



# MODULATION SPECTRUM EQUALIZATION FOR ROBUST SPEECH RECOGNITION

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# Introduction

- The performance of speech recognition systems is very often degraded due to the mismatch between the acoustic conditions of the training and testing environments.
- In this paper, we propose a new approach for modulation spectrum equalization in which the modulation spectra of noisy speech utterances are equalized to those of clean speech.



# Introduction

- The first is to equalize the cumulative density functions (CDFs) of the modulation spectra of clean and noisy speech, such that the differences between them are reduced.
- The second is to equalize the magnitude ratio of lower to higher components in the modulation spectrum.

# Modulation spectrum (1/2)

- Given a sequence of feature vectors  $\{x(n), n = 1, 2, \dots, N\}$  for an utterance, each including  $D$  feature parameters,

$$x(n) = [x(n, 1), x(n, 2), \dots, x(n, D)]^T, \quad n = 1, \dots, N$$

- where  $n$  is the time index, and  $d = 1, \dots, D$  is the parameter index.

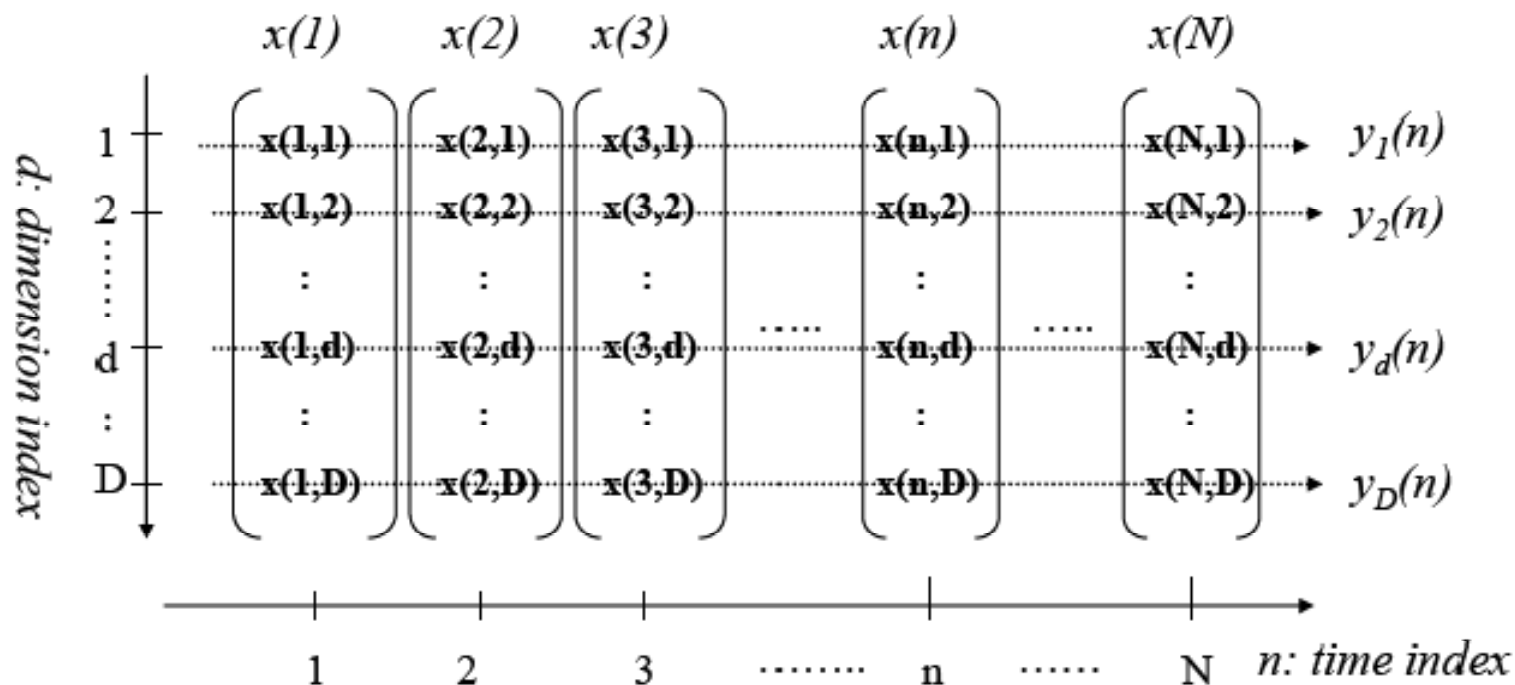


Figure 1: *The representation of the time trajectories of feature parameter sequences*

# Modulation spectrum (2/2)

- The modulation spectrum  $Y_d(k)$  of the  $d$ -th time trajectory can be obtained by applying discrete Fourier transform:

$$Y_d(k) = \sum_{n=0}^{N-1} y_d(n) \cdot \exp(-j2\pi nk / N)$$

$$k = 0, 1, 2, \dots, N-1; \quad d = 1, 2, \dots, D$$

# Spectral Histogram Equalization

- We first calculate the **cumulative distribution function** (CDF) of the magnitudes of the modulation spectra,  $|Y_d(k)|$ , for all utterances in the clean training data of AURORA 2 to be used as the reference CDF,  $\text{CDF}_{\text{ref}}[\cdot]$ .
- For any test utterance, the CDF for its modulation spectrum magnitude,  $|Y_{d,\text{test}}(k)|$ , can be similarly obtained as  $\text{CDF}_{\text{test}}[\cdot]$ .

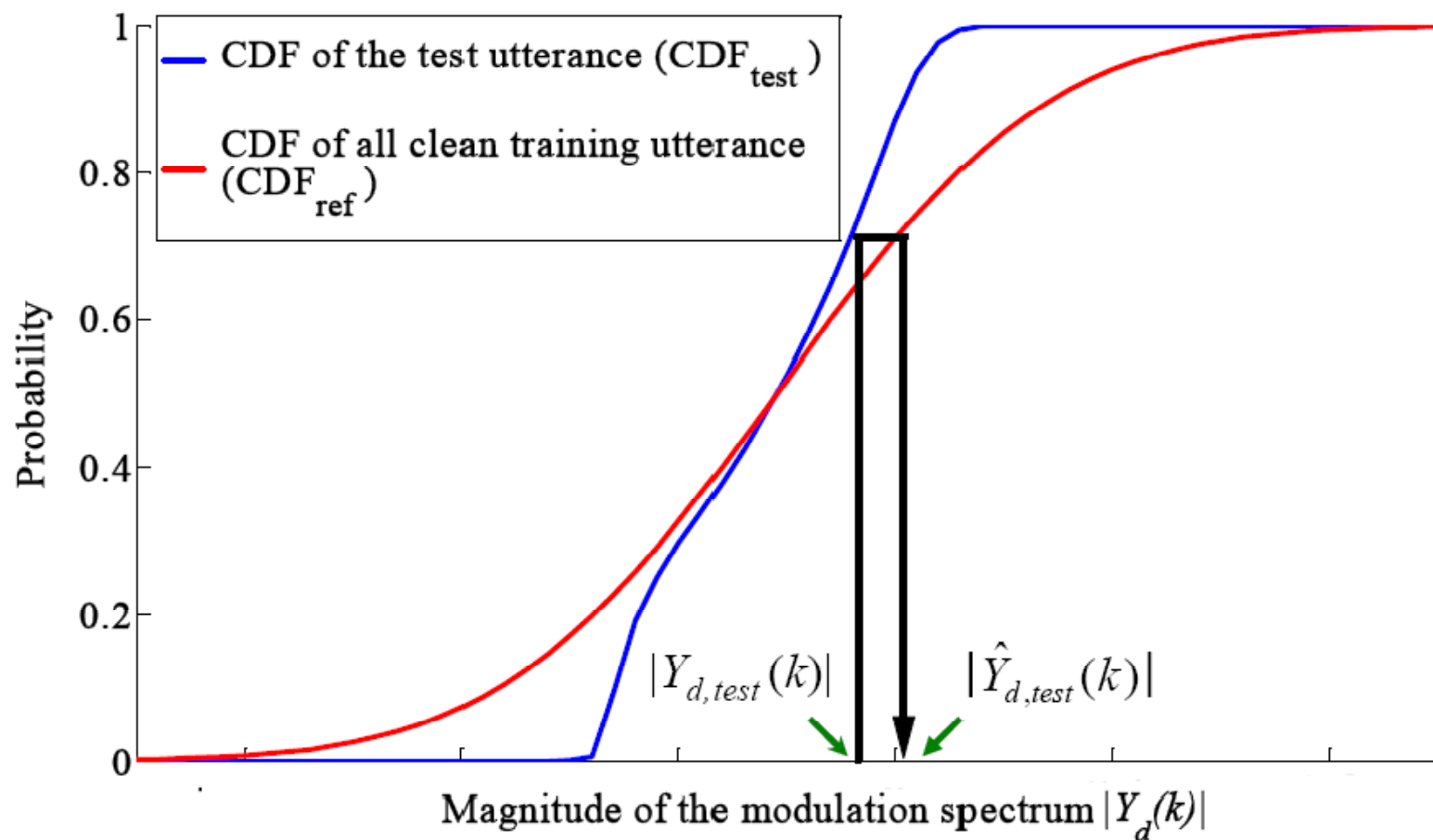


Figure 2: *The concept of the spectral histogram equalization (SHE).*



# Spectral Histogram Equalization

- Hence the equalized magnitude of modulation spectrum  $|\hat{Y}_{d,test}(k)|$  is

$$|\hat{Y}_{d,test}(k)| = CDF_{ref}^{-1}(CDF_{test}[|Y_{d,test}(k)|])$$

# Magnitude Ratio Magnitude Ratio Equalization

- We first define a magnitude ratio (MR) for lower to higher frequency components for each parameter index  $d$  as follows:

$$MR_d = \frac{\sum_{k=0}^{k_c} |Y_d(k)|}{\sum_{k=0}^{\left[\frac{N}{2}\right]+1} |Y_d(k)|}$$

- where  $k_c$  is the cut-off frequency used here,  $N$  is the order of the discrete Fourier transform.

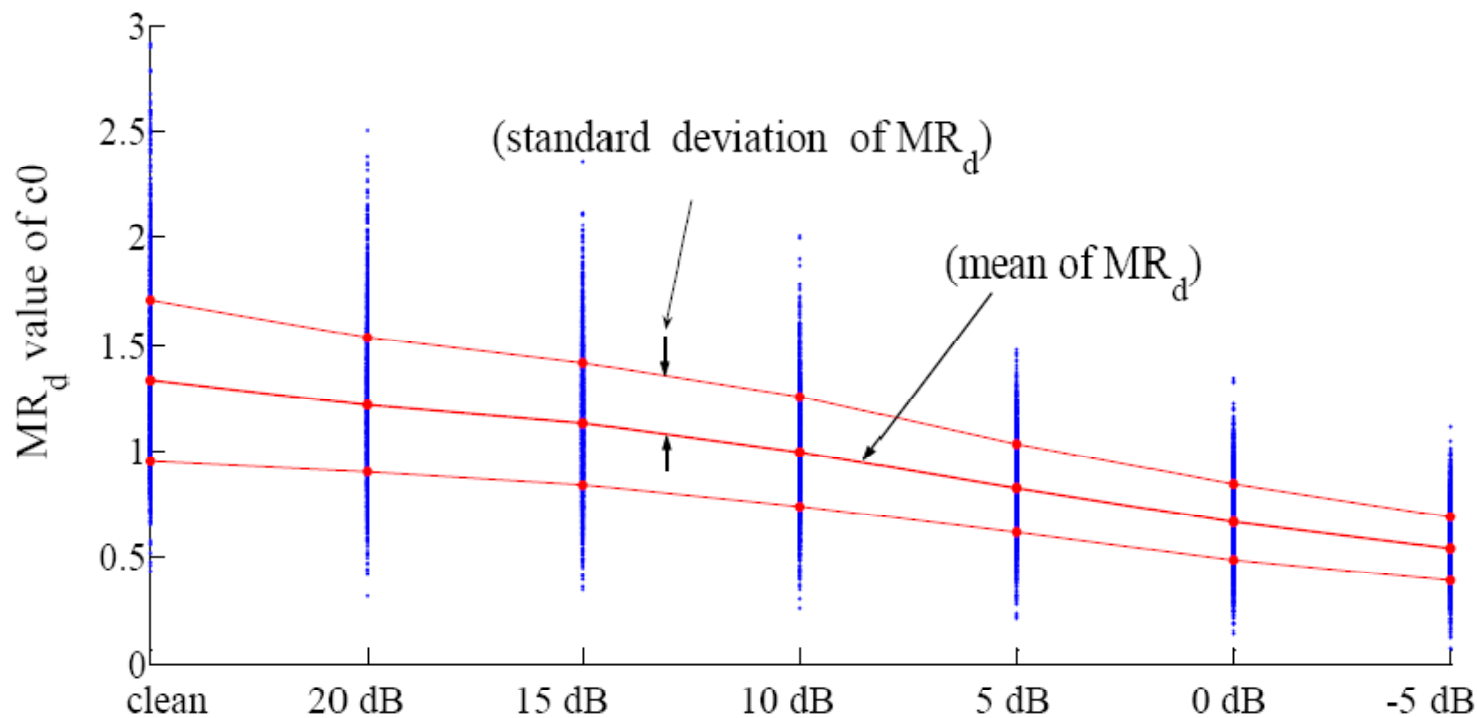


Figure 3: *The distribution of the magnitude ratio ( $MR_d$ ) values of  $c_0$  for all testing utterances in AURORA 2 for all sets at all SNRs. Each point represents the  $MR_d$  value of  $c_0$  for an utterance.*

# Magnitude Ratio

- We can observe from this figure that the mean value of  $MR_d$  is degraded when SNR is degraded, and thus  $MR_d$  is highly correlated with SNR.
- It is therefore reasonable to equalize the value of  $MR_d$  for a noisy utterance to a reference  $MR_d$  value obtained from clean training data.

# Magnitude Ratio Equalization

- We first calculate the average of  $MR_d$  for all utterances in the clean training data of AURORA 2 as the reference value  $MR_{d,ref}$  .
- We then calculate the value of  $MR_d$  for each test utterance as  $MR_{d,test}$  .

# Magnitude Ratio Equalization

- We equalize the magnitude of the modulation spectrum for the test utterance  $|Y_{d,test}(k)|$  as

$$|\hat{Y}_{d,test}(k)| = \begin{cases} \left(\frac{MR_{d,ref}}{MR_{d,test}}\right)^p \cdot |Y_{d,test}(k)| & , k \leq k_c \\ \frac{1}{\left(\frac{MR_{d,ref}}{MR_{d,test}}\right)^{(1-p)}} \cdot |Y_{d,test}(k)| & , k > k_c \end{cases}$$

where  $0 < p < 1$  is the weighted-power for the scaling factor.



# EXPERIMENTAL SETUP

- AURORA 2
- The speech features were extracted by the AURORA WI007 front-end.
- Figure 4

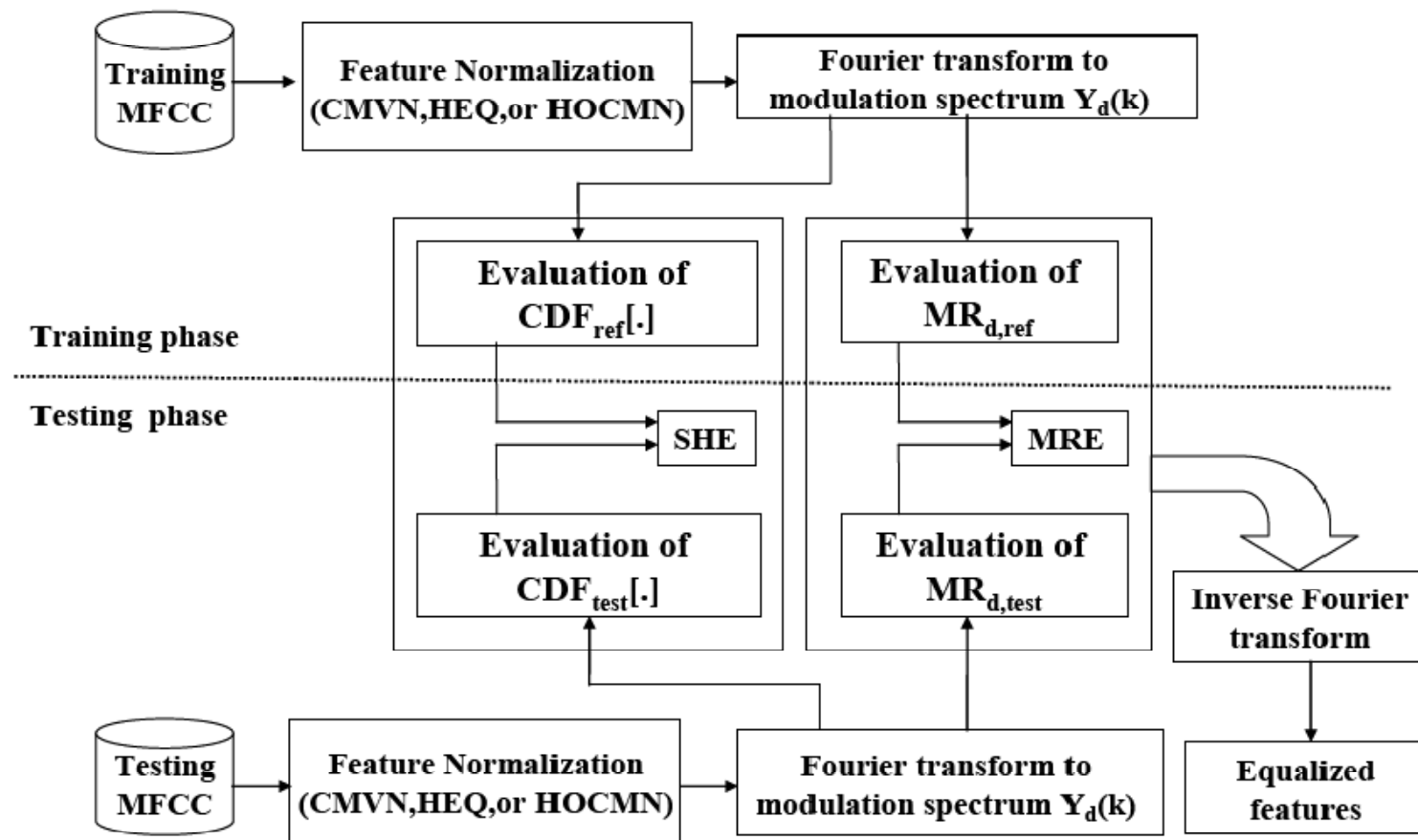
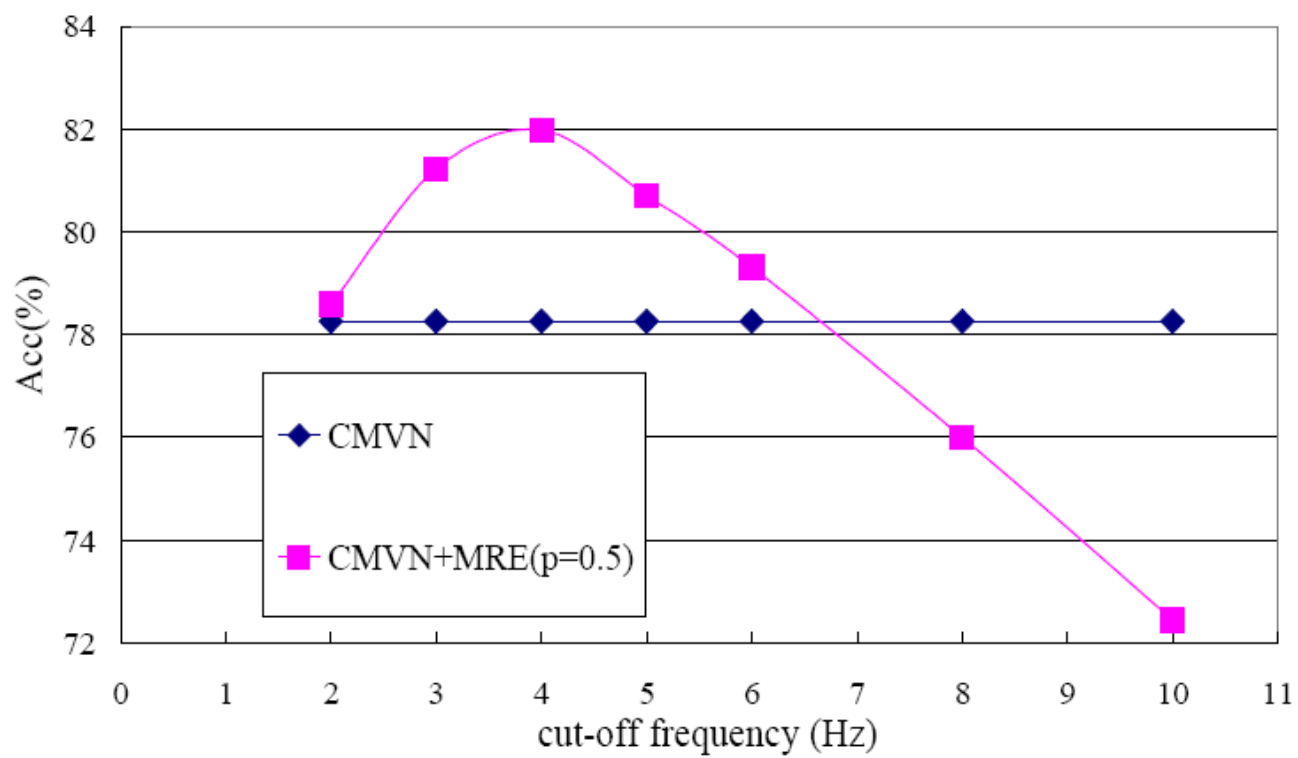
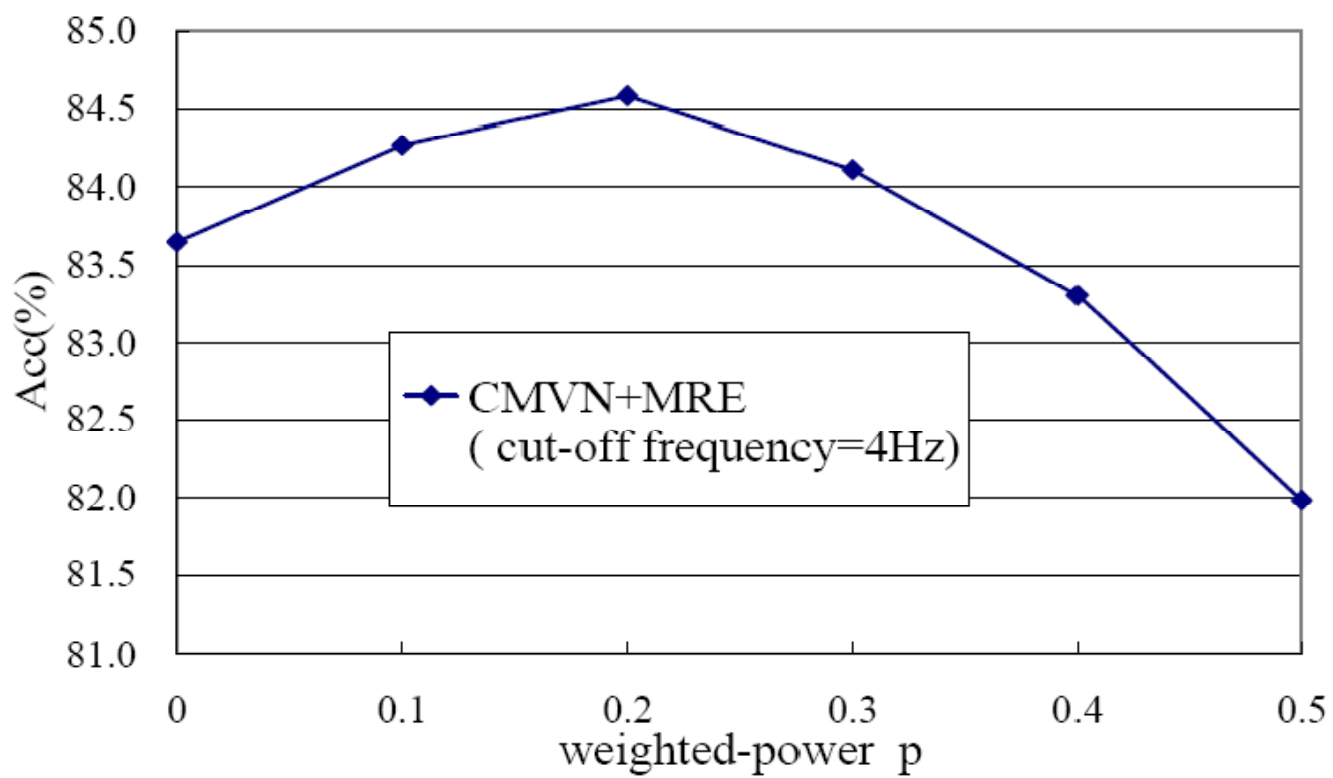


Figure 4: *The overall framework of modulation spectrum equalization techniques.*

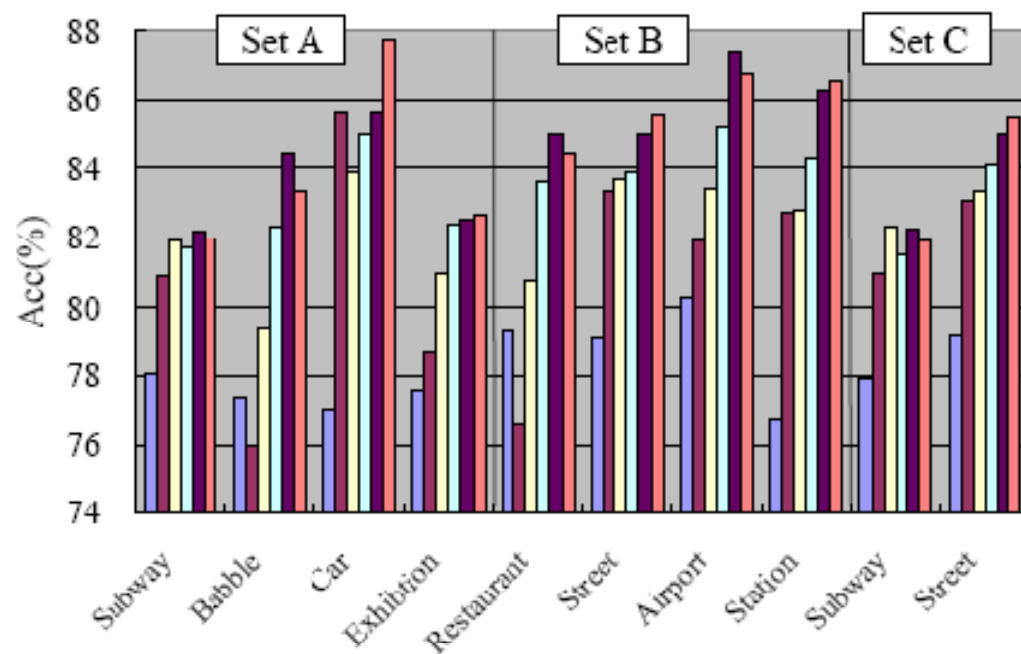




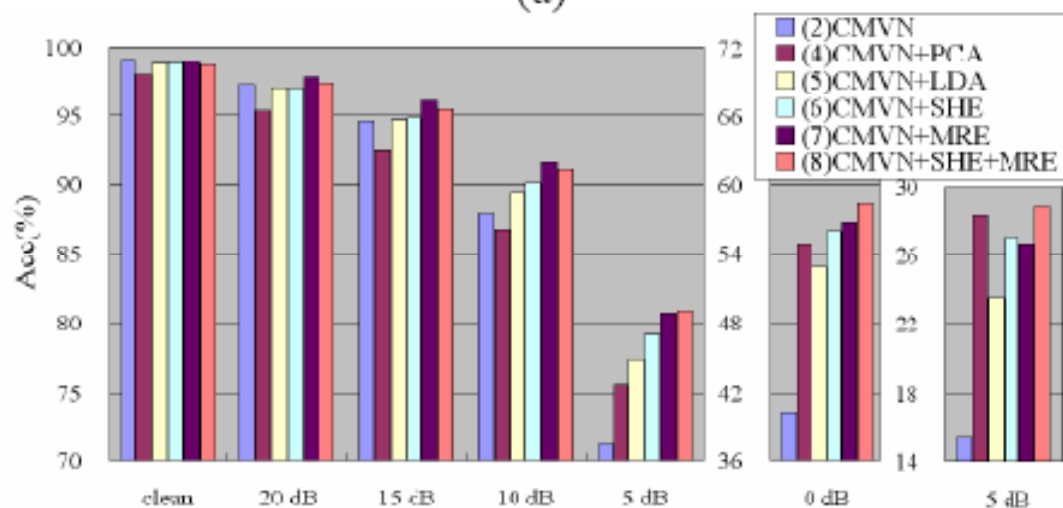


Clean condition training	Set A	Set B	Set C	Avg.	Impr.
(1)MFCC(c0)	58.89	54.29	67.14	58.70	-----
(2)CMVN	77.52	78.86	78.53	78.26	-----
(3)CMVN+RASTA	77.70	79.00	78.41	78.36	0.45%
(4)CMVN+PCA(L=15)	80.31	81.15	82.02	80.99	12.56%
(5)CMVN+LDA(L=5)	81.54	82.65	82.85	82.25	18.35%
(6)CMVN+SHE	82.86	84.24	82.82	83.40	23.64%
(7)CMVN+MRE(best)	83.71	85.93	83.63	84.58	29.07%
(8)CMVN+SHE+MRE(best)	83.94	85.82	83.73	84.65	29.39%

Table 1: *Comparison of several representative methods for AURORA 2 clean-condition training. “Impr.” is the error rate reduction as compared to CMVN.*



(a)



(b)



# Integration of MRE with Other Feature Normalization Techniques

- We only consider MRE here because the additional improvements obtainable with SHE+MRE as shown in Table 1 were found to be limited, and indeed involved much higher computational costs.

Clean condition training	Set A	Set B	Set C	Avg.	Relative error rate reduction
(1)CMVN	77.52	78.86	78.53	78.26	-----
(2)HEQ	82.44	84.45	83.11	83.38	-----
(3)HEQ+MRE	84.31	86.47	84.56	85.22	(to HEQ) 11.07%
(4)HOCMN	83.78	86.12	83.87	84.73	-----
(5)HOCMN+MRE	85.10	87.15	85.34	85.97	(to HOCMN) 8.12%
(6)AFE	86.49	85.58	84.90	85.81	-----

Table 2: *Recognition results of MRE integrated with HEQ and HOCMN under AURORA 2 clean-condition training.*