heap

- complete binary tree (review)
- heap and priority queues (Chapter 9)
- binary heap and min-heap
- max-heap demo
- max-heap coding
- heap sort (Chapter 7)

heap coding: heap.h

Heap ADT: A **one dimensional array** is used to simplify parent and child calculations.

```
struct Heap {
 int *nodes;  // an array of nodes
 int capacity; // array size of node or key, item
 int N; // the number of nodes in the heap
 bool (*comp) (Heap*, int, int);
 Heap(int capa = 2) {
   capacity = capa;
   nodes = new int[capacity];
   N = 0;
   comp = nullptr;
 };
 ~Heap() {};
};
using heap = Heap*;
```

heap coding: heap.h

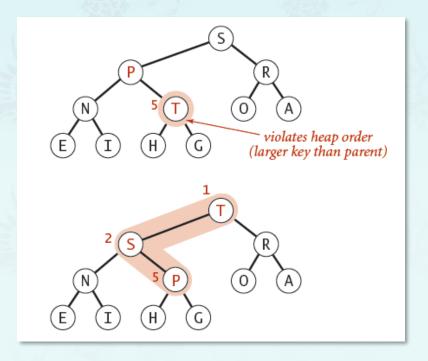
```
void clear(heap hp);
                             // deallocate heap
int size (heap hp);
                          // return nodes in heap currently
int level(int n);
                             // return level based on num of nodes
int capacity (heap hp);
                          // return its capacity (array size)
int reserve (heap hp, int capa); // reserve the array size (= capacity)
                          // return true/false
int full (heap hp);
int empty(heap hp);
                           // return true/false
                       // add a new key
void grow(heap hp, int key);
                          // delete a queue
void trim(heap hp);
                             // convert a complete BT into a heap
int heapify (heap hp);
// helper functions to support grow/trim functions
int less(heap hp, int i, int j); // used in max heap
int more (heap hp, int i, int j); // used in min heap
// helper functions to check heap invariant
```

Promotion in a heap: swim

- To eliminate the violation:
 - Swap key in child with key in parent.
 - Repeat until heap order restored.

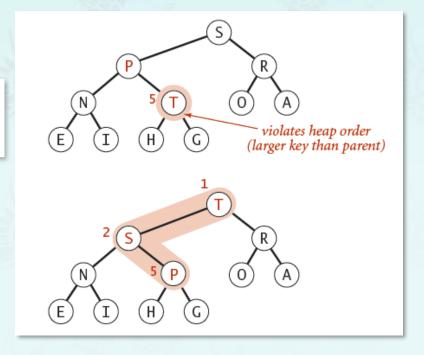
swim up or sink down

This is a maxheap example.

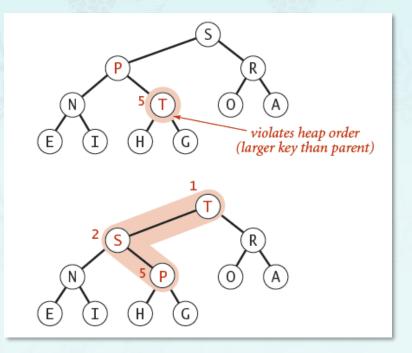


- To eliminate the violation:
 - Swap key in child with key in parent.
 - Repeat until heap order restored.

```
bool (heap h, int p, int c) {
   return h->nodes[p] < h->nodes[c];
}
```



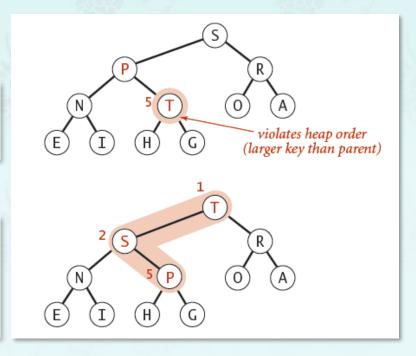
- To eliminate the violation:
 - Swap key in child with key in parent.
 - Repeat until heap order restored.



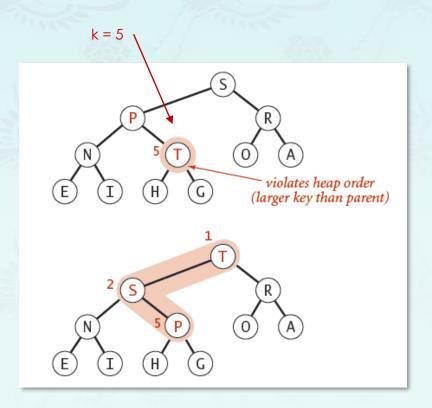
- To eliminate the violation:
 - Swap key in child with key in parent.
 - Repeat until heap order restored.

```
bool less(heap h, int p, int c) {
    return h->nodes[p] < h->nodes[c];
}
```

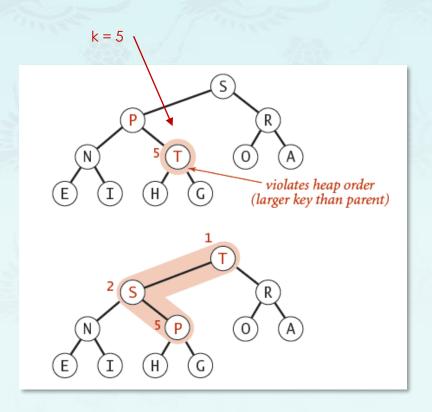
```
void swap(heap h, int p, int c) {
   int item = h->nodes[p];
   h->nodes[p] = h->nodes[c];
   h->nodes[c] = item;
}
```



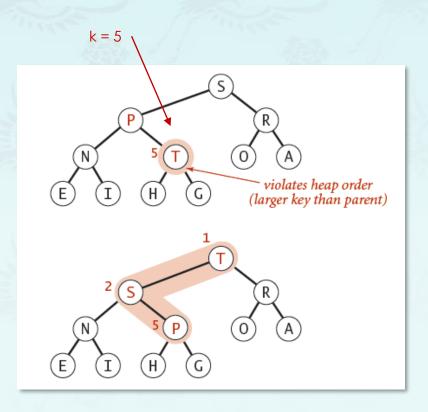
- To eliminate the violation:
 - Swap key in child with key in parent.
 - Repeat until heap order restored.



- To eliminate the violation:
 - Swap key in child with key in parent.
 - Repeat until heap order restored.



- To eliminate the violation:
 - Swap key in child with key in parent.
 - Repeat until heap order restored.



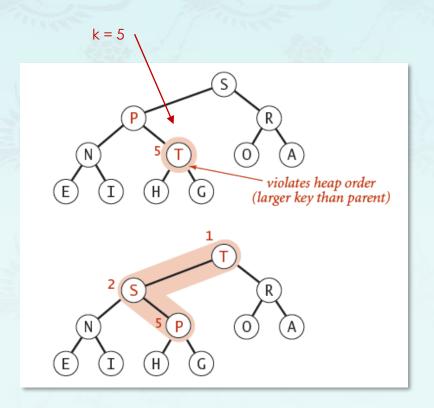
- To eliminate the violation:
 - Swap key in child with key in parent.
 - Repeat until heap order restored.

```
not reached at root parent of k

void swim(h p h, int k)

while (

{
```



- To eliminate the violation:
 - Swap key in child with key in parent.
 - Repeat until heap order restored.

```
not reached at root

void swim(h p h, int k)

while (k > 1 &&

{

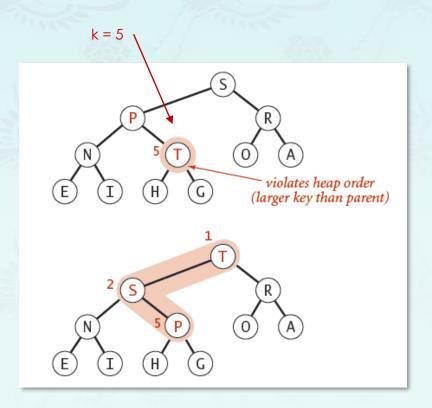
while (k > 1 &&

{

parent(k/2) is less its child(k)

| the continuous parent(k/2) is less its child(k)

| the continuous parent(k/2) is less its child(k)
```



- To eliminate the violation:
 - Swap key in child with key in parent.
 - Repeat until heap order restored.

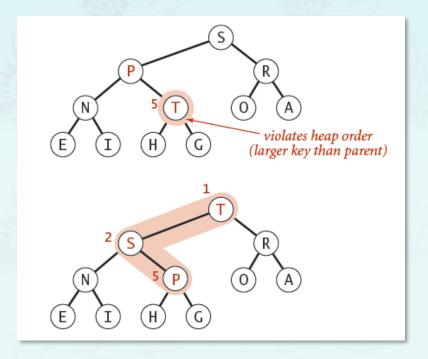
```
not reached at root

void swim(h p h, int k)

while (k > 1 && less(h, k / 2, k))

swap parent(k/2) and its child(k)

swap parent(k/2) and its child(k)
```



- To eliminate the violation:
 - Swap key in child with key in parent.
 - Repeat until heap order restored.

```
not reached
  at root

void swim(h p h, int k)

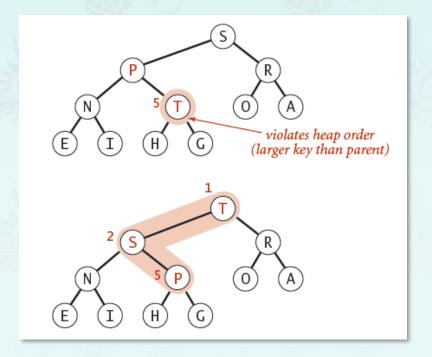
while (k > 1 && less(h, k / 2, k))

swap(h, k / 2, k);

move up
  one level

parent(k/2) is less
  its child(k)

swap parent(k/2)
  and its child(k)
```



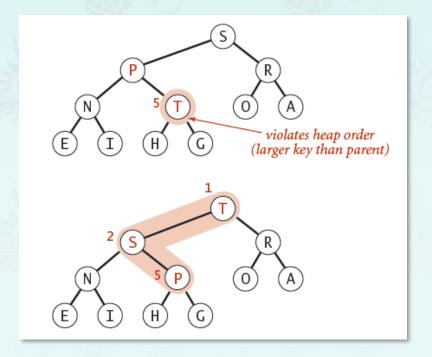
- To eliminate the violation:
 - Swap key in child with key in parent.
 - Repeat until heap order restored.

```
not reached
    at root

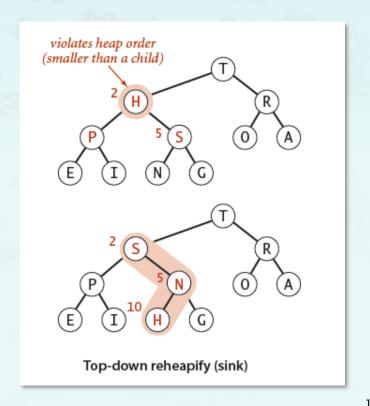
void swim(h p h, int k)

{
    while (k > 1 && less(h, k / 2, k))
    {
        swap(h, k / 2, k);
        k = k / 2;
    }
}

move up
    one level
```



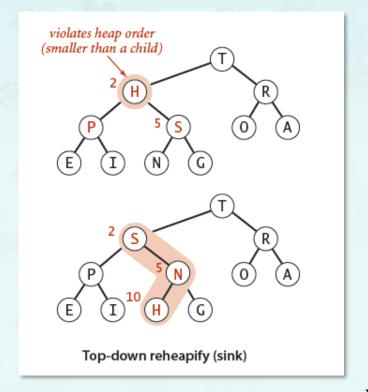
swim up or sink down



Demotion in a heap: sink

- Parent's key becomes smaller than one (or both) of its children's.
- To eliminate the violation:
 - Swap key in parent with key in larger child (of two)
 - Repeat until heap order restored.

This is a maxheap example.

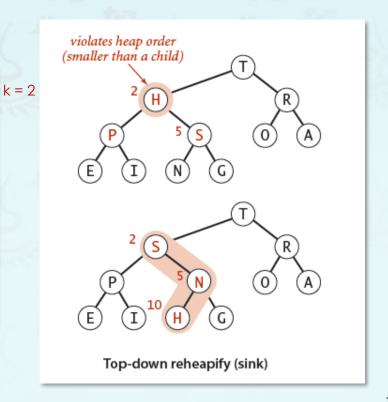


Demotion in a heap: sink

- Parent's key becomes smaller than one (or both) of its children's.
- To eliminate the violation:
 - Swap key in parent with key in larger child (of two)
 - Repeat until heap order restored.

```
void sink(heap h, int k)
{
  while (k's child not reached the last)
  {
    find the larger child of k, let it be j. (j = 5)

    if k's key is not less than j's key, break;
    swap k and j since k's key > j's key
    set k to the next node w
}
}
```

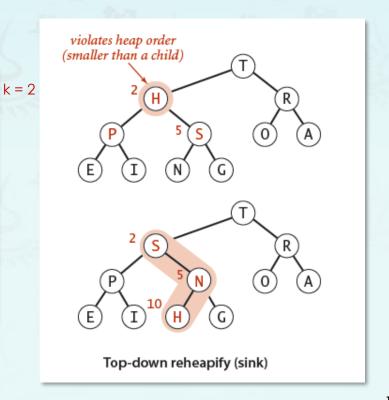


Demotion in a heap: sink

- Parent's key becomes smaller than one (or both) of its children's.
- To eliminate the violation:
 - Swap key in parent with key in larger child (of two)
 - Repeat until heap order restored.

```
void sink(heap h, int k)
{
  while (k's child not reached the last)
  {
    find the larger child of k, let it be j. (j = 5)

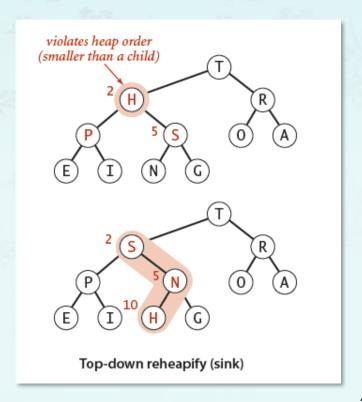
    if k's key is not less than j's key, break;
    swap k and j since k's key > j's key
    set k to the next node which is j.
  }
}
```



Demotion in a heap: sink

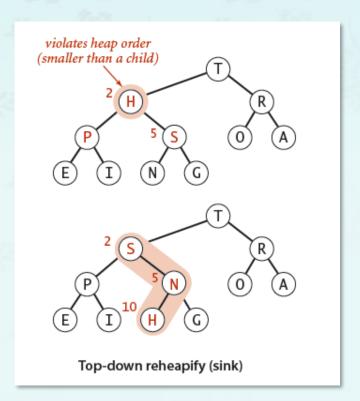
- Parent's key becomes smaller than one (or both) of its children's.
- To eliminate the violation:
 - Swap key in parent with key in larger child
 - Repeat until heap order restored.

```
void sink(heap h, int k)
{
  while (k's child not reached the last)
  {
    find the larger child of k, let it be j. (j = 5)
}
```



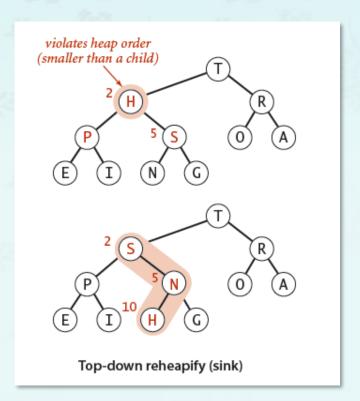
Demotion in a heap: sink

- Parent's key becomes smaller than one (or both) of its children's.
- To eliminate the violation:
 - Swap key in parent with key in larger child
 - Repeat until heap order restored.



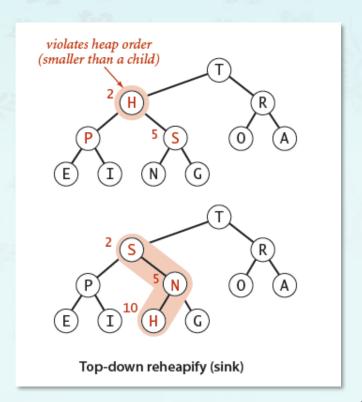
Demotion in a heap: sink

- Parent's key becomes smaller than one (or both) of its children's.
- To eliminate the violation:
 - Swap key in parent with key in larger child
 - Repeat until heap order restored.



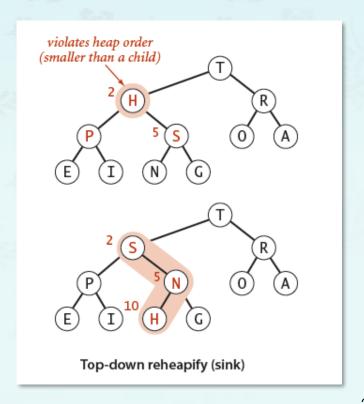
Demotion in a heap: sink

- Parent's key becomes smaller than one (or both) of its children's.
- To eliminate the violation:
 - Swap key in parent with key in larger child
 - Repeat until heap order restored.



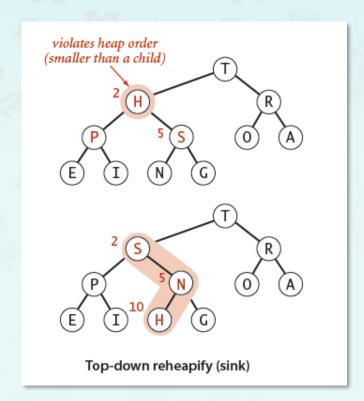
Demotion in a heap: sink

- Parent's key becomes smaller than one (or both) of its children's.
- To eliminate the violation:
 - Swap key in parent with key in larger child
 - Repeat until heap order restored.



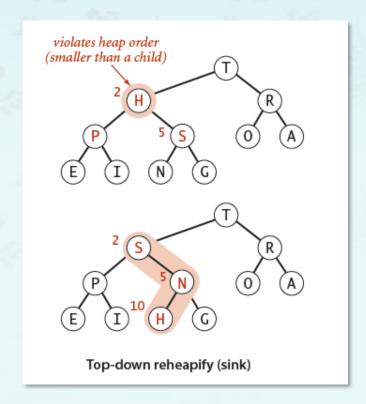
Demotion in a heap: sink

- Parent's key becomes smaller than one (or both) of its children's.
- To eliminate the violation:
 - Swap key in parent with key in larger child
 - Repeat until heap order restored.



Demotion in a heap: sink

- Parent's key becomes smaller than one (or both) of its children's.
- To eliminate the violation:
 - Swap key in parent with key in larger child
 - Repeat until heap order restored.

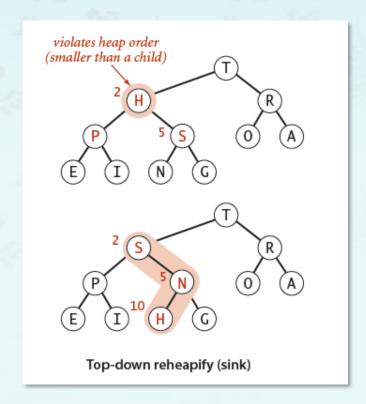


Demotion in a heap: sink

- Parent's key becomes smaller than one (or both) of its children's.
- To eliminate the violation:
 - Swap key in parent with key in larger child
 - Repeat until heap order restored.

```
void sink(heap h, int k)
{
    while (2 * k <= h->N)
    {
        int j = 2 * k;

        if (j < h->N && less(h, j, j + 1)) j++;
        if (!less(h, k, j)) break;
        swap(h, k, j);
        k = j;
    }
}
```



Insert: Add node at end, then swim it up.

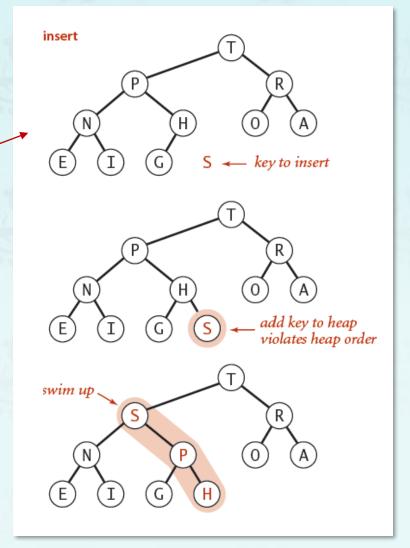
Cost: At most 1 + log N compares.

What is N now?

Insert

Step 1

Step 2



Insertion in a heap: insert Insert: Add node at end, then swim it up. Cost: At most 1 + log N compares. What is N now? (E)void insert(heap h, int key) add key to heap violates heap order struct Heap { // an array of nodes int *nodes; swim up // array size of node or key, item int capacity; // the number of nodes in the heap int N; using heap = *Heap;

Insertion in a heap:

- Insert: Add node at end, then swim it up.
 - Cost: At most 1 + log N compares.

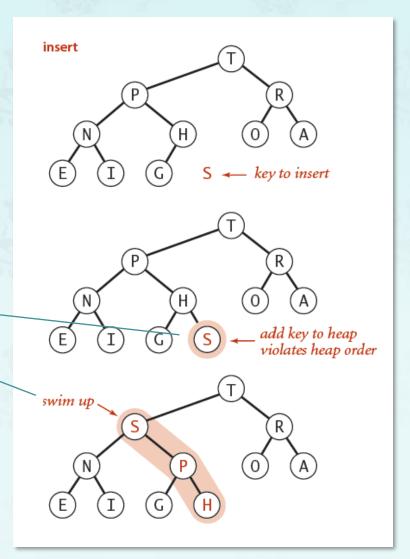
```
void insert(heap h, int key)
{
    h->nodes[++h->N] = key;
}

struct Heap {
    int *nodes;
    int capacity;
    int N;
    int N;
    // the number of nodes in the heap

//
};
using heap = *Heap;

void swim(heap h, int k)
```

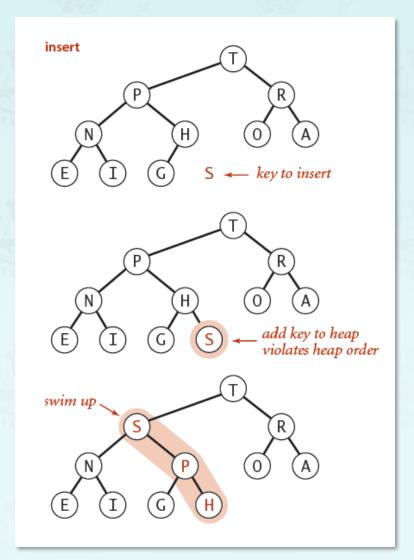
void sink(heap h, int k)



Insertion in a heap:

- Insert: Add node at end, then swim it up.
 - Cost: At most 1 + log N compares.

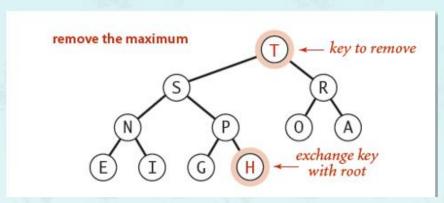
```
void insert(heap h, int key)
{
  h->nodes[++h->N] = key;
  swim(h, h->N);
}
```







- (1) Delete the root (max or min) in a heap:
- (2) How many times do comparisons occur for n nodes ? (select one): n, 2n, n^2, 2 log n, n log n, log n



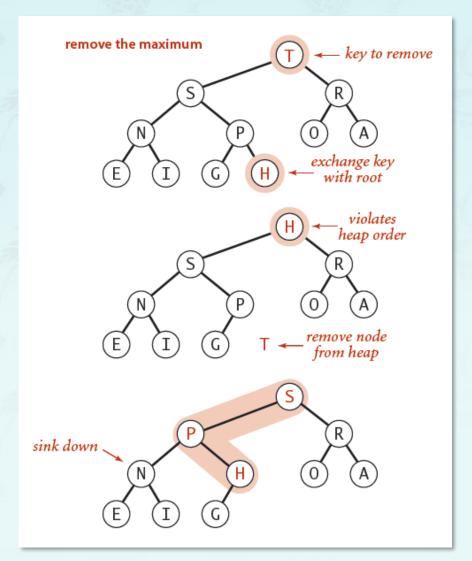
```
void swim(heap h, int k)
void sink(heap h, int k)
bool less(heap h, int p, int c)
void swap(heap h, int p, int c)
```

- Delete root: Swap root with node at end, then sink it down.
- Cost: At most 2 log N compares.

```
void delete(heap h) {

    swap(h, ..., ...);
    sink(h, ...);
}
```

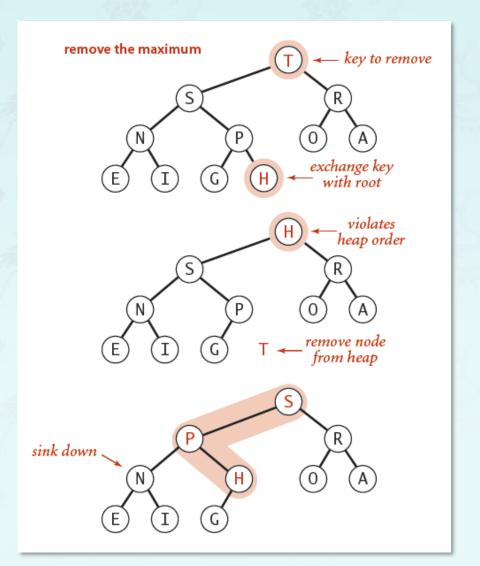
```
void swim(heap h, int k)
void sink(heap h, int k)
bool less(heap h, int p, int c)
void swap(heap h, int p, int c)
```



- Delete root: Swap root with node at end, then sink it down.
- Cost: At most 2 log N compares.

```
void delete(heap h) {
}
```

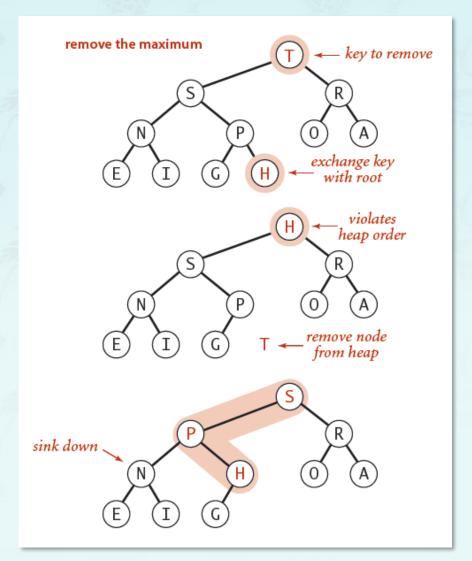
```
void swim(heap h, int k)
void sink(heap h, int k)
bool less(heap h, int p, int c)
void swap(heap h, int p, int c)
```



- Delete root: Swap root with node at end, then sink it down.
- Cost: At most 2 log N compares.

```
void delete(heap h) {
    swap(h, 1, h->N--);
}
```

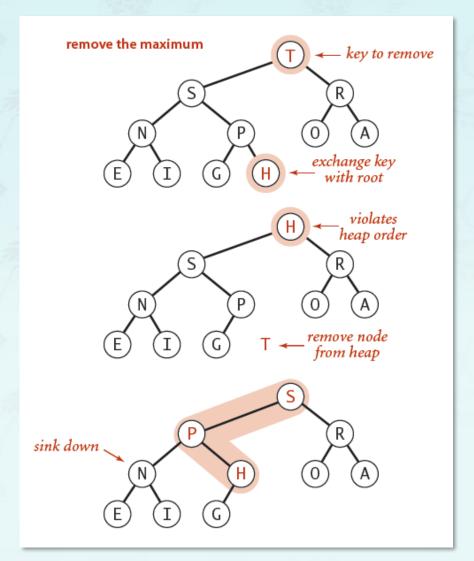
```
void swim(heap h, int k)
void sink(heap h, int k)
bool less(heap h, int p, int c)
void swap(heap h, int p, int c)
```



- Delete root: Swap root with node at end, then sink it down.
- Cost: At most 2 log N compares.

```
void delete(heap h) {
    swap(h, 1, h->N--);
    sink(h, 1);
}
```

```
void swim(heap h, int k)
void sink(heap h, int k)
bool less(heap h, int p, int c)
void swap(heap h, int p, int c)
```



```
void clear(heap hp);
                         // deallocate heap
int size (heap hp);
                         // return nodes in heap currently
int level(int n);
                         // return level based on num of nodes
int capacity(heap hp);  // return its capacity (array size)
int reserve (heap hp, int capa); // reserve the array size (= capacity)
               // return true/false
int full (heap hp);
               // return true/false
int empty(heap hp);
void trim(heap hp);
                     // delete a queue
int heapify (heap hp);
               // convert a complete BT into a heap
// helper functions to support grow/trim functions
int less(heap hp, int i, int j);  // used in max heap
int more (heap hp, int i, int j); // used in min heap
// helper functions to check heap invariant
```

```
// return the number of items in heap
int size(heap hp) {
    return heap->N;
// Is this heap empty?
int empty(heap hp) {
   return (heap->N == 0) ? true : false;
// Is this heap full?
int full(heap hp) {
    return (heap->N == heap->capacity - 1) ? true : false;
```

```
int less(heap hp, int i, int j) {
   return heap->nodes[i] < heap->nodes[j];
}
```

```
void swap(heap hp, int i, int j) {
   int t = heap->nodes[i];
   heap->nodes[i] = heap->nodes[j];
   heap->nodes[j] = t;
}
```

```
void swim(heap hp, int k) {
}
```

```
void sink(heap hp, int k) {
}
```

```
void grow(heap hp, int key) {
    cout << "YOUR CODE HERE\n";
    // add key @ ++heap->N
    // swim up @ heap->N
}
```

```
void trim(heap hp) {
   if (empty(heap)) return;

cout << "YOUR CODE HERE\n";
}</pre>
```

newCBT()	with a given array, instantiate a new complete binary tree its result is neither maxheap nor minheap.
heapify() heapsort() heapprint()	make a complete binary tree into a max/minheap use max/min-heap to sort elements in heap build a binary tree from heap/CBT for display purpose only

newCBT() - convert an int array to CBT

```
// instantiates a CBT with given data and its size.
heap newCBT(int *a, int n) {
   int capa = ?

   heap p = new Heap{ capa };

   p->N = n;
   for (int i = 0; i < n; i++)
       p->nodes[i + 1] = a[i];
   return p;
}
```

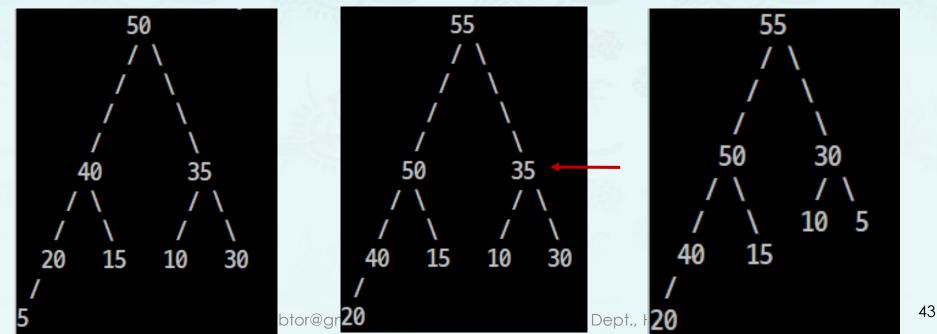
Priority queue

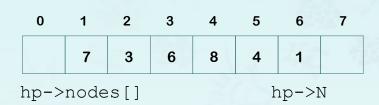
It is like a regular queue or stack data structure, but where additionally **each element** has a "priority" associated with it. In a priority queue, an element with high priority is served before an element with low priority.

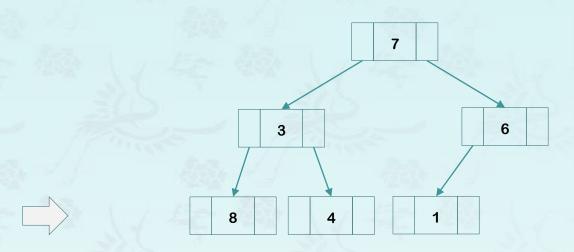
- "trim" removes the root which has the highest priority
- "priority queue" lets user modify the priority (or value) of an element) and move it to the position based on its new priority in the queue.

For example:

- If you **change 5 to 55**, it will go up to the root and 20 is placed at the bottom.
- If you **change 35 to 5**, 30 will go up where 35 is, then 5 goes down to the right corner.

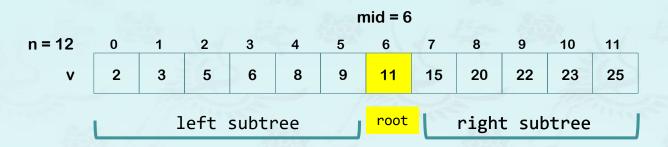




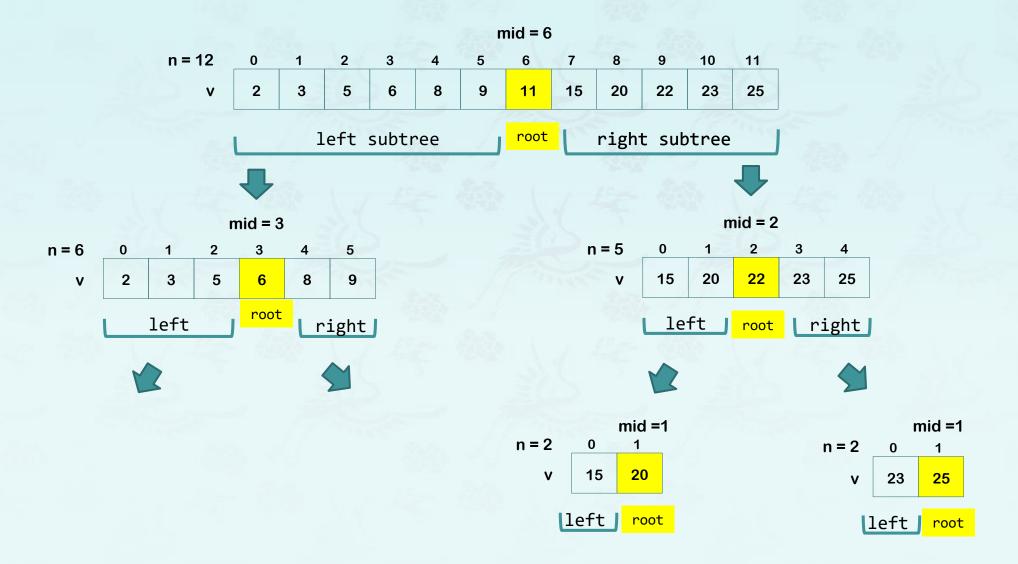




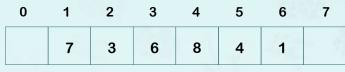
Building AVL tree from BST in O(n) - Review



Building AVL tree from BST in O(n) - Review



Building AVL tree from BST in O(n) - Review





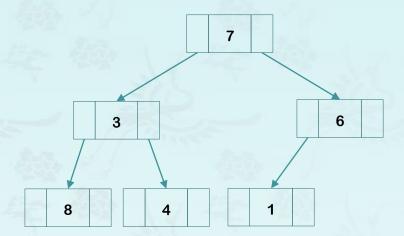
hp->nodes[]

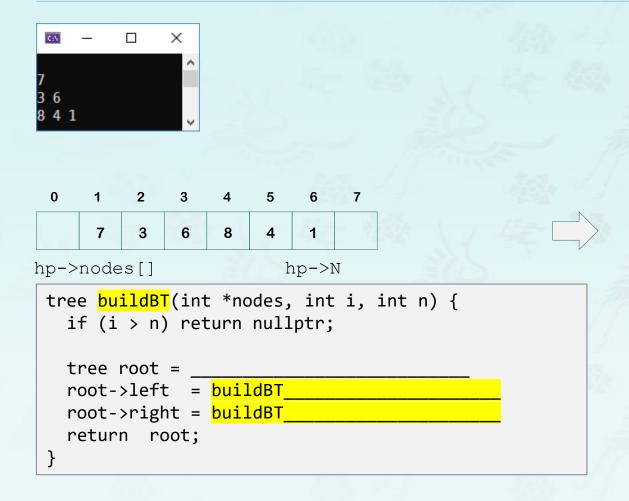
hp->N

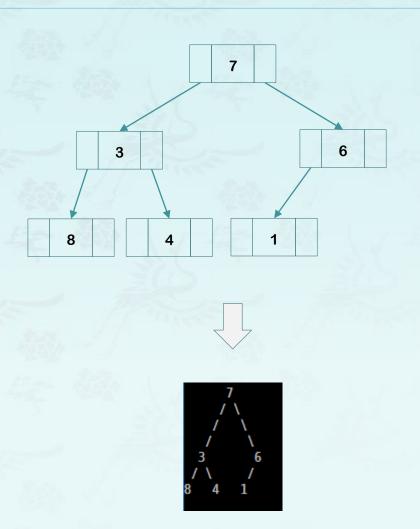
Create a recursive function that creates a binary tree from an int array. This function takes an int array, starting index, and size of the array and returns the root as shown below:

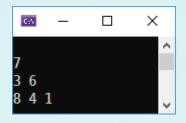
tree buildBT(int *nodes, int i, int n) {

- 1. If i > n, return nulltptr terminate condition
- 2. Create the tree (root) node with nodes[i]).
 - A. Invoke buildBT() for all its left children (or i * 2). Set its return to the left child of the root.
 - B. Invoke buildBT() for all its right children (or **i** * **2** + **1**). Set its return to the right child of the root.
- 3. return root









```
0 1 2 3 4 5 6 7

7 3 6 8 4 1

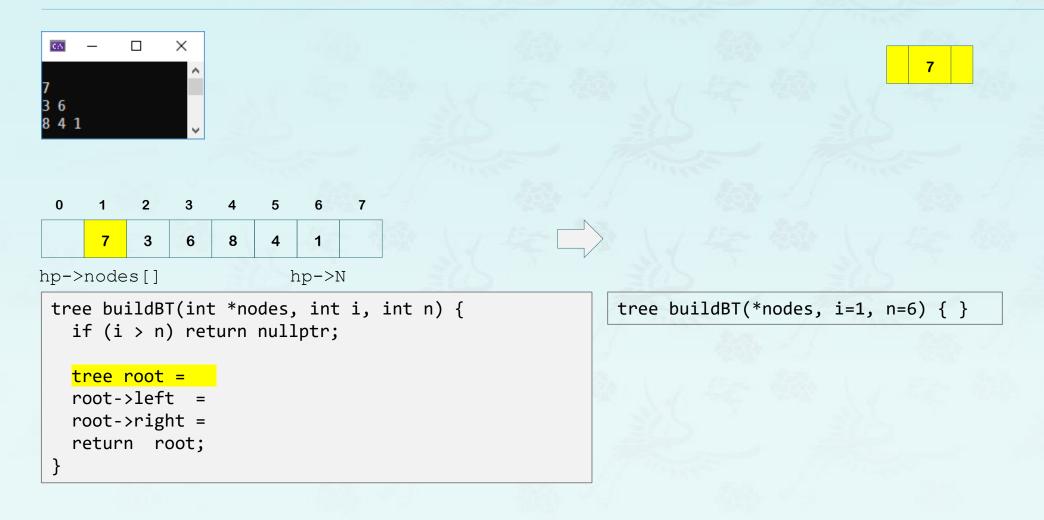
hp->nodes[] hp->N
```

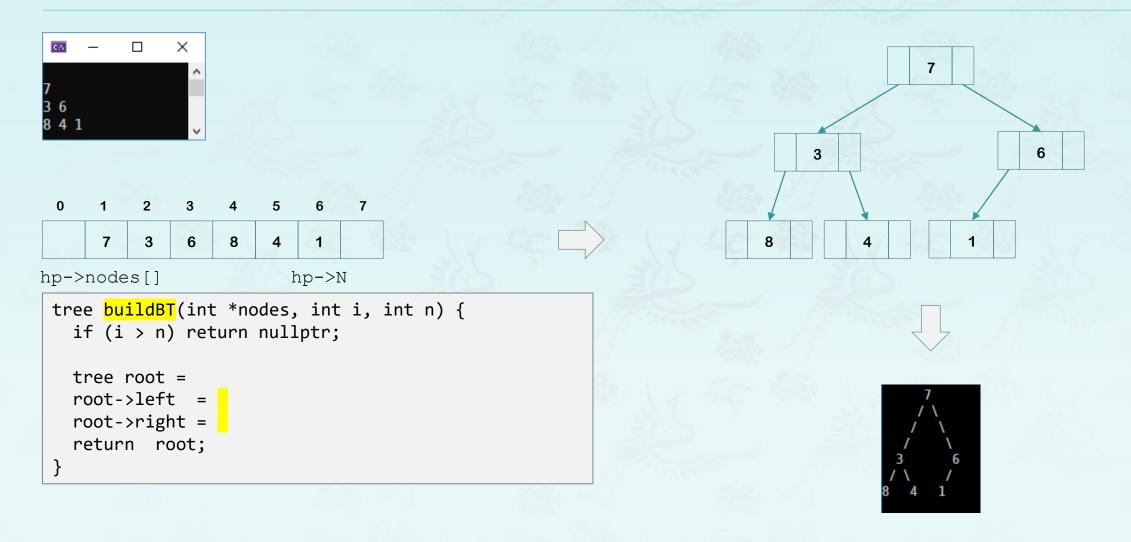
```
tree buildBT(int *nodes, int i, int n) {
  if (i > n) return nullptr;

  tree root =
  root->left =
  root->right =
  return root;
}
```

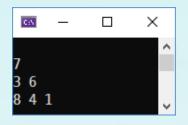
```
void heapprint(heap p) {
  if (empty(p)) return;
  tree root = buildBT(p->nodes, 1, size(p));
  treeprint(root);
}
```

tree buildBT(*nodes, i=1, n=6) { }



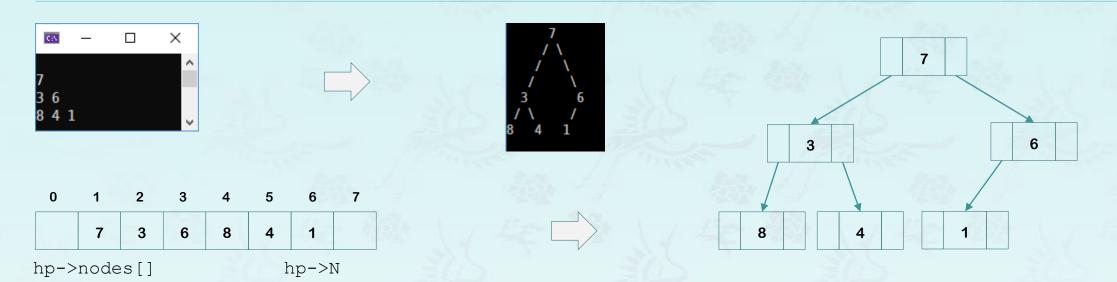


Heapprint(): build a tree from CBT

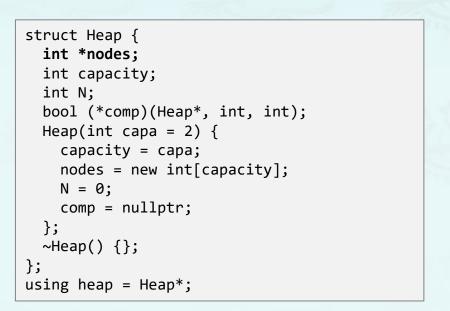






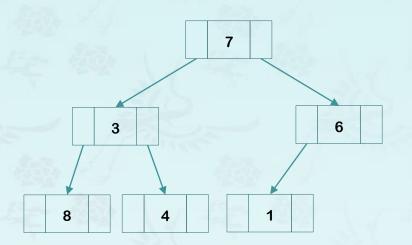




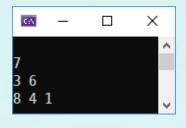


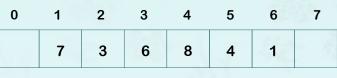






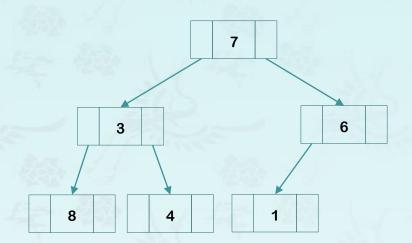
```
struct TreeNode {
   int key;
   TreeNode *left;
   TreeNode *right;
   TreeNode(int k, TreeNode* l, TreeNode* r) {
        key = k; left = l; right = r;
   }
   TreeNode(int k) : key(k), left(nullptr), right(nullptr) {}
   ~TreeNode() {}
};
using tree = TreeNode*;
```



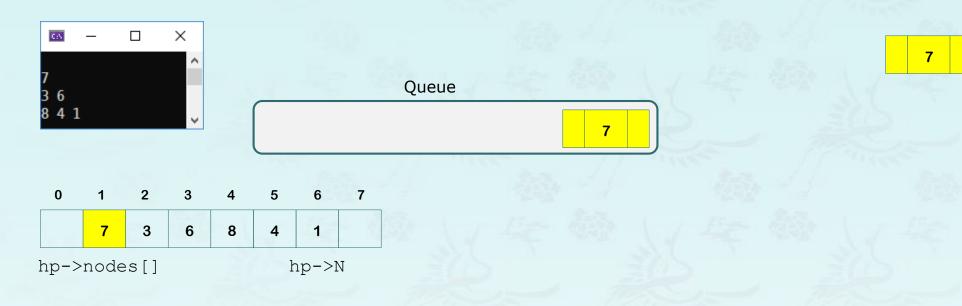


hp->nodes[]

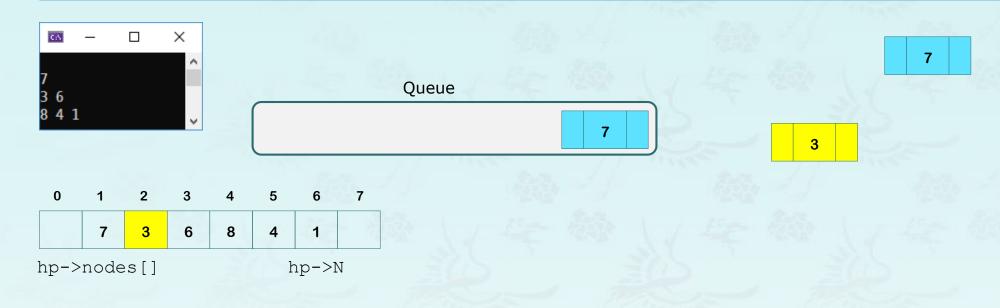




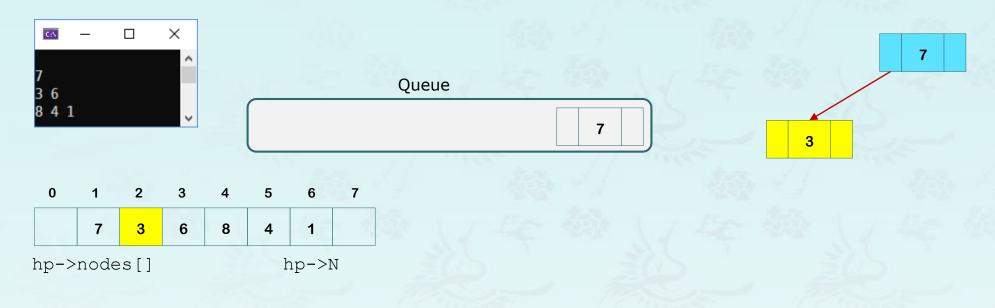
- 1. Create the tree (root) node with the first key from CBT (or nodes[1]).
- 2. Enqueue the root node.
- 3. Loop through from the CBT nodes[2] to nodes[N]
 - A. Make a new node from nodes[].
 - B. Get a tree node in the queue.
 - C. If the left of the tree node doesn't exist, set the new node to the left of the tree node. else if the right of this tree node doesn't exist, set the new node to the right of the tree node.
 - D. If this tree node is full, pop (or dequeu) it.
 - E. enqueue the new node (to add children later if any).
- 4. treeprint(root)



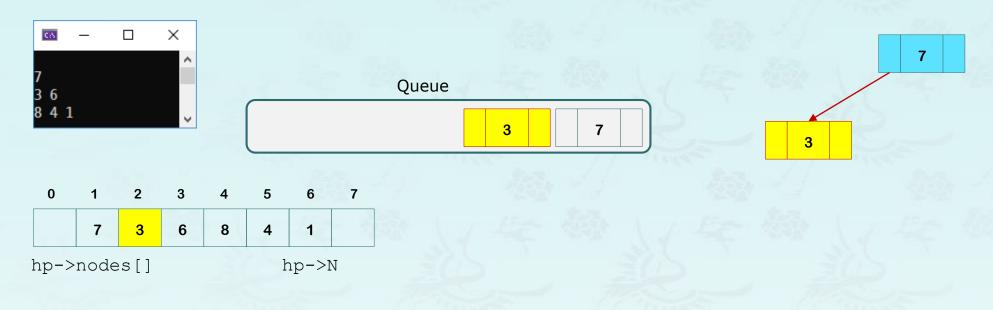
- 1. Create the tree (root) node with the first key from CBT (or nodes[1]).
- 2. Enqueue the root node.
- 3. Loop through from the CBT nodes[2] to nodes[N]
 - A. Make a new node from nodes[].
 - B. Get a **tree node** in the queue.
 - C. If the left of the tree node doesn't exist, set the new node to the left of the tree node. else if the right of this tree node doesn't exist, set the new node to the right of the tree node.
 - D. If this tree node is full, pop (or dequeu) it.
 - E. enqueue the new node (to add children later if any).
- 4. treeprint(root)



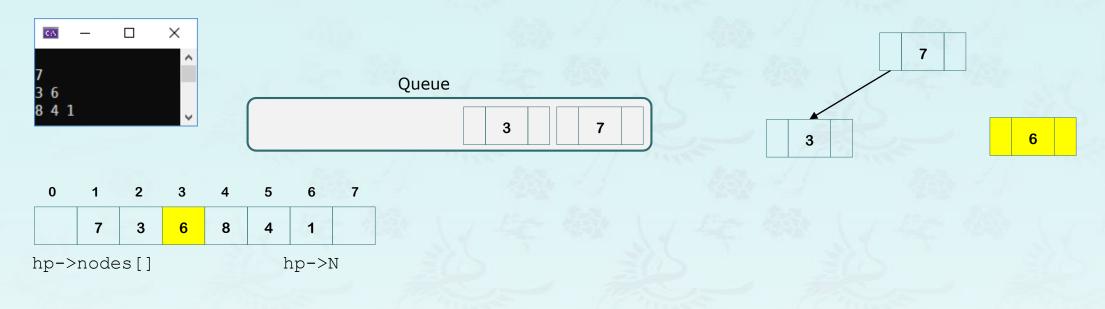
- 1. Create the tree (root) node with the first key from CBT (or nodes[1]).
- 2. Enqueue the root node.
- 3. Loop through from the CBT nodes[2] to nodes[N]
 - A. Make a **new node from nodes**[].
 - B. Get a **tree node** in the queue.
 - C. If the left of the tree node doesn't exist, set the new node to the left of the tree node. else if the right of this tree node doesn't exist, set the new node to the right of the tree node.
 - D. If this tree node is full, pop (or dequeu) it.
 - E. enqueue the new node (to add children later if any).
- 4. treeprint(root)



- 1. Create the tree (root) node with the first key from CBT (or nodes[1]).
- 2. Enqueue the root node.
- 3. Loop through from the CBT nodes[2] to nodes[N]
 - A. Make a new node from nodes[].
 - B. Get a tree node in the queue.
 - C. If the left of the tree node doesn't exist, set the new node to the left of the tree node. else if the right of this tree node doesn't exist, set the new node to the right of the tree node.
 - D. If this tree node is full, pop (or dequeu) it.
 - E. enqueue the new node (to add children later if any).
- 4. treeprint(root)



- 1. Create the tree (root) node with the first key from CBT (or nodes[1]).
- 2. Enqueue the root node.
- 3. Loop through from the CBT nodes[2] to nodes[N]
 - A. Make a new node from nodes[].
 - B. Get a **tree node** in the queue.
 - C. If the left of the tree node doesn't exist, set the new node to the left of the tree node. else if the right of this tree node doesn't exist, set the new node to the right of the tree node.
 - D. If this tree node is full, pop (or dequeu) it.
 - E. enqueue the new node (to add children later if any).
- 4. treeprint(root)



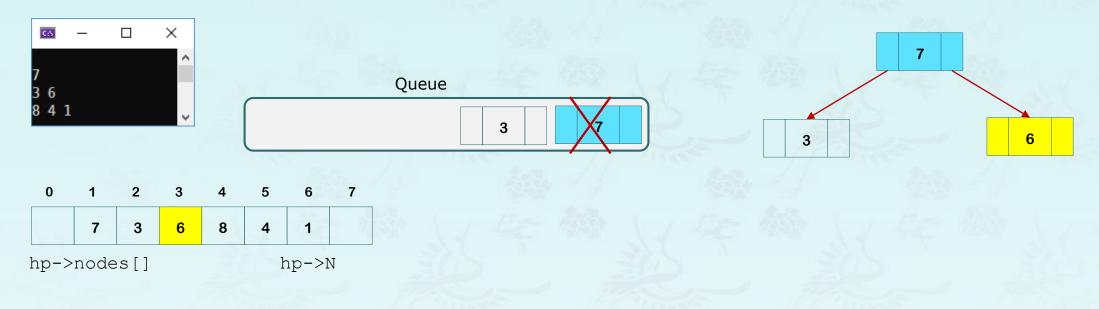
- 1. Create the tree (root) node with the first key from CBT (or nodes[1]).
- 2. Enqueue the root node.
- 3. Loop through from the CBT nodes[2] to nodes[N]
 - A. Make a **new node from nodes**[].
 - B. Get a tree node in the queue.
 - C. If the left of the tree node doesn't exist, set the new node to the left of the tree node. else if the right of this tree node doesn't exist, set the new node to the right of the tree node.
 - D. If this tree node is full, pop (or dequeu) it.
 - E. enqueue the new node (to add children later if any).
- 4. treeprint(root)



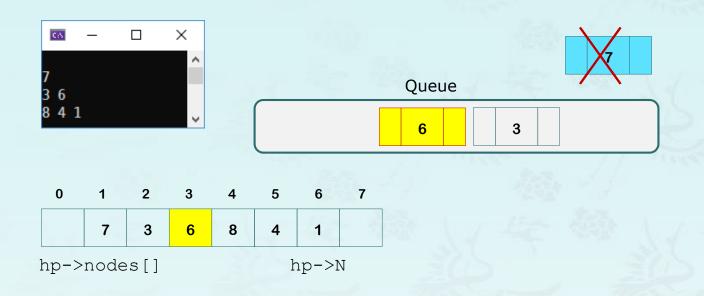
- 1. Create the tree (root) node with the first key from CBT (or nodes[1]).
- 2. Enqueue the root node.
- 3. Loop through from the CBT nodes[2] to nodes[N]
 - A. Make a new node from nodes[].
 - B. Get a **tree node** in the queue.
 - C. If the left of the tree node doesn't exist, set the new node to the left of the tree node. else if the right of this tree node doesn't exist, set the new node to the right of the tree node.
 - D. If this tree node is full, pop (or dequeu) it.
 - E. enqueue the new node (to add children later if any).
- 4. treeprint(root)

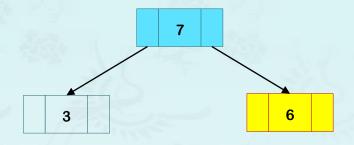


- 1. Create the tree (root) node with the first key from CBT (or nodes[1]).
- 2. Enqueue the root node.
- 3. Loop through from the CBT nodes[2] to nodes[N]
 - A. Make a new node from nodes[].
 - B. Get a **tree node** in the queue.
 - C. If the left of the tree node doesn't exist, set the new node to the left of the tree node.
 - else if the right of this tree node doesn't exist, set the new node to the right of the tree node.
 - D. If this tree node is full, pop (or dequeu) it.
 - E. enqueue the new node (to add children later if any).
- 4. treeprint(root)

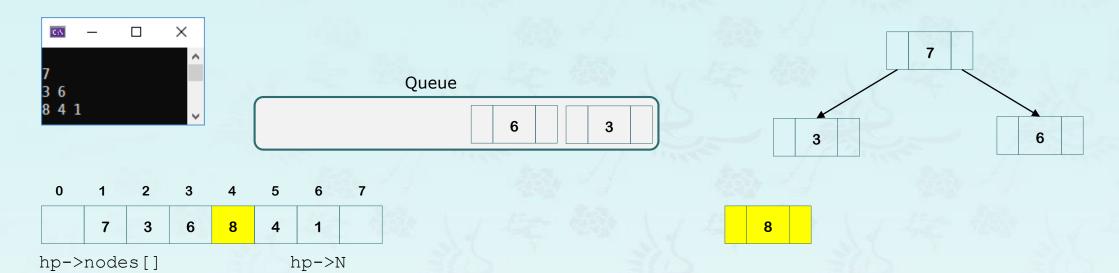


- 1. Create the tree (root) node with the first key from CBT (or nodes[1]).
- 2. Enqueue the root node.
- B. Loop through from the CBT nodes[2] to nodes[N]
 - A. Make a **new node from nodes**[].
 - B. Get a **tree node** in the queue.
 - C. If the left of the tree node doesn't exist, set the new node to the left of the tree node. else if the right of this tree node doesn't exist, set the new node to the right of the tree node.
 - D. If this tree node is full, pop (or dequeu) it.
 - E. enqueue the new node (to add children later if any).
- 4. treeprint(root)





- 1. Create the tree (root) node with the first key from CBT (or nodes[1]).
- 2. Enqueue the root node.
- 3. Loop through from the CBT nodes[2] to nodes[N]
 - A. Make a new node from nodes[].
 - B. Get a **tree node** in the queue.
 - C. If the left of the tree node doesn't exist, set the new node to the left of the tree node. else if the right of this tree node doesn't exist, set the new node to the right of the tree node.
 - D. If this tree node is full, pop (or dequeu) it.
 - E. enqueue the new node (to add children later if any).
- 4. treeprint(root)



- 1. Create the tree (root) node with the first key from CBT (or nodes[1]).
- 2. Enqueue the root node.
- 3. Loop through from the CBT nodes[2] to nodes[N]
 - A. Make a **new node from nodes**[].
 - B. Get a tree node in the queue.
 - C. If the left of the tree node doesn't exist, set the new node to the left of the tree node. else if the right of this tree node doesn't exist, set the new node to the right of the tree node.
 - D. If this tree node is full, pop (or dequeu) it.
 - E. enqueue the new node (to add children later if any).
- 4. treeprint(root)



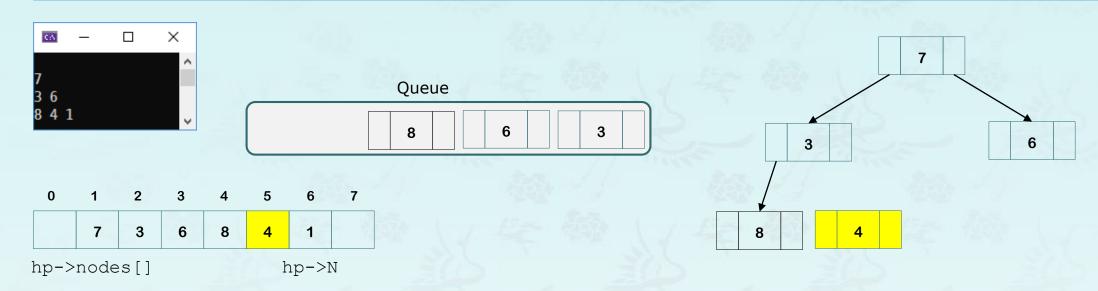
- 1. Create the tree (root) node with the first key from CBT (or nodes[1]).
- 2. Enqueue the root node.
- 3. Loop through from the CBT nodes[2] to nodes[N]
 - A. Make a new node from nodes[].
 - B. Get a **tree node** in the queue.
 - C. If the left of the tree node doesn't exist, set the new node to the left of the tree node. else if the right of this tree node doesn't exist, set the new node to the right of the tree node.
 - D. If this tree node is full, pop (or dequeu) it.
 - E. enqueue the new node (to add children later if any).
- 4. treeprint(root)



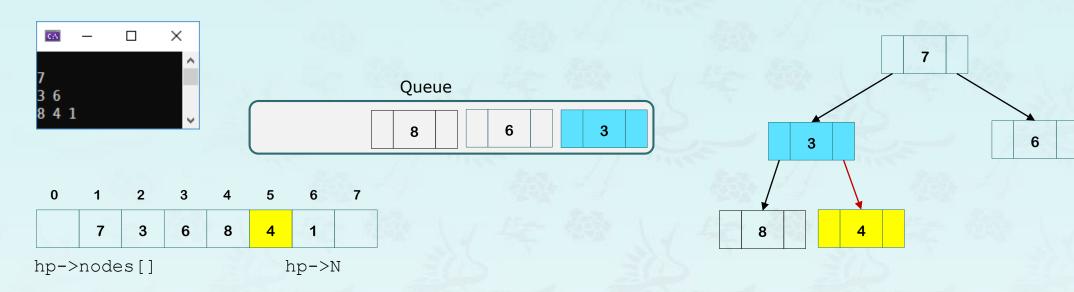
- 1. Create the tree (root) node with the first key from CBT (or nodes[1]).
- 2. Enqueue the root node.
- 3. Loop through from the CBT nodes[2] to nodes[N]
 - A. Make a new node from nodes[].
 - B. Get a **tree node** in the queue.
 - C. If the left of the tree node doesn't exist, set the new node to the left of the tree node. else if the right of this tree node doesn't exist, set the new node to the right of the tree node.
 - D. If this tree node is full, pop (or dequeu) it.
 - E. enqueue the new node (to add children later if any).
- 4. treeprint(root)



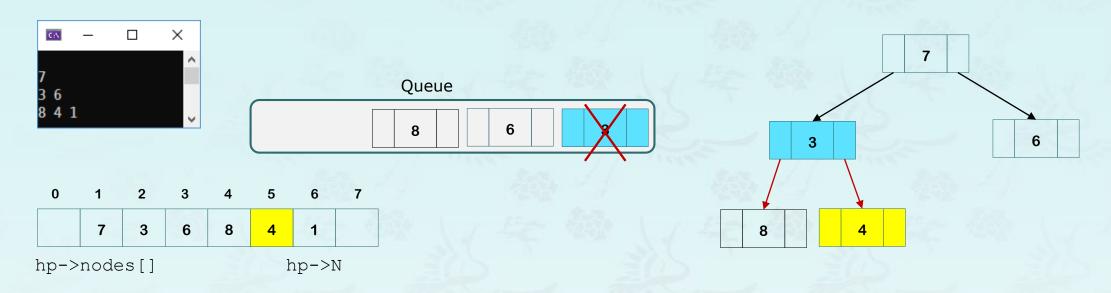
- 1. Create the tree (root) node with the first key from CBT (or nodes[1]).
- 2. Enqueue the root node.
- 3. Loop through from the CBT nodes[2] to nodes[N]
 - A. Make a new node from nodes[].
 - B. Get a **tree node** in the queue.
 - C. If the left of the tree node doesn't exist, set the new node to the left of the tree node. else if the right of this tree node doesn't exist, set the new node to the right of the tree node.
 - D. If this tree node is full, pop (or dequeu) it.
 - E. enqueue the new node (to add children later if any).
- 4. treeprint(root)



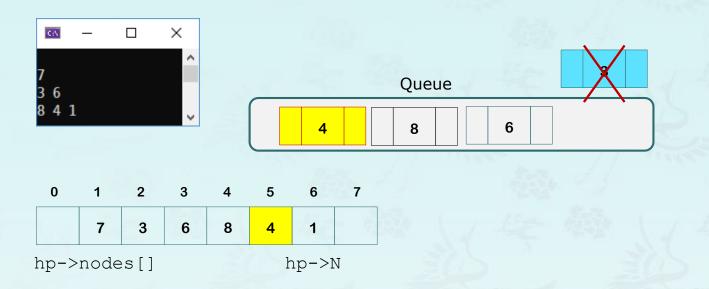
- 1. Create the tree (root) node with the first key from CBT (or nodes[1]).
- 2. Enqueue the root node.
- 3. Loop through from the CBT nodes[2] to nodes[N]
 - A. Make a new node from nodes[].
 - B. Get a tree node in the queue.
 - C. If the left of the tree node doesn't exist, set the new node to the left of the tree node. else if the right of this tree node doesn't exist, set the new node to the right of the tree node.
 - D. If this tree node is full, pop (or dequeu) it.
 - E. enqueue the new node (to add children later if any).
- 4. treeprint(root)

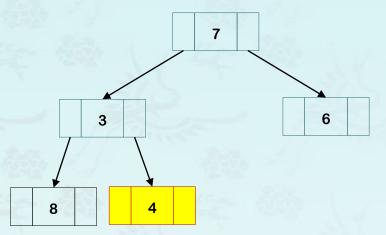


- 1. Create the tree (root) node with the first key from CBT (or nodes[1]).
- 2. Enqueue the root node.
- 3. Loop through from the CBT nodes[2] to nodes[N]
 - A. Make a new node from nodes[].
 - B. Get a **tree node** in the queue.
 - C. If the left of the tree node doesn't exist, set the new node to the left of the tree node.
 - else if the right of this tree node doesn't exist, set the new node to the right of the tree node.
 - D. If this tree node is full, pop (or dequeu) it.
 - E. enqueue the new node (to add children later if any).
- 4. treeprint(root)

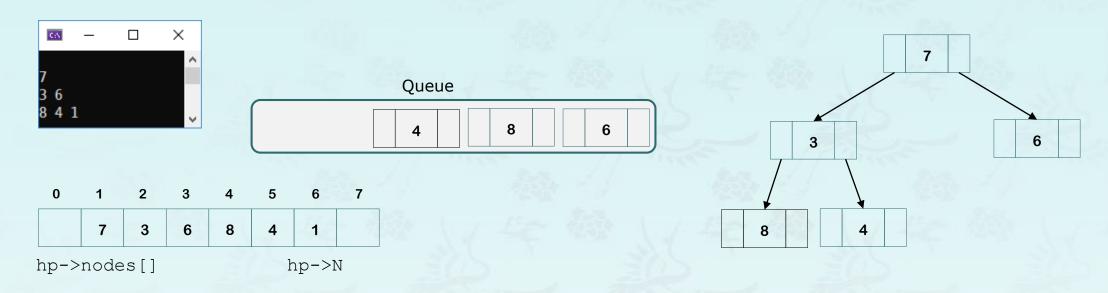


- 1. Create the tree (root) node with the first key from CBT (or nodes[1]).
- 2. Enqueue the root node.
- 3. Loop through from the CBT nodes[2] to nodes[N]
 - A. Make a new node from nodes[].
 - B. Get a **tree node** in the queue.
 - C. If the left of the tree node doesn't exist, set the new node to the left of the tree node. else if the right of this tree node doesn't exist, set the new node to the right of the tree node.
 - D. If this tree node is full, pop (or dequeu) it.
 - E. enqueue the new node (to add children later if any).
- 4. treeprint(root)

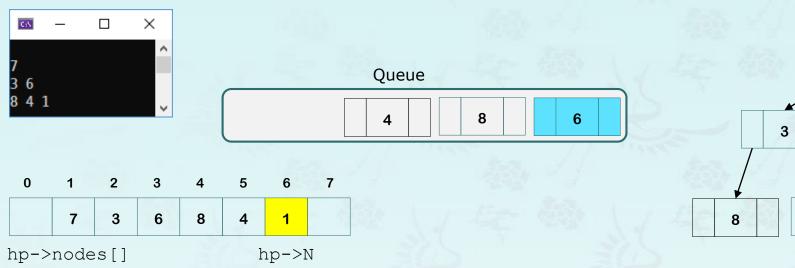


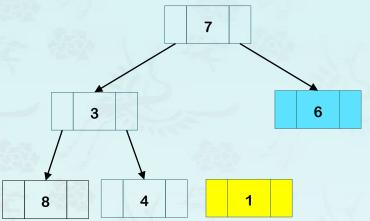


- 1. Create the **tree (root) node** with the first key from CBT (or **nodes[1]**).
- 2. Enqueue the root node.
- 3. Loop through from the CBT nodes[2] to nodes[N]
 - A. Make a new node from nodes[].
 - B. Get a **tree node** in the queue.
 - C. If the left of the tree node doesn't exist, set the new node to the left of the tree node. else if the right of this tree node doesn't exist, set the new node to the right of the tree node.
 - D. If this tree node is full, pop (or dequeu) it.
 - E. enqueue the new node (to add children later if any).
- 4. treeprint(root)

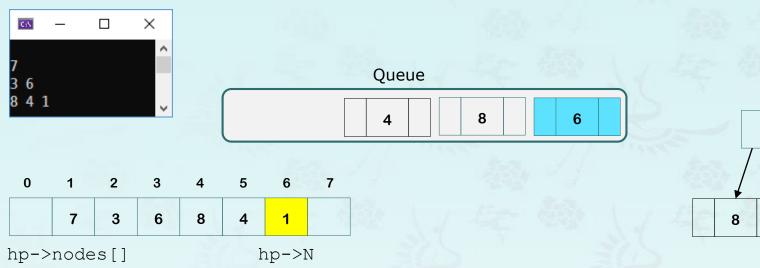


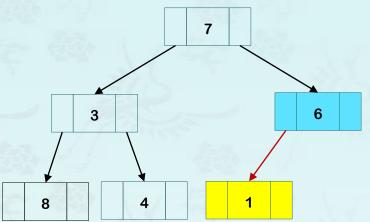
- 1. Create the tree (root) node with the first key from CBT (or nodes[1]).
- 2. Enqueue the root node.
- 3. Loop through from the CBT nodes[2] to nodes[N]
 - A. Make a new node from nodes[].
 - B. Get a tree node in the queue.
 - C. If the left of the tree node doesn't exist, set the new node to the left of the tree node. else if the right of this tree node doesn't exist, set the new node to the right of the tree node.
 - D. If this tree node is full, pop (or dequeu) it.
 - E. enqueue the new node (to add children later if any).
- 4. treeprint(root)



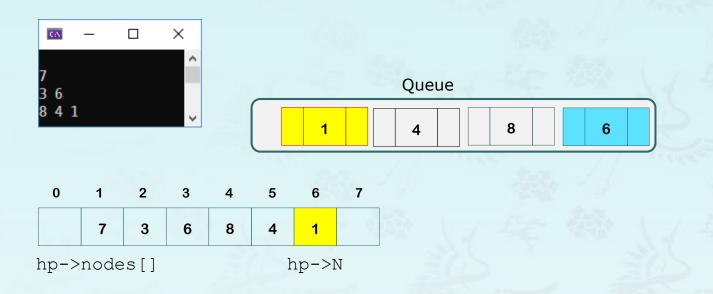


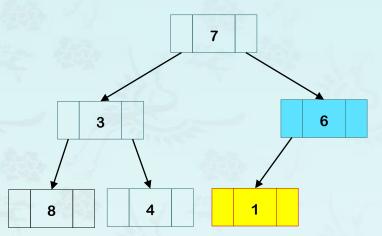
- 1. Create the tree (root) node with the first key from CBT (or nodes[1]).
- 2. Enqueue the root node.
- 3. Loop through from the CBT nodes[2] to nodes[N]
 - A. Make a new node from nodes[].
 - B. Get a **tree node** in the queue.
 - C. If the left of the tree node doesn't exist, set the new node to the left of the tree node. else if the right of this tree node doesn't exist, set the new node to the right of the tree node.
 - D. If this tree node is full, pop (or dequeu) it.
 - E. enqueue the new node (to add children later if any).
- 4. treeprint(root)



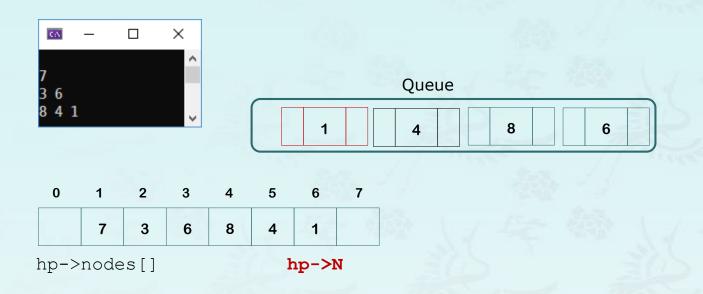


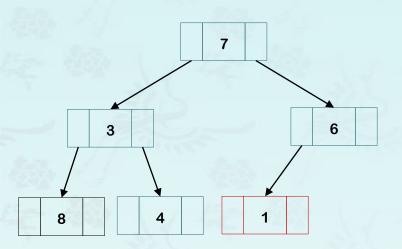
- 1. Create the tree (root) node with the first key from CBT (or nodes[1]).
- 2. Enqueue the root node.
- 3. Loop through from the CBT nodes[2] to nodes[N]
 - A. Make a new node from nodes[].
 - B. Get a **tree node** in the queue.
 - C. If the left of the tree node doesn't exist, set the new node to the left of the tree node. else if the right of this tree node doesn't exist, set the new node to the right of the tree node.
 - D. If this tree node is full, pop (or dequeu) it.
 - E. enqueue the new node (to add children later if any).
- 4. treeprint(root)





- 1. Create the tree (root) node with the first key from CBT (or nodes[1]).
- 2. Enqueue the root node.
- 3. Loop through from the CBT nodes[2] to nodes[N]
 - A. Make a new node from nodes[].
 - B. Get a **tree node** in the queue.
 - C. If the left of the tree node doesn't exist, set the new node to the left of the tree node. else if the right of this tree node doesn't exist, set the new node to the right of the tree node.
 - D. If this tree node is full, pop (or dequeu) it.
 - E. enqueue the new node (to add children later if any).
- 4. treeprint(root)





- 1. Create the tree (root) node with the first key from CBT (or nodes[1]).
- 2. Enqueue the root node.
- 3. Loop through from the CBT nodes[2] to nodes[N]
 - A. Make a new node from nodes[].
 - B. Get a tree node in the queue.
 - C. If the left of the tree node doesn't exist, set the new node to the left of the tree node. else if the right of this tree node doesn't exist, set the new node to the right of the tree node.
 - D. If this tree node is full, pop (or dequeu) it.
 - E. enqueue the new node (to add children later if any).
- 4. treeprint(root)

heap

- complete binary tree (review)
- heap and priority queues (Chapter 9)
- binary heap and min-heap
- max-heap demo
- max-heap coding
- heapsort (Chapter 7)