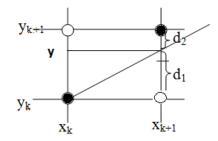
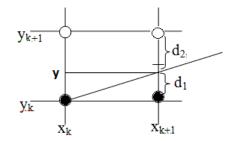
## Bresenham's Line Drawing Algorithm for Lines with Slope <=1

For the line with slope less than equal to one, the pixel positions are determined by sampling at unit 'x' interval i.e.  $x_{k+1} = x_k + 1$ , with the starting pixel at  $(x_0, y_0)$  from left hand.

For any  $k^{th}$  step, assuming position  $(x_k, y_k)$  has been selected at previous step, we determine next position  $(x_{k+1}, y_{k+1})$  as either  $(x_{k+1}, y_k)$  or  $(x_{k+1}, y_k + 1)$ 

At  $x_{k+1}$  label vertical pixel separations from ideal line path as  $d_1$  and  $d_2$ , 'y' coordinate at  $x_{k+1}$  will be  $y = m(x_{k+1}) + c$ 





The distance of lower pixel from the ideal location  $d_1 = y - y_k$  or  $d_1 = m(x_k+1) + c - y_k$ The distance of the ideal location from the upper pixel  $d_2 = y_k + 1 - y$  or  $d_2 = y_k + 1 - m(x_k+1) - c$ Thus the difference between the separations of two pixel positions from the actual line path,

$$d_1 - d_2 = m(x_k+1) + c - y_k - y_k - 1 + m(x_k+1) + c$$
  
$$d_1 - d_2 = 2m(x_k+1) + 2c - 2y_k - 1$$

Substituting  $m = \Delta y/\Delta x$ , we get

$$\Delta x \ (d_1-d_2) = 2 \ \Delta y. \ x_k + 2\Delta y \ + \Delta x.2c \ - \Delta x.2y_k - \Delta x$$

 $P_k = \Delta x.(d_1 - d_2) = 2 \Delta y. \ x_k - 2\Delta x. \ y_k + b \dots$  (i) where  $b = 2\Delta y + \Delta x.2c - \Delta x$  and  $P_k$  is the decision parameter at the  $k^{th}$  step

At the k+1<sup>th</sup> step

$$P_{k+1} = 2 \Delta y.x_{k+1} - 2\Delta x.y_{k+1} + b \dots$$
 (ii)

Now subtracting (i) and (ii)

$$P_{k+1} \ = P_k + 2 \Delta y. \ (y_{k+1} - y_k) \text{ - } 2 \Delta x. \ (x_{k+1} - x_k)$$

Since the slope of the line is less than one, we sample in 'x' direction i.e.  $x_{k+1} - x_k = 1$  so,

$$P_{k+1} = P_k + 2\Delta y. (y_{k+1} - y_k) - 2\Delta x \dots (iii)$$

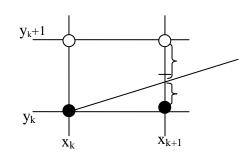
Case 1:

if  $P_k \le 0$  then the pixel on scanline

' $y_k$ ' is closer to the line path and  $y_{k+1} = y_k$ 

i.e. from equation (iii)

$$P_{k+1} = P_k + 2\Delta y$$



The Initial Decision Parameter  $P_0 = ?$ 

We have,

$$d_1 - d_2 = 2m(x_k+1) + 2c - 2y_k - 1$$

if the line passes thru  $(x_0, y_0)$  then

$$d_1 - d_2 = 2m (x_0+1) + 2c - 2y_0 - 1$$

$$= 2mx_0 + 2c - 2y_0 + 2m - 1$$
or  $d_1 - d_2 = 2m - 1$  since,  $2mx_0 + 2c - 2y_0 = 0$ 
or  $\mathbf{P_0} = \Delta x (d_1 - d_2) = 2\Delta y - \Delta x$ 

## Algorithm

## For |m| <= 1

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i. Read xa,ya,xb,yb (Assume -1 <= m <=1)  
ii. Load (x_0, y_0) into the frame buffer (i.e. plot the first point)  
iii. Calculate constants \Delta y, \Delta x, 2\Delta y and 2\Delta y - 2\Delta x  
Obtain the first decision parameter p_0 = 2\Delta y - \Delta x  
iv. At each x_k along the line starting at k=0 perform the following tests:  
If p_k < 0 then the next point to plot is (x_k +1 , y_k) and p_{k+1} = p_k + 2\Delta y  
else the next point to plot is (x_k +1 , y_k +1) and p_{k+1} = p_k + 2\Delta y - 2\Delta x  
v. Repeat step iv \Delta x times
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Here first we initialize the decision parameter and set the first pixel. Next, during each iteration, we increment 'x' to the next horizontal position, then use the current value of the decision parameter to select the bottom or top pixel (increment y) and update the decision parameter and at the end set the chosen pixel.