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## [1] PIRMOSIOS EILĖS DIFERENCIALINĖ LYGTIS SU ATSKIRIAMAIS KINTAMAISIAIS

eq: $2 \cdot x + x \cdot y^2 + (4 - x^2)^(1/2) \cdot diff(y,x) = 0$ ;

$$\sqrt{4-x^2} \left( \frac{d}{dx} y \right) + x y^2 + 2 x = 0$$

Nenaudojant ODE2 funkcijos

 $eq-(x\cdot y^2+2\cdot x);$ 

$$\sqrt{4-x^2} \left( \frac{d}{dx} y \right) = -x y^2 - 2 x$$

factor(%);

$$\sqrt{4-x^2} \left( \frac{d}{dx} y \right) = -x \left( y^2 + 2 \right)$$

eq1: $%/(y^2+2)/((4-x^2)^(1/2));$ 

$$\frac{\frac{d}{dx}y}{y^2+2} = -\frac{x}{\sqrt{4-x^2}}$$

subst([y=y(x),dx=1,dy=diff(y(x),x)],eq1);

$$\frac{\frac{d}{dx}y(x)}{y(x)^2+2} = -\frac{x}{\sqrt{4-x^2}}$$

integrate(%,x);

$$\frac{\frac{d}{dx}y(x)}{y(x)^{2}+2}x = \sqrt{4-x^{2}} + \%c1$$

/\* integravimas ranka \*/

res:  $(1/\sqrt{2})\cdot \arctan(y(x)/\sqrt{2}) = \sqrt{4-x^2} + \sqrt{1}$ 

$$\frac{\arctan\left|\frac{y(x)}{\sqrt{2!}}\right|}{\sqrt{2!}} = \sqrt{4 - x^2} + \%c1$$

res:res- $sqrt(4-x^2)$ ;

$$\frac{\arctan\left(\frac{y(x)}{\sqrt{2^1}}\right)}{\sqrt{2^1}} - \sqrt{4-x^2} = \%c1$$

lhs(%)=C;

$$\frac{\arctan\left(\frac{y(x)}{\sqrt{2^1}}\right)}{\sqrt{2^1}} - \sqrt{4 - x^2} = C$$

Atsakymas:

ats:subst(y(x)=y,%);

$$\frac{\arctan\left|\frac{y}{\sqrt{2^1}}\right|}{\sqrt{2^1}} - \sqrt{4 - x^2} = C$$

Naudojant ODE2 funkciją

eq2:solve(eq,'diff(y,x))[1];

$$\frac{d}{dx} y = -\frac{x y^2 + 2 x}{\sqrt{4 - x^2}}$$

ode2(eq2,y,x);

$$-\frac{\operatorname{atan}\left|\frac{y}{\sqrt{2^{1}}}\right|}{\sqrt{2^{1}}} = %c - \sqrt{4 - x^{2^{1}}}$$

Pertvarkome šį sprendinį

%+(4-x^2)^(1/2);

$$\sqrt{4-x^2} - \frac{\operatorname{atan}\left|\frac{y}{\sqrt{2^1}}\right|}{\sqrt{2^1}} = \%c$$

%·**-1**;

$$\frac{\operatorname{atan}\left|\frac{y}{\sqrt{2^{1}}}\right|}{\sqrt{2^{1}}} - \sqrt{4 - x^{2}} = -\%c$$

Atsakymas:

ats:lhs(%)=C;

$$\frac{\operatorname{atan}\left|\frac{y}{\sqrt{2^{1}}}\right|}{\sqrt{2^{1}}} - \sqrt{4 - x^{2}} = C$$

Patikrinimas:

depends(y,x);

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diff(ats,x);

$$\frac{\frac{d}{dx}y}{2\left[\frac{y^2}{2}+1\right]} + \frac{x}{\sqrt{4-x^2}} = 0$$

solve(%,'diff(y,x));

$$\[ \frac{d}{dx} y = - \frac{x y^2 + 2 x}{\sqrt{4 - x^2}} \]$$

subst(%,eq2);

$$-\frac{xy^{2}+2x}{\sqrt{4-x^{2}}}=-\frac{xy^{2}+2x}{\sqrt{4-x^{2}}}$$

is(%);

true

Nubrėšime keletą integralinių kreivių, kai C=1/10, C=1/2, C=1. (Lyg ir ne toks brėžinys turėtų gautis pagal dėst.)

kr:makelist(ev(ats),C,[1/10,1/2,1]);

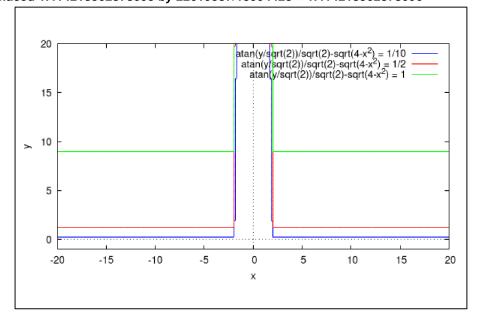
$$\begin{bmatrix}
\frac{\operatorname{atan}\left|\frac{y}{\sqrt{2^{1}}}\right|}{\sqrt{2^{1}}} & -\sqrt{4-x^{2}} = \frac{1}{10}, \frac{\operatorname{atan}\left|\frac{y}{\sqrt{2^{1}}}\right|}{\sqrt{2^{1}}} & -\sqrt{4-x^{2}} = \frac{1}{2}, \frac{\operatorname{atan}\left|\frac{y}{\sqrt{2^{1}}}\right|}{\sqrt{2^{1}}} & -\sqrt{2}, \frac{\operatorname{atan}\left|\frac{y}{\sqrt{2}}\right|}$$

load(implicit\_plot)\$

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## $wximplicit_plot(kr,[x,-20,20],[y,-1,20],same_xy)$ \$

rat: replaced 1.414213562373095 by 22619537/15994428 = 1.414213562373096 rat: replaced 1.414213562373095 by 22619537/15994428 = 1.414213562373096



Nubrėšime izoklines ir krypčių lauką.

## load(drawdf)\$

f:rhs(eq1);

$$-\frac{x}{\sqrt{4-x^2}}$$

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 \begin{array}{l} wxdrawdf(f,[x,-5,5],[y,-5,5],\\ color=red,\\ line\_width=2,\\ implicit(kr[1],x,-5,5,y,-5,5),\\ implicit(kr[2],x,-5,5,y,-5,5),\\ implicit(kr[3],x,-5,5,y,-5,5),\\ proportional\_axes='xy) \\ \end{array}
```

rat: replaced 1.414213562373095 by 22619537/15994428 = 1.414213562373096 rat: replaced 1.414213562373095 by 22619537/15994428 = 1.414213562373096

"/tmp/maxout\_163114\_1.gnuplot" line 338: warning: Skipping data file with no valid points

