

- Rate of rxn: change in conc. of any of reactants or product per unit time.

$$\text{Rxn rate} = - \frac{\Delta[\text{Reactant}]}{(\text{St. coeff.}) \Delta t} = - \frac{\Delta[\text{Product}]}{(\text{St. coeff.}) \Delta t}$$

- Rate law: An expression which shows how the rxn rate is related to concs of the reactant
 For ex $\rightarrow 2A + B \rightarrow \text{product}$ $\text{rate} = k[A]^m[B]^n$

- Order: Sum of powers of conc terms in the rate law

Methods for determination of order - 1) Using integrated rate equations (devised by Vaid Hoff)
 2) Graphical method
 3) Using half life period (Ostwald)
 4) The differential method ($r = k[A]^n$)
 5) Ostwald's isolation method

Unit of rate constant

$$k = (\text{mol l}^{-1})^{n-1} \text{s}^{-1}$$

n is order

- Molecularity: for elementary rxn - number of reactant molecules involved in a rxn.
 for complex rxn - number of molecules or atoms taking part in rate determining step (i.e. slowest step)

Order

1. Sum of powers of conc in rate law expression
2. experimentally determined value
3. can have fractional value
4. can assume zero value
5. can change with physical conditions.

Molecularity

1. number of reacting species undergoing simultaneous collision
2. Theoretical concept
3. always a whole number
4. cannot have zero value
5. is invariant for a chemical eqn.

- Factors influencing rate: 1) Nature of reactants (defines E_a)
 2) concs of reactants (increases no. of collisions)
 3) Temperature (increase in energy, hence increase in no. of collision)
 generally $\text{temp} \uparrow \text{rate} \uparrow$
 As a rule, an increase of temp by 10°C doubles the rxn rate.
 Ratio of rate constants of rxn at 2 diff temps differing by 10° is called Temperature coefficient = $\frac{k_{35^\circ}}{k_{25^\circ}}$
 4) Catalyst (lowers E_a)
 5) Pressure (increase in collisions, hence prob. of to get preferred orientation increases)
 6) Surface area of solid reactants (lowers E_a)

- Zero order rxn: reactant A decomposes

Differential rate law

Zero order $-\frac{d[A]}{dt} = k[A]^0$

First order $-\frac{d[A]}{dt} = k[A]$

Second order $-\frac{d[A]}{dt} = k[A]^2$

Integral rate law

$[A] = [A]_0 - kt$

$[A] = [A]_0 e^{-kt}$

$\frac{1}{[A]} - \frac{1}{[A]_0} = kt$

- Pseudo order rxn: one of the reactants is in excess, hence it shows an order different from the actual order. ex- hydrolysis of ester

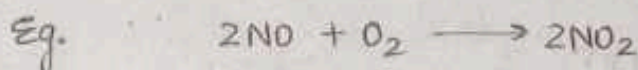
Unit-2

Chemical Kinetics

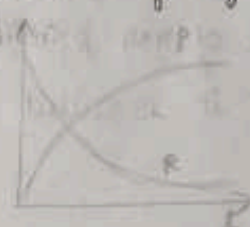
- Second order reactions
- Fast and slow rxns
- Temperature effect
- Concept of Activated state - Energy
- Determination of order
- Steady state approx
- Temperature effect
- Potential Energy Surface
- Theories of rxn rate

Rate of a Reaction -

Rate of rxn is defined as the rate of change of concentration of any of the products or reactants.



$$\text{rate of reaction} = -\frac{d[\text{NO}]}{2 \cdot dt} = -\frac{d[\text{O}_2]}{1 \cdot dt} = +\frac{d[\text{NO}_2]}{2 \cdot dt}$$



Rate law

Rate law is an expression which shows how the reaction rate is related to the concentration of reactants. is called.



$$r = k[\text{A}]^x [\text{B}]^y$$

Order of a rxn

Sum of the powers of concentration terms in rate law.

$$r = k[\text{A}]^x [\text{B}]^y$$

$$\text{Order of rxn} = (x+y)$$

Methods for determination of order of a rxn

- ① By using integrated rate eq.
- ② Graphical method
- ③ using Half life period
- ④ Ostwald's isolation method

① Integrated rate equations

In a reaction in which one of the reactant is present in large concentration (in excess), the rxn shows a different order of rxn practically from the one calculated theoretically. Hence it is called pseudo-order reactions.

$$r = k[A][B]$$

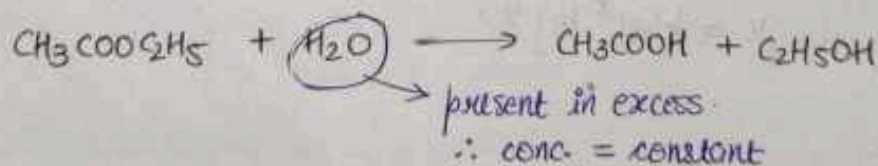
If B is present in large conc., the practically it's conc. remains constant -

$$\therefore r = k'[A]$$

Pseudo First Order Rxn.

Example -

Hydrolysis of Ester -



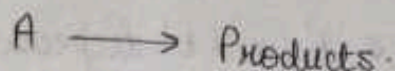
$$r = k [\text{CH}_3\text{COOC}_2\text{H}_5] [\text{H}_2\text{O}]$$

$$r = k' [\text{CH}_3\text{COOC}_2\text{H}_5]$$

Second Order Reactions

One reactant

Reaction —



$$t=0 \quad a \quad 0$$

$$t=t \quad a-x \quad x$$

a = initial concentration.
(mol l^{-1}).

x moles have reacted
in time ' t '

$$r = k[A]^2$$

$$r = -\frac{d[A]}{dt}$$

$$\frac{dx}{dt} = k(a-x)^2$$

$$\int_{(x=0)}^{(x=x)} \frac{dx}{(a-x)^2} = \int_{(t=0)}^{(t=t)} k dt$$

$$\left[\frac{1}{a-x} \right]_0^x = kt$$

$$\left(\frac{1}{a-x} - \frac{1}{a} \right) = kt$$

$$\boxed{R = \frac{1}{t} \cdot \frac{x}{a(a-x)}} \quad \text{Integrated rate eqn.}$$

Ex. \rightarrow Hydrolysis of Ester by NaOH.

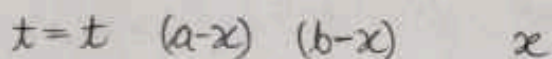
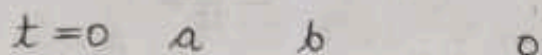


⇒ Integrated rate equation when two different reactants are present.



Initial concentration of A and B are 'a' & 'b' mol l⁻¹ respectively.

$$r = -\frac{d[A]}{dt} = -\frac{d[B]}{dt}$$



$$r = \frac{dx}{dt} = k(a-x)(b-x)$$

$$\int_0^x \frac{dx}{(a-x)(b-x)} = \int_0^t k dt$$

$$\int_0^x \frac{dx}{(b-a)(a-x)} + \int_0^x \frac{dx}{(a-b)(b-x)} = kt$$

$$\left(\frac{1}{a-b}\right) \left[\ln\left(\frac{b-x}{b}\right) - \ln\left(\frac{a-x}{a}\right) \right] = kt$$

$$\boxed{\left(\frac{1}{a-b}\right) \ln \left[\frac{(b-x)a}{(a-x)b} \right] = kt}$$

Derive an expression for half-life of n^{th} order reaction.



$$r = k[A]^n$$

$$r = -\frac{d[A]}{dt}$$

$$-\frac{d[A]}{dt} = k[A]^n$$

$$\int_{A_0}^{A_0/2} \frac{d[A]}{[A]^n} = \int_0^t -k dt$$

$$\left[\frac{A^{-n+1}}{-n+1} \right]_{A_0}^{A_0/2} = -kt$$

$$\left(\frac{1}{n-1} \right) \left[\frac{1}{A^{n-1}} \right]_{A_0}^{A_0/2} = kt$$

$$\left(\frac{1}{n-1} \right) \left[\frac{(2)^{n-1}}{(A_0)^{n-1}} - \frac{1}{(A_0)^{n-1}} \right] = kt$$

$$\frac{1}{(n-1)t} \left(\frac{(2)^{n-1} - 1}{(A_0)^{n-1}} \right) = k$$

$$t_{1/2} = \frac{1}{(n-1)k} \left(\frac{(2)^{n-1} - 1}{(A_0)^{n-1}} \right)$$

② Graphical Method.

First order —

$$t = \frac{1}{k} \ln \left(\frac{C_0}{C_t} \right) \quad / \quad t = \frac{1}{k} \ln \left(\frac{a}{a-x} \right)$$

(C_0 = initial conc.)
(C_t = conc. at time t .)

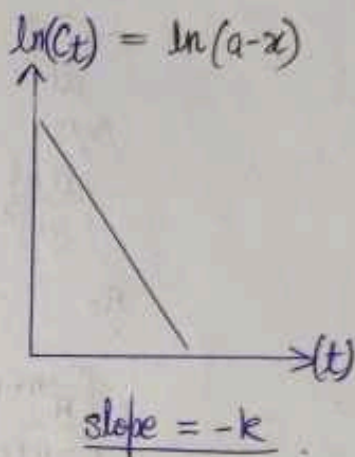
$$\ln C_0 - \ln C_t = kt$$

$$\ln C_t = \ln C_0 - kt \rightarrow x$$

y

$$y = -mx + c$$

$$\begin{pmatrix} m = k \\ c = \ln C_0 \end{pmatrix}$$



Second order

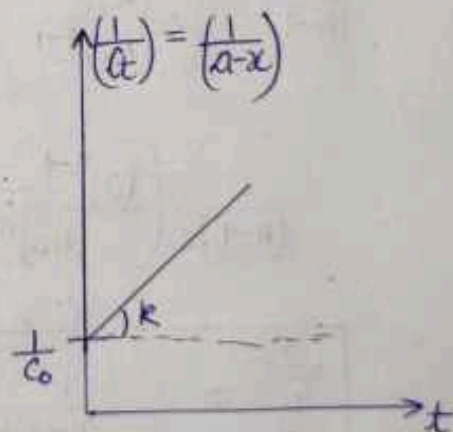
$$t = \frac{1}{k} \left[\frac{1}{C_t} - \frac{1}{C_0} \right] \quad / \quad t = \frac{1}{k} \left[\frac{1}{(a-x)} - \frac{1}{a} \right]$$

$$\frac{kt}{x} = \frac{1}{(a-x)} - \frac{1}{a}$$

x

$$y = mx + c$$

$$\begin{pmatrix} m = k \\ c = \frac{1}{C_0} \end{pmatrix}$$



③ Half life period method.

$$T_{1/2} \propto \frac{1}{[A]}$$

2nd order rxn

(A = initial concentration)

$$T_{1/2} \propto \frac{1}{[A]^2}$$

3rd order rxn.

$$T_{1/2} \propto \frac{1}{[A]^{n-1}}$$

nth order rxn.

$$t_1 \propto \frac{1}{[A_1]^{n-1}} ; t_2 = \frac{1}{[A_2]^{n-1}}$$

$$\frac{t_1}{t_2} = \frac{[A_2]^{n-1}}{[A_1]^{n-1}}$$

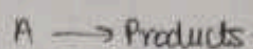
simplifying,

$$n = 1 + \frac{\log[t_1/t_2]}{\log[A_2/A_1]}$$

Formulas -:

First Order -

$$k = \frac{2.303}{t} \log_{10} \left(\frac{C_0}{C_t} \right) \quad (\text{single reactant})$$



$$T_{1/2} = \frac{0.693}{k}$$

$$\left[\begin{array}{l} C_0 = \text{Initial conc.} \\ C_t = \text{conc. of A after} \\ \text{some time 't'} \end{array} \right]$$

Second order -

$$k = \frac{1}{t} \left[\frac{1}{C_t} - \frac{1}{C_0} \right] \quad (\text{single reactant}) \quad A \rightarrow \text{Pro.}$$

$$k = \left(\frac{1}{A_0 - B_0} \right) \log \left(\frac{(B_0 - x)(A_0)}{(A_0 - x)(B_0)} \right) \quad (\text{two reactants}) \quad A + B \rightarrow \text{Pro.}$$

$$t=0. \quad A_0 \quad B_0 \quad 0$$

$$t=t \quad A_t \quad B_t \quad x$$

$$\left(\begin{array}{l} A_t = A_0 - x \\ B_t = B_0 - x \end{array} \right)$$

$$T_{1/2} = \frac{1}{kC_0}$$

Zero Order

$$k = \frac{C_0 - C_t}{t} \quad (\text{single reactant})$$

$$T_{1/2} = \frac{2C_0}{2k}$$

④ Ostwald's Isolation Method



- Order with respect to A, B and C are found out individually.
- For determining order wrt A, B and C are taken in large amounts, so that their conc. remains constant.
- Same is done for B and C.

$$n = \text{order of rxn} = n_A + n_B + n_C$$

\uparrow \uparrow \uparrow
order wrt A order wrt B order wrt C.

— **SOLVED PROBLEM.** From the following data for the decomposition of N_2O_5 in CCl_4 solution at 48°C , show that the reaction is of the first order

t (mts)	10	15	20	∞
Vol of O_2 evolved	6.30	8.95	11.40	34.75

SOLUTION

For a first order reaction the integrated rate equation is

$$\frac{1}{t} \log \frac{V_\infty}{V_\infty - V_t} = k$$

In this example, $V_\infty = 34.75$

t	$V_\infty - V_t$	$\frac{1}{t} \log \frac{V_\infty}{V_\infty - V_t}$	$= k$
10	28.45	$\frac{1}{10} \log \frac{34.75}{28.45}$	$= 0.00868$
15	25.80	$\frac{1}{15} \log \frac{34.75}{25.80}$	$= 0.00862$
20	23.35	$\frac{1}{20} \log \frac{34.75}{23.35}$	$= 0.00863$

— Since the value of k is fairly constant, it is a **first order reaction**.

SOLVED PROBLEM. The following data was obtained on hydrolysis of methyl acetate at 25°C in 0.35N hydrochloric acid. Establish that it is a first order reaction.

t (secs)	0	4500	7140	∞
ml alkali used	24.36	29.32	31.72	47.15

SOLUTION

For a first order reaction,

$$k = \frac{2.303}{t} \log \frac{a}{a-x}$$

At any time, the volume of alkali used is needed for the acid present as catalyst and the acid produced by hydrolysis.

The volume of alkali used for total change from t_0 to t_∞ gives the initial concentration of ester. Thus,

$$a = 47.15 - 24.36 = 22.79 \text{ ml}$$

$$(a-x) \text{ after } 4500 \text{ sec} = 47.15 - 29.32 = 17.83 \text{ ml}$$

$$(a-x) \text{ after } 7140 \text{ sec} = 47.15 - 31.72 = 15.43 \text{ ml}$$

Substituting values in the rate equation above, we have

$$k = \frac{2.303}{4500} \log \frac{22.79}{17.83} = 0.00005455$$

$$k = \frac{2.303}{7140} \log \frac{22.79}{15.43} = 0.0000546$$

Since the values of k in the two experiments are fairly constant, the reaction is of the first order.

Theories of Reaction -

① Collision Theory -

Rate constant = k

$$k = Zpf$$

$$f \propto e^{-E_a/RT}$$

$$k = Ae^{-E_a/RT}$$

Z = collision frequency

p = the fraction of molecules with proper orientation.

f = the fraction of molecules with sufficient energy.

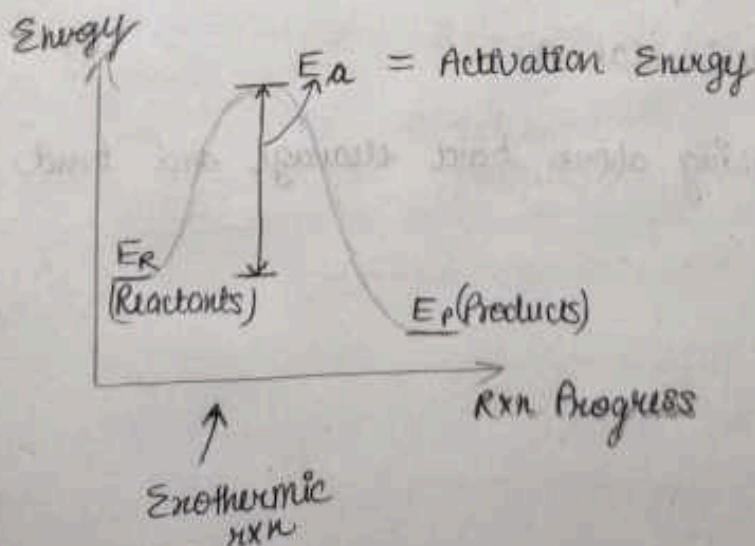
Arrhenius equation.

Theory -

Says that

A chemical reaction will take place between the reactants only if -

- ① The molecules of reactants collide in a proper orientation.
 - ② The molecules must collide with sufficient kinetic energy, to overcome the activation energy barrier and rxn can take place.
- correct orientation = ensure direct contact b/w atoms for bond formation and bond breaking.



Arrhenius Equation

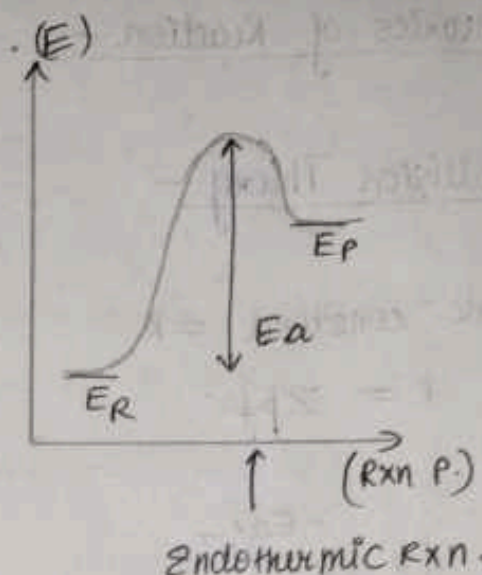
$$k = Ae^{-E_a/RT}$$

$$\log k = \log A + \left(\frac{-E_a}{RT} \right) \times \frac{1}{2.303}$$

$$\log k_1 = \log A + \frac{(-E_a)}{2.303RT_1}$$

$$\log k_2 = \log A + \frac{(-E_a)}{2.303RT_2}$$

$$\log \frac{k_2}{k_1} = \frac{E_a}{2.303R} \left[\frac{1}{T_1} - \frac{1}{T_2} \right]$$

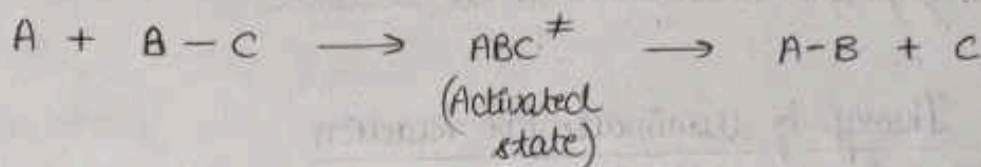


Limitations of Collision Theory:

- ① ~~They~~ This theory applies to only simple gaseous rxns, or rxn in which reactants are simple molecules.
- ② This theory assumes that only Kinetic Energy contributes for overcoming Energy barrier, ignoring Rotational and vibrational Energy.
- ③ No method to determine steric effect.
- ④ In case of complex rxn, the theoretical rate constants are different from the experimental one.
- ⑤ They theory says nothing about bond cleavage and bond formation.

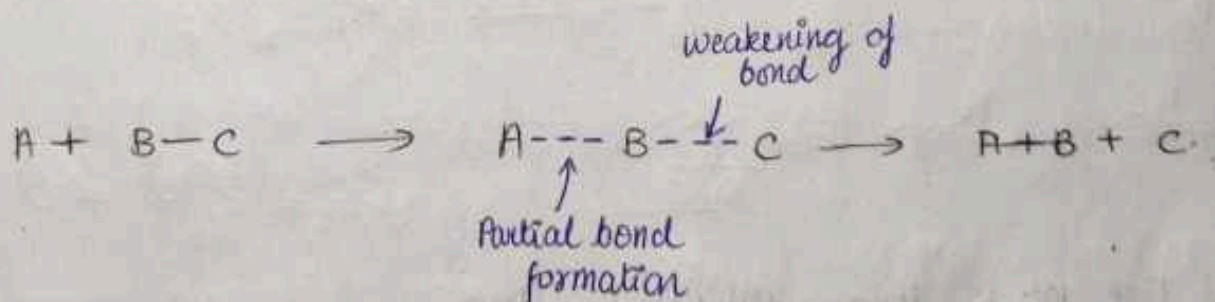
② Transition state theory

This theory states that, direct collision of reactant molecules does not yield product, during the rxn a transition state or activated complex is formed which decomposes to yield product.



As

- ① The colliding molecules approach each other, they are slowed down due to repulsion caused by their electron clouds.
In this process the kinetic energy is converted to potential energy.
- ② As the molecules come close \rightarrow electron clouds interpenetrate \rightarrow causing rearrangement of valence electrons.
- ③ A partial bond is formed b/w $A \& B$, with simultaneous weakening of bonds b/w $B \& C$. This state is called Transition State.



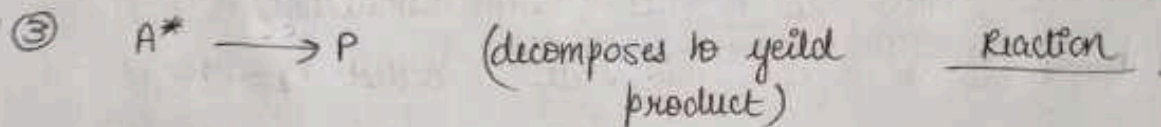
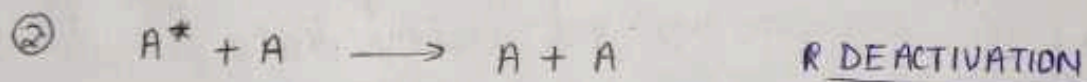
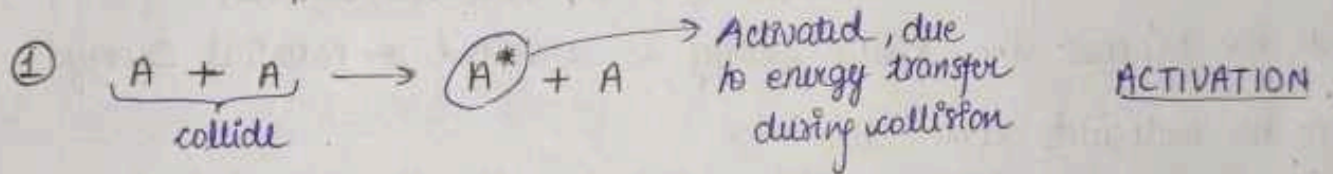
→ Role of catalyst :-

- ① It provides an alternative pathway of reaction, with lower activation Energy.
- ② It provides a surface area to the substrate, and the substrate forms weak van der Waals forces with catalyst.
- Hence.
- ③ ~~It~~ providing proper orientation to the reactants.

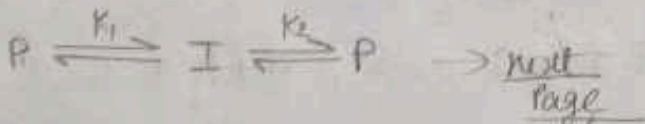
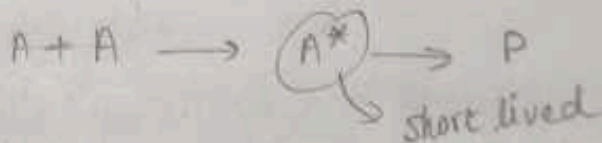
Lindeman's Theory of Unimolecular Reaction.

⇒ There existed a time lag b/w activation and rxn of molecules.
In case of unimolecular rxn —

There are three possibilities -



$$\frac{d[A^*]}{dt} = 0$$



by $\text{S.S.A.} = \frac{d[A^*]}{dt} = 0$

* If time gap is long, step (3) is slow, the rxn should follow FIRST ORDER kinetics.

* If A reacts as soon as formed, step (2) is slow then rxn should be second order.

The equilibrium Approximation -

Suppose a reaction occurs with formation of a series of intermediates.



To find the rate equation, we assume that a rate-determining step exists.

Rate determining step \rightarrow Slowest

It is further assumed that all the steps preceding the r.d.s are in equilibrium.



The Steady-state Approximation

In rxns where rate determining step (slowest) does not exist,

SSA is assumed for transition state

\rightarrow short lived.

$$\frac{d[I_1]}{dt} = \frac{d[I_2]}{dt} = \frac{d[I_n]}{dt} = 0$$

rate of formation = rate of decomposition \rightarrow For transition state

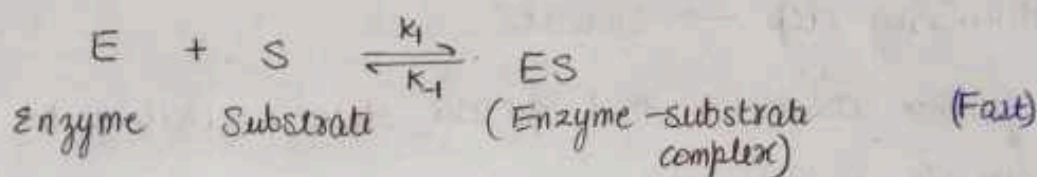
Enzyme Catalysis

complex organic substances = enzymes

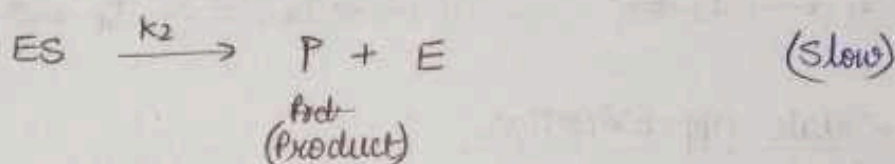
↳ Proteins with high molar masses.

Mechanism and Kinetics of Enzyme catalyzed Rxn —

Step 1



Step 2



⇒ A true equilibrium can't be established in fast step because the subsequent slow rxn is continuously removing the intermediate complex (ES).

⇒ concentration $\rightarrow [E] \ll [S]$

∴ $[ES] \ll [S] \rightarrow$ (steady state approx. can be used)

$$r = -\frac{d[S]}{dt} = \frac{d[P]}{dt} = k_2[ES]$$

$$0 = \frac{d[ES]}{dt} = \underbrace{k_1[E][S]}_{\text{formation}} - \underbrace{(k_{-1}[ES] + k_2[ES])}_{\text{decomposition}}$$

Rate of Formation of intermediate = Rate of decomposition of intermediate

$[E]$ can't be measured experimentally.

Enzyme conservation equation —

$$[E_0]_0 = [ES] + [E]$$

↑ Total enzyme concentration ↓ reached/bound enzyme conc. → free enzyme conc.

$$[E] = [E_0]_0 - [ES]$$

substituting —

$$\frac{d[ES]}{dt} = k_1 [E_0]_0 [S] - k_{-1} [ES] - k_2 [ES] = 0.$$

$$k_1 [E_0]_0 [S] = [k_{-1} + k_2] [ES]$$

$$[ES] = \frac{k_1 [E_0]_0 [S]}{k_{-1} + k_2 + [S] k_1} \Rightarrow \mu = \frac{k_1 k_2 [E_0]_0 [S]}{k_{-1} + k_2 + [S] k_1}$$

$$[ES] = \frac{\mu}{k_2}$$

dividing num. & denom. by k_1 —

Michael-Menten equation $\rightarrow \frac{[ES]}{\mu} = \frac{[E_0]_0 [S] k_2}{\left(\frac{k_{-1} + k_2}{k_1}\right) + [S]} = \frac{[E_0]_0 [S] k_2}{K_m + [S]}$

K_m = Michaelis constant

$$K_m = \left(\frac{k_{-1} + k_2}{k_1} \right)$$

⇒ when all the enzyme has reacted with substrate,
the reaction will be going at max. rate.

$$[E] = [ES]$$

$$r_{\text{max}} = k_2 [E]_0 = v_{\text{max}}$$

↑
maximum rate,
in notation of Enzymology.

Now Michaelis - Menten eq. becomes —

$$\Rightarrow r = v_{\text{max}} \times \frac{[S]}{K_m + [S]}$$

Case I

(a) when $K_m \gg [S]$

$$K_m + [S] \approx K_m$$

$$r = v_{\text{max}} \cdot \frac{[S]}{K_m}$$

$$r = k' [S]$$

(FIRST-ORDER RXN)

Case II

(b) when $[S] \gg K_m$

$$r = v_{\text{max}} \frac{[S]}{[S]} = v_{\text{max}} = \text{constant}$$

(ZERO ORDER)

SOLVED PROBLEM. In the reduction of nitric oxide, 50% of reaction was completed in 108 seconds when initial pressure was 336 mm Hg and in 147 seconds initial pressure was 288 mm Hg. Find the order of the reaction.

SOLUTION

We know that

$$\frac{t_2}{t_1} = \left[\frac{A_1}{A_2} \right]^{n-1} \quad \dots(1)$$

where t_1 and t_2 are half-life periods and $[A_1]$ and $[A_2]$ are the corresponding initial concentrations, while n is the order of the reaction.

Taking logs of the expression (1), we have

$$n = 1 + \frac{\log [t_2 / t_1]}{\log [A_1 / A_2]} \quad \dots(2)$$

Substituting values in expression (2),

$$\begin{aligned} n &= 1 + \frac{\log 108/147}{\log 288/336} \\ &= 1 + \frac{0.1339}{0.0669} = 1 + 2 = 3 \end{aligned}$$

Therefore, the reaction is of the **third order**.

SOLVED PROBLEM. The gas-phase reaction between methane (CH_4) and diatomic sulphur (S_2) is given by the equation



At 550°C the rate constant for this reaction is $1.1 \text{ l mol}^{-1} \text{ sec}$ and at 625°C the rate constant is $6.4 \text{ l mol}^{-1} \text{ sec}$. Calculate E_a for this reaction.

SOLUTION

Here

$$k_1 = 1.1 \text{ litre mol}^{-1} \text{ sec.} \quad T_1 = 550 + 273 = 823 \text{ K}$$

$$k_2 = 6.4 \text{ litre mol}^{-1} \text{ sec.} \quad T_2 = 625 + 273 = 898 \text{ K}$$

Substituting the values in the equation

$$\ln \left(\frac{k_2}{k_1} \right) = \frac{E_a}{R} \left(\frac{1}{T_1} - \frac{1}{T_2} \right)$$

$$\ln \left(\frac{6.4}{1.1} \right) = \frac{E_a}{8.3145 \text{ JK}^{-1} \text{ mol}^{-1}} \left(\frac{1}{823 \text{ K}} - \frac{1}{898 \text{ K}} \right)$$

Solving for E_a , gives

$$\begin{aligned} E_a &= \frac{(8.3145 \text{ JK}^{-1} \text{ mol}^{-1}) \ln \left(\frac{6.4}{1.1} \right)}{\left(\frac{1}{823 \text{ K}} - \frac{1}{898 \text{ K}} \right)} \\ &= 1.4 \times 10^5 \text{ J/mol} \end{aligned}$$