so there must be something that makes the indexing in (24) impossible.

Percus then proposes the following descriptive generalization:

- (25) GENERALIZATION X: The situation pronoun that a verb selects for must be coindexed with the nearest λ above it.

We expect that there will need to be a lot of work done to understand the deeper sources of this generalization. But note that we could implement the constraint in our system by brute force: the *OP* operator can only be generated as the sister of a main predicate, not as the sister of a predicate inside an argument nominal.

Percus works with situation pronouns rather than world pronouns, an immaterial difference for our purposes here.

7.5 Excursus: Semantic reconstruction revisited

Let us look back at the account of non-specific readings of raised subjects that we sketched earlier in Section 5.2.3. We showed that you can derive such readings by positing a high type trace for the subject raising, a trace of type $\langle s, \langle et, t \rangle \rangle$. Before the lower predicate can combine with the trace, the semantic value of the trace has to be extensionalized by being applied to the lower evaluation world (done via the EFA composition principle). Upstairs the raised subject has to be combined with the λ -abstract (which will be of type $\langle \langle s, \langle et, t \rangle \rangle, t \rangle$) via its intension.

We then saw data suggesting that syntactic reconstruction is actually what is going on. This, of course, raises the question of why semantic reconstruction is unavailable (otherwise we wouldn't expect the data that we observed).

In this excursus, we will briefly consider whether our new framework has something to say about this issue. Let's figure out what we would have to do in the new framework to replicate the account in the section on semantics reconstruction.

Downstairs, we would have a trace of type $\langle s, \langle et, t \rangle \rangle$. To calculate its extension, we do not need recourse to a special composition principle, but can simply give it a world-argument (co-indexed with the abstractor resulting from the movement of the *w-OP* in the argument position of the lower verb).

Now, what has to happen upstairs? Well, there we need the subject to be of type $\langle s, \langle et, t \rangle \rangle$, the same type as the trace, to make sure that its semantics will enter the truth-conditions downstairs. But how can we do this?

We need the DP *somebody from New York* to have as its semantic value an intension, the function from any world to the existential quantifier over individuals who are people from New York in that world. This is actually hard to do in our system. It *would* be possible if (i) the predicate(s) inside the DP

received *w*-PRO as their argument, and if (ii) that *w*-PRO were allowed to move to adjoin to the DP. If we manage to rule out at least one of the two preconditions on principled grounds, we would have derived the impossibility of semantic reconstruction as a way of getting non-specific readings of raised subjects.

- (i) may be ruled out by the Binding Theory for world pronominals, when it gets developed.
- (ii) may be ruled out by principled considerations as well. Perhaps, world-abtractors are only allowed at sentential boundaries.

See [Larson \(2002\)](#) for some discussion of recalcitrant cases, one of which is the object position of so-called intensional transitive verbs, a topic for another occasion.

7.6 Further reading

There is an interesting literature spawned by [Percus 2000](#):

Romoli

Keshet

Schwarz

Keshet and Schwarz

Fodor also discussed a fourth reading, specific opaque, which is hard to fit into our framework. Whether it really exists is a question discussed in some recent work:

Szabo

who else

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