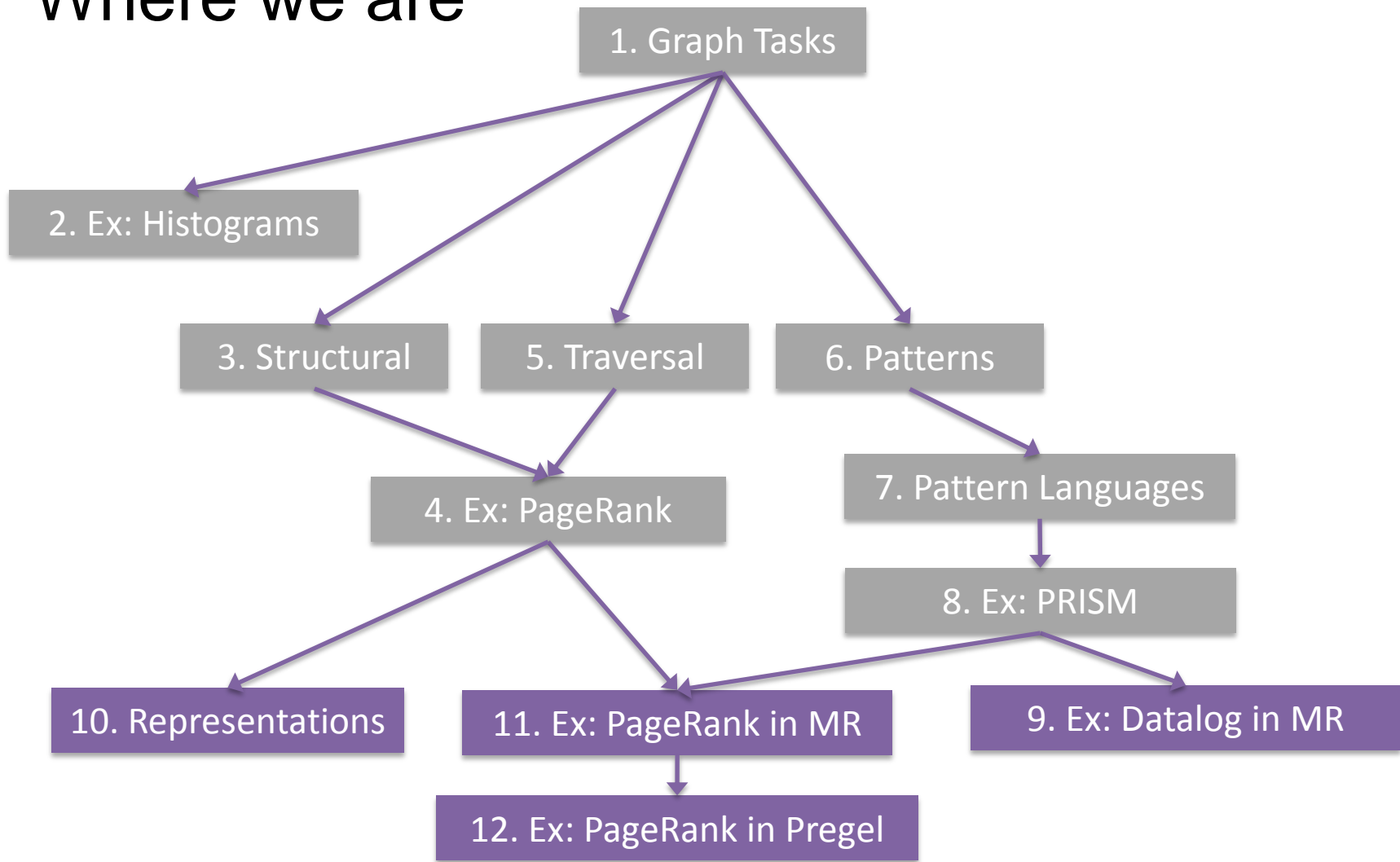


# Where we are



# Evaluation of Recursive Programs

Reachability from a given node

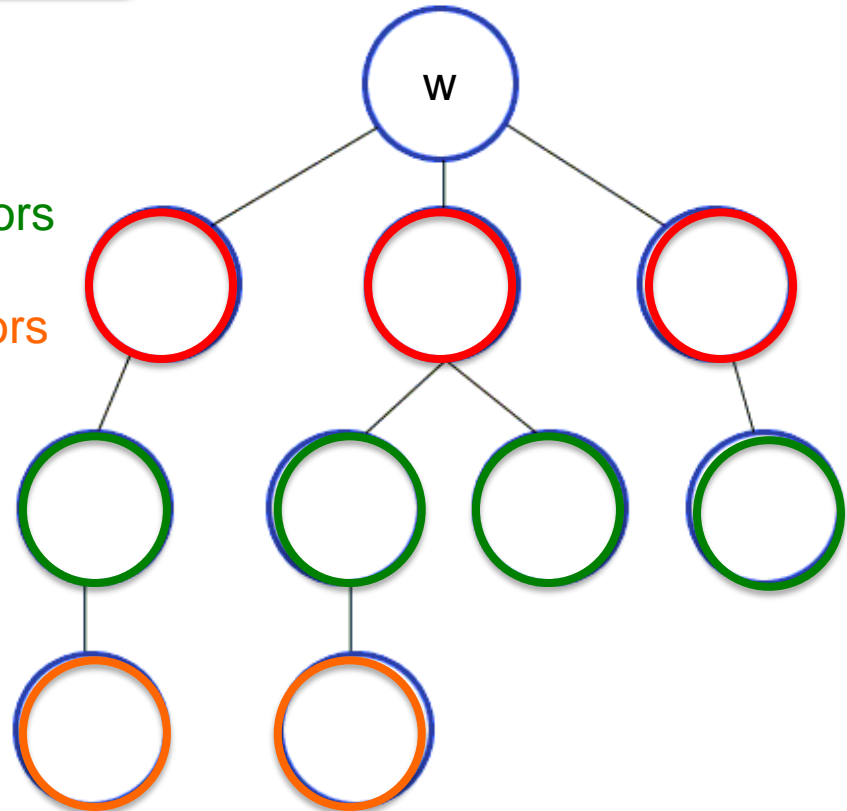
$A(y) :- \text{Edge}('w', y)$

$A(y) :- A(x), \text{Edge}(x, y)$

step 0:  $A_0$  = all nodes connected to 'w'

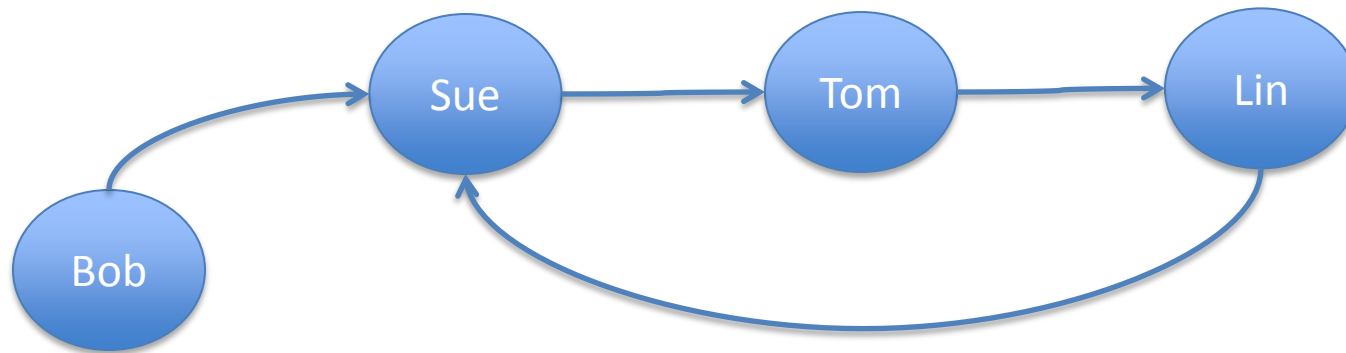
step 1: for each node in  $A_0$ , find neighbors

step 2: for each node in  $A_1$ , find neighbors



# Evaluating Recursive Queries

- Problems with this approach
  - What if there are cycles in the graph?



# Example of Semi-Naïve Evaluation

Reachability from 'a' in datalog

$A(y) :- R('a', y)$ $A(y) :- A(x), R(x, y)$
--

$$\Delta A^0 = R', i = 1$$

while  $\Delta A^{i-1}$  is not empty:

$$A^i = (\Delta A^0 \cup \dots \cup \Delta A^{i-1})$$

$$\Delta A^i = (\Delta A^{i-1} \bowtie R) - A^i$$

$$i = i + 1$$



Join



Dupe-elim

# In MapReduce

