Verifiable C

Applying the Verified Software Toolchain to C programs

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with Josiah Dodds

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1 Getting started

This *summary reference manual* is a brief guide to the VST Separation Logic for the C language. The Verified Software Toolchain and the principles of its program logics are described in the book:

Program Logics for Certified Compilers, by Andrew W. Appel *et al.*, Cambridge University Press, 2014.

TO INSTALL THE VST SEPARATION LOGIC FOR C LIGHT:

- 1. Get VST from vst.cs.princeton.edu/download, or get the bleeding-edge version from the Subversion repository, https://svn.princeton.edu/appel/vst.
- 2. Examine vst/compcert/VERSION to determine which version of CompCert to download. The VST comes with a copy of the CompCert front-end, in vst/compcert/, but (at present) CompCert's clightgen utility is not buildable from just the front-end distributed with VST. You'll need clightgen to translate .c files into .v files containing C light abstract syntax. Thus it's recommended to download and build CompCert.¹
- 3. Get CompCert from compcert.inria.fr/download.html and run ./configure to list configurations. Select the correct option for your machine, then run ./configure <option> followed by make clightgen. Create a file vst/CONFIGURE containing a definition for CompCert's location; if vst and CompCert are installed in the same parent directly, use COMPCERT=../compcert

If you have not installed CompCert, use the CompCert front-end packaged with VST. Do not create a CONFIGURE file, and do: cd vst/compcert; ./make

4. In the vst directory, make.

See also the file vst/BUILD_ORGANIZATION.

 $^{^1\}mathrm{Microsoft}$ Windows / Cygwin users: See Chapter 35 of this manual.

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Within vst, the progs directory contains some sample C programs with their verifications. The workflow is:

- Write a C program *F*.c.
- Run clightgen F.c to translate it into a Coq file F.v.
- Write a verification of *F*.v in a file such as verif_*F*.v. That latter file will import both *F*.v and the VST *Floyd*² program verification system, floyd.proofauto.

LOAD PATHS. Interactive development environments (CoqIDE or Proof General) will need their load paths properly initialized through command-line arguments. Running make in vst creates a file .loadpath with the right arguments. You can then do (for example), coqide `cat .loadpath` progs/verif_reverse.v

The verif_reverse.v example is described in PLCC Chapter 27. You might find it interesting to open this in the IDE, using the command shown above, and interactively step through the definitions and proofs.

Before doing proofs of your own, you may find it helpful to step through this tutorial on C light expressions and assertions: cd examples/floyd_tut; coqide tutorial.v (this tutorial sets up its own load paths.)

²Named after Robert W. Floyd (1936–2001), a pioneer in program verification.

2 Differences from PLCC

The book *Program Logics for Certified Compilers* (Cambridge University Press, early 2014) describes *Verifiable C* version 1.1. More recent VST versions differ in the following ways from what the PLCC book describes:

- field_mapsto is now called field_at, and its last two arguments are swapped.
- typed_mapsto is renamed to data_at, and last two arguments are swapped.
- umapsto ("untyped mapsto") no longer exists.
- mapsto π t v w now permits either (w =Vundef) or the value w belongs to type t. This permits describing uninitialized locations, i.e., mapsto_ π t v = mapsto_ π t v Vundef. See Chapter 31 of this manual.
- Supercanonical form is now suggested; see Chapter 18 of this manual.

3 Memory predicates

The axiomatic semantics (Hoare Logic of Separation) treats memories abstractly. One never has a variable m of type memory. Instead, one uses the Hoare Logic to manipulate predicates P on memories. Our type of "memory predicates" is called mpred

Although intuitively mpred "feels like" the type memory \rightarrow Prop, the underlying semantic model is different; thus we keep the type mpred abstract (opaque). See *Program Logics for Certified Compilers (PLCC)* for more explanation.

On the type mpred we form a natural deduction system NatDed(mpred) with conjuction &&, disjunction \parallel , etc.; a separation logic SepLog(mpred) with separating conjunction * and emp; and an indirection theory Indir(mpred) with \triangleright "later."

The natural deduction system has a sequent (entailment) operator written $P \mid -- Q$ in Coq (written $P \vdash Q$ in print), where P,Q: mpred. We write bientailment simply as P = Q since we assume axioms of extensionality.

4 Separation Logic

```
Class NatDed (A: Type) := mkNatDed {
   and p: A \rightarrow A \rightarrow A; (Notation &&)
   orp: A \rightarrow A \rightarrow A; (Notation ||)
   exp: \forall \{T:Type\}, (T \rightarrow A) \rightarrow A;
                                                            (Notation EX)
   allp: \forall \{T:Type\}, (T \rightarrow A) \rightarrow A; (Notation ALL)
   imp: A \rightarrow A \rightarrow A; (Notation -->, here written \longrightarrow)
   prop: Prop →A;
                                    (Notation!!)
   derives: A \rightarrow A \rightarrow Prop; (Notation |--, here written \vdash)
   pred_ext: \forall P Q, P \vdash Q \rightarrow Q \vdash P \rightarrow P = Q;
   derives_refl: \forall P, P \vdash P;
   derives_trans: \forall \{P \ Q \ R\}, P \vdash Q \rightarrow Q \vdash R \rightarrow P \vdash R:
   TT := !!True;
   FF := !!False;
   and p_right: \forall X P Q:A, X \vdash P \rightarrow X \vdash Q \rightarrow X \vdash (P\&\&Q);
   andp_left1: \forall P Q R:A, P \vdash R \rightarrow P\&\&Q \vdash R;
   andp_left2: \forall P Q R:A, Q \vdash R \rightarrow P\&\&Q \vdash R;
   orp_left: \forall P Q R, P \vdash R \rightarrow Q \vdash R \rightarrow P || Q \vdash R;
   orp_right1: \forall P Q R, P \vdash Q \rightarrow P \vdash Q || R;
   orp_right2: \forall P Q R, P \vdash R \rightarrow P \vdash Q || R;
   exp_right: \forall \{B: Type\}(x:B)(P:A)(Q: B \rightarrow A), P \vdash Q \times \rightarrow P \vdash EX \times B, Q;
   exp_left: \forall \{B: Type\}(P:B \rightarrow A)(Q:A), (\forall x, Px \vdash Q) \rightarrow EX x:B,P \vdash Q;
   allp_left: \forall \{B\}(P: B \rightarrow A) \times Q, P \times P \rightarrow ALL \times B, P P Q;
   allp_right: \forall \{B\}(P: A)(Q:B \rightarrow A), (\forall v, P \vdash Q v) \rightarrow P \vdash ALL x:B,Q;
   imp_andp_adjoint: \forall P Q R, P\&\&Q\vdash R \leftrightarrow P\vdash (Q\longrightarrow R);
   prop_left: \forall (P: Prop) Q, (P \rightarrow (TT \vdash Q)) \rightarrow !!P \vdash Q;
   prop_right: \forall (P: Prop) Q, P \rightarrow (Q \vdash !!P);
   not_prop_right: \forall (P:A)(Q:Prop), (Q \rightarrow (P \vdash FF)) \rightarrow P \vdash !!(\sim Q)
}.
```

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```
Class SepLog (A: Type) {ND: NatDed A} := mkSepLog {
   emp: A;
   sepcon: A \rightarrow A \rightarrow A; (Notation *)
   wand: A \rightarrow A \rightarrow A; (Notation -*; here written -*)
   ewand: A \rightarrow A \rightarrow A; (no notation; here written \rightarrow)
   sepcon_assoc: \forall P Q R, (P*Q)*R = P*(Q*R);
   sepcon_comm: \forall P Q, P*Q = Q*P;
   wand_sepcon_adjoint: \forall (P Q R: A), P*Q\vdash R \leftrightarrow P \vdash Q \twoheadrightarrow R;
   sepcon_andp_prop: \forall P Q R, P*(!!Q \&\& R) = !!Q \&\& (P*R);
   sepcon_derives: \forall P P' Q Q' : A, P \vdash P' \rightarrow Q \vdash Q' \rightarrow P*Q \vdash P'*Q':
   ewand_sepcon: \forall (P Q R : A), (P*Q) \multimap R = P \multimap (Q \multimap R);
   ewand_TT_sepcon: ∀(PQR: A),
           (P*Q)\&\&(R \multimap TT) \vdash (P \&\&(R \multimap TT))*(Q \&\& (R \multimap TT));
   exclude_elsewhere: \forall P Q: A, P*Q \vdash (P \&\&(Q \multimap TT))*Q;
   ewand_conflict: \forall P Q R, P*Q\vdash FF \rightarrow P\&\&(Q\multimap R) \vdash FF
}.
Class Indir (A: Type) {ND: NatDed A} := mkIndir {
   later: A \rightarrow A; (Notation \triangleright)
   now_later: \forall P: A, P \vdash \triangleright P;
   later_K: \forall P Q, \triangleright (P \longrightarrow Q) \vdash (\triangleright P \longrightarrow \triangleright Q);
   later_allp: \forall T (F: T \rightarrow A), \triangleright (ALL x:T, F x) = ALL x:T, \triangleright (F x);
   later_exp: \forall T (F: T \rightarrow A), EX x:T, \triangleright (F x) \vdash \triangleright (EX x: F x);
   later_exp': \forall T \text{ (any:T) } F, \triangleright (EX x: F x) = EX x:T, \triangleright (F x);
   later\_imp: \forall P Q, \triangleright (P \longrightarrow Q) = (\triangleright P \longrightarrow \triangleright Q);
   loeb: \forall P, \triangleright P \vdash P \rightarrow TT \vdash P
}.
Class SepIndir (A: Type) {NA: NatDed A}{SA: SepLog A}{IA: Indir A} :=
 mkSepIndir {
   later_sepcon: \forall P Q, \triangleright (P * Q) = \triangleright P * \triangleright Q;
   later_wand: \forall P Q, \triangleright (P \rightarrow Q) = \triangleright P \rightarrow \triangleright Q;
  later_ewand: \forall P Q, \triangleright (P \multimap Q) = (\triangleright P) \multimap (\triangleright Q)
}.
```

Aside from the standard operators and axioms of separation logic, we have exactly two primitive memory predicates:

Parameter address_mapsto:

memory_chunk \rightarrow val \rightarrow share \rightarrow share \rightarrow address \rightarrow mpred.

Parameter func_ptr : funspec \rightarrow val \rightarrow mpred.

func_ptr ϕ v means that value ν is a pointer to a function with specification ϕ .

address_maps to expresses what is typically written $x \mapsto y$ in separation logic, that is, a singleton heap containing just value y at address x. But we almost always use one of the following derived forms:

mapsto (π :share) (t:type) (v w: val) : mpred describes a singleton heap with just one value w of (C-language) type t at address v, with permission-share π .

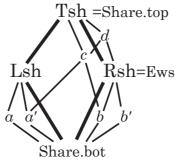
mapsto_ (π :share) (t:type) (v:val): mpred describes an *uninitialized* singleton heap with space to hold a value of type t at address v, with permission-share π .

field_at (π : share) (t: type) (fld: ident) (w v: val) : mpred describes a heap that holds just field fld of struct-value v, belonging to struct-type t, containing value w. Note: arguments w, v are swapped compared to the PLCC book.

field_at_(π : share) (t: type) (fld: ident) (v: val) : mpred is the corresponding uninitialized structure-field.

6 Shares

The maps to operator (and related operators) take a permission share, here written π and typically written sh in Coq, expressing whether the mapsto grants read permission, write permission, or some other fractional permission.



The top share, written Tsh or Share top, gives total permission: to deallocate any cells within the footprint of this mapsto, to read, to write.

Share.split Tsh = (Lsh,Rsh)
Share.split Lsh =
$$(a,a')$$
 Share.split Rsh = (b,b')
 $a' \oplus b = c$ lub $(c,Rsh) = a' \oplus Rsh = d$

Any share may be split into a left half and a right half. The left and right of the top share are given distinguished names Lsh, Rsh.

The right-half share of the top share (or any share containing it such as *d*) is sufficient to grant write permission to the data: "the right share is the write share." A thread of execution holding only Lsh-or subshares of it such as a, a'—can neither read or write the object, but such shares are not completely useless: holding any nonempty share prevents other threads from deallocating the object.

Any subshare of Rsh, in fact any share that overlaps Rsh, grants read permission to the object. Overlap can be tested using the glb (greatest lower bound) operator.

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Whenever (mapsto π t v w) holds, then the share π must include at least a read share, thus this give permission to load memory at address ν to get a value w of type t.

To make sure π has enough permission to write (i.e., Rsh $\sqsubset \pi$, we can say writable_share π : Prop.

Memory obtained from malloc comes with the top share Tsh. Writable extern global variables and stack-allocated addressable locals (which of course must not be deallocated) come with the "extern writable share" Ews which is equal to Rsh. Read-only globals come with a half-share of Rsh.

Sequential programs usually have little need of any shares except the Tsh and Ews. However, many function specifications can be parameterized over any share, and this sort of generalized specification makes the functions usable in more contexts.

In C it is undefined to test deallocated pointers for equality or inequalities, so the Hoare-logic rule for pointer comparison also requires some permission-share; see page 54.

7 CompCert C

The CompCert verified C compiler translates standard C source programs into an abstract syntax for *CompCert C*, and then translates that into abstract syntax for *C light*. Then VST Separation Logic is applied to the C light abstract syntax. C light programs proved correct using the VST separation logic can then be compiled (by CompCert) to assembly language.

C light syntax is defined by these Coq files from CompCert:

Integers. 32-bit (and 8-bit, 16-bit, 64-bit) signed/unsigned integers.

Floats. IEEE floating point numbers.

Values. The val type: integer + float + pointer + undefined.

AST. Generic support for abstract syntax.

Ctypes. C-language types and structure-field-offset computations.

Cop. Semantics of C-language arithmetic operators.

Clight. Abstract syntax of C-light expressions, statements, and functions. **veric.expr.** (from VST, not CompCert) Semantics of expression evaluation.

Some of the important types and operators are described over the next few pages.

8 Verifiable C programming See PLCC Chapter

In writing Verifiable C programs you must:

- Make each dereference into a top level expression (PLCC page 143)
- Make most pointer comparisons into a top level expression (PLCC page 145)
- Remove casts between int and pointer types (result in values that crash if used)

The clightgen tool automatically:

- Factors function calls into top level expressions
- Factors logical and/or operators into if statements (to capture short circuiting behavior)

Proof automation detects these two transformations and processes them with a single tactic application.

If your program uses malloc or free, you must declare and specify these as external functions. If you don't want to keep track of the size of each allocated object, you may want to change the interface of the free function. We do this in our example definitions of malloc and free in progs/queue.c and their specifications in progs/verif_queue.v.

The VST program logic uses CompCert's 32-bit integer type.

Inductive comparison := Ceq | Cne | Clt | Cle | Cgt | Cge.

Definition wordsize: nat := 32. (* also instantiations for 8, 16, 64 *)

Definition modulus : Z := two_power_nat wordsize.

Definition half_modulus : Z := modulus / 2.

Definition max_unsigned : Z := modulus -1. **Definition** max_signed : Z := half_modulus -1.

Definition $min_signed : Z := -half_modulus.$

Parameter int : Type.

Parameter unsigned : int \rightarrow Z. Parameter signed : int \rightarrow Z. Parameter repr : Z \rightarrow int.

Definition zero := repr 0.

Definition eq (x y: int) : bool.

Definition lt (x y: int) : bool.

Definition ltu (x y: int) : bool.

Definition neg (x: int): int := repr (- unsigned x).

Definition add $(x \ y: int): int := repr (unsigned <math>x + unsigned y)$.

Definition sub (x y: int): int := repr (unsigned x - unsigned y).

Definition mul (x y: int): int := repr (unsigned x * unsigned y).

Definition divs (x y: int) : int.

Definition mods (x y: int) : int.

Definition divu (x y: int) : int.

Definition modu (x y: int) : int.

Definition and (x y: int): int := bitwise_binop and b x y.

Definition or $(x \ y: int)$: int := bitwise_binop orb $x \ y$.

Definition xor (x y: int) : int := bitwise_binop xorb x y.

Definition not (x: int) : int := xor x mone.

Definition shl (x y: int): int.

Definition shru (x y: int): int.

Definition shr (x y: int): int.

Definition rol (x y: int) : int.

Definition ror (x y: int) : int.

Definition rolm (x a m: int): int.

Definition cmp (c: comparison) (x y: int) : bool.

Definition cmpu (c: comparison) (x y: int) : bool.

Lemma eq_dec: \forall (x y: int), $\{x = y\} + \{x <> y\}$.

Theorem unsigned_range: $\forall i, 0 \le unsigned i \le modulus$.

Theorem unsigned_range_2: \forall i, $0 \le unsigned$ i $\le max_unsigned$.

Theorem signed_range: \forall i, min_signed \leq signed i \leq max_signed.

Theorem repr_unsigned: \forall i, repr (unsigned i) = i.

Lemma repr_signed: $\forall i$, repr (signed i) = i.

Theorem unsigned_repr:

 $\forall z, 0 \le z \le \max_{unsigned} \rightarrow unsigned (repr z) = z.$

Theorem signed_repr:

 \forall z, min_signed \leq z \leq max_signed \rightarrow signed (repr z) = z.

Theorem signed_eq_unsigned:

 $\forall x$, unsigned $x \le \max_x \text{signed } x = \text{unsigned } x$.

Theorem unsigned_zero: unsigned zero = 0.

Theorem unsigned_one: unsigned one = 1.

Theorem signed_zero: signed zero = 0.

Theorem eq_sym: $\forall x \ y$, eq $x \ y = eq \ y \ x$.

Theorem eq_spec: \forall (x y: int), if eq x y then x = y else x <> y.

Theorem eq_true: $\forall x$, eq x x = true.

Theorem eq_false: $\forall x y, x <> y \rightarrow eq x y = false$.

Theorem add_unsigned: $\forall x y$, add x y = repr (unsigned x + unsigned y).

Theorem add_signed: $\forall x y$, add x y = repr (signed x + signed y).

Theorem add_commut: $\forall x y$, add x y = add y x.

Theorem add_zero: $\forall x$, add x zero = x.

Theorem add_zero_l: $\forall x$, add zero x = x.

Theorem add_assoc: $\forall x \ y \ z$, add (add $x \ y$) $z = add \ x$ (add $y \ z$).

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Theorem neg_repr: $\forall z$, neg (repr z) = repr (-z).

Theorem neg_zero: neg zero = zero.

Theorem neg_involutive: $\forall x$, neg (neg x) = x.

Theorem $neg_add_distr: \forall x y, neg(add x y) = add (neg x) (neg y).$

Theorem sub_zero_l: $\forall x$, sub x zero = x.

Theorem sub_zero_r: $\forall x$, sub zero x = neg x.

Theorem sub_add_opp: $\forall x y$, sub x y = add x (neg y).

Theorem sub_idem: $\forall x$, sub x x = zero.

Theorem sub_add_l: $\forall x \ y \ z$, sub (add $x \ y$) z = add (sub $x \ z$) y.

Theorem sub_add_r: $\forall x \ y \ z$, sub x (add y z) = add (sub x z) (neg y).

Theorem sub_shifted: $\forall x \ y \ z$, sub (add $x \ z$) (add $y \ z$) = sub $x \ y$.

Theorem sub_signed: $\forall x y$, sub x y = repr (signed x -signed y).

Theorem mul_commut: $\forall x y$, mul x y = mul y x.

Theorem $mul_zero: \forall x, mul x zero = zero.$

Theorem mul_one: $\forall x$, mul x one = x.

Theorem mul_assoc: $\forall x \ y \ z$, mul (mul $x \ y$) $z = \text{mul } x \ (\text{mul } y \ z)$.

Theorem mul_add_distr_l: $\forall x \ y \ z$, mul (add $x \ y$) z = add (mul $x \ z$) (mul $y \ z$).

Theorem mul_signed: $\forall x y$, mul x y = repr (signed x * signed y).

and many more axioms for the bitwise operators, shift operators, signed/unsigned division and mod operators.

(compcert/common/Values.v)

10 Values

Definition block : Type := positive.

Inductive val: Type :=

| Vundef: val | Vint: int →val | Vlong: int64 →val | Vfloat: float →val | Vptr: block →int →val.

Vundef is the *undefined* value—found, for example, in an uninitialized local variable.

Vint(i) is an integer value, where i is a CompCert 32-bit integer.

Vfloat(f) is an floating-point value, where f is a Flocq 64-bit floating-point number.

Vptr $b\ z$ is a pointer value, where b is an abstract block number and z is an offset within that block. Different malloc operations, or different extern global variables, or stack-memory-resident local variables, will have different abstract block numbers. Pointer arithmetic must be done within the same abstract block, with $(\operatorname{Vptr} bz) + (\operatorname{Vint} i) = \operatorname{Vptr} b(z+i)$. Of course, the C-language + operator first multiplies i by the size of the array-element that $\operatorname{Vptr} bz$ points to.

11 C types

```
Inductive signedness := Signed | Unsigned.
Inductive intsize := 18 | 116 | 132 | 1Bool.
Inductive floatsize := F32 | F64.
Record attr : Type := mk_attr {
  attr_volatile: bool
}.
Definition noattr := {| attr_volatile := false |}.
Inductive type : Type :=
    Tvoid: type
    Tint: intsize \rightarrow signedness \rightarrow attr \rightarrow type
    Tlong: signedness \rightarrow attr \rightarrow type
    Tfloat: floatsize \rightarrow attr \rightarrow type
    Tpointer: type \rightarrow attr \rightarrow type
    Tarray: type \rightarrow Z \rightarrow attr \rightarrow type
    Tfunction: typelist \rightarrow type \rightarrow type
    Tstruct: ident \rightarrow fieldlist \rightarrow attr \rightarrow type
    Tunion: ident \rightarrow fieldlist \rightarrow attr \rightarrow type
    Tcomp_ptr: ident \rightarrow attr \rightarrow type
with typelist : Type :=
   | Tnil: typelist
   | Tcons: type \rightarrow typelist \rightarrow typelist
with fieldlist : Type :=
   | Fnil: fieldlist
   | Fcons: ident \rightarrow type \rightarrow fieldlist \rightarrow fieldlist.
Definition typeconv (ty: type) : type :=
   match ty with
    Tint (18 \mid 116 \mid 1Bool) _a \Rightarrow Tint 132 Signed a
    Tarray t sz a ⇒ Tpointer t a
    Tfunction __⇒ Tpointer ty noattr
```

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```
| _⇒ ty
  end.
Fixpoint alignof (t: type) : Z :=
  match t with
    Tint I8 __⇒ 1
   Tint I16 __⇒ 2
   Tint I32 __⇒ 4
   Tlong <sub>--</sub>⇒ 8
   Tfloat F32 \Rightarrow 4
   Tfloat F64 \Rightarrow 8
   | Tpointer __⇒ 4
  ... et cetera
  end.
(** Size of a type, in bytes. *)
Fixpoint sizeof (t: type) : Z :=
  match t with
   Tint I8 __ ⇒ 1
   Tint 116 \implies 2
   Tint I32 __⇒ 4
   Tlong <sub>--</sub>⇒ 8
   Tfloat F32 \Rightarrow 4
   Tfloat F64 \Rightarrow 8
   | Tpointer <sub>--</sub>⇒ 4
  ... et cetera
  end.
Lemma sizeof_pos: \forall t, sizeof t > 0.
```

Definition field_offset (id: ident) (fld: fieldlist) : res Z.

Fixpoint field_type (id: ident) (fld: fieldlist) {struct fld} : res type.

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```
Inductive mode: Type :=
   By_value: memory_chunk → mode
   By_reference: mode
   By_copy: mode
   By_nothing: mode.
Definition access_mode (ty: type) : mode :=
  match ty with
   Tint 18 Signed _⇒ By_value Mint8signed
   Tint 18 Unsigned _⇒ By_value Mint8unsigned
   Tint I16 Signed _⇒ By_value Mint16signed
   Tint I16 Unsigned → By_value Mint16unsigned
   Tint I32 __⇒ By_value Mint32
   Tint IBool __⇒ By_value Mint8unsigned
   Tlong __⇒ By_value Mint64
   Tfloat F32 _⇒ By_value Mfloat32
   Tfloat F64 _⇒ By_value Mfloat64
   Tvoid ⇒ By_nothing
   Tpointer __⇒ By_value Mint32
   Tarray ___⇒ By_reference
   Tfunction __⇒ By_reference
   Tstruct ___⇒ By_copy
   Tunion ___⇒ By_copy
   Tcomp_ptr __⇒ By_nothing
end.
```

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COMPCERT handles self-referential structure types in the following way that deserves at least some explanation, not provided here:

```
Fixpoint unroll_composite (cid: ident) (comp: type) (ty: type) : type :=
  match ty with
    Tvoid \Rightarrow ty
   Tint ___⇒ tv
   Tlong <sub>--</sub>⇒ ty
   Tfloat __⇒ ty
   Tpointer t1 a \Rightarrow Tpointer (unroll_composite t1) a
   Tarray t1 sz a ⇒ Tarray (unroll_composite t1) sz a
   Tfunction t1 t2 \Rightarrow
         Tfunction (unroll_composite_list t1) (unroll_composite t2)
  | Tstruct id fld a \Rightarrow
         if ident_eq id cid then ty
         else Tstruct id (unroll_composite_fields fld) a
  | Tunion id fld a \Rightarrow
         if ident_eq id cid then ty
         else Tunion id (unroll_composite_fields fld) a
  | Tcomp_ptr id a \Rightarrow
         if ident_eq id cid then Tpointer comp a else ty
  end
with unroll_composite_list cid comp(tl: typelist): typelist := ...
with unroll_composite_fields cid comp (fld: fieldlist): fieldlist := ...
Lemma alignof_unroll_composite:
  \forall cid comp ty, alignof (unroll_composite cid comp ty) = alignof ty.
Lemma sizeof_unroll_composite:
  \forall cid comp ty, sizeof (unroll_composite cid comp ty) = sizeof ty.
```

12 C expression syntax

(compcert/cfrontend/Clight.v)

```
Inductive expr : Type :=
(* 1 *) | \text{ Econst\_int: int } \rightarrow \text{type} \rightarrow \text{expr}
(* 1.0 *) | \text{ Econst\_float: float } \rightarrow \text{type} \rightarrow \text{expr}
(* 1L *) | \text{ Econst\_long: int64} \rightarrow \text{type} \rightarrow \text{expr}
(* x *) | \text{ Evar: ident } \rightarrow \text{type} \rightarrow \text{expr}
(* x *) | \text{ Etempvar: ident } \rightarrow \text{type} \rightarrow \text{expr}
(* x *) | \text{ Ederef: expr} \rightarrow \text{type} \rightarrow \text{expr}
(* * * *) | \text{ Ederef: expr} \rightarrow \text{type} \rightarrow \text{expr}
(* * * * *) | \text{ Eaddrof: expr} \rightarrow \text{type} \rightarrow \text{expr}
(* * * * * *) | \text{ Eunop: unary\_operation } \rightarrow \text{expr} \rightarrow \text{type} \rightarrow \text{expr}
(* * * * * *) | \text{ Ebinop: binary\_operation } \rightarrow \text{expr} \rightarrow \text{expr} \rightarrow \text{type} \rightarrow \text{expr}
(* * * * * *) | \text{ Ecast: expr} \rightarrow \text{type} \rightarrow \text{expr}
(* * * * * *) | \text{ Efield: expr} \rightarrow \text{ident} \rightarrow \text{type} \rightarrow \text{expr}.
```

```
Definition typeof (e: expr) : type :=
  match e with
  | Econst_int _ty ⇒ ty
  | Econst_float _ty ⇒ ty
  | Evar _ty ⇒ ty
  | ... et cetera.
```

13 C operators

```
Function bool_val (v: val) (t: type) : option bool :=
  match classify_bool t with
  | bool_case_i ⇒
       match v with
       | Vint n \Rightarrow Some (negb (Int.eq n Int.zero))
        _⇒ None
       end
  | bool_case_f ⇒
       match v with
       | Vfloat f \Rightarrow Some (negb (Float.cmp Ceq f Float.zero))
       | <sub>-</sub>⇒ None
       end
  | bool_case_p ⇒
       match v with
       | Vint n \Rightarrow Some (negb (Int.eq n Int.zero))
       | Vptr b ofs \Rightarrow Some true
        _⇒ None
       end
  | bool_default ⇒ None
  end.
Function sem_neg (v: val) (ty: type) : option val :=
  match classify_neg ty with
  | neg_case_i sg ⇒
       match v with
       | Vint n \Rightarrow Some (Vint (Int.neg n))
       | _⇒ None
       end
  \mid neg\_case\_f \Rightarrow
       match v with
       | Vfloat f \Rightarrow Some (Vfloat (Float.neg f))
       | <sub>-</sub>⇒ None
       end
```

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```
\mid neg\_default \Rightarrow None
  end.
Function sem_add (v1:val) (t1:type) (v2: val) (t2:type) : option val :=
  match classify_add t1 t2 with
  | add_case_ii sg \Rightarrow (**r integer addition *)
       match v1, v2 with
       | Vint n1, Vint n2 \Rightarrow Some (Vint (Int.add n1 n2))
       | _, _⇒ None
       end
  | add_case_ff \Rightarrow (**r float addition *)
       match v1, v2 with
       | Vfloat n1, Vfloat n2 \Rightarrow Some (Vfloat (Float.add n1 n2))
       \mid \_, \_ \Rightarrow \mathsf{None}
       end
  | add_case_if sg \Rightarrow (**r int plus float *)
       match v1, v2 with
       | Vint n1, Vfloat n2 \Rightarrow Some (Vfloat (Float.add (cast_int_float sg n1) n2
       | _, _⇒ None
       end
  ... (cases omitted)
  | add_case_ip ty \Rightarrow (**r integer plus pointer *)
       match v1.v2 with
       | Vint n1, Vptr b2 ofs2 \Rightarrow
         Some (Vptr b2 (Int.add ofs2 (Int.mul (Int.repr (sizeof ty)) n1)))
       | _, _⇒ None
       end
  \mid add\_default \Rightarrow None
end.
Function sem_sub (v1:val) (t1:type) (v2: val) (t2:type) : option val.
Function sem_mul (v1:val) (t1:type) (v2: val) (t2:type) : option val.
Function sem_div (v1:val) (t1:type) (v2: val) (t2:type) : option val.
Function sem_mod (v1:val) (t1:type) (v2: val) (t2:type) : option val.
Function sem_and (v1:val) (t1:type) (v2: val) (t2:type) : option val.
```

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```
Function sem_cmp (c:comparison)
                     (v1: val) (t1: type) (v2: val) (t2: type)
                     (m: mem): option val :=
  match classify_cmp t1 t2 with
  | cmp_case_ii Signed ⇒
       match v1,v2 with
       | Vint n1, Vint n2 \Rightarrow Some (Val.of_bool (Int.cmp c n1 n2))
       | _, _⇒ None
       end
  ... (many more cases)
  end.
Definition sem_binary_operation
    (op: binary_operation)
    (v1: val) (t1: type) (v2: val) (t2:type)
    (m: mem): option val :=
  match op with
   Oadd \Rightarrow sem add v1 t1 v2 t2
   Osub \Rightarrow sem sub v1 t1 v2 t2
   Omul \Rightarrow sem_mul v1 t1 v2 t2
    Omod \Rightarrow sem_mod v1 t1 v2 t2
    Odiv \Rightarrow sem div v1 t1 v2 t2
   Oand \Rightarrow sem_and v1 t1 v2 t2
    Oor \Rightarrow sem_or v1 t1 v2 t2
    Oxor \Rightarrow sem_xor v1 t1 v2 t2
    Oshl \Rightarrow sem shl v1 t1 v2 t2
    Oshr \Rightarrow sem_shr v1 t1 v2 t2
    Oeq \Rightarrow sem\_cmp Ceq v1 t1 v2 t2 m
   One \Rightarrow sem_cmp Cne v1 t1 v2 t2 m
   Olt \Rightarrow sem_cmp Clt v1 t1 v2 t2 m
   Ogt \Rightarrow sem\_cmp Cgt v1 t1 v2 t2 m
   Ole \Rightarrow sem_cmp Cle v1 t1 v2 t2 m
   Oge \Rightarrow sem_cmp Cge v1 t1 v2 t2 m
  end.
```

14 C expression evaluation (vst/veric/expr.v)

```
Definition eval_id (id: ident) (\rho: environ).
  (* look up the tempory variable ``id'' in \rho *)
```

```
Definition eval_cast (t t': type) (v: val) : val.
  (* cast value v from type t to type t', but beware! There are
     be three types involved, if you include the native type of v. *)
```

Definition eval_unop (op: Cop.unary_operation) (t1 : type) (v1 : val) : val.

```
Definition eval_binop (op: Cop.binary_operation)
                (t1 t2 : type) (v1 v2: val) : val.
```

Definition force_ptr (v: val) : val := match v with Vptr I ofs \Rightarrow v | \rightarrow Vundef end.

```
Definition eval_struct_field (delta: Z) (v: val) : val.
   (* offset the pointer-value v by delta *)
```

Definition eval_field (ty: type) (fld: ident) (v: val) : val. (* calculate the Ivalue of (but do not fetch/dereference!) a structure/union field of value v *)

Definition eval_var (id:ident) (ty: type) (rho: environ) : val. (* Get the Ivalue (address of) an addressable local variable (if there is one of that name) or else a global variable *)

Definition deref_noload (ty: type) (v: val) : val. (* For By_reference types such as arrays that dereference without actually fetching *) match access_mode ty with By_reference $\Rightarrow v \mid _\Rightarrow Vundef end$.

```
Fixpoint eval_expr (e: expr) : environ \rightarrow val :=
 match e with
  Econst_int i ty \Rightarrow `(Vint i)
  Econst_float f ty \Rightarrow `(Vfloat f)
  Etempor id ty \Rightarrow eval_id id
  Eaddrof a ty \Rightarrow eval_lvalue a
  Eunop op a ty \Rightarrow `(eval_unop op (typeof a)) (eval_expr a)
 | Ebinop op a1 a2 ty \Rightarrow
              `(eval_binop op (typeof a1) (typeof a2))
                 (eval_expr a1) (eval_expr a2)
  Ecast a ty \Rightarrow `(eval_cast (typeof a) ty) (eval_expr a)
  Evar id ty \Rightarrow `(deref_noload ty) (eval_var id ty)
  Ederef a ty \Rightarrow `(deref_noload ty) (`force_ptr (eval_expr a))
  | Efield a i ty ⇒ `(deref_noload ty)
                           (`(eval_field (typeof a) i) (eval_lvalue a))
 end
 with eval_lvalue (e: expr) : environ \rightarrow val :=
 match e with
 | Evar id ty \Rightarrow eval_var id ty
 | Ederef a ty ⇒ `force_ptr (eval_expr a)
  Efield a i ty \Rightarrow `(eval_field (typeof a) i) (eval_lvalue a)
  _⇒ `Vundef
 end.
```

15 *C* type checking

Ideally, you will never notice the typechecker, but it may occasionally generate side conditions that can not be solved automatically. If you get a proof goal from the typechecker, it will be an entailment $P \vdash denote_tc_assert$ (...). PLCC Chapter Chapter 26 discusses what you can do to solve these goals.

If you are asked to prove an entailment where the typechecking condition evaluates to False, this is because your program is not written in Verifiable C. You may need to perform some local transformations on your C program in order to proceed. We listed these transformations on page 14.

The type-context will always be visible in your proof in a line that looks like Delta := abbreviate : tycontext. The abbreviate hides the implementation of the type context (which is generally large and uninteresting). The query_context tactic shows the result of looking up a variable in a typecontext. Applying query_context Delta _p. will add hypothesis QUERY : (temp_types Delta) ! _p = Some (tptr t_struct_list, true). This means that in Delta, _p is a temporary variable with type tptr t_struct_list and that it is known to be initialized.

Assertions in our Hoare triple of separation are presented as env \rightarrow mpred, that is, functions from environment to memory-predicate, using our natural deduction system NatDed(mpred) and separation logic SepLog(mpred).

Given a separation logic over a type B of formulas, and an arbitrary type A, we can define a *lifted* separation logic over functions $A \rightarrow B$. The operations are simply lifted pointwise over the elements of A. Let $P,Q:A\to B$, let $R: T \rightarrow A \rightarrow B$ then define,

```
(P \&\& Q): A \rightarrow B := \text{fun } a \Rightarrow Pa \&\& Qa
     (P \parallel Q): A \rightarrow B := \text{fun } a \Rightarrow Pa \parallel Qa
(\exists x.R(x)): A \rightarrow B := \text{fun } a \Rightarrow \exists x.Rxa
(\forall x.R(x)): A \rightarrow B := \text{fun } a \Rightarrow \forall x. Rxa
(P \longrightarrow Q): A \rightarrow B := \text{fun } a \Rightarrow Pa \longrightarrow Qa
    (P \vdash Q): A \rightarrow B := \forall a. Pa \vdash Qa
     (P*Q): A \rightarrow B := \text{fun } a \Rightarrow Pa*Qa
   (P \rightarrow Q): A \rightarrow B := \text{fun } a \Rightarrow Pa \rightarrow Qa
```

In Coq we formalize the typeclass instances LiftNatDed, LiftSepLog, etc., as shown below. For a type B, whenever NatDed B and SepLog B (and so on) have been defined, the lifted instances NatDed ($A \rightarrow B$) and SepLog $(A \rightarrow B)$ (and so on) are automagically provided by the typeclass system.

```
Instance LiftNatDed(A B: Type){ND: NatDed B}: NatDed (A \rightarrow B):=
 mkNatDed (A \rightarrow B)
      (*andp*) (fun P Q x \Rightarrow andp (P x) (Q x))
      (*orp*) (fun P Q x \Rightarrow orp (P x) (Q x))
      (*exp*) (fun \{T\} (F: T \rightarrow A \rightarrow B) (a: A) \Rightarrow exp (fun x \Rightarrow F \times a))
      (*allp*) (fun \{T\} (F: T \rightarrow A \rightarrow B) (a: A) \Rightarrow allp (fun x \Rightarrow F \times a))
      (*imp*) (fun P Q x \Rightarrow imp (P x) (Q x))
      (*prop*) (fun P x \Rightarrow prop P)
      (*derives*) (fun P Q \Rightarrow \forall x, derives (P x) (Q x))
```

In particular, if P and Q are functions of type environ \rightarrow mpred then we can write P * Q, P && Q, and so on.

Consider this assertion:

```
\begin{array}{c} \text{fun } \rho \Rightarrow \text{mapsto } \pi \text{ tint (eval\_id \_x } \rho) \text{ (eval\_id \_y } \rho) \\ * \text{ mapsto } \pi \text{ tint (eval\_id \_u } \rho) \text{ (Vint Int.zero)} \end{array}
```

which might appear as the precondition of a Hoare triple. It represents $(x \mapsto y) * (u \mapsto 0)$ written in informal separation logic, where x, y, u are C-language variables of integer type. Because it can be inconvenient to manipulate explicit lambda expressions and explicit environment variables ρ , we may write it in lifted form,

```
`(mapsto \pi tint) (eval_id _x) (eval_id _y) 
* `(mapsto \pi tint) (eval_id _u) `(Vint Int.zero)
```

Each of the first two backquotes lifts a function from type val \rightarrow val \rightarrow mpred to type (environ \rightarrow val) \rightarrow (environ \rightarrow val) \rightarrow (environ \rightarrow mpred), and the third one lifts from val to environ \rightarrow val.

17 Canonical forms

We write a canonical form of an assertion as,

$$PROP(P_0; P_1; ..., P_{l-1}) LOCAL(Q_0; Q_1; ..., Q_{m-1}) SEP(R_0; R_1; ..., R_{n-1})$$

The P_i : Prop are Coq propositions—these are independent of the program variables and the memory. The Q_i : environ \rightarrow Prop are local—they depend on program variables but not on memory. The R_i : environ \rightarrow mpred are assertions of separation logic, which may depend on both program variables and memory.

The PROP/LOCAL/SEP form is defined formally as,

```
Definition PROPx (P: list Prop) (Q: assert) := andp (prop (fold_right and True P)) Q.
```

Notation "'PROP' (x; ...; y) z" :=

(PROPx (cons x%type .. (cons y%type nil) ..) z) (at level 10) : logic.

Notation "'PROP' () z" := (PROPx nil z) (at level 10) : logic.

```
Definition LOCALx (Q: list (environ \rightarrow Prop)) (R: assert) := andp (local (fold_right (`and) (`True) Q)) R.
```

Notation "'LOCAL' (x; ...; y) z" :=

(LOCALx (cons x%type .. (cons y%type nil) ..) z) (at level 9) : logic.

Notation "'LOCAL' () z" := (LOCALx nil z) (at level 9) : logic.

Definition SEPx (R: list assert): assert := fold_right sepcon emp R.

```
Notation " 'SEP' ( x ; ...; y )" := 
 (SEPx (cons x%logic ... (cons y%logic nil) ..)) (at level 8) : logic. 
 Notation " 'SEP' ( ) " := (SEPx nil) (at level 8) : logic. 
 Notation " 'SEP' () " := (SEPx nil) (at level 8) : logic.
```

Thus, $PROP(P_0; P_1)LOCAL(Q_0; Q_1)SEP(R_0; R_1)$ is equivalent to $prop P_0 \land prop P_1 \&\& `prop Q_0 \&\& `prop Q_1 \&\& (R_0 *R_1).$

18 Supercanonical forms

A canonical form $PROP(\vec{P})LOCAL(\vec{Q})SEP(\vec{R})$ is supercanonical if,

- every element of \vec{Q} has the form `(eq V) (eval_id i), where V is any Coq expression of type val and i is $\beta\eta$ -equivalent to a constant (a ground term of type ident).
- every element of R is either
 `(E) where E is a Coq expression of type mpred, or
 `(F) (evalvar i t) where F is a Coq expression of type val→mpred and i is βη-equivalent to a constant.

When assertions (preconditions of semax) are kept in supercanonical form, the forward tactic for symbolic execution runs *much* faster. That is,

- In VST 1.3, forward through ordinary assignment statements (not loads/stores) is up to 10 times faster for supercanonical preconditions than for ordinary (canonical) preconditions.
- In future versions of VST, forward through other kinds of statements will be faster supercanonical preconditions.
- Future versions of the forward tactic may *require* the precondition to be in supercanonical form.

19 Go_lower

An entailment $PROP(\vec{P})LOCAL(\vec{Q})SEP(\vec{R}) \vdash PROP(\vec{P'})LOCAL(\vec{Q'})SEP(\vec{R'})$ is a sequent in our *lifted* separation logic; each side has type environ \rightarrow mpred. By definition of the lifted entailment \vdash it means exactly, $\forall \rho$. $PROP(\vec{P})LOCAL(\vec{Q})SEP(\vec{R})\rho \vdash PROP(\vec{P'})LOCAL(\vec{Q'})SEP(\vec{R'})\rho$. There are two ways to prove such an entailment: Explicitly introduce ρ (descend into an entailment on mpred) and unfold the PROP/LOCAL/SEP form; or stay in canonical form and rewrite in the lifted logic. Either way may be appropriate; this chapter describes how to descend. The go_lower tactic, described on this page, is rarely called directly; it is the first step of the entailer tactic (page 40) when applied to lifted entailments.

The tactic go_lower tactic does the following:

- 1. intros ?rho, as described above.
- 2. If the first conjunct of the left-hand-side locals is tc_environ $\Delta \rho$, move it above the line; this be useful in step 6.
- 3. Unfold definitions for canonical forms (PROPx LOCALx SEPx), expression evaluation (eval_exprlist eval_expr eval_lvalue cast_expropt eval_cast eval_binop eval_unop), casting (eval_cast classify_cast) type-checking (tc_expropt tc_expr tc_lvalue typecheck_expr typecheck_lvalue denote_tc_assert), function postcondition operators (function_body_ret_assert make_args' bind_ret get_result1 retval), lifting operators (liftx LiftEnviron Tarrow Tend lift_S lift_T lift_prod lift_last lifted lift_uncurry_open lift_curry local lift lift0 lift1 lift2 lift3).
- 4. Simplify by simpl.
- 5. Rewrite by the rewrite-hint environment go_lower, which contains just a very few rules to evaluate certain environment lookups.
- 6. Recognize local variables.

Local variables that appear in the lifted canonical form as (eval_id_x) will be replaced by Coq variables x, provided that: (1) \vec{Q} includes a clause of the form (tc_environ Δ), and (2) there is a hypothesis name x_x "above the line." (See PLCC section 26). In addition, a typechecking hypothesis for x will be introduced above the line.

20 Normalize

The normalize tactic performs autorewrite **with** norm and several other transformations. Many of the simplifications performed by normalize on entailments (whether lifted or unlifted) can be done more efficiently and systematically by entailer. However, on Hoare triples, entailer does not apply, and normalize is quite appropriate.

The norm rewrite-hint database uses several sets of rules.

Generic separation-logic simplifications.

Unlifting.

'f
$$\rho = f$$
 [when f has arity 0] 'f $a_1 \rho = f$ ($a_1 \rho$) [when f has arity 1]
'f $a_1 a_2 \rho = f$ ($a_1 \rho$) ($a_2 \rho$) [when f has arity 2, etc.]
local $P \rho = !!(P \rho)$ ($P * Q)\rho = P\rho * Q\rho$ ($P \&\& Q)\rho = P\rho \&\& Q\rho$ ($!!P)\rho = !!P$!!($P \land Q$) = !! $P \&\& !!Q$
(EX $x : A, P x)\rho = EX x : A, P x \rho$ '(EX $x : B, P x$) = EX $x : B,$ '($P x$))
'($P * Q$) = ' $P * Q$ '($P \&\& Q$) = ' $P \&\& Q$

20. Normalize 36

Pulling nonspatial propositions out of spatial ones.

local
$$P$$
 && !! Q =!! Q && local P local P && (!! Q && R) =!! Q && (local P && R) (local P && R) $= |P| = |$

Canonical forms.

$$\begin{aligned} \log & |Q_1 \otimes \& (\text{PROP}(\vec{P}) \text{LOCAL}(\vec{Q}) \text{SEP}(\vec{R})) = \text{PROP}(\vec{P}) \text{LOCAL}(Q_1; \vec{Q}) \text{SEP}(\vec{R}) \\ & \text{PROP} \vec{P} \text{LOCAL} \vec{Q} \text{SEP}(!!P_1; \vec{R}) = \text{PROP}(P_1; \vec{P}) \text{LOCAL}(\vec{Q}) \text{SEP}(\vec{R}) \\ & \text{PROP}(\vec{P}) \text{LOCAL}(\vec{Q}) \text{SEP}(\text{local}Q_1; \vec{R}) = \text{PROP}(\vec{P}) \text{LOCAL}(Q_1; \vec{Q}) \text{SEP}(\vec{R}) \end{aligned}$$

Modular Integer arithmetic.

Int.sub
$$x$$
 $x = \text{Int.zero}$ Int.sub x Int.zero $= x$
Int.add x (Int.neg x) $= \text{Int.zero}$ Int.add x Int.zero $= x$
Int.add Int.zero $x = x$

$$x \neq y \to \text{offset_val}(\text{offset_val } v \ i) \ j = \text{offset_val } v \ (\text{Int.add } i \ j)$$
Int.add(Int.repr i)(Int.repr j) $= \text{Int.repr}(i + j)$
Int.add(Int.add x (Int.repr x)) (Int.repr x) $= \text{Int.add } x$ (Int.repr(x))
$$x > 0 \to (\text{align } 0 \ x = 0)$$
 force_int(Vint x) $= x$

20. Normalize 37

Type checking and miscellaneous.

Expression evaluation. (autorewrite with eval, but in fact these are usually handled just by simpl or unfold.)

$$\mathsf{deref_noload}(\mathsf{tarray}\ t\ n) = (\mathsf{fun}\ v \Rightarrow v)$$

$$\mathsf{eval_expr}(\mathsf{Etempvar}\ i\ t) = \mathsf{eval_id}\ i \qquad \mathsf{eval_expr}(\mathsf{Econst_int}\ i\ t) = \mathsf{`(Vint}\ i)$$

$$\mathsf{eval_expr}(\mathsf{Ebinop}\ op\ a\ b\ t) =$$

$$\mathsf{`(eval_binop}\ op\ (\mathsf{typeof}\ a)\ (\mathsf{typeof}\ b))\ (\mathsf{eval_expr}\ a)\ (\mathsf{eval_expr}\ b)$$

$$\mathsf{eval_expr}(\mathsf{Eunop}\ op\ a\ t) = \mathsf{`(eval_unop}\ op\ (\mathsf{typeof}\ a))\ (\mathsf{eval_expr}\ a)$$

$$\mathsf{eval_expr}(\mathsf{Ecast}\ e\ t) = \mathsf{`(eval_cast}(\mathsf{typeof}\ e)\ t)\ (\mathsf{eval_expr}\ e)$$

$$\mathsf{eval_lvalue}(\mathsf{Ederef}\ e\ t) = \mathsf{`force_ptr}\ (\mathsf{eval_expr}\ e)$$

20. Normalize 38

```
Structure fields.
```

```
field_mapsto \pi t fld (force_ptr v) = field_mapsto \pi t fld v

field_mapsto_\pi t fld (force_ptr v) = field_mapsto_\pi t fld v

field_mapsto \pi t x (offset_val v Int.zero) = field_mapsto_\pi t x v

field_mapsto_\pi t x (offset_val v Int.zero) = field_mapsto_\pi t x v

memory_block \pi Int.zero (Vptr b z) = emp

Postconditions. (autorewrite with ret_assert.)

normal_ret_assert \bot ek \lorl = \bot

frame_ret_assert(normal_ret_assert P) Q = normal_ret_assert (P*Q)
```

normal_ret_assert P ek vl = (!!(ek = EK_normal) && (!!(vl = None) && P))

loop1_ret_assert P Q EK_normal None = PoverridePost P R EK_normal None = PoverridePost P R EK_return = R EK_return

function_body_ret_assert t P EK_return vl = bind_ret vl t P

20. Normalize 39

Function return values.

bind_ret (Some v) t Q = (!!tc_val t v && 'Q(make_args(ret_temp :: nil)) (v :: nil))) make_args' σ a ρ = make_args (map fst (fst σ)) (a ρ) ρ make_args(i :: l)(v :: r) ρ = env_set(make_args(l)(r) ρ) i v make_args nil nil = globals_only get_result(Some x) = get_result1(x) retval(get_result1 i ρ) = eval_id i ρ retval(env_set ρ ret_temp v) = v retval(make_args(ret_temp :: nil)) (v :: nil) ρ) = v ret_type(initialized i Δ) = ret_type(Δ)

IN ADDITION TO REWRITING, the normalize tactic applies the following rules:

$$P \vdash \top$$
 $\bot \vdash P$ $P \vdash P * \top$ $(\forall x. (P \vdash Q)) \rightarrow (EXx : A, P \vdash Q)$
 $(P \rightarrow (\top \vdash Q)) \rightarrow (!!P \vdash Q)$ $(P \rightarrow (Q \vdash R)) \rightarrow (!!P \& Q \vdash R)$

and does some rewriting and substitution when *P* is an equality in the goal, $(P \rightarrow (Q \vdash R))$.

Given the goal $x \to P$, where x is not a Prop, the normalize avoids doing an intro. This allows the user to choose an appropriate name for x.

21 Entailer

Our entailer tactic is a partial solver for entailments in the separation logic over mpred. If it cannot solve the goal entirely, it leaves a simplified subgoal for the user to prove. The algorithm is this:

- 1. Apply go_lower if the goal is in the lifted separation logic.
- 2. Gather all the pure propositions to a single pure proposition (in each of the hypothesis and conclusion).
- 3. Given the resulting goal $!!(P_1 \wedge ... \wedge P_n) \&\& (Q_1 * ... * Q_m) \vdash !!(P'_1 \wedge ... \wedge P'_{n'}) \&\& (Q'_1 ... * Q'_{m'})$, move each of the pure propositions P_i "above the line." Any P_i that's an easy consequence of other above-the-line hypotheses is deleted. Certain kinds of P_i are simplified in some ways.
- 4. For each of the Q_i , saturate_local extracts any pure propositions that are consequences of spatial facts, and inserts them above the line if they are not already present. For example, $p \mapsto_{\tau} q$ has two pure consequences: isptr p (meaning that p is a pointer value, not an integer or float) and tc_val τ q (that the value q has type τ).
- 5. For any equations (x = ...) or (... = x) above the line, substitute x.
- 6. Simplify C-language comparisons.
- 7. Rewriting: the normalize tactic, as explained in Chapter 14.
- 8. Repeat from step 2, as long as progress is made.
- 9. Now the proof goal has the form $(Q_1 \dots * Q_m) \vdash !!(P'_1 \wedge \dots \wedge P'_{n'}) \&\& (Q'_1 \dots * Q'_{m'})$. Any of the P'_i provable by auto are removed. If $Q_1 * \dots * Q_m \vdash Q'_1 * \dots * Q'_{m'}$ is trivially proved, then the entire $\&\& Q'_1 * \dots * Q'_{m'}$ is removed.

At this point the entailment may have been solved entirely. Or there may be some remaining P'_i and/or Q'_i proof goals on the right hand side.

Given an entailment $(A_1 * A_2) * ((A_3 * A_4) * A_5) \vdash A'_4 * (A'_5 * A'_1) * (A'_3 * A'_2)$ for any associative-commutative rearrangement of the A_i , and where (for each i), A_i is $\beta \eta$ equivalent to A'_i , then the cancel tactic will solve the goal.

When we say A_i is $\beta \eta$ equivalence to A'_i , that is equivalent to saying that (change (A_i) with (A'_i)) would succeed.

If the goal has the form $(A_1 * A_2) * ((A_3 * A_4) * A_5) \vdash (A'_4 * B_1 * A'_1) * B_2$ where there is only a partial match, then cancel will remove the matching conjuncts and leave a subgoal such as $A_2 * A_3 * A_5 \vdash B_1 * B_2$.

If the goal is $(A_1 * A_2) * ((A_3 * A_4) * A_5) \vdash A'_4 * \top * A'_1$, where some terms cancel and the rest can be absorbed into \top , then cancel will solve the goal.

If the goal has the form

$$F := ?224 : list(environ \rightarrow mpred)$$

$$(A_1 * A_2) * ((A_3 * A_4) * A_5) \vdash A'_4 * (fold_right sepcon emp F) * A'_1$$

where F is a *frame* that is an abbreviation for an uninstantiated logical variable of type list(environ \rightarrow mpred), then the cancel tactic will perform *frame inference*: it will unfold the definition F, instantiate the variable (in this case, to $A_2 :: A_3 :: A_5 :: nil$), and solve the goal.

The frame may have been created by evar(F: list(environ→mpred)). This is typically done automatically, as part of forward symbolic execution through a function call.

23 The Hoare triple

In the judgment $\Delta \vdash \{P\} c \{R\}$, written in Coq as semax (Δ : tycontext) (P: environ \rightarrow mpred) (c: statement) (R: ret_assert)

- Δ is a *type context*, giving types of function parameters, local variables, and global variables; and giving *specifications* (funspec) of global functions.
- *P* is the precondition;
- c is a command in the C language; and
- *R* is the postcondition. Because a *c* statement can exit in different ways (fall-through, continue, break, return), a ret_assert has predicates for all of these cases.

The *basic* VST separation logic is specified in vst/veric/SeparationLogic.v, and contains rules such as,

```
semax_set_forward \Delta \vdash \{ \triangleright P \} \ x := e \ \{ \exists v. \ x = (e[v/x]) \land P[v/x] \}
```

```
Axiom semax_set_forward: \forall \Delta P (x: ident) (e: expr), semax \Delta (\triangleright (local (tc_expr \Delta e) \&\& local (tc_temp_id id (typeof e) \Delta e) \&\& P)) (Sset \times e) (normal_ret_assert (EX old:val, local (`eq (eval_id x) (subst x (`old) (eval_expr e))) && subst x (`old) P)).
```

However, most C-program verifications will not use the *basic* rules, but will use derived rules whose preconditions are in canonical (PROP/LOCAL/SEP) form. Furthermore, program verifications do not even use the derived rules directly, but use *symbolic execution tactics* that choose which derived rules to apply. So we will not show the rules here; we describe how to use the tactical system.

24 Later

Many of the Hoare rules, such as the one on page 42,

semax_set_forward
$$\Delta \vdash \{ \triangleright P \} \ x := e \ \{ \exists v. \ x = (e[v/x]) \land P[v/x] \}$$

have the operater ▷ (pronounced "later") in their precondition.

The modal assertion $\triangleright P$ is a slightly weaker version of the assertion P. It is used for reasoning by induction over how many steps left we intend to run the program. The most important thing to know about \triangleright later is that P is stronger than $\triangleright P$, that is, $P \vdash \triangleright P$; and that operators such as *, && , ALL (and so on) commute with later: $\triangleright (P * Q) = (\triangleright P) * (\triangleright Q)$.

This means that if we are trying to apply a rule such as semax_set_forward; and if we have a precondition such as

local (tc_expr
$$\Delta$$
 e) && \triangleright local (tc_temp_id id t Δ e) && ($P_1 * \triangleright P_2$)

then we can use the rule of consequence to weaken this precondition to \triangleright (local (tc_expr \triangle e) && local (tc_temp_id id t \triangle e) && ($P_1 * P_2$))

and then apply semax_set_forward. We do the same for many other kinds of command rules.

This weakening of the precondition is done automatically by the forward tactic, as long as there is only one plater in a row at any point among the various conjuncts of the precondition.

A more sophisticated understanding of \triangleright is needed to build proof rules for recursive data types and for some kinds of object-oriented programming; see PLCC Chapter 19.

Let F be a C-language function, $t_{ret} F (t_1 x_1, t_2 x_2, \dots t_n x_n) \{ \dots \}$. The formal parameters are $\vec{x}:\vec{t}$ (that is, $x_1:t_1,x_2:t_2,\ldots x_n:t_n$) and the return type is t_{ret} .

Specify F with precondition $P(\vec{a}:\vec{\tau})(\vec{x}:\vec{t})$ and postcondition $Q(\vec{a}:\vec{\tau})(retval)$ where \vec{a} are logical variables that both the precondition and the postcondition can refer to.

The x_i are C-language variable identifiers, and the t_i are C-language types (tint, tfloat, tptr(tint), etc.). The a_i are Coq variables and the τ_i are Coq types.

```
Definition F-spec :=
 DECLARE _F
  WITH a_1 : \tau_1, \ldots a_k : \tau_k
  PRE [x_1 OF t_1, ..., x_n OF t_n] P
  POST [t_{rot}] Q.
```

Example: for a C function, int sumlist (struct list *p);

```
Definition sumlist_spec :=
 DECLARE _sumlist
 WITH sh: share, contents: list int, p: val,
  PRE [ _p OF (tptr t_struct_list)]
       local (`(eq p) (eval_id _p))
       && `(Iseg LS sh contents p nullval)
  POST [tint]
       local (`(eq (Vint (sum_int contents))) retval)
       && `(lseg LS sh contents p nullval).
```

The specification itself is an object of type ident*funspec, and in some cases it can be useful to define the components separately:

```
Definition sumlist_funspec : funspec :=
 WITH sh: share, contents: list int, p: val,
```

```
PRE [ _p OF (tptr t_struct_list)]
    local (`(eq p) (eval_id _p))
    && `(lseg LS sh contents p nullval)

POST [ tint ]
    local (`(eq (Vint (sum_int contents))) retval)
    && `(lseg LS sh contents p nullval).
```

Definition sumlist_spec : ident*funspec := DECLARE _sumlist sumlist_funspec.

The precondition may be written in *simple form*, as shown above, or in *canonical form*:

```
Definition sumlist_spec :=
DECLARE _sumlist
WITH sh : share, contents : list int, p: val,
PRE [ _p OF (tptr t_struct_list)]
        PROP() LOCAL(`(eq p) (eval_id _p))
        SEP(`(lseg LS sh contents p nullval))
POST [ tint ]
        local (`(eq (Vint (sum_int contents))) retval)
        && `(lseg LS sh contents p nullval).
```

At present, postconditions may not use PROP/LOCAL/SEP form.

26 Specifying all functions

We give each function a *specification*, typically using the DECLARE/WITH/PRE/POST notation. Then we combine these together into a *global specification*:

$$\Gamma$$
: list (ident*funspec) := $(\iota_1, \phi_1) :: (\iota_2, \phi_2) :: (\iota_3, \phi_3) :: (\iota_4, \phi_4) :: nil.$

We also make a *global variables type specification*, listing the types of all extern global variables:

$$V : \mathsf{list} (\mathsf{ident*type}) := (x_1, t_1) :: (x_2, t_2) :: \mathsf{nil}$$

The *initialization values* of extern globals are not part of V, as (generally) they are not invariant over program execution—global variables can be updated by storing into them. Initializers are accessible in the precondition to the _main function.

C-language functions can call each other, and themselves, and access global variables. Correctness proofs of individual functions can take advantage of the specifications of all global functions and types of global variables. Thus we construct Γ and V before proving correctness of any functions.

The next step (in a program proof) is to prove correctness of each function. For each function F in a C program, CompCert clightgen produces $_F$: ident. f_F : function. where function is a record telling the parameters and locals (and their types) and the function body. The predicate semax_body states that F meets its specification; for each F we must prove:

Lemma body_F: semax_body $V \Gamma$ f_F F_spec.

27 Proving a function

The predicate semax_body states that function F's implementation (function body) meets its specification (funspec). The definition of the predicate, written in veric/SeparationLogic.v, basically states the Hoare triple of the function body, $\Delta \vdash \{Pre\} \ c \ \{Post\}$, where Pre and Post are taken from the funspec for f, c is the fn_body of the function F, and the type-context Δ is calculated from the global type-context overlaid with the parameter- and local-types of the function.

To prove this, we begin with the tactic start_function, which takes care of some simple bookkeeping—unfolding certain definitions, destructing certain tuples, and putting the precondition in canonical form.

Lemma body_F: semax_body $V \Gamma f_F F_spec.$

Proof.

start_function.

name x _x.

name y $_{-}$ y. name z $_{-}$ z.

Then, for each function parameter and nonaddressable local variable (scalar local variable whose address is never taken), we write a name declaration; in each case, _x is the identifier definition that clightgen has created from the source-language name, and x is the Coq name that we wish to use for the *value* of variable _x at various points. The only purpose of the name tactic is to assist the go_lower tactic in choosing nice names.

At this point the proof goal will be a judgment of the form, semax Δ (PROP(\vec{P})LOCAL(\vec{Q})SEP(\vec{R})) c *Post*.

We prove such judgments as follows:

1. Manipulate the precondition $PROP(\vec{P})LOCAL(\vec{Q})SEP(\vec{R})$ until it takes a form suitable for forward symbolic execution through the first statement in the command c. (In this we are effectively using the rule of consequence.)

- 2. Apply a forward tactic to step into c. This will produce zero or more entailments $A \vdash B$ to prove, where A is in canonical form; and zero or more semax judgments to prove.
- 3. Prove the entailments, typically using go_lower; prove the judgment, i.e., back to step 1.

Each kind of C command has different requirements on the form of the precondition, for the forward tactic to succeed. In each of the following cases, the expression E must not contain loads, stores, side effects, function calls, or pointer comparisons. The variable x must be a nonaddressable local variable.

- c_1 ; c_2 Sequencing of two commands. The forward tactic will work on c_1 first.
- (c_1 ; c_2) c_3 In this case, forward will re-associate the commands using the seq_assoc axiom, and work on c_1 ; (c_2 ; c_3).
- x=E; Assignment statement. Expression E must not contain memory dereferences (loads or stores using *prefix, suffix[], or -> operators). Expression E must not contain pointer-comparisons. No restrictions on the form of the precondition (except that it must be in canonical form). The expression &p \rightarrow next does not actually load or store (it just computes an address) and is permitted.
- x=*E; Memory load. The SEP component of the precondition must contain an item of the form `(mapsto π t) e ν , where e is equivalent to (eval_expr E). For example, if E is just an identifer (Etempvar _y t), then e could be either (eval_expr (Etempvar _y t)) or (eval_id _y).
- x = a[E]; Array load. This is just a memory load, equivalent to x = *(a+E);.
- $x = E \rightarrow fld$; Field load. This is equivalent to x = *(E.fld) and can actually be handled by the "memory load" case, but a special-purpose field-load rule is easier to use (and will be automatically applied by the forward tactic). In this case the SEP component of the precondition must contain `(field_at π t fld) v e, where t is the structure type to which the field fld belongs, and e is equivalent to (eval_expr E).

- * $E_1 = E_2$; Memory store. The SEP component of the precondition must contain an item of the form `(mapsto π t) e_1 ν or an item `(mapsto_ π t) e_1 , where e_1 is equivalent to (eval_expr E_1).
- $a[E_1]=E_2$; Array store. This is equivalent to *(a+ E_1)= E_2 ; and is handled by the previous case.
- $E_1 \rightarrow fld = E_2$; Field store. This can be handled by the general store case, but a special-purpose field-store rule is easier to use. The SEP component of the precondition must contain either `(field_at π t fld) v e_1 or `(field_mapsto_ π t fld) e_1 , where t is the structure type to which the field fld belongs, and e_1 is equivalent to (eval_expr E_1). The share π must be strong enough to grant write permission, that is, writable_share(π).
- $x=E_1$ op E_2 ; If E_1 or E_2 evaluate to *pointers*, and *op* is a comparison operator (=, !=, <, <=, >, \geq), then E_1 op E_2 must not occur except in this special-case assignment rule. When E_1 and E_2 both have numeric values, the ordinary *assignment statement* rule applies.

Pointer comparisons are tricky in CompCert C for reasons explained at PLCC page 249; the program logic uses the semax_ptr_compare rule (PLCC page 164). After applying the forward tactic, the user will be left with some proof obligations: Prove that both E_1 and E_2 evaluate to allocated locations (i.e., that the precondition implies $E_1 \stackrel{\pi_1}{\mapsto} -*TT$ and also implies $E_2 \stackrel{\pi_2}{\mapsto} -*TT$, for any π_1 and π_2). If the comparison is any of >, <, \geq , <=, prove that E_1 and E_2 both point within the same allocated object. These are preconditions for even being permitted to test the pointers for equality (or inequality). See also page 54.

- if (*E*) C_1 else C_2 No restrictions on the form of the precondition. forward will create 3 subgoals: (1) prove that the precondition entails tc_expr Δ *E*. For many expressions *E*, the condition tc_expr Δ *E* is simply TT, which is trivial to prove. (2) the **then** clause... (3) the **else** clause...
- **while (***E***)** *C* For a while-loop, use the forward_while tactic (page **??**).
- **return** *E*; No special precondition, except that the presence/absence of *E* must match the nonvoid/void return type of the function. The proof goal left by forward is to show that the precondition (with appropriate

substitution for the abstract variable ret_var) entails the function's postcondition.

 $x = f(a_1, ..., a_n)$; For a function call, use forward. This results a proof goal to show that the precondition implies the function precondition and includes two uninstantiated variables. witness is the function arguments. To instantiate it use

instantiate (1:= $\langle arguments here \rangle$) in (Value of witness).

You may get an error message saying "Instance is not well-typed in the environment of ...". This means a variable used for the instantiation was introduced after the creation of the witness evar. To resolve this, apply semax_pre with an assertion that the variables exist, then introduce the variables before calling forward. An example of this is in progs/veriv_queue before fifo_put is called. The Frame variable represents the part of the spacial precondition that is unchanged by the function call. It will generally be instantiated by a call to cancel.

28 Manipulating preconditions

In some cases you cannot go forward until the precondition has a certain form. For example, in ordinary separation logic we might have $\{p \neq q \land p \leadsto q\} \ x := p \to tail \{Post\}$. In order to use the proof rule for load, we must use the rule of consequence, to prove,

$$p \neq q \land p \rightarrow q \vdash p \neq q \land \exists h, t. p \mapsto (h, t) * t \rightarrow q$$

then instantiate the existentials; this finally gives us

$$\{p \neq q \land p \mapsto (h, t) * t \rightarrow q\} x := p \rightarrow tail \{Post\}$$

which is provable by the standard load rule of separation logic.

Faced with the proof goal semax Δ (PROP(\vec{P})LOCAL(\vec{Q})SEP(\vec{R})) c *Post* where PROP(\vec{P})LOCAL(\vec{Q})SEP(\vec{R}) does not match the requirements for forward symbolic execution, you have several choices:

- Use the rule of consequence explicitly: apply semax_pre with PROP($\vec{P'}$)LOCAL($\vec{Q'}$)SEP($\vec{R'}$), then prove $\vec{P}; \vec{Q}; \vec{R} \vdash \vec{P'}; \vec{Q'}; \vec{R'}$ using go_lower (page 34).
- Use the rule of consequence implicitly, by using tactics that modify the precondition (and may leave entailments for you to prove).
- Do rewriting in the precondition, either directly by the standard rewrite and change tactics, or by normalize.
- Extract propositions and existentials from the precondition, by using normalize (or by applying the rules extract_exists_pre and semax_extract_PROP).

TACTICS FOR MANIPULATING PRECONDITIONS. In many of these tactics we select specific conjucts from the SEP items, that is, the semicolon-separated list of separating conjuncts. These tactic refer to the list by zero-based position number, 0,1,2,.... For example, suppose the goal is a semax or

- entailment containing PROP(\vec{P})LOCAL(\vec{Q})SEP(a;b;c;d;e;f;g;h;i;j). Then:
- focus_SEP i j k. Bring items #i, j, k to the front of the SEP list.
 - focus_sep 5. $results in PROP(\vec{P})LOCAL(\vec{Q})SEP(f;a;b;c;d;e;g;h;i;j).$
 - focus_sep 0. $results in PROP(\vec{P})LOCAL(\vec{Q})SEP(a;b;c;d;e;f;g;h;i;j)$.
 - focus_SEP 1 3. results in PROP(\vec{P})LOCAL(\vec{Q})SEP(b;d;a;c;e;f;g;h;i;j)
 - focus_SEP 3 1. results in $PROP(\vec{P})LOCAL(\vec{Q})SEP(d;b;a;c;e;f;g;h;i;j)$
- gather_SEP i j k. Bring items #i, j, k to the front of the SEP list and conjoin them into a single element.
 - gather_sep 5. results in PROP(\vec{P})LOCAL(\vec{Q})SEP(f;a;b;c;d;e;g;h;i;j). gather_SEP 1 3. results in PROP(\vec{P})LOCAL(\vec{Q})SEP(b*d;a;c;e;f;g;h;i;j)
 - gather_SEP 3 1. results in PROP(\vec{P})LOCAL(\vec{Q})SEP(d*b;a;c;e;f;g;h;i;j)
- replace_SEP i R. Replace the ith element the SEP list with the assertion R, and leave a subgoal to prove.
 - replace_sep 3 R. results in PROP(\vec{P})LOCAL(\vec{Q})SEP(a;b;c;R;e;f;g;h;i;j). with subgoal PROP(\vec{P})LOCAL(\vec{Q})SEP(d) \vdash R.
- replace_in_pre S S'. Replace S with S' anywhere it occurs in the precondition then leave $(\vec{P}; \vec{Q}; \vec{R}) \vdash (\vec{P}; \vec{Q}; \vec{R})[S'/S]$ as a subgoal.
- frame_SEP $i\ j\ k$. Apply the frame rule, keeping only elements i,j,k of the SEP list. See Chapter 29.

29 The Frame rule

Separation Logic supports the Frame rule,

Frame
$$\frac{\{P\} c \{Q\}}{\{P * F\} c \{Q * F\}}$$

To use this in a forward proof, suppose you have the proof goal, semax $\triangle \mathsf{PROP}(\vec{P})\mathsf{LOCAL}(\vec{Q})\mathsf{SEP}(R_0;R_1;R_2)$ $c_1;c_2;c_3$ *Post*

and suppose you want to "frame out" R_2 for the duration of c_1 ; c_2 , and have it back again for c_3 . First you rewrite by seq_assoc to yield the goal semax $\Delta \ \mathsf{PROP}(\vec{P})\mathsf{LOCAL}(\vec{Q})\mathsf{SEP}(R_0;R_1;R_2) \ (c_1;c_2); c_3 \ \mathit{Post}$

Then eapply semax_seq' to peel off the first command $(c_1; c_2)$ in the new sequence:

semax
$$\Delta \ \mathsf{PROP}(\vec{P}) \mathsf{LOCAL}(\vec{Q}) \mathsf{SEP}(R_0; R_1; R_2) \ c_1; c_2$$
 ?88

semax Δ' ?88 c_3 Post

Then frame_SEP 0 2 to retain only R_0 ; R_2 . semax \triangle PROP(\vec{P})LOCAL(\vec{Q})SEP(R_0 ; R_2) c_1 ; c_2 ...

You'll see that (in the precondition of the second subgoal) the unification variable ?88 has been instantiated in such a way that R_2 is added back in.

30 Pointer comparisons

See PLCC Chapter 25

Pointer comparisons can be split into two cases:

- 1. Comparisons between two expressions that evaluate to be pointers. In this case, both of the pointers must be to *allocated* objects, or the expression will not evaluate
- 2. Comparisons between an expression that evaluates to the null pointer and any expression that evaluates to a value with a pointer type. This expression will always evaluate

If you are sure that your pointer comparison falls into the first case, you may treat it exactly like any other expression. The proof may eventually generate a side-condition asking you to prove that one of the expressions evaluates to the null pointer. If your pointer comparison might be between two pointers, however, the expression should be factored into its own statement (PLCC page 145).

When you use forward on a pointer comparison you might get a side condition with a disjunction. The left and right sides of the disjunction correspond to the first and second type of comparison above. In simple cases, the tactic can solve the disjunction automatically.

31 Structured data

The C programming language has struct and array to represent structured data. The *Verifiable C* logic provides operators field_at, array_at, and data_at to describe assertions about structs and arrays.

Given a struct definition, struct list {int head; struct list *tail;}; the clightgen utility produces the type t_struct_list describing fields head and tail. Then these assertions are all equivalent:

```
mapsto \pi tint p h * mapsto \pi (tptr t_struct_list) (offset_val p (Vint.repr 4)) t field_at \pi t_struct_list _head h p * field_at \pi t_struct_list _tail t p data_at \pi t_struct_list (h,t) p
```

The version using maps to is correct (assuming a 32-bit configuration of CompCert) but rather ugly; the second version is useful when loading or storing a particular field; the third version describes the contents of all structure-fields at once.

The data_at predicate is dependently typed; the *type* of its third argument (h, t) depends on the *value* of its second argument. The dependent type is expressed by the function, reptype: type \rightarrow Type that converts C-language types into Coq Types.

Here, reptype t_struct_list = val*val, so the type of (h, t) is (val*val). The value h may be Vint(i) or Vundef, and t may be Vpointer b z, Vint Int.zero, or Vundef. The Vundef values represent uninitialized data fields.

The tactic simpl_data_at converts data_at predicates to their expanded form as field_at. One would use simpl_data_at before forward through a load or store that accesses one of the field_at predicates. A future version of the proof automation rules for Verifiable C may permit field access without expanding data_at.

WHY ARE THE ARGUMENTS BACKWARDS? We write

field_at π t_struct_list _head h p where Reynolds would have written $p.\text{head} \mapsto h$, and we write data_at π t_struct_list (h,t) p where Reynolds would have written $p \hookrightarrow (h,t)$. Putting the *contents* argument before the *pointer* argument makes it easier to express identities in our lifted separation logic. That is, we commonly have formulas such as

```
`(data_at \pi t_struct_list (h,t)) (eval_id _p )tptr t_struct_list)) which simplify to `(field_at \pi t_struct_list _head h * field_at \pi t_struct_list _tail t) (eval_id _p (tptr t_struct_list))
```

Expressing these equivalences with the arguments in the other order would lead to extra lambdas, which are (ironically) no fun at all.

Partially initialized data structures. Consider the program

```
struct list *f(void) {
   struct list *p = (struct list *)malloc(sizeof(struct list));
   /* 1 */ p→head= 3;
   /* 2 */ p→tail= NULL;
   /* 3 */ return p;
}
```

We do not want to assume that malloc returns initialized memory, so at point 1 the contents of head and tail are Vundef. We can write this as any of the following:

If malloc returns fields that—operationally—contain defined values instead of Vundef, these assertions are still valid, as they ignore the contents of the fields.

At point 2, all the assertions above are still true, but they are weaker than the "appropriate" assertion, which may be written as any of,

At point 3, we can write either of,

FULLY INITIALIZED DATA STRUCTURES. In a function precondition it is sometimes convenient to write,

```
WITH data: reptype t_struct_list
PRE [_p OF tptr t_struct_list] (**)
    `(data_at Tsh t_struct_list data) (eval_id _p (tptr t_struct_list))
POST [ ... ] ...
```

If $p \rightarrow$ head and $p \rightarrow$ tail may be uninitialized, this is fine. But if the structure is known to be initialized, the precondition as written does not express this fact. One would need to add the conjunct !!(is_int (fst data) \land is_pointer_or_null (snd data)) at the point marked (**).

The function reptype': type \rightarrow Type expresses the type of *initialized* data structures. For example, reptype' t_struct_list is (int*val). The function

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```
expresses injections from (possibly) undefined to defined values. Suppose
```

(h: int, t: val) is a value of type reptype' t_struct_list . Then repinj t_struct_list (h,t) = (Vint h, t)

```
Using reptype' one could write,
```

repinj (t: type): reptype' t → reptype t

```
WITH data: reptype' t_struct_list

PRE [_p OF tptr t_struct_list]
    !!(is_pointer_or_null (snd data) &&
    `(data_at Tsh t_struct_list (repinj _data)) (eval_id _p (tptr t_struct_list))

POST [ ... ] ...
```

Notice that this only solves half the problem—for integers but not for pointers. Since defined pointers can be either NULL or a Vpointer, we use val to represent them, and the Coq type alone does not express the refinement. One could imagine a version of reptype' that uses a refinement type to accomplish this, but it might be unwieldy.

32 Signed and unsigned integers

Mathematical proofs use the mathematical integers (the Z type in Coq); C progams use 32-bit signed or unsigned integers. They are related as follows:

Int.repr: $Z \rightarrow int$. Int.unsigned: int $\rightarrow Z$. Int.signed: int $\rightarrow Z$.

with the following lemmas:

Int.repr truncates to a 32-bit twos-complement representation (losing information if the input is out of range). Int.signed and Int.unsigned are different injections back to Z that never lose information.

When doing proofs about integers, the recommended proof technique is to make sure your integers never overflow. That is, if the C variable $_{\perp}x$ contains the value Vint (Int.repr x), then make sure x is in the appropriate range. Let's assume that $_{\perp}x$ is a signed integer, i.e. declared in C as int x; then the hypothesis is,

H: Int.min_signed $\leq x \leq$ Int.max_signed

If you maintain this hypothesis "above the line", then the normalize tactic can automatically rewrite with Int.signed (Int.repr x) = x. Also, to solve goals such as,

...
H2: 0 <= n <= Int.max_signed
...
Int.min_signed <= 0 <= n

you can use the repable_signed tactic, which is basically just omega with knowledge of the values of Int.min_signed, Int.max_signed, and Int.max_unsigned.

To take advantage of this, put conjuncts into the PROP part of your function precondition such as $0 \le i < n$; $n \le \text{Int.max_signed}$. Then the start_function tactic will move them above the line, and the other tactics mentioned above will make use of them.

To see an example in action, look at progs/verif_sumarray.v. The array size and index (variables size and i) are kept within bounds; but the *contents* of the array might overflow when added up, which is why add_elem uses Int.add instead of Z.add.

33 For loops

The C-language for loop has the general form,

for (init; test; incr) body

To solve a proof goal of this form (or when this is followed by other statements in sequence), use the tactic

forward_for Inv PreIncr PostCond

where Inv, PreIncr, PostCond are assertions (in PROP/LOCAL/SEP form):

Inv is the loop invariant, that holds immediately after the *init* command is executed and before each time the *test* is done; *PreIncr* is the invarint that holds immediately after the loop *body* and right before the *incr*;

PostCond is the assertion that holds after the loop is complete (whether by a break statement, or the test evaluating to false).

The following feature will appear in VST version 1.5.

Many for-loops have this special form, for (init; id < hi; id++) body such that the expression hi will evaluate to the same value every time around the loop. This upper-bound expression need not be a literal constant, it just needs to be invariant. Then you can use the tactic,

forward_for_simple_bound n (EX i:Z, PROP(\vec{P}) LOCAL(\vec{Q}) SEP(\vec{R}).

where n is the upper bound: a Coq value of type Z such that hi will evaluate to n. The loop invariant is given by the expression (EX i:Z, PROP(\vec{P}) LOCAL(\vec{Q}) SEP(\vec{R}), where i is the value (in each iteration) of the loop iteration variable id. This tactic generates simpler subgoals than the general forward_for tactic.

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When the loop has the form, for (id=lo; id < hi; id++) body where lo is a literal constant, then the forward_for_simple_bound tactic will generate slightly simpler subgoals.

34 Nested Loads

This experimental feature will appear in VST release 1.5.

To handle assignment statements with nested loads, such as x[i]=y[i]+z[i]; the recommended method is to break it down into smaller statments compatible with separation logic: t=y[i]; u=z[i]; x[i]=t+u;. However, sometimes you may be proving correctness of preexisting or machinegenerated C programs. Verifiable C has an *experimental* nested-load mechanism to support this.

We use an expression-evaluation relation $e \downarrow v$ which comes in two flavors:

```
rel_expr : expr \rightarrow val \rightarrow rho \rightarrow mpred. rel_lvalue: expr \rightarrow val \rightarrow rho \rightarrow mpred.
```

The assertion rel_expr $e \ v \ \rho$ says, "expression e evaluates to value v in environment ρ and in the current memory." The rel_lvalue evaluates the expression as an l-value, to a pointer to the data.

Evaluation rules for rel_expr are listed here:

```
rel_expr_const_int:
                                 \forall (i : int) \ \tau \ (P : mpred) \ (\rho : environ),
   P \vdash \text{rel\_expr} (\text{Econst\_int } i \ \tau) (\text{Vint } i) \ \rho.
rel_expr_const_float: \forall (f : float) \ \tau \ P \ (\rho : environ),
   P \vdash \text{rel\_expr} (\text{Econst\_float } f \mid \tau) (\text{Vfloat } f) \rho.
rel_expr_const_long: \forall (i : int64) \tau P \rho,
   P \vdash \text{rel\_expr} (\text{Econst\_long } i \ \tau) (\text{Vlong } i) \ \rho.
                                  \forall (id: ident) \tau (\nu: val) P \rho,
rel_expr_tempvar:
    Map.get (te_of \rho) id = Some \nu \rightarrow
   P \vdash \text{rel\_expr} (\text{Etempvar id } \tau) \vee \rho.
rel_expr_addrof: \forall (e : expr) \ \tau \ (v : val) \ P \ \rho,
   P \vdash \text{rel\_lvalue } e \lor \rho \rightarrow
   P \vdash \text{rel\_expr} (\mathsf{Eaddrof} \ e \ \tau) \ v \ \rho.
\mathsf{rel\_expr\_unop:} \qquad \forall \, P \, \left( e_1 : \mathsf{expr} \right) \left( \nu_1 \, \, \nu \, : \mathsf{val} \right) \, \tau \, \, \mathit{op} \, \, \rho \, ,
   P \vdash \text{rel\_expr } e_1 \ v_1 \ \rho \rightarrow
   Cop.sem_unary_operation op v_1 (typeof e_1) = Some v \rightarrow
```

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```
P \vdash \text{rel\_expr} (\text{Eunop } op \ e_1 \ \tau) \ \nu \ \rho.
rel_expr_binop: \forall (e_1 \ e_2 : expr) (v_1 \ v_2 \ v : val) \ \tau \ op \ P \ \rho,
   P \vdash \text{rel\_expr } e_1 \ v_1 \ \rho \rightarrow
   P \vdash \text{rel\_expr } e_2 \ v_2 \ \rho \rightarrow
   (∀ m : Memory.Mem.mem,
     Cop.sem_binary_operation op v_1 e (typeof e_1) v_2 (typeof e_2) m = Some v) –
   P \vdash \text{rel\_expr} (\text{Ebinop } op \ e_1 \ e_2 \ \tau) \ \nu \ \rho.
rel_expr_cast: \forall (e_1 : expr) (v_1 \ v : val) \ \tau \ P \ \rho,
   P \vdash \mathsf{rel}_{-}\mathsf{expr}\ e_1\ v_1\ \rho \rightarrow
   Cop.sem_cast v_1 (typeof e_1) \tau = \text{Some } v \rightarrow
   P \vdash \text{rel\_expr} (\text{Ecast } e_1 \ \tau) \ \nu \ \rho.
rel_expr_lvalue: \forall (a : expr) (sh : Share.t) (v_1 v_2 : val) P \rho,
   P \vdash \text{rel_lvalue a } \nu_1 \rho \rightarrow
   P \vdash \text{mapsto sh (typeof a)} \ v_1 \ v_2 * TT \rightarrow
   \nu_2 <> Vundef \rightarrow
   P \vdash \text{rel\_expr a } v_2 \rho.
rel_lvalue_local: \forall (id : ident) \tau (b : block) P \rho,
   P \vdash !!(\mathsf{Map.get} \ (\mathsf{ve\_of} \ \rho) \ \mathsf{id} = \mathsf{Some} \ (\mathsf{b}, \ \tau)) \rightarrow
   P \vdash \text{rel\_lvalue} (\text{Evar id } \tau) (\text{Vptr b Int.zero}) \rho.
rel_lvalue_global:
                             \forall (id: ident) \tau (\nu: val) P \rho,
   P
   \vdash !!(\mathsf{Map.get} \ (\mathsf{ve\_of} \ \rho) \ \mathsf{id} = \mathsf{None} \ \land
                Map.get (ge_of \rho) id = Some (v, \tau)) \rightarrow
   P \vdash \text{rel\_lvalue} (\text{Evar id } \tau) \vee \rho.
                           \forall (a : expr) (b : block) (z : int) \tau P \rho,
rel_lvalue_deref:
   P \vdash \text{rel\_expr a (Vptr b z) } \rho \rightarrow
   P \vdash \text{rel\_lvalue} (\text{Ederef a } \tau) (\text{Vptr b z}) \rho.
rel_lvalue_field_struct: \forall (i id : ident) \tau e (b : block) (z : int) (fList : fieldlist) a
   typeof e = \text{Tstruct id fList att} \rightarrow
   field_offset i fList = Errors.OK \delta \rightarrow
   P \vdash \text{rel\_expr } e \text{ (Vptr b z) } \rho \rightarrow
   P \vdash \text{rel\_lvalue} (\text{Efield } e \mid \tau) (\text{Vptr b (Int.add z (Int.repr } \delta))) \rho.
```

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The primitive nested-load assignment rule is,

```
Axiom semax_loadstore:
```

```
\label{eq:continuous_problem} \begin{array}{l} \forall\, v0\ v1\ v2\ \Delta\ e1\ e2\ sh\ P\ P',\\ \text{writable\_share sh} \to\\ P\ \vdash !!\ (tc\_val\ (typeof\ e1)\ v2)\\ \&\&\ rel\_lvalue\ e1\ v1\\ \&\&\ rel\_expr\ (Ecast\ e2\ (typeof\ e1))\ v2\\ \&\&\ (`(mapsto\ sh\ (typeof\ e1)\ v1\ v0)\ *\ P')\to\\ \text{semax}\ \Delta\ (\triangleright\ P)\ (Sassign\ e1\ e2)\\ &\ (normal\_ret\_assert\ (`(mapsto\ sh\ (typeof\ e1)\ v1\ v2)\ *\ P')). \end{array}
```

but do not use this rule! It is best to use a derived rule, such as,

Lemma semax_loadstore_array:

```
\forall n vi lo hi t1 (contents: Z \rightarrow reptype t1) v1 v2 \triangle e1 ei e2 sh P Q R,
 reptype t1 = val \rightarrow
 type_is_by_value t1 \rightarrow
 legal_alignas_type t1 = true \rightarrow
 typeof e1 = tptr t1 \rightarrow
 typeof ei = tint \rightarrow
 PROPx P (LOCALx Q (SEPx R))
     ⊢rel_expr e1 v1
       && rel_expr ei (Vint (Int.repr vi))
       && rel_expr (Ecast e2 t1) v2 \rightarrow
 nth_error R n = Some (`(array_at t1 sh contents lo hi v1)) \rightarrow
 writable_share sh →
 tc_val t1 v2 \rightarrow
 in_range lo hi vi →
 semax \Delta (> PROPx P (LOCALx Q (SEPx R)))
  (Sassign (Ederef (Ebinop Oadd e1 ei (tptr t1)) t1) e2)
  (normal_ret_assert
   (PROPx P (LOCALx Q (SEPx
    (replace_nth n R
      `(array_at t1 sh (upd contents vi (valinject _ v2)) lo hi v1)))))).
```

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```
Proof-automation support is available for semax_loadstore_array and rel_expr, in the form of the forward_nl (for "forward nested loads") tactic. For example, with this proof goal,
```

```
semax Delta
  (PROP ()
   LOCAL(`(eq (Vint (Int.repr i))) (eval_id _i); `(eq x) (eval_id _x);
   `(eq y) (eval_id _y); `(eq z) (eval_id _z))
   SEP(`(array_at tdouble Tsh (Vfloat oo fx) 0 n x);
   `(array_at tdouble Tsh (Vfloat oo fy) 0 n y);
   `(array_at tdouble Tsh (Vfloat oo fz) 0 n z)))
  (Ssequence
     (Sassign (*x[i] = y[i] + z[i]; *)
        (Ederef
           (Ebinop Oadd (Etempvar _x (tptr tdouble)) (Etempvar _i tint)
              (tptr tdouble)) tdouble)
        (Ebinop Oadd
           (Ederef
              (Ebinop Oadd (Etempvar _y (tptr tdouble)) (Etempvar _i tint)
                  (tptr tdouble)) tdouble)
           (Ederef
              (Ebinop Oadd (Etempvar _z (tptr tdouble)) (Etempvar _i tint)
                  (tptr tdouble)) tdouble) tdouble))
      MORE_COMMANDS)
  POSTCONDITION
```

the tactic-application forward_nl yields the new proof goal,

`(array_at tdouble Tsh (Vfloat oo fz) 0 n z)))
MORE_COMMANDS
POSTCONDITION

35 Cygwin

Users of Microsoft Windows should install VST under Cygwin. Unfortunately, CompCert 2.3 does not (completely) build under Cygwin. That is, CompCert's Coq development builds fine; the subset of CompCert imported into VST (which is mirrored in vst/compcert) has no problems. The problem is with the Ocaml build of the extracted code. CompCert uses the Menhir parser generator, which does not build in Cygwin (as of July 2014).

This means that you cannot use CompCert's clightgen front-end to translate .c files into .v files, on cygwin. You will have to use a CompCert installation on a Mac or Linux machine (or virtual machine) to do this.