

# Fourier Series 'Properties

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## Properties of the FT

Property	Given FT pair : $x(t) \leftrightarrow X(j\omega)$	Remarks
Linearity	$\checkmark \sum_k \alpha_k x_k(t) \leftrightarrow \sum_k \alpha_k X_k(j\omega)$	
Time shift	$\checkmark x(t-\tau) \leftrightarrow X(j\omega) e^{-j\omega\tau}$	
Time scaling	$\checkmark x(\alpha t) \leftrightarrow \frac{1}{ \alpha } X\left(\frac{j\omega}{\alpha}\right)$	$\alpha \neq 0$ real
Frequency shift	$\checkmark x(t) e^{j\omega_0 t} \leftrightarrow X(j(\omega-\omega_0))$	$\omega_0$ real
Derivative in time $\frac{d}{dt}$	$\checkmark \frac{d x(t)}{dt} \leftrightarrow j\omega X(j\omega)$	
Conjugate symmetry	$x^*(t) \leftrightarrow X^*(-j\omega)$	
Derivative in frequency	$\checkmark t x(t) \leftrightarrow j \frac{d X(j\omega)}{d\omega}$	
Convolution in time	$x(t) * y(t) \leftrightarrow X(j\omega) Y(j\omega)$	卷积
Duality	$X(jt) \leftrightarrow 2\pi x(-\omega)$	
Multiplication in time	$x(t) y(t) \leftrightarrow \frac{1}{2\pi} X(j\omega) * Y(j\omega)$	
Integration in time	$\int_{-\infty}^t x(\tau) d\tau \leftrightarrow \frac{1}{j\omega} X(j\omega) + \pi X(j0) \delta(\omega)$	
<u>Parseval Theorem</u>	$\int_{-\infty}^{+\infty} x(t) y(t) dt = \frac{1}{2\pi} \int_{-\infty}^{+\infty} X(j\xi) Y(j\xi) d\xi$	

$$x[n-n_0] \leftrightarrow X(e^{j\Omega}) e^{-j\Omega n_0}$$

$$e^{j\Omega_0 n} x[n] \leftrightarrow X(e^{j(\Omega-\Omega_0)})$$

$$-jn x[n] \leftrightarrow \frac{dX(e^{j\Omega})}{d\Omega}$$

$$x[-n] \leftrightarrow X(e^{-j\Omega})$$

$$x[n] * y[n] \leftrightarrow X(e^{j\Omega}) Y(e^{j\Omega})$$

$$x[n] y[n] \leftrightarrow \frac{1}{2\pi} \int_{-\pi}^{\pi} X(e^{j\xi}) Y(e^{j(\Omega-\xi)}) d\xi$$

$$x^*[n] \leftrightarrow X^*(e^{-j\Omega})$$