

# **02244 Language-Based Security**

## **Security Protocols**

### **Automated Analysis II: Abstraction**

Sebastian Mödersheim

April 23, 2018

# The Sources of Infinity



- For security protocols, the **state space** can be infinite for (at least) the following reasons:

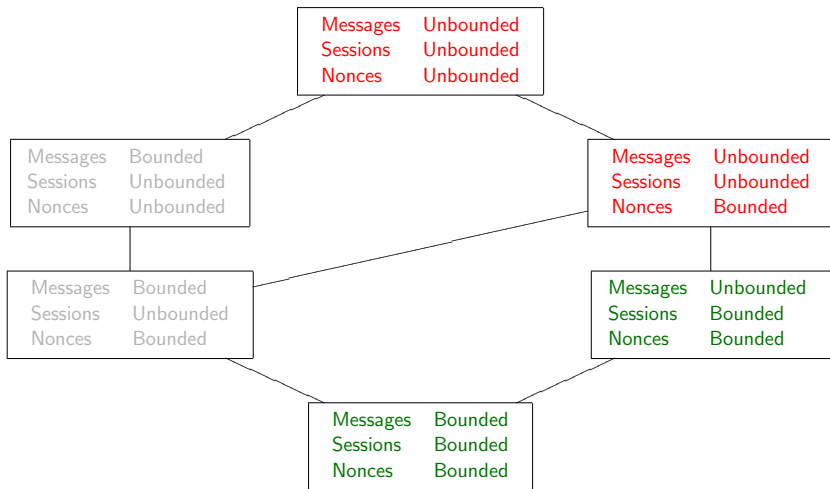
**Messages** The intruder can compose arbitrarily complex messages from his knowledge, e.g.  $i, h(i), h(h(i)), \dots$

**Sessions** No bound on the number of executions of the protocol.  
(In our model: infinitely many threads in the initial state).

**Nonces** In an unbounded number of sessions, honest agents create an infinite number of fresh nonces.

- Consider the models that arise from bounding any subset of these parameters:
  - ★ Decidability/Automation?
  - ★ Can we justify the bounds?

# Decidability Lattice



Today we look at the remaining two elements.

# Typed Model

Declare for all variables and constants a type, e.g.,

$A, B, C, a, b, c, i, \dots$	<i>Agent</i>
$NA, NB, na_{17}, \dots$	<i>Nonce</i>
$KAB, kab, \dots$	<i>SymmetricKey</i>

## Typed Model

We allow that variables are only instantiated with constants of the same type.

- This means bounding the depth of messages. Why?

# Typed Model

Declare for all variables and constants a type, e.g.,

$A, B, C, a, b, c, i, \dots$	<i>Agent</i>
$NA, NB, na_{17}, \dots$	<i>Nonce</i>
$KAB, kab, \dots$	<i>SymmetricKey</i>

## Typed Model

We allow that variables are only instantiated with constants of the same type.

- This means bounding the depth of messages. Why?
- Can this be justified?
  - ★ i.e., don't we exclude some attacks with this in general?

# No Fresh Nonces

## Idea

Consider a scenario where agents do not create fresh nonces in every protocol run, but use **the same nonce** in all protocol runs with **the same communication partners**.

## Example NSPK

Replace the fresh nonces with functions of the involved agent names. For NSPK, we choose  $NA$  becomes  $na(A, B)$  and  $NB$  becomes  $nb(B, A)$ .

$$\begin{array}{lcl} A & \rightarrow & B : \{na(A, B), A\}_{pk(B)} \\ B & \rightarrow & A : \{na(A, B), nb(B, A)\}_{pk(A)} \\ A & \rightarrow & B : \{nb(B, A)\}_{pk(B)} \end{array}$$

---

$NA$  secret of  $A, B$

$NB$  secret of  $A, B$

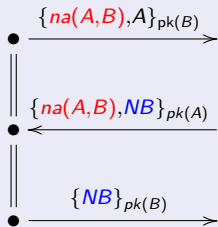
# No Fresh Nonces

## Idea

Consider a scenario where agents do not create fresh nonces in every protocol run, but use **the same nonce** in all protocol runs with **the same communication partners**.

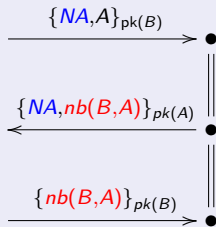
Example NSPK:

**Role A: replace  $NA$  with  $na(A, B)$ .**



Leave received nonce  $NB$  as is.

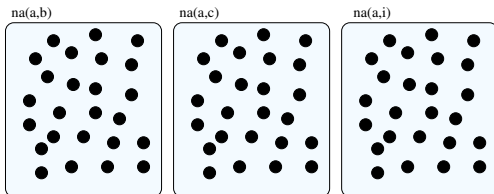
**Role B: replace  $NB$  with  $nb(B, A)$ .**



Leave received nonce  $NA$  as is.

# Abstract Interpretation

We have **partitioned** the set of all **concrete nonces** into **abstract equivalence classes**:



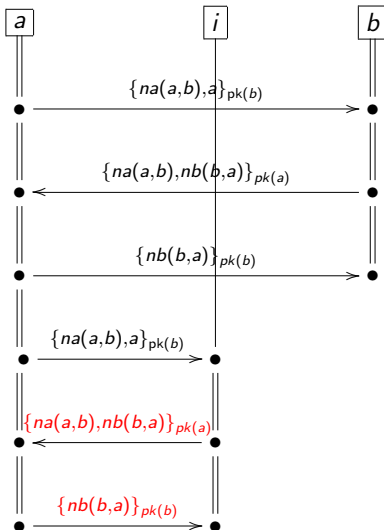
$a$ 's nonces for communication with  $b$ ,  $c$ , and  $i$

and replace in the protocol model each **concrete value** with its **abstract equivalence class**.



# Abstract Interpretation

- Every reachable concrete state has an abstract counter-part,
- but some abstract states have no concrete counter-part:

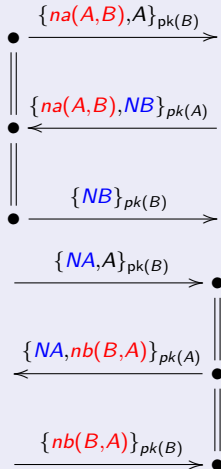


# Abstract Interpretation

- Every reachable concrete state has an abstract counter-part,
- but some abstract states have no concrete counter-part.
- So the abstract model is an **over-approximation** of the concrete model, allowing at least as many behaviors.
- The abstract model is easier to verify than the concrete one.
- Claim: if the abstract model has no attack trace, then the concrete model has none. (True?)
- An attack trace in the abstract model may be a **false positive**: no (corresponding) attack trace in the concrete model.

# Abstracting States

**Idea:** regard honest agents just as a set of **oracles** that the intruder can ask to get an answer from.



$$ik(\{na(A, B), A\}_{pk(B)})$$

$$ik(\{na(A, B), NB\}_{pk(A)}) \\ \Rightarrow ik(\{NB\}_{pk(B)})$$

$ik(m)$ : intruder knows message  $m$

$$ik(\{NA, A\}_{pk(B)}) \\ \Rightarrow ik(\{NA, nb(B, A)\}_{pk(A)})$$

(Intruder learns nothing)

# Abstracting States

There is no notion of states or development anymore. Rather we consider with  $ik(m)$  all messages that the intruder can **ever** know.

$ik(\{na(A, B), A\}_{pk(B)})$  for all agents  $A, B$

$ik(\{NA, A\}_{pk(B)}) \Rightarrow ik(\{NA, nb(B, A)\}_{pk(A)})$

$ik(\{na(A, B), NB\}_{pk(A)}) \Rightarrow ik(\{NB\}_{pk(B)})$

---

... plus standard intruder deduction rule (Dolev-Yao):

$ik(M) \wedge ik(K) \Rightarrow ik(\{M\}_K)$

$ik(\{M\}_K) \wedge ik(inv(K)) \Rightarrow ik(M)$

$ik(M_1) \wedge ik(M_2) \Rightarrow ik(\langle M_1, M_2 \rangle)$

$ik(\langle M_1, M_2 \rangle) \Rightarrow ik(M_1) \wedge ik(M_2)$

---

Initial intruder knowledge:  $ik(inv(pk(i)))$   $ik(A)$   $ik(pk(A))$  for every  $A$

---

Goal: For every honest  $A \neq i$  and  $B \neq i$ :

$ik(na(A, B)) \Rightarrow \text{attack}$

$ik(nb(B, A)) \Rightarrow \text{attack}$

# Abstracting States

There is no notion of states or development anymore. Rather we consider with  $ik(m)$  all messages that the intruder can **ever** know.

$ik(\{na(A, B), A\}_{pk(B)})$  for all agents  $A, B$

$ik(\{NA, A\}_{pk(B)}) \Rightarrow ik(\{NA, nb(B, A)\}_{pk(A)})$

$ik(\{na(A, B), NB\}_{pk(A)}) \Rightarrow ik(\{NB\}_{pk(B)})$

... plus standard intruder deduction rule (Dolev-Yao):

$ik(M) \wedge ik(K) \Rightarrow ik(\{M\}_K)$

$ik(\{M\}_K) \wedge ik(inv(K)) \Rightarrow ik(M)$

$ik(M_1) \wedge ik(M_2) \Rightarrow ik(\langle M_1, M_2 \rangle)$

$ik(\langle M_1, M_2 \rangle) \Rightarrow ik(M_1) \wedge ik(M_2)$

Initial intruder knowledge:  $ik(inv(pk(i)))$   $ik(A)$   $ik(pk(A))$  for every  $A$

Goal: For every honest  $A \neq i$  and  $B \neq i$ :

$ik(na(A, B)) \Rightarrow \text{attack}$

$ik(nb(B, A)) \Rightarrow \text{attack}$

Can you write this in Prolog?

# The Fixedpoint for NSPK

①  $\{na(A, B), A\}_{pk(B)}$  by step 1

# The Fixedpoint for NSPK

- ①  $\{na(A, B), A\}_{pk(B)}$  by step 1
- ②  $na(A, i)$  by intruder deduction on ① when  $B = i$

# The Fixedpoint for NSPK

- ①  $\{na(A, B), A\}_{pk(B)}$  by step 1
- ②  $na(A, i)$  by intruder deduction on ① when  $B = i$
- ③  $\{na(A, B), nb(B, A)\}_{pk(A)}$  by step 2 on ①



# The Fixedpoint for NSPK

- ①  $\{na(A, B), A\}_{pk(B)}$  by step 1
- ②  $na(A, i)$  by intruder deduction on ① when  $B = i$
- ③  $\{na(A, B), nb(B, A)\}_{pk(A)}$  by step 2 on ①
- ④  $\{N, nb(B, A)\}_{pk(A)}$  by step 2 with intr. ded.  
for any nonce  $N$  that the intruder can derive in this fixedpoint

# The Fixedpoint for NSPK

- ①  $\{na(A, B), A\}_{pk(B)}$  by step 1
- ②  $na(A, i)$  by intruder deduction on ① when  $B = i$
- ③  $\{na(A, B), nb(B, A)\}_{pk(A)}$  by step 2 on ①
- ④  $\{N, nb(B, A)\}_{pk(A)}$  by step 2 with intr. ded.  
for any nonce  $N$  that the intruder can derive in this fixedpoint  
(e.g.  $N = na(A, i)$  by ②)

# The Fixedpoint for NSPK

- ①  $\{na(A, B), A\}_{pk(B)}$  by step 1
- ②  $na(A, i)$  by intruder deduction on ① when  $B = i$
- ③  $\{na(A, B), nb(B, A)\}_{pk(A)}$  by step 2 on ①
- ④  $\{N, nb(B, A)\}_{pk(A)}$  by step 2 with intr. ded.  
for any nonce  $N$  that the intruder can derive in this fixedpoint  
(e.g.  $N = na(A, i)$  by ②)
- ⑤  $nb(B, i)$  by intruder deduction on ④

# The Fixedpoint for NSPK

- ①  $\{na(A, B), A\}_{pk(B)}$  by step 1
- ②  $na(A, i)$  by intruder deduction on ① when  $B = i$
- ③  $\{na(A, B), nb(B, A)\}_{pk(A)}$  by step 2 on ①
- ④  $\{N, nb(B, A)\}_{pk(A)}$  by step 2 with intr. ded.  
for any nonce  $N$  that the intruder can derive in this fixedpoint  
(e.g.  $N = na(A, i)$  by ②)
- ⑤  $nb(B, i)$  by intruder deduction on ④
- ⑥  $\{nb(B, A)\}_{pk(B)}$  by step 3 on ③

# The Fixedpoint for NSPK

- ①  $\{na(A, B), A\}_{pk(B)}$  by step 1
- ②  $na(A, i)$  by intruder deduction on ① when  $B = i$
- ③  $\{na(A, B), nb(B, A)\}_{pk(A)}$  by step 2 on ①
- ④  $\{N, nb(B, A)\}_{pk(A)}$  by step 2 with intr. ded.  
for any nonce  $N$  that the intruder can derive in this fixedpoint  
(e.g.  $N = na(A, i)$  by ②)
- ⑤  $nb(B, i)$  by intruder deduction on ④
- ⑥  $\{nb(B, A)\}_{pk(B)}$  by step 3 on ③
- ⑦  $nb(i, A)$  by intruder deduction on ⑥

# The Fixedpoint for NSPK

- ➊  $\{na(A, B), A\}_{pk(B)}$  by step 1
- ➋  $na(A, i)$  by intruder deduction on ➊ when  $B = i$
- ➌  $\{na(A, B), nb(B, A)\}_{pk(A)}$  by step 2 on ➊
- ➍  $\{N, nb(B, A)\}_{pk(A)}$  by step 2 with intr. ded.  
for any nonce  $N$  that the intruder can derive in this fixedpoint  
(e.g.  $N = na(A, i)$  by ➋)
- ➎  $nb(B, i)$  by intruder deduction on ➍
- ➏  $\{nb(B, A)\}_{pk(B)}$  by step 3 on ➌
- ➐  $nb(i, A)$  by intruder deduction on ➏
- ➑  $\{N\}_{pk(i)}$  by step 3 on ➍ and intruder ded.

# The Fixedpoint for NSPK

- ①  $\{na(A, B), A\}_{pk(B)}$  by step 1
- ②  $na(A, i)$  by intruder deduction on ① when  $B = i$
- ③  $\{na(A, B), nb(B, A)\}_{pk(A)}$  by step 2 on ①
- ④  $\{N, nb(B, A)\}_{pk(A)}$  by step 2 with intr. ded.  
for any nonce  $N$  that the intruder can derive in this fixedpoint  
(e.g.  $N = na(A, i)$  by ②)
- ⑤  $nb(B, i)$  by intruder deduction on ④
- ⑥  $\{nb(B, A)\}_{pk(B)}$  by step 3 on ③
- ⑦  $nb(i, A)$  by intruder deduction on ⑥
- ⑧  $\{N\}_{pk(i)}$  by step 3 on ② and intruder ded.
- ⑨  $\{nb(B, A)\}_{pk(i)}$  by step 3 on ④ with  $N = na(A, i)$

# The Fixedpoint for NSPK

- ①  $\{na(A, B), A\}_{pk(B)}$  by step 1
- ②  $na(A, i)$  by intruder deduction on ① when  $B = i$
- ③  $\{na(A, B), nb(B, A)\}_{pk(A)}$  by step 2 on ①
- ④  $\{N, nb(B, A)\}_{pk(A)}$  by step 2 with intr. ded.  
for any nonce  $N$  that the intruder can derive in this fixedpoint  
(e.g.  $N = na(A, i)$  by ②)
- ⑤  $nb(B, i)$  by intruder deduction on ④
- ⑥  $\{nb(B, A)\}_{pk(B)}$  by step 3 on ③
- ⑦  $nb(i, A)$  by intruder deduction on ⑥
- ⑧  $\{N\}_{pk(i)}$  by step 3 on ② and intruder ded.
- ⑨  $\{nb(B, A)\}_{pk(i)}$  by step 3 on ④ with  $N = na(A, i)$
- ⑩  $nb(B, A)$  intruder deduction on ⑨ — attack



## Note on Variables

We have left variables  $A$ ,  $B$ , and  $N$  in the above fixedpoint:

- $A$  and  $B$  represent arbitrary agent names
- $N$  represents any nonce the intruder knows

## Note on Variables

We have left variables  $A$ ,  $B$ , and  $N$  in the above fixedpoint:

- $A$  and  $B$  represent arbitrary agent names
- $N$  represents any nonce the intruder knows
- In general, this represents an infinite fixedpoint, when replacing arbitrary agent names for  $A$  and  $B$  like  $a_1, a_2, a_3, \dots$

## Note on Variables

We have left variables  $A$ ,  $B$ , and  $N$  in the above fixedpoint:

- $A$  and  $B$  represent arbitrary agent names
- $N$  represents any nonce the intruder knows
- In general, this represents an infinite fixedpoint, when replacing arbitrary agent names for  $A$  and  $B$  like  $a_1, a_2, a_3, \dots$
- There are some results that show: for many problems it is sufficient to work with only a fixed number of agents  $\{a, b, i\}$ . But makes the *descriptions* of the fixedpoint longer...

# Note on Variables

- We can easily calculate with facts that have variables, but mind incorrect **variable capturing**:
  - ★ Fact  $\{na(A, i), nb(B, A)\}_{pk(A)}$  of the previous fixedpoint
  - ★ and the rule  $\{na(A, B), NB\}_{pk(A)} \Rightarrow \{NB\}_{pk(B)}$ .

# Note on Variables

- We can easily calculate with facts that have variables, but mind incorrect **variable capturing**:
  - ★ Fact  $\{na(A, i), nb(B, A)\}_{pk(A)}$  of the previous fixedpoint
  - ★ and the rule  $\{na(A, B), NB\}_{pk(A)} \Rightarrow \{NB\}_{pk(B)}$ .
  - ★ Seems to allow only  $B = i$  and  $NB = nb(i, A)$ ?

# Note on Variables

- We can easily calculate with facts that have variables, but mind incorrect **variable capturing**:
  - ★ Fact  $\{na(A, i), nb(B, A)\}_{pk(A)}$  of the previous fixedpoint
  - ★ and the rule  $\{na(A, B), NB\}_{pk(A)} \Rightarrow \{NB\}_{pk(B)}$ .
  - ★ Seems to allow only  $B = i$  and  $NB = nb(i, A)$ ?
  - ★ But  $A$  and  $B$  can be anybody, so we could rename this fact to:

$$\{na(A', i), nb(B', A')\}_{pk(A')}$$

# Note on Variables

- We can easily calculate with facts that have variables, but mind incorrect **variable capturing**:
  - ★ Fact  $\{na(A, i), nb(B, A)\}_{pk(A)}$  of the previous fixedpoint
  - ★ and the rule  $\{na(A, B), NB\}_{pk(A)} \Rightarrow \{NB\}_{pk(B)}$ .
  - ★ Seems to allow only  $B = i$  and  $NB = nb(i, A)$ ?
  - ★ But  $A$  and  $B$  can be anybody, so we could rename this fact to:

$$\{na(A', i), nb(B', A')\}_{pk(A')}$$

- ★ Now solution:  $A = A', B = i, NB = nb(B', A)$  more general!

# Note on Variables

- We can easily calculate with facts that have variables, but mind incorrect **variable capturing**:
  - ★ Fact  $\{na(A, i), nb(B, A)\}_{pk(A)}$  of the previous fixedpoint
  - ★ and the rule  $\{na(A, B), NB\}_{pk(A)} \Rightarrow \{NB\}_{pk(B)}$ .
  - ★ Seems to allow only  $B = i$  and  $NB = nb(i, A)$ ?
  - ★ But  $A$  and  $B$  can be anybody, so we could rename this fact to:

$$\{na(A', i), nb(B', A')\}_{pk(A')}$$

- ★ Now solution:  $A = A', B = i, NB = nb(B', A)$  more general!
- ★ Thus the intruder obtains the secret nonce between any two agents  $B'$  and  $A$ . (attack)



# Lowe's fix for NSPK (NSL)

Insert the **name of  $B$**  in the second message:

## Example (NSL)

$$\begin{aligned} A &\rightarrow B : \{NA, A\}_{pk(B)} \\ B &\rightarrow A : \{NA, NB, \textcolor{red}{B}\}_{pk(A)} \\ A &\rightarrow B : \{NB\}_{pk(B)} \end{aligned}$$

# The Fixedpoint for NSL

①  $\{na(A, B), A\}_{pk(B)}$  by step 1

# The Fixedpoint for NSL

- ①  $\{na(A, B), A\}_{pk(B)}$  by step 1
- ②  $na(A, i)$  by intruder deduction on ①

# The Fixedpoint for NSL

- ①  $\{na(A, B), A\}_{pk(B)}$  by step 1
- ②  $na(A, i)$  by intruder deduction on ①
- ③  $\{na(A, B), nb(B, A), B\}_{pk(A)}$  by step 2 on ①

# The Fixedpoint for NSL

- ①  $\{na(A, B), A\}_{pk(B)}$  by step 1
- ②  $na(A, i)$  by intruder deduction on ①
- ③  $\{na(A, B), nb(B, A), B\}_{pk(A)}$  by step 2 on ①
- ④  $\{N, nb(B, A), B\}_{pk(A)}$  by step 2 with intr. ded.  
for any nonce  $N$  that the intruder can derive in this fixedpoint  
(e.g.  $N = na(A, i)$  by ②)

# The Fixedpoint for NSL

- ①  $\{na(A, B), A\}_{pk(B)}$  by step 1
- ②  $na(A, i)$  by intruder deduction on ①
- ③  $\{na(A, B), nb(B, A), B\}_{pk(A)}$  by step 2 on ①
- ④  $\{N, nb(B, A), B\}_{pk(A)}$  by step 2 with intr. ded.  
for any nonce  $N$  that the intruder can derive in this fixedpoint  
(e.g.  $N = na(A, i)$  by ②)
- ⑤  $nb(B, i)$  by intruder deduction on ③

# The Fixedpoint for NSL

- ①  $\{na(A, B), A\}_{pk(B)}$  by step 1
- ②  $na(A, i)$  by intruder deduction on ①
- ③  $\{na(A, B), nb(B, A), B\}_{pk(A)}$  by step 2 on ①
- ④  $\{N, nb(B, A), B\}_{pk(A)}$  by step 2 with intr. ded.  
for any nonce  $N$  that the intruder can derive in this fixedpoint  
(e.g.  $N = na(A, i)$  by ②)
- ⑤  $nb(B, i)$  by intruder deduction on ③
- ⑥  $\{nb(B, A)\}_{pk(B)}$  by step 3 on ③

# The Fixedpoint for NSL

- ①  $\{na(A, B), A\}_{pk(B)}$  by step 1
- ②  $na(A, i)$  by intruder deduction on ①
- ③  $\{na(A, B), nb(B, A), B\}_{pk(A)}$  by step 2 on ①
- ④  $\{N, nb(B, A), B\}_{pk(A)}$  by step 2 with intr. ded.  
for any nonce  $N$  that the intruder can derive in this fixedpoint  
(e.g.  $N = na(A, i)$  by ②)
- ⑤  $nb(B, i)$  by intruder deduction on ③
- ⑥  $\{nb(B, A)\}_{pk(B)}$  by step 3 on ③
- ⑦  $nb(i, A)$  by intruder deduction on ⑥



# The Fixedpoint for NSL

- ①  $\{na(A, B), A\}_{pk(B)}$  by step 1
- ②  $na(A, i)$  by intruder deduction on ①
- ③  $\{na(A, B), nb(B, A), B\}_{pk(A)}$  by step 2 on ①
- ④  $\{N, nb(B, A), B\}_{pk(A)}$  by step 2 with intr. ded.  
for any nonce  $N$  that the intruder can derive in this fixedpoint  
(e.g.  $N = na(A, i)$  by ②)
- ⑤  $nb(B, i)$  by intruder deduction on ③
- ⑥  $\{nb(B, A)\}_{pk(B)}$  by step 3 on ③
- ⑦  $nb(i, A)$  by intruder deduction on ⑥
- ⑧  $\{N\}_{pk(i)}$  by step 3 on ② and intruder ded.

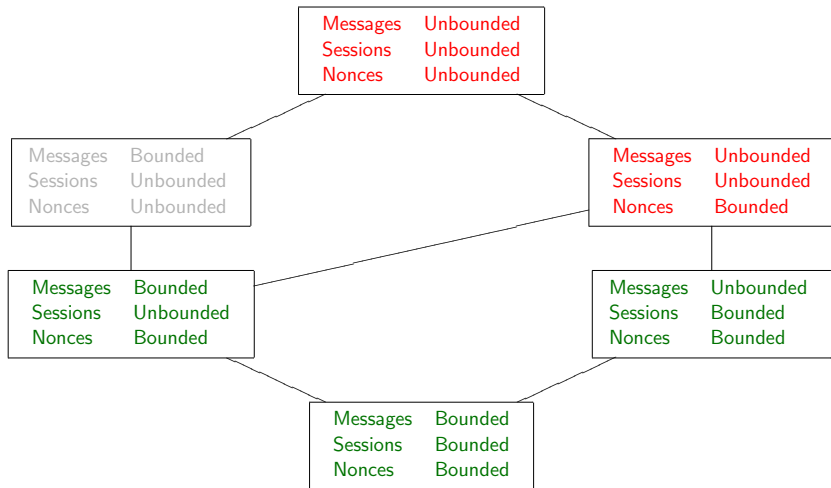
# The Fixedpoint for NSL

- ①  $\{na(A, B), A\}_{pk(B)}$  by step 1
- ②  $na(A, i)$  by intruder deduction on ①
- ③  $\{na(A, B), nb(B, A), B\}_{pk(A)}$  by step 2 on ①
- ④  $\{N, nb(B, A), B\}_{pk(A)}$  by step 2 with intr. ded.  
for any nonce  $N$  that the intruder can derive in this fixedpoint  
(e.g.  $N = na(A, i)$  by ②)
- ⑤  $nb(B, i)$  by intruder deduction on ③
- ⑥  $\{nb(B, A)\}_{pk(B)}$  by step 3 on ③
- ⑦  $nb(i, A)$  by intruder deduction on ⑥
- ⑧  $\{N\}_{pk(i)}$  by step 3 on ② and intruder ded.  
Not derivable anymore:  $\{nb(B, A)\}_{pk(i)}$

# Abstraction Based Analysis

- We have now a verification procedure for **unbounded sessions** when **bounding fresh nonces and messages...**
- This also avoids the entire **state explosion** problem of standard model-checking: the number of reachable states is (at least) exponential in the number of concurrent processes.

# Decidability Lattice



- ProVerif [Blanchet 2001ff] is a protocol verifier based on the abstract-interpretation method where messages are unbounded by default.
- Horn clauses like  $P_1 \wedge \dots \wedge P_n \Rightarrow Q$  can be equivalently written as  $\neg P_1 \vee \dots \vee \neg P_n \vee Q$ .

## Resolution

Find two clauses  $p \vee \phi$  and  $\neg p \vee \psi$ . Then we can derive the clause  $\phi \vee \psi$

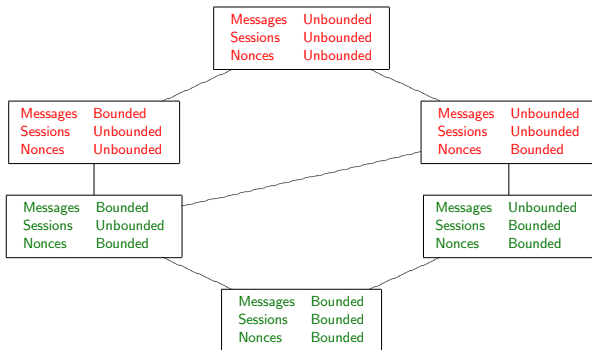
- Add the clause  $\neg \text{attack}$ : if the protocol has an attack, then this leads to a contradiction, deriving the empty clause “False”.
- Resolution is refutation-complete: a set of clauses is consistent iff False is not derivable with resolution.
- With bounded messages, resolution is guaranteed to terminate.
- In an untyped model without bounding messages, this approach **can** lead to non-termination, but often it does terminate!

- To complete our picture:

## Theorem ([Durgin et al. 2004])

*For an unbounded number of sessions and an unbounded number of nonces, protocol security is undecidable, even when bounding messages.*

# Decidability Lattice



## Conclusion:

For decidability, we may have either unbounded messages or unbounded sessions (with bounded nonces), but not both.

# Bibliography

- ProVerif:  
<http://prosecco.gforge.inria.fr/personal/bblanche/proverif/>
- Sebastian Mödersheim and Georgios Katsoris. *A Sound Abstraction of the Parsing Problem*. CSF 2014.
- Hubert Comon and Véronique Cortier. *Security Properties: Two Agents Are Sufficient*. In ESOP 2003.