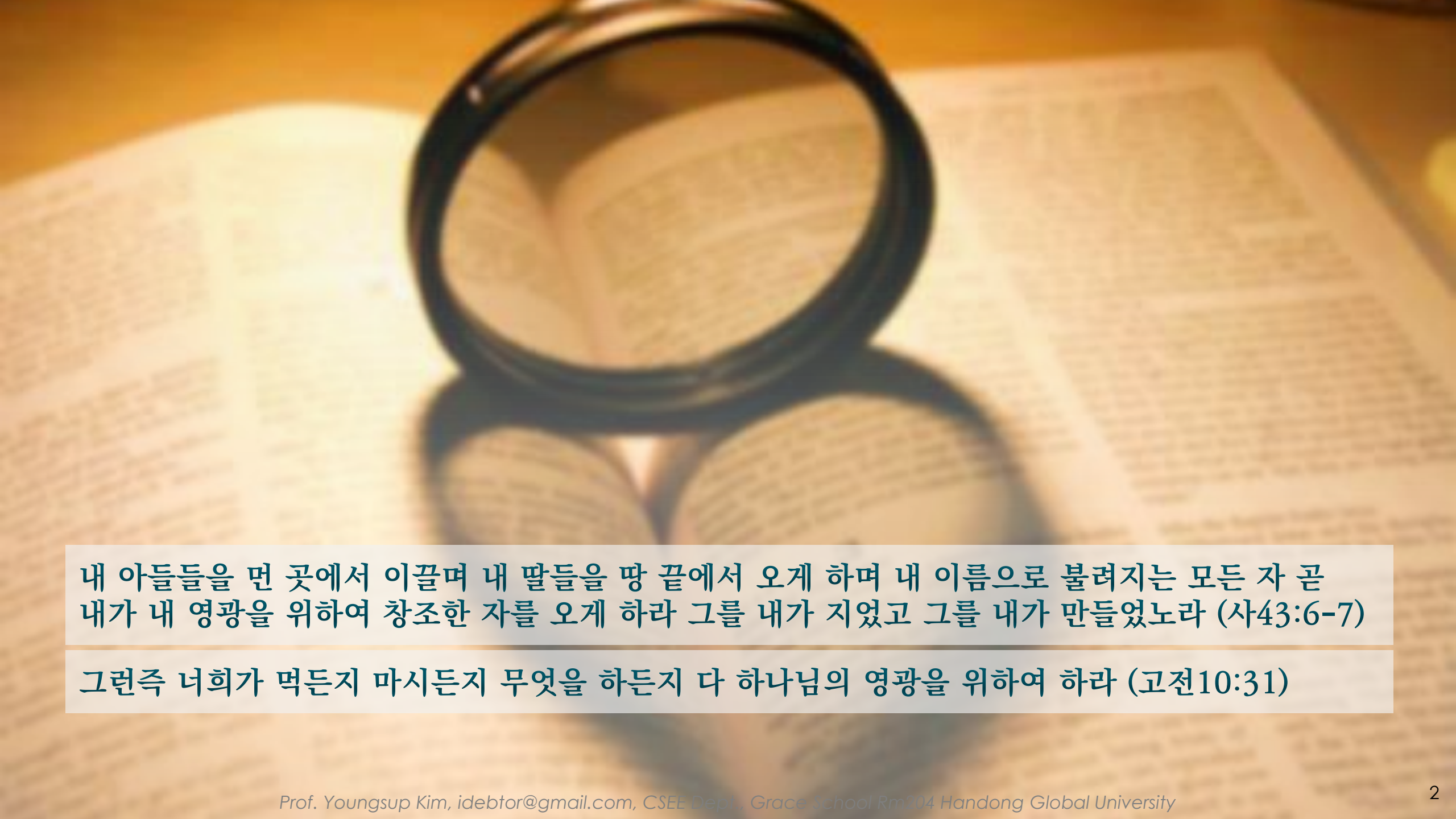


## Data Structures

### Chapter 4

1. Singly Linked List
  - Pointer Reviewed & Linked
  - Linked List (1)
  - **Linked List (2)**
2. Doubly Linked List

A pair of black-rimmed glasses is placed on an open book. The book's pages are yellowed with age, and the text is mostly illegible due to blurring. The lighting is warm and soft, creating a contemplative atmosphere.

내 아들들을 먼 곳에서 이끌며 내 딸들을 땅 끝에서 오게 하며 내 이름으로 불려지는 모든 자 곧  
내가 내 영광을 위하여 창조한 자를 오게 하라 그를 내가 지었고 그를 내가 만들었노라 (사43:6-7)

그런즉 너희가 먹든지 마시든지 무엇을 하든지 다 하나님의 영광을 위하여 하라 (고전10:31)

# Self-Referenced Data Structures

---

```
class Node {  
public:  
    int    data;  
    Node* next;  
};
```



constructor, destructor

# Self-Referenced Data Structures

```
class Node {  
public:  
    int    data;  
    Node* next;  
};
```

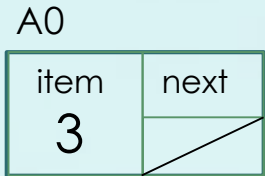
```
struct Node {  
    int    data;  
    Node* next;  
  
    Node(int i=0, Node* n=nullptr){  
        item = i, next = n;  
    }  
    ~Node() {};  
};  
  
int main( ) {  
    Node* head, *x, *y;  
    Node* p = new Node;  
    ...  
}
```

```
struct Node {  
    int    data;  
    Node* next;  
};  
using pNode Node*;  
  
int main() {  
    pNode head, x, y;  
    pNode p = new Node;  
    ...  
}
```

Yet another style of constructor: **"initializer"**

```
Node(int i, Node* n): item(i), next(n) {}
```

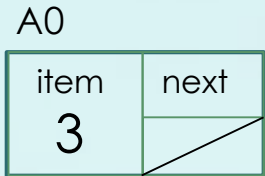
## a new node instantiation



- (1) `pNode n = new Node;`  
`Node* n = new Node;` ← no values set
- (2) `Node* n = new Node();` ← set to 0 or nullptr
- (3) `Node* n = new Node{};` ← set to 0 or nullptr
- (4) `Node* n = new Node(4);` ← Compiler error
- (5) `Node* n = new Node{5};` ← set to 5 or nullptr

```
struct Node {  
    int    item;  
    Node*  prev; ← unused in  
    Node*  next; ← singly linked  
};  
  
struct List {  
    Node*  head;  
    Node*  tail;  
    int    size; //optional  
};  
using pNode = Node*;  
using pList = List*;
```

## a new node instantiation



(1)

```
pNode n = new Node(3);
```



```
Node* n = new Node(3);
```

{2}

```
Node* n = new Node{3};
```

{3}

```
Node* n = new Node{3, nullptr};
```

{4}

```
Node* n = new Node{3, nullptr, nullptr};
```

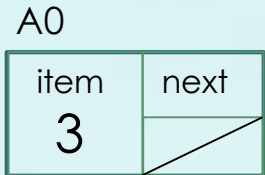
```
struct Node {  
    int    item;  
    Node*  prev; ← unused in singly linked  
    Node*  next;  
};
```

```
struct List {  
    Node*  head;  
    Node*  tail;  
    int    size; //optional  
};  
using pNode = Node*;  
using pList = List*;
```

Any invalid initialization code?



## a new node instantiation



```
pNode n = new Node{3};
```

```
Node* n = new Node{3};
```

```
pNode n = new Node{3, nullptr, nullptr};
```

```
Node* n = new Node{3, nullptr, nullptr};
```

```
struct Node {  
    int    item;  
    Node*  prev; ← unused in singly linked  
    Node*  next;  
};  
  
struct List {  
    Node*  head;  
    Node*  tail;  
    int    size; //optional  
};  
using pNode = Node*;  
using pList = List*;
```

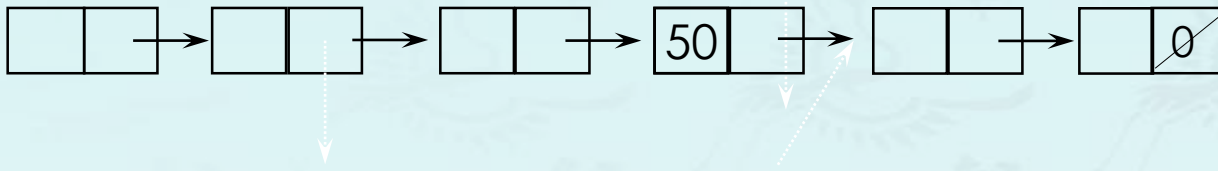
```
struct Node{  
    int item;  
    Node* prev;  
    Node* next;  
    // constructor  
    Node(int d=0, Node* p=nullptr, Node* x=nullptr) {  
        item = d;    prev = p; next = x;  
    }  
    // destructor  
    ~Node() {}  
};
```

can be omitted

## Linked List – find()

**TASK:** Code a function that returns the first node **data = 50** if any, otherwise nullptr.

head



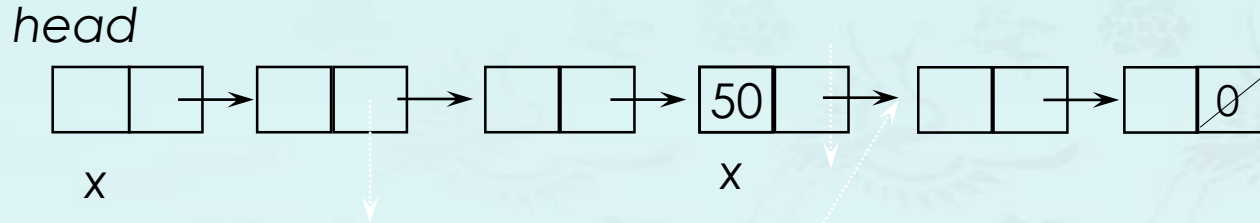
```
pNode find(pNode head, int val)
if (empty(head)) return nullptr;
```

```
bool empty(pNode head)
return head == nullptr;
```



## Linked List – find()

**TASK:** Code a function that returns the first node **data = 50** if any, otherwise nullptr.



```
pNode find(pNode head, int val)
if (empty(head)) return nullptr;

pNode x = head;
while (x != nullptr) {
    if (x->data == val) return x;
    x = x->next;
}
return x;
```

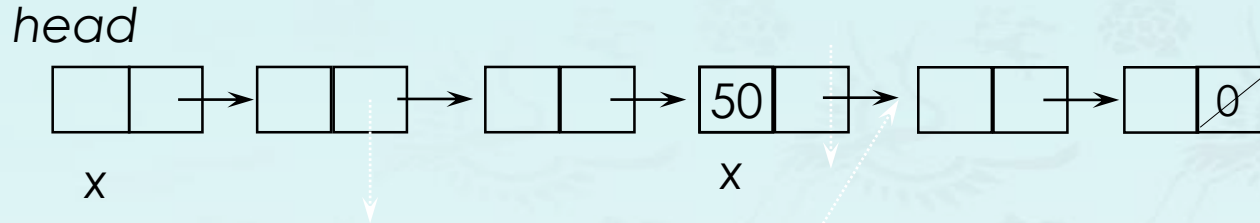
```
bool empty(pNode head)
return head == nullptr;
```

```
pNode find(pNode head, int val)
if (empty(head)) return nullptr;

pNode x = head;
while (x->next != nullptr) {
    if (x->data == val) return x;
    x = x->next;
}
return x;
```

## Linked List – find()

**TASK:** Code a function that returns the first node **data = 50** if any, otherwise nullptr.




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}
return x;
```

```
bool empty(pNode head)
return head == nullptr;
```

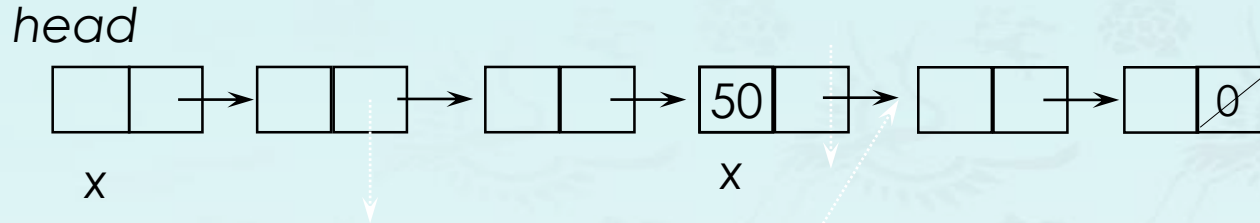
```
pNode find(pNode head, int val)
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pNode x = head;
while (x->next != nullptr) {
    if (x->data == val) return x;
    x = x->next;
}
return x;
```



## Linked List – find()

**TASK:** Code a function that returns the first node **data = 50** if any, otherwise nullptr.



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pNode find(pNode head, int val)
if (empty(head)) return nullptr;

pNode x = head;
while (x != nullptr) {
    if (x->data == val) return x;
    x = x->next;
}
return x;
```

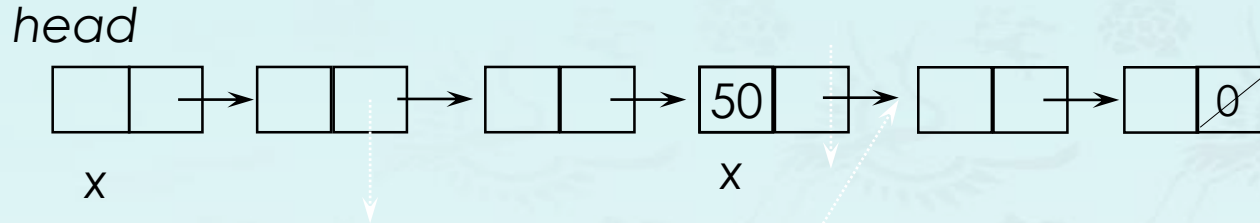
```
bool empty(pNode head)
return head == nullptr;
```

```
pNode find(pNode head, int val)
if (empty(head)) return nullptr;

while (head != nullptr) {
    if (head->data == val) return head;
    head = head->next;
}
return head;
```

## Linked List – find()

**TASK:** Code a function that returns the first node **data = 50** if any, otherwise nullptr.



```
pNode find(pNode head, int val)
if (empty(head)) return nullptr;

pNode x = head;
while (x != nullptr) {
    if (x->data == val) return x;
    x = x->next;
}
return x;
```

```
pNode find(pNode head, int val)
if (empty(head)) return nullptr;

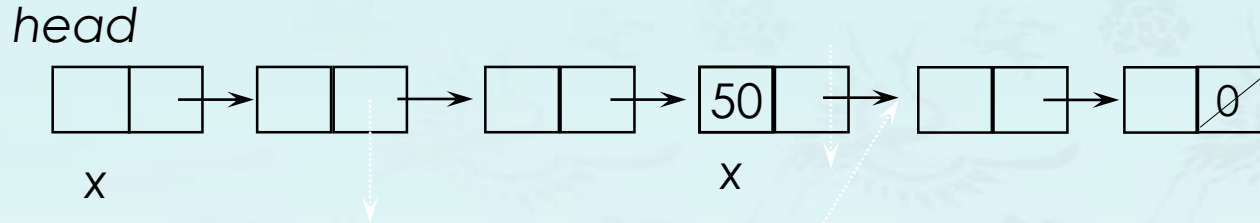
for (pNode x=head; x!=nullptr; x=x->next;){
    if (x->data == val) return x;
}
return x;
```



What is wrong?

## Linked List – find()

**TASK:** Code a function that returns the first node **data = 50** if any, otherwise nullptr.



```
pNode find(pNode head, int val)
if (empty(head)) return nullptr;

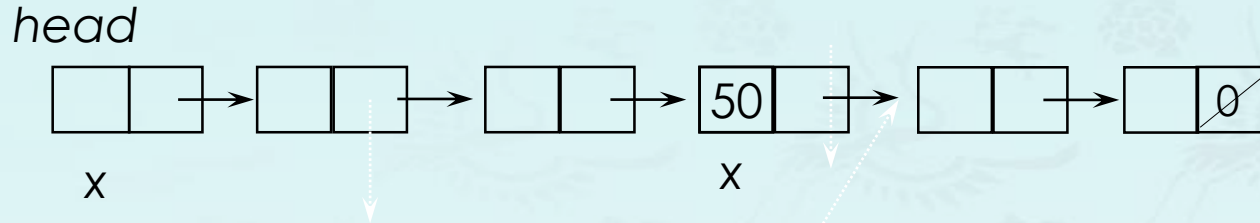
pNode x = head;
while (x != nullptr) {
    if (x->data == val) return x;
    x = x->next;
}
return x;
```

```
pNode find(pNode head, int val)
if (empty(head)) return nullptr;

pNode x = head;
for ( ; x != nullptr; )
    if (x->data == val) return x;
    x = x->next;
}
return x;
```

## Linked List – find()

**TASK:** Code a function that returns the first node **data = 50** if any, otherwise nullptr.



```
pNode find(pNode head, int val)
if (empty(head)) return nullptr;

pNode x = head;
while (x != nullptr) {
    if (x->data == val) return x;
    x = x->next;
}
return x;
```

```
pNode find(pNode head, int val)
if (empty(head)) return nullptr;

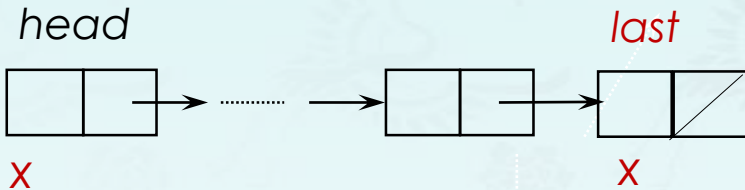
pNode x = head;
for ( ; x != nullptr; x = x->next;){
    if (x->data == val) return x;
}
return x;
```



## Linked List – push\_back()

**TASK:** Code a function that appends a node at the end of the list.

- If the list is empty, the new node becomes the head node.



```
pNode last(pNode head)
```

```
pNode x = head;
while (x != nullptr)
    x = x->next;
return x
```

```
pNode push_back(pNode head, int val)
```

```
if (empty(head))
    return new Node{val, nullptr};
```

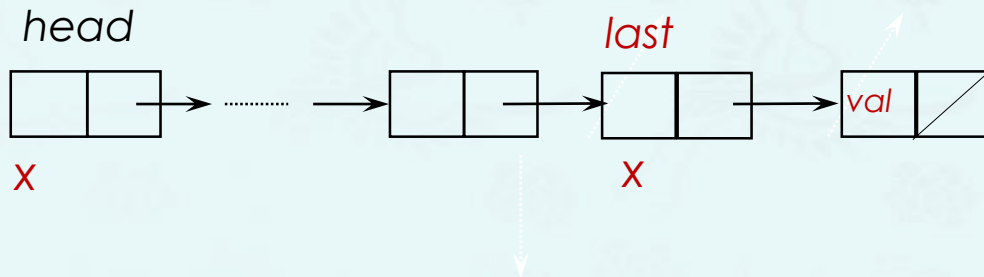
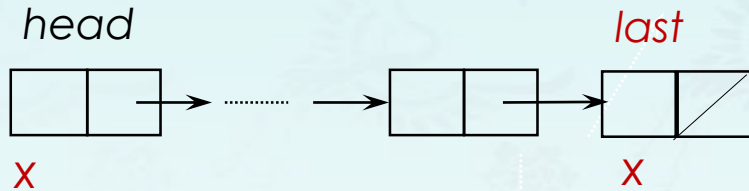
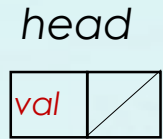
```
pNode last(pNode head)
```

```
pNode x = head;
while (x->next != nullptr)
    x = x->next;
return x;
```

**Q: Which one is correct?**

## Linked List – push\_back()

**TASK:** Code a function that appends a node at the end of the list.  
- If the list is empty, the new node becomes the head node.



```
pNode push_back(pNode head, int val)
```

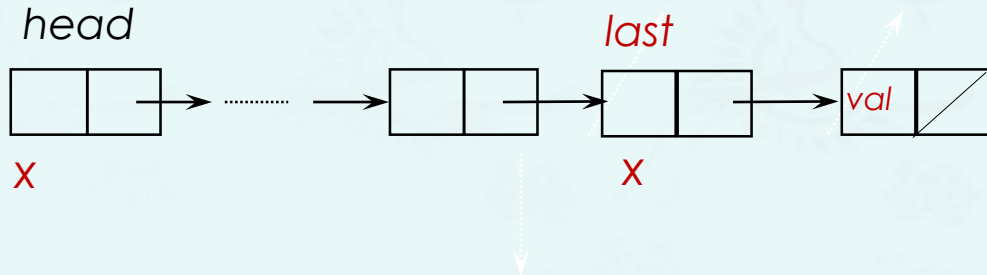
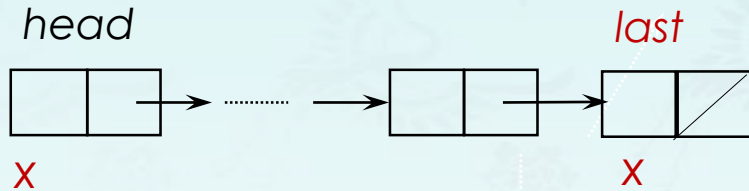
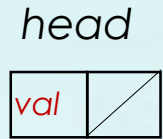
```
if (empty(head))  
    return new Node{val, nullptr};
```

```
pNode last(pNode head)
```

```
pNode x = head;  
while (x->next != nullptr)  
    x = x->next;  
return x;
```

## Linked List – push\_back()

**TASK:** Code a function that appends a node at the end of the list.  
- If the list is empty, the new node becomes the head node.



```
pNode push_back(pNode head, int val)
```

```
if (empty(head))  
    return new Node{val, nullptr};
```

```
pNode x = last(head);  
x->next = new Node{val, nullptr};  
return head;
```

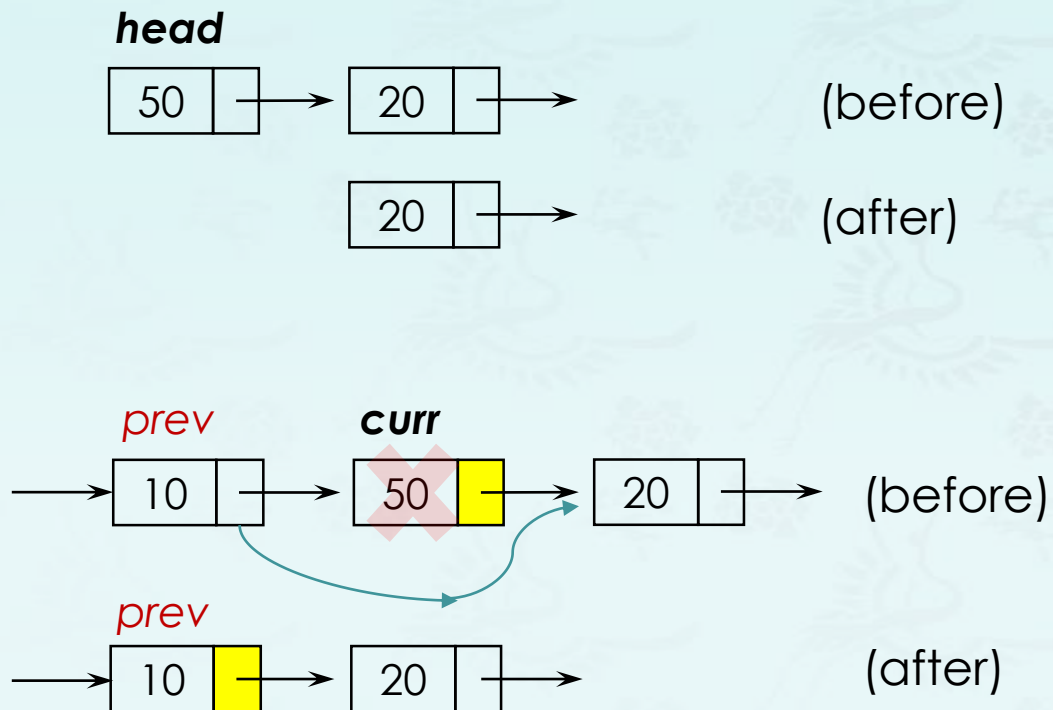
```
pNode last(pNode head)
```

```
pNode x = head;  
while (x->next != nullptr)  
    x = x->next;  
return x;
```

## Linked List – pop()

**TASK:** Code a function that deletes a node with a value specified.

- If the first node(or **head**) is the one to delete, then just invoke **pop\_front()**.
- As observed below, we must know **the pointer x** which is stored in the **previous node** of node x.



```
pNode pop(pNode head, int val)
```

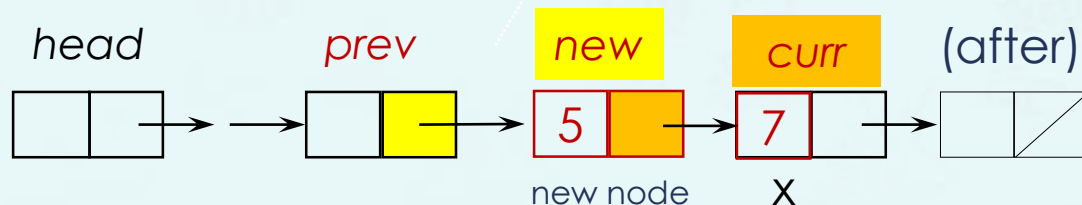
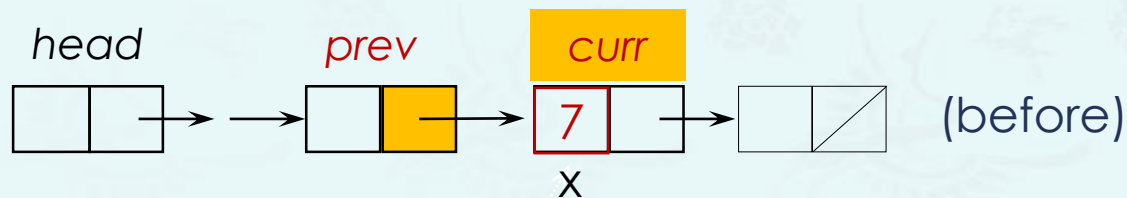
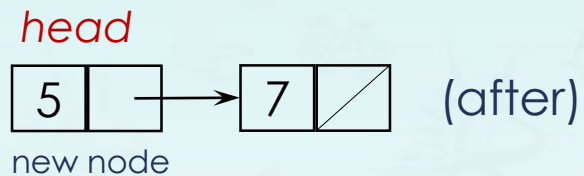
```
if (head->data == val)
    return pop_front(head);

pNode curr = head;
pNode prev = nullptr;
while (curr != nullptr) {
    if (curr->data == val) {
        prev->next = curr->next;
        delete curr;
        return head;
    }
    prev = curr;
    curr = curr->next;
}
return head;
```

## Linked List – insert()

**TASK:** Code a function that inserts a node(5) **at a node position x** specified by a value(7).

- If the first node(or **head**) is the position, then just invoke **push\_front()**.
- As observed below, we must to know **the pointer x** which is stored in the **previous node** of node x.



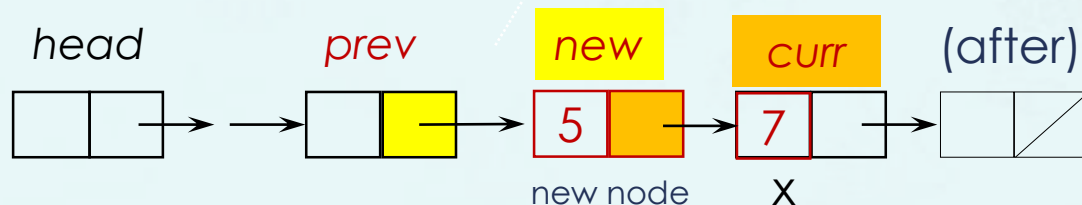
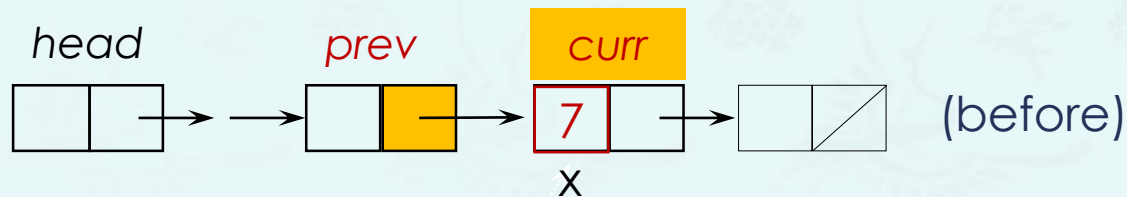
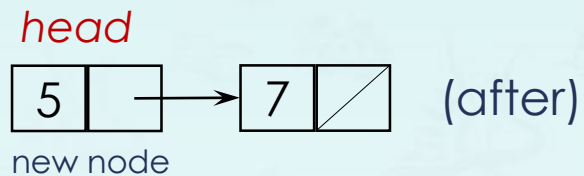
```
pNode insert(pNode head, int val, int x)
{
    if (head->data == x)
        return push_front(val, head);

    pNode curr = head;
    pNode prev = nullptr;
    while (curr != nullptr) {
        if (curr->data == x) {
            [ ] = new Node{ [ ] };
            return head;
        }
        prev = curr;
        curr = curr->next;
    }
    return head;
}
```

## Linked List – insert()

**TASK:** Code a function that inserts a node(5) **at a node position x** specified by a value(7).

- If the first node(or **head**) is the position, then just invoke **push\_front()**.
- As observed below, we must to know **the pointer x** which is stored in the **previous node** of node x.



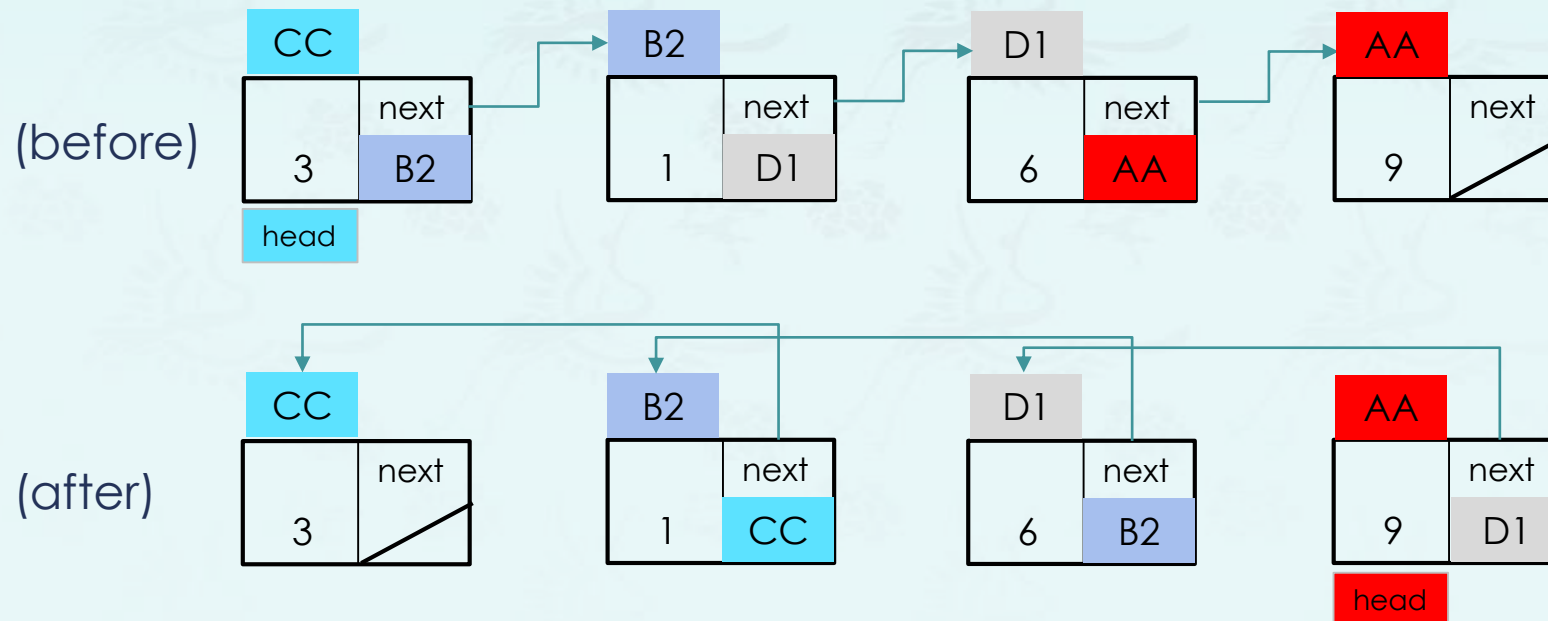
```
pNode insert(pNode head, int val, int x)
{
    if (head->data == x)
        return push_front(val, head);

    pNode curr = head;
    pNode prev = nullptr;
    while (curr != nullptr) {
        if (curr->data == x) {
            prev->next = new Node{val, prev->next};
            return head;
        }
        prev = curr;
        curr = curr->next;
    }
    return head;
}
```



## Linked List – reverse()

**TASK:** reverse a singly linked list in  $O(n)$  which goes through the list once.



## Linked List – reverse()

**TASK:** reverse a singly linked list in  $O(n)$  which goes through the list once and return the new head.

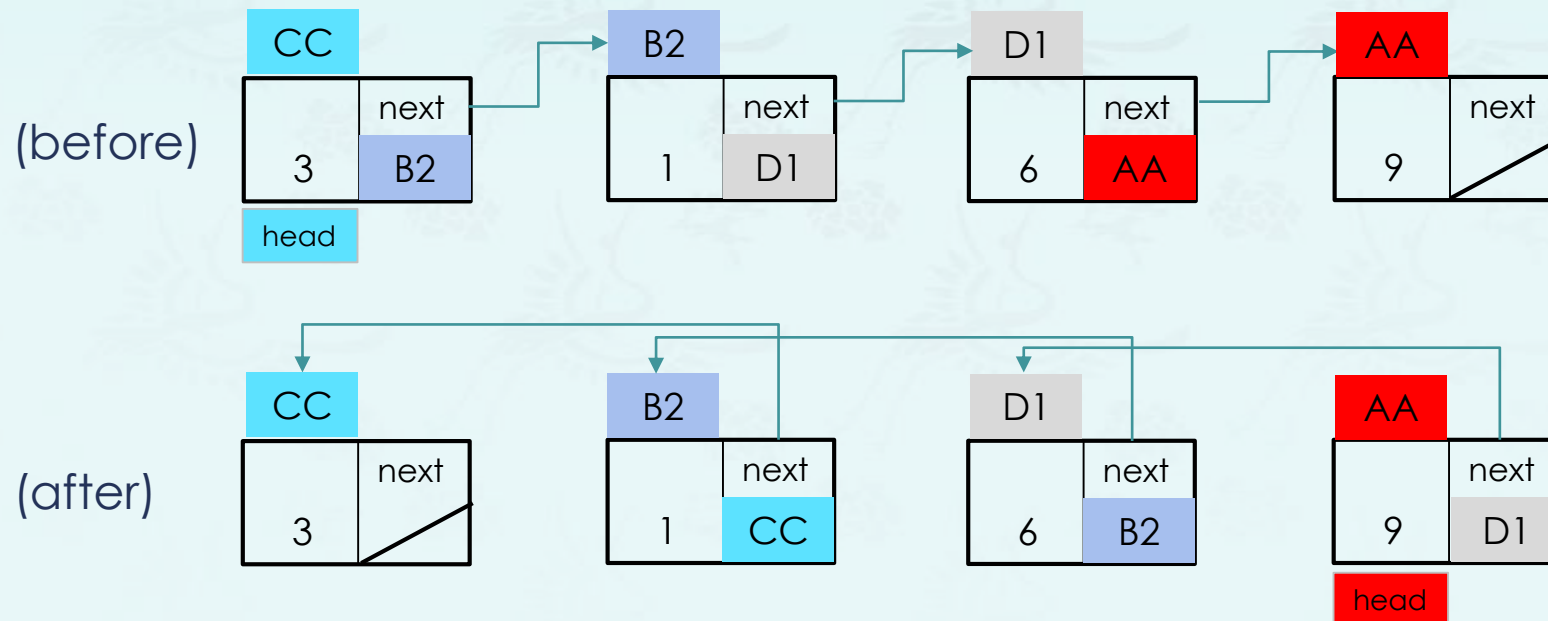
**Tips and Hints:** Before while() loop, set **prev = nullptr**, and **curr = head**. During while() loop,

(1) Before setting **curr→next** to a new pointer, store the **curr→next** as a temporary node **temp**.

(2) Before going for the next node in while loop, make sure two things:

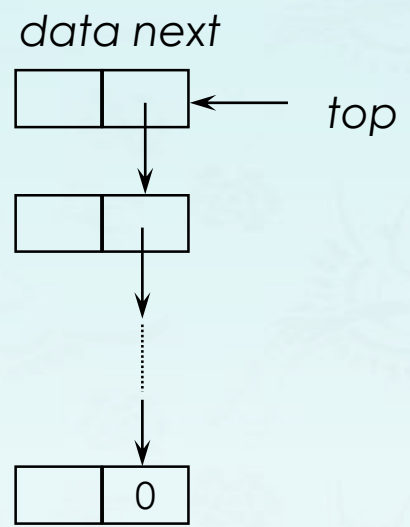
A. set **prev** to **curr** (e.g. **curr** becomes **prev**).

B. set **curr** to the next node you will process.

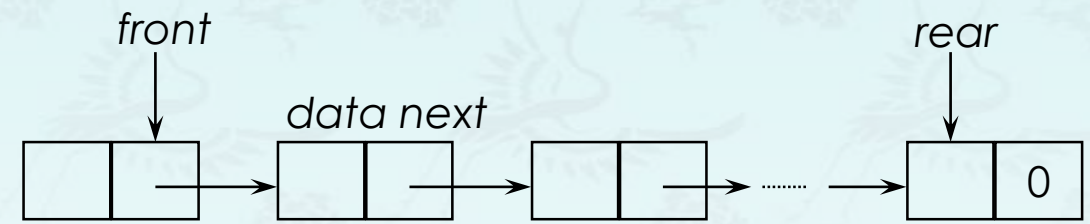


# Linked List

Using linked lists, **stacks** and **queues** facilitate easy insertion and deletion of nodes.



(a) linked stack



(b) linked queue

# Polynomials

Using linked lists, **stacks** and **queues** facilitate easy insertion and deletion of nodes.

- **Polynomials representation**

$$A(x) = a_{m-1}x^{e_{m-1}} + \dots + a_0x^{e_0}$$

$a_i$  = nonzero coefficients

$e_i$  = nonnegative integer exponents such as

$$e_{m-1} > e_{m-2} > \dots > a_0 \geq 0$$

- We may draw a **poly node** as

coef	expo	next
------	------	------

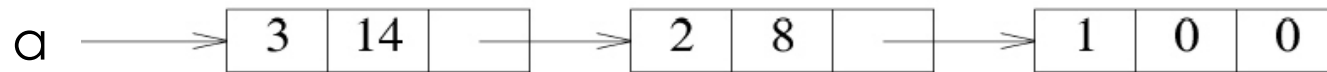
- **Type definition**

```
struct Poly {  
    double  coef;  
    double  expo;  
    Poly*   next;  
};  
using pPoly = Poly*;
```

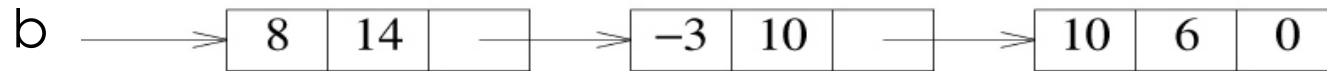
# Polynomials

Using linked lists, **stacks** and **queues** facilitate easy insertion and deletion of nodes.

- **Example:**



(a)  $3x^{14} + 2x^8 + 1$



(b)  $8x^{14} + 3x^{10} + 10x^6$

- **Q: How to add two polynomials?**

$$a = 3x^{14} + 2x^8 + 1$$

$$b = 8x^{14} - 3x^{10} + 10x^6$$

$$c = a + b$$

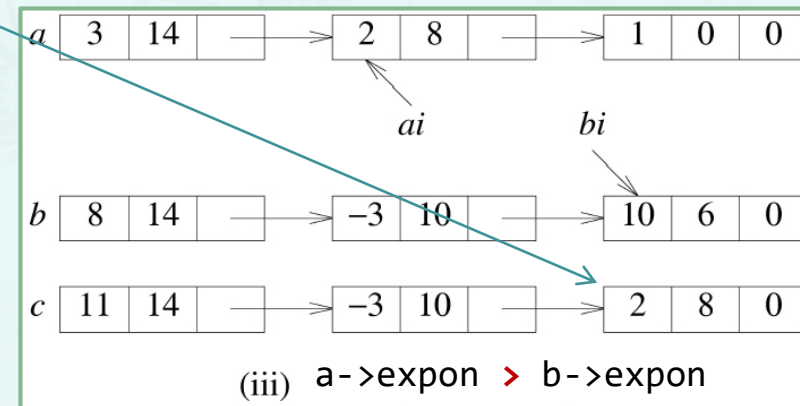
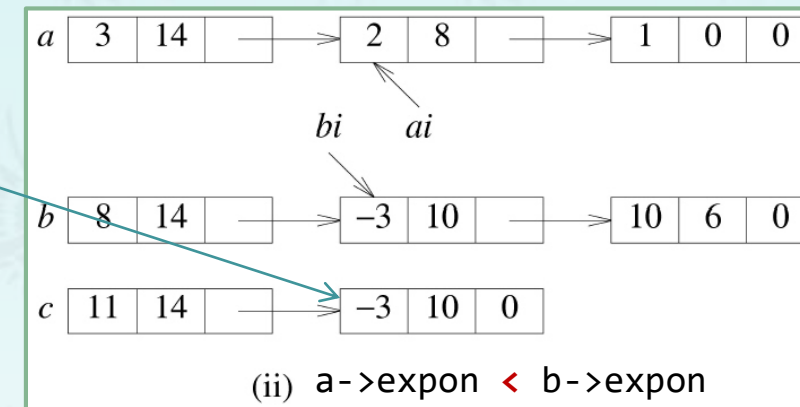
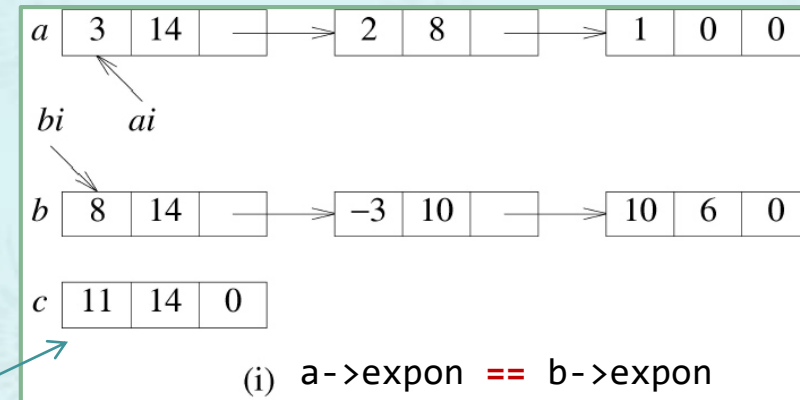
$$= 11x^{14} - 3x^{10} + 2x^8 + 10x^6 + 1$$

$$a = 3x^{14} + 2x^8 + 1$$

$$b = 8x^{14} - 3x^{10} + 10x^6$$

$$c = a + b$$

$$= 11x^{14} - 3x^{10} + 2x^8 + 10x^6 + 1$$





# Linked List

---

## Resizing Array vs. Linked List

- **Tradeoffs.** Can implement a stack with either resizing array or linked list; Client can use interchangeably. Which one is better?
- **Linked-list implementation**
  - Every operation takes constant time in the worst case.
  - Uses extra time and space to deal with the links.
- **Resizing-array implementation**
  - Every operation takes constant amortized time.
  - Less waste space

## Doubly Linked lists

---

### Q. Array vs. Singly linked list vs. Doubly linked list, **Why?**

- **Advantages of linked list:**

- Dynamic structure (Memory Allocated at run-time)
- Have more than one data type.
- Re-arrange of linked list is easy (Insertion-Deletion).
- **It doesn't waste memory.**

- **Disadvantages of linked list:**

- In linked list, if we want to access any node it is difficult.
- **It uses more memory.**

- **Advantages of doubly linked list:**

- A doubly linked list can be **traversed in both directions** (forward and backward).  
A singly linked list can only be traversed in one direction.
- Most operations are  $O(1)$  instead of  $O(n)$ .

# Data Structures

## Chapter 4

### 1. Singly Linked List

- Pointer Reviewed & Linked
- Linked List (1)
- **Linked List (2)**

### 2. Doubly Linked List

*Summary &*  
*quaestio quaestio* 90 < 9 9 ? ?  
→