

$$3.1(a) \quad z\left[\left(\frac{1}{2}\right)^n u[n]\right] = \sum_{n=0}^{\infty} \left(\frac{1}{2}\right)^n z^{-n} = \sum_{n=0}^{\infty} \left(\frac{1}{2z}\right)^n = \frac{1}{1 - \frac{1}{2}z^{-1}}, |z| > \frac{1}{2}$$

$$(d) \quad z[\delta[n]] = z^0 = 1, \quad \text{all } z$$

$$(g) \quad z\left[\left(\frac{1}{2}\right)^n (u[n] - u[n-10])\right] = \sum_{n=0}^9 \left(\frac{1}{2z}\right)^n = \frac{1 - (2z)^{-10}}{1 - (2z)^{-1}}, |z| > 0$$

$$\begin{aligned} X(z) &= (1+2z)(1+3z^{-1})(1-z^{-1}) \\ &= 2z+5-4z^{-1}-3z^{-2} \\ 3.5 \quad &= \sum_{n=-\infty}^{\infty} x[n]z^{-n} \\ x[n] &= 2\delta[n+1] + 5\delta[n] - 4\delta[n-1] - 3\delta[n-2] \end{aligned}$$

$$\begin{aligned} x[n] &= u[-n-1] + \left(\frac{1}{2}\right)^n u[n] \\ X(z) &= \frac{-1}{1-z^{-1}} + \frac{1}{1-\frac{1}{2}z^{-1}}, \frac{1}{2} < |z| < 1 \\ 3.7 \end{aligned}$$

$$H(z) = \frac{Y(z)}{X(z)} = \frac{\frac{-1}{2}z^{-1}}{(1-\frac{1}{2}z^{-1})(1+z^{-1})} \cdot \frac{(1-z^{-1})(1-\frac{1}{2}z^{-1})}{\frac{-1}{2}z^{-1}} = \frac{1-z^{-1}}{1+z^{-1}}, |z| > 1$$

$$\begin{aligned} H(z) &= \frac{1}{1-\frac{1}{4}z^{-2}} \\ &= \frac{1}{(1-\frac{1}{2}z^{-1})(1+\frac{1}{2}z^{-1})} \\ 3.14 \quad &= \frac{0.5}{1-\frac{1}{2}z^{-1}} + \frac{0.5}{1+\frac{1}{2}z^{-1}} \\ h[n] &= \frac{1}{2}\left(\frac{1}{2}\right)^n u[n] + \frac{1}{2}\left(\frac{-1}{2}\right)^n u[n], A_1 = \frac{1}{2}, \alpha_1 = \frac{1}{2}, A_2 = \frac{1}{2}, \alpha_2 = \frac{-1}{2} \end{aligned}$$

$$3.19(a) \quad |z| > \frac{1}{2}$$

$$(b) \quad \frac{1}{3} < |z| < 2$$