

# Foundations of DL

Deep Learning



ALF



Alfredo Canziani, Ritchie Ng  
@alfcnz, @RitchieNg

# Convolutional Neural Nets

Exploiting stationarity, locality, and compositionality of natural data

# Signals can be represented as vectors



$$\mathbf{x} = [x_1 \ x_2 \ x_3 \ \dots \ x_t \ \dots]^\top$$

$x_t$  are waveform heights



$$\mathbf{x} = [x_{11} \ x_{12} \ \dots \ x_{1n} \ x_{21} \ x_{22} \ \dots]^\top$$

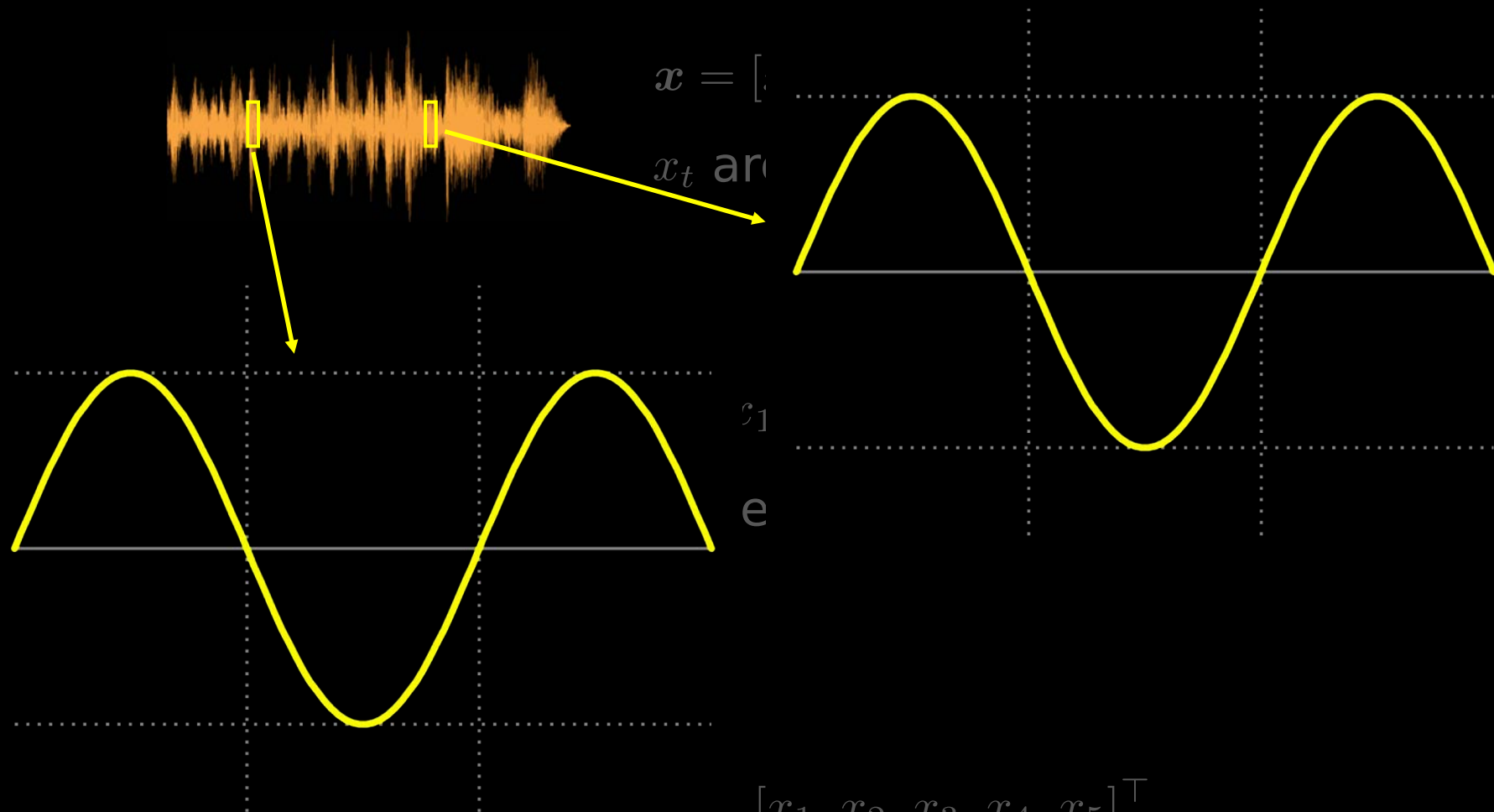
$x_{ij}$  are pixel values

“John picked up the apple”

$$\mathbf{x} = [x_1 \ x_2 \ x_3 \ x_4 \ x_5]^\top$$

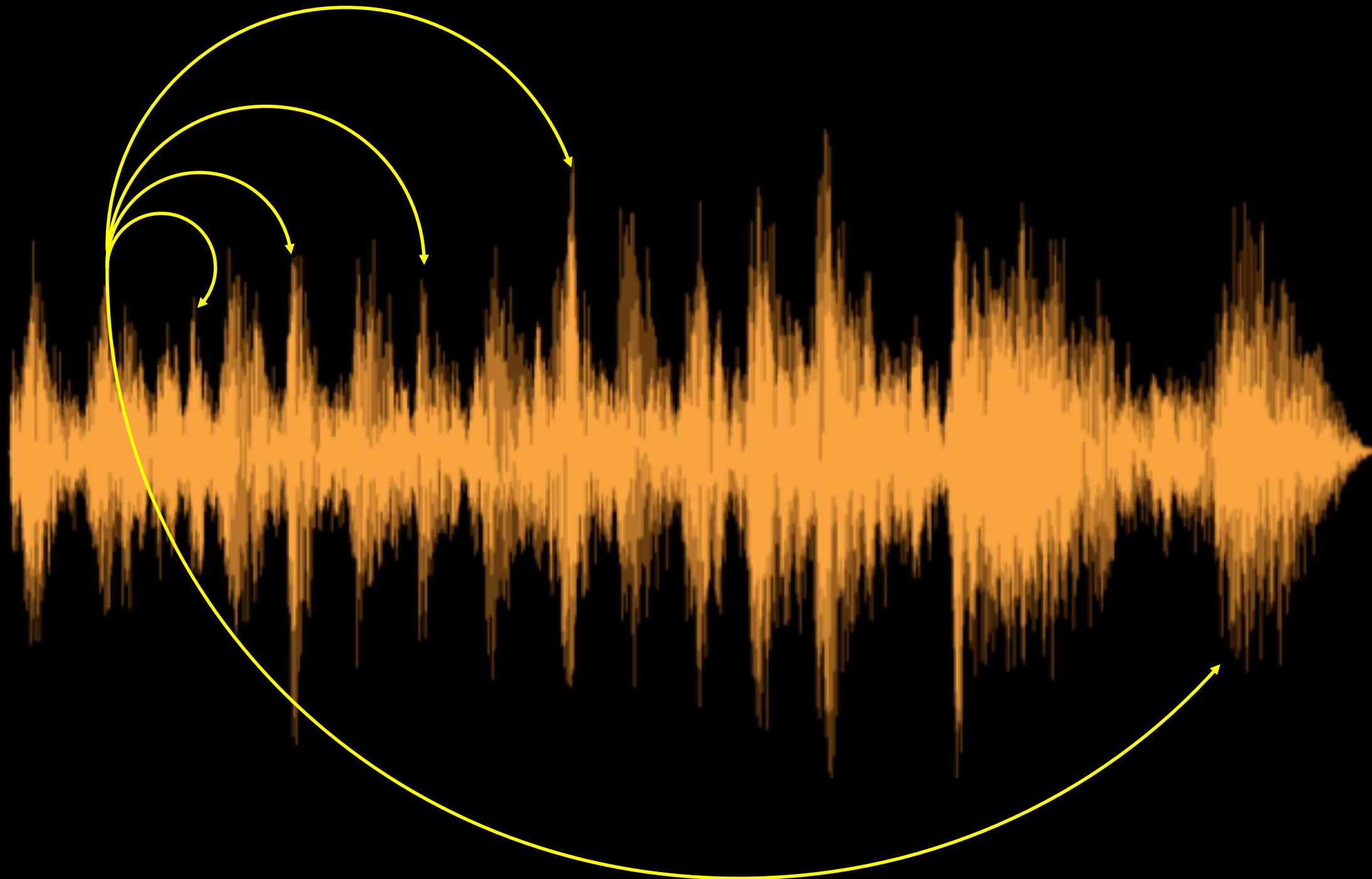
$x_t$  are one-hot vectors

# Signals can be represented as vectors



"John picked up the apple"

$x_t$  are one-hot vectors

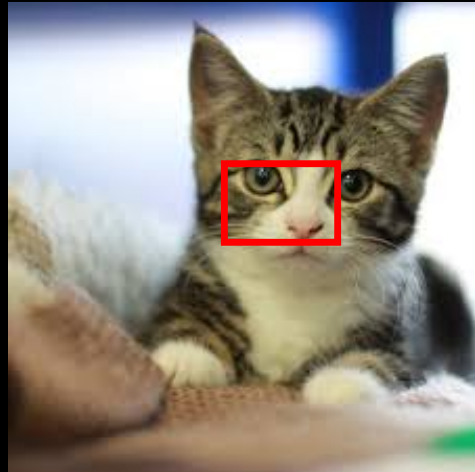


# Signals can be represented as vectors



$$\mathbf{x} = [x_1 \ x_2 \ x_3 \ \dots \ x_t \ \dots]^\top$$

$x_t$  are waveform heights



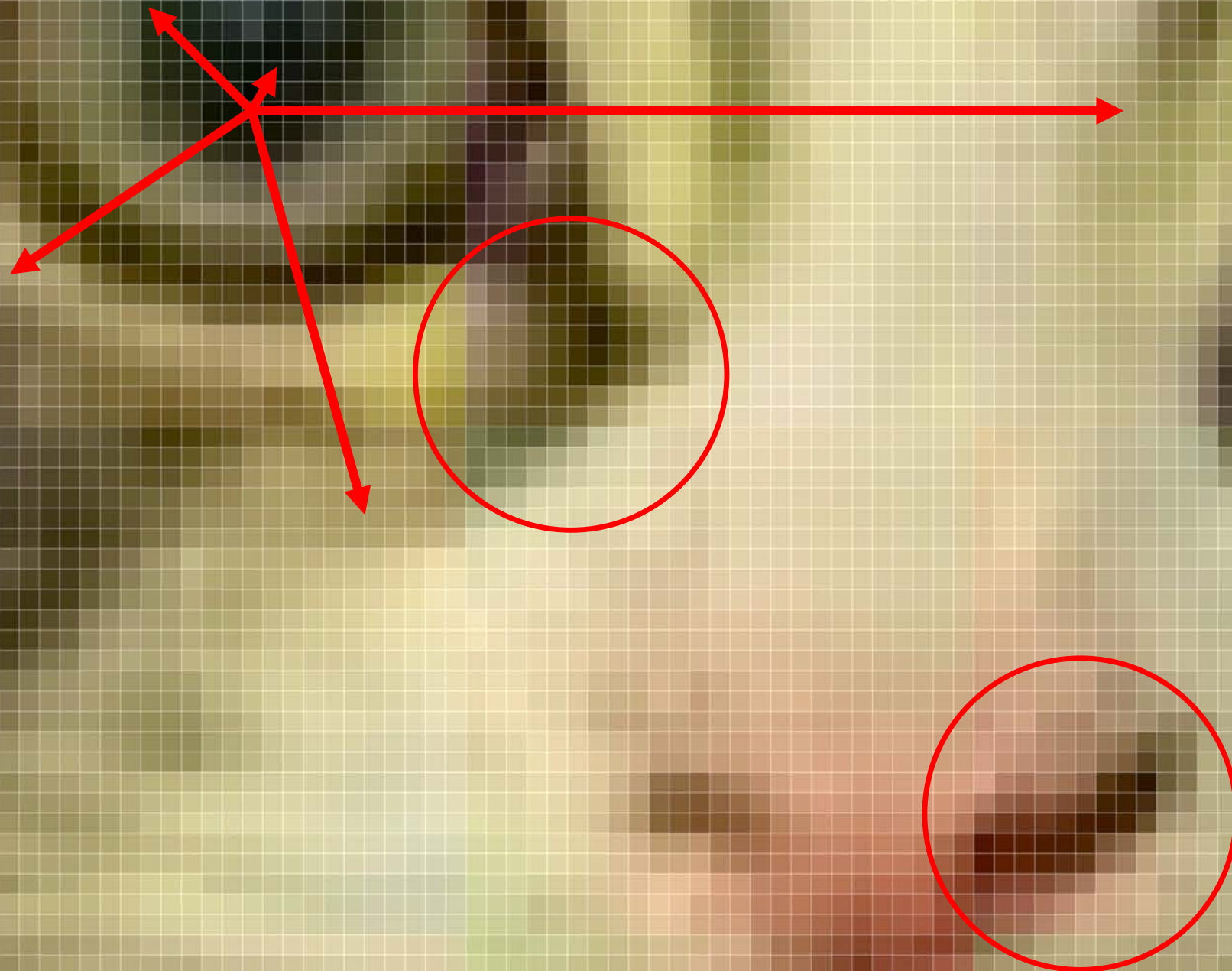
$$\mathbf{x} = [x_{11} \ x_{12} \ \dots \ x_{1n} \ x_{21} \ x_{22} \ \dots]^\top$$

$x_{ij}$  are pixel values

“John picked up the apple”

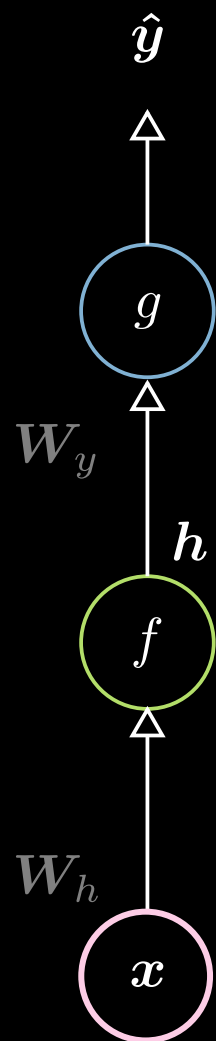
$$\mathbf{x} = [x_1 \ x_2 \ x_3 \ x_4 \ x_5]^\top$$

$x_t$  are one-hot vectors





# Fully connected (FC) layer



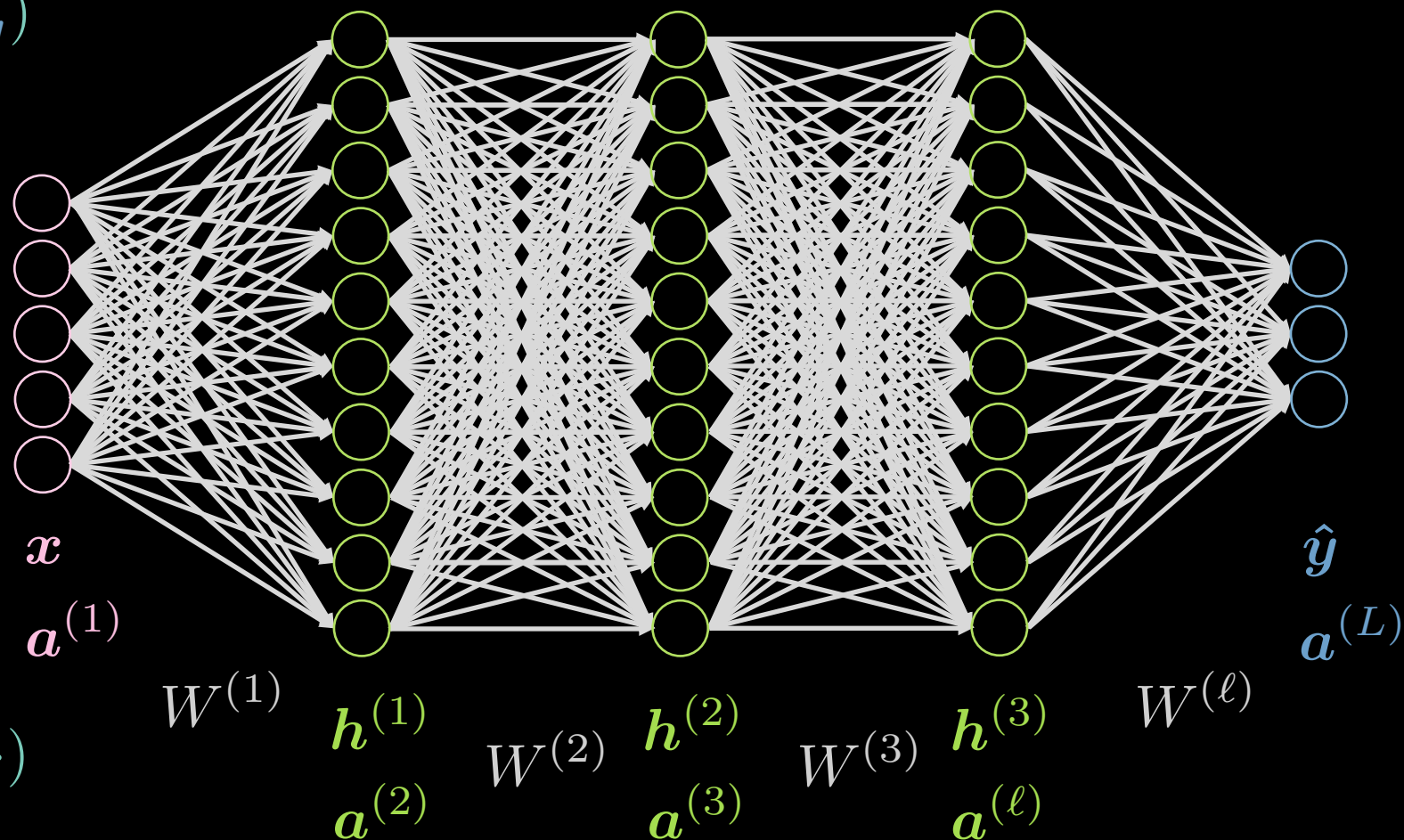
$$\mathbf{h} = f(\mathbf{W}_h \mathbf{x} + \mathbf{b}_h)$$

$$\hat{\mathbf{y}} = g(\mathbf{W}_y \mathbf{h} + \mathbf{b}_y)$$

$$f, g = (\cdot)^+, \sigma(\cdot), \tanh(\cdot), \text{softmax}(\cdot)$$

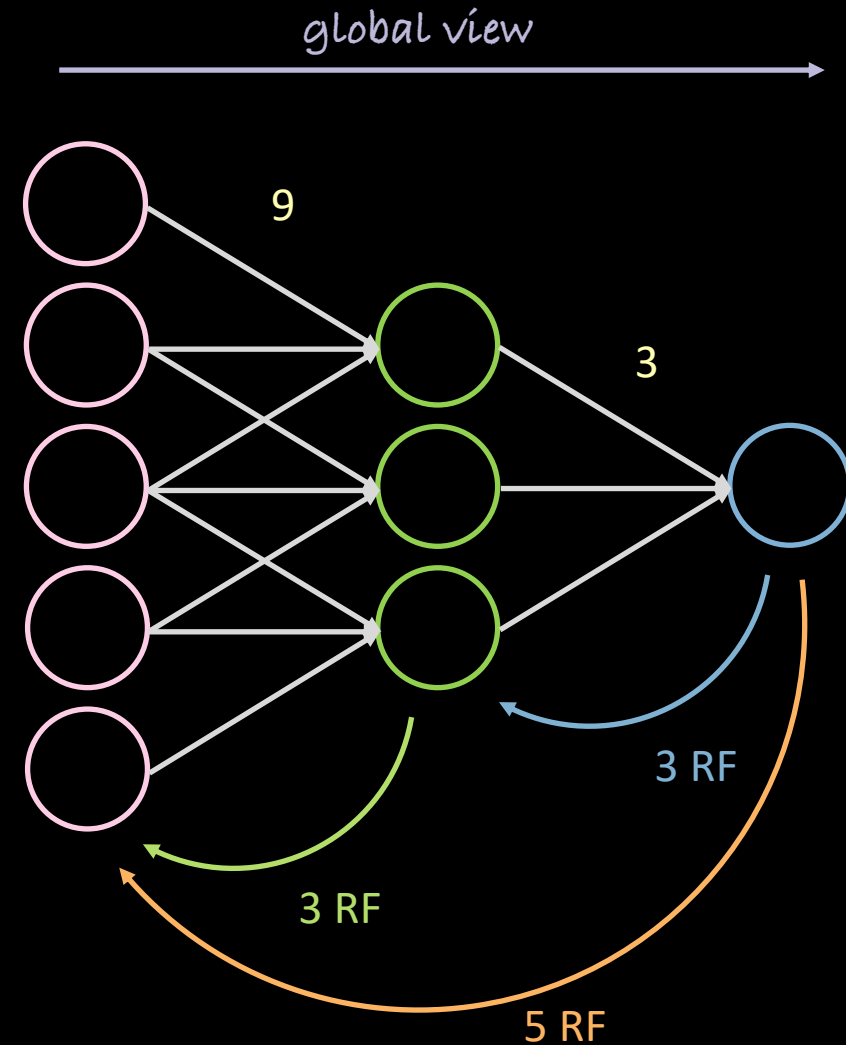
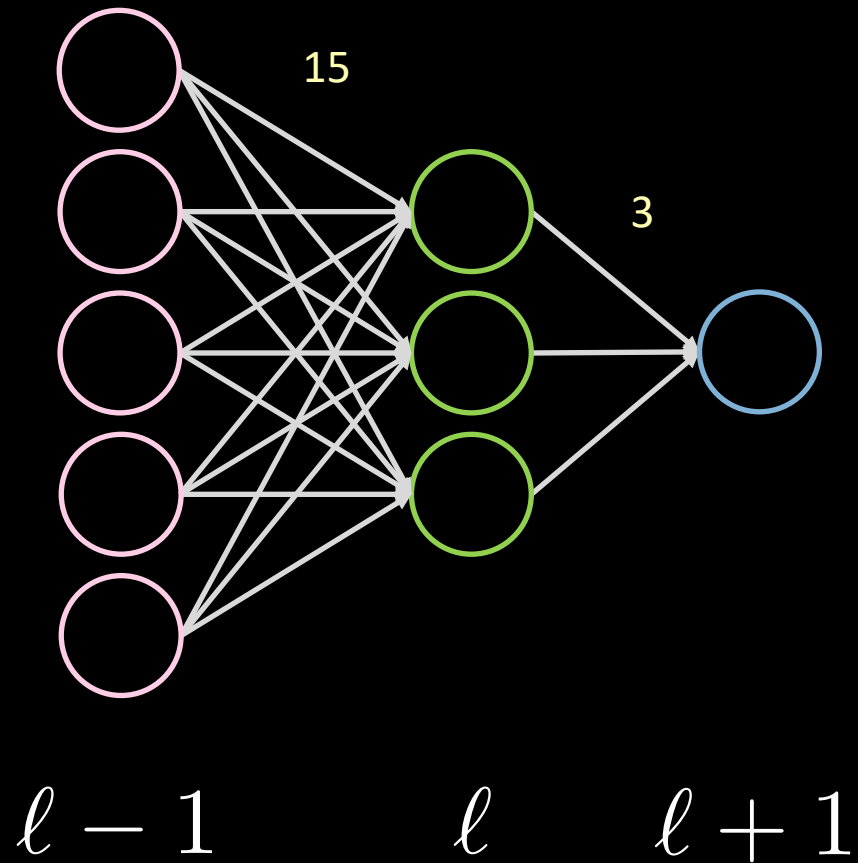
$j$ -th row of  $W^{(1)}$

$$a_j^{(2)} = f(\boxed{w^{(j)}} \mathbf{x} + b_j) = f\left(\left(\sum_{i=1}^n w_i^{(j)} x_i\right) + b_j\right)$$

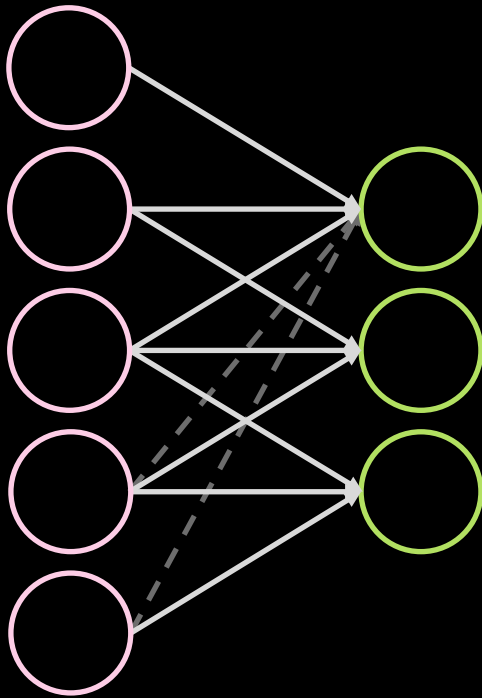




Locality  $\Rightarrow$  sparsity



# Stationarity $\Rightarrow$ parameters sharing

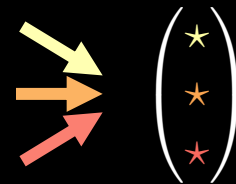
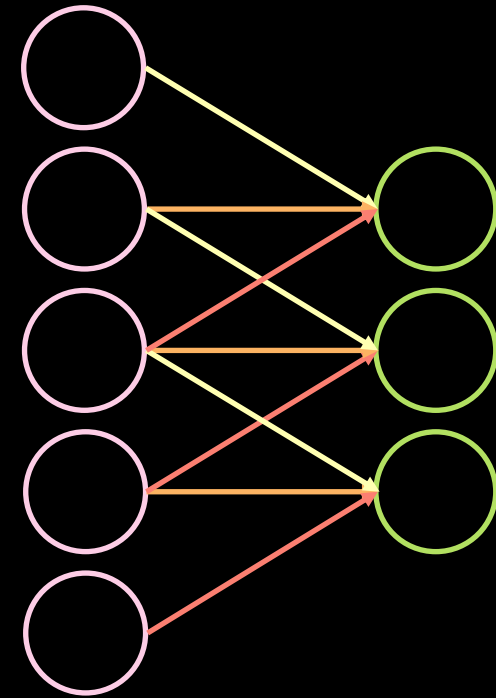


## Parameters sharing

- faster convergence
- better generalisation
- not constrained to input size
- kernel independence  
 $\Rightarrow$  high parallelisation

## Connection sparsity

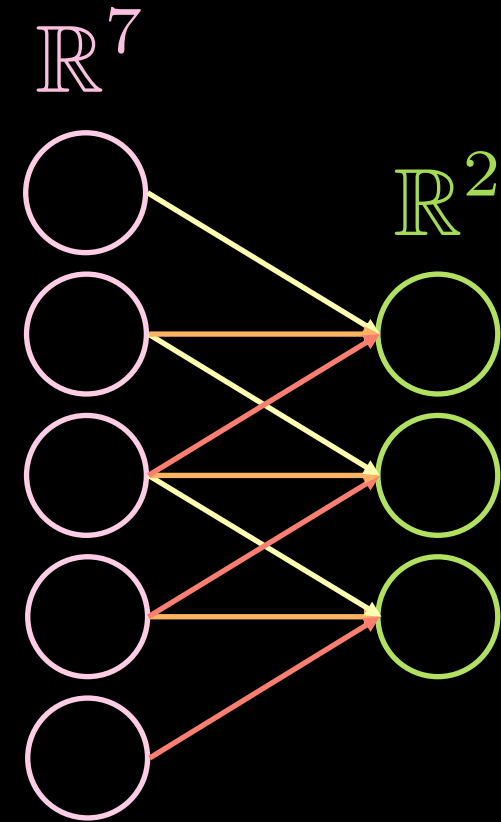
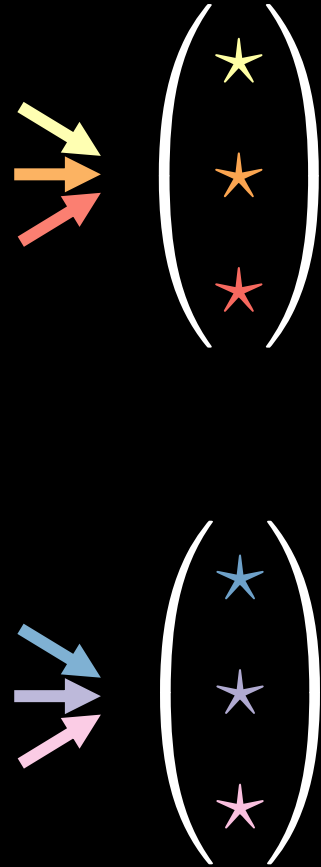
- reduced amount of computation



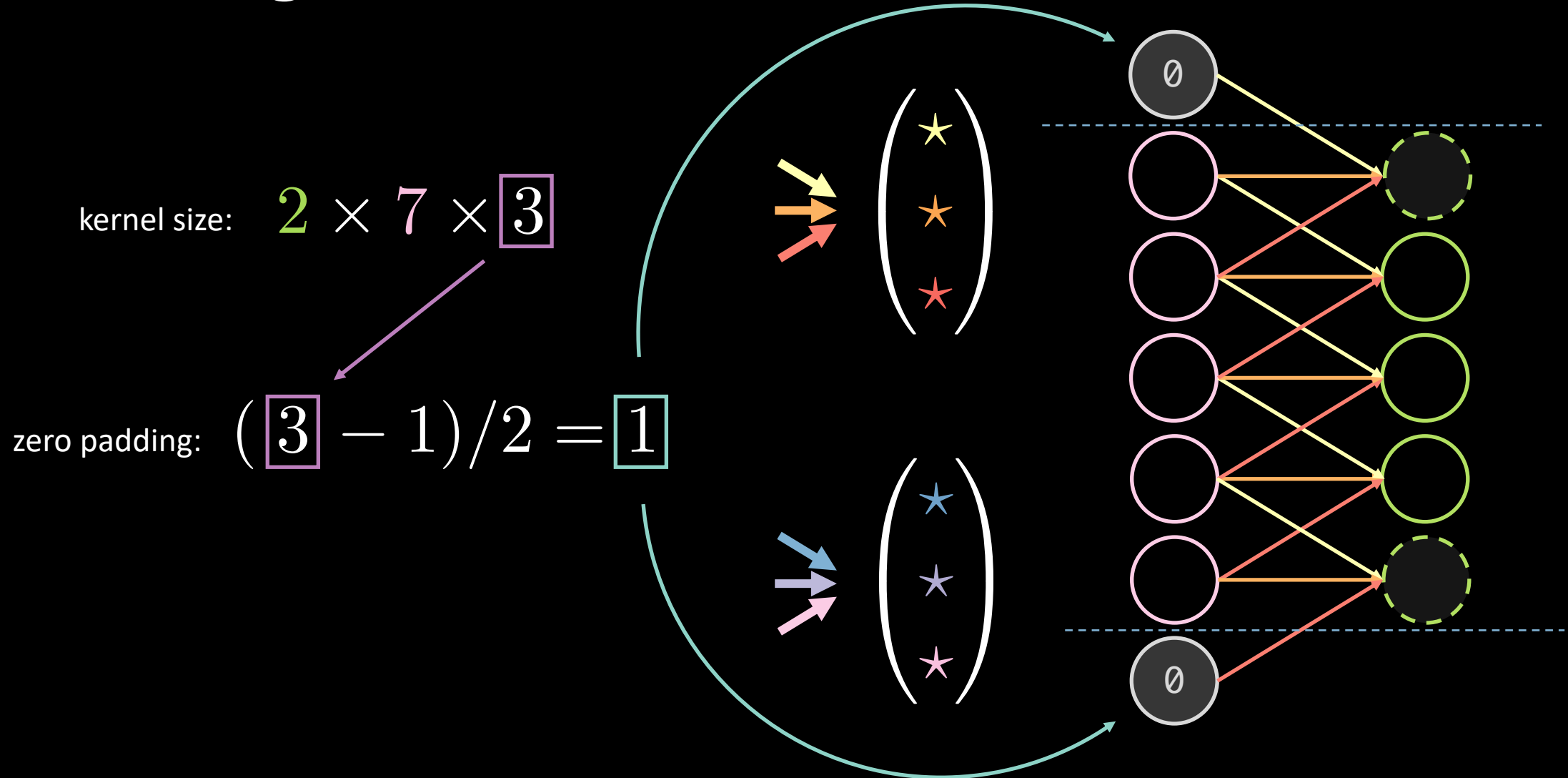
# Kernels – 1D data

kernel size:  $2 \times 7 \times 3$

1D data uses 3D kernels!

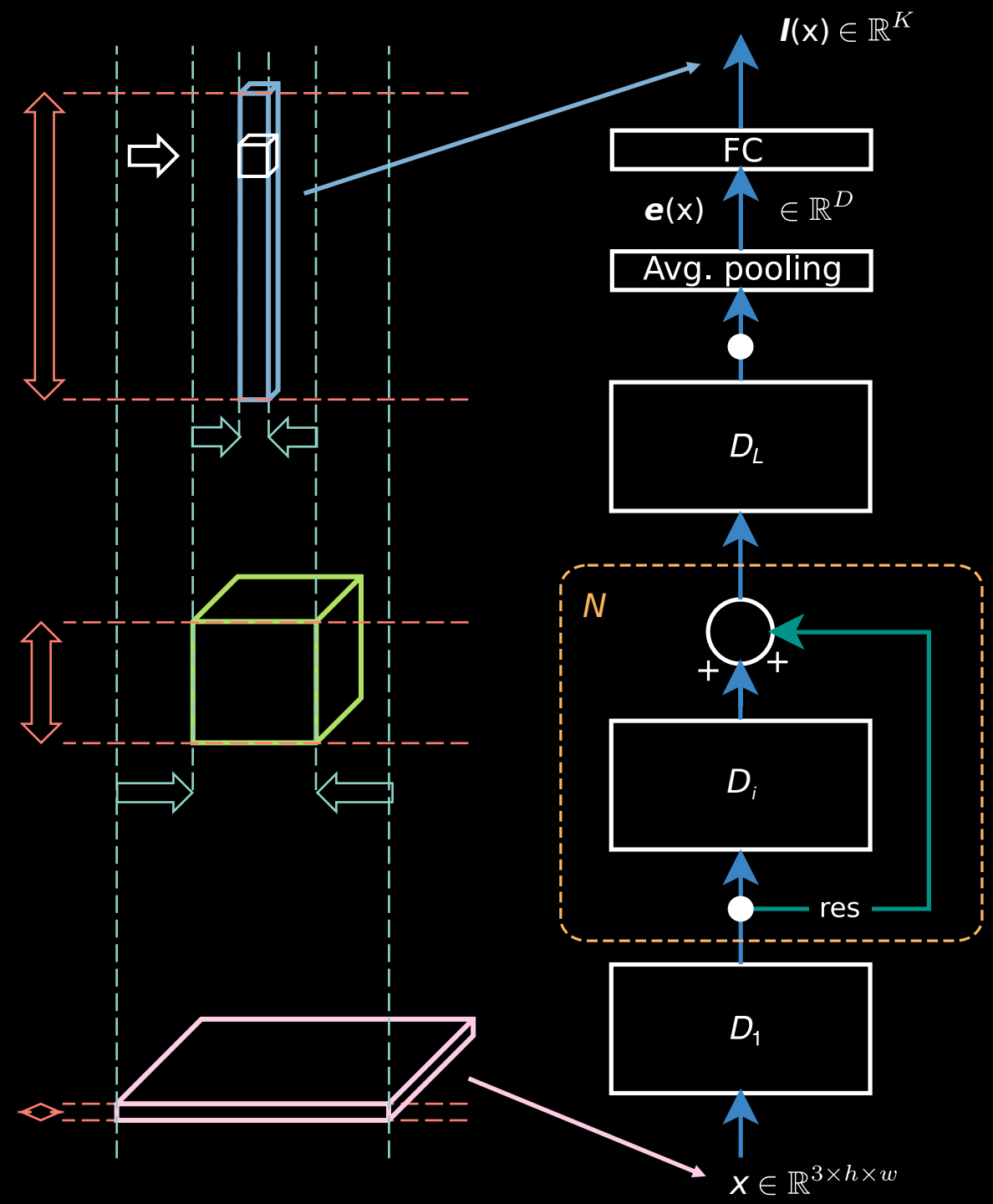


# Padding – 1D data



# Standard spatial CNN

- Multiple layers
  - Convolution
  - Non-linearity
  - Pooling
  - Batch normalisation
- Residual bypass connection



# Pooling

$$\|x\|_p := \left( \sum_i |x_i|^p \right)^{1/p}$$

$$\|x\|_p \rightarrow \max(x), p \rightarrow +\infty$$

