

# Computational Statistics-Report

David Niederkofler, Erlend Lokna

2022-11-30

```
mydata<-read.table("Report2_Dataset.txt", header=FALSE)
```

## Statistical Analysis of Covariates

It is important to mention the use of notation before we proceed. We will in this section use the notation  $\mathbf{x} = \{x_1, x_2, \dots, x_n\}$  as our covariate vector.

### Bernoulli - Beta, Ascicles

Since the Ascicles - covariate has a 0-1 outcome we can assume that it is Bernoulli distributed with parameter  $\theta$ . A natural conjugate prior for the Bernoulli distribution is the Beta distribution. Therefor we have the following initial information:

$$\begin{aligned}f(x_i|\theta) &= \theta^{x_i}(1-\theta)^{1-x_i} \\L(\mathbf{x}|\theta) &= \theta^{\sum_{i=1}^n x_i}(1-\theta)^{n-\sum_{i=1}^n x_i} \\h(\theta) &= \text{Beta}(a, b)\end{aligned}$$

We proceed by calculating the posterior distribution for  $\theta$

$$\begin{aligned}h(\theta|\mathbf{x}) &\propto L(\mathbf{x}|\theta)h(\theta) = \theta^{\sum_{i=1}^n x_i}(1-\theta)^{n-\sum_{i=1}^n x_i} \frac{1}{B(a, b)} \theta^{a-1}(1-\theta)^{b-1} I(0 < \theta < 1) \\&\propto \text{Beta}(\theta|a + \sum_{i=1}^n x_i, b + n - \sum_{i=1}^n x_i)\end{aligned}$$

### 1.1 Model selection

### 1.2 Results