

Method Description

General Information

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Team Members (*if applicable*):

1 st Member	
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Information about the method utilized

Name of Method	Bunch linear extrapolation
Type of Method (<i>Statistical, Machine Learning, Combination, Other</i>)	Other
Short Description (up to 200 words)	Bunch linear extrapolation generates a set of lines. Each line passes through the two points of time series: (t_i, y_i) and (t_n, y_n) , where (t_n, y_n) is the last point of time series, and (t_i, y_i) is the i -th point, $i = 1, 2, \dots, n-1$. So, as a result we have $n-1$ lines, all passing through the last n -th point. Then, we determine the median line for these $n-1$ lines. The forecasts for the next h points are the median for $(n+1, n+2, \dots, n+h)$. Having the median line we calculate 95% prediction interval using standard approach for a linear model.

Extended Description:

For yearly, monthly, weekly and daily time series the model is constructed as follows:

1. If the number of points in the time series $n > 10 \cdot h$ (h is a forecast horizon) then remove first points from 1 to $n - 10 \cdot h$. So, the time series is shorten to $10 \cdot h$ last points.
2. Create $n - 1$ lines passing through the two points of time series: (t_i, y_i) and (t_n, y_n) , where (t_n, y_n) is the last point of the time series, and (t_i, y_i) is the i -th point, $i = 1, 2, \dots, n - 1$. So, as a result we have $n - 1$ lines, all passing through the last n -th point.
3. Determine the median line for a bunch of $n - 1$ lines created in step 2. Each point of the median line is calculated as a median of corresponding points from $n - 1$ lines.
4. Determine the forecasts for the next h points as the median for $(n + 1, n + 2, \dots, n + h)$.
5. Calculate 95% prediction interval using standard approach for a linear model:

$$\hat{y} \pm t_{(1-\alpha/2, n-2)} s_y \sqrt{1 + \frac{1}{n} + \frac{(t^* - \bar{t})^2}{(n-1)s_t^2}}$$

For quartely and hourly time series expressing seasonal patterns the seasonal version of the model is used. In this case the quartely time series is decomposed on four time series:

- 1) $\{y_t\}$, $t = 1, 5, 9, \dots$,
- 2) $\{y_t\}$, $t = 2, 6, 10, \dots$,
- 3) $\{y_t\}$, $t = 3, 7, 11, \dots$,
- 4) $\{y_t\}$, $t = 4, 8, 12, \dots$

Similarly the hourly time series is decomposed into 24 time series:

- 1) $\{y_t\}$, $t = 1, 25, 49, \dots$,
- 2) $\{y_t\}$, $t = 2, 26, 50, \dots$,
- ...
- 24) $\{y_t\}$, $t = 24, 48, 72, \dots$

Each of these new time series is forecasted independently.

The model is constructed as follows:

1. If the number of points in the time series $n > 10 \cdot h$ (h is a forecast horizon) then remove first points from 1 to $n - 10 \cdot h$. So, the time series is shorten to $10 \cdot h$ last points.
2. Decompose the time series into 4 or 24 time series (see above).
3. For each decomposed time series having n^* points create $n^* - 1$ lines passing through the two points of time series: (t_i, y_i) and (t_{n^*}, y_{n^*}) , where (t_{n^*}, y_{n^*}) is the last point of time series, and (t_i, y_i) is the i -th point, $i = 1, 2, \dots, n^* - 1$. So, as a result we have $n^* - 1$ lines, all passing through the last n^* -th point.
4. For each decomposed time series determine the median line for a bunch of $n^* - 1$ lines created in step 2. Each point of the median line is calculated as a median of the corresponding points from $n^* - 1$ lines.

5. For each decomposed time series determine the forecasts for the next h^* points as the median for $(n^*+1, n^*+2, \dots, n^*+h^*)$, where in our case $h^* = 2$.
6. For each decomposed time series calculate 95% prediction interval using standard approach for a linear model:

$$\hat{y} \pm t_{(1-\alpha/2, n-2)} s_y \sqrt{1 + \frac{1}{n^*} + \frac{(t^* - \bar{t})^2}{(n^* - 1)s_t^2}}$$

BLE model features:

- no parameters
- no assumptions
- no initialization
- no training
- no complex calculations
- clear and understandable model
- simple implementation in any environment
- fast execution
- seasonal approach needs time series decomposition

Source and output files

The BLE models are implemented in Matlab:

- BLE_for_YeMoWeDa.m - model for yearly, monthly, weekly and daily time series,
- BLE_for_QuHo.m - model for seasonal quartely and hourly time series.

The input data are provided in the files:

- Yearly-train1.csv
- Quarterly-train1.csv
- Monthly-train1.csv
- Weekly-train1.csv
- Daily-train1.csv
- Hourly-train1.csv

which are the same as original data files but without quotation marks around numerical values.

To execute the m-file select the input file in the source code. Results are saved in output files (variable 'file'):

- Yerly_wyn.mat
- Quart_wyn.mat
- Month_wyn.mat
- Week_wyn.mat
- Dail_wyn.mat
- Hourl_wyn.mat

Each file include: time series label, forecasts (ypro), lower (y025) and upper (y975) bounds of prediction intervals.

Remark: the scripts for running need Statistics and Machine Learning Toolbox to be installed. It is needed for prediction intervals calculation where `tinvcdf` function is used (Student's t inverse cumulative distribution function) which is from Statistics and Machine Learning Toolbox.