

Introduction to Generative Models (and GANs)

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April. 2019

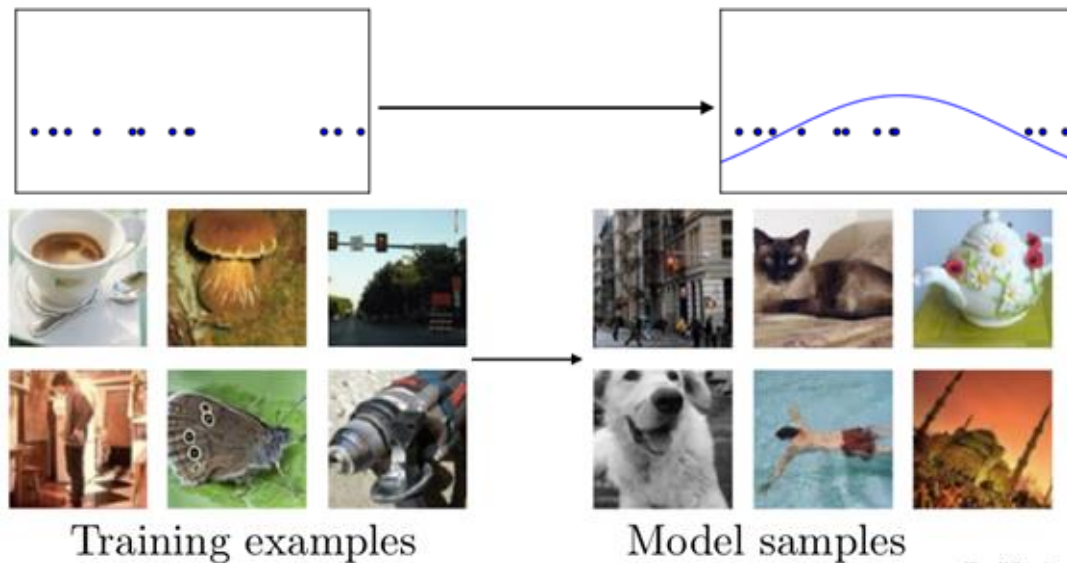
Agenda Today

- GAN
- 3D Reconstruction
- Misc topics in Computational Photography

Generative Models: Learning the Distributions

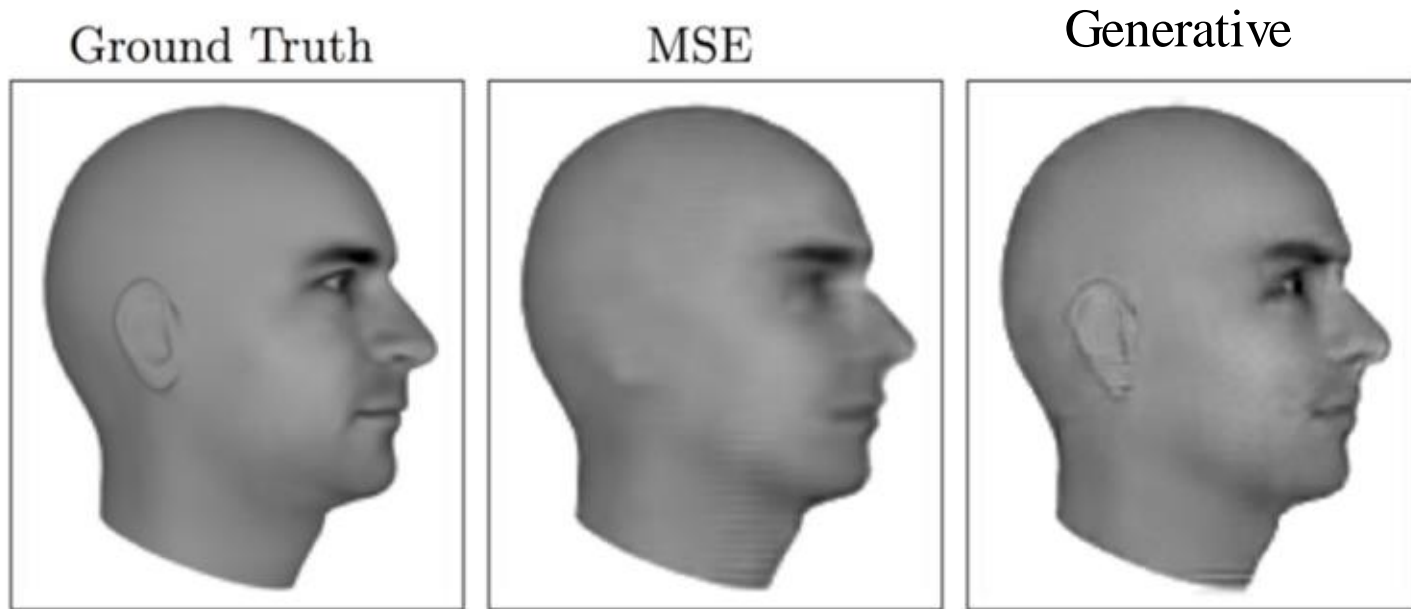
Discriminative: learns the likelihood

Generative: performs Density Estimation (learns the distribution) to allow sampling



Loss function for distribution: Ambiguity and the “blur” effect

MSE: a Discriminative model just smoothes all possibilities.



Ambiguity and the “blur” effect

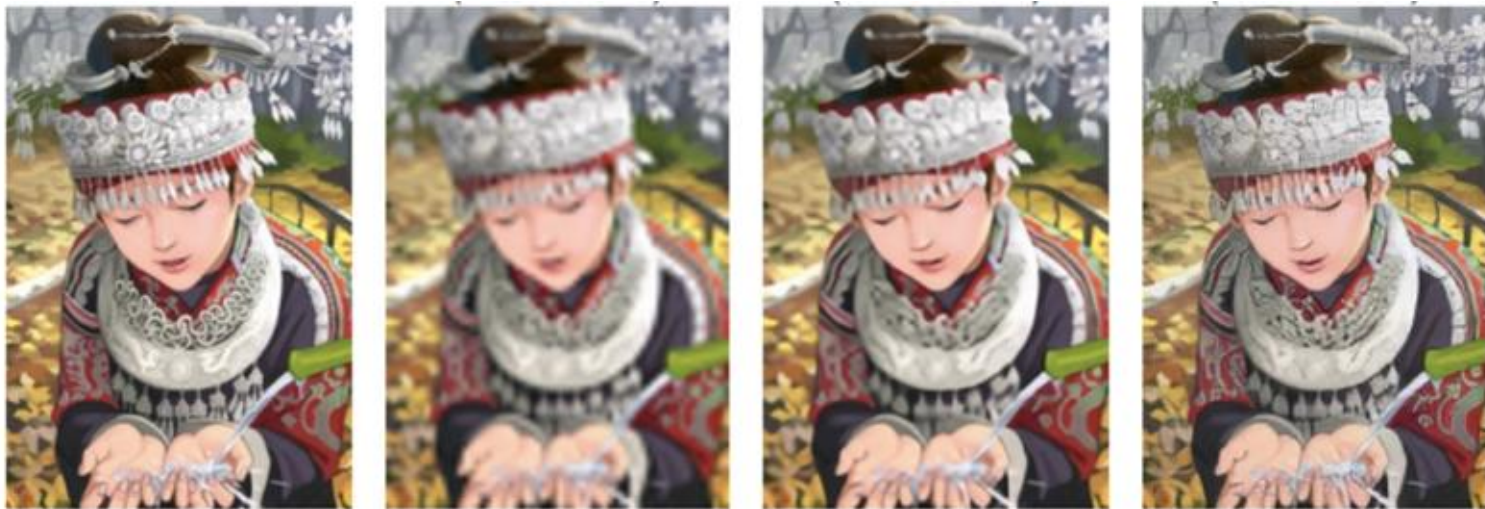


Photo-Realistic Single Image Super-Resolution Using a Generative Adversarial Network

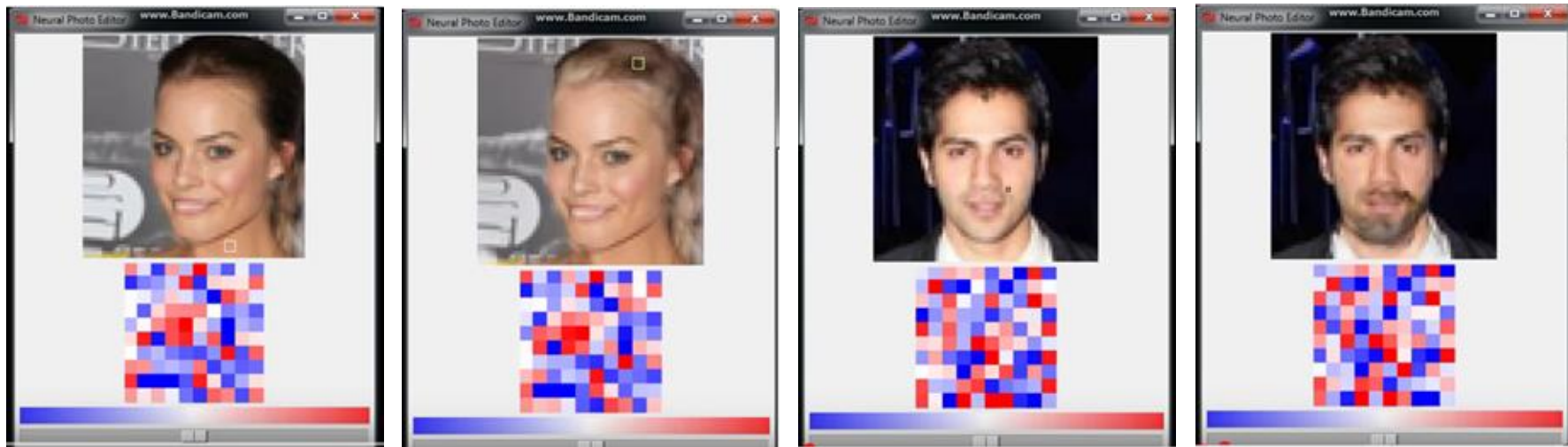
Example Application of Generative Models

Image Generation from Sketch



iGAN: Interactive Image Generation via Generative Adversarial Networks

Interactive Editing



Neural Photo Editing with Introspective Adversarial Networks

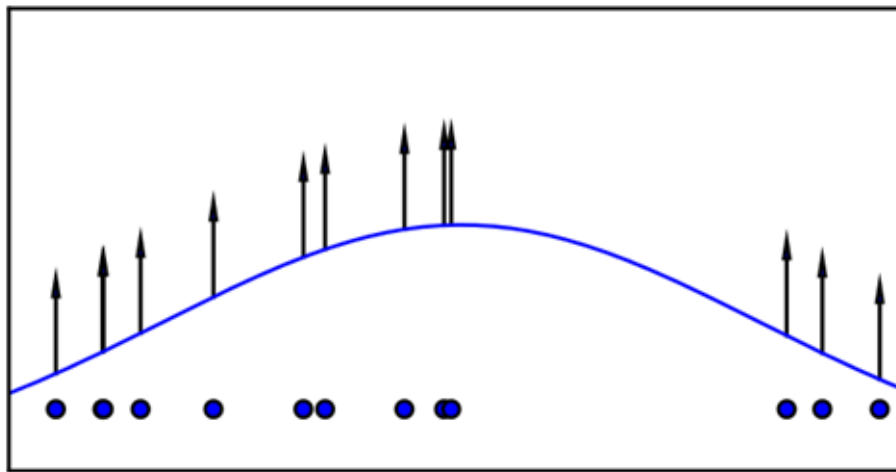
Figures adapted from NIPS 2016 Tutorial Generative Adversarial Networks

Image to Image Translation



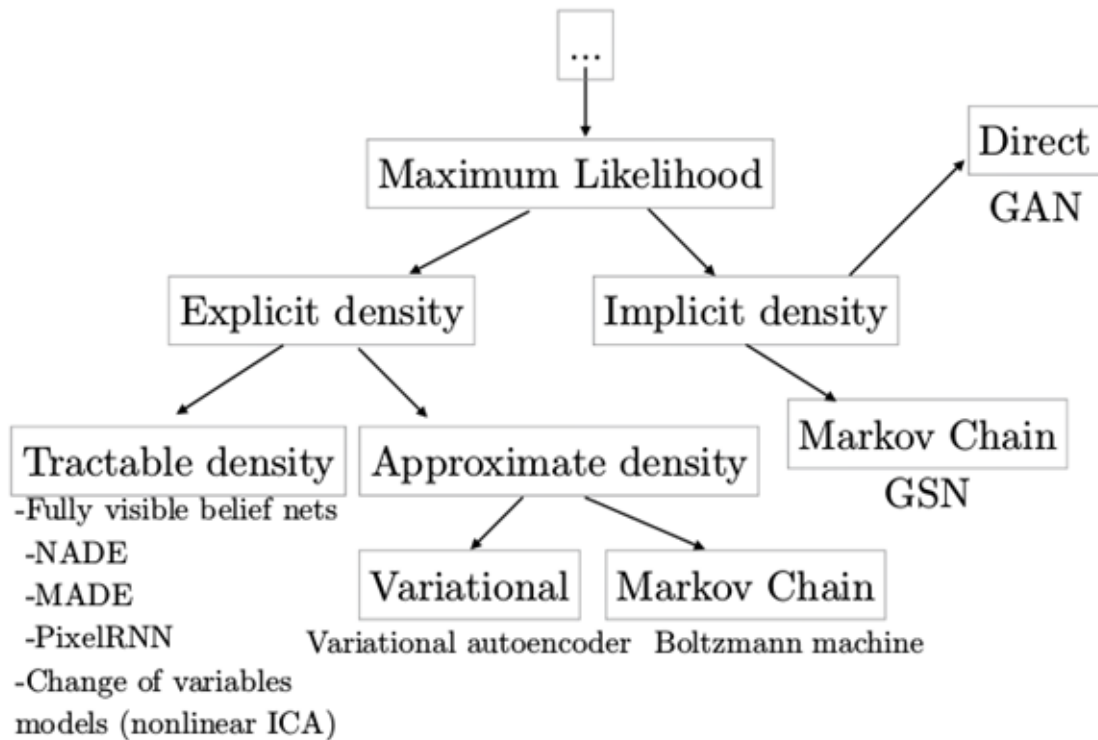
How Generative Models are Trained

Learning Generative Models

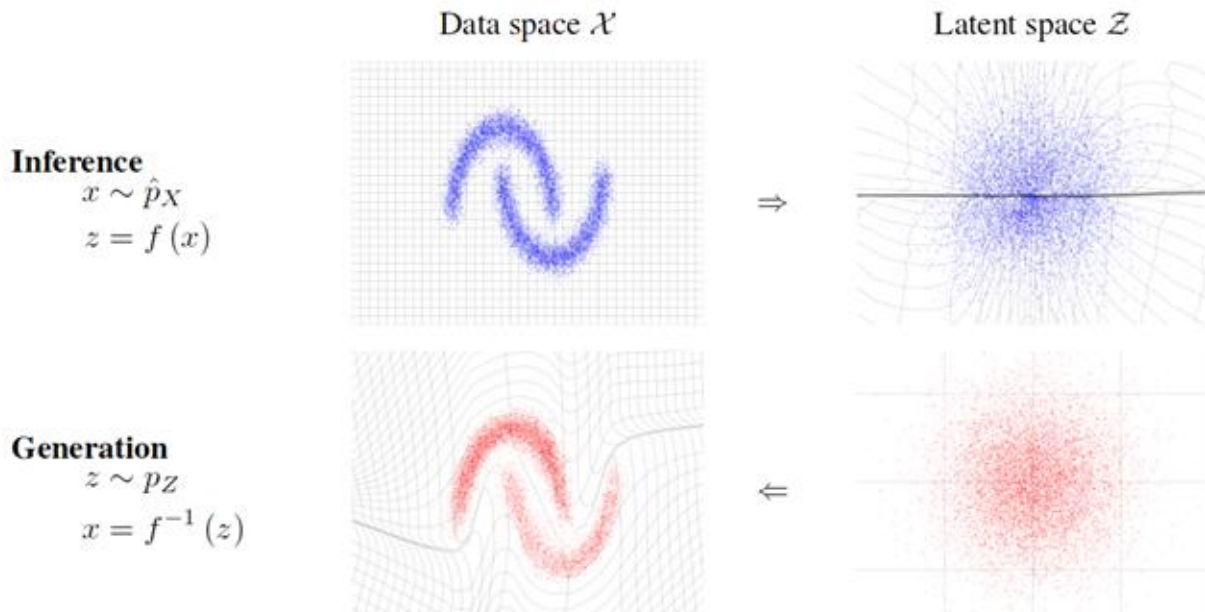


$$\theta^* = \arg \max_{\theta} \mathbb{E}_{x \sim p_{\text{data}}} \log p_{\text{model}}(x | \theta)$$

Taxonomy of Generative Models

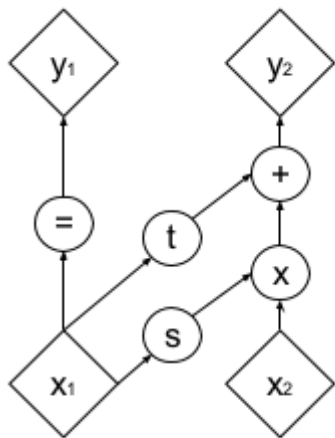


Exact Model: NVP (non-volume preserving)

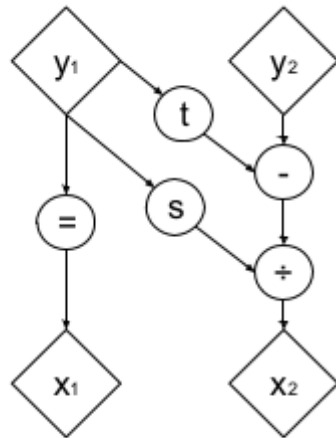


Real NVP: Invertible Non-linear Transforms

$$p_x(\mathbf{x}) = p_z(g^{-1}(\mathbf{x})) \left| \det \left(\frac{\partial g^{-1}(\mathbf{x})}{\partial \mathbf{x}} \right) \right|.$$



(a) Forward propagation



(b) Inverse propagation

| | | | |
|---|---|---|---|
| 1 | 2 | 5 | 6 |
| 3 | 4 | 7 | 8 |
| | | | |
| | | | |

| | | | |
|---|---|---|---|
| 4 | 8 | | |
| | 3 | 7 | |
| | | 2 | 6 |
| | | | 1 |
| | | | |

Real NVP: Examples

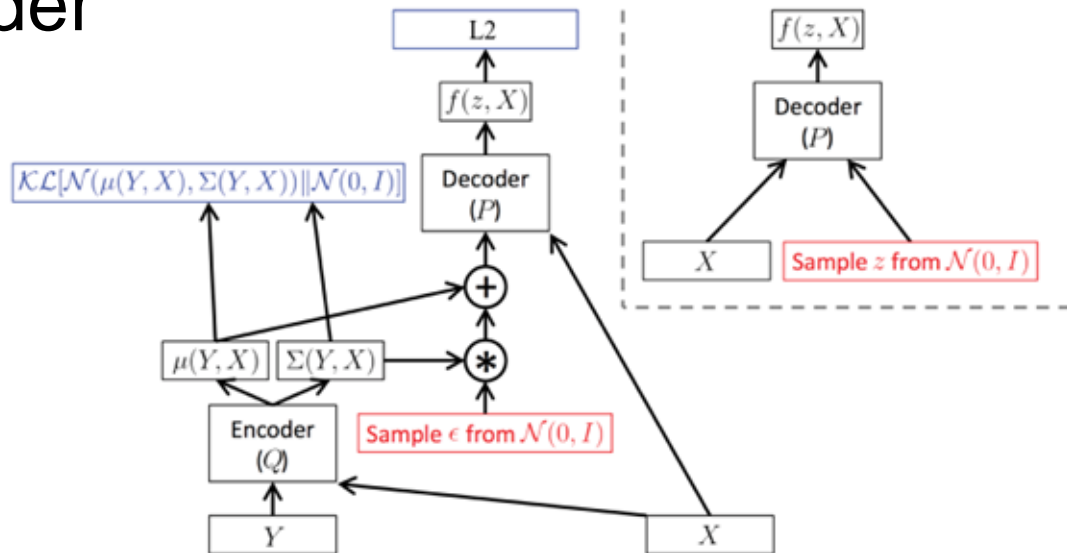


Real NVP

Restriction on the source domain: must be of the same as the target.

Variational Auto-Encoder

Auto-encoding with noise in hidden variable



$$\log p_{\theta}(\mathbf{x}^{(i)}) = D_{KL}(q_{\phi}(\mathbf{z}|\mathbf{x}^{(i)})||p_{\theta}(\mathbf{z}|\mathbf{x}^{(i)})) + \mathcal{L}(\theta, \phi; \mathbf{x}^{(i)})$$

$$\mathcal{L}(\theta, \phi; \mathbf{x}^{(i)}) \simeq \frac{1}{2} \sum_{j=1}^J \left(1 + \log((\sigma_j^{(i)})^2) - (\mu_j^{(i)})^2 - (\sigma_j^{(i)})^2 \right) + \frac{1}{L} \sum_{l=1}^L \log p_{\theta}(\mathbf{x}^{(i)} | \mathbf{z}^{(i,l)})$$

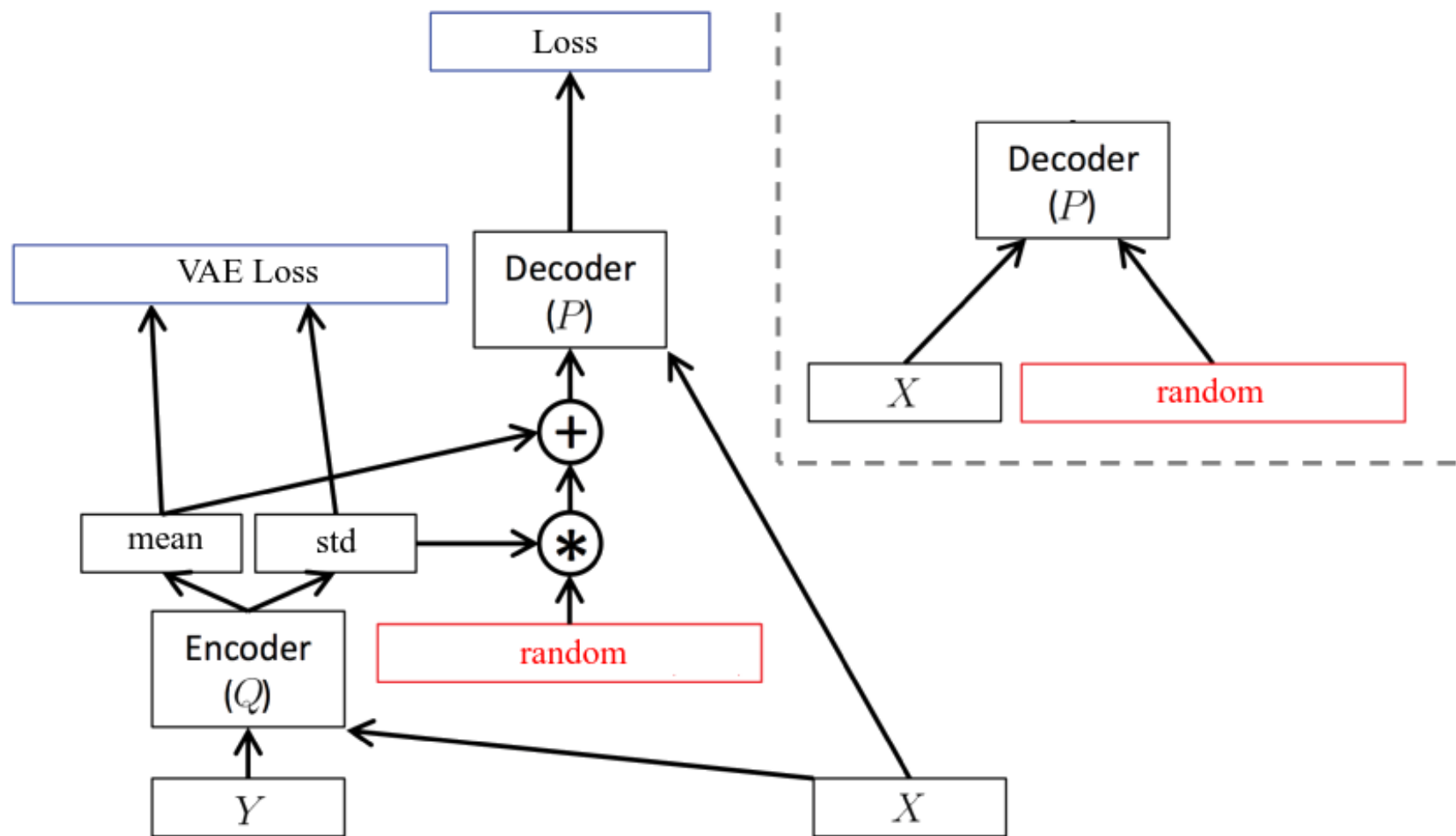
Variational Auto-Encoder

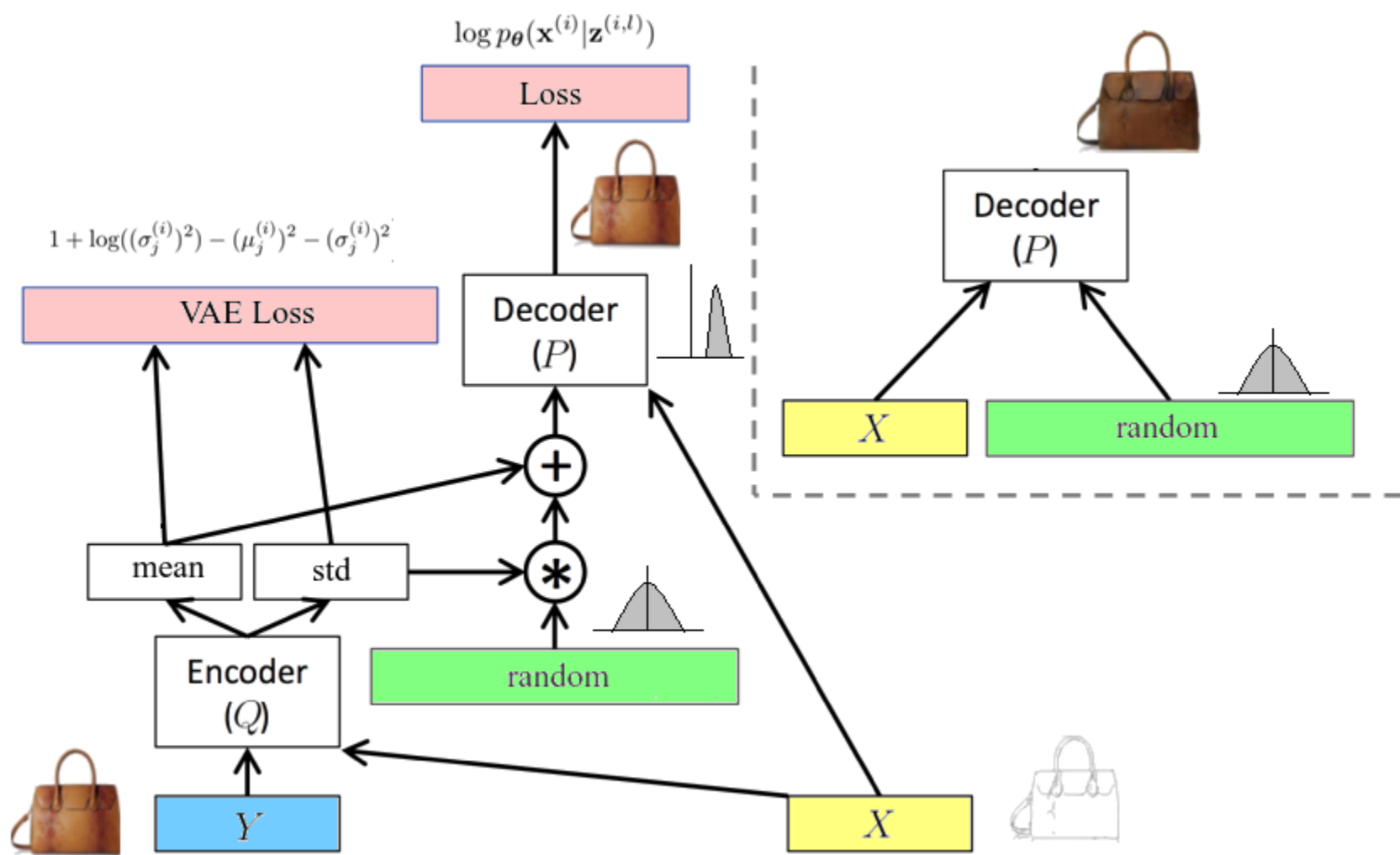
$$\mathcal{D}[Q(z)||P(z|X)] = E_{z \sim Q} [\log Q(z) - \log P(z|X)].$$

$$\mathcal{D}[Q(z)||P(z|X)] = E_{z \sim Q} [\log Q(z) - \log P(X|z) - \log P(z)] + \log P(X).$$

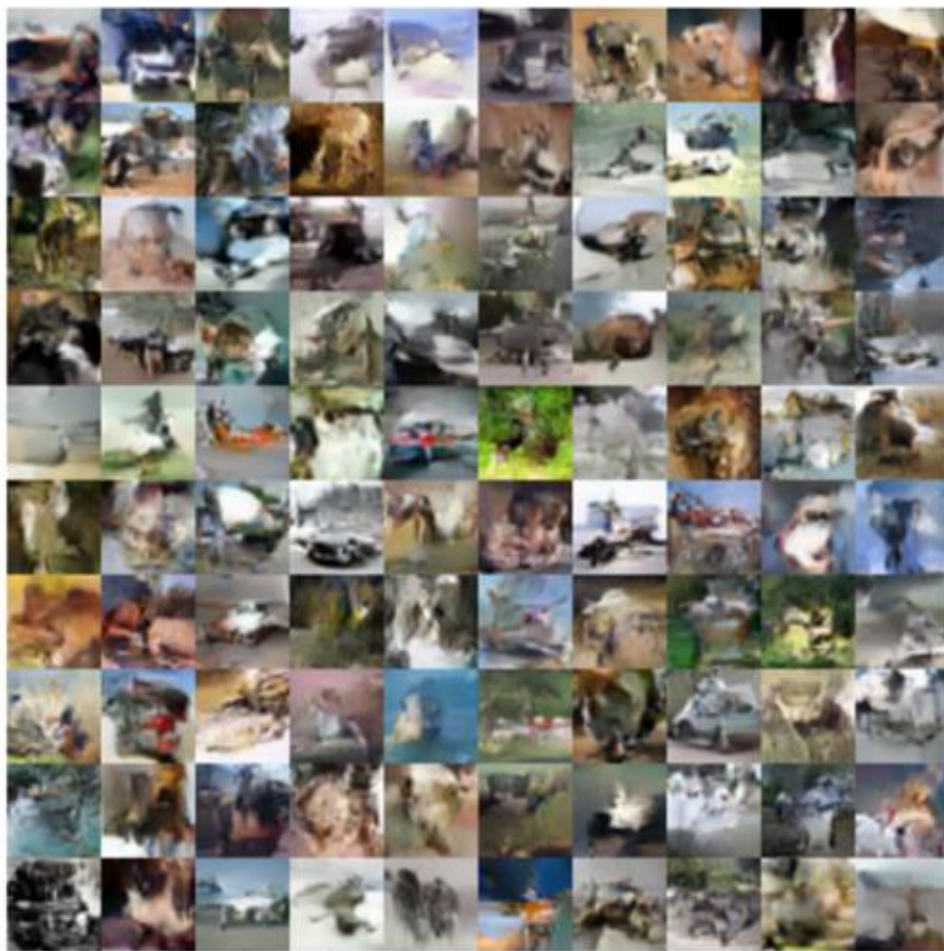
$$\log P(X) - \mathcal{D}[Q(z)||P(z|X)] = E_{z \sim Q} [\log P(X|z)] - \mathcal{D}[Q(z)||P(z)]$$

$$\log P(X) - \mathcal{D}[Q(z|X)||P(z|X)] = E_{z \sim Q} [\log P(X|z)] - \mathcal{D}[Q(z|X)||P(z)]$$

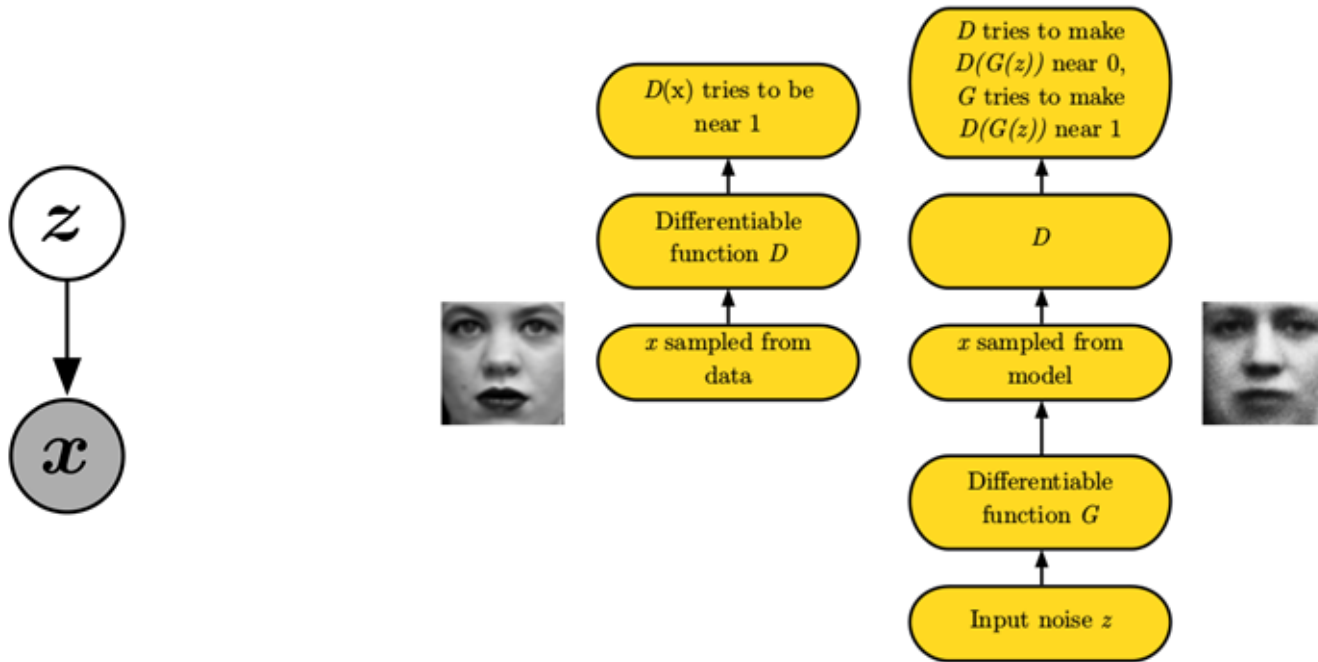




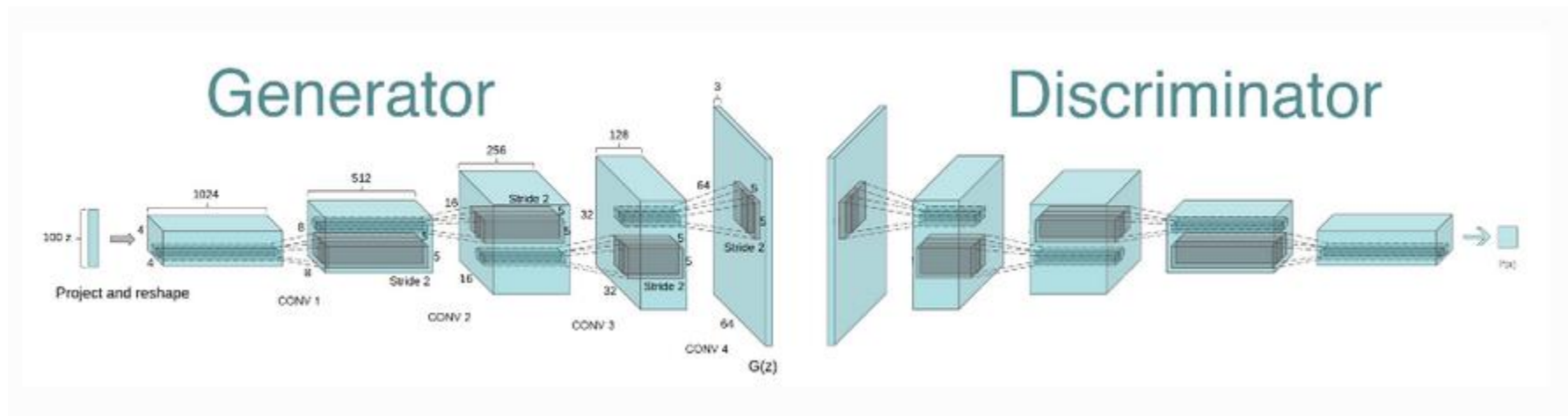
VAE: Examples



Generative Adversarial Networks (GAN)



DCGAN



Train D by $\text{Loss}(D(\text{real}), 1), \text{Loss}(D(G(\text{random})), 0)$

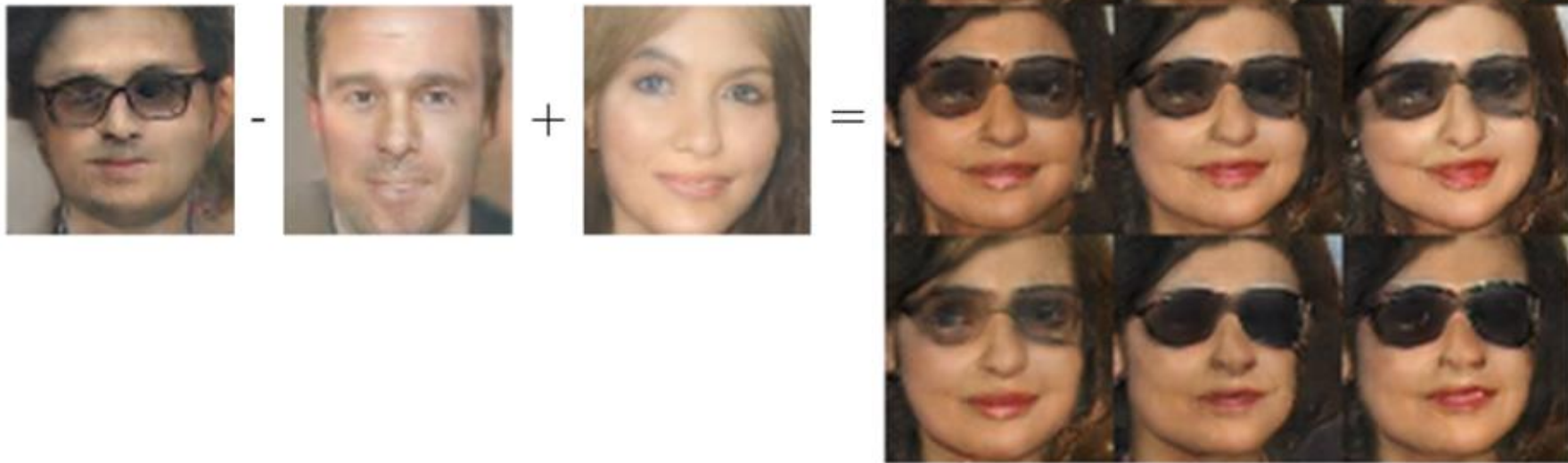
Train G by $\text{Loss}(D(G(\text{random}))), 1)$

DCGAN: Examples



DCGAN: Example of Feature Manipulation

Vector arithmetics in feature space



Conditional, Cross-domain Generation

Generative adversarial text to image synthesis

this small bird has a pink breast and crown, and black primaries and secondaries.



this magnificent fellow is almost all black with a red crest, and white cheek patch.



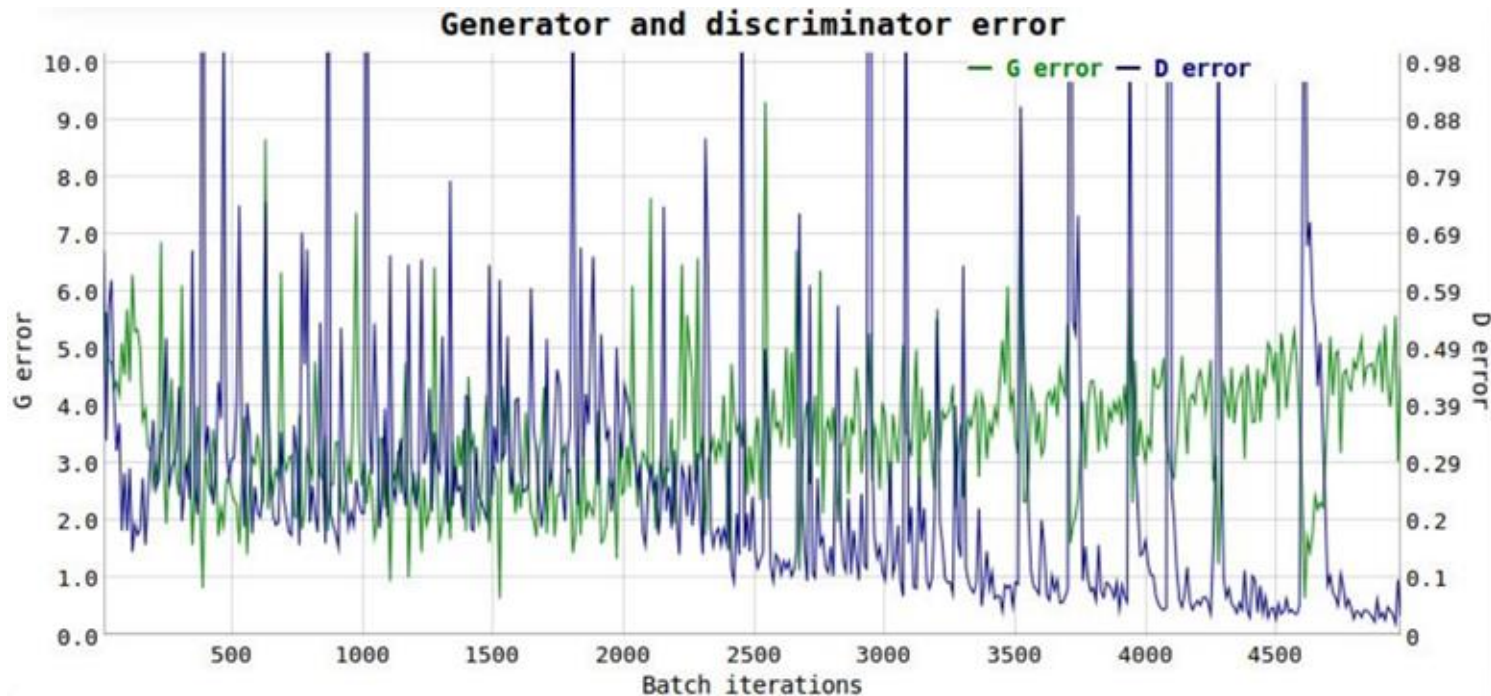
the flower has petals that are bright pinkish purple with white stigma



this white and yellow flower have thin white petals and a round yellow stamen



GAN training problems: unstable losses



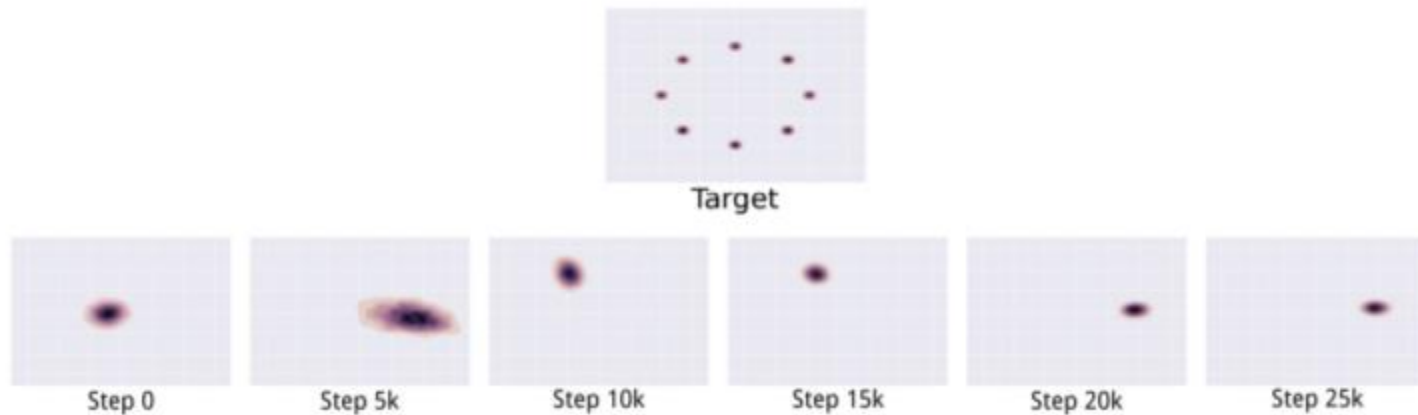
GAN training problems: Mini-batch Fluctuation

Differs much even between consecutive minibatches.



GAN training problems: Mode Collapse

Lack of diversity in generated results.



Improve GAN training: Label Smoothing

Improves stability of training

```
d_on_data = discriminator_logits(data_minibatch)
d_on_samples = discriminator_logits(samples_minibatch)
loss = tf.nn.sigmoid_cross_entropy_with_logits(d_on_data, .9) + \
      tf.nn.sigmoid_cross_entropy_with_logits(d_on_samples, 0.)
```

Improve GAN training: Wasserstein GAN

Use linear instead of log

$$W(\mathbb{P}_r, \mathbb{P}_\theta) = \sup_{\|f\|_L \leq 1} \mathbb{E}_{x \sim \mathbb{P}_r}[f(x)] - \mathbb{E}_{x \sim \mathbb{P}_\theta}[f(x)]$$

for $t = 0, \dots, n_{\text{critic}}$ **do**

Sample $\{x^{(i)}\}_{i=1}^m \sim \mathbb{P}_r$ a batch from the real data.

Sample $\{z^{(i)}\}_{i=1}^m \sim p(z)$ a batch of prior samples.

$g_w \leftarrow \nabla_w \left[\frac{1}{m} \sum_{i=1}^m f_w(x^{(i)}) - \frac{1}{m} \sum_{i=1}^m f_w(g_\theta(z^{(i)})) \right]$

$w \leftarrow w + \alpha \cdot \text{RMSPProp}(w, g_w)$

$w \leftarrow \text{clip}(w, -c, c)$

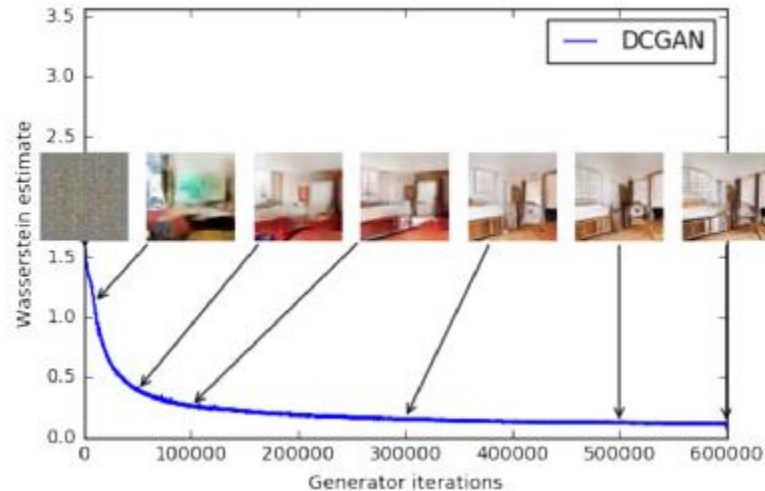
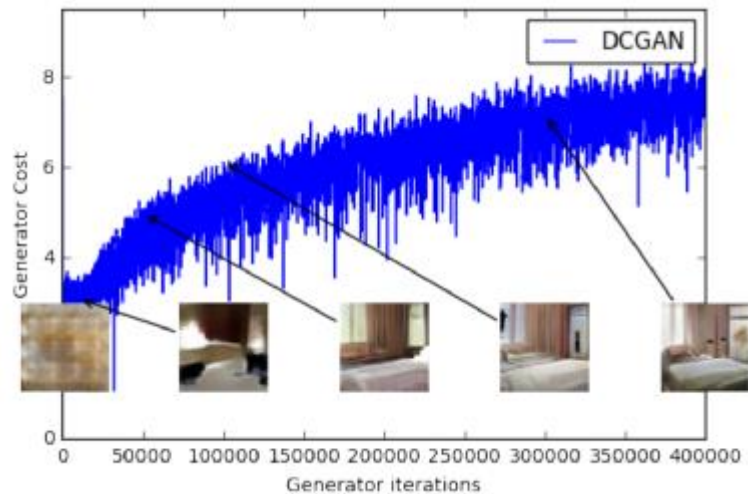
end for

Sample $\{z^{(i)}\}_{i=1}^m \sim p(z)$ a batch of prior samples.

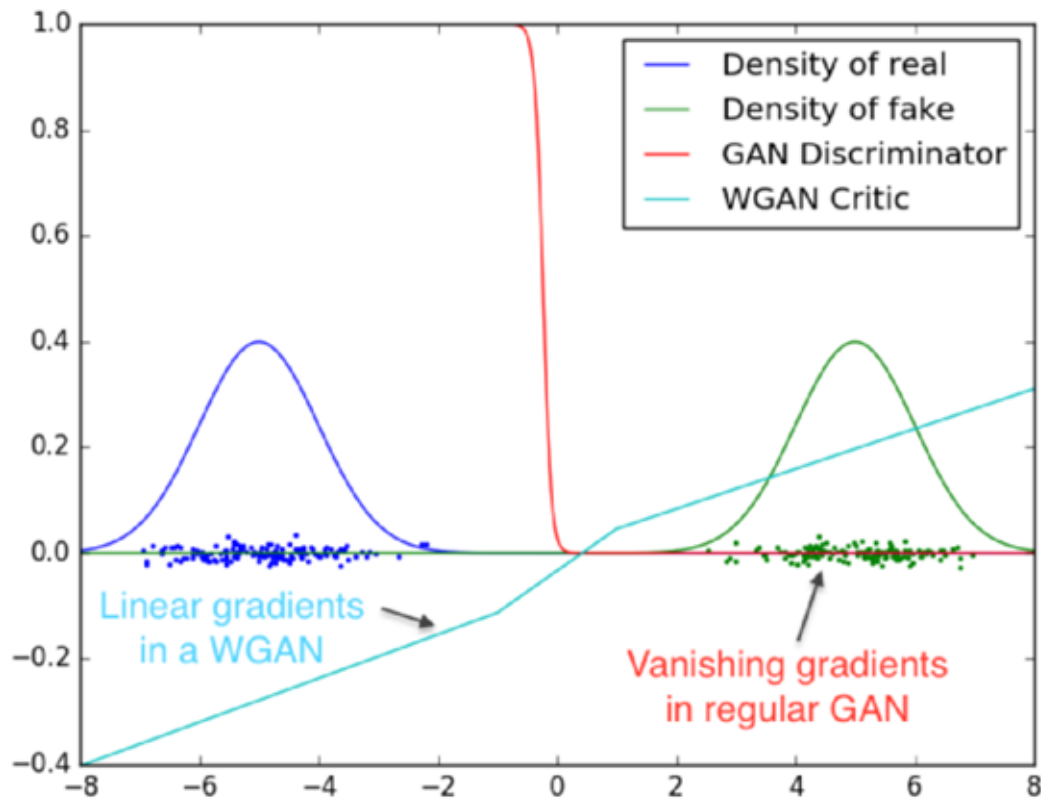
$g_\theta \leftarrow -\nabla_\theta \frac{1}{m} \sum_{i=1}^m f_w(g_\theta(z^{(i)}))$

$\theta \leftarrow \theta - \alpha \cdot \text{RMSPProp}(\theta, g_\theta)$

WGAN: Stabilized Training Curve



WGAN: Non-vanishing Gradient



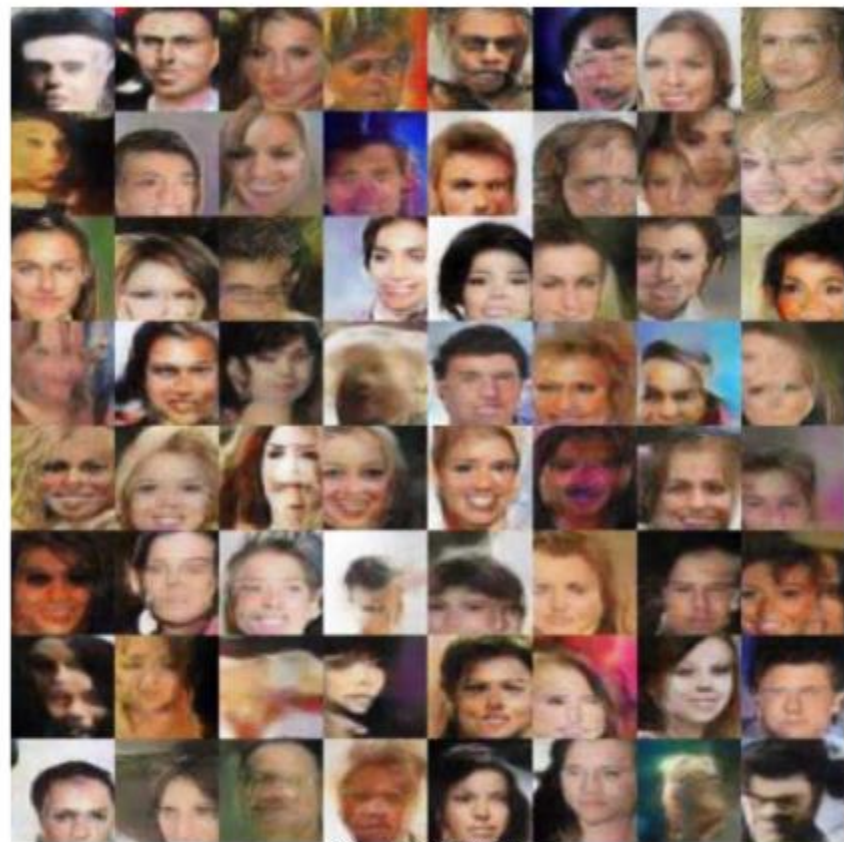
Loss Sensitive GAN

$$\min_{\theta} S_{n,m}(\phi^*, \theta) \triangleq \frac{1}{n} \sum_{i=1}^n L_{\theta}(\mathbf{x}_i) \quad (8)$$

$$+ \frac{\lambda}{nm} \sum_{i,j=1}^{n,m} (\Delta(\mathbf{x}_i, G_{\phi^*}(\mathbf{z}_j)) + L_{\theta}(\mathbf{x}_i) - L_{\theta}(G_{\phi^*}(\mathbf{z}_j)))_+$$

and

$$\min_{\phi} T_k(\theta^*, \phi) = \frac{1}{k} \sum_{i=1}^k L_{\theta^*}(G_{\phi}(\mathbf{z}'_i)) \quad (9)$$



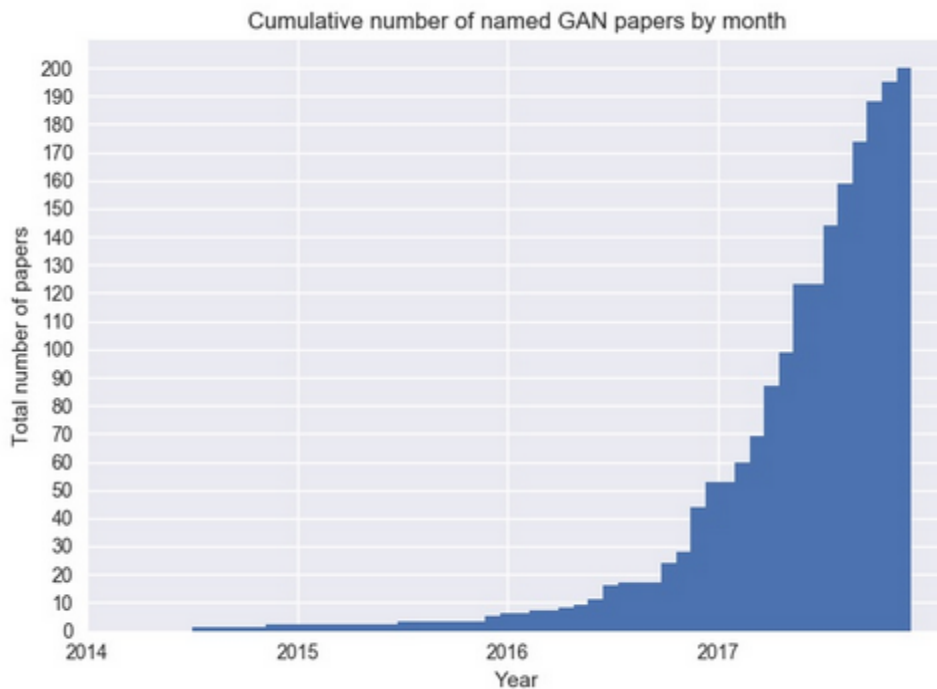
(a) DCGAN



(b) LS-GAN

The GAN Zoo

<https://github.com/hindupuravinash/the-gan-zoo>



- 3D-GAN - [Learning a Probabilistic Latent Space of Object Shapes via 3D Generative-Adversarial Modeling \(github\)](#)
- 3D-IWGAN - [Improved Adversarial Systems for 3D Object Generation and Reconstruction \(github\)](#)
- 3D-RecGAN - [3D Object Reconstruction from a Single Depth View with Adversarial Learning \(github\)](#)
- ABC-GAN - [ABC-GAN: Adaptive Blur and Control for improved training stability of Generative Adversarial Networks \(github\)](#)
- AC-GAN - [Conditional Image Synthesis With Auxiliary Classifier GANs](#)
- acGAN - [Face Aging With Conditional Generative Adversarial Networks](#)
- AdaGAN - [AdaGAN: Boosting Generative Models](#)
- AE-GAN - [AE-GAN: adversarial eliminating with GAN](#)
- AEGAN - [Learning Inverse Mapping by Autoencoder based Generative Adversarial Nets](#)
- AffGAN - [Amortised MAP Inference for Image Super-resolution](#)
- AL-CGAN - [Learning to Generate Images of Outdoor Scenes from Attributes and Semantic Layouts](#)
- ALI - [Adversarially Learned Inference](#)
- AlignGAN - [AlignGAN: Learning to Align Cross-Domain Images with Conditional Generative Adversarial Networks](#)
- AM-GAN - [Activation Maximization Generative Adversarial Nets](#)
- AnoGAN - [Unsupervised Anomaly Detection with Generative Adversarial Networks to Guide Marker Discovery](#)
- ARAE - [Adversarially Regularized Autoencoders for Generating Discrete Structures \(github\)](#)
- ARDA - [Adversarial Representation Learning for Domain Adaptation](#)
- ARIGAN - [ARIGAN: Synthetic Arabidopsis Plants using Generative Adversarial Network](#)
- ArtGAN - [ArtGAN: Artwork Synthesis with Conditional Categorical GANs](#)
- b-GAN - [Generative Adversarial Nets from a Density Ratio Estimation Perspective](#)
- Bayesian GAN - [Deep and Hierarchical Implicit Models](#)
- Bayesian GAN - [Bayesian GAN](#)
- BCGAN - [Bayesian Conditional Generative Adversarial Networks](#)
- BEGAN - [BEGAN: Boundary Equilibrium Generative Adversarial Networks](#)
- BGAN - [Binary Generative Adversarial Networks for Image Retrieval \(github\)](#)

- BiGAN - [Adversarial Feature Learning](#)
- BS-GAN - [Boundary-Seeking Generative Adversarial Networks](#)
- C-RNN-GAN - [C-RNN-GAN: Continuous recurrent neural networks with adversarial training](#) (github)
- CaloGAN - [CaloGAN: Simulating 3D High Energy Particle Showers in Multi-Layer Electromagnetic Calorimeters with Generative Adversarial Networks](#) (github)
- CAN - [CAN: Creative Adversarial Networks, Generating Art by Learning About Styles and Deviating from Style Norms](#)
- CatGAN - [Unsupervised and Semi-supervised Learning with Categorical Generative Adversarial Networks](#)
- CausalGAN - [CausalGAN: Learning Causal Implicit Generative Models with Adversarial Training](#)
- CC-GAN - [Semi-Supervised Learning with Context-Conditional Generative Adversarial Networks](#) (github)
- CDcGAN - [Simultaneously Color-Depth Super-Resolution with Conditional Generative Adversarial Network](#)
- CGAN - [Conditional Generative Adversarial Nets](#)
- CGAN - [Controllable Generative Adversarial Network](#)
- Chekhov GAN - [An Online Learning Approach to Generative Adversarial Networks](#)
- CM-GAN - [CM-GANs: Cross-modal Generative Adversarial Networks for Common Representation Learning](#)
- CoGAN - [Coupled Generative Adversarial Networks](#)
- Conditional cycleGAN - [Conditional CycleGAN for Attribute Guided Face Image Generation](#)
- contrast-GAN - [Generative Semantic Manipulation with Contrasting GAN](#)
- Context-RNN-GAN - [Contextual RNN-GANs for Abstract Reasoning Diagram Generation](#)
- Coulomb GAN - [Coulomb GANs: Provably Optimal Nash Equilibria via Potential Fields](#)
- Cramèr GAN - [The Cramer Distance as a Solution to Biased Wasserstein Gradients](#)
- crVAE-GAN - [Channel-Recurrent Variational Autoencoders](#)
- CS-GAN - [Improving Neural Machine Translation with Conditional Sequence Generative Adversarial Nets](#)
- CVAE-GAN - [CVAE-GAN: Fine-Grained Image Generation through Asymmetric Training](#)
- CycleGAN - [Unpaired Image-to-Image Translation using Cycle-Consistent Adversarial Networks](#) (github)
- D2GAN - [Dual Discriminator Generative Adversarial Nets](#)

- DAN - [Distributional Adversarial Networks](#)
- DCGAN - [Unsupervised Representation Learning with Deep Convolutional Generative Adversarial Networks](#) (github)
- DeLiGAN - [DeLiGAN : Generative Adversarial Networks for Diverse and Limited Data](#) (github)
- DiscoGAN - [Learning to Discover Cross-Domain Relations with Generative Adversarial Networks](#)
- DistanceGAN - [One-Sided Unsupervised Domain Mapping](#)
- DM-GAN - [Dual Motion GAN for Future-Flow Embedded Video Prediction](#)
- DR-GAN - [Representation Learning by Rotating Your Faces](#)
- DRAGAN - [How to Train Your DRAGAN](#) (github)
- DSP-GAN - [Depth Structure Preserving Scene Image Generation](#)
- DTN - [Unsupervised Cross-Domain Image Generation](#)
- DualGAN - [DualGAN: Unsupervised Dual Learning for Image-to-Image Translation](#)
- Dualing GAN - [Dualing GANs](#)
- EBGAN - [Energy-based Generative Adversarial Network](#)
- ED//GAN - [Stabilizing Training of Generative Adversarial Networks through Regularization](#)
- EGAN - [Enhanced Experience Replay Generation for Efficient Reinforcement Learning](#)
- ExprGAN - [ExprGAN: Facial Expression Editing with Controllable Expression Intensity](#)
- f-GAN - [f-GAN: Training Generative Neural Samplers using Variational Divergence Minimization](#)
- FF-GAN - [Towards Large-Pose Face Frontalization in the Wild](#)
- Fila-GAN - [Synthesizing Filamentary Structured Images with GANs](#)
- Fisher GAN - [Fisher GAN](#)
- Flow-GAN - [Flow-GAN: Bridging implicit and prescribed learning in generative models](#)
- GAMN - [Generative Adversarial Mapping Networks](#)
- GAN - [Generative Adversarial Networks](#) (github)
- GAN-ATV - [A Novel Approach to Artistic Textual Visualization via GAN](#)
- GAN-CLS - [Generative Adversarial Text to Image Synthesis](#) (github)
- GAN-sep - [GANs for Biological Image Synthesis](#) (github)

- GAN-VFS - Generative Adversarial Network-based Synthesis of Visible Faces from Polarimetric Thermal Faces
- GANCS - Deep Generative Adversarial Networks for Compressed Sensing Automates MRI
- GANDI - Guiding the search in continuous state-action spaces by learning an action sampling distribution from off-target samples
- GAP - Context-Aware Generative Adversarial Privacy
- GAWWN - Learning What and Where to Draw (github)
- GeneGAN - GeneGAN: Learning Object Transfiguration and Attribute Subspace from Unpaired Data (github)
- Geometric GAN - Geometric GAN
- GMAN - Generative Multi-Adversarial Networks
- GMM-GAN - Towards Understanding the Dynamics of Generative Adversarial Networks
- GoGAN - Gang of GANs: Generative Adversarial Networks with Maximum Margin Ranking
- GP-GAN - GP-GAN: Towards Realistic High-Resolution Image Blending (github)
- GP-GAN - GP-GAN: Gender Preserving GAN for Synthesizing Faces from Landmarks
- GRAN - Generating images with recurrent adversarial networks (github)
- IAN - Neural Photo Editing with Introspective Adversarial Networks (github)
- IcGAN - Invertible Conditional GANs for image editing (github)
- ID-CGAN - Image De-raining Using a Conditional Generative Adversarial Network
- iGAN - Generative Visual Manipulation on the Natural Image Manifold (github)
- Improved GAN - Improved Techniques for Training GANs (github)
- InfoGAN - InfoGAN: Interpretable Representation Learning by Information Maximizing Generative Adversarial Nets (github)
- IRGAN - IRGAN: A Minimax Game for Unifying Generative and Discriminative Information Retrieval models
- IWGAN - On Unifying Deep Generative Models
- KGAN - KGAN: How to Break The Minimax Game in GAN
- I-GAN - Representation Learning and Adversarial Generation of 3D Point Clouds
- LAGAN - Learning Particle Physics by Example: Location-Aware Generative Adversarial Networks for Physics Synthesis

- LAPGAN - Deep Generative Image Models using a Laplacian Pyramid of Adversarial Networks (github)
- LD-GAN - Linear Discriminant Generative Adversarial Networks
- LDAN - Label Denoising Adversarial Network (LDAN) for Inverse Lighting of Face Images
- LeakGAN - Long Text Generation via Adversarial Training with Leaked Information
- LeGAN - Likelihood Estimation for Generative Adversarial Networks
- LR-GAN - LR-GAN: Layered Recursive Generative Adversarial Networks for Image Generation
- LS-GAN - Loss-Sensitive Generative Adversarial Networks on Lipschitz Densities
- LSGAN - Least Squares Generative Adversarial Networks
- MAD-GAN - Multi-Agent Diverse Generative Adversarial Networks
- MAGAN - MAGAN: Margin Adaptation for Generative Adversarial Networks
- MalGAN - Generating Adversarial Malware Examples for Black-Box Attacks Based on GAN
- MaliGAN - Maximum-Likelihood Augmented Discrete Generative Adversarial Networks
- MARTA-GAN - Deep Unsupervised Representation Learning for Remote Sensing Images
- McGAN - McGan: Mean and Covariance Feature Matching GAN
- MD-GAN - Learning to Generate Time-Lapse Videos Using Multi-Stage Dynamic Generative Adversarial Networks
- MDGAN - Mode Regularized Generative Adversarial Networks
- MedGAN - Generating Multi-label Discrete Electronic Health Records using Generative Adversarial Networks
- MGAN - Precomputed Real-Time Texture Synthesis with Markovian Generative Adversarial Networks (github)
- MGGAN - Multi-Generator Generative Adversarial Nets
- MIX+GAN - Generalization and Equilibrium in Generative Adversarial Nets (GANs)
- MLGAN - Metric Learning-based Generative Adversarial Network
- MMD-GAN - MMD GAN: Towards Deeper Understanding of Moment Matching Network (github)
- MMGAN - MMGAN: Manifold Matching Generative Adversarial Network for Generating Images
- MoCoGAN - MoCoGAN: Decomposing Motion and Content for Video Generation (github)
- MPM-GAN - Message Passing Multi-Agent GANs
- MuseGAN - MuseGAN: Symbolic-domain Music Generation and Accompaniment with Multi-track Sequential Generative Adversarial Networks
- MV-BiGAN - Multi-view Generative Adversarial Networks

- OptionGAN - [OptionGAN: Learning Joint Reward-Policy Options using Generative Adversarial Inverse Reinforcement Learning](#)
- ORGAN - [Objective-Reinforced Generative Adversarial Networks \(ORGAN\) for Sequence Generation Models](#)
- PAN - [Perceptual Adversarial Networks for Image-to-Image Transformation](#)
- PassGAN - [PassGAN: A Deep Learning Approach for Password Guessing](#)
- Perceptual GAN - [Perceptual Generative Adversarial Networks for Small Object Detection](#)
- PGAN - [Probabilistic Generative Adversarial Networks](#)
- pix2pix - [Image-to-Image Translation with Conditional Adversarial Networks \(github\)](#)
- PixelGAN - [PixelGAN Autoencoders](#)
- Pose-GAN - [The Pose Knows: Video Forecasting by Generating Pose Futures](#)
- PPGN - [Plug & Play Generative Networks: Conditional Iterative Generation of Images in Latent Space](#)
- PrGAN - [3D Shape Induction from 2D Views of Multiple Objects](#)
- PSGAN - [Learning Texture Manifolds with the Periodic Spatial GAN](#)
- PS²-GAN - [High-Quality Facial Photo-Sketch Synthesis Using Multi-Adversarial Networks](#)
- RankGAN - [Adversarial Ranking for Language Generation](#)
- RCGAN - [Real-valued \(Medical\) Time Series Generation with Recurrent Conditional GANs](#)
- RefineGAN - [Compressed Sensing MRI Reconstruction with Cyclic Loss in Generative Adversarial Networks](#)
- RenderGAN - [RenderGAN: Generating Realistic Labeled Data](#)
- ResGAN - [Generative Adversarial Network based on Resnet for Conditional Image Restoration](#)
- RNN-WGAN - [Language Generation with Recurrent Generative Adversarial Networks without Pre-training \(github\)](#)
- RPGAN - [Stabilizing GAN Training with Multiple Random Projections \(github\)](#)
- RTT-GAN - [Recurrent Topic-Transition GAN for Visual Paragraph Generation](#)
- RWGAN - [Relaxed Wasserstein with Applications to GANs](#)
- SAD-GAN - [SAD-GAN: Synthetic Autonomous Driving using Generative Adversarial Networks](#)
- SalGAN - [SalGAN: Visual Saliency Prediction with Generative Adversarial Networks \(github\)](#)
- SBADA-GAN - [From source to target and back: symmetric bi-directional adaptive GAN](#)
- SD-GAN - [Semantically Decomposing the Latent Spaces of Generative Adversarial Networks](#)
- SEGAN - [SEGAN: Speech Enhancement Generative Adversarial Network](#)

- SeGAN - [SeGAN: Segmenting and Generating the Invisible](#)
- SegAN - [SegAN: Adversarial Network with Multi-scale L1 Loss for Medical Image Segmentation](#)
- SeqGAN - [SeqGAN: Sequence Generative Adversarial Nets with Policy Gradient \(github\)](#)
- SGAN - [Texture Synthesis with Spatial Generative Adversarial Networks](#)
- SGAN - [Stacked Generative Adversarial Networks \(github\)](#)
- SGAN - [Steganographic Generative Adversarial Networks](#)
- SimGAN - [Learning from Simulated and Unsupervised Images through Adversarial Training](#)
- SketchGAN - [Adversarial Training For Sketch Retrieval](#)
- SL-GAN - [Semi-Latent GAN: Learning to generate and modify facial images from attributes](#)
- SN-GAN - [Spectral Normalization for Generative Adversarial Networks \(github\)](#)
- Softmax-GAN - [Softmax GAN](#)
- Splitting GAN - [Class-Splitting Generative Adversarial Networks](#)
- SRGAN - [Photo-Realistic Single Image Super-Resolution Using a Generative Adversarial Network](#)
- SS-GAN - [Semi-supervised Conditional GANs](#)
- ss-InfoGAN - [Guiding InfoGAN with Semi-Supervision](#)
- SSGAN - [SSGAN: Secure Steganography Based on Generative Adversarial Networks](#)
- SSL-GAN - [Semi-Supervised Learning with Context-Conditional Generative Adversarial Networks](#)
- ST-GAN - [Style Transfer Generative Adversarial Networks: Learning to Play Chess Differently](#)
- StackGAN - [StackGAN: Text to Photo-realistic Image Synthesis with Stacked Generative Adversarial Networks](#)
- SteinGAN - [Learning Deep Energy Models: Contrastive Divergence vs. Amortized MLE](#)
- SVSGAN - [SVSGAN: Singing Voice Separation via Generative Adversarial Network](#)
- S²GAN - [Generative Image Modeling using Style and Structure Adversarial Networks](#)
- TAC-GAN - [TAC-GAN - Text Conditioned Auxiliary Classifier Generative Adversarial Network \(github\)](#)
- TAN - [Outline Colorization through Tandem Adversarial Networks](#)
- TextureGAN - [TextureGAN: Controlling Deep Image Synthesis with Texture Patches](#)
- TGAN - [Temporal Generative Adversarial Nets](#)
- TGAN - [Tensorizing Generative Adversarial Nets](#)

- TGAN - Tensor-Generative Adversarial Network with Two-dimensional Sparse Coding: Application to Real-time Indoor Localization
- TP-GAN - Beyond Face Rotation: Global and Local Perception GAN for Photorealistic and Identity Preserving Frontal View Synthesis
- Triple-GAN - Triple Generative Adversarial Nets
- Unrolled GAN - Unrolled Generative Adversarial Networks (github)
- VAE-GAN - Autoencoding beyond pixels using a learned similarity metric
- VariGAN - Multi-View Image Generation from a Single-View
- VAW-GAN - Voice Conversion from Unaligned Corpora using Variational Autoencoding Wasserstein Generative Adversarial Networks
- VEEGAN - VEEGAN: Reducing Mode Collapse in GANs using Implicit Variational Learning (github)
- VGAN - Generating Videos with Scene Dynamics (github)
- VGAN - Generative Adversarial Networks as Variational Training of Energy Based Models (github)
- ViGAN - Image Generation and Editing with Variational Info Generative Adversarial Networks
- VIGAN - VIGAN: Missing View Imputation with Generative Adversarial Networks
- VRAL - Variance Regularizing Adversarial Learning
- WaterGAN - WaterGAN: Unsupervised Generative Network to Enable Real-time Color Correction of Monocular Underwater Images
- WGAN - Wasserstein GAN (github)
- WGAN-GP - Improved Training of Wasserstein GANs (github)
- WS-GAN - Weakly Supervised Generative Adversarial Networks for 3D Reconstruction
- ZipNet-GAN - ZipNet-GAN: Inferring Fine-grained Mobile Traffic Patterns via a Generative Adversarial Neural Network
- α -GAN - Variational Approaches for Auto-Encoding Generative Adversarial Networks (github)
- Δ -GAN - Triangle Generative Adversarial Networks

Cycle GAN: Correspondence from Unpaired Data

Monet \leftrightarrow Photos



Monet \rightarrow photo

Zebras \leftrightarrow Horses



zebra \rightarrow horse

Summer \leftrightarrow Winter



summer \rightarrow winter



photo \rightarrow Monet



horse \rightarrow zebra



winter \rightarrow summer



Photograph



Monet



Van Gogh

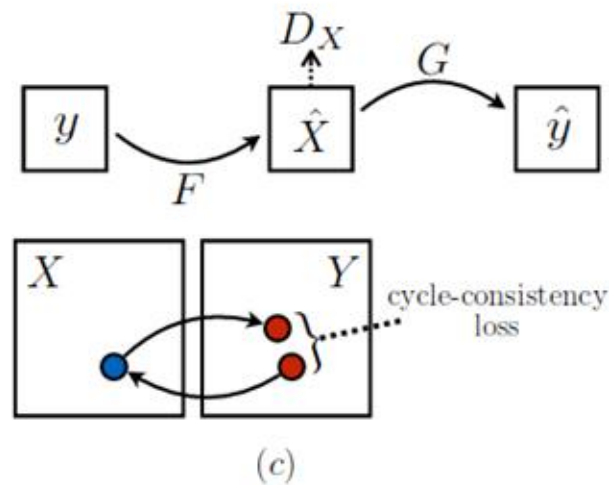
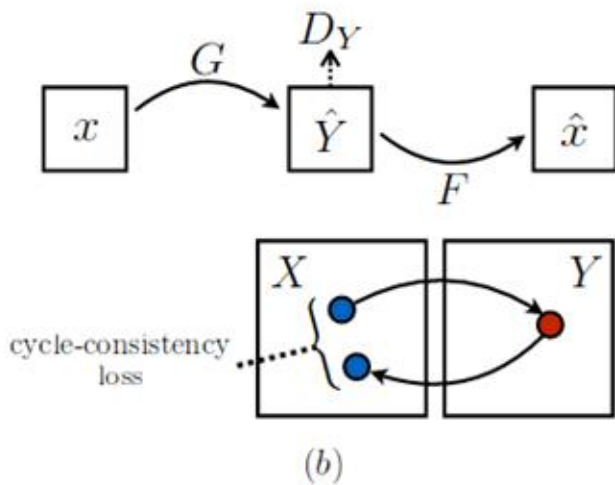
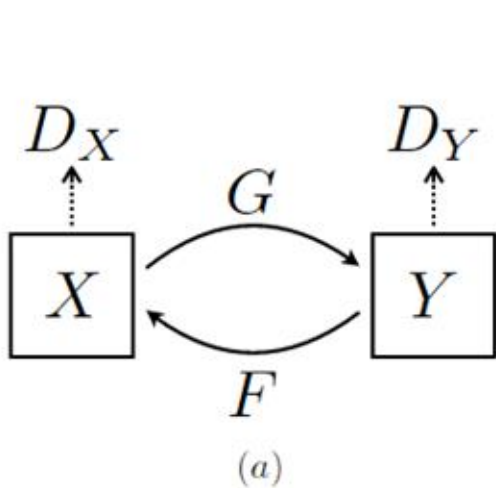


Cezanne



Ukiyo-e

Cycle GAN

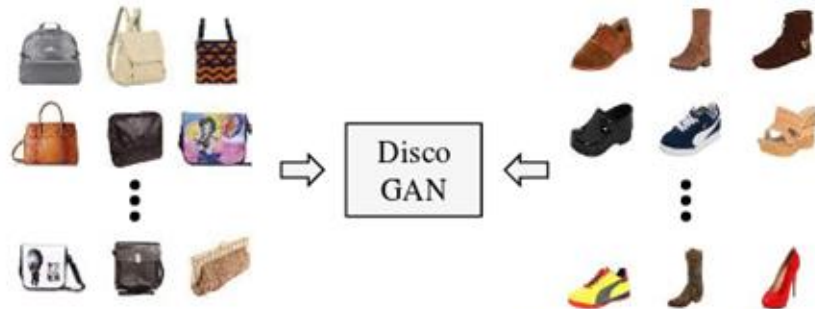


Cycle GAN: Bad Cases



DiscoGAN

Cross-domain relation



(a) Learning cross-domain relations **without any extra label**

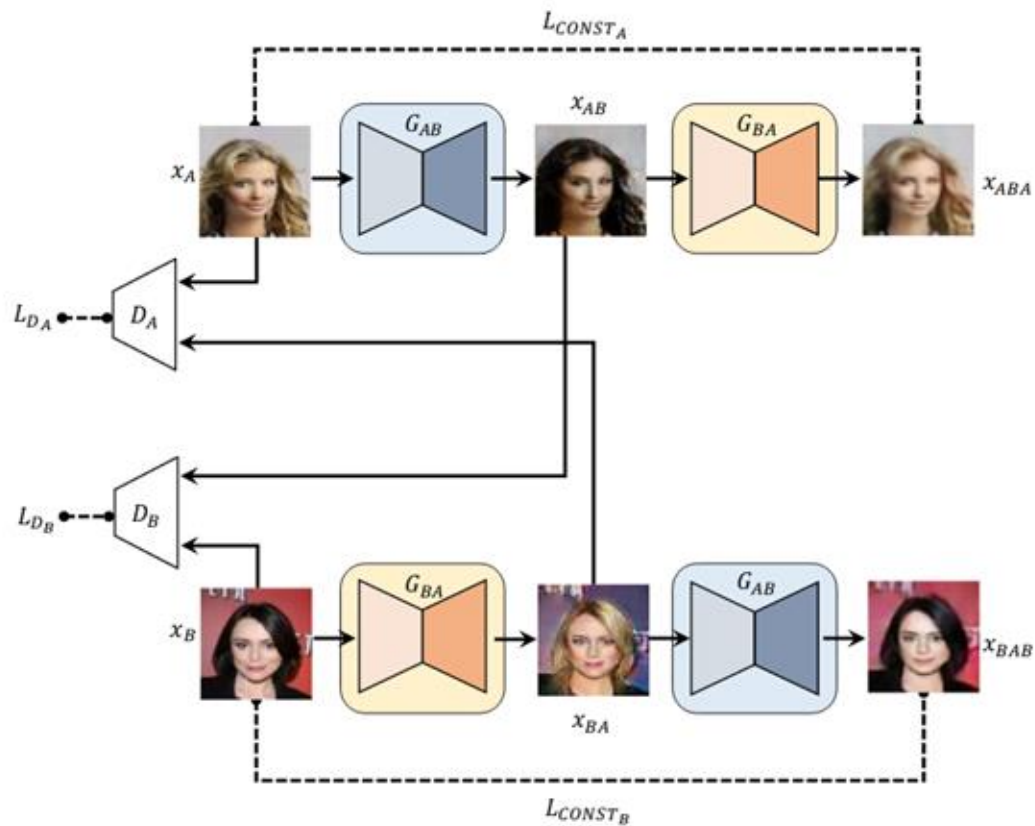


(b) Handbag images (input) & **Generated** shoe images (output)

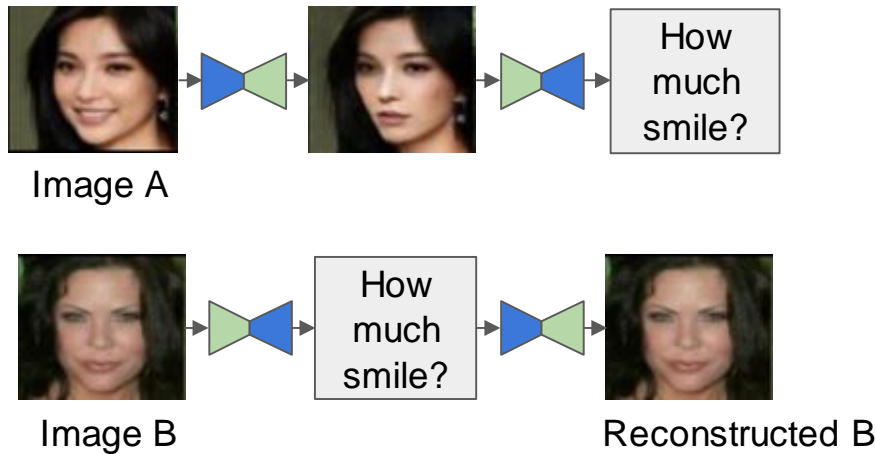


(c) Shoe images (input) & **Generated** handbag images (output)

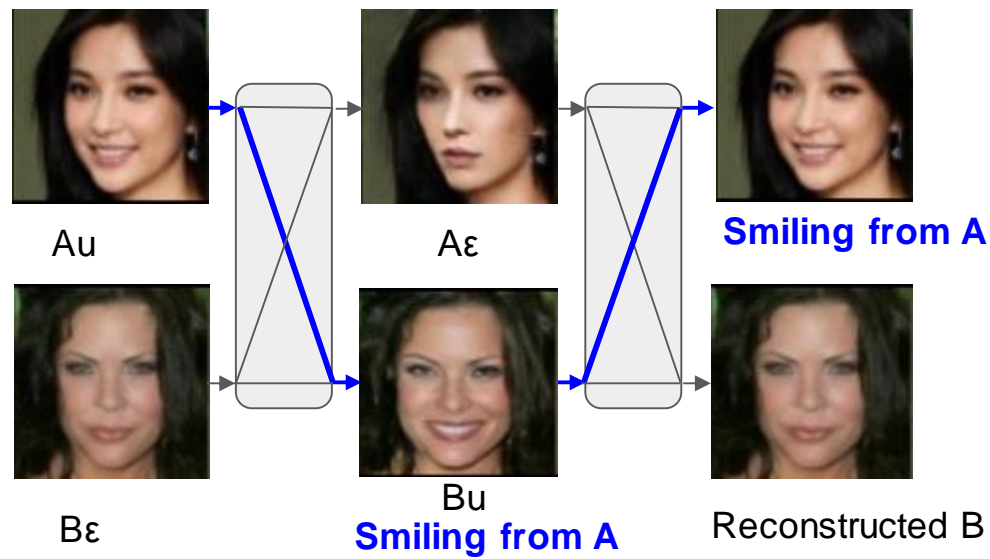
DiscoGAN



Underdetermined CycleGAN pattern

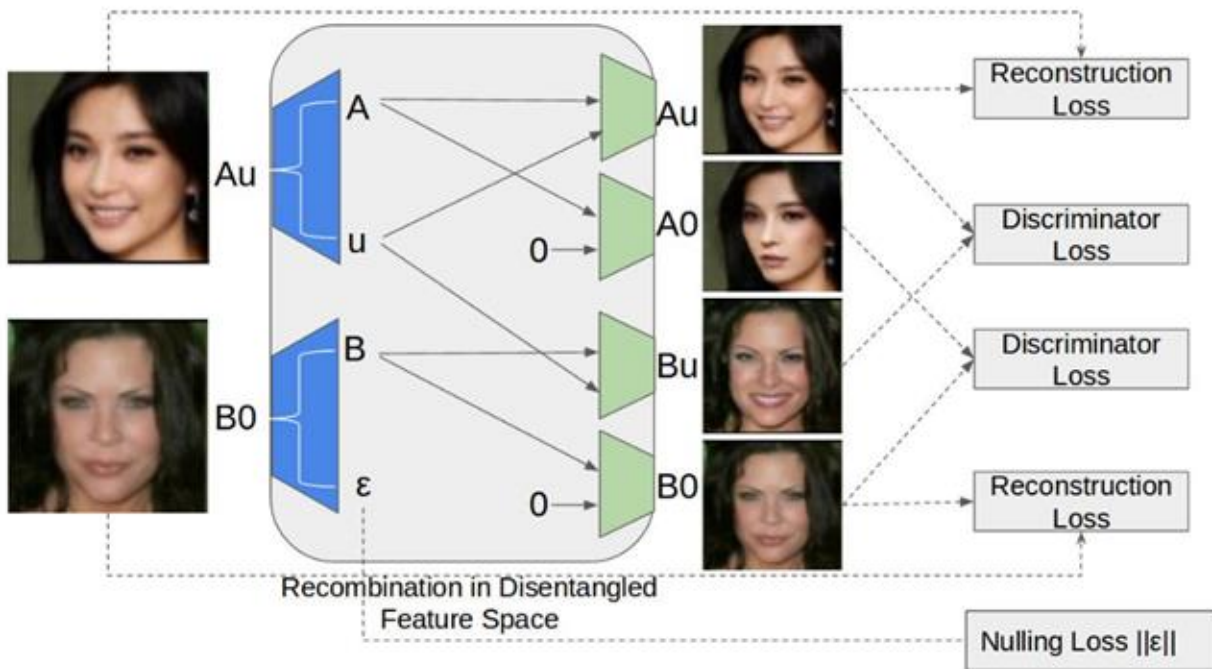


Information Preserving GeneGAN pattern



GeneGAN: shorter pathway improves training

Cross breeds and reproductions



GeneGAN: Object Transfiguration

Transfer "*my*" hairstyle to him, not just *a* hairstyle.

[Slide](#)

[Github](#)



Math behind Generative Models

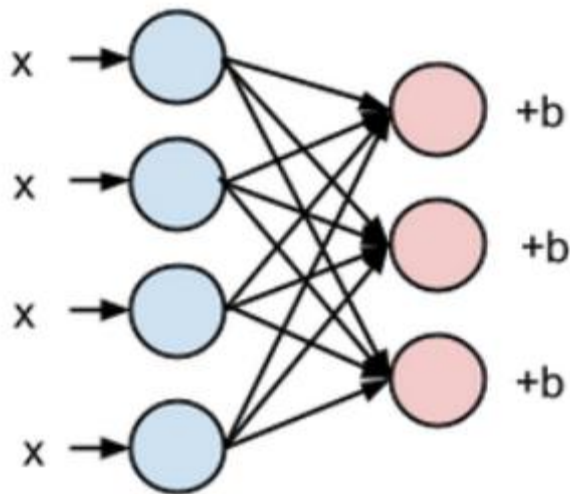
Those who don't care about math or theory can open their
PyTorch now...

Formulation of Generative Models

sampling v.s. density estimation

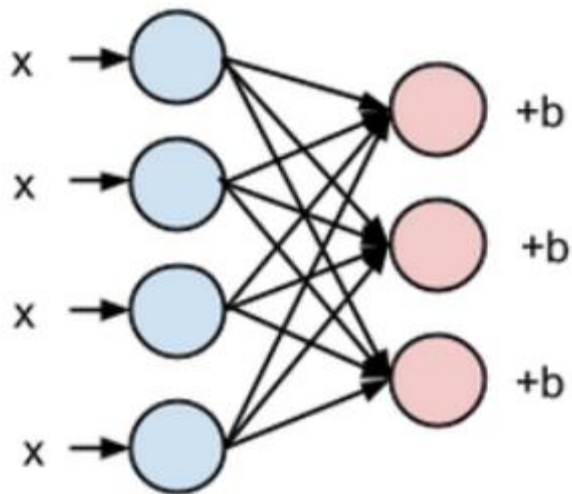
RBM

$$p(x) = \frac{1}{Z} \sum_{y \in \{0,1\}^n} e^{x^T A y + x^T b + y^T c}$$



RBM

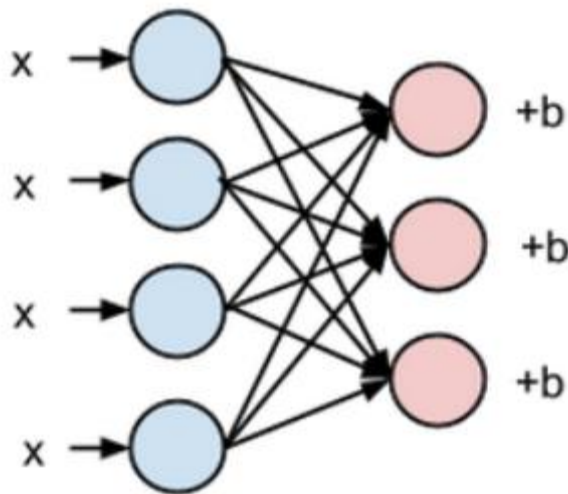
$$p(x) = \frac{1}{Z} \sum_{y \in \{0,1\}^n} e^{x^T A y + x^T b + y^T c}$$



It is NP-Hard to estimate Z

RBM

$$p(x) = \frac{1}{Z} \sum_{y \in \{0,1\}^n} e^{x^T A y + x^T b + y^T c}$$



It is NP-Hard to sample from P

Score Matching

Let L be the likelihood function, score V is:

$$V \equiv V(\theta, X) = \frac{\partial}{\partial \theta} \log \mathcal{L}(\theta; X) = \frac{1}{\mathcal{L}(\theta; X)} \frac{\partial \mathcal{L}(\theta; X)}{\partial \theta}$$

If two distribution's scores match, they also match.

A Connection Between Score Matching and Denoising Autoencoders

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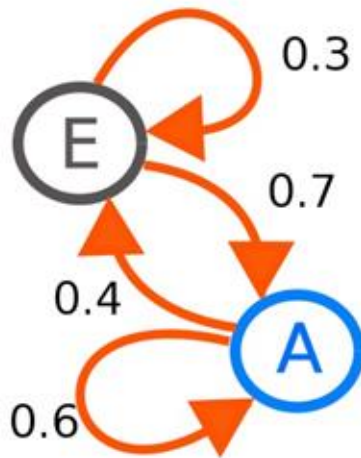
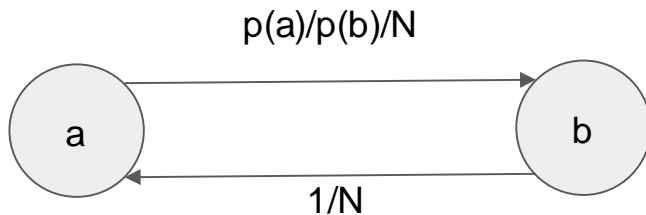
Markov Chain Monte Carlo

From each node a ,

walk to “neighbor” b with probability **proportional** to $p(b)$.

Neighbors must be reciprocal: $a \leftrightarrow b$

Walk for long enough time to reach equilibrium



MCMC in RBM

Sample x given y

Sample y given x

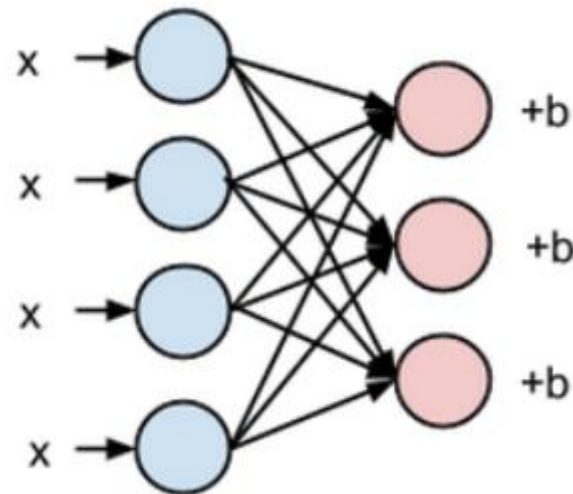
Sample x given y

.....

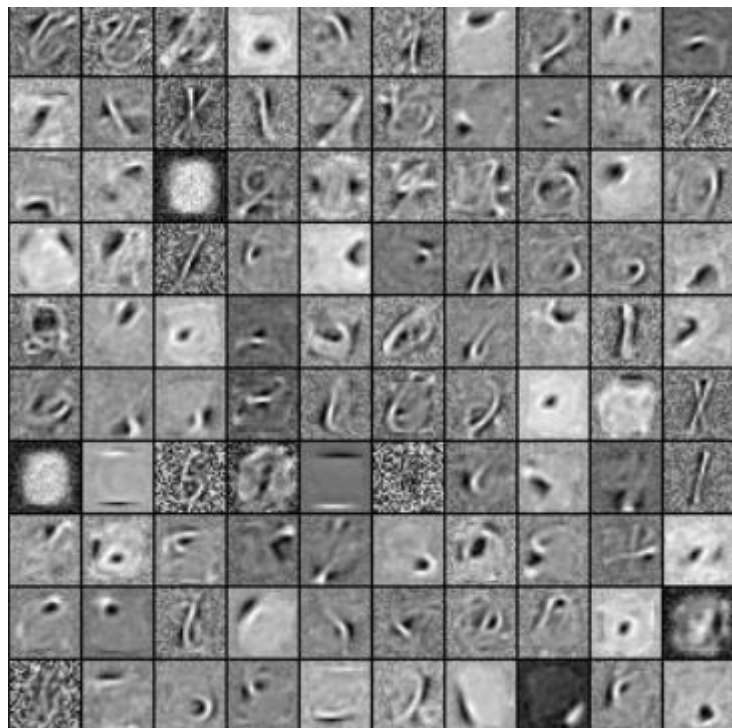
In theory, repeat for long enough time.

In practice, repeat a few times. ("burnin")

$$p(x) = \frac{1}{Z} \sum_{y \in \{0,1\}^n} e^{x^T A y + x^T b + y^T c}$$



RBM: Learned “Filters”



From Density to Sample

Given density function $p(x)$, can we efficiently black-box sample from it?

No! $p(x) = \text{MD5}(x) == 0$

Unless query $\Omega(N)$ samples, it is hard to determine.

From Sample to Density

Given black-box sampler G , can we efficiently estimate the density (frequency) of x ?

Naive bound: $\Omega(\varepsilon^{-2})$ absolute, $\Omega(1/p(x) \varepsilon^{-2})$ relative

Cannot essentially do better.

Example: Sample x randomly. Retry iff $x=0$.

What can be done if only samples are available?

Problem: Given black box sampler G , decide if:

- (1) it is uniform
- (2) it is ϵ -far from uniform

How to define distance between distributions?

Statistical distance: $\frac{1}{2} \sum |p(x) - q(x)|$ $p:G$ $q:\text{Uniform}$

L2 distance: $\sum (p(x) - q(x))^2$

KL divergence: $\sum q(x) \log(q(x)/p(x))$

Uniformity Check using $q(x)\log(q(x)/p(x))$

Impossible to check unless $\Omega(N)$ samples are obtained.

Consider $\{1, 2, \dots, N\}^T$ and $\{1, 2, \dots, N-1\}^T$. Unbound KL.

Statistical distance = $\sum \max(p(x) - q(x), 0)$

$((N-1)/N)^T = 1 - o(1)$ if $T = o(N)$

Statistical distance is the best distinguisher's advantage over random guess!

advantage = $2 * |\Pr(\text{guess correct}) - 0.5|$

Uniformity Check using L2 Distance

$$\sum (p(x)-q(x))^2 = \sum p(x)^2 + q(x)^2 - 2p(x)q(x) = \sum p(x)^2 - 1/N$$

$p(x)^2$: seeing two x in a row

$\sum p(x)^2$: counting collisions

Algorithm: Get T samples, count the number of $x[i]==x[j]$ for $i < j$, divide by $C(T,2)$

variance calculation: $O(\epsilon^2)$ is enough!

Uniformity Check using L1 Distance

Estimate collision probability to $1 \pm O(\epsilon^2)$

$O(\epsilon^{-4} \sqrt{N})$ samples are enough.

Lessons Learned: What We Can Get From Samples

Given samples, some properties of the distribution can be learned, while others cannot.

Discriminator based distances

$$\max_D E(D(x))_{x \sim p} - E(D(y))_{y \sim q}$$

$0 \leq D \leq 1$: Statistical Distance

D is Lipschitz Continuous: Wasserstein Distance

Wasserstein Distance

Duality

Earth Mover Distance:

$$W_p(\mu, \nu) := \left(\inf_{\gamma \in \Gamma(\mu, \nu)} \int_{M \times M} d(x, y)^p \, d\gamma(x, y) \right)^{1/p}$$

Definition using Discriminator:

$$W_1(\mu, \nu) = \sup \left\{ \int_M f(x) \, d(\mu - \nu)(x) \mid \text{continuous } f : M \rightarrow \mathbb{R}, \text{Lip}(f) \leq 1 \right\}$$

Estimating Wasserstein Distance in High Dimension

The curse of dimensionality

There is no algorithm that, for any two distributions P and Q in an n -dimensional space with radius r ,

takes $\text{poly}(n)$ samples from P and Q and estimates $W(P, Q)$ to precision $o(1)^*r$ w.h.p.

Finite Sample Version of EMD

Let $W_N(P, Q)$ be the expected EMD between N samples from P and Q .

$$W_N(P, Q) \geq W(P, Q)$$

$$W(P, Q) \geq W_N(P, Q) - \min(W_N(P, P), W_N(Q, Q))$$

Projected Wasserstein Distance

The k-dimensional projected EMD: let σ be a random k-dim subspace

$$W^k(P, Q) = E_{\sigma} W(\sigma(P), \sigma(Q))$$

As a lower bounding approach

$$W(P, Q) \geq \sqrt{n} W^1(P, Q) \geq \sqrt{n} (W_N^1(P, Q) - W_N^1(P, P))$$

Game Theory: The Generator - Discriminator Game

Stackelberg Game:

min. D max. G

min. G max. D

Nash equilibrium

(G,D) where both G and D will not deviate

Which is the largest?

Linear Model

minimax theorem

Let $X \subset \mathbb{R}^n$ and $Y \subset \mathbb{R}^m$ be compact convex sets. If $f : X \times Y \rightarrow \mathbb{R}$ is a continuous function that is convex-concave, i.e.

$f(\cdot, y) : X \rightarrow \mathbb{R}$ is convex for fixed y , and

$f(x, \cdot) : Y \rightarrow \mathbb{R}$ is concave for fixed x .

Then we have that

$$\min_{x \in X} \max_{y \in Y} f(x, y) = \max_{y \in Y} \min_{x \in X} f(x, y).$$

The Future of GANs

Guaranteed stabilization: new distance

Broader application: apply adversarial loss in XX / different type of data

References

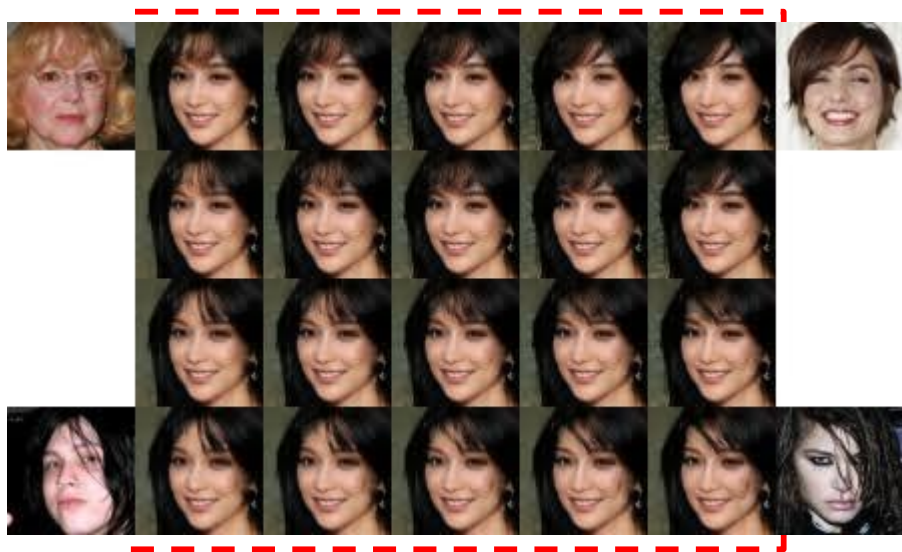
GAN Tutorial: <https://arxiv.org/pdf/1701.00160.pdf>

Slides: <https://media.nips.cc/Conferences/2016/Slides/6202-Slides.pdf>

Backup after this slide

GeneGAN: Interpolation in Object Subspace

Check the directions of the hairs.



Bi-linearly interpolated

