

DESIGN ANALYSIS AND ALGORITHM

PRACTICAL NO 10

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Experiment No - 10**Date of Experiment:- 06th December 2021**

Program: Implement Chinese remainder theorem to a constraint satisfaction problem. Analyze its complexity.

Algorithm for Chinese Remainder Theorem

- **Step 1:-** Find $M = m_1 * m_2 * \dots * m_k$. This is the common modulus.

Step 2:- Find $M_1 = M/m_1, M_2 = M/m_2, \dots, M_k = M/m_k$.

- **Step 3:-** Find the multiplicative inverse of M_1, M_2, \dots, M_k using the corresponding moduli (m_1, m_2, \dots, m_k). Call the inverses as:-
 $M_1^{-1}, M_2^{-1}, \dots, M_k^{-1}$.

- **Step 4:** The solution to the simultaneous equations is:-

$$x = (a_1 * M_1^{-1} + a_2 * M_2^{-1} + \dots + a_k * M_k^{-1}) \bmod M$$

Input: $\text{num}[] = \{5, 7\}, \text{rem}[] = \{1, 3\}$

Output: 31

Explanation:

31 is the smallest number such that:

- (1) When we divide it by 5, we get remainder 1.
- (2) When we divide it by 7, we get remainder 3.

Input: $\text{num}[] = \{3, 4, 5\}, \text{rem}[] = \{2, 3, 1\}$

Output: 11

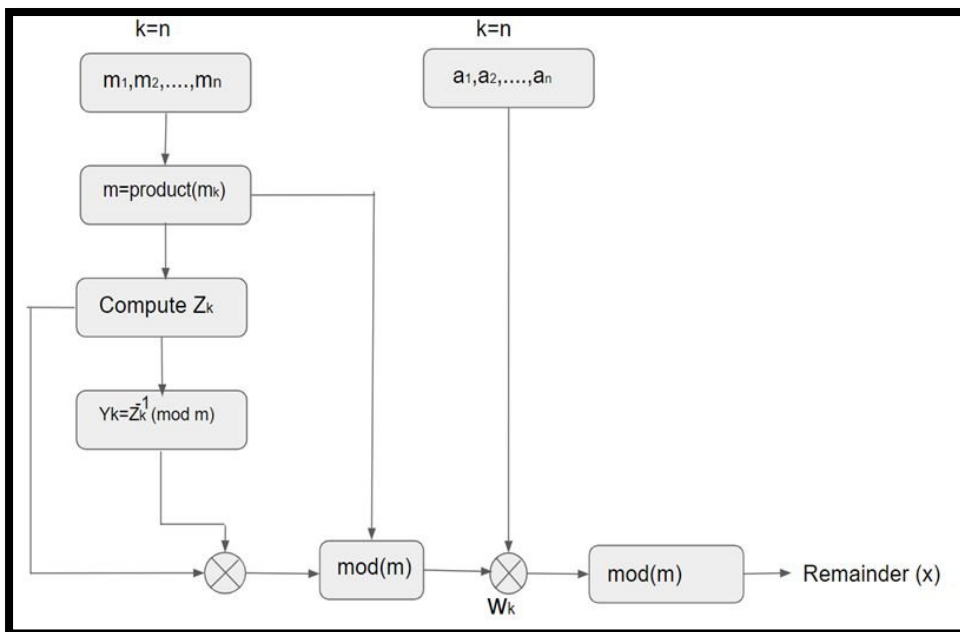
Explanation:

11 is the smallest number such that:

- (1) When we divide it by 3, we get remainder 2.
- (2) When we divide it by 4, we get remainder 3.

(3) When we divide it by 5, we get remainder 1.

Figure:



Practical Implementation of Chinese Remainder Theorem

```

# Chinese Remainder Theorem
def findMinX(num, rem, k):
    x = 1;
    while(True):
        j = 0;
        while(j < k):
            if (x % num[j] != rem[j]):
                break;
            j += 1;
        if (j == k):
            return x;
        x += 1;
    num = [3, 4, 5];
    rem = [2, 3, 1];
    k = len(num);
    print("x is", findMinX(num, rem, k));
  
```

Output:

```
x is 11
```

Time Complexity: $O(M)$, M is the product of all elements of `num[]` array.

Auxiliary Space: $O(1)$

Conclusion: Successfully Implemented the Chinese Remainder Theorem.