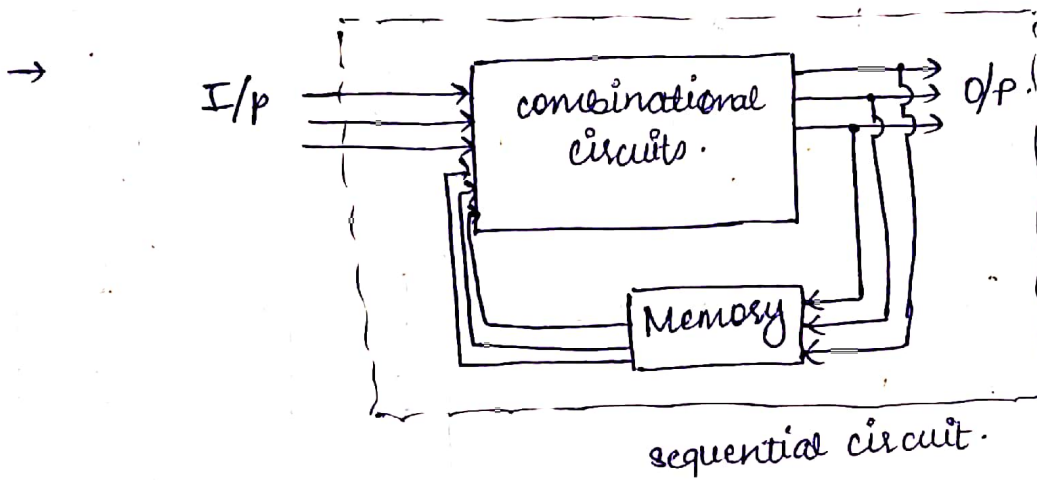


Registers

Sequential Circuits : Introduction

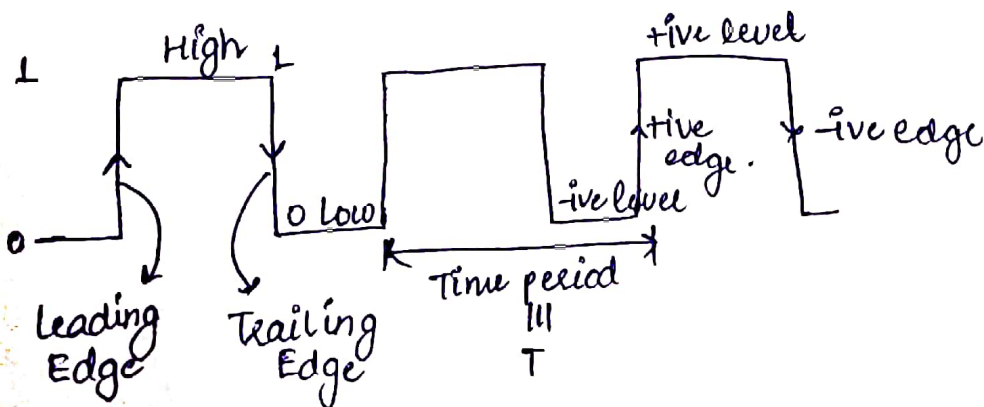
- Sequential circuits are combinational circuits with memory.
- In sequential circuits, the present o/p depends on the present i/p as well as previous output.
- combinational circuits are those in which present o/p depend on present i/p.

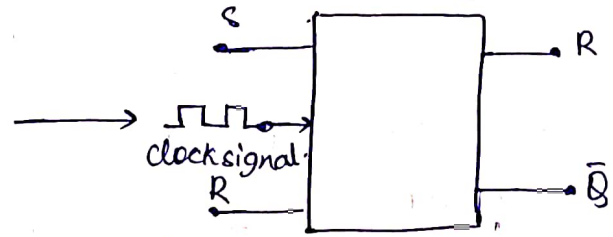
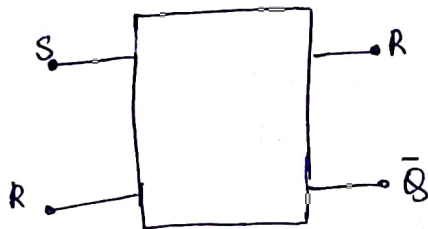
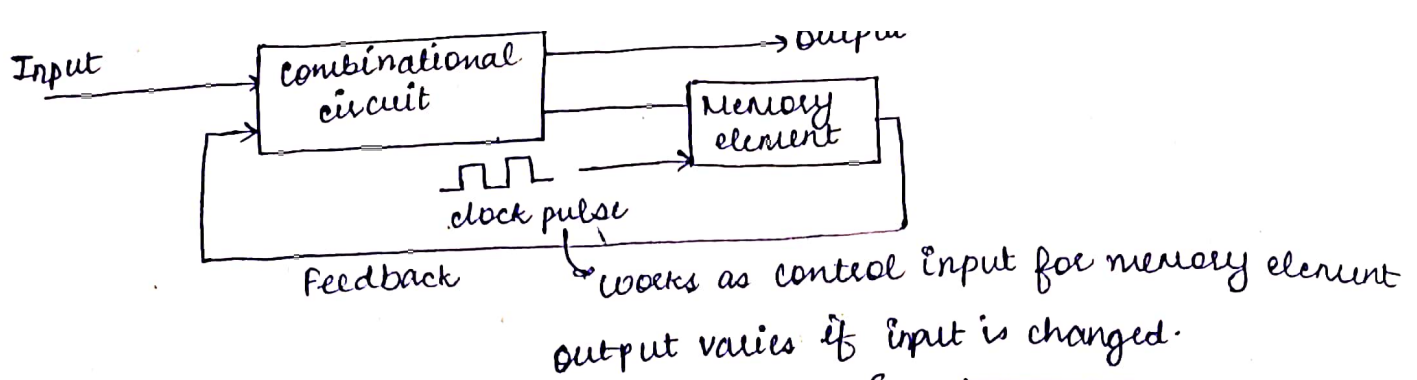
- Adder
- Subtractor
- Multiplexer.
- Decoders
- Encoders.



Clock & Triggering Methods

- Clock signal is a timing signal.
- Used to provide sequence of the circuit.
- Clock is a rectangular signal called clock pulse with duty cycle equal to 50%.





→ when nothing is applied to this circuit it behaves asynchronously and is called latch.

$$\text{clock frequency} = \frac{1}{T}$$

$$\text{duty cycle} = \frac{\text{ratio of time for which pulse is high}}{\text{total time}}$$

→ now this circuit becomes synchronous and is called SR Flip Flop.

→ Output is shown when clock signal is in high state.

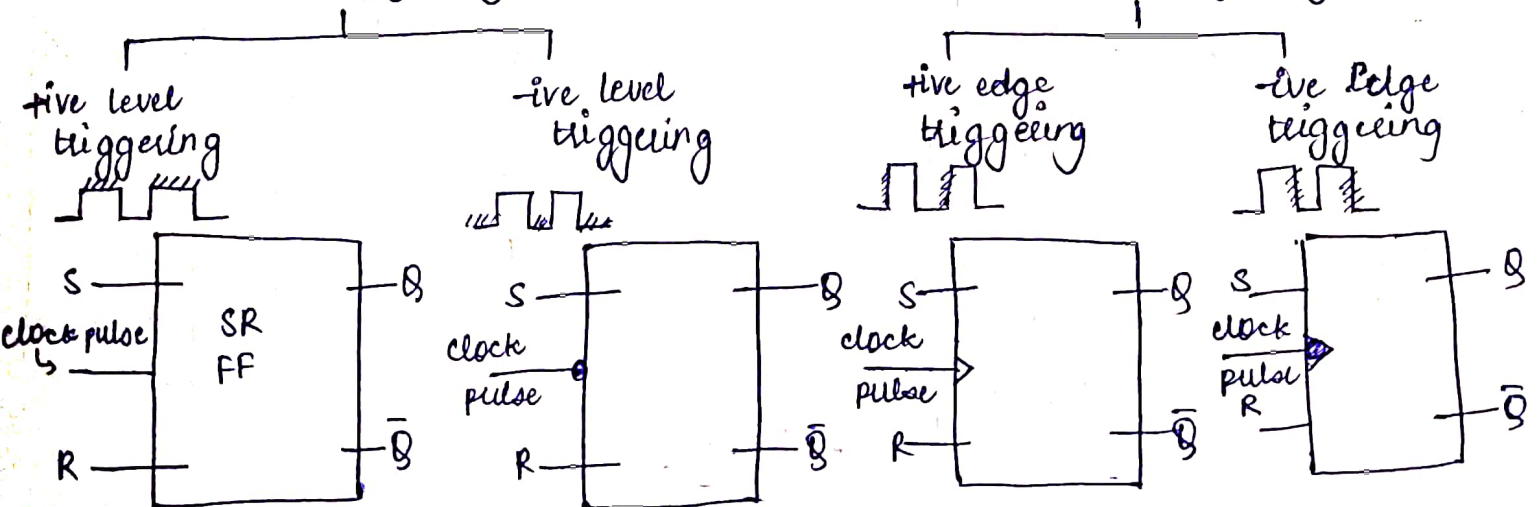
→ The clock signal decides if the change in input signal must be reflected in the output signal or not.

→ speed of the circuit can be varied by changing the frequency of clock signal.

Triggering Methods

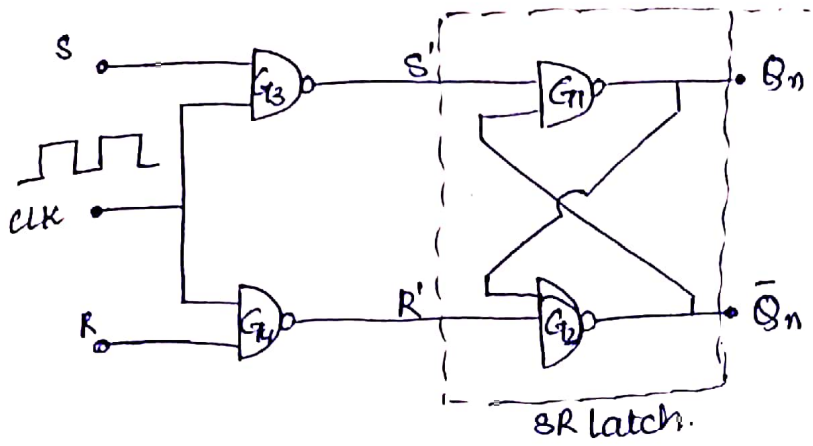
Level Triggering

Edge Triggering



NAND Gates used

SR FLIP FLOP



$$S' = \overline{S \cdot CLK} = \overline{S} + \overline{CLK} \quad (1)$$

$$R' = \overline{R \cdot CLK} = \overline{R} + \overline{CLK} \quad (2)$$

when CLK=0

$$S' = \overline{S} + \overline{0} \Rightarrow S' = \overline{S} + 1 = 1$$

$$R' = \overline{R} + \overline{0} \Rightarrow R' = \overline{R} + 1 = 1$$

TRUTH Table of SR Latch

Truth Table for SR FF

X \equiv either 0 or 1

| CLK | S | R | Q_n | \overline{Q}_{n+1} |
|-----------------------|---|---|----------------------|----------------------|
| 0 | X | X | Prev. state (Memory) | \overline{Q}_n |
| 1 | 0 | 0 | Prev. state (Memory) | \overline{Q}_n |
| Reset \rightarrow 1 | 0 | 1 | 0 | 1 |
| Set \rightarrow 1 | 1 | 0 | 1 | 0 |
| 1 | 1 | 1 | Invalid. | |

when CLK=1

(i) $S=0, R=0$

$$S'=1, R'=1$$

(ii) $S=0, R=1$

$$S'=1, R'=0$$

(iii) $S=1, R=0$

$$S'=0, R'=1$$

(iv) $S=1, R=1$

$$S'=0, R'=0$$

| S | R | Q | \overline{Q} |
|---|---|----------------------|----------------|
| 0 | 0 | Invalid. | |
| 0 | 1 | 1 | 0 |
| 1 | 0 | 0 | 1 |
| 1 | 1 | Prev. state (Memory) | |

Characteristic Equation of SRFF.

Present state $\equiv Q_n$

Next state $\equiv Q_{n+1}$

Q_n also acts as an input

Truth table of SRFF

| CLK | S | R | Q_{n+1} |
|-----|---|---|-----------|
| 0 | X | X | Q_n |
| 1 | 0 | 0 | Q_n |
| 1 | 0 | 1 | 0 Reset |
| 1 | 1 | 0 | 1 Set |
| 1 | 1 | 1 | Invalid |

char Table

| Q_n | S_n | R_n | Q_{n+1} |
|-------|-------|-------|-----------|
| 0 | 0 | 0 | 0 |
| 0 | 0 | 1 | 0 |
| 0 | 1 | 0 | 1 |
| 0 | 1 | 1 | X Invalid |
| 1 | 0 | 0 | 1 |
| 1 | 0 | 1 | 0 |
| 1 | 1 | 0 | 1 |
| 1 | 1 | 1 | X Invalid |

| $S_n R_n \bar{S}_n \bar{R}_n$ | 00 | 01 | 11 | 10 |
|-------------------------------|----|----|----|----|
| 0 | 0 | 0 | X | 1 |
| 1 | 1 | 0 | X | 1 |

$$Q_{n+1} = S_n + Q_n \bar{R}_n$$

Excitation Table for SR FF

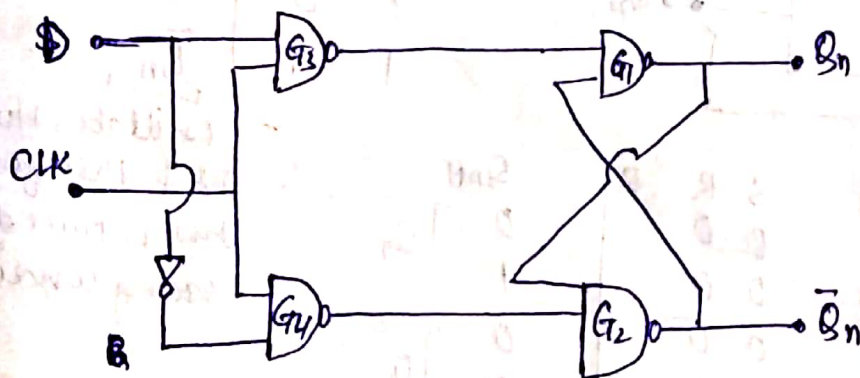
Char Table

| Q_n | S_n | R_n | Q_{n+1} |
|-------|-------|-------|-----------|
| 0 | 0 | 0 | 0 |
| 0 | 0 | 1 | 0 |
| 0 | 1 | 0 | 1 |
| 0 | 1 | 1 | X |
| 1 | 0 | 0 | 1 |
| 1 | 0 | 1 | 0 |
| 1 | 1 | 0 | 1 |
| 1 | 1 | 1 | X |

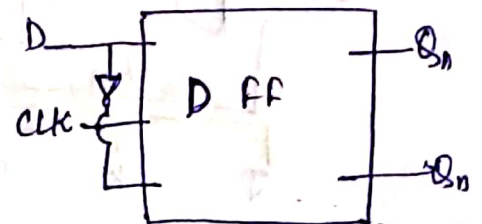
| Present state Q_n | Next state Q_{n+1} | Input $S_n R_n$ |
|---------------------|----------------------|-----------------|
| 0 | 0 | 0 0 |
| 0 | 1 | 1 0 |
| 1 | 0 | 0 1 |
| 1 | 1 | 0 0 |

Excitation table is used when output all given and we have to find the corresponding input.

D FLIP FLOP (used for data storage)



($S=0, R=1 \rightarrow 0$ Reset
 $S=1, R=0 \rightarrow 1$ set.)



TRUTH TABLE OF D FF

| CLK | D | Q_{n+1} |
|-----|---|--------------|
| 0 | X | Q_n Memory |
| 1 | 0 | 0 Reset |
| 1 | 1 | 1 set |

Characteristic Eqⁿ

| clk | D | Q_{n+1} |
|-----|---|-----------|
| 0 | X | Q_n |
| 1 | 0 | 0 |
| 1 | 1 | 1 |

char table

| Q_n | D | Q_{n+1} |
|-------|---|-----------|
| 0 | 0 | 0 |
| 0 | 1 | 1 |
| 1 | 0 | 0 |
| 1 | 1 | 1 |

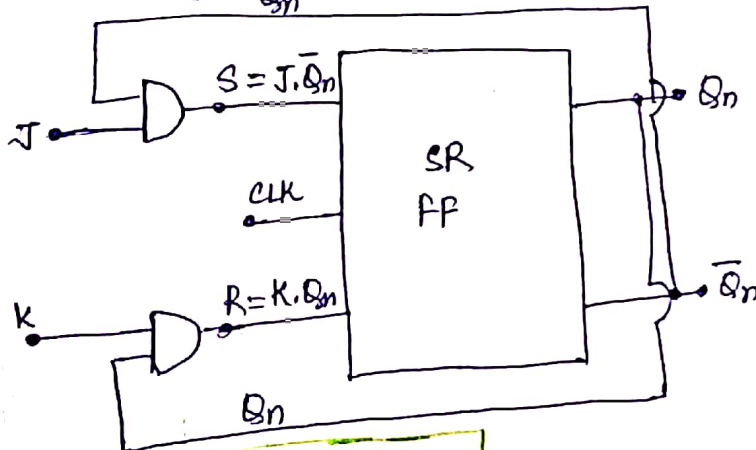
Char. Equation: $Q_{n+1} = D$

Excitation table

| Present Q_n | Next Q_{n+1} | D |
|---------------|----------------|---|
| 0 | 0 | 0 |
| 0 | 1 | 1 |
| 1 | 0 | 0 |
| 1 | 1 | 1 |

[just used for last input where $S=1, R=1$]

JK FLIP FLOP (we change the invalid state of SR FF into Q_n condition of Racing)



Truth Table

| J | K | Q_{n+1} |
|---|---|-------------|
| 0 | 0 | Q_n |
| 0 | 1 | 0 |
| 1 | 0 | 1 |
| 1 | 1 | \bar{Q}_n |

| J | K | Q_n | \bar{Q}_n | S | R | Q_{n+1} |
|---|---|-------|-------------|---|---|-----------|
| 0 | 0 | 0 | 1 | 0 | 0 | 0 |
| 0 | 0 | 1 | 0 | 0 | 0 | 1 |
| 0 | 1 | 0 | 1 | 0 | 1 | 0 |
| 0 | 1 | 1 | 0 | 1 | 0 | 1 |
| 1 | 0 | 0 | 1 | 0 | 0 | 1 |
| 1 | 0 | 1 | 0 | 1 | 0 | 0 |
| 1 | 1 | 0 | 1 | 0 | 1 | 1 |
| 1 | 1 | 1 | 0 | 1 | 1 | 0 |

oscillates b/w 0 & 1 therefore this is called racing condition.

Char Table

| Q_n | J | K | Q_{n+1} |
|-------|---|---|-----------|
| 0 | 0 | 0 | 0 |
| 0 | 0 | 1 | 0 |
| 0 | 1 | 0 | 1 |
| 0 | 1 | 1 | 1 |
| 1 | 0 | 0 | 1 |
| 1 | 0 | 1 | 0 |
| 1 | 1 | 0 | 1 |
| 1 | 1 | 1 | 0 |

$$Q_{n+1} = \bar{Q}_n J + Q_n \bar{K}$$

Excitation Table

| Present state Q_n | Next Q_{n+1} | J | K |
|---------------------|----------------|---|---|
| 0 | 0 | 0 | 0 |
| 0 | 1 | 1 | 0 |
| 1 | 0 | 0 | 1 |
| 1 | 1 | 1 | 0 |

Excitation Table.

| Q_n | Q_{n+1} | J | K |
|-------|-----------|---|---|
| 0 | 0 | 0 | X |
| 0 | 1 | 1 | X |
| 1 | 0 | X | 1 |
| 1 | 1 | X | 0 |

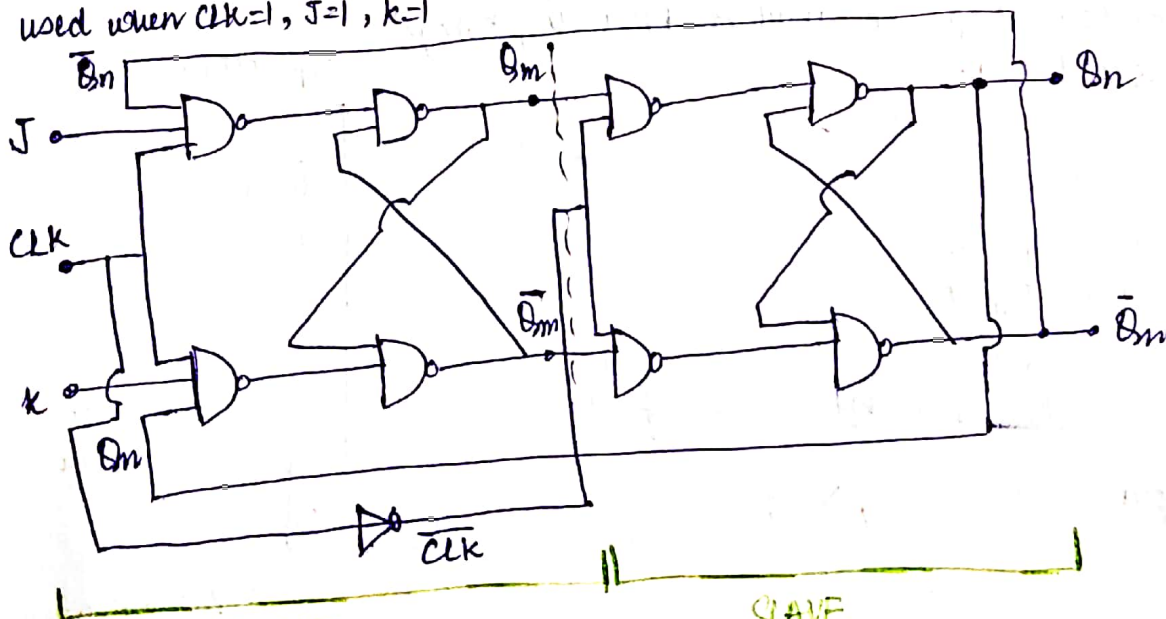
$$J = Q_{n+1}$$

$$K = \bar{Q}_{n+1}$$

- Race Around condition can be removed by
- Important → 1. clock time < Propagation time.
2. Edge triggering. (Master slave JK FF)

MASTER SLAVE JK FF (triggering)

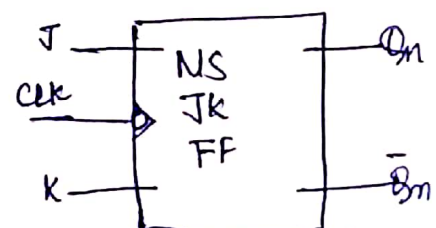
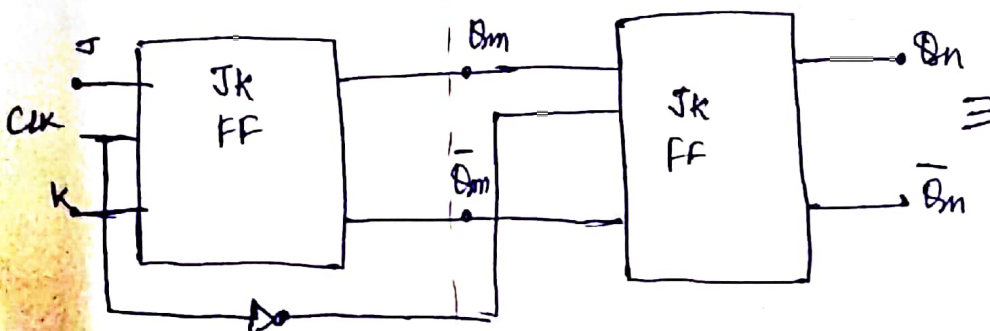
used when CLK=1, J=1, K=1



MASTER

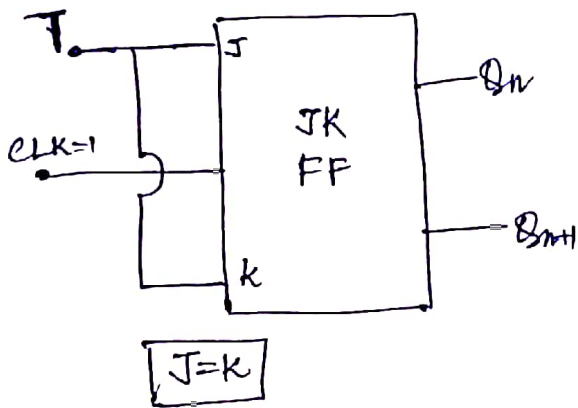
SLAVE

when master is ON slave is OFF and vice versa.



ive edge triggering

T FLIPFLOP (When we have to do only toggling)



| clk | J | K | Q_{n+1} |
|-----|---|---|-------------|
| 0 | X | X | Q_n |
| 1 | 0 | 0 | Q_n |
| 1 | 0 | 1 | 0 |
| 1 | 1 | 0 | 1 |
| 1 | 1 | 1 | \bar{Q}_n |

TRUTH TABLE

| CLK | T | Q_{n+1} |
|-----|---|-------------|
| 0 | X | Q_n |
| 1 | 0 | Q_n |
| 1 | 1 | \bar{Q}_n |

Excitation Table

| Q_n | Q_{n+1} | T |
|-------|-----------|---|
| 0 | 0 | 0 |
| 0 | 1 | 1 |
| 1 | 0 | 1 |
| 1 | 1 | 0 |

Char Table

| Q_n | T | Q_{n+1} |
|-------|---|-----------|
| 0 | 0 | 0 |
| 0 | 1 | 1 |
| 1 | 0 | 1 |
| 1 | 1 | 0 |

FLIP FLOP CONVERSION

1. Identify available & seq. FF.
2. Make excitation table for Available FF.
3. Make char table for seq. FF.
4. Write Boolean exp. for available FF using Kmap.
5. Draw circuit dia.

LVDI

$$E_0 = E_{S1} - E_{S2}$$

$$\text{when } E_{S1} = E_{S2}$$

$$E_0 = 0$$

⇒ Null position

LHS displacement $E_{S1} > E_{S2}$

$$E_0 > 0$$

RHS displacement $E_{S1} < E_{S2}$

$$E_0 < 0$$

