

1. Prove DeMorgan's laws. That is, that  $(A \cup B)^c = A^c \cap B^c$  and  $(A \cap B)^c = A^c \cup B^c$ .
2. Prove that  $(A^c)^c = A$ .
3. Prove that  $(A \cup B) \cap C = (A \cap C) \cup (B \cap C)$ .
4. Show that the function  $\frac{1}{\beta} \exp(-x/\beta)$  integrates to 1 over  $x > 0$  for  $\beta > 0$ .
5. Show that the function  $\frac{e^{-x}}{(1+e^{-x})^2}$  integrates to 1 over  $-\infty < x < \infty$ .
6. Show that the derivative of the function  $(1+e^{-x})^{-1}$  is the function from the previous problem.
7. Argue that  $\sum_{x=0}^{\infty} e^{-\lambda} \lambda^x / x! = 1$  for  $\lambda > 0$ .
8. Plot the functions from the previous 3 problems in R.