# Stereo-Based Stochastic Noise Compensation Based on Trajectory GMMs

Author: Heiga Zen, Yoshihiko

Nankaku, Keiichi Tokuda

Professor:陳嘉平

Reporter:吳柏鋒

### 簡介

· 以GMMs為基礎的立體聲連續隨機特徵對映 技術已應用到噪音補償上

- 此對映技術分為三個階段:
  - (1)由一GMMs集合計算噪音和乾淨特徵間的聯合機 率密度函式
  - (2)從給定的一噪音,可從聯合機率密度函式估算 出乾淨特徵的條件機率密度函式
  - (3)根據條件機率密度函式何時造成最小的MMSE, 來決定乾淨特徵的對映

#### 簡介

此對映技術在音框與音框間的<u>動態特性</u>對 映上,效果較不佳

• 因此又使用以GMMs為基礎且對動態特徵作限制的特徵對映技術,來改善此問題。但 在訓練與對映上仍然有可能會產生不一致

#### 簡介

· 以這概念為基礎,提出以GMMs軌跡為基礎 的連續隨機特徵對映技術

#### MFCC向量序列

$$x = \begin{bmatrix} x_1^\top, \dots, x_T^\top \end{bmatrix}^\top, \quad y = \begin{bmatrix} y_1^\top, \dots, y_T^\top \end{bmatrix}^\top, \tag{1}$$

其中 $x_t$ 和 $y_t$ 分別表示在第t個音框的噪音和乾淨MFCC 靜態特徵向量且其維度為M,T為音框總數

### 聯合機率密度函式(JPDF)

• 由軌跡GMMs獲得的 x 和 y 的聯合機率密度 函式定義:

$$p(z \mid \lambda) = \sum_{\forall q} P(q \mid \lambda) p(z \mid q, \lambda), \qquad (2)$$

其中

$$P(q \mid \lambda) = \prod_{t=1}^{T} c_{q_t}$$
 (即混合事前機率的乘積)

$$p(z \mid q, \lambda) = \mathcal{N}\left(z; \bar{z}_q, P_q\right) \tag{3}$$

$$R_q \bar{z}_q = r_q \tag{4}$$

### 對映(Mapping)

• 條件機率(重寫式子(3))

$$p(z \mid q, \lambda) = \mathcal{N}\left(\begin{bmatrix} x \\ y \end{bmatrix}; \begin{bmatrix} \bar{x}_q \\ \bar{y}_q \end{bmatrix}, \begin{bmatrix} P_q^{(xx)} & P_q^{(xy)} \\ P_q^{(yx)} & P_q^{(yy)} \end{bmatrix}\right)$$
 共中
$$P_q^{(xx)} = C_q^{(xx)^{-1}}, \quad P_q^{(yy)} = C_q^{(yy)^{-1}},$$

$$P_q^{(xy)} = -R_q^{(xx)^{-1}} R_q^{(xy)} C_q^{(yy)^{-1}} = P_q^{(yx)^{\top}}$$

$$\bar{x}_q = P_q^{(xx)} \left( r_q^{(x)} - R_q^{(xy)} R_q^{(yy)^{-1}} r_q^{(y)} \right)$$

$$\bar{y}_q = P_q^{(yy)} \left( r_q^{(y)} - R_q^{(yx)} R_q^{(xx)^{-1}} r_q^{(x)} \right)$$
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$$C_{q}^{(xx)} = R_{q}^{(xx)} - R_{q}^{(xy)} R_{q}^{(yy)^{-1}} R_{q}^{(yx)}$$

$$C_{q}^{(yy)} = R_{q}^{(yy)} - R_{q}^{(yx)} R_{q}^{(xx)^{-1}} R_{q}^{(xy)}$$

$$R_{q}^{(xx)} = W^{(x)^{\top}} \Omega_{q}^{(xx)} W^{(x)},$$

$$R_{q}^{(yy)} = W^{(y)^{\top}} \Omega_{q}^{(yy)} W^{(y)},$$

$$R_{q}^{(xy)} = W^{(x)^{\top}} \Omega_{q}^{(xy)} W^{(y)} = R_{q}^{(yx)^{\top}}$$

$$\Omega_{q}^{(xx)} = \text{diag} \left[ \Omega_{q_{1}}^{(xx)}, \dots, \Omega_{q_{T}}^{(xy)} \right],$$

$$\Omega_{q}^{(yy)} = \text{diag} \left[ \Omega_{q_{1}}^{(yy)}, \dots, \Omega_{q_{T}}^{(yy)} \right],$$

$$\Omega_{q}^{(xy)} = \text{diag} \left[ \Omega_{q_{1}}^{(xy)}, \dots, \Omega_{q_{T}}^{(xy)} \right] = \Omega_{q}^{(yx)}$$

$$r_{q}^{(x)} = W^{(x)}^{\top} \left( \Omega_{q}^{(xx)} \mu_{q}^{(x)} + \Omega_{q}^{(xy)} \mu_{q}^{(y)} \right),$$

$$r_{q}^{(y)} = W^{(y)}^{\top} \left( \Omega_{q}^{(yy)} \mu_{q}^{(y)} + \Omega_{q}^{(yx)} \mu_{q}^{(x)} \right),$$

$$\mu_{q}^{(x)} = \left[ \mu_{q_{1}}^{(x)}^{\top}, \dots, \mu_{q_{T}}^{(x)}^{\top} \right]^{\top},$$

$$\mu_{q}^{(y)} = \left[ \mu_{q_{1}}^{(y)}^{\top}, \dots, \mu_{q_{T}}^{(y)}^{\top} \right]^{\top}.$$

## 對映(Mapping)

· 在給定 x 和 λ 下 , y 的條件機率:

$$p(y \mid x, \lambda) = \sum_{\forall q} \gamma_q \cdot p(y \mid x, q, \lambda)$$

其中 
$$\gamma_q$$
 是  $q$  的事後機率 
$$p(y \mid x, q, \lambda) = \mathcal{N}\left(y \; ; \; \tilde{y}_q, \tilde{P}_q^{(yy)}\right)$$
  $\tilde{y}_q = \bar{y}_q + P_q^{(yx)}C_q^{(xx)}\left(x - \bar{x}_q\right)$   $\tilde{P}_q^{(yy)} = P_q^{(yy)} - P_q^{(yx)}C_q^{(xx)}P_q^{(xy)}$ 

#### 以最小均方差(MMSE)為基礎的對映

• 可以由乾淨的靜態MFCC向量序列ŷ來估算 MMSE:

MMSE: 
$$\hat{y} = E[y \mid x] = \int p(y \mid x, \lambda) y dy$$
$$= \int \sum_{\forall q} \gamma_q \cdot p(y \mid x, q, \lambda) y dy$$
$$= \sum_{\forall q} \gamma_q \cdot \tilde{y}_q,$$

其中 E[]是平均值的期望值

## 實驗

• 使用AURORA-2語料庫

 AURORA-2是由一連續英文數字句所組成, 並人工加入8種不同的SNR(-5dB, 0dB, 5 dB, 10dB, 15dB, 20dB, clean)到測試集A與B中

## 實驗

- 實驗中針對四種對映技術做比較:
  - (1) GMM-Static:

基本的GMM對映(MMSE對映+SPLICE),應 用在13維的靜態MFCC向量上

(2) GMM-Complete:

類似SPLICE,在13維的靜態MFCC向量加入動態特徵之後再進行以GMM為基礎的對映

## 實驗

#### (3) GMM-Dynamic:

13維的靜態MFCC向量在靜態和動態特徵之間具有限制下的GMM對映

#### (4)Trajectory GMM:

以軌跡GMM為基礎的對映對13維靜態MFCC 向量作轉換

# 實驗結果(1)(2)

Aurora 2 Clean Training + GMM-Static

	A					В						С		Overal1	Percentage
	Subway	Babble	Car	Exhibition	Average	Restaurant	Street	Airport	Station	Average	Subway M	Street M	Average	Average	Improvement
Clean	98.86	99.00	98.96	99.23	99.01	98.86	99.00	98.96	99.23	99.01	99.14	98.97	99.06	99.02	-0.56%
20 dB	97.33	98.10	97.70	97.53	97.67	96.99	96.46	96.93	96.91	96.82	96.75	95.01	95.88	96.97	37.63%
15 <b>dB</b>	94.60	95.98	96.27	95.62	95.62	95.00	92.59	93.14	94.35	93.77	93.06	89.81	91.44	94.04	51.53%
10 dB	90.27	90.81	90.75	91.51	90.84	87.38	83.07	85.09	85.75	85.32	81.27	77.45	79.36	86.34	56.58%
5 <b>dB</b>	80.50	72.61	77.27	80.13	77.63	69.63	59.31	63.14	64.83	64.23	54.31	53.66	53.99	67.54	45.45%
0 dB	59.16	35.70	46.82	61.06	50.69	37.70	29.14	28.96	29.99	31.45	25.64	26.03	25.84	38.02	25.02%
-5 <b>dB</b>	26.90	4.05	16.13	32.12	19.80	7.55	10.01	3.13	1.88	5.64	11.54	12.85	12.20	12.62	4.52%
Average	84.37	78.64	81.76	85.17	82.49	77.34	72.11	73.45	74.37	74.32	70.21	68.39	69.30	76.58	
															41.36%
	48.77%	57.38%	53.71%	57.15%	54.69%	52.20%	27.53%	43.21%	42.23%	41.96%	11.95%	6.73%	9.33%		41.3070
					Δ	Aurora 2	Clean T	raining -	- GMM-	Comple	te				
_		_	Δ	_	A	Aurora 2	Clean T	raining -	GMM-	·Comple	te	C		Overall	Dercentage
	Subway	Babble	A Car	Exhibition				В				C Street M	Average	Overall Average	Percentage Improvement
Clean	Subway 98.96	Babble	A Car 98.96	Exhibition 99.23	Average	Restaurant	Street	B Airport	Station	Average	Subway M	C Street M	Average	Average	Improvement
	98.96	99.00	98.96	99.23	Average 99.04	Restaurant 98.96	Street 99.00	B Airport 98.96	Station 99.23	Average 99.04	Subway M 99.14	C Street M 98.97 97.22	99.06	Average 99.04	Improvement 1.31%
Clean 20 dB 15 dB	98.96 97.88	99.00 98.31	98.96 98.06	99.23 97.84	Average 99.04 98.02	Restaurant 98.96 97.48	Street 99.00 97.64	B Airport 98.96 97.82	Station 99.23 97.87	Average 99.04 97.70	Subway M 99.14 97.42	97.22	99.06 97.32	Average 99.04 97.75	Improvement 1.31% 53.55%
20 dB	98.96	99.00	98.96	99.23	Average 99.04	Restaurant 98.96	Street 99.00	B Airport 98.96	Station 99.23	Average 99.04	Subway M 99.14		99.06	Average 99.04	Improvement 1.31%
20 dB 15 dB	98.96 97.88 96.75	99.00 98.31 96.83	98.96 98.06 96.96	99.23 97.84 96.88	Average 99.04 98.02 96.86	Restaurant 98.96 97.48 96.28	Street 99.00 97.64 96.46	B Airport 98.96 97.82 96.36	Station 99.23 97.87 95.53	Average 99.04 97.70 96.16	Subway M 99.14 97.42 94.96	97.22 94.89	99.06 97.32 94.93	Average 99.04 97.75 96.19	Improvement 1.31% 53.55% 69.46%
20 dB 15 dB 10 dB	98.96 97.88 96.75 93.37	99.00 98.31 96.83 94.23	98.96 98.06 96.96 94.93	99.23 97.84 96.88 93.64	Average 99.04 98.02 96.86 94.04	Restaurant 98.96 97.48 96.28 91.71	Street 99.00 97.64 96.46 91.57	B Airport 98.96 97.82 96.36 91.05	Station 99.23 97.87 95.53 90.71	Average 99.04 97.70 96.16 91.26	Subway M 99.14 97.42 94.96 87.66	97.22 94.89 86.43	99.06 97.32 94.93 87.05	Average 99.04 97.75 96.19 91.53	Improvement 1.31% 53.55% 69.46% 72.89%
20 dB 15 dB 10 dB 5 dB	98.96 97.88 96.75 93.37 88.12	99.00 98.31 96.83 94.23 84.89	98.96 98.06 96.96 94.93 88.04	99.23 97.84 96.88 93.64 86.27	Average 99.04 98.02 96.86 94.04 86.83	Restaurant 98.96 97.48 96.28 91.71 80.47	Street 99.00 97.64 96.46 91.57 78.96	B Airport 98.96 97.82 96.36 91.05 79.54	Station 99.23 97.87 95.53 90.71 78.25	Average 99.04 97.70 96.16 91.26 79.31	Subway M 99.14 97.42 94.96 87.66 70.53	97.22 94.89 86.43 68.95	99.06 97.32 94.93 87.05 69.74	Average 99.04 97.75 96.19 91.53 80.40	Improvement 1.31% 53.55% 69.46% 72.89% 66.78%
20 dB 15 dB 10 dB 5 dB 0 dB	98.96 97.88 96.75 93.37 88.12 69.76	99.00 98.31 96.83 94.23 84.89 53.63	98.96 98.06 96.96 94.93 88.04 63.88	99.23 97.84 96.88 93.64 86.27 70.32	Average 99.04 98.02 96.86 94.04 86.83 64.40	Restaurant 98.96 97.48 96.28 91.71 80.47 50.51	Street 99.00 97.64 96.46 91.57 78.96 51.09	B Airport 98.96 97.82 96.36 91.05 79.54 50.52	Station 99.23 97.87 95.53 90.71 78.25 46.13	Average 99.04 97.70 96.16 91.26 79.31 49.56	Subway M 99.14 97.42 94.96 87.66 70.53 39.58	97.22 94.89 86.43 68.95 41.57	99.06 97.32 94.93 87.05 69.74 40.58	Average 99.04 97.75 96.19 91.53 80.40 53.70	Improvement 1.31% 53.55% 69.46% 72.89% 66.78% 43.89%
20 dB 15 dB 10 dB 5 dB 0 dB -5 dB	98.96 97.88 96.75 93.37 88.12 69.76 32.98	99.00 98.31 96.83 94.23 84.89 53.63 18.65	98.96 98.06 96.96 94.93 88.04 63.88 23.83	99.23 97.84 96.88 93.64 86.27 70.32 32.34	Average 99.04 98.02 96.86 94.04 86.83 64.40 26.95	Restaurant 98.96 97.48 96.28 91.71 80.47 50.51 14.92	Street 99.00 97.64 96.46 91.57 78.96 51.09 18.71	B Airport 98.96 97.82 96.36 91.05 79.54 50.52 12.44	Station 99.23 97.87 95.53 90.71 78.25 46.13 11.82	Average 99.04 97.70 96.16 91.26 79.31 49.56 14.47	Subway M 99.14 97.42 94.96 87.66 70.53 39.58 17.75	97.22 94.89 86.43 68.95 41.57 19.50	99.06 97.32 94.93 87.05 69.74 40.58 18.63	Average 99.04 97.75 96.19 91.53 80.40 53.70 20.29	Improvement 1.31% 53.55% 69.46% 72.89% 66.78% 43.89% 12.85%
20 dB 15 dB 10 dB 5 dB 0 dB -5 dB	98.96 97.88 96.75 93.37 88.12 69.76 32.98	99.00 98.31 96.83 94.23 84.89 53.63 18.65	98.96 98.06 96.96 94.93 88.04 63.88 23.83	99.23 97.84 96.88 93.64 86.27 70.32 32.34	Average 99.04 98.02 96.86 94.04 86.83 64.40 26.95	Restaurant 98.96 97.48 96.28 91.71 80.47 50.51 14.92	Street 99.00 97.64 96.46 91.57 78.96 51.09 18.71	B Airport 98.96 97.82 96.36 91.05 79.54 50.52 12.44	Station 99.23 97.87 95.53 90.71 78.25 46.13 11.82	Average 99.04 97.70 96.16 91.26 79.31 49.56 14.47	Subway M 99.14 97.42 94.96 87.66 70.53 39.58 17.75	97.22 94.89 86.43 68.95 41.57 19.50	99.06 97.32 94.93 87.05 69.74 40.58 18.63	Average 99.04 97.75 96.19 91.53 80.40 53.70 20.29	Improvement 1.31% 53.55% 69.46% 72.89% 66.78% 43.89%

## 實驗結果(3)(4)

Aurora 2 Clean Training + GMM-Dynamic															
			A			В					С			Overall	Percentage
	Subway	Babble	Car	Exhibition	Average	Restaurant	Street	Airport	Station	Average	Subway M	Street M	Average	Average	Improvement
Clean	98.93	99.00	98.96	99.23	99.03	98.93	99.00	98.96	99.23	99.03	99.14	98.97	99.06	99.04	0.75%
20 dB	98.16	98.19	98.27	98.21	98.21	97.45	97.49	98.03	97.22	97.55	97.54	97.37	97.46	97.79	55.32%
15 dB	96.65	97.19	97.55	96.95	97.09	95.67	95.77	95.76	94.57	95.44	95.39	94.44	94.92	95.99	68.34%
10 dB	94.11	94.59	95.59	93.98	94.57	90.08	90.15	90.01	89.76	90.00	89.32	86.91	88.12	91.45	73.22%
5 <b>dB</b>	88.73	84.85	88.70	86.58	87.22	78.26	77.09	77.54	75.29	77.05	75.65	70.56	73.11	80.33	67.11%
0 dB	71.48	52.24	65.05	68.13	64.23	46.27	46.70	46.47	41.10	45.14	43.75	42.20	42.98	52.34	42.43%
5 <b>dB</b>	35.46	17.26	24.16	32.46	27.34	12.59	18.14	14.94	11.20	14.22	18.27	19.20	18.74	20.37	12.96%
Average	89.83	85.41	89.03	88.77	88.26	81.55	81.44	81.56	79.59	81.03	80.33	78.30	79.31	83.58	
															 58.88%
	66.65%	70.89%	72.16%	67.55%	69.63%	61.07%	51.77%	60.56%	54.00%	57.14%	41.87%	35.95%	38.91%		00.00/0

	Aurora 2 Clean Training + Trajectory GMM														
			A							C		Overall	Percentage		
	Subway	Babble	Car	Exhibition	Average	Restaurant	Street	Airport	Station	Average	Subway M	Street M	Average	Average	Improvement
Clean	98.93	99.00	98.96	99.23	99.03	98.93	99.00	98.96	99.23	99.03	99.14	98.97	99.06	99.04	0.75%
20 dB	97.97	98.16	98.18	98.40	98.18	97.39	97.58	97.61	97.16	97.44	97.67	97.43	97.55	97.76	54.73%
15 dB	96.81	97.16	97.46	96.79	97.06	95.18	95.98	95.05	94.63	95.21	96.01	94.74	95.38	95.98	68.73%
10 dB	94.66	94.77	95.44	94.72	94.90	88.73	90.45	89.53	90.44	89.79	90.30	87.30	88.80	91.63	74.16%
5 <b>dB</b>	90.60	84.49	90.67	87.84	88.40	77.40	77.42	76.86	77.82	77.38	78.39	71.95	75.17	81.34	68.99%
0  dB	76.05	54.23	70.03	73.25	68.39	47.34	48.40	48.67	47.21	47.91	49.34	45.56	47.45	56.01	46.93%
-5 dB	41.57	15.72	30.15	39.46	31.73	12.19	17.17	13.48	11.94	13.70	20.02	20.56	20.29	22.23	15.05%
Averag	91.22	85.76	90.36	90.20	89.38	81.21	81.97	81.54	81.45	81.54	82.34	79.40	80.87	84.54	
															61 200/
	71.21%	71.59%	75.52%	71.68%	72.54%	60.36%	53.14%	60.52%	58.20%	58.29%	47.81%	39.20%	43.50%		61.30%