# PStat 131 Final Project 2016 Election

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```
library(tidyverse)
library(plyr)
library(ggplot2)
library(cluster)
library(NbClust)
library(tree)
library(randomForest)
library(maptree)
library(ROCR)
library(class)
library(rpart)
```

### Question 1

There are many reasons as to why predicting the outcome of an election is so hard. One of the main reasons that it is so difficult is that the president is chosen on a national level, but states vote seperately. Another reason is that because no one knows the result untill after it is an un observed variable. The data the polls brings in deals with how people think they'll vote but not how they actually vote. One other reason is that there are many different polls at state and national levels with varying amounts of credibility, yet they all have to be considered. These are all some of the reasons that predicting the election is so difficult.

#### Question 2

Nate Silver did a couple of things that were unique in his approach include a method in which he would calculate the probability that Obama would win if the election was called on that specific day. Another thing that he did that was unique was when he saw a nationwide shift, he would take into account the levels of support that a candidate has in certain regions before applying the shift to those regions.

### Question 3

There were many explanations as to what could have gone wrong in 2016. A few of the explanations given in the article were that while in is normal for polls to have error, in 2016 the error was all in the same direction. Another reason is that the polls may have underestimated a certain demographic, particularly whites without college degrees. This combined with the fact that Trump outperformed almost all of his swing state predictions. One of the issues that relates to why election predicting is to hard is that Democrats had a lower than expected turnout. This relates to how polls gather info on how they think they will vote but not how they will or if they will vote. Some of the things that could be done to make future predictions better could include creating a heavier focus on swing states and making sure to use time scaling to see how the predictions change as time moves on and compare national shifts with state shifts in support.

### **Data Preparing**

```
election.raw = read.csv("election.csv") %>% as.tbl
census_meta = read.csv("metadata.csv", sep = ";") %>% as.tbl
census = read.csv("census.csv") %>% as.tbl
census$CensusTract = as.factor(census$CensusTract)
```

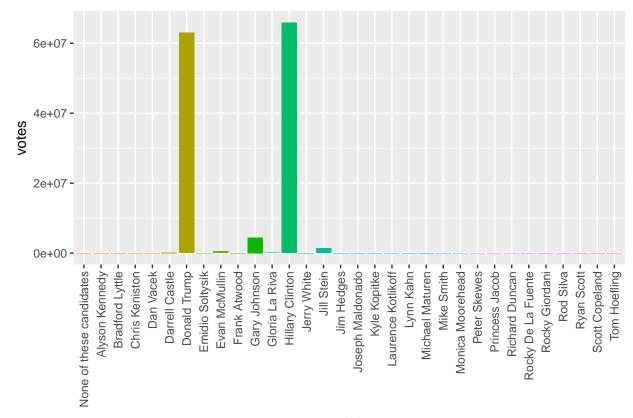
```
election_federal <- subset(election.raw, election.raw$fips=="US")</pre>
election_state <- c()</pre>
for (i in 1:nrow(election.raw)){
  for (j in 1:length(state.abb)){
    if (election.raw$fips[i] == state.abb[j]){
      election_state <- rbind(election_state, election.raw[i,])</pre>
    }
 }
}
abc <- rbind(election_federal, election_state)</pre>
election <- election.raw[!(election.raw$fips %in% abc$fips),]</pre>
head(election_federal)
## # A tibble: 6 x 5
             fips
                          candidate state
##
     county
                                               votes
##
     <fctr> <fctr>
                             <fctr> <fctr>
                                               <int>
## 1
       <NA>
                US
                      Donald Trump
                                        US 62984825
## 2
       <NA>
                US Hillary Clinton
                                        US 65853516
## 3
       <NA>
                US
                       Gary Johnson
                                        US 4489221
## 4
      <NA>
                US
                         Jill Stein
                                        US 1429596
## 5
       <NA>
                US
                     Evan McMullin
                                        US
                                             510002
## 6
       <NA>
                US Darrell Castle
                                        US
                                              186545
head(election_state)
## # A tibble: 6 x 5
##
     county fips
                          candidate state
                                              votes
     <fctr> <fctr>
                             <fctr> <fctr>
                                              <int>
## 1
       <NA>
                CA Hillary Clinton
                                        CA 8753788
## 2
       <NA>
                      Donald Trump
                                        CA 4483810
                CA
## 3
       <NA>
                CA
                       Gary Johnson
                                        CA 478500
       <NA>
                CA
                         Jill Stein
                                        CA 278657
## 5
       <NA>
                CA Gloria La Riva
                                        CA
                                              66101
       <NA>
                                        FL 4617886
                      Donald Trump
head(election)
## # A tibble: 6 x 5
##
                           fips
                                      candidate state
                 county
                                                          votes
##
                 <fctr> <fctr>
                                          <fctr> <fctr>
                                                          <int>
## 1 Los Angeles County
                           6037 Hillary Clinton
                                                     CA 2464364
## 2 Los Angeles County
                           6037
                                   Donald Trump
                                                     CA 769743
```

```
## 3 Los Angeles County
                           6037
                                   Gary Johnson
                                                     CA
                                                           88968
## 4 Los Angeles County
                           6037
                                      Jill Stein
                                                     CA
                                                           76465
## 5 Los Angeles County
                           6037 Gloria La Riva
                                                     CA
                                                           21993
            Cook County
## 6
                          17031 Hillary Clinton
                                                     IL 1611946
```

```
length(election_federal$candidate)
```

#### ## [1] 32

```
ggplot(election_federal, aes(x=candidate, y=votes, fill=candidate)) +
  geom_bar(stat="identity") +
  guides(fill=FALSE) +
  theme(axis.text.x=element_text(angle=90, hjust=1, vjust=0.5))
```



### candidate

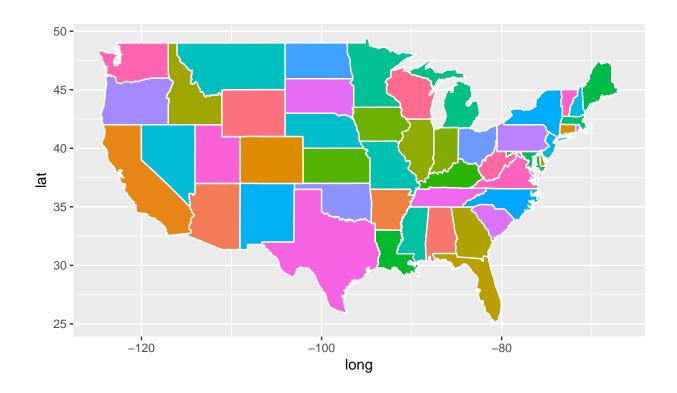
The Graph below shows the names for 31 candidates in the 2016 election. However, it also shows that only 5 of those candidates had enough votes to appear on the graph and of those five almost all of the votes went to Donald Trump or Hillary Clinton.

```
candidate=candidate,
                   pct=votes/sum(votes),
                   state =state,
                   votes=votes,
                   county = county)
county_winner <- pct.county %>%
 group_by(fips) %>%
 top_n(n=1, wt=pct)
head(county_winner)
## # A tibble: 6 x 6
              fips [6]
## # Groups:
##
      fips
                 candidate
                                 pct state votes
                                                              county
##
    <fctr>
                    <fctr>
                               <dbl> <fctr> <int>
                                                              <fctr>
## 1 10001 Donald Trump 0.4981282
                                         DE 36991
                                                         Kent County
## 2 10003 Hillary Clinton 0.6230005
                                         DE 162919 New Castle County
## 3 10005 Donald Trump 0.5916578
                                         DE 62611
                                                       Sussex County
## 4 1001
              Donald Trump 0.7339553
                                         AL 18172
                                                      Autauga County
## 5 1003
              Donald Trump 0.7732042
                                         AL 72883
                                                      Baldwin County
## 6 1005
              Donald Trump 0.5226140
                                         AL 5454
                                                      Barbour County
pct.state <- ddply(election_state,</pre>
                  ~fips,
                  summarise,
                  candidate=candidate,
                  pct=votes/sum(votes))
state_winner <- pct.state %>%
 group_by(fips) %>%
 top_n(n=1, wt=pct)
head(state_winner)
## # A tibble: 6 x 3
## # Groups:
              fips [6]
##
                 candidate
      fips
##
    <fctr>
                    <fctr>
                               <dbl>
## 1
              Donald Trump 0.5280650
        ΑK
## 2
        AL
              Donald Trump 0.6272447
## 3
       AR
              Donald Trump 0.6057410
## 4
       ΑZ
              Donald Trump 0.4903224
## 5
        CA Hillary Clinton 0.6225644
## 6
        CO Hillary Clinton 0.4815698
```

```
states <- map_data("state")

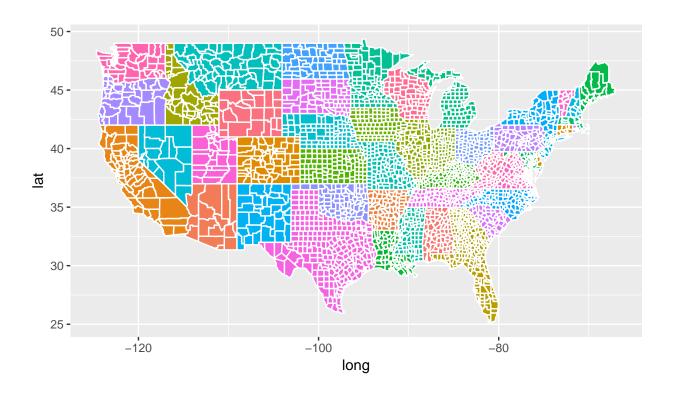
ggplot(data = states) +
  geom_polygon(aes(x = long, y = lat, fill = region, group = group), color = "white") +
  coord_fixed(1.3) +</pre>
```

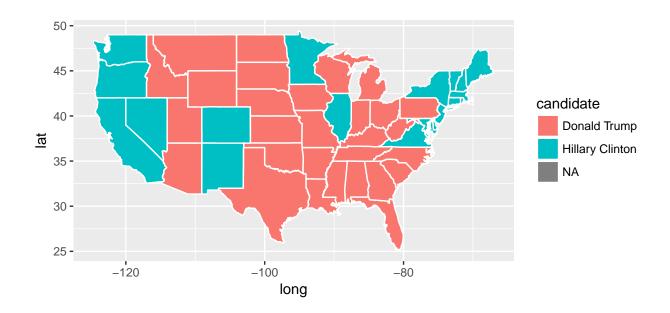
## guides(fill=FALSE)



```
conties <- map_data("county")

ggplot(data=conties) +
  geom_polygon(aes(x=long, y=lat, fill=region, group=group), color="white") +
  coord_fixed(1.3) +
  guides(fill=FALSE)</pre>
```





```
county <- conties

county.split <- maps::county.fips %>%
    separate(polyname, c("region", "subregion"), ",")

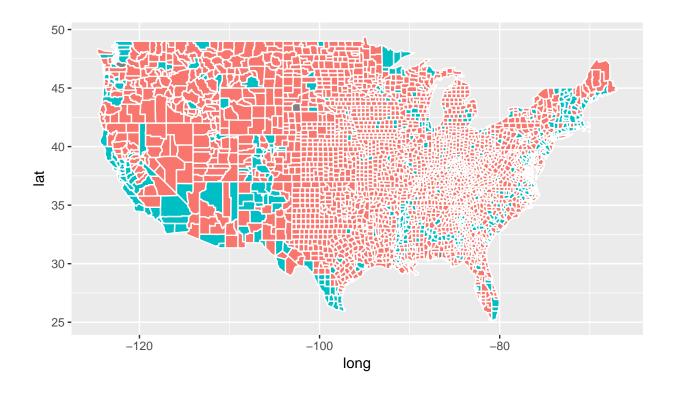
county.split <- cbind(as.character(county.split[,1]), county.split[,2:3])

colnames(county.split)[1] <- "fips"

county2 <- left_join(county, county.split, by=c("region", "subregion"))

county3 <- left_join(county2, county_winner, by="fips")

ggplot(data = county3) +
    geom_polygon(data=county3, aes(x=long, y=lat, fill=candidate, group=group), color = "white") +
    coord_fixed(1.3) +
    guides(fill=FALSE)</pre>
```



We will use the cleaned census data for visualization on question 10, therefore question 10 will appear after question 11.

### Question 11 Part 1

## head(census.del)

```
CensusTract
                   State County TotalPop
                                                 Men Women Hispanic White Black
                                                                     87.4
     1001020100 Alabama Autauga
                                      1948 48.25462
                                                      1008
                                                                0.9
                                                                             7.7
## 2 1001020200 Alabama Autauga
                                      2156 49.11874
                                                      1097
                                                                0.8 40.4 53.3
     1001020300 Alabama Autauga
                                      2968 45.95687
                                                      1604
                                                                0.0
                                                                     74.5
                                                                            18.6
## 4
     1001020400 Alabama Autauga
                                      4423 49.10694
                                                      2251
                                                               10.5
                                                                      82.8
                                                                             3.7
## 5
     1001020500 Alabama Autauga
                                     10763 45.73074
                                                      5841
                                                                0.7
                                                                      68.5
                                                                            24.8
## 6 1001020600 Alabama Autauga
                                      3851 46.40353 2064
                                                               13.1 72.9 11.9
     Native Asian Pacific Citizen Income IncomeErr IncomePerCap
## 1
        0.3
              0.6
                      0.0 77.15606
                                     61838
                                                11900
                                                             25713
## 2
        0.0
              2.3
                      0.0 77.08720
                                     32303
                                                13538
                                                             18021
## 3
        0.5
              1.4
                      0.3 78.67251
                                     44922
                                                5629
                                                             20689
## 4
        1.6
              0.0
                      0.0 74.74565
                                     54329
                                                7003
                                                             24125
## 5
        0.0
              3.8
                      0.0 71.22549
                                     51965
                                                 6935
                                                             27526
## 6
                      0.0 68.60556
        0.0
              0.0
                                     63092
                                                 9585
                                                             30480
     IncomePerCapErr Poverty ChildPoverty Professional Service Office
## 1
                4548
                         8.1
                                       8.4
                                                    34.7
                                                            17.0
                                                                    21.3
## 2
                2474
                         25.5
                                      40.3
                                                    22.3
                                                            24.7
                                                                    21.5
## 3
                2817
                                      19.7
                                                            24.9
                                                                   22.1
                         12.7
                                                    31.4
## 4
                2870
                                                    27.0
                                                            20.8
                          2.1
                                       1.6
                                                                    27.0
## 5
                                                    49.6
                2813
                         11.4
                                      17.5
                                                            14.2
                                                                    18.2
## 6
                7550
                         14.4
                                      21.9
                                                    24.2
                                                            17.5
                                                                    35.4
##
     Production Drive Carpool Transit OtherTransp WorkAtHome MeanCommute
## 1
           15.2 90.2
                          4.8
                                     0
                                               2.3
                                                           2.1
                                                                       25.0
## 2
           22.0 86.3
                                     0
                                               0.7
                                                           0.0
                                                                       23.4
                          13.1
## 3
           12.4 94.8
                          2.8
                                     0
                                               0.0
                                                           2.5
                                                                       19.6
## 4
           16.4 86.6
                          9.1
                                     0
                                               2.6
                                                           1.6
                                                                       25.3
## 5
           15.8 88.0
                          10.5
                                     0
                                               0.6
                                                           0.9
                                                                       24.8
## 6
           14.9
                 82.7
                           6.9
                                     0
                                                6.0
                                                           4.5
                                                                       19.8
     Employed PrivateWork SelfEmployed FamilyWork Unemployment Minority
##
## 1 48.40862
                     77.1
                                    4.6
                                                 0
                                                             5.4
## 2 34.92579
                     77.0
                                    6.1
                                                  0
                                                            13.3
                                                                      56.4
## 3 46.26011
                      64.1
                                   12.3
                                                  0
                                                             6.2
                                                                      20.8
## 4 40.28940
                     75.7
                                    3.1
                                                  0
                                                            10.8
                                                                      15.8
## 5 46.79922
                      67.1
                                    5.3
                                                  0
                                                             4.2
                                                                      29.3
## 6 40.50896
                     79.4
                                    5.8
                                                  0
                                                            10.9
                                                                      25.0
```

### Question 11 Part 2

```
census.del2 <- census.del %>%
  group_by(State, County) %>%
  add_tally(sum(TotalPop))

names(census.del2)[names(census.del2)=="n"] <- "CountyTotal"

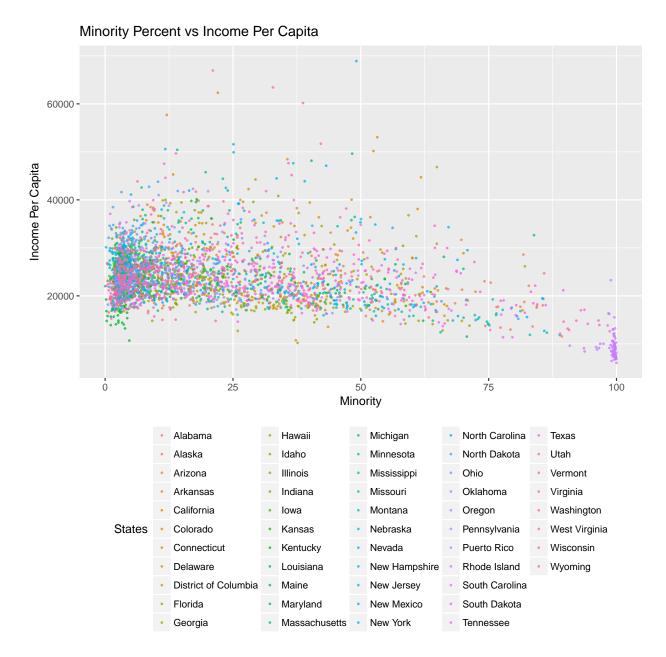
Weight <- census.del2$TotalPop/census.del2$CountyTotal

census.subct <- data.frame(census.del2, Weight)</pre>
```

### Question 11 Part 3 & 4

```
census.ct <- census.subct %>%
  group_by(State, County) %>%
  summarise_at(vars(TotalPop:Weight), mean)
head(census.ct)
## # A tibble: 6 x 36
## # Groups: State [1]
      State County TotalPop
                                                                      Black
##
                                          Women Hispanic
                                                            White
                                   Men
      <fctr> <fctr>
                        <dbl>
                                 <dbl>
                                          <dbl>
                                                   <dbl>
                                                            <dbl>
                                                                      <dbl>
## 1 Alabama Autauga 4601.750 48.36759 2373.000 2.850000 73.15000 20.825000
## 2 Alabama Baldwin 6294.226 48.82690 3219.581 4.064516 83.45484 9.625806
## 3 Alabama Barbour 2992.444 52.22358 1381.667 4.800000 46.61111 46.488889
## 4 Alabama
                Bibb 5651.000 53.24573 2632.750 2.475000 77.50000 17.725000
## 5 Alabama Blount 6412.222 49.53062 3244.222 8.888889 87.80000 1.355556
## 6 Alabama Bullock 3559.333 51.78404 1672.667 2.766667 22.00000 72.466667
## # ... with 28 more variables: Native <dbl>, Asian <dbl>, Pacific <dbl>,
      Citizen <dbl>, Income <dbl>, IncomeErr <dbl>, IncomePerCap <dbl>,
      IncomePerCapErr <dbl>, Poverty <dbl>, ChildPoverty <dbl>,
      Professional <dbl>, Service <dbl>, Office <dbl>, Production <dbl>,
      Drive <dbl>, Carpool <dbl>, Transit <dbl>, OtherTransp <dbl>,
## #
## #
      WorkAtHome <dbl>, MeanCommute <dbl>, Employed <dbl>,
      PrivateWork <dbl>, SelfEmployed <dbl>, FamilyWork <dbl>,
## #
      Unemployment <dbl>, Minority <dbl>, CountyTotal <dbl>, Weight <dbl>
```

```
ggplot() + geom_point(data = census.ct, aes(Minority, IncomePerCap,color = census.ct$State), size = .5,
```



The Scatterplot above shows the Income per Capita compared to the percentage of the population that are minorities. Each point represents a unique county within either a state, DC, or Puerto Rico. We can see that there is some slight correlation between income and percentage of minorities. The higher the percentage of minorities the less income per capita in a county.

```
census.subct2 <- census.subct[, 4:ncol(census.subct)]
pc.census.subct <- prcomp(census.subct2)
pc.subct <- pc.census.subct$x
subct.pc <- data.frame(pc.subct)
head(subct.pc)</pre>
```

```
PC1
                    PC2
                                PC3
                                           PC4
                                                      PC5
               4871.206 3758.05874 -3466.8919 -2906.0191 -1174.5827
## 1 -1041580
## 2 -1041625 -24805.729 -1998.73551 -7734.2190 -1527.2696
## 3 -1041609 -13257.720
                         2080.65654
                                    1126.5607 -1622.6782
                                                          -232.5840
## 4 -1041594
              -3181.689
                         3111.09445
                                      940.5835
                                               -188.9382
                                                            -36.0470
## 5 -1041595
              -3814.383
                         -244.61498
                                    1964.2855
                                               7370.8815
                                                           512.2022
                                     -290.0689
## 6 -1041577
               7901.386
                          -71.85555
                                               -776.5284 -3393.2172
##
           PC7
                     PC8
                                PC9
                                         PC10
                                                    PC11
                                                              PC12
## 1
     42.652629 -45.71414
                          -2.706350 7.273573 -10.700236
                                                          1.090680
## 2
      1.070415 22.66795 -31.879474 22.845329
                                                3.493737
                                                          2.624855
     93.022695 -26.46305 -10.223634 13.016356
                                              -7.732274
                                                         -9.247962
      8.686037 -30.66701
                           4.255256 6.301381 -16.710345
                                                          7.095454
## 5 302.961977 -14.07746 -19.345572 6.434501
                                              -4.971781 -12.574450
                                                3.263702
## 6 115.689192 -23.32654
                           2.959755 6.098167
                                                          8.913942
##
          PC13
                     PC14
                                 PC15
                                           PC16
                                                      PC17
## 1 0.4164734 -3.0482889
                           -0.1441516 -1.756269
                                                 -4.636772 -1.9629464
                          -1.2536464 -2.577693
## 2 -1.8681576 5.7749187
                                               -1.734599 1.7615628
     4.1242753
               4.3483050
                          -2.7263015 5.415055 -12.180391 -5.1936642
     6.2128913 8.9694762
                            1.8201036 -1.305101
                                                 2.699007 -4.1159591
     2.1727623
                0.7537019 -11.4399572 -7.741069
                                                -7.391125 2.2823116
## 6
     1.8355572 3.1849597
                            3.0792899 3.025831
                                                  3.283700 0.1581135
           PC19
                      PC20
                                  PC21
                                             PC22
                                                        PC23
     3.87709301 2.4218958 0.03079033 1.0601141 0.06426869 -1.1212229
     3.36291103 -1.3155632 -2.32066332 -2.4246190
                                                 1.87874047 -1.5626241
    2.57264634 5.0372218 -5.40127878 -0.1350388 -1.41132137 0.2037725
     0.08042313 2.2837875 0.57637364 -2.1532622 3.26812968 2.1837067
     3.99756155 -0.2326278 -2.49299335 -1.6770415 3.80502301 -2.4951940
## 6 -8.79351038 7.4114772 -3.32864202 0.9402121 -0.82388741
                                                              2.5657114
                    PC26
                               PC27
                                          PC28
                                                      PC29
                                                                PC30
         PC25
## 1 -1.823366 -1.4741706 -0.1555711 -0.5348014 -1.28682674 0.1866775
    1.536534 -0.9194317
                         ## 3 2.667171 -0.8490568
                         1.5054519 0.0339869 -1.87956938 -0.9490494
## 4 -3.765097 -0.7575186
                         1.3968121 -0.1519115 0.94387612 0.4477034
## 5 -1.191036 0.2201392
                         1.3055341 3.4574611 2.60857296 -0.2131685
## 6 -3.115814 -2.5947006
                         1.9492875 -0.7007477 -0.09863811 1.9597324
           PC31
                     PC32
                                 PC33
                                               PC34
## 1 -0.29065743 0.1580542 -0.02151739
                                      1.824720e-12
## 2 -0.32303102 0.1543218 -0.02770026 3.366201e-12
## 3 -0.29565888 0.2484390 -0.05287911
                                      4.747033e-12
## 4 -0.02084545 0.1602690 0.02638878 -8.466301e-13
## 5 0.03668122 0.1446216 0.08854063 -4.456397e-12
## 6 -0.24337700 0.1885632 0.04439608 -2.799975e-12
summary(pc.census.subct)
## Importance of components:
##
                               PC1
                                         PC2
                                                   PC3
                                                             PC4
                                                                 PC5
                                                                      PC6
                         1.927e+06 3.154e+04 7.708e+03 4.488e+03 2235 1527
## Standard deviation
## Proportion of Variance 9.997e-01 2.700e-04 2.000e-05 1.000e-05
## Cumulative Proportion 9.997e-01 1.000e+00 1.000e+00 1.000e+00
                                                                   1
                                 PC8
                                       PC9 PC10 PC11 PC12 PC13 PC14
```

1.0 1.00

1.00 1.00 1.00 1.00 1.000 1.000

PC15 PC16 PC17 PC18 PC19 PC20 PC21 PC22 PC23

## Standard deviation

##

## Proportion of Variance

## Cumulative Proportion

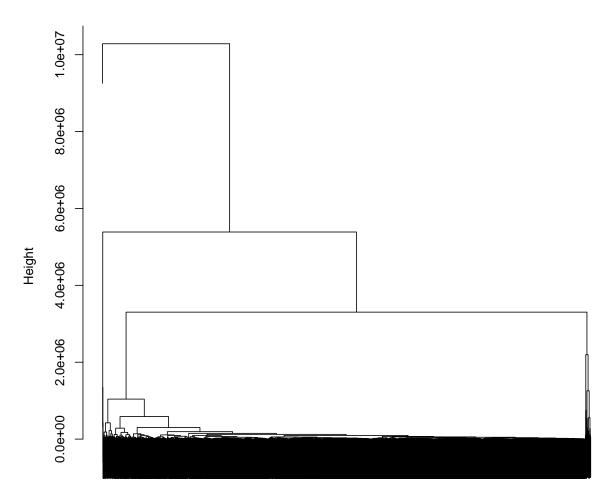
```
7.221 6.887 6.383 6.053 5.625 5.09 4.765 4.23 3.861
## Standard deviation
PC24 PC25 PC26 PC27 PC28 PC29 PC30 PC31
##
## Standard deviation
                        3.499 2.878 2.432 2.123 1.876 1.842 1.533 0.995
## Proportion of Variance 0.000 0.000 0.000 0.000 0.000 0.000 0.000 0.000
## Cumulative Proportion 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000
                         PC32
                                PC33
                                         PC34
## Standard deviation
                        0.4477 0.0826 1.913e-10
## Proportion of Variance 0.0000 0.0000 0.000e+00
## Cumulative Proportion 1.0000 1.0000 1.000e+00
census.ct2 <- census.ct[, 3:ncol(census.ct)]</pre>
pc.census.ct <- prcomp(census.ct2)</pre>
pc.ct <- pc.census.ct$x</pre>
ct.pc <- data.frame(pc.ct)
head(ct.pc)
##
          PC1
                   PC2
                              PC3
                                       PC4
                                                  PC5
                                                           PC6
                                                                    PC7
     43802.85 -3768.187
## 1
                         956.17081
                                  834.6755
                                             439.5024
                                                     393.4899 -72.02159
## 2 -96086.83 -1949.164 -1407.48258 1962.8070
                                           2691.3329 -376.1157 -20.78861
## 3
     72330.85 15110.277
                         415.48296
                                   251.6863 -1061.2769
                                                      108.7560 89.97443
     76558.18 7130.621
                       2440.91707 366.3961
                                           1442.2920 873.8584 158.22626
## 5
                       3488.76356 2355.4039 1717.2446 -976.0526 -19.31670
     41387.49 2338.540
## 6
     88561.91 13381.289
                         85.34153 2902.7391
                                            -667.8090 189.0576 84.96449
##
          PC8
                    PC9
                                PC10
                                         PC11
                                                   PC12
                                                              PC13
                                              3.7790706 6.0811096
## 1 11.06519
             12.879906
                        -2.382204497 -3.017225
    19.38906
              -2.642667
                         2.668046988 -2.489090 0.6712149 5.0424223
## 3 -27.61447 42.512467 -10.923271230 6.456375 -0.3036778 -0.4747089
     25.63285
             13.997325
                        -5.201966723 -2.938133 -3.2878290 -1.1929414
    34.00864 -11.866322
                         0.009722318 2.440199 -1.4830869 -1.6024197
## 6 -46.63262 66.509284 -11.371209541 -5.578639 -3.7088213 -9.2074075
         PC14
                   PC15
                             PC16
                                       PC17
                                                 PC18
##
                                                            PC19
     1.943107 -0.4015538 -0.6038176 -1.1364789
                                             0.7887315 0.5340313
    1.376539 2.2835389 -0.6342368 1.3840665
                                            1.5542532 -2.3711436
## 3 -1.956219 -4.3949189 1.9926756 -0.9144222 -1.6299579 -4.3098216
    6.635150 -5.2397779 1.9151465 -2.0950941 -0.5792294 2.3356183
     5.144780 -4.0789245 4.0650116 2.1729609 0.2900468 -0.2518585
     6.353620 -2.2289188 4.7625717 -1.3721596 2.2848686 -5.3523539
          PC20
                     PC21
                               PC22
                                         PC23
                                                    PC24
## 1 -1.8691793 -1.19418415 -0.3490629 0.5739089 -0.68668924 1.1258399
## 2 0.5804598 -0.64851699 0.1312563 0.6994323 0.19123323 0.3838623
## 3 -1.7283747 0.09778255 -0.6657844 -0.5217046 -2.94098089 1.6349367
## 4 1.4364446 1.57220213 1.0475415 1.3356205 -2.52093514 0.2697769
               0.10223120 1.5710080 2.6038253 0.01425523 0.9747514
## 5 -0.2102285
    1.0349583 3.90691257 -1.0631081 -0.8713284 -1.75527086 1.5832893
## 6
##
           PC26
                     PC27
                                PC28
                                           PC29
                                                      PC30
    0.07373209 -0.7068069 -0.07896022 -0.03368132 0.07168155 0.12586516
## 2 -0.14366015
                0.2908329
                          0.30601277 -0.66634961
                                                0.23300221 -0.21740424
## 3 -0.13617586 -0.1407877 -0.23188336 -0.54716108 0.12116239 0.03435296
               1.6516710 0.01554409 0.55166212 -0.22141516 -0.66782586
## 4 1.83083127
                ## 5 -0.54174595
                1.8474901 -0.11320995 0.12284482 -0.14257318 0.16610582
## 6 -0.53114429
##
           PC32
                       PC33
                                    PC34
## 1 0.037438506 0.04004560 1.416653e-12
```

```
## 2 -0.008856174 0.01129161 -1.672304e-12
## 3 -0.021916611 0.14735162 6.391634e-12
## 4 0.127951003 0.03343784 -1.145152e-11
## 5 -0.080443829 -0.02651660 2.796080e-13
## 6 0.024677783 -0.05266250 -5.861206e-13
summary(pc.census.ct)
## Importance of components:
##
                              PC1
                                       PC2
                                                PC3
                                                          PC4
                                                                   PC5
## Standard deviation
                        3.179e+05 1.407e+04 2.678e+03 2.022e+03 1.204e+03
## Proportion of Variance 9.979e-01 1.960e-03 7.000e-05 4.000e-05 1.000e-05
## Cumulative Proportion 9.979e-01 9.999e-01 9.999e-01 1.000e+00 1.000e+00
##
                               PC7
                                     PC8
                                           PC9 PC10 PC11 PC12 PC13
                          PC6
## Standard deviation
                        662.9 83.44 30.05 16.94 10.53 7.442 6.879 5.974
                          0.0 0.00 0.00 0.00 0.00 0.000 0.000 0.000
## Proportion of Variance
## Cumulative Proportion
                          1.0 1.00 1.00 1.00 1.00 1.000 1.000 1.000
##
                         PC14 PC15 PC16 PC17 PC18 PC19 PC20 PC21
## Standard deviation
                        5.152 4.575 3.774 3.335 3.238 2.967 2.6 2.553
## Proportion of Variance 0.000 0.000 0.000 0.000 0.000 0.000 0.000
##
                         PC22 PC23 PC24 PC25 PC26 PC27 PC28
## Standard deviation
                        2.244 2.212 1.867 1.845 1.627 1.444 1.049 0.8689
## Proportion of Variance 0.000 0.000 0.000 0.000 0.000 0.000 0.000 0.000
## Cumulative Proportion 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000
                                PC31
                                       PC32
                                             PC33
##
                          PC30
                                                       PC34
## Standard deviation
                        0.7898 0.3905 0.3302 0.1663 3.136e-11
## Proportion of Variance 0.0000 0.0000 0.0000 0.0000 0.000e+00
## Cumulative Proportion 1.0000 1.0000 1.0000 1.0000 1.000e+00
```

The most Prominent Loadings are PC1 and PC2.

```
dist.census.ct <- dist(census.ct, method="euclidean")
hc.census.ct <- hclust(dist.census.ct, method="complete")
plot(hc.census.ct, main="HClust census.ct", labels = FALSE)</pre>
```

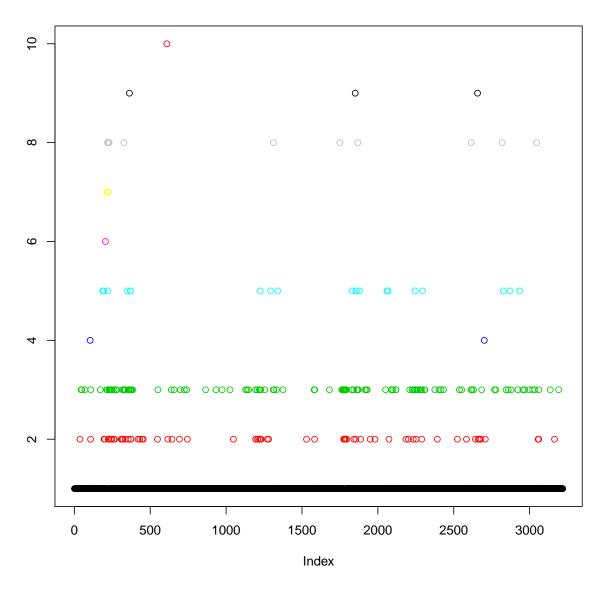
## **HClust census.ct**



dist.census.ct hclust (\*, "complete")

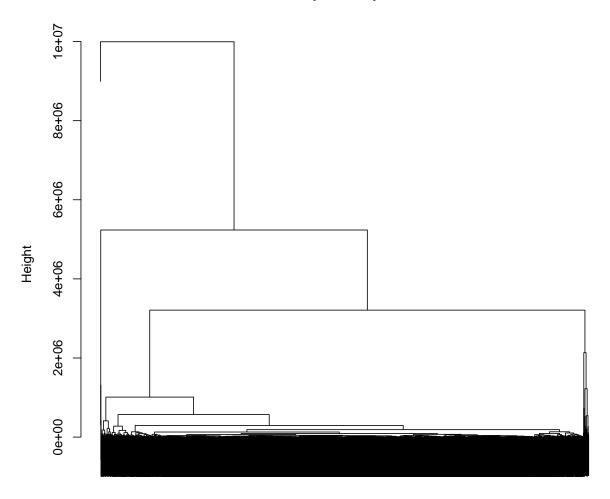
```
hc.census.cut <- cutree(hc.census.ct, 10)
plot(hc.census.cut, col=hc.census.cut, ylab = "", main = "Cut Tree census.ct")</pre>
```

### **Cut Tree census.ct**



```
repeat.census.ct <- ct.pc[,1:5]
repeat.dist.census.ct <- dist(repeat.census.ct, method="euclidean")
repeat.hc.census.ct <- hclust(repeat.dist.census.ct, method="complete")
plot(repeat.hc.census.ct, main="5 Principal Components", labels = FALSE)</pre>
```

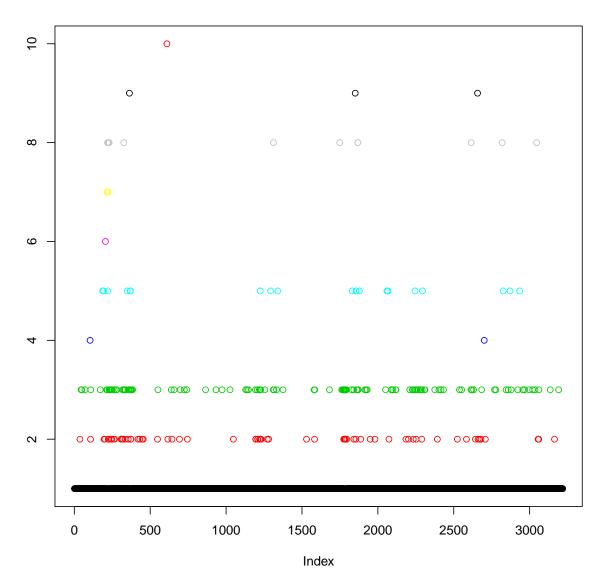
# **5 Principal Components**



repeat.dist.census.ct hclust (\*, "complete")

```
repeat.hc.census.cut <- cutree(repeat.hc.census.ct, 10)
plot(repeat.hc.census.cut, col=repeat.hc.census.cut, ylab = "", main="Cut Tree 5 PCs")</pre>
```

### **Cut Tree 5 PCs**



### San Mateo clusters

```
census.ct[which(census.ct$County == "San Mateo") ,]
## # A tibble: 1 x 36
## # Groups:
               State [1]
##
                   County TotalPop
                                              Women Hispanic
          State
                                                                 White
                                        Men
##
         <fctr>
                   <fctr>
                             <dbl>
                                      <dbl>
                                               <dbl>
                                                        <dbl>
                                                                 <dbl>
## 1 California San Mateo 4813.348 49.19307 2445.29 23.43871 43.61097
## # ... with 29 more variables: Black <dbl>, Native <dbl>, Asian <dbl>,
       Pacific <dbl>, Citizen <dbl>, Income <dbl>, IncomeErr <dbl>,
       IncomePerCap <dbl>, IncomePerCapErr <dbl>, Poverty <dbl>,
```

```
## #
       ChildPoverty <dbl>, Professional <dbl>, Service <dbl>, Office <dbl>,
## #
       Production <dbl>, Drive <dbl>, Carpool <dbl>, Transit <dbl>,
## #
       OtherTransp <dbl>, WorkAtHome <dbl>, MeanCommute <dbl>,
       Employed <dbl>, PrivateWork <dbl>, SelfEmployed <dbl>,
## #
## #
       FamilyWork <dbl>, Unemployment <dbl>, Minority <dbl>,
## #
       CountyTotal <dbl>, Weight <dbl>
repeat.hc.census.cut[which(census.ct$County == "San Mateo")]
## [1] 2
#census.ct[which(hc.census.cut==2),]
#census.ct[which(repeat.hc.census.cut==2),]
```

According to the result, we can see that in both census.ct and repeated with first 5 PCs in ct.pc, San Mateo county is in the same cluster. In this case, we can conclude that whether or not we are using the original data set or the data set with principle components, San Mateo county has similar features as other counties in the same clusters in both cases.

By observing the result of two lines of code with "#"(since each contains 69 rows of dataframe, we will not print that out), we can assume that the similar features are total populations and employment information. Therefore, the first 5 PCs may have already contained those features for clustering which will result in the same clustering in both cases.

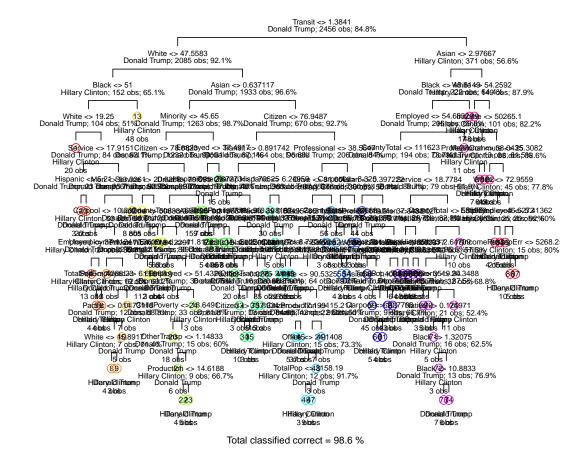
#### Classification

```
tmpwinner <- county_winner %>% ungroup %>%
  mutate(state = state.name[match(state, state.abb)]) %>%
  mutate_at(vars(state, county), tolower) %>%
  mutate(county = gsub(" county| columbia| city| parish", "", county))
census.ct$State <- tolower(census.ct$State)</pre>
tmpcensus <- census.ct %>%
 mutate_at(vars(1, 2), tolower)
election.cl <- tmpwinner %>%
  left_join(tmpcensus, by = c("state"="State", "county"="County")) %>%
  na.omit
attr(election.cl, "location") <- election.cl %>%
  select(c(county, fips, state, votes, pct))
election.cl <- election.cl %>%
  select(-c(county, fips, state, votes, pct))
set.seed(10)
n = nrow(election.cl)
in.trn <- sample.int(n, 0.8*n)</pre>
trn.cl <- election.cl[in.trn,]</pre>
tst.cl <- election.cl[-in.trn,]
set.seed(20)
nfold <- 10
```

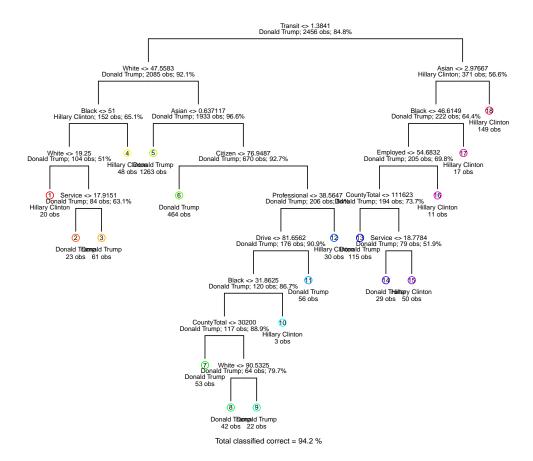
```
folds <- sample(cut(1:nrow(trn.cl), breaks=nfold, labels=FALSE))
calc_error_rate <- function(predicted.value, true.value){
   return(mean(true.value!=predicted.value))
}
records <- matrix(NA, nrow=3, ncol=2)
colnames(records) <- c("train.error","test.error")
rownames(records) <- c("tree","knn","lda")</pre>
```

### Question another 13

```
trntree <- tree(candidate~., data = trn.cl)</pre>
trncontrol <- tree.control(nobs=2456, minsize = 7, mindev = 1e-6)</pre>
trntree <- tree(candidate~., data = trn.cl, control = trncontrol)</pre>
summary(trntree)
##
## Classification tree:
## tree(formula = candidate ~ ., data = trn.cl, control = trncontrol)
## Variables actually used in tree construction:
## [1] "Transit"
                           "White"
                                             "Black"
## [4] "Service"
                           "Hispanic"
                                             "Men"
## [7] "Carpool"
                           "Employed"
                                             "TotalPop"
## [10] "Unemployment"
                           "SelfEmployed"
                                             "Pacific"
## [13] "Asian"
                           "Minority"
                                             "Citizen"
## [16] "Income"
                                             "Drive"
                           "PrivateWork"
## [19] "CountyTotal"
                           "ChildPoverty"
                                             "OtherTransp"
## [22] "Production"
                           "FamilyWork"
                                             "Professional"
## [25] "Office"
                           "WorkAtHome"
                                             "Poverty"
                           "MeanCommute"
## [28] "Native"
                                             "IncomePerCapErr"
## Number of terminal nodes: 87
## Residual mean deviance: 0.05358 = 126.9 / 2369
## Misclassification error rate: 0.01425 = 35 / 2456
draw.tree(trntree, nodeinfo=TRUE, cex=.6)
```



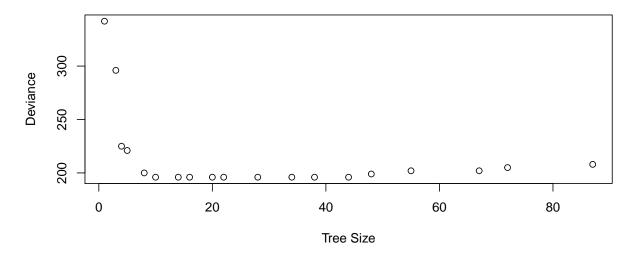
```
prunedtree <- prune.tree(trntree,best=15)</pre>
summary(prunedtree)
##
## Classification tree:
## snip.tree(tree = trntree, nodes = c(34L, 98L, 738L, 99L, 47L,
## 739L, 10L, 48L, 22L, 35L, 7L))
## Variables actually used in tree construction:
                                                      "Service"
##
  [1] "Transit"
                       "White"
                                       "Black"
##
   [5] "Asian"
                       "Citizen"
                                       "Professional" "Drive"
##
  [9] "CountyTotal" "Employed"
## Number of terminal nodes: 18
## Residual mean deviance: 0.317 = 772.9 / 2438
## Misclassification error rate: 0.05782 = 142 / 2456
```



```
good.test <- tst.cl$candidate
cvtree <- cv.tree(trntree,rand=folds,prune.misclass, K=9)

op <- par(mfrow = c(2,1))
plot(cvtree$size,cvtree$dev, xlab = "Tree Size", ylab = "Deviance", main = "Tree Size Deviance")
par(op)</pre>
```

## **Tree Size Deviance**



```
# best size is 23
trntree.pruned <- prune.tree(trntree,best=23)

predictions <- predict(trntree.pruned, trn.cl, type="vector")
for (i in 1:2456){
    d = predictions[i,7]
    predictions[i,7] <- ifelse(d < 0.5,'Hillary Clinton','Donald Trump')
}

c = list()
for (i in 1:2456){
    c[[length(c)+1]] <- predictions[i,7]
}</pre>
```

```
tree.train.error <- calc_error_rate(c, trn.cl$candidate)</pre>
predictions2 <- predict(trntree.pruned, tst.cl, type="vector")</pre>
for (i in 1:614){
  d = predictions2[i,7]
  predictions2[i,7] <- ifelse(d < 0.5, 'Hillary Clinton', 'Donald Trump')</pre>
d = list()
for (i in 1:614){
  d[[length(d)+1]] <- predictions2[i,7]</pre>
}
tree.test.error <- calc_error_rate(d, tst.cl$candidate)</pre>
records[1,] <- c(tree.train.error, tree.test.error)</pre>
records
        train.error test.error
## tree 0.04845277 0.09446254
## knn
                  NA
                              NA
## lda
                  NA
                              NA
```

```
set.seed(20)
nfold <- 10
folds <- sample(cut(1:nrow(trn.cl), breaks=nfold, labels=FALSE))</pre>
kvec \leftarrow c(1, seq(10, 50, length.out=9))
do.chunk <- function(chunkid, folddef, Xdat, Ydat, k){</pre>
  train = (folddef!=chunkid)
  Xtr = Xdat[train,]
  Ytr = Ydat[train]
  Xvl = Xdat[!train,]
  Yvl = Ydat[!train]
  predYtr = knn(train = Xtr, test = Xtr, cl = Ytr, k = k)
  predYvl = knn(train = Xtr, test = Xvl, cl = Ytr, k = k)
  data.frame(train.error = calc_error_rate(predYtr, Ytr),
             val.error = calc error rate(predYvl, Yvl))
}
avg.train.error.vec <- c()</pre>
avg.test.error.vec <- c()</pre>
for(i in 1:10) {
  a = ldply(1:9,
             do.chunk,
             folddef=folds,
             Xdat= dplyr::select(trn.cl,-candidate),
```

```
Ydat= trn.cl$candidate,
            k=kvec[i])
  avg.train.error = (a[1,1]+a[2,1]+a[3,1]+a[4,1]+a[5,1]+a[6,1]+a[7,1]+a[8,1]+a[9,1])/9
  avg.test.error = (a[1,2]+a[2,2]+a[3,2]+a[4,2]+a[5,2]+a[6,2]+a[7,2]+a[8,2]+a[9,2])/9
  avg.train.error.vec = c(avg.train.error.vec, avg.train.error)
  avg.test.error.vec = c(avg.test.error.vec, avg.test.error)
knn.test.error <- min(avg.test.error.vec)</pre>
knn.train.error <- avg.train.error.vec[which.min(avg.test.error.vec)]</pre>
records[2,] <- c(knn.train.error, knn.test.error)</pre>
records
##
        train.error test.error
## tree 0.04845277 0.09446254
## knn 0.11400409 0.11628413
## lda
                 NA
```

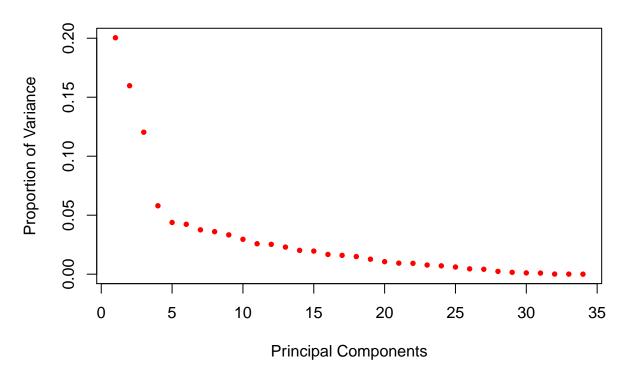
```
pca.records <- matrix(NA, nrow=3, ncol=2)</pre>
colnames(pca.records) <- c("train.error", "test.error")</pre>
rownames(pca.records) <- c("tree", "knn", "lda")</pre>
election.cl2 <- select(election.cl,-candidate)</pre>
election.cl2$TotalPop <- as.numeric(election.cl2$TotalPop)</pre>
election.cl2 <- scale(election.cl2)</pre>
election.cl.pca <- prcomp(election.cl2)</pre>
str(election.cl.pca)
## List of 5
## $ sdev
            : num [1:34] 2.61 2.33 2.02 1.4 1.22 ...
## $ rotation: num [1:34, 1:34] -0.0496 0.0261 -0.0484 -0.041 0.1841 ...
   ..- attr(*, "dimnames")=List of 2
     ....$ : chr [1:34] "TotalPop" "Men" "Women" "Hispanic" ...
    ....$ : chr [1:34] "PC1" "PC2" "PC3" "PC4" ...
##
## $ center : Named num [1:34] 5.15e-17 -1.55e-15 -1.33e-16 -2.13e-17 -1.28e-18 ...
## ..- attr(*, "names")= chr [1:34] "TotalPop" "Men" "Women" "Hispanic" ...
## $ scale : Named num [1:34] 1213.38 2.06 614.12 13.31 19.39 ...
   ..- attr(*, "names")= chr [1:34] "TotalPop" "Men" "Women" "Hispanic" ...
## $ x : num [1:3070, 1:34] -0.535 1.924 1.682 -0.545 0.271 ...
## ..- attr(*, "dimnames")=List of 2
     .. ..$ : NULL
##
    ....$ : chr [1:34] "PC1" "PC2" "PC3" "PC4" ...
## - attr(*, "class")= chr "prcomp"
sum.ele.pca <- summary(election.cl.pca)</pre>
sum.var <- 0
for (i in 1:34){
  sum.var = sum.ele.pca$importance[2,i] + sum.var
  if (sum.var>0.9){
   print(i)
   break
```

```
}

## [1] 17

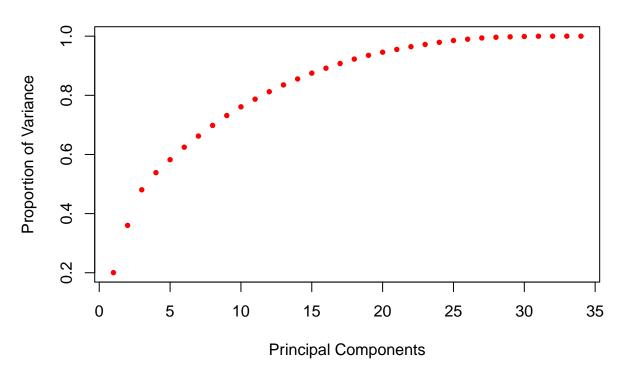
var.pca <- election.cl.pca$sdev^2
proportion <- var.pca/sum(var.pca)
plot(proportion,
    main = "Prop of Var by Number of PCs",
    xlab = "Principal Components",
    ylab = "Proportion of Variance",
    pch = 16,
    cex = .75,
    col='red')</pre>
```

# **Prop of Var by Number of PCs**



```
Cproportion <- cumsum(var.pca)/sum(var.pca)
plot(Cproportion,
    main = "Cumulative Prop of Var by Number of PCs",
    xlab = "Principal Components",
    ylab = "Proportion of Variance",
    pch=16,
    cex = .75,
    col='red')</pre>
```

## **Cumulative Prop of Var by Number of PCs**



Looking at the summary of the PCA matrix we can see that the minimum number of Principal Components in order to accout for 90% of the total variance is 17.

### Question 16

## 942 Donald Trump -0.9662062

## 1310 Donald Trump 1.1819360

## 2126 Donald Trump -2.1549878

## 262

Donald Trump -2.1833761

```
df.election.pca.x <- as.data.frame(election.cl.pca$x)</pre>
data.pca <- cbind(election.cl$candidate, df.election.pca.x)</pre>
data.pca <- as.data.frame(data.pca)</pre>
names(data.pca)[1] <- "candidate"</pre>
set.seed(10)
n <- nrow(data.pca)</pre>
in.trn <- sample.int(n, 0.8*n)</pre>
tr.pca <- data.pca[in.trn,]</pre>
test.pca <- data.pca[-in.trn,]</pre>
head(tr.pca)
                                                        PC3
##
            candidate
                               PC1
                                            PC2
                                                                     PC4
                                                                                   PC5
## 1558 Donald Trump -5.3041389 -0.8597815 -3.9675468 -3.1957783 -0.08047004
```

0.3852831 -0.5765413

## 691 Donald Trump 1.1790534 0.2997215 1.3729761 0.4051871 0.63029585

0.5149412 0.9165879 1.3590921 0.31156203

0.6409613 2.6441019 -1.5220651 -0.15204084 3.6317331 -8.4591013 1.7221043 1.02262677

1.0240136 -0.86382767

```
PC6
                      PC7
                              PC8
                                        PC9
                                                PC10
## 1558 -0.2419150 -0.3030275 1.115791 0.7736474 1.0817168 -0.39551352
## 942 -0.3275572 0.1044763 2.039305 0.1564399
                                           0.9356193 -0.22259964
## 1310 0.9224057 -0.3148161 -0.471737 -0.2689322 0.2316760 0.53176979
## 2126 -1.9265475 -3.6522067 -3.339325 0.2123036 2.3671493 4.48949413
       ## 691 -1.1040825 1.0835762 -1.094231 -0.4025593 -0.1493833 -0.01278583
                                                    PC16
##
            PC12
                      PC13
                                PC14
                                         PC15
## 1558 -1.77444240 0.8582194 -0.70865405 -1.0232428 0.40936073 -0.4087346
## 942 -0.73864743 0.3383973 -0.07839124 1.0049390 -0.50942075 -0.2598862
## 1310 -0.23294167 0.6923908 0.42935992 0.6265949 -0.18616729 -0.3350760
## 2126 -0.00855891 -1.6603832 1.76443313 -0.1192481 -0.71515157 -0.7027052
      -0.99548418 1.7350957 0.07506511 0.5497652 -0.03162557 0.3862599
      -0.76271657 0.3433607 0.17632125 -1.0376911 0.80906514 0.3186242
## 691
             PC18
                        PC19
                                  PC20
                                           PC21
##
                                                     PC22
## 1558 0.002812804 -1.664468408 -0.7154521 -0.3564166
                                                0.48047263
## 942 -0.368365808 -0.164644357 -0.1666981 -0.3187658 -0.23004946
  1310 0.055973856 -0.003147345 -0.1458947 0.1047890 0.08386894
0.07119740
##
  691
       0.45302731
            PC23
                       PC24
                                 PC25
## 1558 -0.41503309 0.263220433 0.2602436 -0.05394346
                                               0.21312365
       0.08747367 -0.009176133 0.1261544 0.36653039
                                                0.07260519
## 1310 -0.16532222 0.077449451 -0.2906918 -0.28797890 0.10535407
## 2126 0.14626976 -0.485658615 0.5781911 -0.15602897 -0.22124949
      -0.07536905 -0.186171309 -0.8846307 -1.04682961 -0.02571918
      -0.02006442 -0.569668153 -0.3606024 0.26014074
                                                0.74593694
            PC28
                       PC29
                                  PC30
                                            PC31
##
      ## 1558
                                                 0.04216274
       0.11781239 -0.017207230 0.07759823 -0.02462265
                                                 0.01164107
  0.02831389
## 2126
      0.42390910 -0.175789454 0.05821555 0.83455592 -0.35894525
       0.49980727 \quad 0.252205358 \quad 0.06805872 \quad -0.06007699
## 262
                                                 0.04862443
      -0.07562252 -0.247336258 -0.19282318 -0.10559412 0.01556989
##
              PC33
##
                          PC34
## 1558
       1.224719e-02 -1.729597e-15
       2.264389e-03 1.254097e-17
## 942
## 1310 6.987968e-04 -3.072648e-16
## 2126 -1.042742e-01 3.833156e-15
## 262 -6.063129e-03 8.298596e-16
## 691 -7.313651e-05 -3.858342e-16
```

#### head(test.pca)

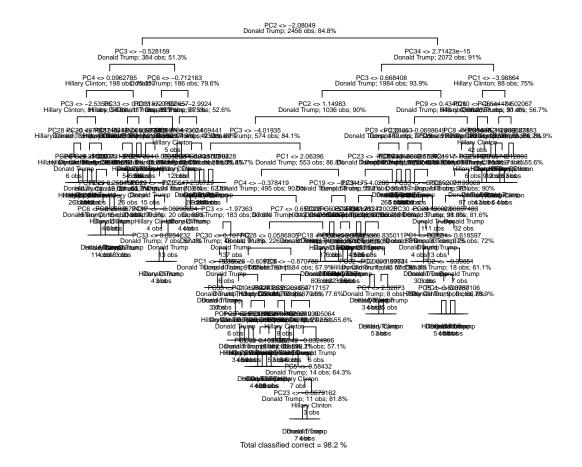
```
PC2
                                                 PC3
                                                                        PC5
##
           candidate
                           PC1
                                                            PC4
        Donald Trump -0.534608 -2.3383326 0.2488554 0.4221960 -0.01942941
## 1
## 8
        Donald Trump -1.482219 -1.6541146 2.7819220 -1.1469909 1.39109379
        Donald Trump -1.259255 0.7768294 0.9297121
                                                     0.1162212 -1.60271706
        Donald Trump -2.193477 0.3694519 0.8698010 0.3009422 0.78962702
## 35 Hillary Clinton -9.220720 -0.6106496 -2.2871919 3.2130451 -2.37419723
## 37
        Donald Trump -1.657118 0.5538342 0.4970016 0.6161101 -1.42656026
            PC6
                       PC7
                                   PC8
                                              PC9
                                                         PC10
                                                                      PC11
## 1 -1.0554443 -0.4119244 -0.44915407 -0.1309234 -0.36891586 -0.365332423
## 8 -0.7317522 0.7456810 -1.84320054 -0.5888855 0.03107667 -0.483867285
```

```
1.3129312 0.3974195 -1.12809833 -1.1501539 -0.60363483 1.047091176
     0.2449074 0.2819398 -0.57793586 0.3376414 -0.38067382 0.004649763
      0.8040246 0.4303297 -1.28042346 -0.3190843 -1.95498817 -0.208457566
## 37
      0.8700131
               0.2550706 -0.05052385 -0.1925798 -0.56565791
                                                        0.309364315
##
           PC12
                     PC13
                                 PC14
                                          PC15
                                                    PC16
                                                              PC17
      0.6026566
## 1
                                               0.3507514
                                                         0.4045562
     -0.43760553 -0.6952835 -0.006475763 -0.5209882 0.3940848 -0.2780899
## 24 -0.37358661 -0.1730428 1.524862626 0.7606203 -0.1111132 -0.1194390
## 34 -0.45302687 -0.5387033 -0.140455059 -0.4545016 -0.4091450 -0.1558792
      0.54185562  0.8891842  1.016156580
                                      1.10918134 -0.3378709 -0.123521692
                                      0.2876865 0.2889031 1.1630388
                      PC19
##
           PC18
                                 PC20
                                            PC21
                                                      PC22
## 1
     -0.04984370 -0.01705522 0.03733451 -0.188834103 -0.3771647
    -0.51886480 0.01518771 0.80496933
                                     0.026239732 0.1134704
## 24 -0.17209014 -0.41639130 -0.33008711 -0.009002311 -0.7544363
## 34 -0.21327084 -0.08703761 0.16812438
                                      0.167856222
                                                 0.1345852
     1.01201319 -0.68062543 -0.24100951
                                      0.324914722 0.9032762
  37 -0.02347463 -0.21575240 0.06280952
                                      0.435414955 -0.1232914
##
            PC23
                       PC24
                                 PC25
                                           PC26
                                                       PC27
## 1
      0.004485094
                 0.05360134 -0.4982141
                                      0.32723724 -0.174026207
##
  8
    0.004143709
## 24 -0.175981569  0.33041991 -0.5829753  0.19211016
                                                0.577306596
     0.387025135 -0.05823013 0.5411182 -0.21239206 0.047183145
      0.542351239 -0.45664442 0.8461351 -0.01638456 -0.244888291
## 37 -0.440186732 0.11990347 -0.3963533 -0.48818492 0.085524028
           PC28
                      PC29
                                 PC30
                                           PC31
                                                       PC32
## 1
     -0.18401304
                0.22742544
                           0.08696954 -0.02140527 -0.066203625
## 8
      0.12607318
                0.13438655
                          0.12600460 -0.16445072 0.001628442
## 24 0.05605443 -0.04894544 -0.09708482 -0.19245413 -0.017649050
## 35 -0.09832920
                ## 37
      0.28956941
                0.22907976 -0.00322449 -0.07698337 0.016311475
##
           PC33
                        PC34
      0.03416442
                1.350302e-15
## 1
## 8
      0.03108867 -1.306638e-15
## 24 -0.03324883 9.351918e-16
     0.01243862 -2.030878e-16
## 35
     0.01951005 5.714843e-15
## 37
     0.03460244 1.490226e-15
```

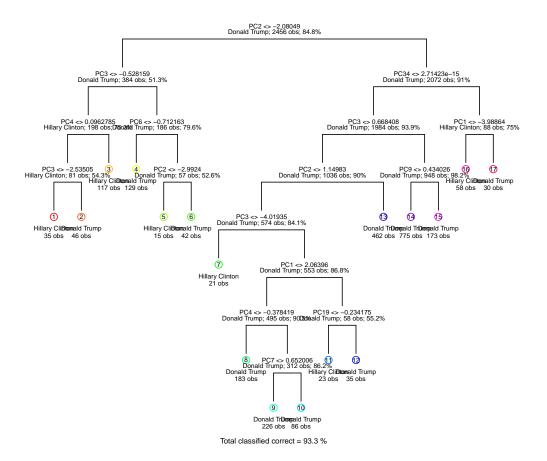
### Some Setups

```
set.seed(20)
nfold <- 10
folds.pca <- sample(cut(1:nrow(trn.cl), breaks=nfold, labels=FALSE))
calc_error_rate <- function(predicted.value, true.value){
   return(mean(true.value!=predicted.value))
}
records.pca <- matrix(NA, nrow=3, ncol=2)
colnames(records.pca) = c("train.error.pca","test.error.pca")
rownames(records.pca) = c("tree","knn","glm")</pre>
```

```
tree.train.pca <- tree(candidate~., data=tr.pca)</pre>
tree.train.control.pca <- tree.control(nobs=3070, minsize = 7, mindev = 1e-6)
tree.train.pca <- tree(candidate~., data = tr.pca, control = tree.train.control.pca)
summary(tree.train.pca)
##
## Classification tree:
## tree(formula = candidate ~ ., data = tr.pca, control = tree.train.control.pca)
## Variables actually used in tree construction:
## [1] "PC2" "PC3" "PC4" "PC28" "PC24" "PC20" "PC1" "PC18" "PC6" "PC3"
## [11] "PC12" "PC30" "PC29" "PC13" "PC17" "PC14" "PC34" "PC19" "PC7" "PC32"
## [21] "PC25" "PC27" "PC5" "PC23" "PC22" "PC9" "PC8" "PC10" "PC16"
## Number of terminal nodes: 99
## Residual mean deviance: 0.07418 = 174.8 / 2357
## Misclassification error rate: 0.01832 = 45 / 2456
cv.tree.pca <- cv.tree(tree.train.pca, rand=folds, prune.misclass)</pre>
cv.tree.pca
## $size
## [1] 99 81 79 73 59 55 49 43 35 23 19 17 15 8 6 4 3 1
## $dev
## [1] 253 249 244 244 237 237 238 238 233 233 233 234 235 236 250 317
## [18] 374
##
## $k
## [1]
             -Inf 0.0000000 0.5000000 0.8333333 1.0000000 1.2500000
## [7] 1.3333333 1.5000000 2.0000000 2.2500000 2.5000000 3.0000000
## [13] 5.5000000 6.0000000 6.5000000 9.0000000 44.0000000 50.0000000
##
## $method
## [1] "misclass"
##
## attr(,"class")
## [1] "prune"
                      "tree.sequence"
draw.tree(tree.train.pca, nodeinfo=TRUE, cex=.5, size = 0)
```



```
prunedtree.pca <- prune.tree(tree.train.pca, best=17)
draw.tree(prunedtree.pca, cex=0.5, nodeinfo=TRUE)</pre>
```



```
prediction.pca <- predict(prunedtree.pca, tr.pca, type="vector")
for (i in 1:nrow(tr.pca)){
    d = prediction.pca[i,7]
    prediction.pca[i,7] <- ifelse(d < 0.5,'Hillary Clinton','Donald Trump')
}

c = list()
for (i in 1:nrow(tr.pca)){
    c[[length(c)+1]] <- prediction.pca[i,7]
}
tree.train.error <- calc_error_rate(c, tr.pca$candidate)

prediction.pca2 <- predict(prunedtree.pca, test.pca, type="vector")
for (i in 1:nrow(test.pca)){</pre>
```

```
d = prediction.pca2[i,7]
  prediction.pca2[i,7] <- ifelse(d < 0.5,'Hillary Clinton','Donald Trump')</pre>
d = list()
for (i in 1:nrow(test.pca)){
  d[[length(d)+1]] <- prediction.pca2[i,7]</pre>
tree.test.error <- calc_error_rate(d, test.pca$candidate)</pre>
records.pca[1,] <- c(tree.train.error, tree.test.error)</pre>
records.pca
##
        train.error.pca test.error.pca
## tree
              0.06718241
                              0.07980456
## knn
                                       NA
## glm
                      NA
                                       NA
```

```
set.seed(20)
nfold <- 10
folds.pca <- sample(cut(1:nrow(trn.cl), breaks=nfold, labels=FALSE))</pre>
kvec \leftarrow c(1, seq(10, 50, length.out=9))
do.chunk <- function(chunkid, folddef, Xdat, Ydat, k){</pre>
 train = (folddef!=chunkid)
 Xtr = Xdat[train.]
 Ytr = Ydat[train]
 Xvl = Xdat[!train,]
 Yvl = Ydat[!train]
  predYtr = knn(train = Xtr, test = Xtr, cl = Ytr, k = k)
 predYvl = knn(train = Xtr, test = Xvl, cl = Ytr, k = k)
  data.frame(train.error = calc_error_rate(predYtr, Ytr),
             val.error = calc_error_rate(predYvl, Yvl))
}
avg.train.error.pca.vec <- c()</pre>
avg.test.error.pca.vec <- c()</pre>
for(i in 1:10) {
  a = ldply(1:9,
            do.chunk,
            folddef=folds,
            Xdat = dplyr::select(tr.pca,-candidate),
            Ydat = tr.pca$candidate,
            k=kvec[i])
  avg.train.error.pca = (a[1,1]+a[2,1]+a[3,1]+a[4,1]+a[5,1]+a[6,1]+a[7,1]+a[8,1]+a[9,1])/9
  avg.test.error.pca = (a[1,2]+a[2,2]+a[3,2]+a[4,2]+a[5,2]+a[6,2]+a[7,2]+a[8,2]+a[9,2])/9
```

```
avg.train.error.pca.vec = c(avg.train.error.pca.vec, avg.train.error.pca)
  avg.test.error.pca.vec = c(avg.test.error.pca.vec, avg.test.error.pca)
knn.test.error.pca <- min(avg.test.error.pca.vec)</pre>
knn.train.error.pca <- avg.train.error.pca.vec[which.min(avg.test.error.pca.vec)]</pre>
records.pca[2,] <- c(knn.train.error.pca, knn.test.error.pca)</pre>
records.pca
##
        train.error.pca test.error.pca
## tree
             0.06718241
                             0.07980456
             0.06660318
                             0.07512674
## knn
## glm
                      NA
```

If our goal is to predict the election, we could use time series analysis to forecast the election results. In the dataset we used, the data was collected after the election was done. Typically, prediction of elections and forecasting is done using multiple data points over set periods of time. Many pollsters and data analysts interested in forecasting use many different polls and sampling techniques to model voter behavior. For example, a certain county may come out with a poll predicting voter behavior in their county, depending on how reliable it is we can add it to a model. If we had the resources to get data on polls leading up to the election we could build models on voter behavior relating to other statistics such as approval ratings, how well the economy is doing, stances on big issues, etc.

Although it would be practically difficult to acquire the data, knowing voter preferences based on demographics could lead to more interesting analysis knowing the actual results. For example, if we had more data on race and preferred candidate, we could figure out how much of each demographic voted for Hillary and how much of each demographic voted for Trump with more accuracy. We could figure out how much of each demographic is worth in terms of electoral votes based on demographic size and voter turnout rate per demographic. Using our techniques we can infer voter preference, but it is hard to determine total votes based on a specific demographic. It is difficult to find datasets online in regards to voter demographics when connecting them to actual behavior. If we had our own resources then exit polls and surveys would likely be the best way to connect demographics with voter behavior. Having more detailed data connecting demographics directly to voter beahvior could lead to better model testing.

### Question 20

#### Additional Classification Methods: Logistic regression

In this question, we are going to use logistic regression method for testing the training error and test error with the original dataset first, and then use the datasets containing PCs to compare the errors.

```
train.glm.data <- trn.cl

train.glm.data[,1] <- as.character(train.glm.data$candidate)
train.glm.data[which(train.glm.data$candidate=="Donald Trump"),1] <- 1
train.glm.data[which(train.glm.data$candidate=="Hillary Clinton"),1] <- 0
train.glm.data[,1] <- as.numeric(train.glm.data$candidate)
train.glm.data[,2] <- as.numeric(train.glm.data$TotalPop)

model <- glm(candidate~., data=train.glm.data, family=binomial)</pre>
```

```
pred.train <- predict(model, data=train.glm.data, type="response")</pre>
pred.train <- ifelse(pred.train > 0.5, 1, 0)
train.error.glm <- calc_error_rate(pred.train, train.glm.data$candidate)</pre>
train.error.glm
## [1] 0.07288274
First of all, we get our training error for logistic regression which is approximately 7%.
test.glm.data <- tst.cl</pre>
test.glm.data[,1] <- as.character(test.glm.data$candidate)</pre>
test.glm.data[which(test.glm.data$candidate=="Donald Trump"),1] <- 1
test.glm.data[which(test.glm.data$candidate=="Hillary Clinton"),1] <- 0</pre>
test.glm.data[,1] <- as.numeric(test.glm.data$candidate)</pre>
test.glm.data[,2] <- as.numeric(test.glm.data$TotalPop)</pre>
pred.test <- predict(model, data=test.glm.data, type="response")</pre>
pred.test <- ifelse(pred.test > 0.5, 1, 0)
test.error.glm <- calc_error_rate(pred.test, test.glm.data$candidate)</pre>
test.error.glm
## [1] 0.2390065
Then, we got our test error for logistic regression which is approximately 24%. Below is the completed records
matrix.
records[3,] <- c(train.error.glm, test.error.glm)</pre>
records
##
        train.error test.error
## tree 0.04845277 0.09446254
## knn 0.11400409 0.11628413
        0.07288274 0.23900651
## lda
Next, we want to find the training and test error with full principle components.
train.glm.pca <- tr.pca</pre>
train.glm.pca[,1] <- as.character(train.glm.pca[,1])</pre>
train.glm.pca[which(train.glm.pca$candidate=="Donald Trump"),1] <- 1</pre>
train.glm.pca[which(train.glm.pca$candidate=="Hillary Clinton"),1] <- 0</pre>
train.glm.pca[,1] <- as.numeric(train.glm.pca$candidate)</pre>
model.pca <- glm(candidate~., data=train.glm.pca, family=binomial)</pre>
pred.train.pca <- predict(model.pca, data=train.glm.pca, type="response")</pre>
pred.train.pca <- ifelse(pred.train.pca > 0.5, 1, 0)
```

## [1] 0.07288274

train.error.glm.pca

train.error.glm.pca <- calc\_error\_rate(pred.train.pca, train.glm.pca\$candidate)</pre>

```
test.glm.pca <- test.pca

test.glm.pca[,1] <- as.character(test.glm.pca[,1])
test.glm.pca[which(test.glm.pca$candidate=="Donald Trump"),1] <- 1
test.glm.pca[which(test.glm.pca$candidate=="Hillary Clinton"),1] <- 0
test.glm.pca[,1] <- as.numeric(test.glm.pca$candidate)

pred.test.pca <- predict(model.pca, data=test.glm.pca, type="response")
pred.test.pca <- ifelse(pred.train.pca > 0.5, 1, 0)

test.error.glm.pca <- calc_error_rate(pred.test.pca, test.glm.pca$candidate)
test.error.glm.pca</pre>
```

### ## [1] 0.2390065

According to our result, we get the same training error and test error as we use the original dataset, because we are using the full PCs, we have captured 100% of the variance. Below is the completed records.pca matrix.

```
records.pca[3,] <- c(train.error.glm.pca, test.error.glm.pca)
records.pca</pre>
```