

# **Employee Turnover Prediction with Machine Learning: A Reliable Approach**

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Abstract. Supervised machine learning methods are described, demonstrated and assessed for the prediction of employee turnover within an organization. In this study, numerical experiments for real and simulated human resources datasets representing organizations of small-, medium- and large-sized employee populations are performed using (1) a decision tree method; (2) a random forest method; (3) a gradient boosting trees method; (4) an extreme gradient boosting method; (5) a logistic regression method; (6) support vector machines; (7) neural networks; (8) linear discriminant analysis; (9) a Naïve Bayes method; and (10) a K-nearest neighbor method. Through a robust and comprehensive evaluation process, the performance of each of these supervised machine learning methods for predicting employee turnover is analyzed and established using statistical methods. Additionally, reliable guidelines are provided on the selection, use and interpretation of these methods for the analysis of human resources datasets of varying size and complexity.

**Keywords:** Machine learning · Artificial intelligence · Data mining Data analytics · Data visualization · Feature selection · Model stability Employee turnover · Human resources management

#### 1 Introduction and Motivation

Employee turnover is one of the most significant problems an organization can encounter throughout its lifecycle, as it is difficult to predict and often introduces noticeable voids in an organization's skilled workforce [1]. Service firms recognize that the timely delivery of their services can become compromised, overall firm productivity can decrease significantly and, consequently, customer loyalty can decline when employees leave unexpectedly [8]. As a result, it is imperative that organizations formulate proper recruitment, acquisition and retention strategies and implement effective mechanisms to prevent and diminish employee turnover, while understanding its underlying, root causes [2, 3].

Most recently, the prevalence of intelligent machine learning algorithms in the field of computer science has led to the development of robust quantitative methods to derive insights from industry data. Supervised machine learning methods—wherein computers learn from analyses of large-scale, historical, labelled datasets—have been shown to garner insights in various fields, like biology and medical sciences [21, 22], transportation [23, 24], political science [25], as well as many other fields. Owing to the advancements in information technology, researchers have also studied numerous machine learning approaches to improve the outcomes of human resource (HR) management [2, 4, 5]. A detailed listing of recent studies in using supervised machine learning on employee turnover is described in Table 1, and lists the data included and related machine learning algorithms that were used therein, including decision tree (DT) methods, random forest (RF) methods, gradient boosting trees (GBT) methods, extreme gradient boosting (XGB), logistic regression (LR), support vector machines (SVM), neural networks (NN), linear discriminant analysis (LDA), Naïve Bayes (NB) methods, K-nearest neighbor (KNN), Bayesian networks (BN) and induction rule methods (IND).

The performance evaluation of machine learning algorithms has also been studied previously by various researchers [6, 9, 13, 14]. Notably, Punnoose and Ajit [13] compared the predictive capabilities of seven different machine learning algorithms, including recently developed algorithms, like Extreme Gradient Boosting [26], on employee turnover. Similarly, Sikaroudi and co-researchers [14] conducted simulations to predict employee turnover using ten different data mining algorithms, including tests on various types of neural networks and induction rule methods.

In addition to placing focus on classification and prediction ability, many researchers have also made substantial efforts to better understand which features (e.g. compensation, age, work experience, etc.) are most influential in predicting employee turnover [1–4, 8, 9, 14]. These features seldom carry equal value in data mining applications, so it is useful to gain a better understanding of their importance [34].

For instance, many of the studies using tree-based quantified feature importance by calculating the impurity reduction by node split in decision trees [1, 35]. Moreover, modified genetic algorithms [8] and sensitivity analysis [6] have been used to understand relative feature importance as well. Numerous studies have also generated classification rules or visualized the classification procedure to provide further insight and confidence in using machine learning methods [2, 6, 35].

Despite the breadth of research outcomes mentioned above, the findings for predicting employee turnover that stem from using machine learning methods are often problem-specific and difficult to generalize. First and foremost, this is primarily because HR data is confidential [7], which inherently impedes conducting in-depth analyses on multiple datasets. In addition, HR data is often noisy, inconsistent and contains missing information [4, 13], a problem that is exacerbated by the small proportion of employee turnover that typically exists within a given set of HR data. Secondly, gaps tend to persist in model performance evaluation. Specifically, previous research on the assessment of machine learning algorithms has generally focused on a narrow evaluation of metrics across various models.

**Table 1.** Overview of recent studies in the application of supervised machine learning methods to predict employee turnover

size of features [1] 309 9 9 [2] 130	ures	type				)	Sapervises maximic reming means							
309 130 881 3852 150 536 < 100	sam		DT	RF	GBT	XGB	LR	SVM	NN	LDA	NB	KNN	BN	IND
309 130 881 3852 150 150 < 100														
130 881 3852 150 150 < 100		Higher	Yes	ı	ı	I	ı	I	I	1	I	ı	ı	ı
130 881 3852 150 150 < 100 < 7577		education												
3852 150 150 536 < 100		IT industry	Yes	1	1	I	1	1	1	1	Yes	1	1	
3852 150 536 < 100		Manufacturing	ı	ı	ı	I	ı	1	I	ı	I	Yes	ı	1
536 < 100		High-tech	Yes	ı	ı	I	ı	I	ı	1	I	1	ı	ı
536 < 100		industry												
536 < 100		Software	Yes	ı	ı	I	Yes	I	Yes	Yes	I	1	ı	1
<ul><li>536</li><li>&lt; 100</li><li>&lt; 2577</li></ul>		company												
< 100		Child welfare	1	1	1	ı	Yes	ı	Yes	1	ı	ı	ı	ı
< 100		agency												
2572		Fabrication	ı	ı	ı	I	ı	I	Yes	1	I	1	ı	ı
2572		firm												
1		IT industry	Yes	Yes	ı	ı	ı	ı	ı	1	Yes	ı	Yes	ı
_ [10] 768		Nurse data	1	1	ı	I	ı	Yes	ı	ı	I	1	ı	
		from hospital												
[11] 1037 –		Call center	Yes	ı	ı	I	ı	ı	ı	ı	Yes	ı	ı	ı
[13] 73115 –		Global retailer	Yes	Yes	ı	Yes	Yes	Yes	ı	Yes	Yes	Yes	ı	ı
[14] – 14		Arak company	Yes	Yes	ı	I	Yes	Yes	Yes	ı	Yes	Yes	ı	Yes
[38]   132   -		Marketing	1	1	ı	ı	Yes	Yes	1	1	ı	1	1	
		firm												
[40] 577 –		Medical center	1	1	ı	ı	Yes	ı	Yes	1	I	ı	ı	ı

Accuracy has traditionally been selected as the primary evaluation standard for this problem, but this approach is questionable as accuracy measures are not reliable for imbalanced datasets [2, 8, 10, 14]. As the proportion of people who leave an organization is generally much smaller than that of those who stay, there is often a risk of computing misleadingly high accuracy correlations. The deficiency of the analysis is often made worse by the limited use of statistical instruments, often only opting for relatively simple comparisons instead. Thirdly, the attempt to improve the model interpretability by ranking feature importance and visualizing classifier rules should be executed cautiously. The analysis of feature importance in several studies [1, 3, 8, 9, 35] could be biased as it takes classifier-dependent approaches, where model performance matters. For instance, some works [1, 35] use decision trees to calculate the feature importance as part of the model building process. However, if decision trees do not perform well, the corresponding feature importance result may be inaccurate. With the assumption that decision trees perform well, visualizing their classification rules could improve the model interpretability. However, decision trees come with high variance and low stability, resulting in precarious model interpretation with a small change in data [34].

The aim of this paper is to provide a comprehensive description, demonstration and assessment of supervised machine learning approaches for the prediction of employee turnover within organizations of varying size. In the present study, ten supervised machine learning methods are evaluated for organizations of small-, medium- and large-sized populations. Details of each supervised machine learning method are given and the benefits, capabilities and performance of each are provided in the context of predicting employee turnover. The effect of data size and data type, and how to get reliable feature importance and data visualization are also discussed. Lastly, general guidelines are provided on the selection, use and interpretation of these ten supervised machine learning methods for reliable analysis of HR datasets of varying size and complexity.

# 2 Methodology

In this research, various supervised machine learning algorithms are described, demonstrated and assessed in their ability to predict employee turnover. This section provides a general overview of the theory behind these algorithms.

#### 2.1 Decision Tree (DT)

Decision tree is a supervised method which builds classification or regression models in a tree-like structure. It is an established method that was first published in 1963 by Morgan and Sonquist [31]. The decision tree method is: (1) conceptually easy yet powerful [34]; (2) intuitive for interpretation; (3) capable of handling missing values and mixed features [44]; and (4) able to select variables automatically [20, 44]. However, its predictive power is not overly competitive. Decision tree is usually not stable with high model variance [44] and small variations in the input data would result in a large effect on the tree structure [17].

### 2.2 Random Forests (RF)

Random forests take an ensemble approach that provides an improvement over the basic decision tree structure by combining a group of weak learners to form a stronger learner (see the paper by Breiman [28]). Ensemble methods utilize a divide-and-conquer approach to improve algorithm performance. In random forests, a number of decision trees, i.e., weak learners, are built on bootstrapped training sets, and a random sample of m predictors are chosen as split candidates from the full set P predictors for each decision tree. As  $m \ll P$ , the majority of the predictors are not considered. In this case, all of the individual trees are unlikely to be dominated by a few influential predictors. By taking the average of these uncorrelated trees, a reduction in variance can be attained [34], making the final result less variable and more reliable [44].

# 2.3 Gradient Boosting Trees (GBT)

Gradient boosting trees is an ensemble machine learning method proposed in 2001 by Friedman [30] for regression and classification purposes. The difference between RF and GBT is the gradient boosted tree models learn sequentially. In GBT, a series of trees are built and each tree attempts to correct the mistakes of the previous tree in the series. Trees are added sequentially until no further enhancement can be achieved. Making predictions in GBT is fast and memory-efficient; boosting could be viewed as a form of  $\ell_1$  regularization to reduce overfitting [20]. However, unlike highly interpretable single DT, GBT is harder to visualize and interpret [34].

## 2.4 Extreme Gradient Boosting (XGB)

Extreme Gradient Boosting is a tree-based method that was introduced in 2014 by Chen [26]. It is also commonly referred to as XGBoost. It is a scalable and accurate implementation of gradient boosted trees, explicitly designed for optimizing the computational speed and model performance. Compared to gradient boosting, XGBoost utilizes a regularization term to reduce the overfitting effect, yielding a better prediction [13] and much faster computational run times.

#### 2.5 Logistic Regression (LR)

Logistic Regression is a traditional classification algorithm involving linear discriminants, as originally proposed in 1958 by Cox [37]. The primary output is a probability that the given input point belongs to a certain class. Based on the value of the probability, the model creates a linear boundary separating the input space into two regions. Logistic regression is easy to implement and work well on linearly separable classes, which makes it one of the most widely used classifiers [43].

#### 2.6 Support Vector Machine (SVM)

Support vector machine was initially proposed in 1995 by Vapnik and Cortes [36]. SVM is commonly used as a discriminative classifier to assign new data samples to one

of two possible categories. The basic idea of SVM is to define a hyperplane which separates the n-dimensional data into two classes, wherein the hyperplane maximizes the geometric distance to the nearest data points, so-called support vectors. It is noteworthy that practical linear SVM often yields similar results as logistic regression [43].

In addition to performing linear classification, SVM also introduces the idea of a kernel method to efficiently perform non-linear classification. It is a feature mapping methodology which transfers the attributes into a new feature space (usually higher in dimension) where the data is separable. For further details, refer to the paper by Muller and co-researchers [32].

#### 2.7 Neural Networks (NN)

Neural networks, also known as multi-layer perceptron, are designed to simulate the operations of the human nervous system. The simplest form of a neural network is a single perceptron. Essential elements for a perceptron are input values, associated weights, bias, activation functions and a computed output. Commonly used activation functions include the sigmoid, hyperbolic tangent (Tanh) and rectified linear units (ReLU). A neural network may contain more than one layer between input and output to handle complex problems.

This sophisticated structure of neural networks makes it a universal approximation tool which could model any smooth function to any desired level of accuracy, given enough hidden units [20]. One can extend the model to become deep with more advantages [20], in what is commonly referred to as deep learning. Due to the rapid development of hardware and the continuous exploration of backpropagation techniques, neural networks are currently the most heavily researched topic in machine learning.

# 2.8 Linear Discriminant Analysis (LDA)

Linear Discriminant Analysis is a commonly used topic modelling technique. It is a generalization of Fisher's linear discriminant, proposed in 1936 by Fisher [19]. LDA dedicates to find the optimal linear combination that can separate data into different clusters by projecting data samples into a lower-dimension space. Unlike the Principle Component Analysis (PCA), LDA is a supervised method, although its performance may be inferior to PCA in certain cases [43].

LDA assumes the data is normally distributed, the class share the identical covariance and features are all independent an identically distributed. To conduct the classification, LDA measures the distance between projected means and utilizes a scatter matrix to maximize the ratio of between-class sample distance to the within-class sample distance.

#### 2.9 Naïve Baves (NB)

Naïve Bayes is a probabilistic approach that uses Bayes Theorem. The Bayes Theorem describes the occurrence probability of an event based on the prior knowledge of

related features. The other important characteristic of Naïve Bayes is the conditional independence assumption of its features. This assumption indicates that the presence of a feature would not influence any other features. Naïve Bayes classifiers first learn joint probability distribution of their inputs by utilizing the conditional independence assumption. Then, for a given input, the methods produce an output by computing the maximum posterior probability with Bayes Theorem. See the paper by Zhang [33] and the book by Géron [17] for more details.

# 2.10 K-Nearest Neighbors (KNN)

K-nearest neighbors is a non-parametric algorithm used for classification and regression problems. For classification problems, the idea is to identify the K data points in the training data that are closest to the new instance and classify this new instance by a majority vote of its K neighbors. In practice, the popular distance measures include the Euclidean distance, the Manhattan distance as well as the Minkowski distance. For regression problems, the idea is to calculate the new instance value by taking the average of its K neighbors. KNN could work well with a small number of features, but it struggles when the feature dimensions increase drastically. See the book by Friedman, Hastie and Tibshirani [34] and the book by Murphy [20] for further information.

# 3 Human Resource Datasets

#### 3.1 Data Sources

In this research, two primary datasets were collected with all personally identifiable information cleansed. The first dataset originates from a regional bank in the United States of America. The bank data was collected from 2013 to 2016, during which time roughly 28% of the bank's employees had left. The raw bank dataset contains 14,322 employee entries and 24 features. The second dataset is a simulated dataset created by IBM Watson Analytics [15] and is included in this research to facilitate a more thorough analysis. The IBM dataset contains 1,470 employee entries and 38 features, in which 237 employees (roughly 16%) left. Some necessary data cleaning was introduced. Firstly, all individuals marked as temporary workers were removed from the datasets. Secondly, any unique-value features that were consistent amongst all employee entries were removed. Following these basic data cleaning procedures, the final datasets consisted of 9,089 employees with 19 features for Bank data and 1,470 employees with 31 features for IBM data. Both datasets contained common HR features like age, compensation, gender and education.

# 3.2 Data Sampling and Simulation

As discussed in the introduction of this paper, previous studies have always focused on a single, small-sized dataset. To best assess the performance of machine learning algorithms in a variety of different settings (i.e., various dataset sizes), data sampling methods were employed to create additional datasets from the two main sets of data.

With the number of features and turnover rate fixed, additional datasets are randomly down-sampled from original datasets without replacement. This process ensured that all newly generated datasets contained minimal overlap. As the intention is to bring diversity and restrict complexity, this research does not use sampling methods like Markov Chain Monte Carlo [34].

Using this sampling method, eight additional HR datasets of varying size were created to augment the original two datasets. The total ten resultant datasets are detailed in Table 2, where the original datasets are bolded. To simplify the comparative analysis, the datasets were categorized into three main groups based on their size: small, medium and large.

Dataset	Group	Population size	Feature	Turnover rate
50_Bank	Small	50	19	0.2800
50_IBM	Small	50	31	0.1600
100_Bank	Small	100	19	0.2800
100_IBM	Small	100	31	0.1600
500_Bank	Medium	500	19	0.2820
500_IBM	Medium	500	31	0.1600
1000_Bank	Medium	1000	19	0.2830
1500_IBM	Medium	1500	31	0.1612
5000_Bank	Large	5000	19	0.2834
9000_Bank	Large	9000	19	0.2834

Table 2. List of experimental and simulated datasets

# 3.3 Data Preprocessing

Data preprocessing is commonly performed in employee turnover prediction studies as the datasets usually contain missing entries, varying degrees of noise and substantial differences in scale per feature. See the papers by Alao and Adeyemo [1], Chang [3] and Chien and Chen [4]. For each dataset listed in Table 2, the following data preprocessing techniques were used to best generate meaningful results.

# (1) Missing Value Imputation

Missing values were imputed to guarantee that all the algorithms would be able to handle them. Nevertheless, some algorithms could deal with missing values automatically without imputation, such as XGBoost. To restrict the comparison complexity, the missing values were imputed based on their data type. For numerical data types, the missing entries are replaced by the median value of the complete entries. For categorical data, the missing entries were replaced by the mode value of the complete entries.

# (2) Data Type Conversion and Feature Selection

One of the essential data preprocessing procedures is to convert categorical variables to numerical format. Some algorithms, such as logistic regression, neural

networks and K-nearest neighbor, are not able to work directly with categorical variables. Traditionally, researchers typically utilize one-hot encoding to conduct the conversion from categorical to numerical data type formats [7, 13] which converts each of the distinct values in a categorical value to binary fields. Naturally, this conversion may significantly increase feature dimensions, provided there are many distinct values for a categorical feature. In this research, data conversion was performed using label encoding via the Scikit-learn package in Python [18]. The feature selection methods are often used to further improve the classifier's predictive capabilities by selecting relevant attributes. In addition, dimensionality reduction methods like principal component analysis are used if the data dimensionality is high. In an effort to restrict the complexity of the results analysis and the interpretation needed of HR data, neither feature selection nor dimensionality reduction was used.

# (3) Feature Scaling

Feature scaling is a data mining approach to adjust the range of features and reduce disparate feature scales. This may help some machine learning classifiers perform better, because significant scale gaps among features are generally not favored within the optimization stage of these algorithms. For example, neural networks are recommended to scale the inputs to achieve good results [34]. In HR datasets, features generally have significantly disparate scales. For example, employee ages could be in the range of 18 to 74 years old, whereas the compensation range could be \$24,521 to \$2,323,000. In this research, both normalization and standardization were performed on the original datasets for a complete assessment.

# 4 Experiment Design

The design of the numerical experiments performed in this research has been created with the intent to comprehensively measure the effectiveness of various supervised machine learning algorithms. Details of the experiment design are presented herein to describe the evaluation criteria, algorithm effectiveness and procedures that were used in conducting the numerical experiments performed in this research.

#### 4.1 Evaluation Matrices

In employee turnover analytics, the imbalance of individuals who left and those who stayed should be taken into account. As defined previously in Table 2, the turnover rate is always below 0.50 (Bank dataset: 0.2834, IBM dataset: 0.1612), making the accuracy an inherently biased measure. To remedy this issue, additional evaluation metrics are introduced to provide complete coverage and analysis of the results.

In this research, the positive class is assigned to the employees who turn over, while the negative class consist of the employees who stay. Five evaluation metrics are introduced in the evaluation of the supervised machine learning algorithms

studied in this research: (1) accuracy (ACC) is defined as the percentage of the correctly classified data by the model; (2) precision (PRC) is defined as the number of true positives divided by the sum of true positives and false positives; (3) recall

(RCL) is defined as the number of true positives divided by the sum of true positives and false negatives; (4) F1 is defined as the harmonic mean of precision and recall; and (5) Receiver operating characteristic (ROC) curve is defined as a graphical plot of the tradeoff between precision and recall [17]. The area under the ROC curve provides another view of the quality of classifiers which is used in this study. As ROC yields further insights in classifier performance regarding imbalanced samples [43], it has been selected as the primary evaluation standard in this research.

### 4.2 Probability and Statistical Analysis

Non-parametric Kruskal-Wallis tests followed by Dunn's post-hoc test [42] were used to conduct multi-group comparison on classifier performances (e.g. data type, size and model selection). The Mann-Whitney U test [41] was used to conduct pairwise comparisons between two groups. For these tests, the probability P < 0.05 was considered significant while the remainder was considered non-significant (NS).

Probability and information theory methods were also used in this study to analyze data characteristics. In general, mutual information (MI) measures how much uncertainty is reduced about random variable (RV) Y after X is observed. MI between X and Y,  $\mathbb{I}(X|Y)$ , is given as follows, where p is the probability:

$$\mathbb{I}(X|Y) = \sum_{x} \sum_{y} p(x, y) \log \frac{p(x, y)}{p(x)p(y)}$$
 (1)

In this study, features include both discrete and continuous RVs. However, MI is only feasible for a pair of discrete RVs, rather than continuous RVs. Therefore, the maximal information coefficient (MIC) was introduced to quantify the linear and nonlinear correlation [20] between features and the predicted value. MIC could measure the MI between continuous and discrete RVs, ranging from 0 (no correlation) to 1 (fully correlated). The function m(x, y) is defined as the approximately maximized MI with various bin sizes and locations while discretizing a continuous random variable:

$$m(x,y) = \frac{\max_{G \in g(x,y)} \mathbb{I}(X(G)|Y(G))}{\log \min(x,y)}$$
 (2)

Where, y(x, y) is the set of 2-dimensional grids with size  $x \times y$ .  $\mathbb{I}(X(G)|Y(G))$  is MI (Eq. 1) enumerated on y(x, y). MIC is then given as:

$$MIC \triangleq \max_{x,y;xy < B} m(x,y) \tag{3}$$

Where, x and y are two RVs and B is a sample size dependent bound.

## 4.3 Model Building and Validation

Cross validation is used to assess the generalization ability of an algorithm on an independent dataset. It can prevent a model from overfitting that is possibly caused by

the high complexity of the model. Grid search is a parameter searching algorithm that is used to automatically find the most optimal parameters within a predefined range [17].

All of the datasets listed in Table 2 were run against the ten algorithms introduced in Sect. 2 with data preprocessing methods. In total, there were 10 datasets, 10 algorithms and 3 data formats (raw, normalized, standardized), yielding a total of 300 numerical experiments performed in this research. For each numerical experiment, the optimal algorithm parameters were defined by the Grid Search technique within a predefined range using GridSearchCV package [18]. Once the optimal parameter was found, the accuracy, precision, recall, F1 and ROC values were calculated using 10-fold cross validation.

#### 5 Results and Discussions

The results of the numerical experiments for datasets representing small-, medium- and large-sized organizations are presented in this section. Various statistical methods mentioned above were utilized to analyze the results: the Kruskal-Wallis test was used to identify significant performance difference in multi-groups, and Dunn's test was applied as the post-hoc test. Although the experimental datasets may deviate slightly from other real-world employee profiles and turnover datasets for varying size of organizations, the datasets used in this research provide a framework to perform a complete and comparative analysis across various machine learning algorithms. Furthermore, the study limited the use of advanced feature engineering methods like feature selection and dimensionality reduction; it is understood that these types of methods would likely increase the predictive capabilities. Lastly, it should be noted that the scope of the presented results and discussion is limited to describing how best to use the data mining methods to understand employee turnover, rather than how best to reduce it. The latter is beyond the scope of this paper.

#### 5.1 Results for Small HR Datasets

The results of small datasets are summarized in Table 3, wherein the top-performing algorithm (based on highest ROC value) for each dataset is bolded within each row. It is worthwhile to note that the ROC value for the 50\_IBM data is not very reliable due to the small dataset size (and low turnover rate), so the F1 score was used in its place. The results presented in Fig. 1 illustrate that no algorithm could consistently outperform the others for small datasets. It is believed it is due to high variance in small datasets, which will be described in further detail shortly.

Dataset	ACC	PRC	RCL	F1	ROC
50_Bank	DT	SVM	DT	DT	RF
50_IBM	NN	NN	NN	NN	_
100_Bank	DT	XGB	GBT	XGB	XGB
100_IBM	LR	SVM	NB	NB	LR

**Table 3.** Best performance classifiers on small datasets

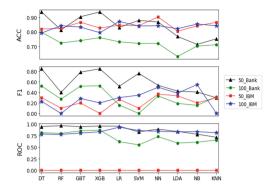


Fig. 1. Classifier performances on small datasets.

For the highest ROC values across small-dataset experiments, random forests achieved 0.9625 for the 50\_Bank dataset, extreme gradient boosting reached 0.8673 on the 100\_Bank dataset and logistic regression accomplished 0.9299 on the 100\_IBM dataset. For the 50\_IBM dataset, the ROC value is not available due to the small dataset size, but it was found that neural networks score the highest for all other evaluation metrics (ACC, PRC, RCL and F1).

#### 5.2 Results for Medium HR Datasets

The results for medium-sized datasets indicate that gradient boosting trees generally rank the highest, as shown in Table 4 and Fig. 2. The highest ROC values for the 500\_Bank, 500\_IBM, 1000\_Bank and 1500\_IBM datasets were 0.9486, 0.7780, 0.9634, and 0.8434, respectively.

Dataset	ACC	PRC	RCL	F1	ROC
500_Bank	XGB	RF	XGB	XGB	GBT
500_IBM	NN	LDA	NN	NN	NN
1000_Bank	XGB	RF	XGB	XGB	XGB
1500_IBM	LR	LDA	NN	NN	GBT

**Table 4.** Best performance classifiers on medium datasets

Neural networks appeared to rank the second highest, behind gradient boosting trees, as they gained the highest ROC value at 0.778 for the 500\_IBM dataset, as well as the second highest ROC classifier on the 1500\_IBM dataset, at 0.840. On the 1500\_IBM dataset, neural networks were found to have very similar ROC values as gradient boosting trees (0.840 and 0.843, respectively) and better results for all other metrics. As a result, it is reasonable to state that for the 500\_Bank and 1000\_Bank datasets, gradient boosting trees are the top performers, whereas for the 500\_IBM and 1500\_IBM datasets, neural networks performed the best. Gradient boosting trees and neural networks have great ability to fit complex data, which explains their decent performance on medium datasets.

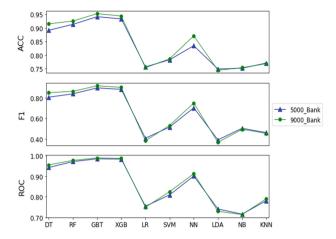


Fig. 2. Classifier performances on medium datasets.

# 5.3 Results for Large HR Datasets

The results of the large datasets are most consistent, where it was found that gradient boosting trees score highest across all measures for both large-sized datasets (Table 5, Fig. 3). The highest ROC values for these datasets are 0.9844 for 5000\_Bank and 0.9885 for 9000\_Bank. Similar to that in medium group, extreme gradient boosting has similar performance as gradient boosting trees. Gradient boosting trees outperform as the trees could generalize well, require minimal data preprocessing, and show great robustness to noisy and missing values.

 Dataset
 ACC
 PRC
 RCL
 F1
 ROC

 5000
 Bank
 GBT
 GBT
 GBT
 GBT
 GBT
 GBT

GBT

GBT

GBT

**GBT** 

**GBT** 

**Table 5.** Best performance classifiers on large datasets

#### 5.4 Effect of Data Source and Data Size

9000 Bank

The effect of data sources (Bank and IBM) was studied first. A Mann-Whitney U test on classifier ROC was not significant (U = 811, P = 0.2243), which implies the data source may not affect the classifier performance; therefore grouping different datasets by size is an appropriate approach.

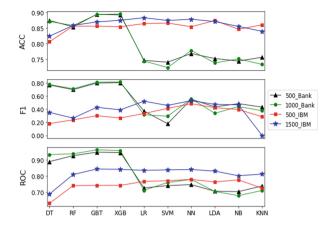


Fig. 3. Classifier performances on large datasets.

Figure 1 shows that for small datasets the best classifier results tend to be more arbitrary in nature, wherein no algorithms could always perform well across all evaluation metrics. As the size of the dataset increases, the top-performing classifier results tend to be more consistent (see Figs. 2 and 3). However, the Kruskal-Wallis test revealed no significant effect of data size (small, medium, large) on ROC value of classifiers ( $\chi^2 = 5.6955, P = 0.0580$ ). Table 6 also shows there is no obvious ROC difference for the three data groups.

**Table 6.** Performance analysis by groups (ROC)

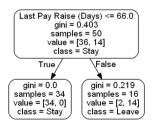
Group	Median	Mean	STD
Small	0.8295	0.8052	0.1129
Medium	0.8052	0.7940	0.0883
Large	0.8629	0.8606	0.1077

The reason for this contradictory observation might be explained by first discussing the characteristics of the datasets. Through the findings presented earlier, HR data usually contains missing and incorrect values, leading to poor quality. The randomness of a small HR dataset, such as 50\_Bank, could be high due to noise and various anomalies. This leads to the tendency of classifiers to overfit on small datasets when a large number of features are present. For example, the 50\_IBM dataset has 31 features but only 50 samples. Additionally, the underlying reasons for employee turnover could be quite complex from case to case, and the event itself could often be considered as fairly stochastic. With this in mind, a small-sized HR dataset may not be able to best capture all underlying reasons behind employee turnover [17], due to its inherent sensitivity to Hughes phenomenon [16]. The small dataset group results look spurious, as they may be dominated by their susceptibility to mediocre data quality and scarcity of features.

To confirm the assumption above, uncertainty analysis was conducted to understand the characteristics of the datasets. The MIC introduced in (3) could quantify the correlation between two random variables. Table 7 summarizes the MIC among features and turnover results in pairwise manner on all datasets. The results indicate that features in small datasets generally have a higher correlation with the turnover results. In 50 Bank, the most influential feature, last pay raise, has a large MIC at 0.8556, which almost dominates the classification result. In 100 IBM data, the highest MIC feature is employee ID, which should be removed in most of the scenarios using common sense. To further investigate the cause, the classification rules on the 50 Bank dataset were visualized using a decision tree (see Fig. 4). It only uses one feature, last pay raise, in its prediction, testing whether an individual has received a pay raise in the last 66 days. This observation confirms the finding using MIC. Even with this single feature and simple classification rule, the model achieves a ROC value of 0.944 and an accuracy of 0.938, and only 2 to 3 employees out of the 50 total are misclassified. Nevertheless, the promising results of small-sized datasets do not guarantee the algorithms are working correctly—it could be due to poor data quality that few features accidently dominate the prediction. This suggests that it is well worth the effort to further investigate the data itself [17]. The classification visualization was repeated for medium- and large-sized datasets, and the results are more reliable than that of smallsized datasets. More features are involved, and the classification rule is more complex. This explains the randomness of best classifiers on small datasets, and more consistent performances on medium and large datasets.

	1	1	ı	1	I
Dataset	Group	Mean	STD	Max	Max feature
50_Bank	Small	0.1834	0.2058	0.8555	Pay raise
100_Bank	Small	0.1150	0.1237	0.5355	Pay raise
500_Bank	Med	0.0945	0.1328	0.5726	Pay raise
1000_Bank	Med	0.0785	0.1295	0.5665	Pay raise
5000_Bank	Large	0.0753	0.1434	0.6250	Pay raise
9000_Bank	Large	0.0750	0.1463	0.6322	Pay raise
50_IBM	Small	0.1284	0.1042	0.3844	Pay/month
100_IBM	Small	0.0876	0.0760	0.2460	Personal ID
500_IBM	Med	0.0471	0.0486	0.1733	Pay/month
1500_IBM	Med	0.0323	0.0352	0.1389	Pay/month

**Table 7.** Mic on all datasets (bank and IBM)



**Fig. 4.** Decision tree visualization on 50\_Bank.

# 5.5 Classifier Performance Analysis

Table 8 ranks classifier performances by median ROC across all datasets. A Kruskal-Wallis test of ROC differences among classifiers was conducted and rendered  $\chi^2=32.4113$  which was significant (P=0.002). A post-hoc test using Dunn's test revealed significant differences among algorithms. Figure 5 illustrates the results of Dunn's test as a heat map. P<0.01 and P<0.001 were also emphasized, although P<0.05 was considered as the evidence of significance. For instance, Fig. 5 tells that extreme gradient boosting performance is significantly different from that of Naïve Bayes (P=0.003), and KNN (P=0.007).

Table of Classifier performance by Noc							
Dataset	Median	Mean	STD	Min	Max		
XGB	0.9462	0.9008	0.0847	0.7411	0.9862		
GBT	0.9417	0.8960	0.0890	0.7408	0.9886		
RF	0.9266	0.8771	0.0955	0.7397	0.9768		
DT	0.8897	0.8412	0.1215	0.6289	0.9550		
NN	0.8407	0.8234	0.0690	0.7268	0.9124		
SVM	0.8096	0.7751	0.0935	0.5489	0.8571		
LR	0.7543	0.7820	0.1062	0.6179	0.9500		
LDA	0.7410	0.7473	0.0804	0.5875	0.8375		
KNN	0.7373	0.7474	0.0543	0.6511	0.8117		
NB	0.7160	0.7340	0.0698	0.6080	0.8333		

Table 8. Classifler performance by ROC

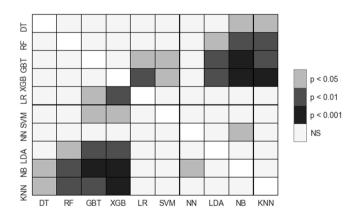


Fig. 5. Classifier performance difference heatmap by Dunn's test.

In this research, tree-based classifiers (XGB, GBT, RF, DT) worked well in general, and were found to be the top four best performing classifiers. Extreme gradient boosting had the best overall performance, and gradient boosting trees ranked second and performed best for the bank datasets. Neural networks ranked behind tree-based methods as the fifth, performing better for the IBM datasets. These methods were found to be most robust and they could handle the HR datasets which contained noise, missing values and were imbalanced. Focusing on tree-based methods, another Kruskal-Wallis test showed no significant difference among them ( $\chi^2 = 2.6116, P = 0.4555$ ). Notably, decision tree had the highest standard deviation, which implies low stability, although it ranked the fourth highest of all (Table 8). In contrast, ensemble approaches (XGB, GBT and RF) mitigate decision trees' instability with lower variance and possibly lower bias as well to improve predictive ability [17, 34, 44]. Although the execution time is not measured in this study, XGB has been reported to run faster than GBT [26]. For neural networks, multilayer settings with nonlinear activation functions seem to provide the greatest potential in handling complex data structures prevalent in larger datasets. With limited data and moderate preprocessing, the performance of neural networks is reasonable and shows the most potential for improvement.

It is also noted that there is an apparent performance gap between the best-performing classifier and some weaker-performing algorithms including K-nearest neighbors, LDA, naïve Bayes, support vector machine and logistic regression. Although this is typical because these methods require more involved data preprocessing to handle spurious datasets, it is hard to pinpoint the specific causes for each of these poor-performing classifiers. Some potential explanations include that the algorithm (1) depends on data conversions from categorical to numerical types, which tends to introduce bias into the data; (2) is sensitive to the data magnitude and require data scaling (e.g. normalization) to operate efficiently; (3) is not robust in handling noisy datasets; (4) does not have strong predictive ability to handle complex problem (e.g. imbalanced data); and (5) lacks the stability required to handle small perturbations in the input data (see the work by Bousquet and Elisseeff [27]). Refer to a detailed study on classifier performance by Kotsiantis [29] for further reading.

Datatype conversion and data scaling tend to be an integral component to specific algorithms. An investigation into the effects of data scaling on the performance of KNN was performed. Table 9 illustrates that data scaling improves the performance of KNN, and similar results are suspected for the aforementioned supervised machine learning algorithms. For KNN on 1000\_Bank, standardization improves ACC by 5.47%, PRC by 45% and ROC by 13.26%; normalization improves RCL by 90.13% and F1 by 72.48%. It is noteworthy that tree-based methods are not affected by data scaling and conversion, which gives rise to more stable performance.

Scaling method	ACC	PRC	RCL	F1	ROC
Raw data	0.6952	0.4012	0.1522	0.2182	0.6262
Normalized	0.7300	0.5472	0.2891	0.3762	0.6667
Standardized	0.7333	0.5801	0.2057	0.3000	0.7095

Table 9. Scaling effects on KNN (1000\_Bank)

# 5.6 Model Interpretability

Machine learning models are often referred to as black boxes due to their limited interpretability. In employee turnover prediction, improving the machine learning model's interpretability is critical for the end-user to make data-driven decisions that are impactful. In an effort to make the machine learning models studied in this research easier to understand, two data mining techniques are introduced: feature importance ranking and classification rule extraction and visualization.

Feature Importance, also known as Relative Importance of Features, is used to determine the influence of specific features [17] in affecting employee turnover as a whole. This helps understand the correlations between features and employee turnover. The idea is closely related to feature selection, or equivalent in some cases. Taking the approach of feature selection, feature importance calculations may be categorized into three approaches (refer to the paper by Haq, Onik and Shah [12]): (1) filter methods evaluate the importance by statistical and probability methods such as MI and MIC [20], which does not rely on any classifiers; (2) wrapper approaches depend on classifiers to evaluate the feature importance, such as perturbing the values of individual features and measuring the effect on the classifier prediction accuracy [6]; and (3) embedded techniques get the feature importance while building the model—the feature importance is automatically generated as part of model building procedure. Most tree-based classifiers fall into this category; tree-based methods calculate feature importance using the total reduction of criterion brought on by the feature itself (see the work of Breiman [28]). For example, gradient boosting trees aggregated the weighted reduction in node purity, and calculate the feature importance by taking the weighted average. Figure 6 provides an example of feature importance ranking on 1000 Bank using XGB. The above approaches may also be combined, such as taking statistical tests on logistic regression coefficients [21].

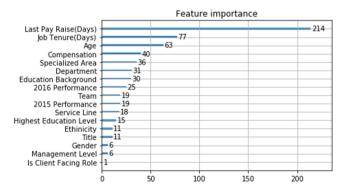


Fig. 6. Feature importance ranking generated by XGB on 1000\_Bank.

In existing employee turnover studies, the feature importance is often calculated with either wrapper or embedded approaches, resulting in classifier-dependent feature importance. For instance, the most prevalent classifier for importance ranking in the

works discussed above [1, 35] is decision tree. However, it is not the best classifier in all experiments, implying that the feature importance by decision tree could be less reliable compared with better performing classifiers. Taking 1000\_Bank dataset as an example, three most important features generated by ensemble methods (GBT, XGB, RF) are the same: last pay raise, job tenure and age. In comparison, decision tree gave different results: last pay raise, performance rating and job tenure, which appeared to be less dependable.

An empirical set of guidelines to achieve reliable feature importance is provided. First of all, feature importance should be calculated after identifying the best performing classifier. Ensemble tree-based method results are generally sound [34]. If the chosen classifier does not support embedded feature selection, the wrapper approach could be executed by observing classifier change by perturbing features included. Alternatively, probability or information theory methods like MIC could be used to get the feature importance without classifier dependency. Partial dependence analysis could also help understand the interactive effect of multiple features [34].

Classifier Rule Visualization and Extraction is a method to convert machine learning models into easy-to-understand, interpretable figures or sets of rules. Besides the feature

importance visualization shown in Fig. 6, classifier visualization provides a more direct way to present the prediction rule. Decision tree models support the creation of classifier visualizations rather naturally. Figure 4 shows a decision tree example on  $50\_Bank$  to generate sequences of logical if statements. As ensemble tree-based methods are hard to visualize [44], visualization on a single tree is picked as the compromise. However, instability of decision tree implies a small change in data could affect the tree split order significantly, resulting in a different tree structures and therefore different rules [34, 44]. As a result, decision tree visualization should be done cautiously; one should always confirm the model performance is decent first and utilize it for illustrative purpose only after. Alternatively, one can pick individual trees in XGB to visualize the decision process [39].

# 5.7 A Reliable Approach

Through the discussions noted above, some empirical guidelines are provided for approaching the employee turnover prediction problem. As noted, small HR datasets may contain high variance and randomness. This would suggest that more time should be spent on data quality assessments [17] and data augmentation in this case. For small datasets, the choice of classifiers should be selected using a heuristic approach.

For medium and large HR datasets, the data variance decreases and a more reliable model may be built. Best practice would be using tree-based ensemble methods such as extreme gradient boosting and gradient boosted trees. Extreme gradient boosting is preferred due to its superior predictive power and speed. This approach requires the least data preparation—it does not need data scaling and type conversions—and is likely to result in decent, if not the best, performance.

Lastly, to improve the model interpretability, feature ranking importance and classification rule visualization and extraction methods are recommended with caution for employee turnover prediction. Although feature importance ranking could be

straightforwardly acquired through tree-based models, a more robust approach is provided in this research (see Sect. 4).

# **6 Concluding Remarks**

Employee turnover has been identified as a pivotal factor to curb the growth of organizations. In this research, the performance of ten supervised machine learning methods was evaluated on various HR datasets. In addition to statistical analysis, a number of data mining techniques were introduced and used in this study, including data scaling, parameter searching and cross validation. To enhance the interpretability of employee turnover model, the examples of feature importance ranking and classifier visualization, and suggestions on how to use them appropriately, were also provided in Sect. 4.

The numerical experiment results indicate that for small HR datasets, the key is to try different algorithms as Hughes phenomenon may result in overoptimistic results. If there are more HR datasets available, extreme gradient boosting is recommended to use as the most reliable algorithm. It requires minimal data preprocessing, has decent predictive power, and ranks the feature importance automatically and reliably. However, due to the complexity of employee turnover prediction, one should try to find the classifier that best fits the underlying data before taking this approach.

# 6.1 Original Contribution

A reliable approach for employee turnover prediction using machine learning is provided in this research. The use of data sampling methods enables the evaluation of how organization size affects the effectiveness of supervised machine learning models. Additionally, a series of information theory and statistical measures are used to analyze the results. This approach is the first of its kind, to the authors' best knowledge, in employee turnover prediction. Existing works in this field usually focus on one dataset with a single evaluation approach, making the generalization of their findings rather limited.

#### 6.2 Recommendations for Future Research

Although data sampling is an efficient way to augment the data, it may still be non-representative of real-world. Further studies are necessary to determine if the conclusion holds. It is also recommended to extend this research to include more baseline models with a focus on feature engineering, i.e. using different data encoding and scaling methods.

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