Machine Learning

in 2018… Deep Learning!

ALF

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Convolutional Neural Nets

Exploiting stationarity, locality, and compositionality of natural data

Signals can be represented as vectors

$$\boldsymbol{x} = [x_1 \;\; x_2 \;\; x_3 \;\; \ldots \;\; x_t \;\; \ldots]^\top$$

x_t are waveform heights

$$\boldsymbol{x} = [x_{11} \;\; x_{12} \;\; \ldots \;\; x_{1n} \;\; x_{21} \;\; x_{22} \;\; \ldots]^\top$$

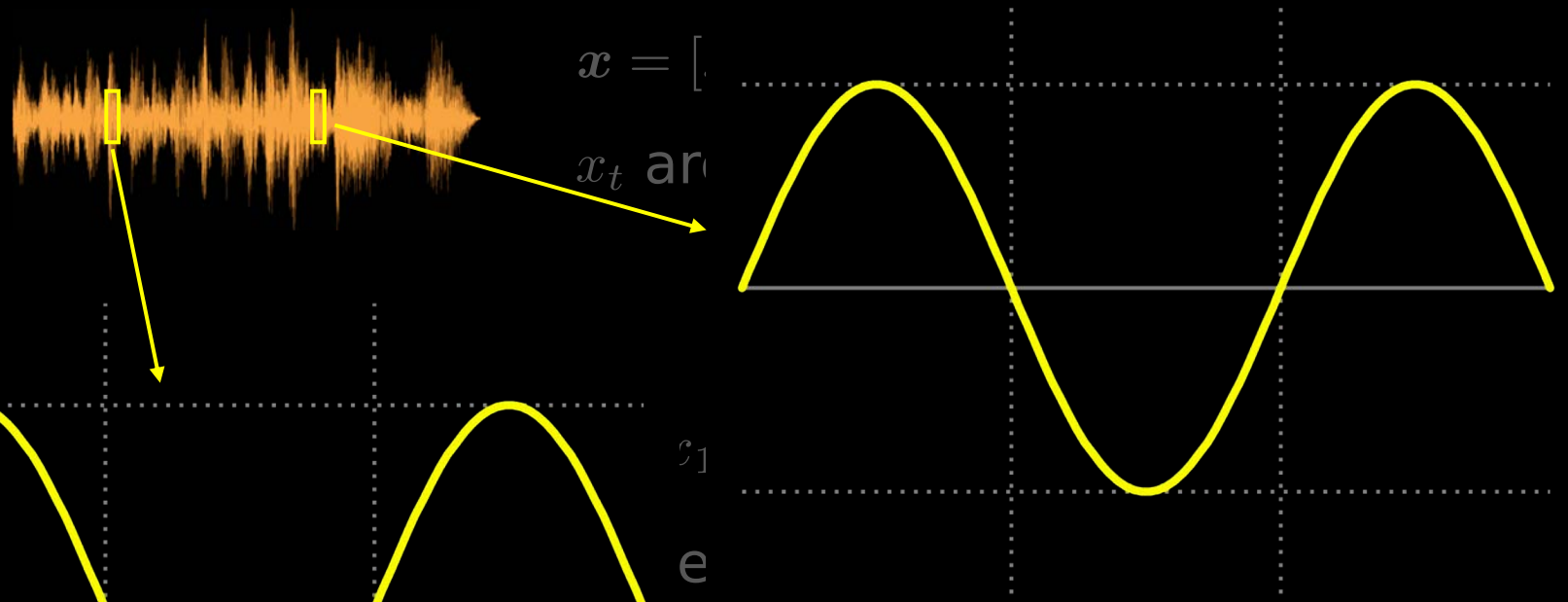
x_{ij} are pixel values

"John picked up the apple"

$$\boldsymbol{x} = [x_1 \;\; x_2 \;\; x_3 \;\; x_4 \;\; x_5]^\top$$

x_t are one-hot vectors

Signals can be represented as vectors



$\boldsymbol{x} = [$

x_t ar

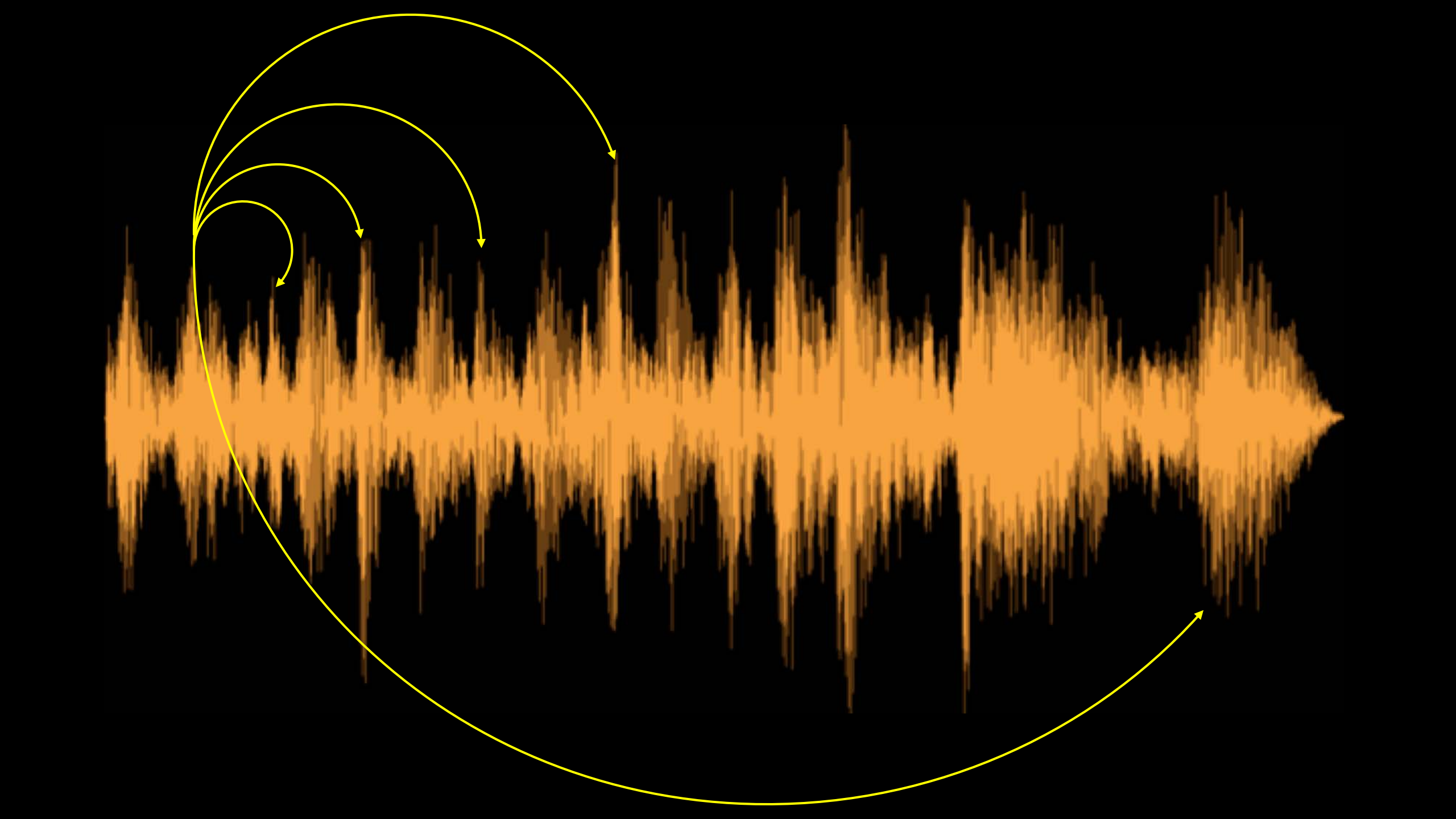
x_1

e

"John picked up the apple"

$[x_1 \;\; x_2 \;\; x_3 \;\; x_4 \;\; x_5]^\top$

x_t are one-hot vectors



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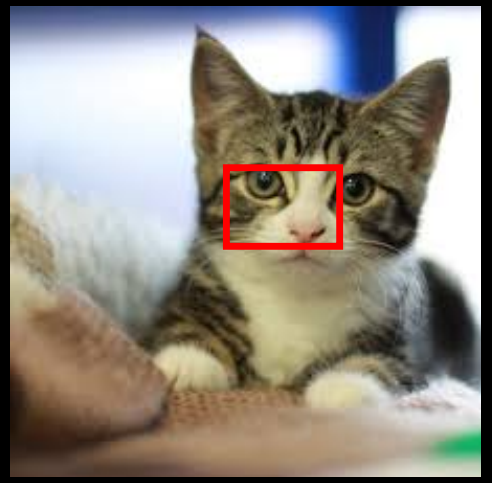

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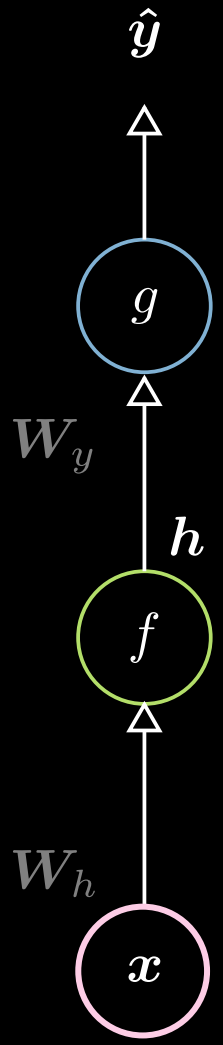
Fully connected (FC) layer

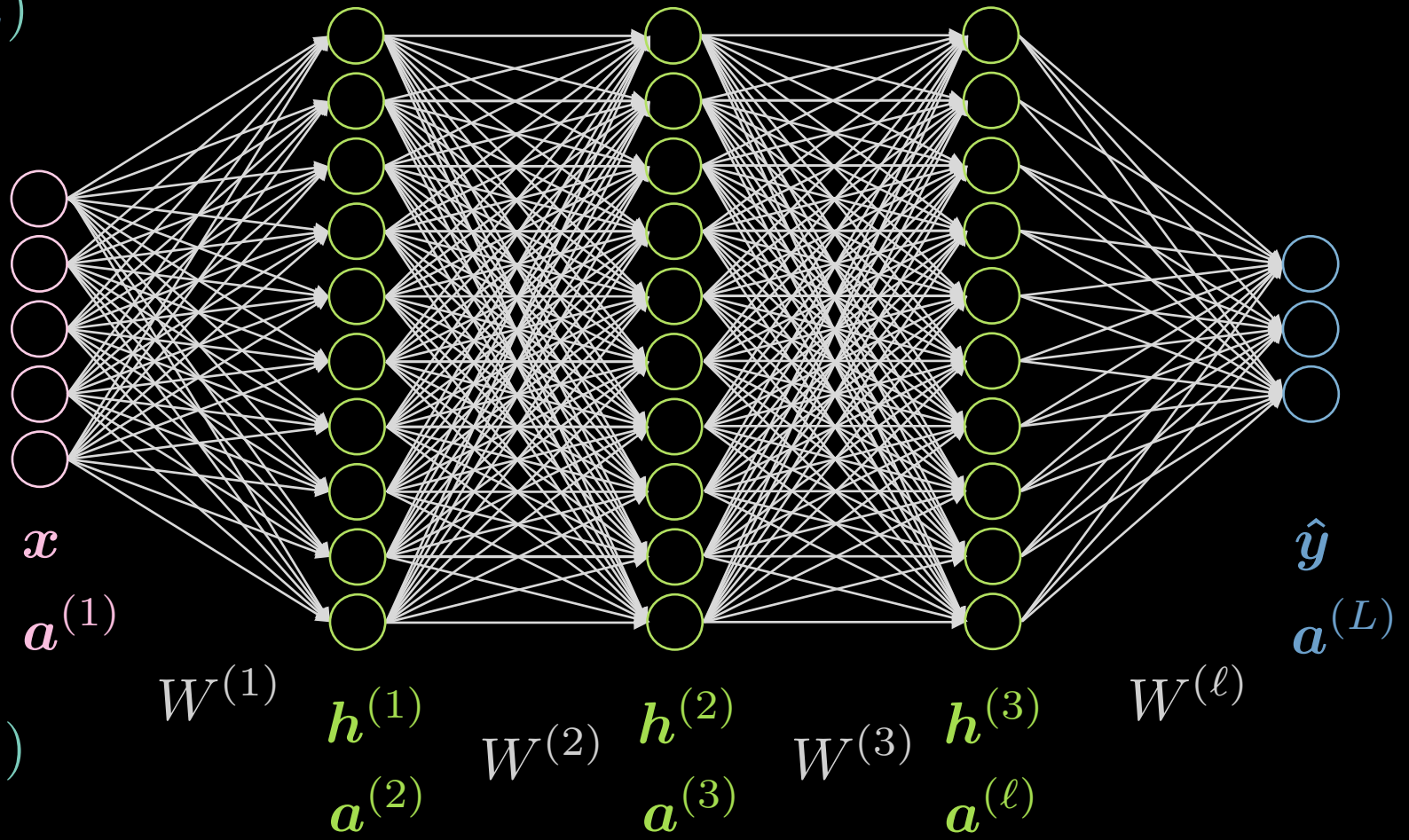
j-th row of $W^{(1)}$

$$a_j^{(2)} = f(\boldsymbol{w}^{(j)}\boldsymbol{x} + b_1) = f\left(\left(\sum_{i=1}^{n} w_i^{(j)} x_i\right) + b_1\right)$$

$$\boldsymbol{h} = f(\boldsymbol{W_h}\boldsymbol{x} + \boldsymbol{b_h})$$

$$\hat{\boldsymbol{y}} = g(\boldsymbol{W_y}\boldsymbol{h} + \boldsymbol{b_y})$$

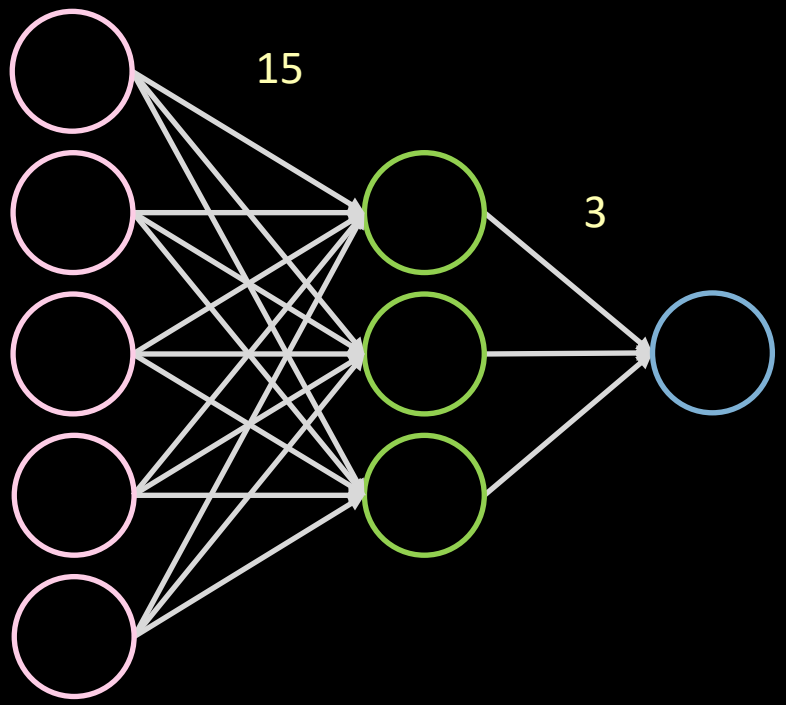


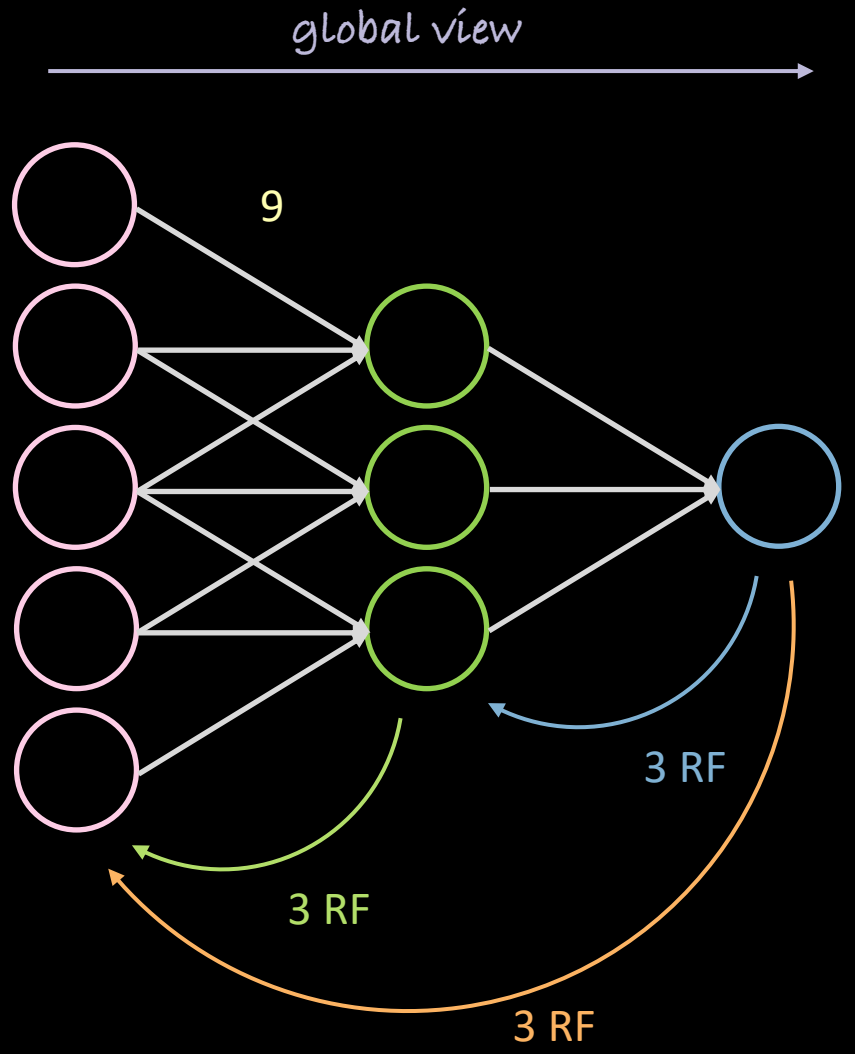


$f, g = (\cdot)^+, \sigma(\cdot),$
$\tanh(\cdot), \mathrm{softmax}(\cdot)$

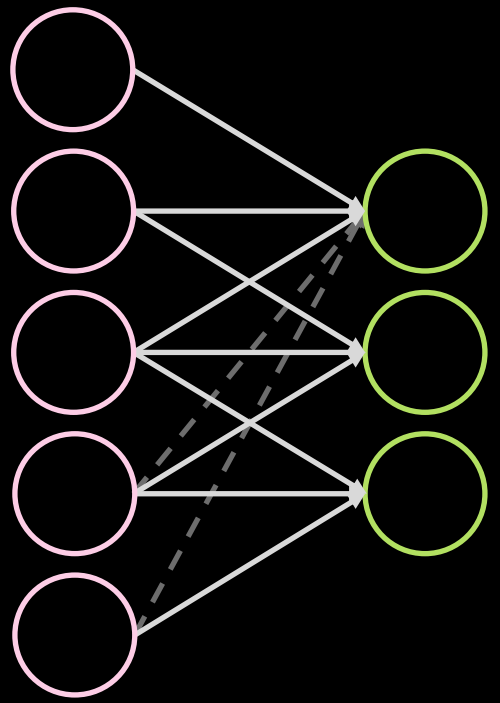
RF: receptive field

Locality ⇒ sparsity





Stationarity ⇒ parameters sharing

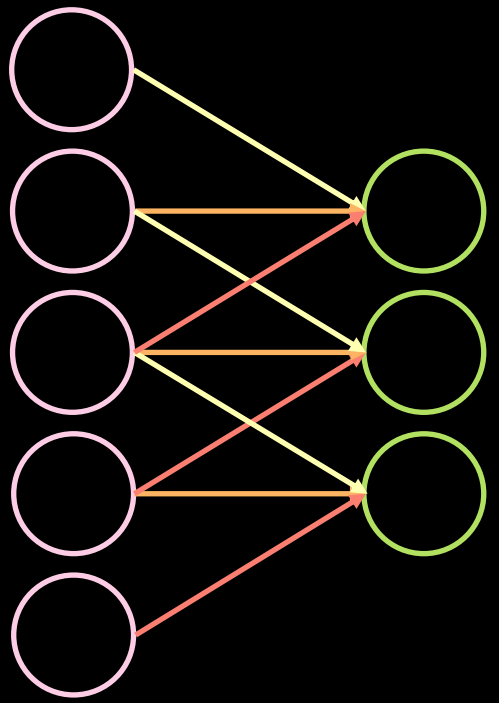


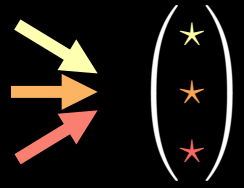
Parameters sharing

- faster convergence
- better generalisation
- not constrained to input size
- kernel independence
  ⇒ high parallelisation

Connection sparsity

- reduced amount of computation

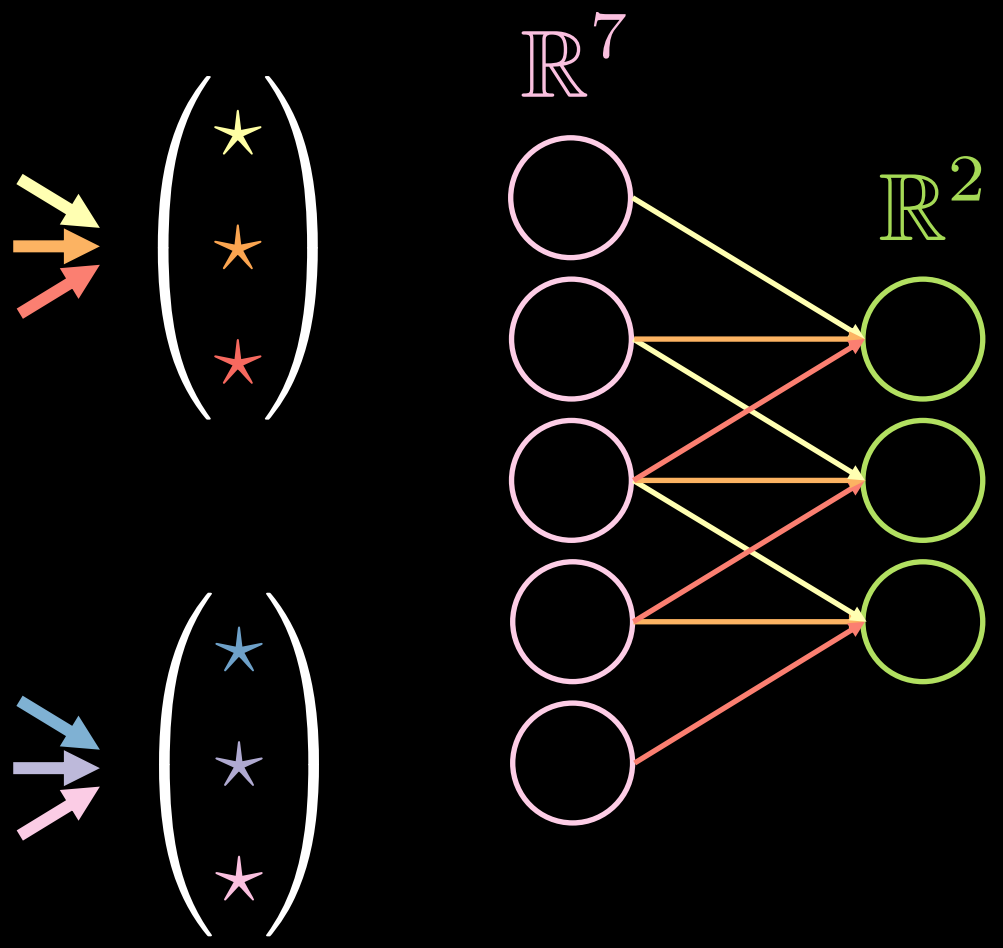




Kernels – 1D data

kernel size: $2 \times 7 \times 3$

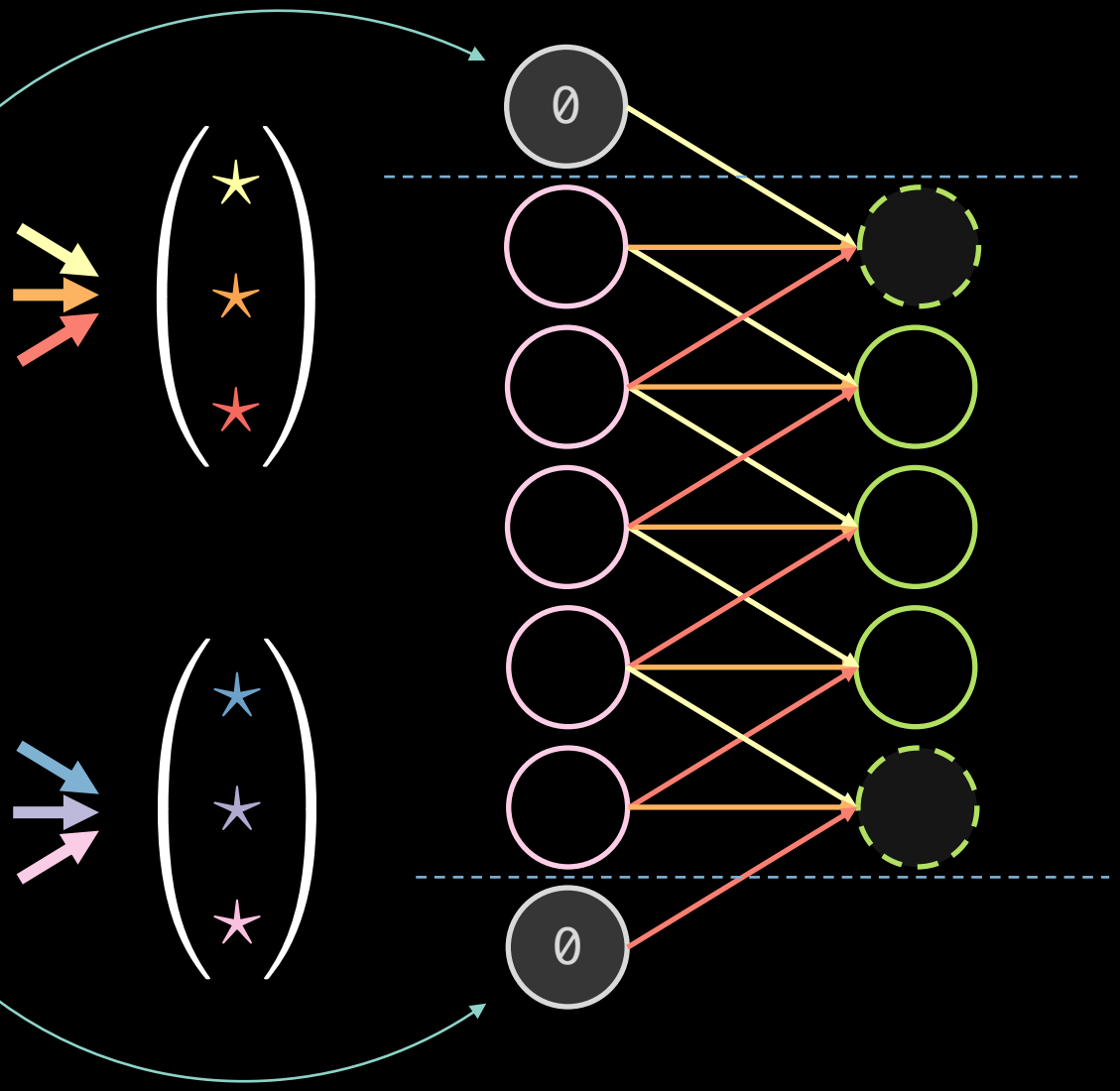
1D data uses 3D kernels!



Padding – 1D data

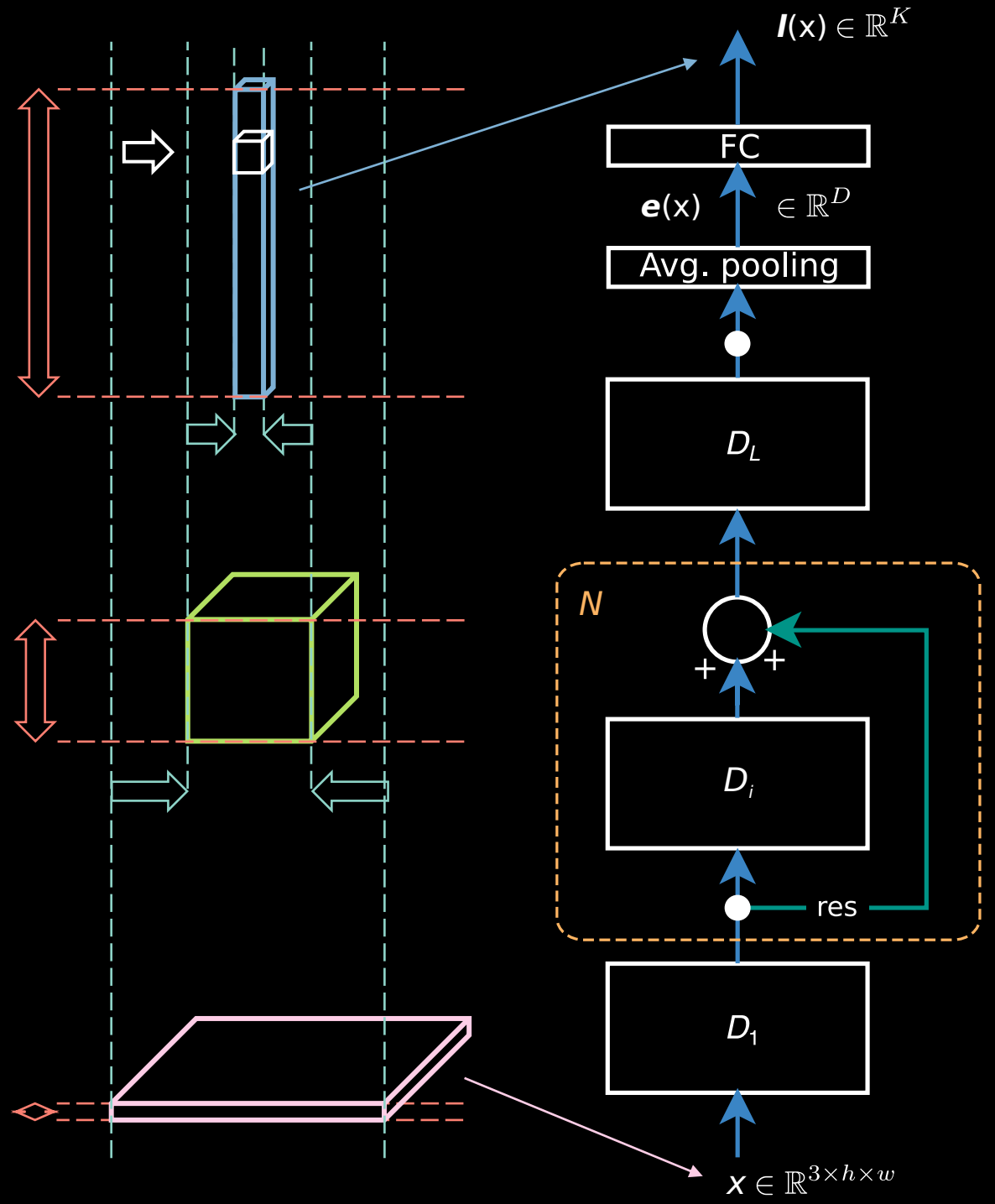
kernel size: $2 \times 7 \times \boxed{3}$

zero padding: $(\boxed{3} - 1)/2 = \boxed{1}$



Standard spatial CNN

- Multiple layers
  - Convolution
  - Non-linearity
  - Pooling
  - Batch normalisation
- Residual bypass connection



Pooling

$$\|\underline{x}\|_p := \left(\sum_i |x_i|^p \right)^{1/p}$$

$$\|\underline{x}\|_p \to \max(\underline{x}), \; p \to +\infty$$