

Data-Flow Analysis

Live-Variable Analysis

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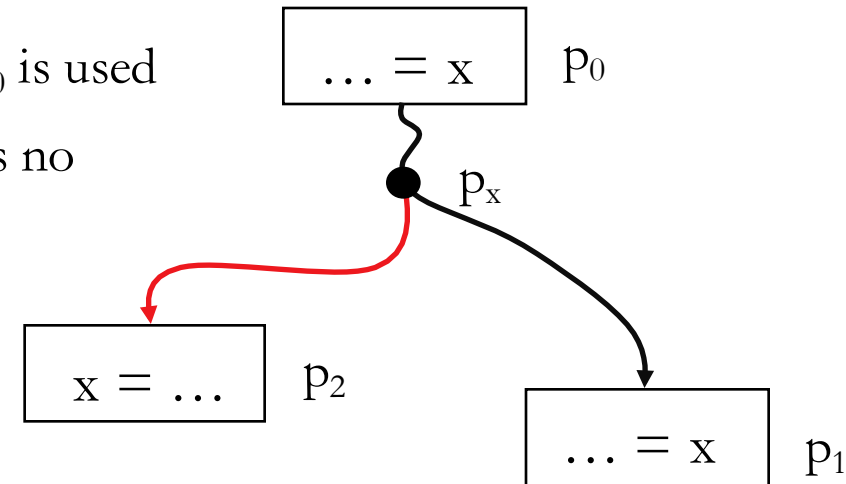
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Live-Variable Analysis

- What is Live-Variable Analysis?
 - For each Variable x where is the last program point p where the a specific value of x is used.
 - In other words, for x and program point p determine if the value of x at p can still be used along some path starting at p .
 - If so, x is live at p
 - If not x is dead at p
 - Must take Control-Flow into account : a Data-Flow Problem !!!
- Applications:
 - Register Allocation: If a variable is dead at a given point p
 - Can reuse its storage, *i.e.*, the register it occupies if any;
 - If its value as been modified must save the value to storage unless it is not live on exit of the procedure or loop

Live-Variable Analysis: Illustration

- At point p_0 the x variable is live:
 - There is a path to p_1 where value at p_0 is used
 - Beyond p_x towards p_2 the value of x is no longer needed and is dead



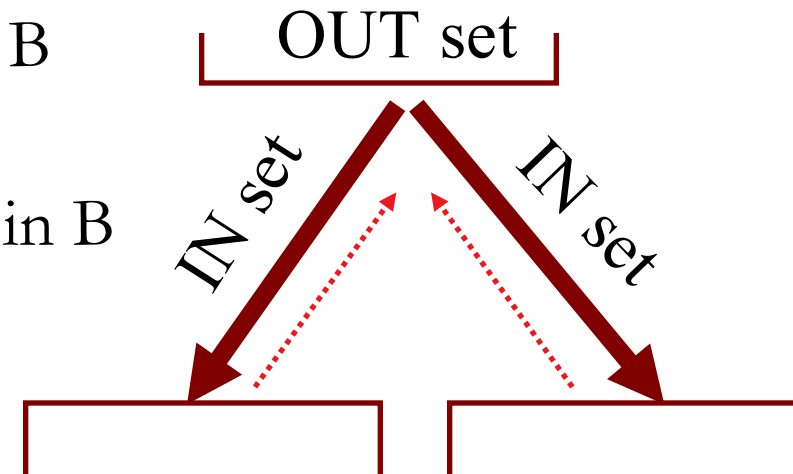
- Need to observe for each variable and for each program point:
 - Where is the last program point beyond which the value is not used
 - Trace back from uses to definitions and observe the first definition (backwards) that reaches that use.
 - That definition kills all uses backwards of it.

Data-Flow Analysis Formulation

- Variable is *live* at a point p if its value is used along *at least one Path*
 - A use of x prior to any definition in basic block means x must be alive
 - A definition of x in B prior to any subsequent use means previous uses must be dead
- Gen Set: Set of Variables Used in B
 - Upward Exposed Reads of B
- Kill Set: Set of Variables Defined in B

$$OUT(B) = \bigcup_{S \text{ a successor of } B} IN(S)$$

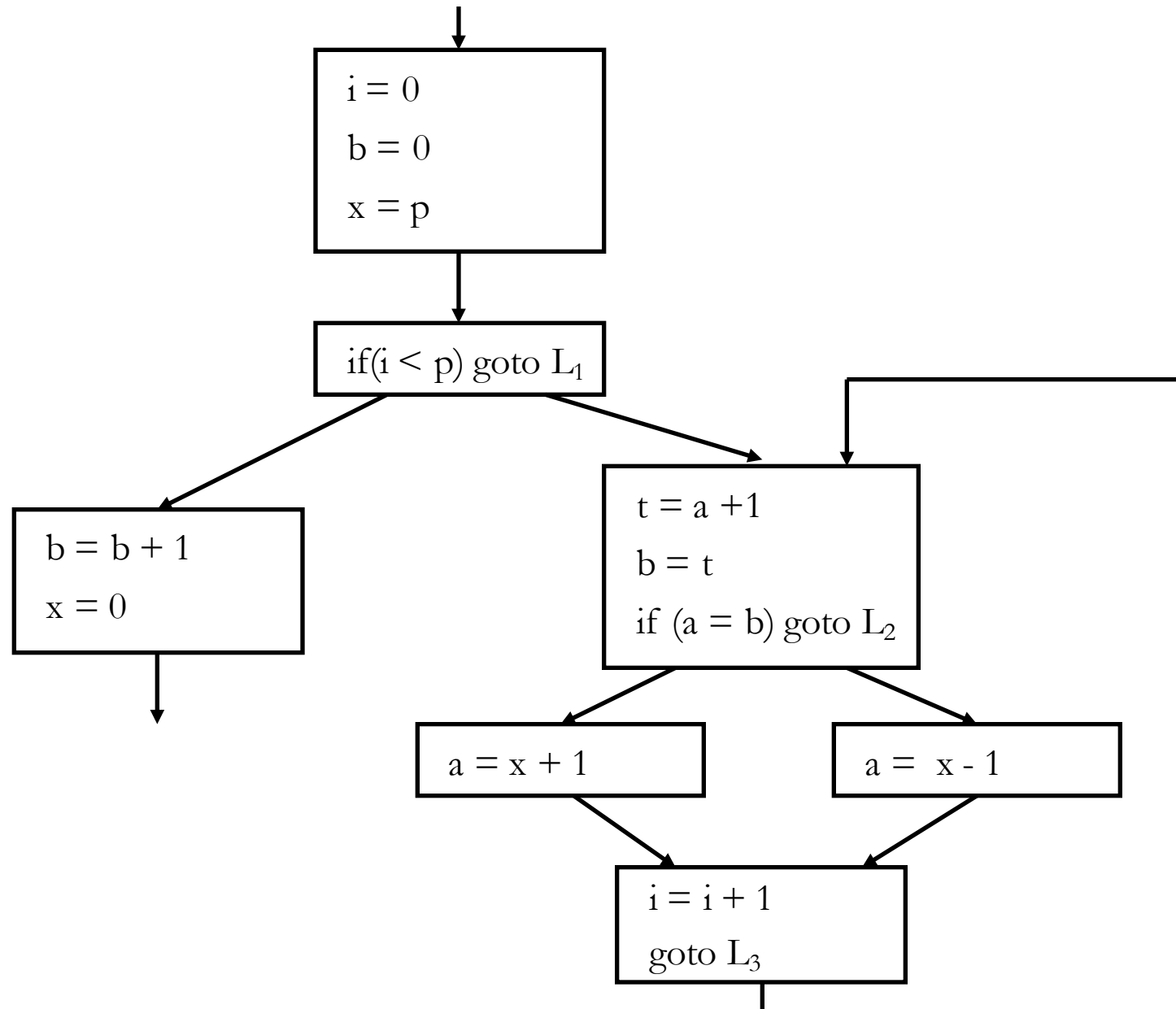
$$IN(B) = Use(B) \cup (OUT(B) - Def(B))$$



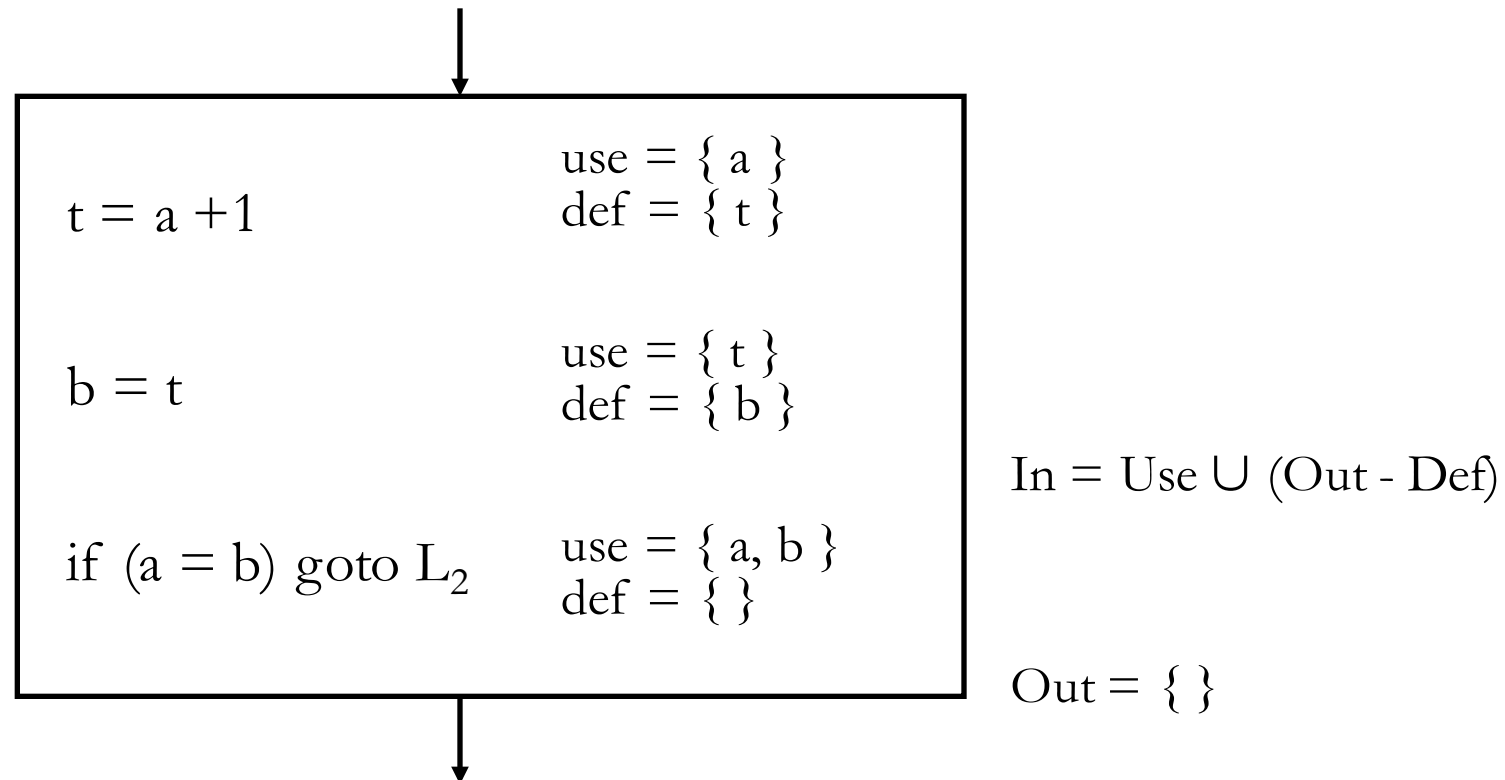
Data-Flow Analysis Formulation

- Initialize $IN(B)$ to Empty Set
- Compute Gen/Use and Kill/Def for each Basic Block
 - Tracing backwards from end of block to beginning of block
 - Initialize Last Instruction's $Out(i)$ to Empty
 - Use $IN(i) = use(i) \cup (OUT(i) - def(i))$
- Iteratively Apply Relations to Basic Block Until Convergence
 - $OUT(B) = \bigcup_{s \text{ a successor of } B} IN(s)$
 - $IN(B) = Use(B) \cup (OUT(B) - Def(B))$
- Given $OUT(B)$ use relations at instruction level to determine the live variables after each instruction

Example

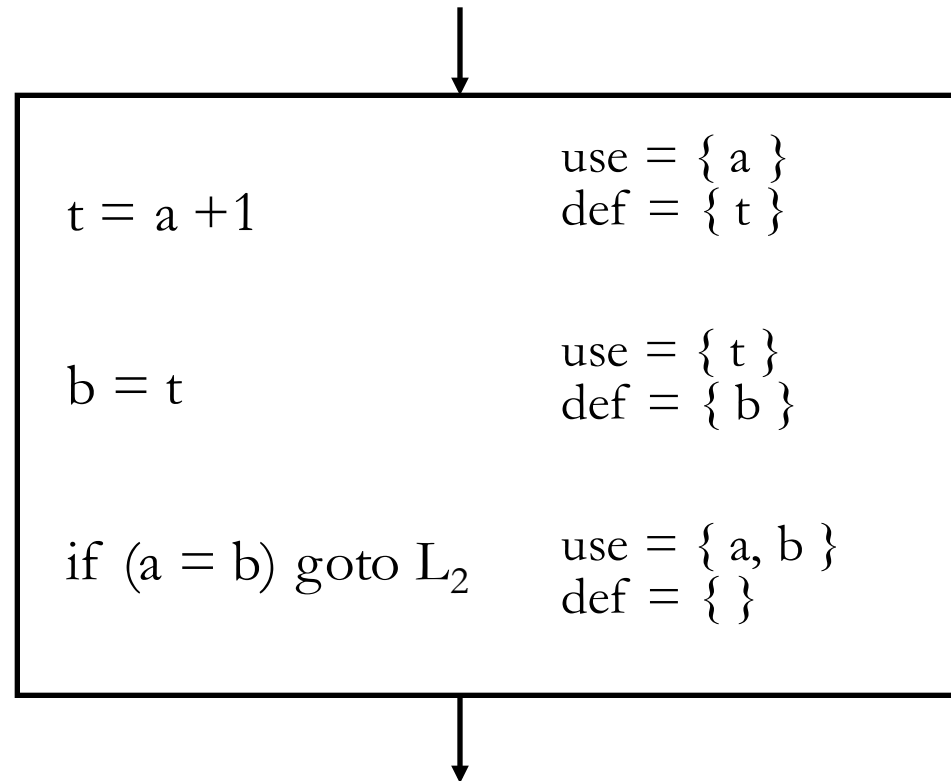


Use & Def Functions for a Basic Block



$$In(i) = Use(i) \cup (Out(i) - Def(i))$$

Use & Def Functions for a Basic Block

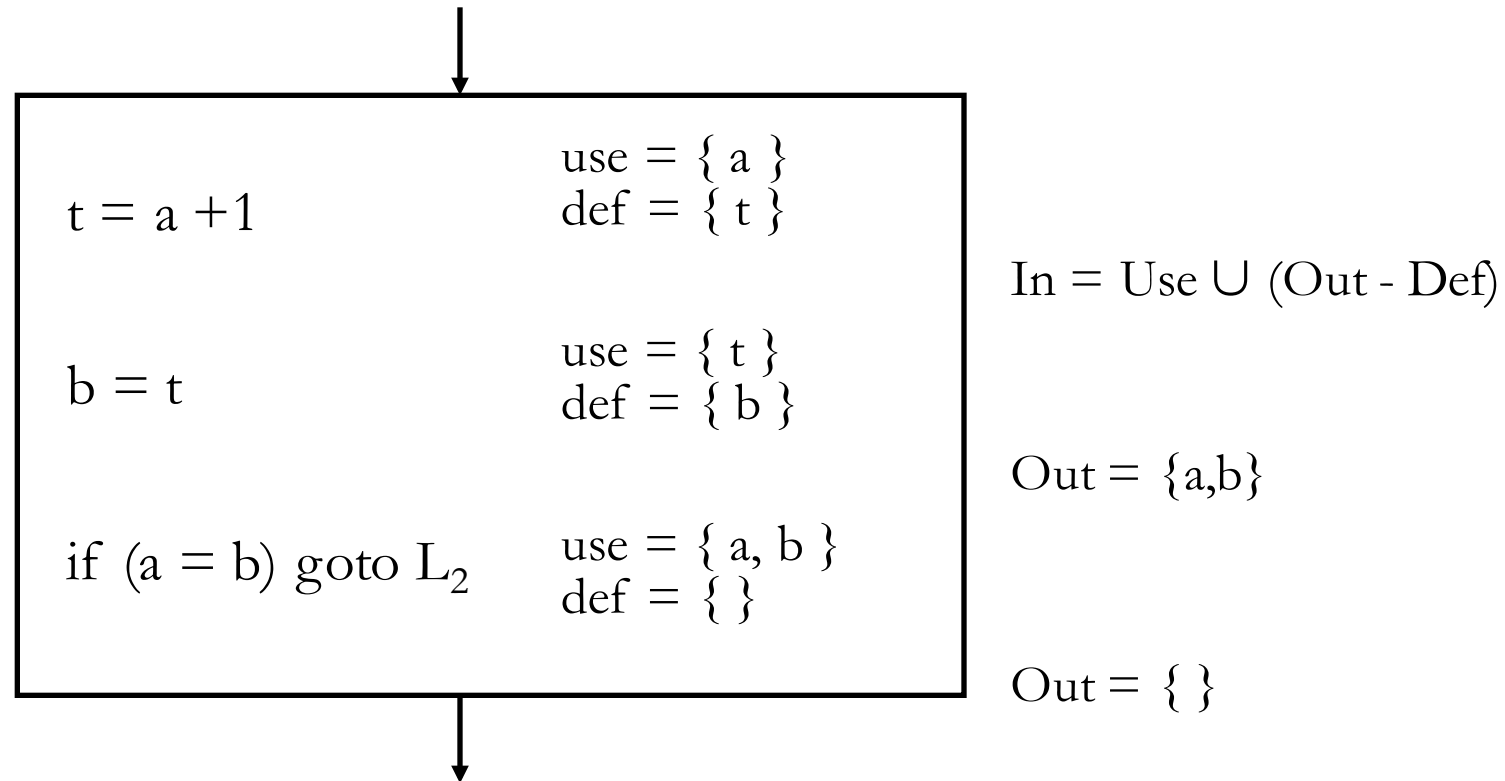


$$In = \{a,b\} \cup (\{\} - \{\}) = \{a,b\}$$

$$Out = \{ \}$$

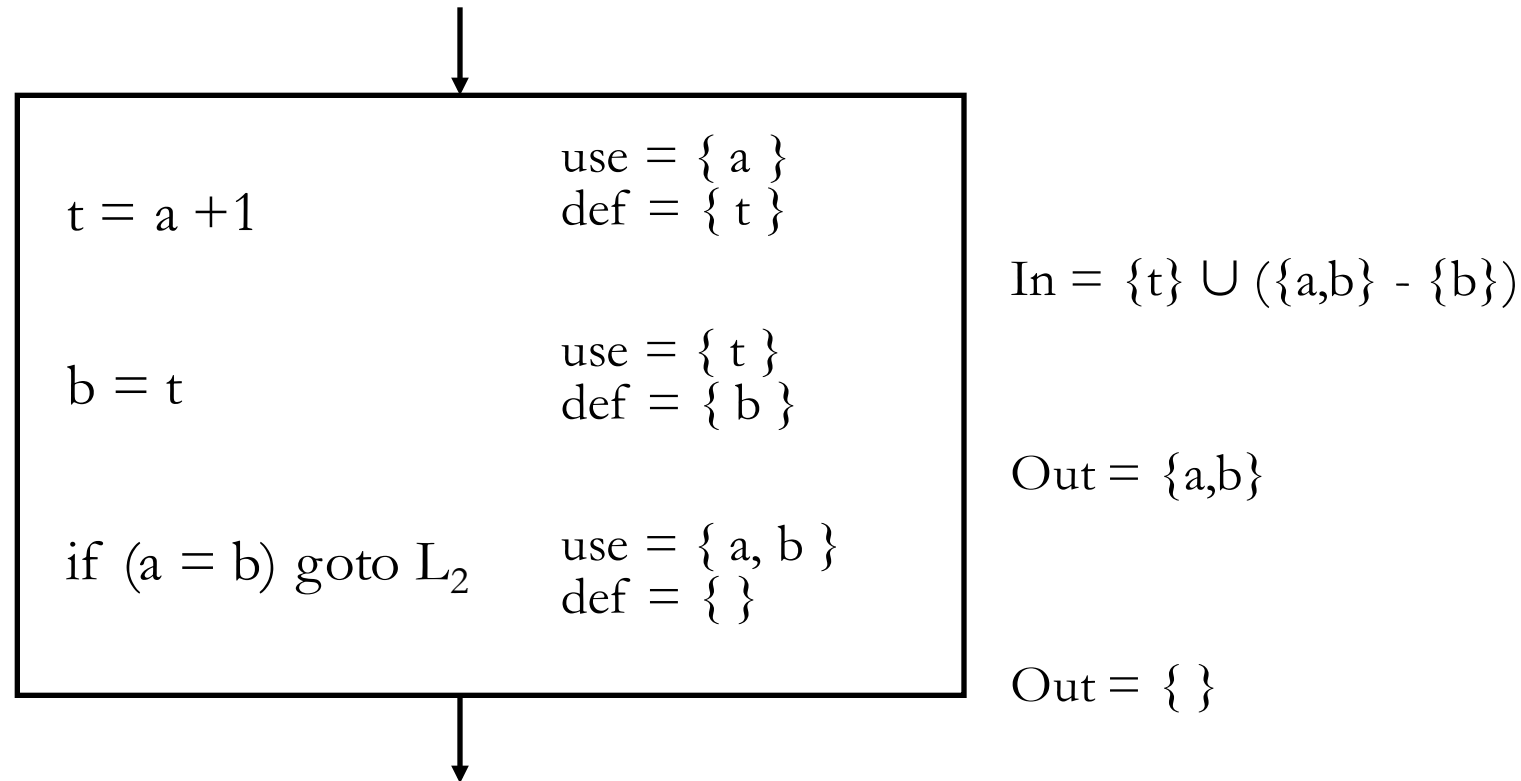
$$In(i) = Use(i) \cup (Out(i) - Def(i))$$

Use & Def Functions for a Basic Block



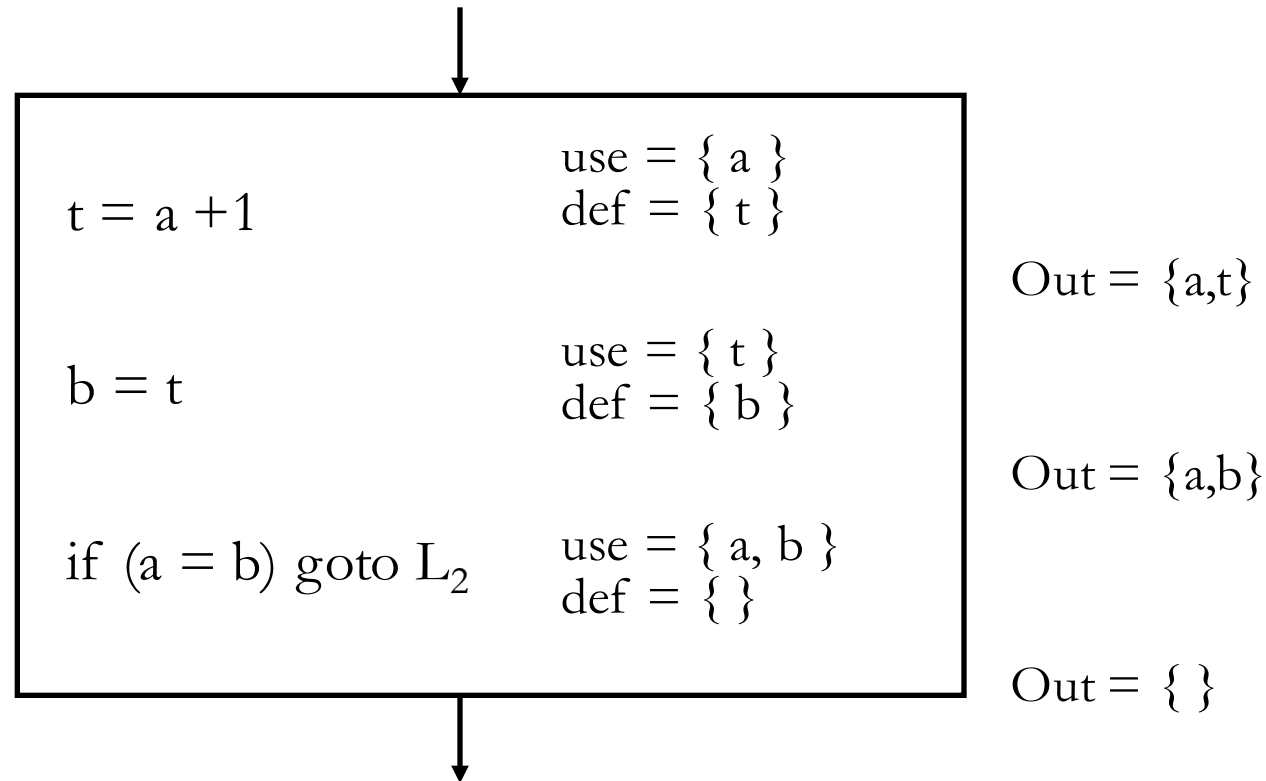
$$\text{In}(i) = \text{Use}(i) \cup (\text{Out}(i) - \text{Def}(i))$$

Use & Def Functions for a Basic Block



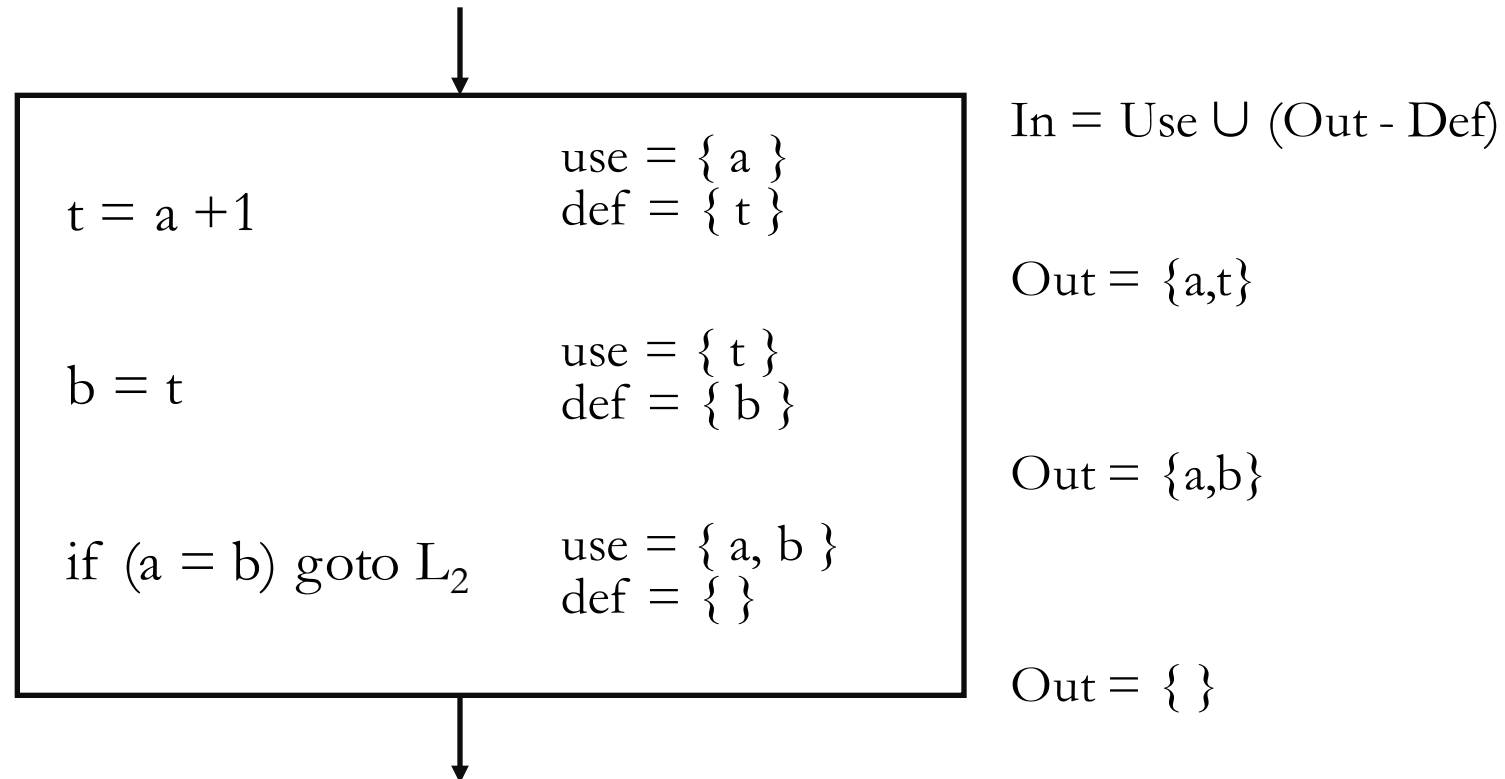
$$\text{In}(i) = \text{Use}(i) \cup (\text{Out}(i) - \text{Def}(i))$$

Use & Def Functions for a Basic Block



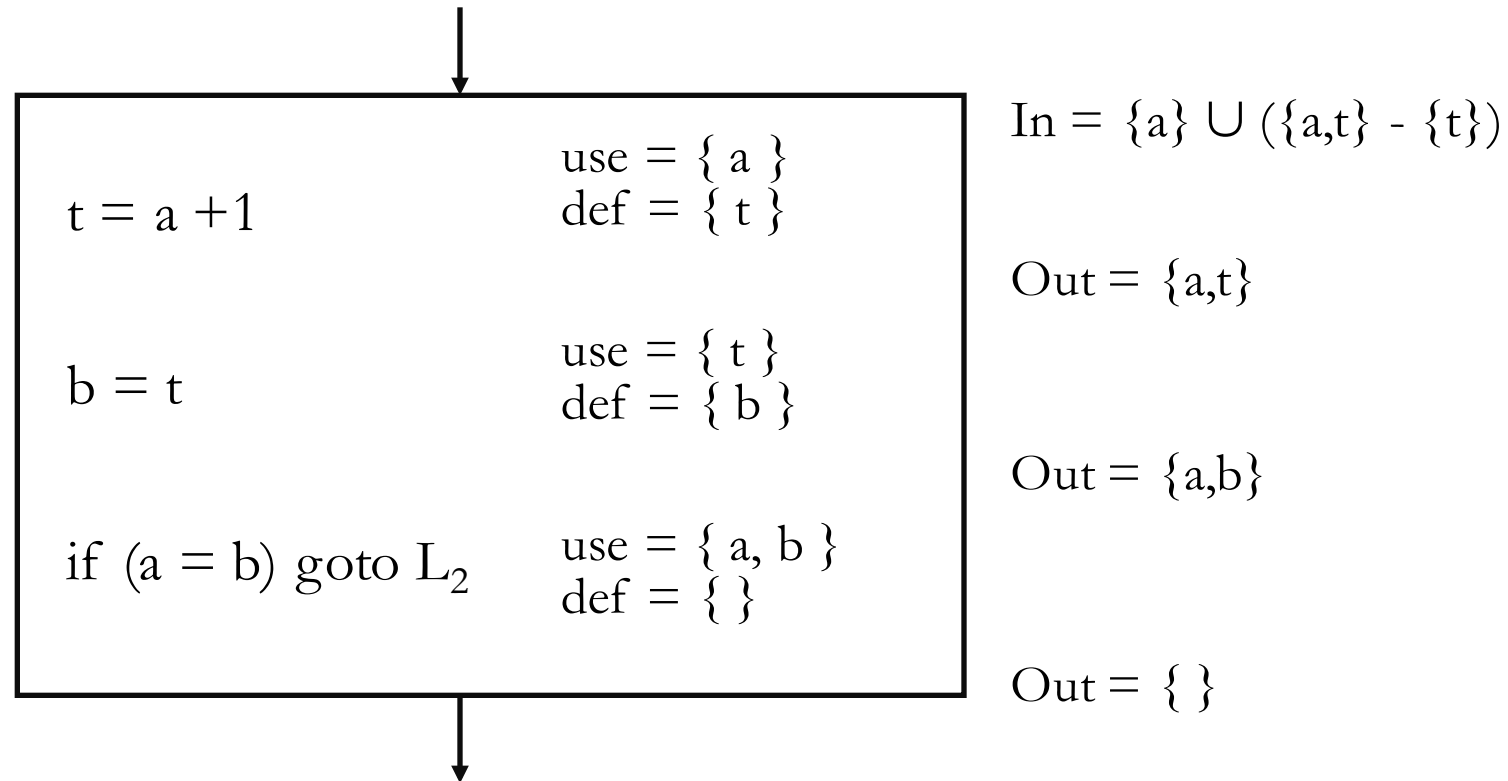
$$\text{In}(i) = \text{Use}(i) \cup (\text{Out}(i) - \text{Def}(i))$$

Use & Def Functions for a Basic Block



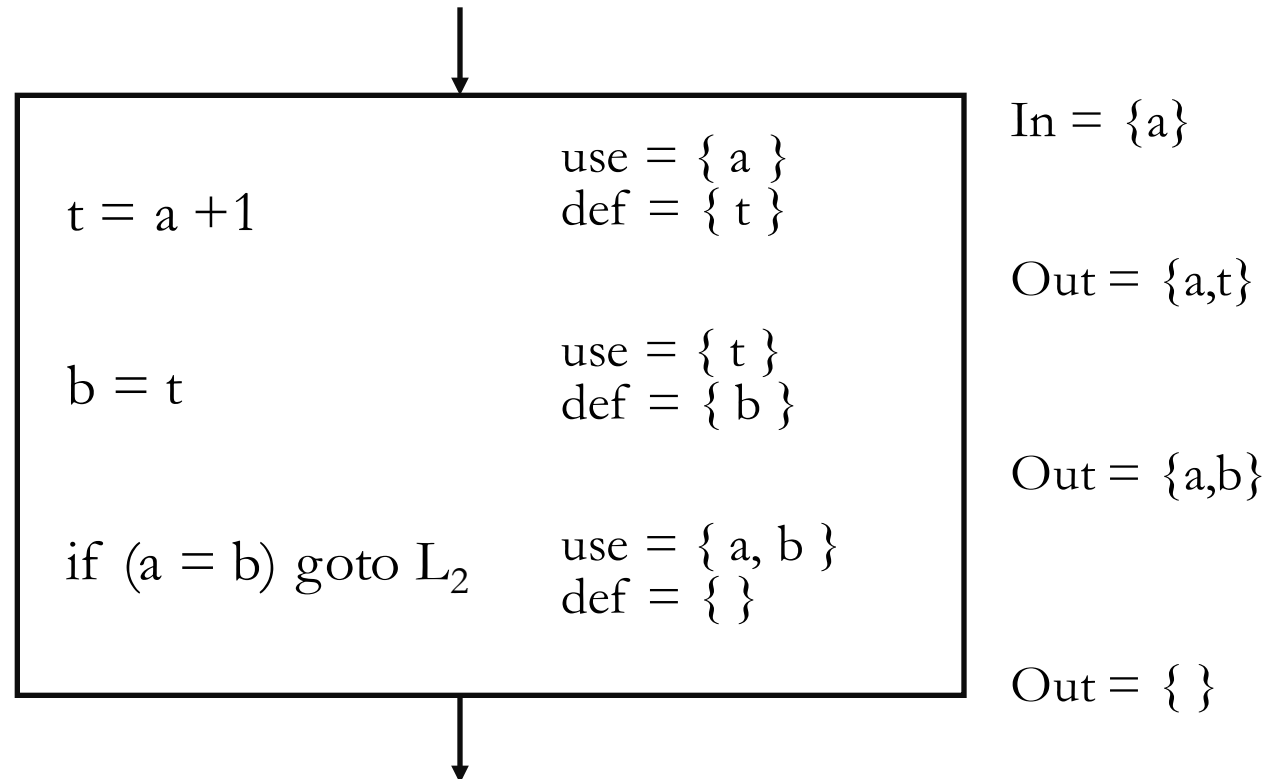
$$In(i) = Use(i) \cup (Out(i) - Def(i))$$

Use & Def Functions for a Basic Block



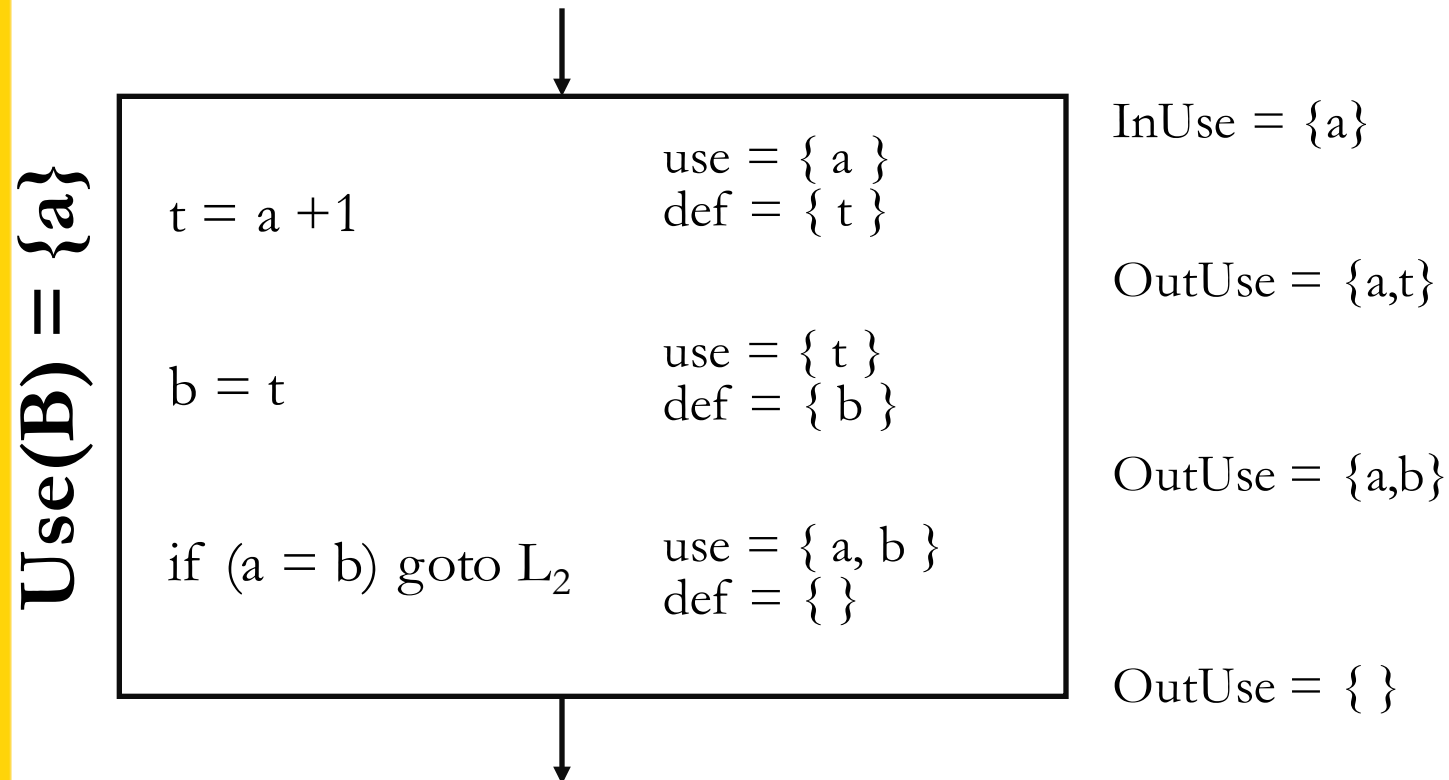
$$\text{In}(i) = \text{Use}(i) \cup (\text{Out}(i) - \text{Def}(i))$$

Use & Def Functions for a Basic Block



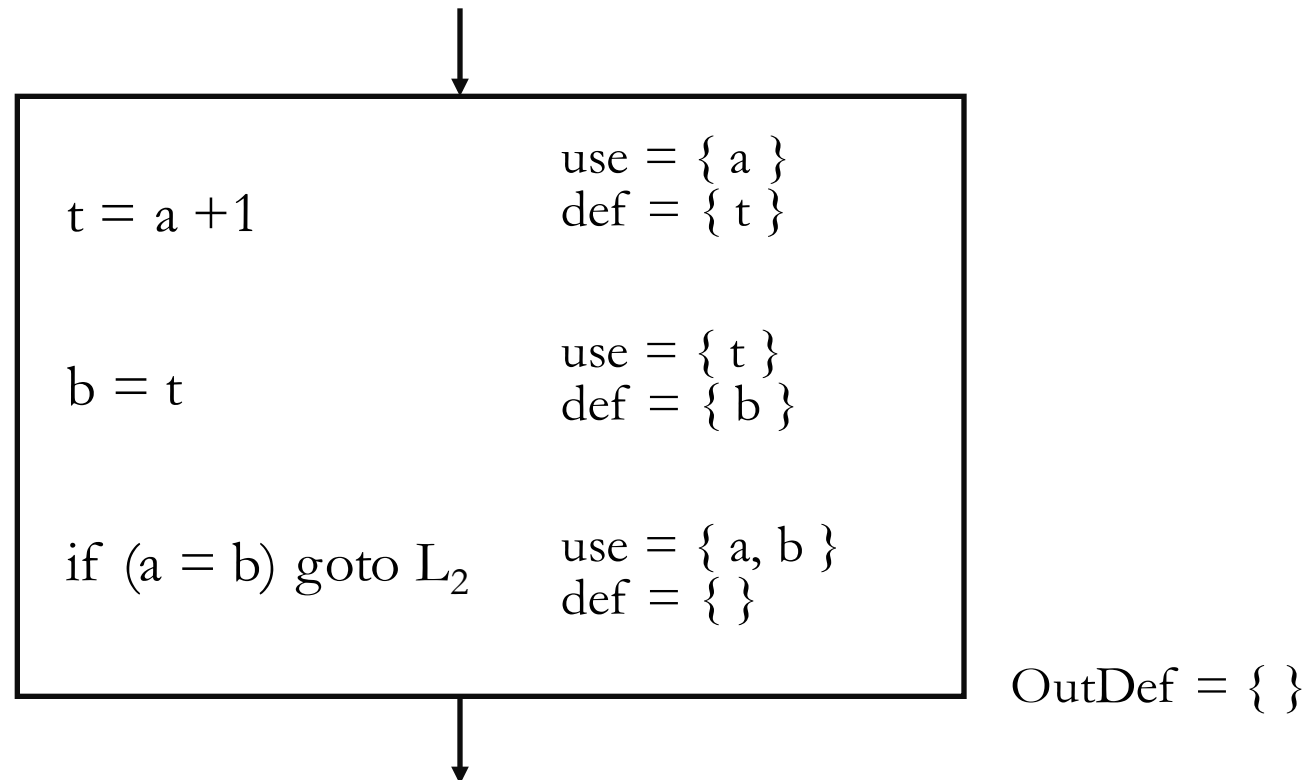
$$\text{In}(i) = \text{Use}(i) \cup (\text{Out}(i) - \text{Def}(i))$$

Use & Def Functions for a Basic Block



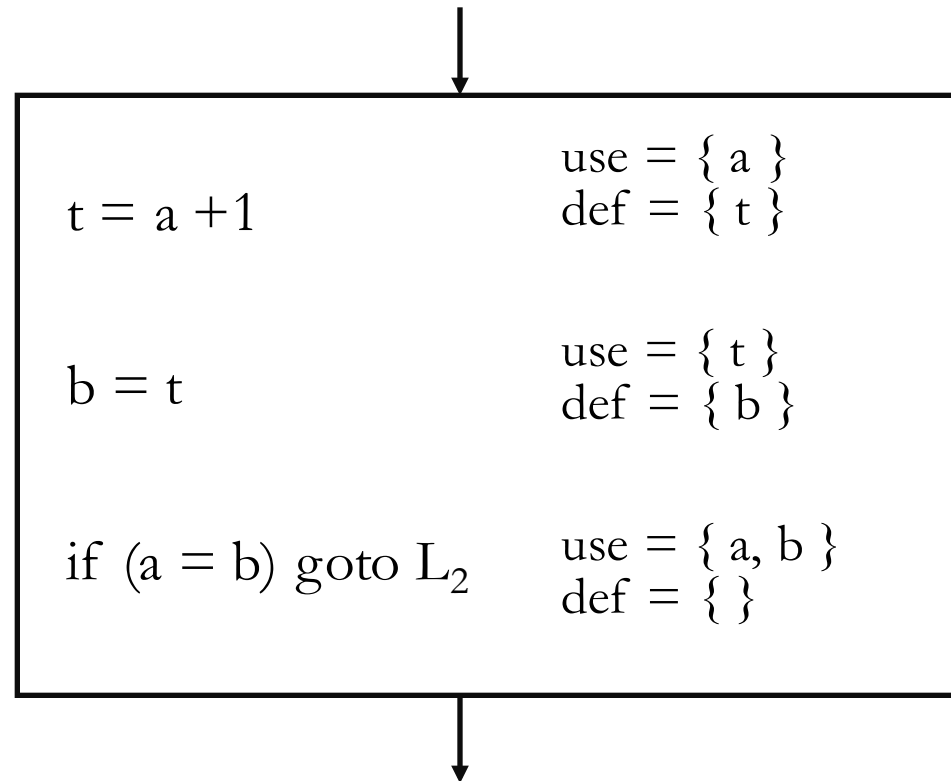
$$InUse(i) = Use(i) \cup (OutUse(i) - Def(i))$$

Use & Def Functions for a Basic Block



$$InDef(i) = Def(i) \cup OutDef(i)$$

Use & Def Functions for a Basic Block

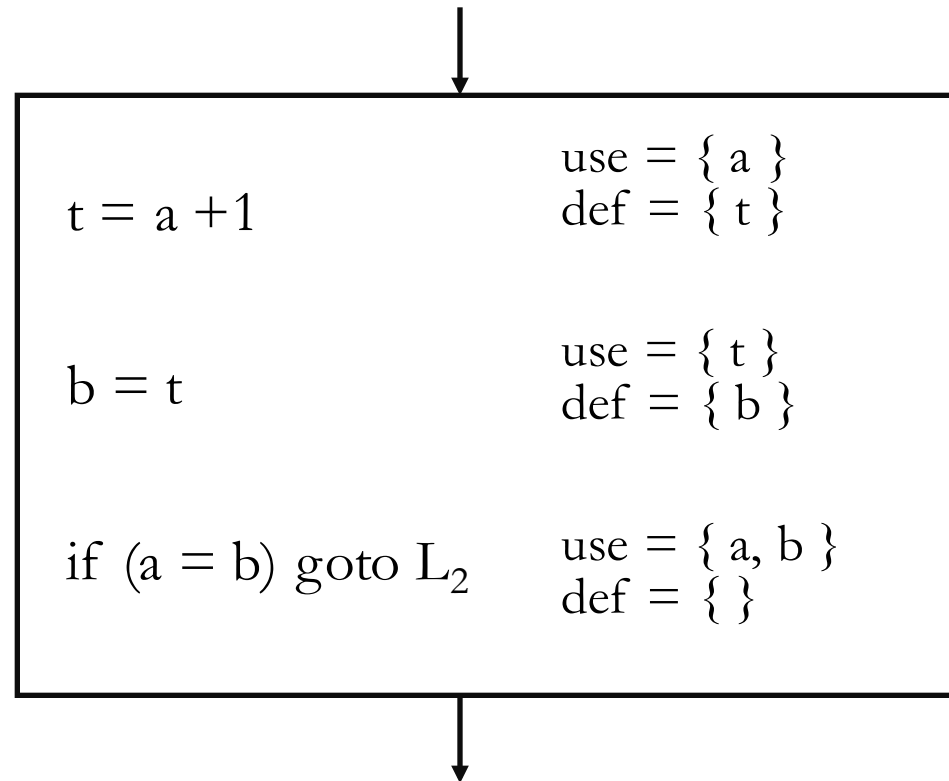


$$InDef = Def \cup OutDef = \{ \}$$

$$OutDef = \{ \}$$

$$InDef(i) = Def(i) \cup OutDef(i)$$

Use & Def Functions for a Basic Block



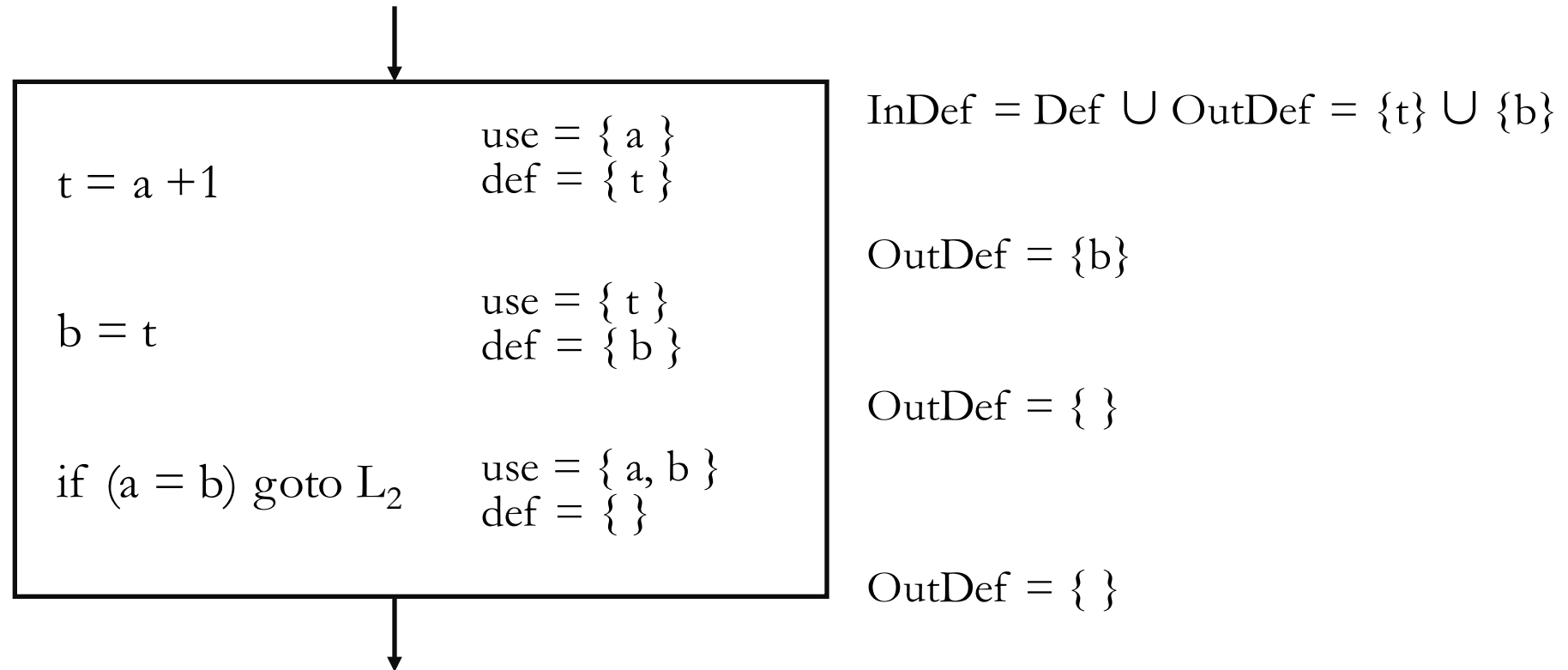
$$InDef = Def \cup OutDef = \{ b \}$$

$$OutDef = \{ \}$$

$$OutDef = \{ \}$$

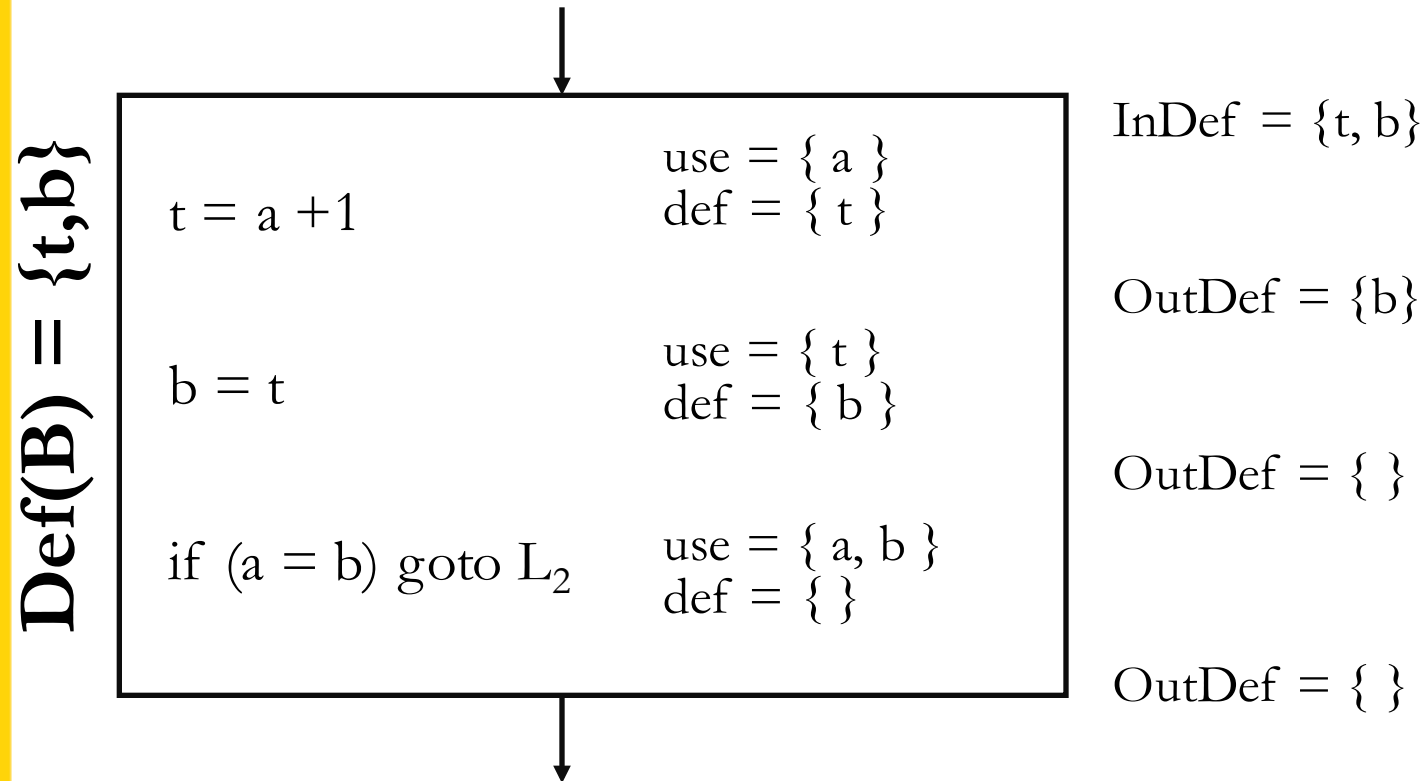
$$InDef(i) = Def(i) \cup OutDef(i)$$

Use & Def Functions for a Basic Block



$$\text{InDef}(i) = \text{Def}(i) \cup \text{OutDef}(i)$$

Use & Def Functions for a Basic Block



$$\text{InDef}(i) = \text{Def}(i) \cup \text{OutDef}(i)$$

Use & Def Functions for a Basic Block

- Can be Accomplished by a Forward Scanning of the Block
 - Keep Track of Which Variables are Read before they are written thus computing the Upwards Exposed Reads (UpExp) or Use Function
 - Track Variables that are Written or Killed (VarKill) or Def Function

// Assume instruction in format “ $x \leftarrow y \text{ op } z$ ”

for $i \leftarrow 1$ to Num Instructions in B do

if (instr(i) is leader of B) then

$b \leftarrow \text{Number}(B);$

$\text{UpExp}(b) \leftarrow \emptyset;$

$\text{VarKill}(b) \leftarrow \emptyset;$

if $y \notin \text{VarKill}(b)$ then

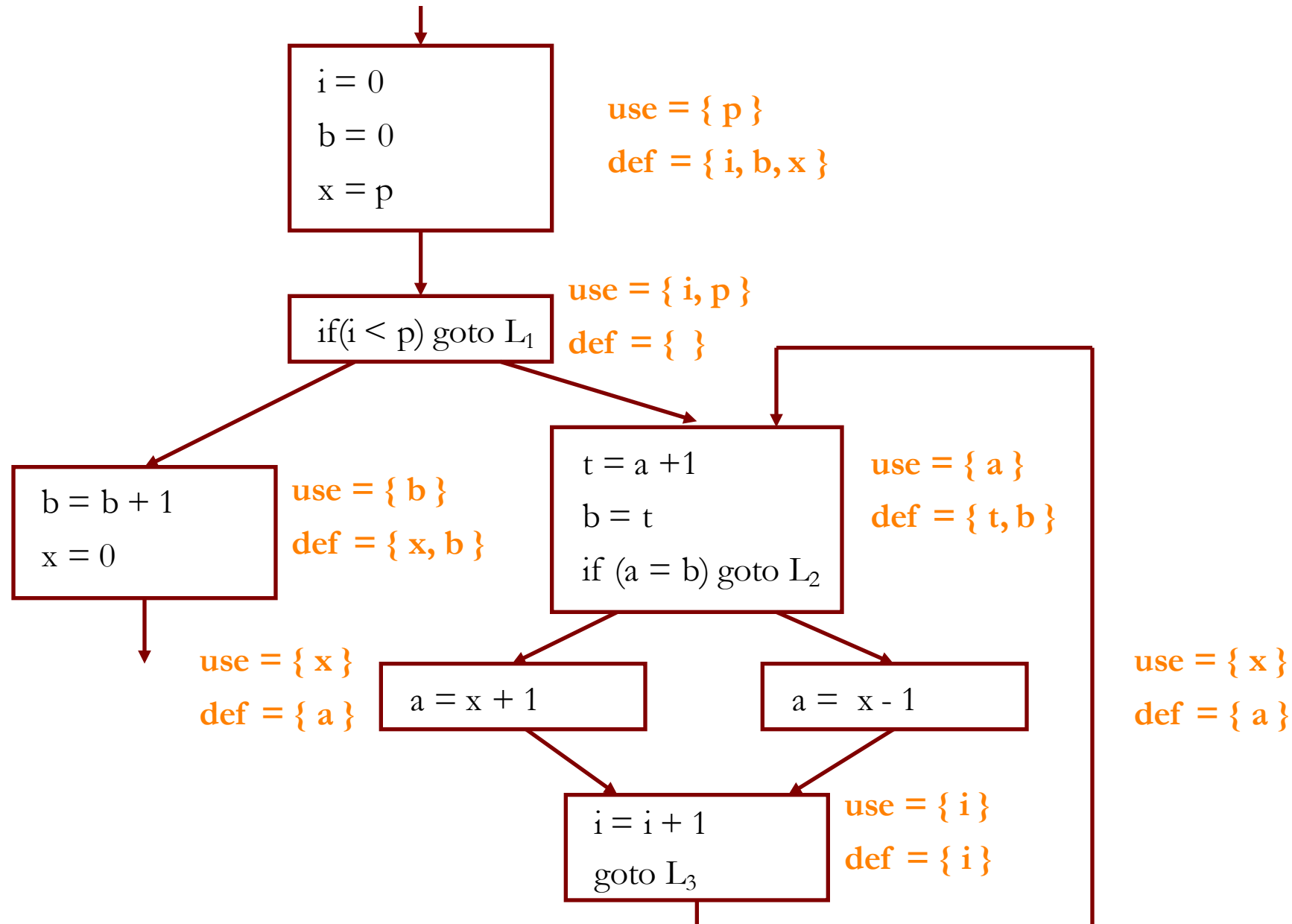
$\text{UpExp}(b) \leftarrow \text{UpExp}(b) \cup \{y\}$

if $z \notin \text{VarKill}(b)$ then

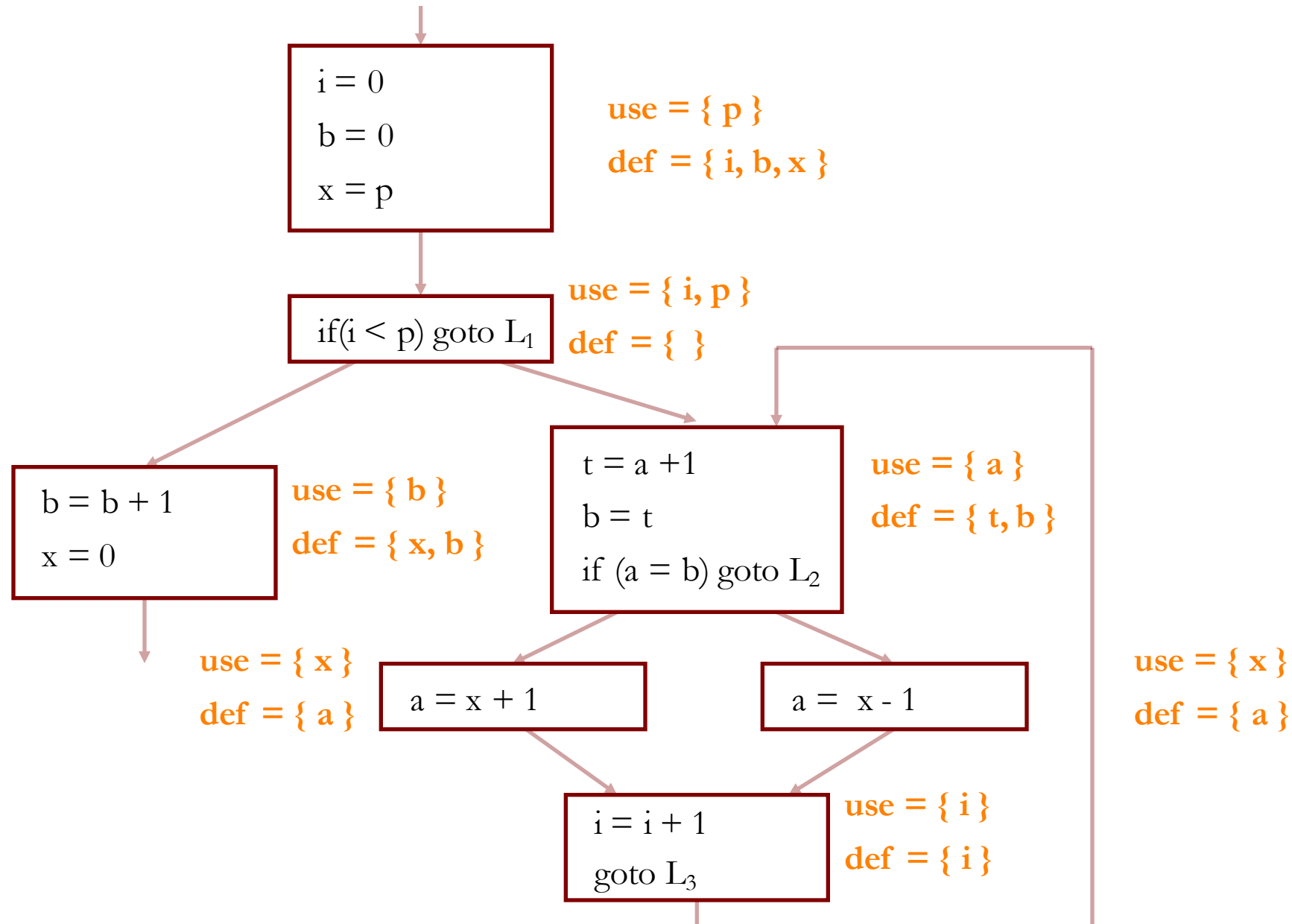
$\text{UpExp}(b) \leftarrow \text{UpExp}(b) \cup \{z\}$

$\text{VarKill}(b) \leftarrow \text{VarKill}(b) \cup \{x\}$

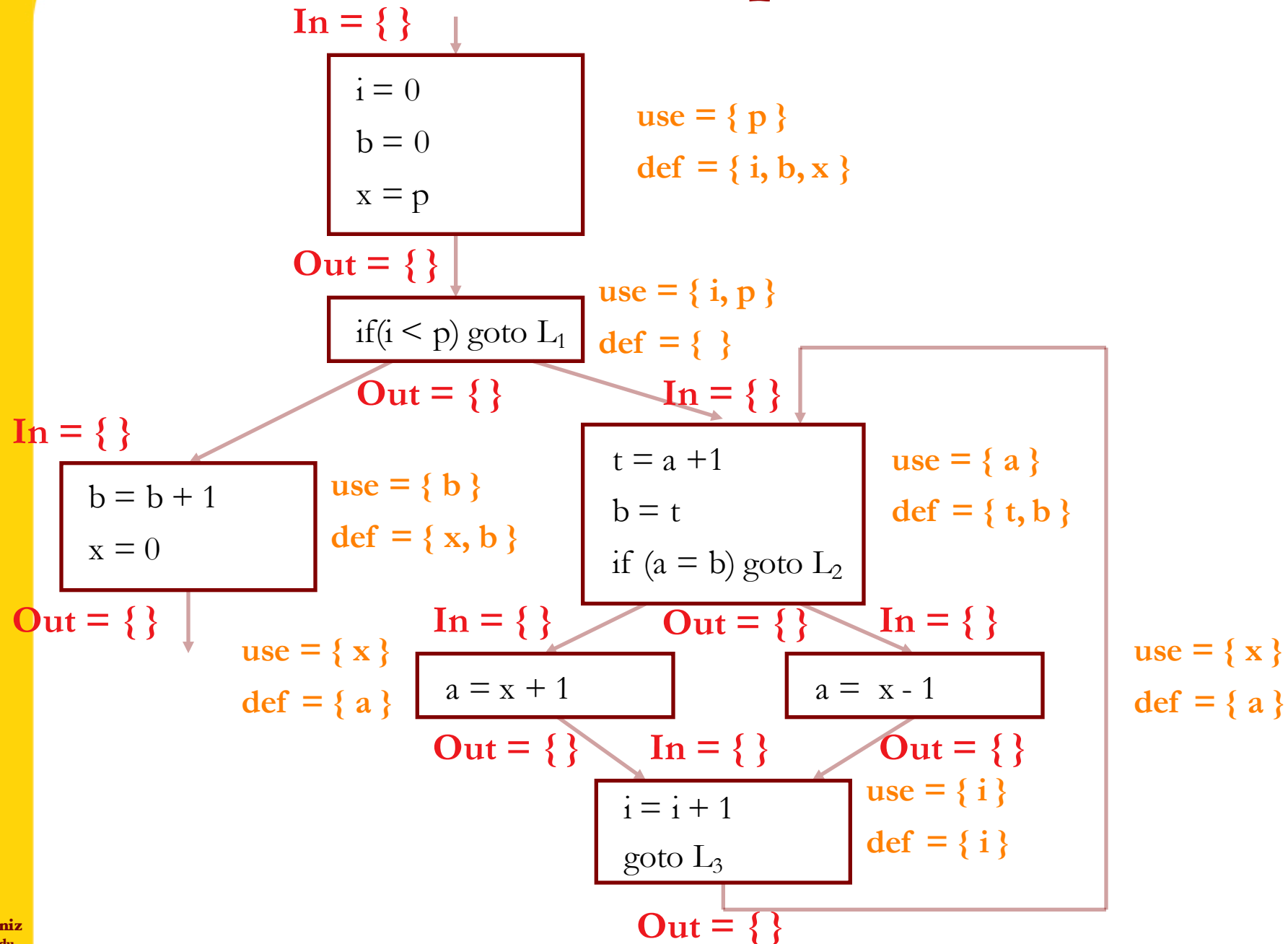
Example



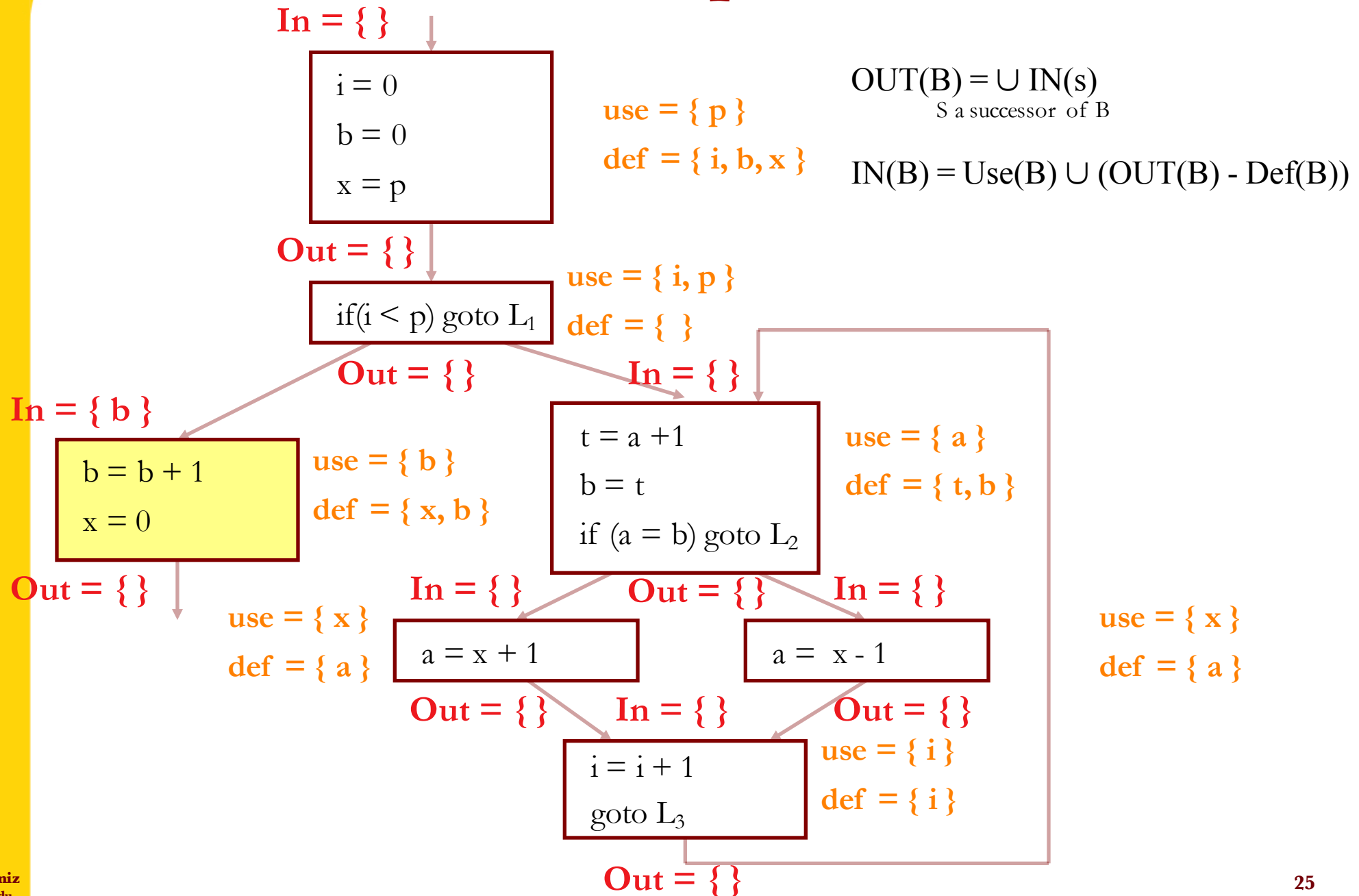
Example



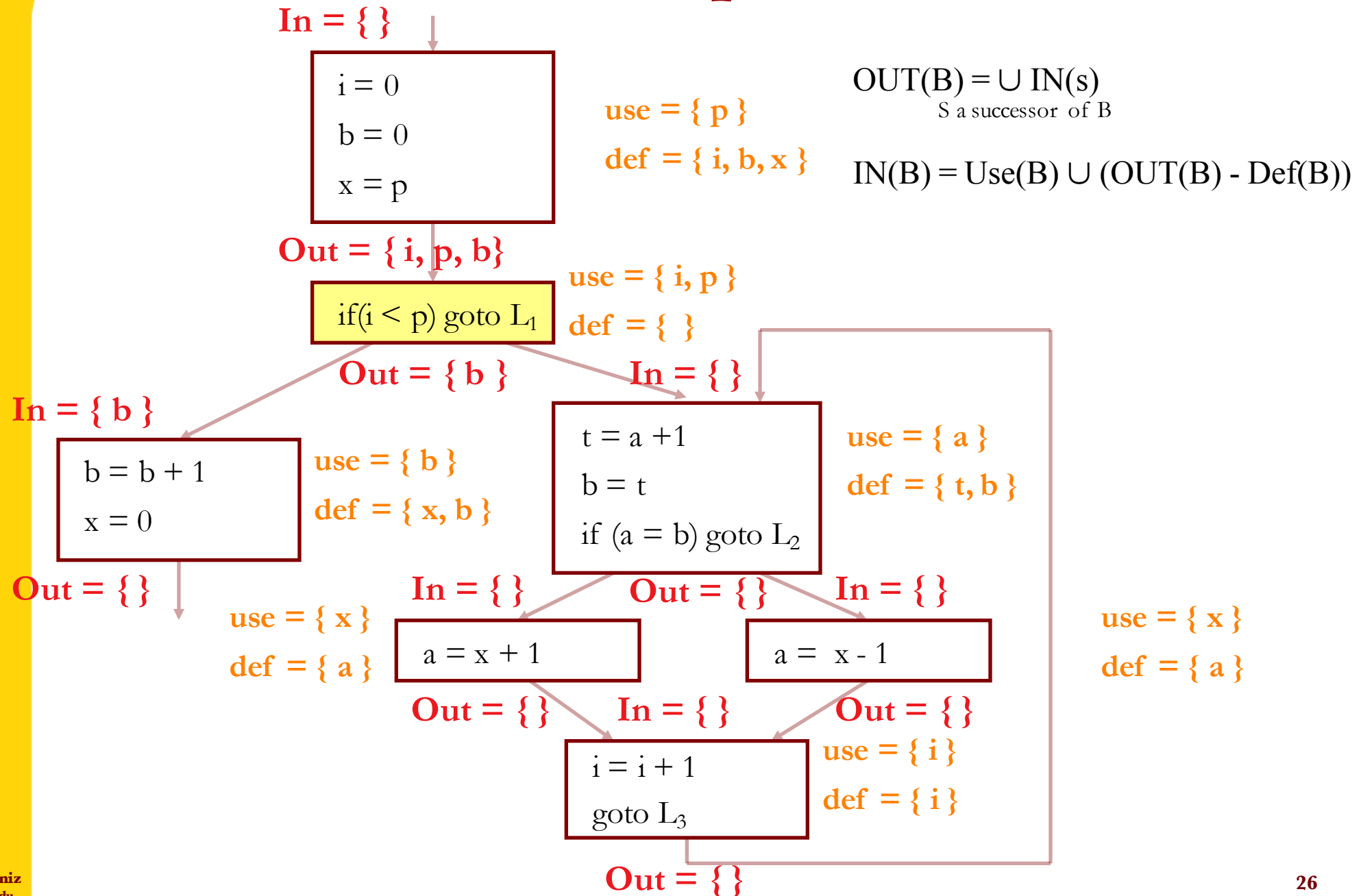
Example



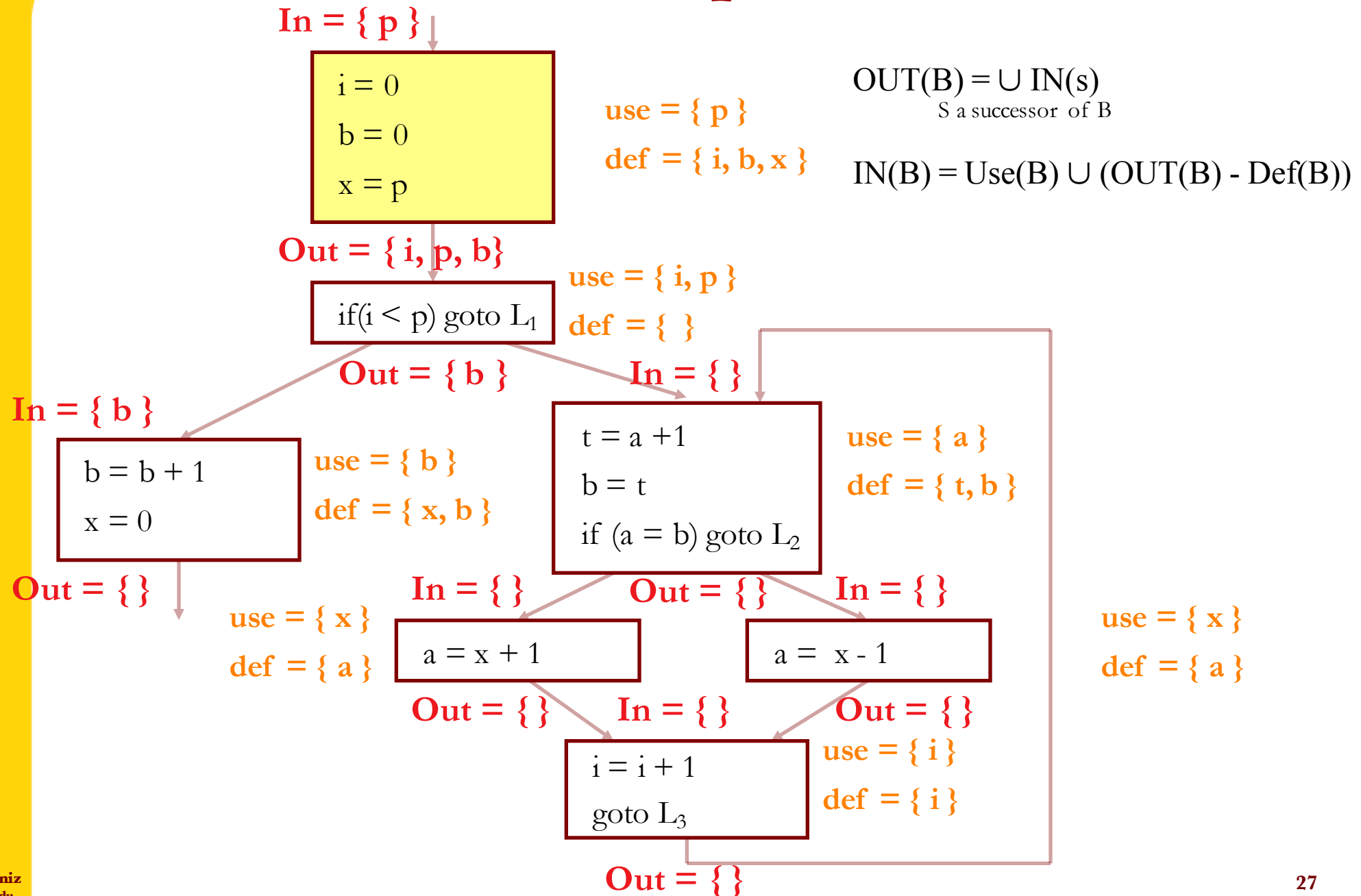
Example



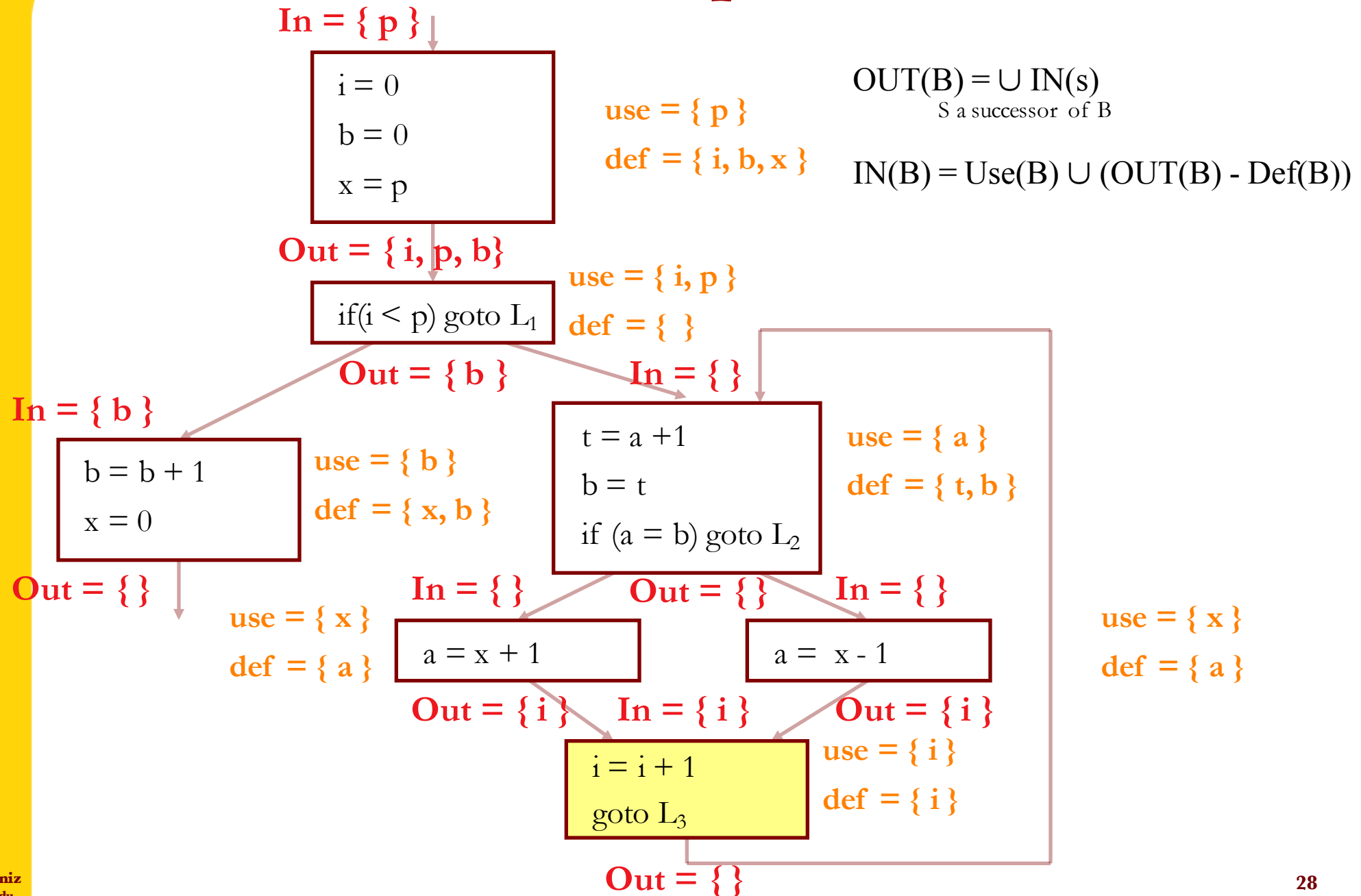
Example



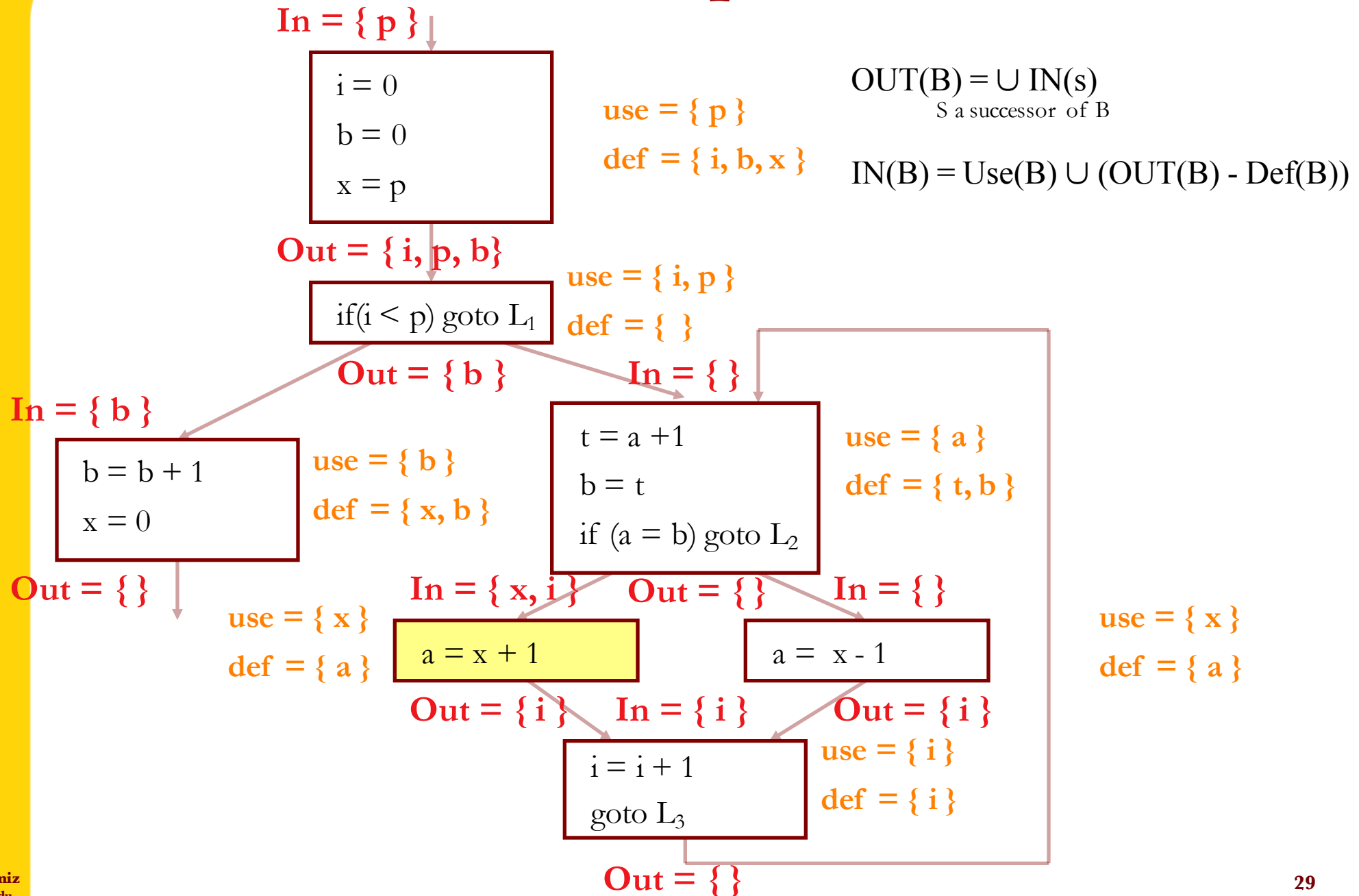
Example



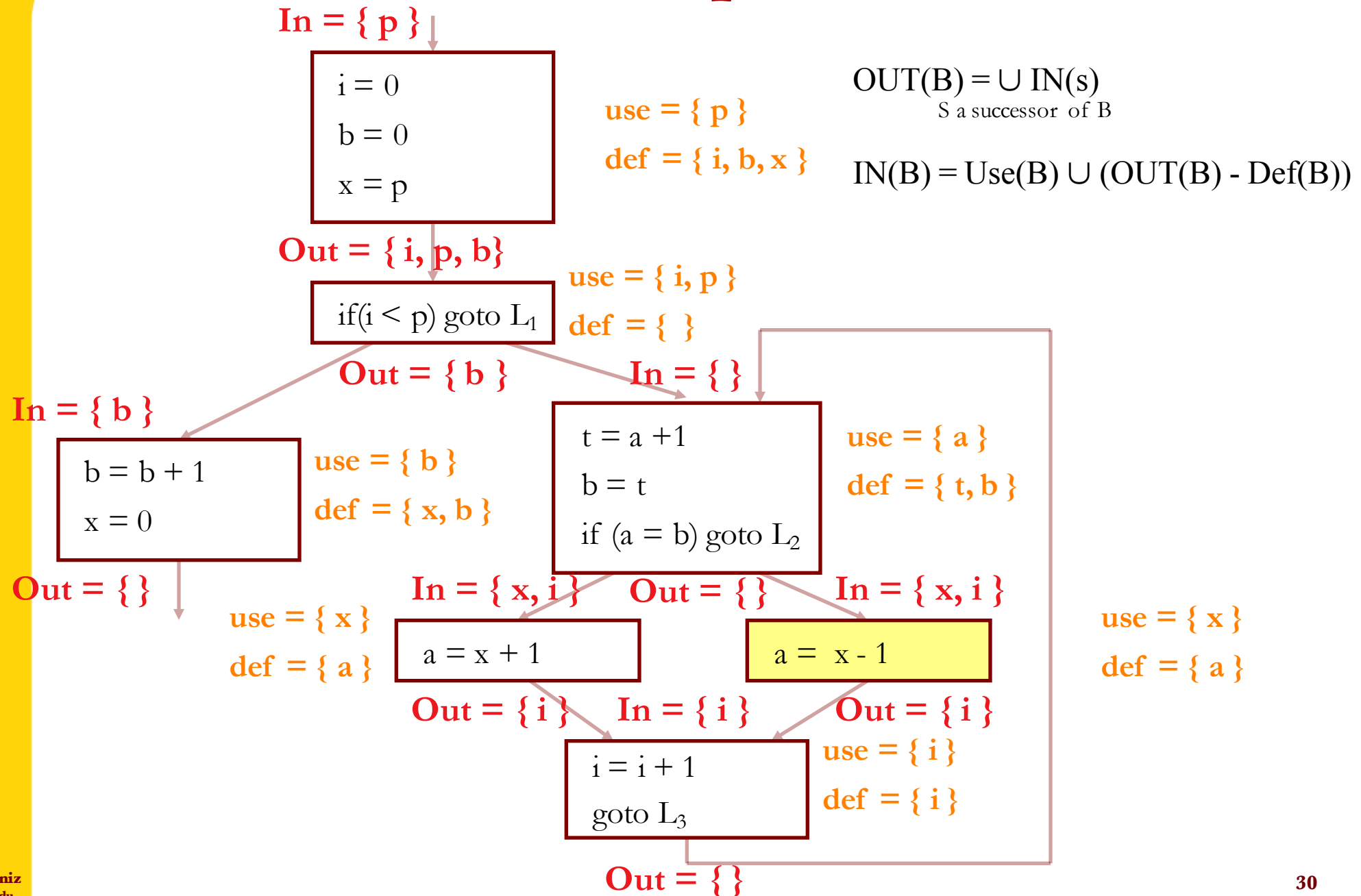
Example



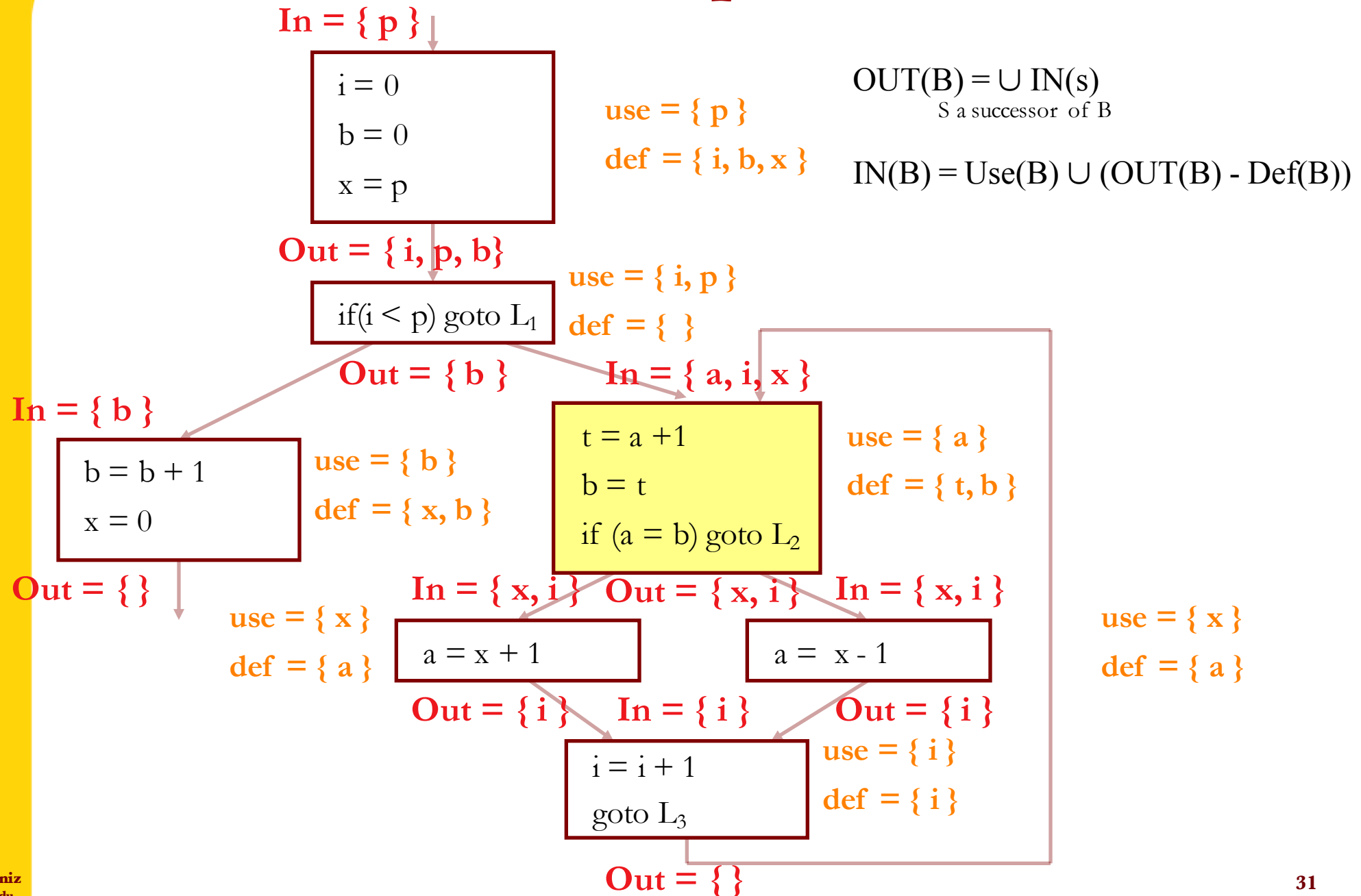
Example



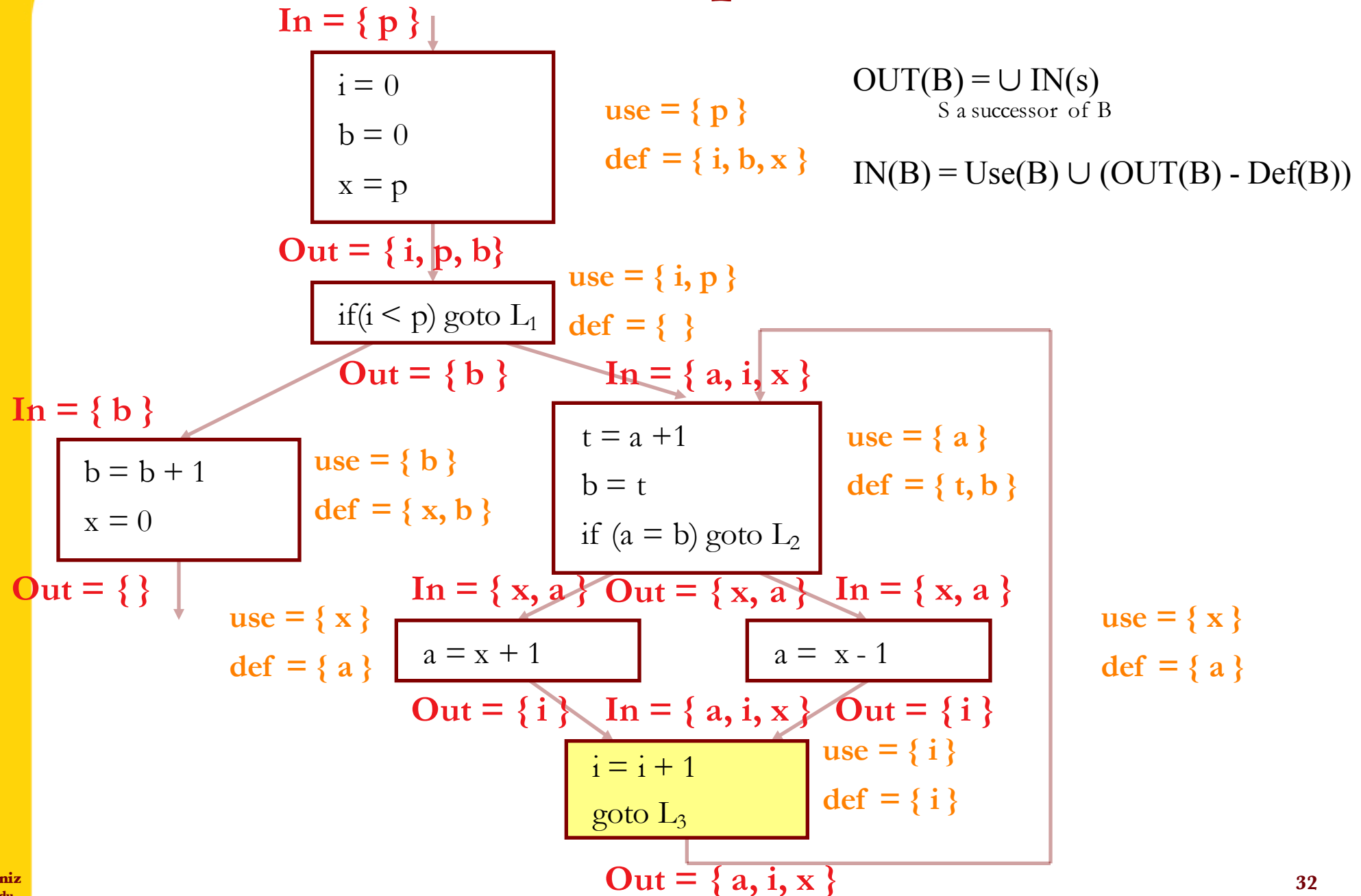
Example



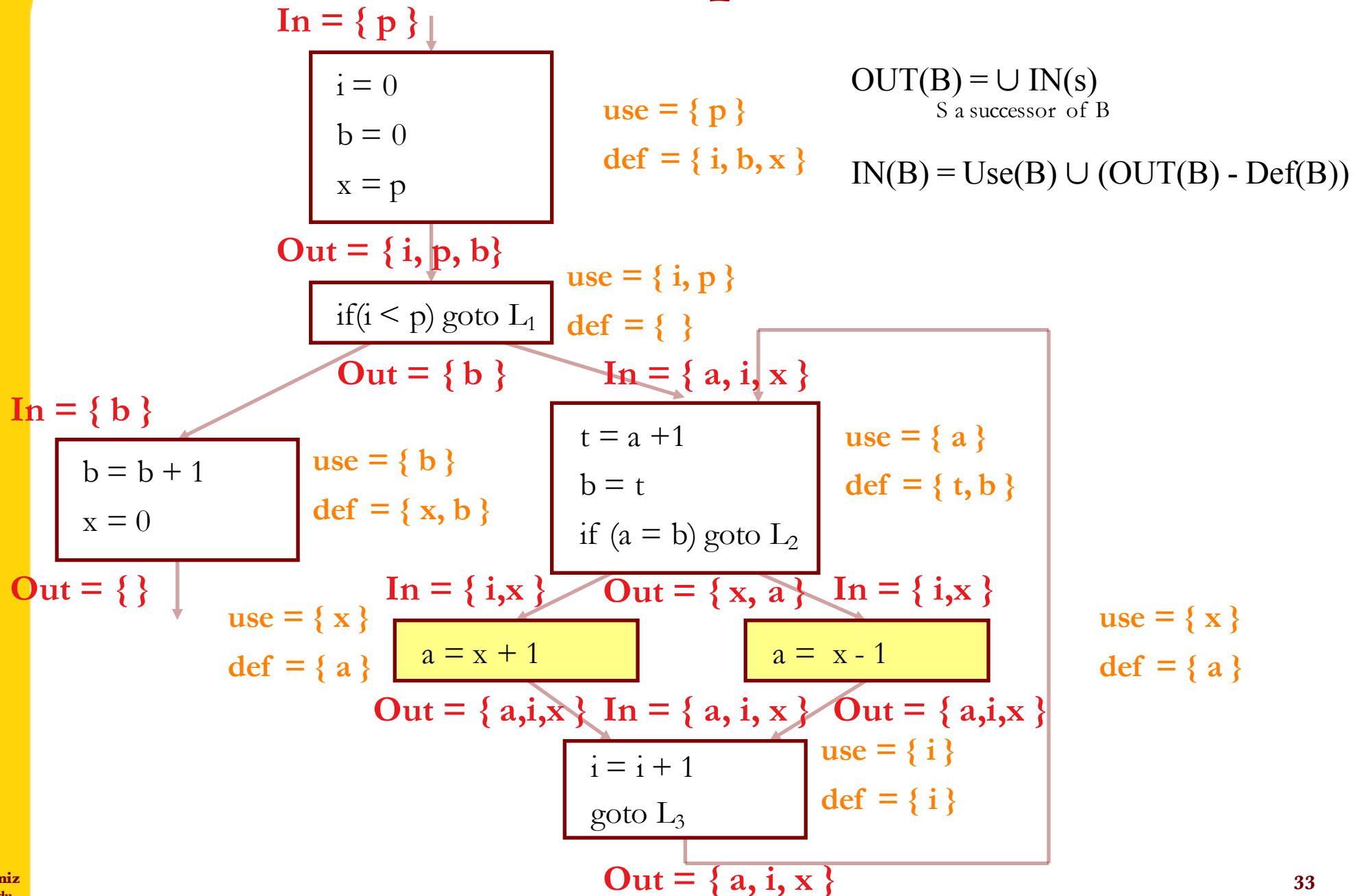
Example



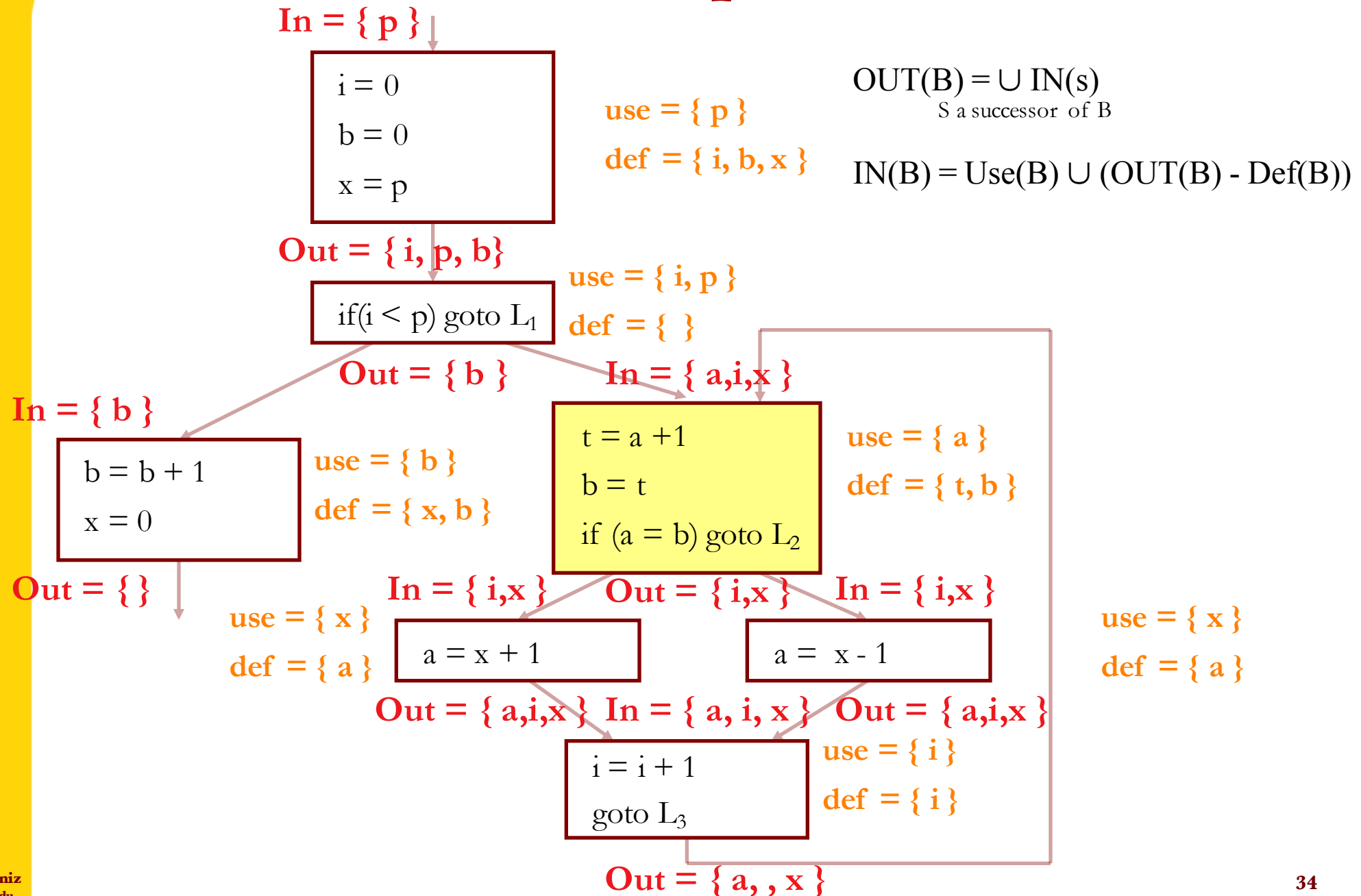
Example



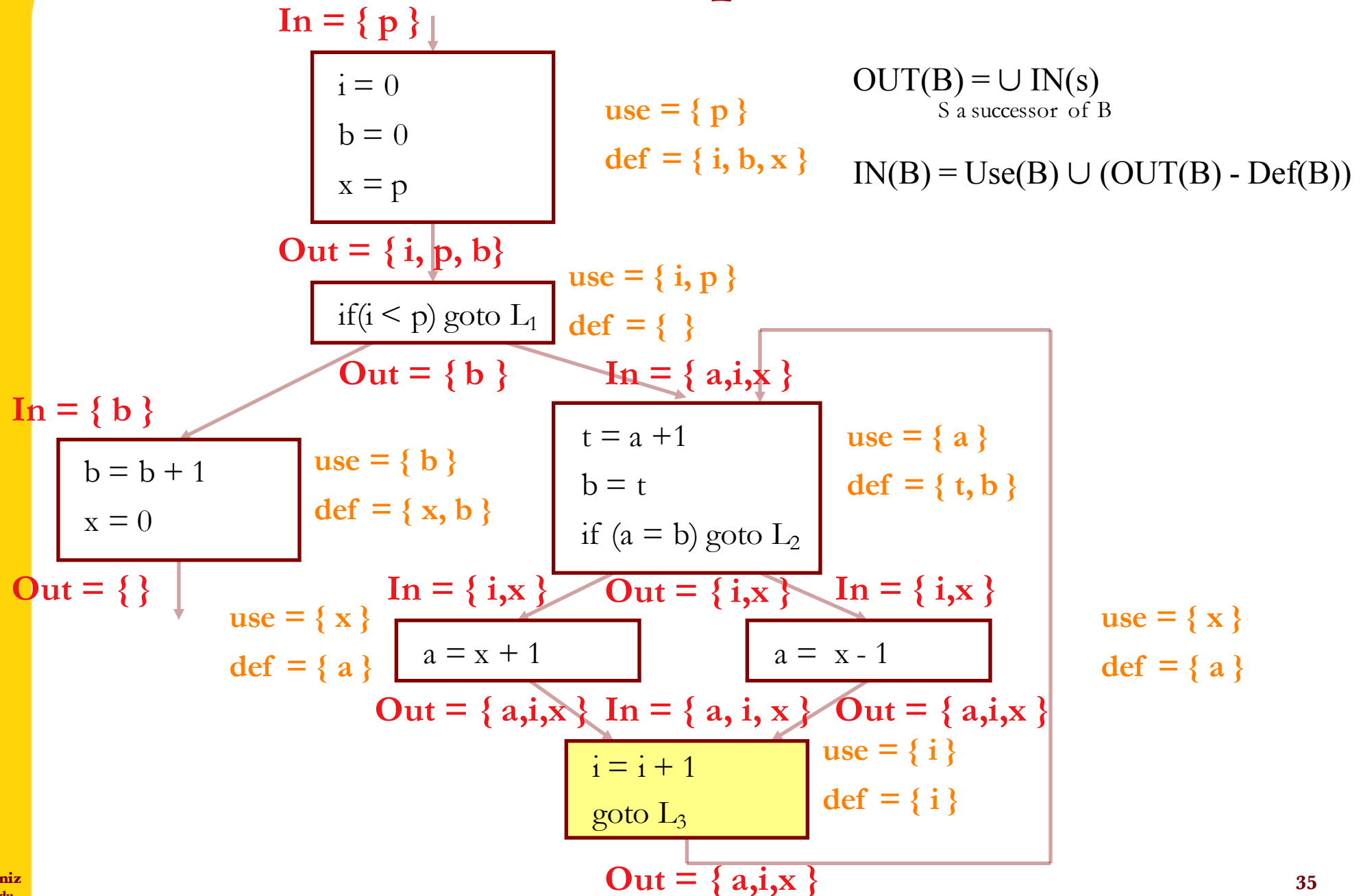
Example



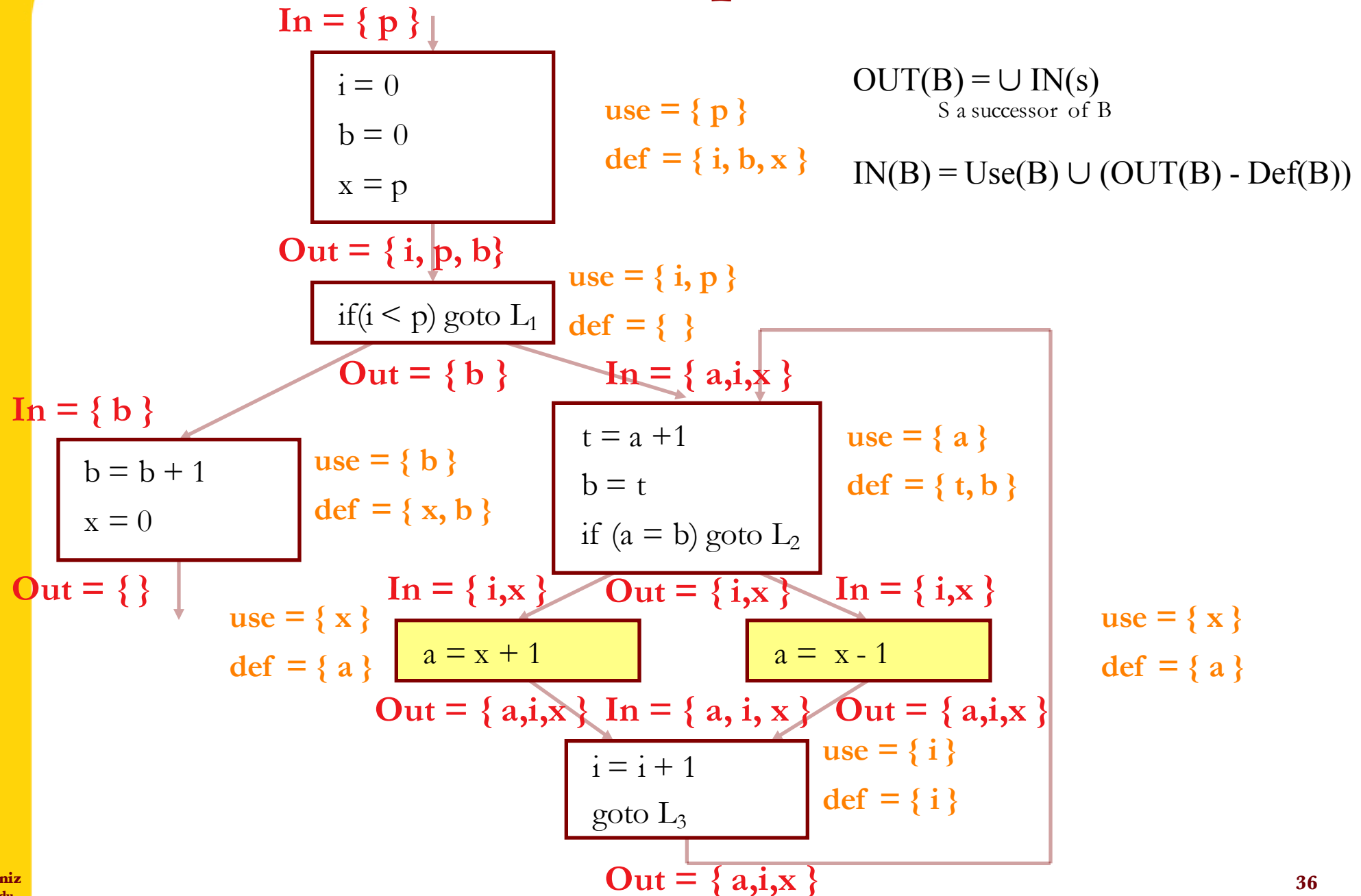
Example



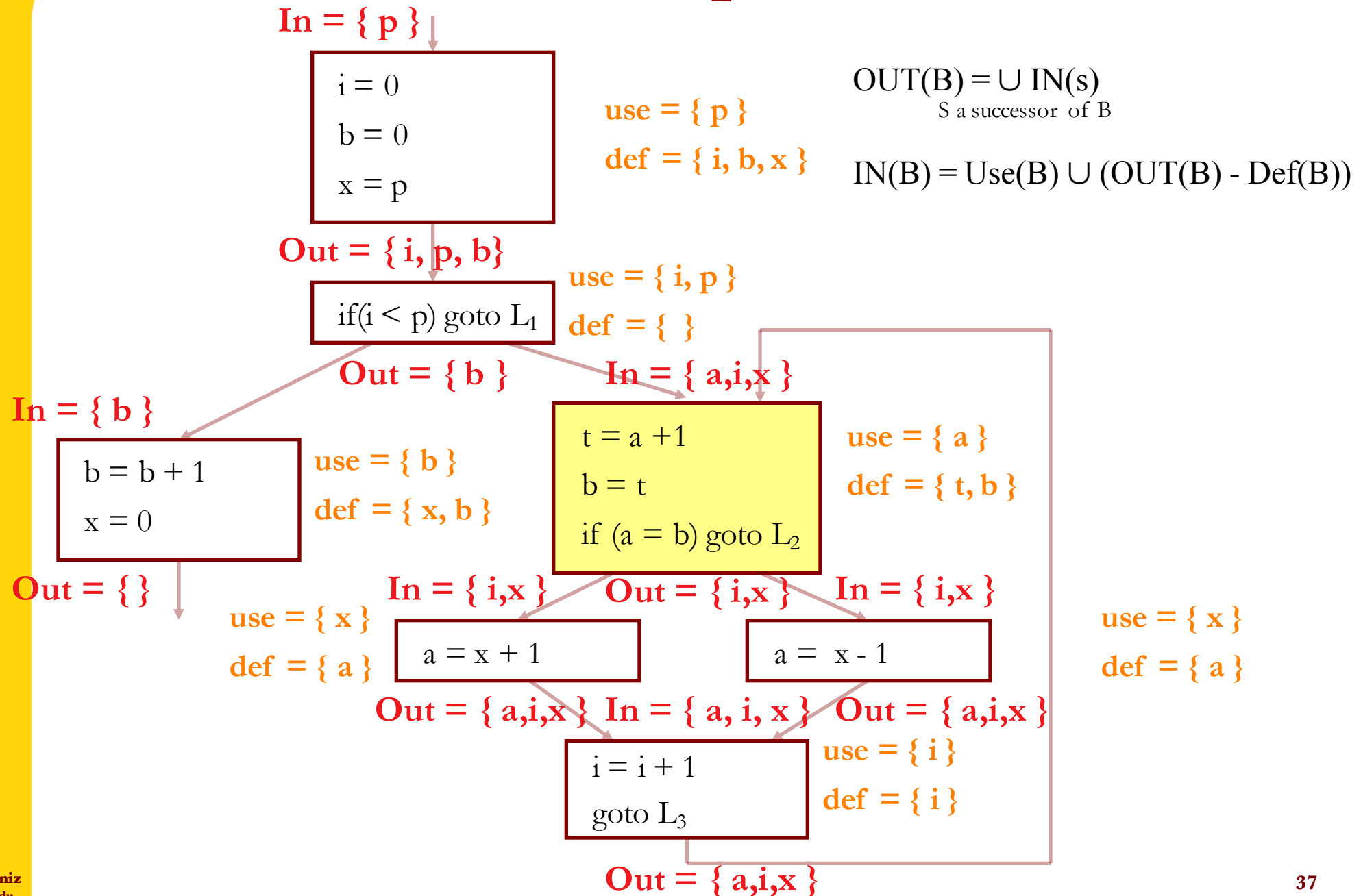
Example



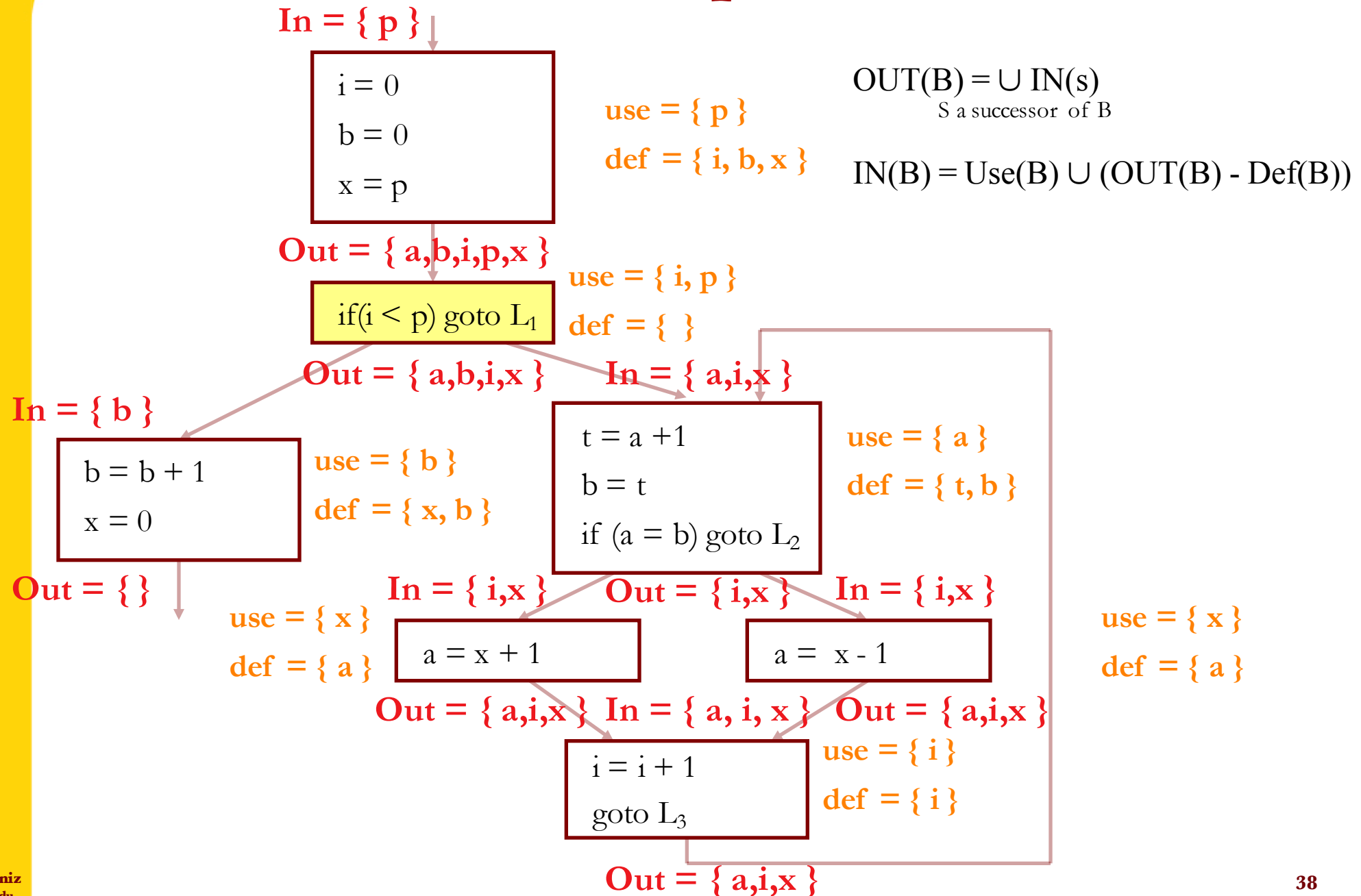
Example



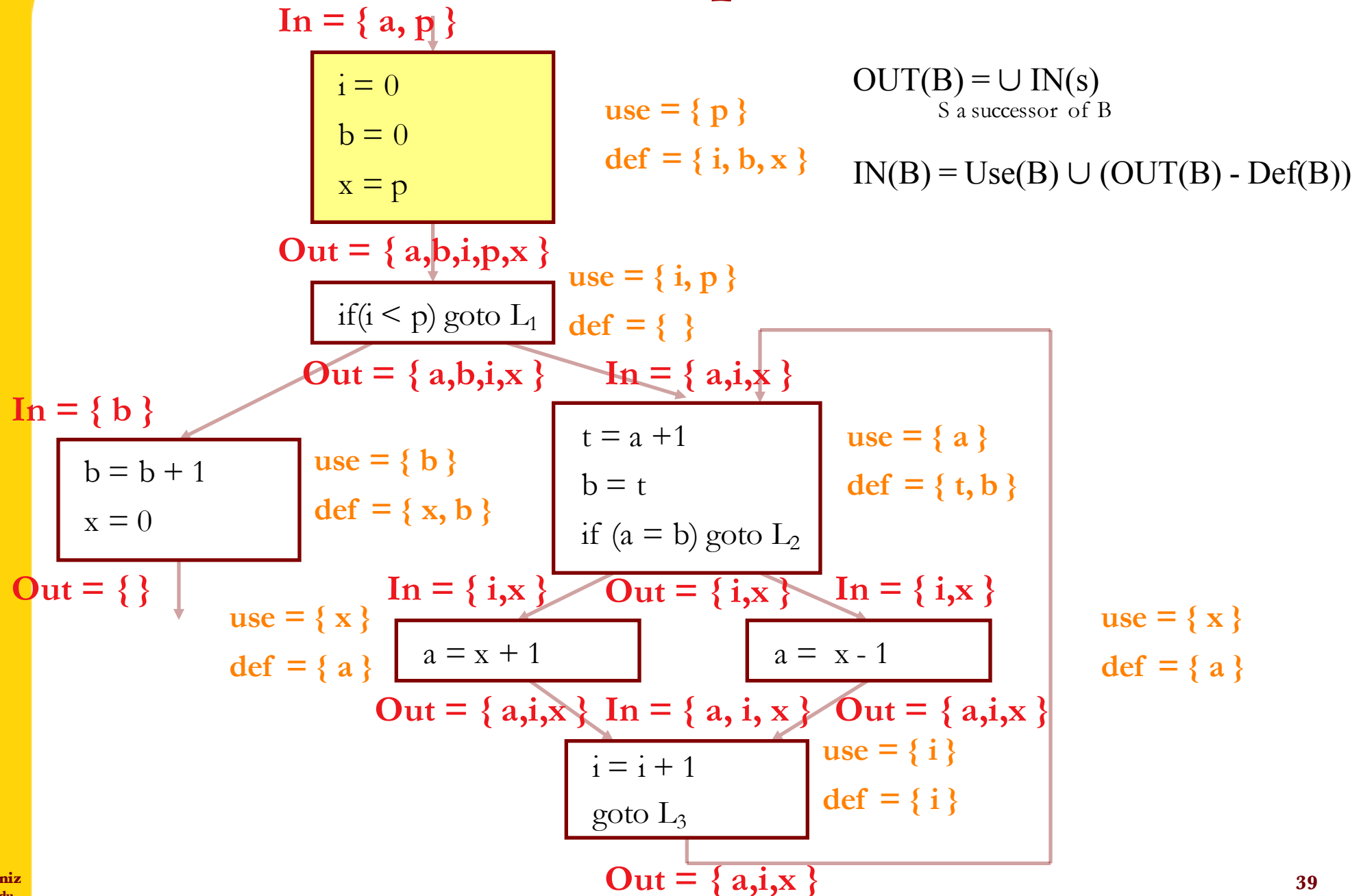
Example



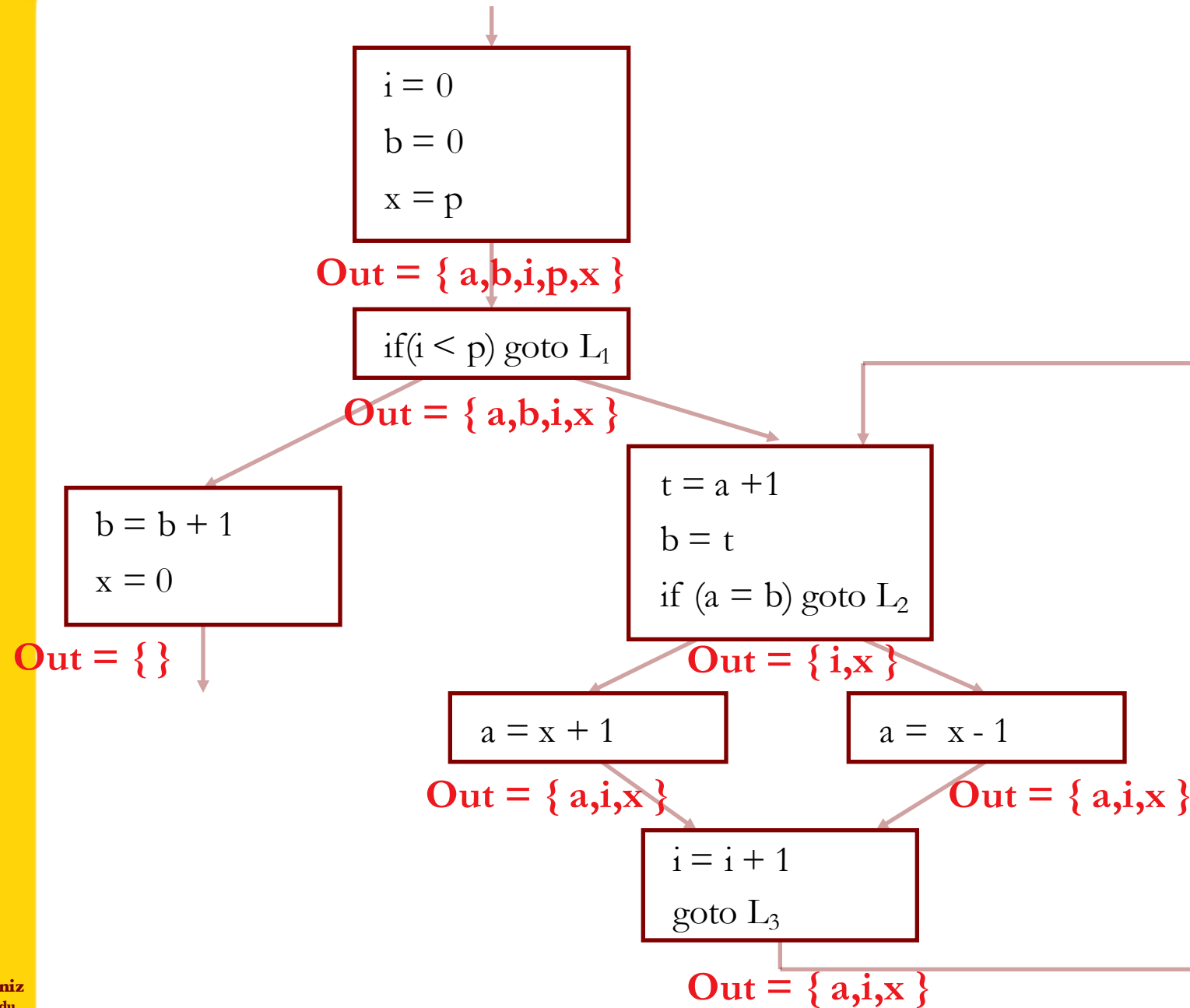
Example



Example



Example



Summary

- What is Live-Variable Analysis?
 - Backward Data-Flow Analysis Problem
 - Upwards Exposed (Gen) - Computed in a Forward Pass
- Most Significant Application
 - Register Allocation