

# DATA SCIENCE

## MODEL EVALUATION PROCEDURES

*Q: What's wrong with training error?*

*Thought experiment:*

*Suppose we train our model using the entire dataset.*

*Q: How low can we push the training error?*

- We can make the model arbitrarily complex (effectively “memorizing” the entire training set).*

*A: Down to zero!*

*Q: What's wrong with training error?*

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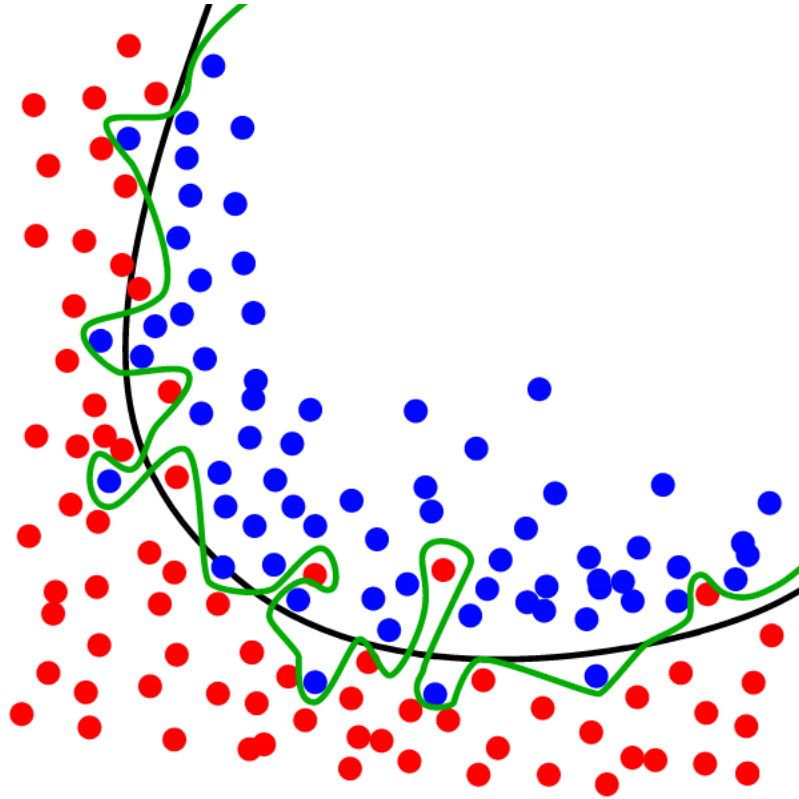
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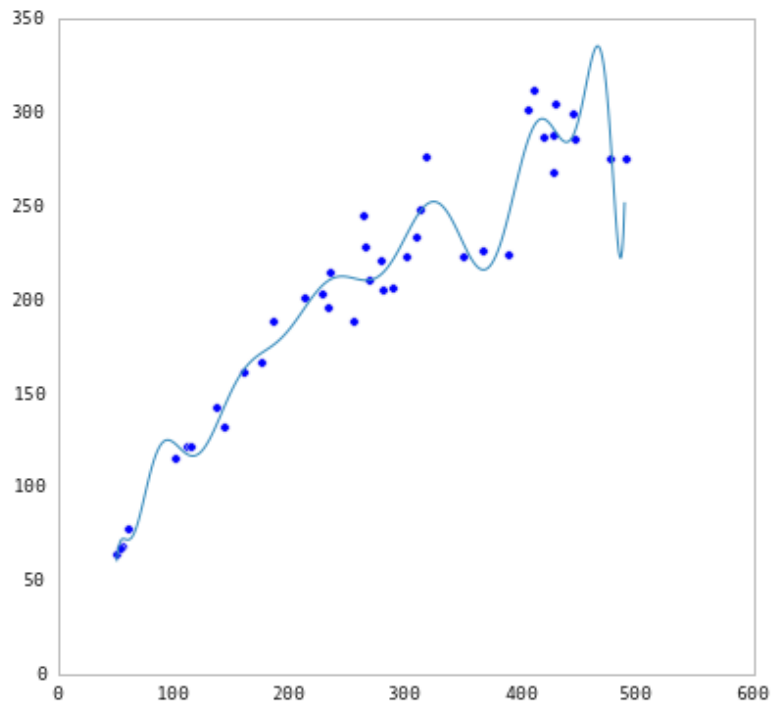
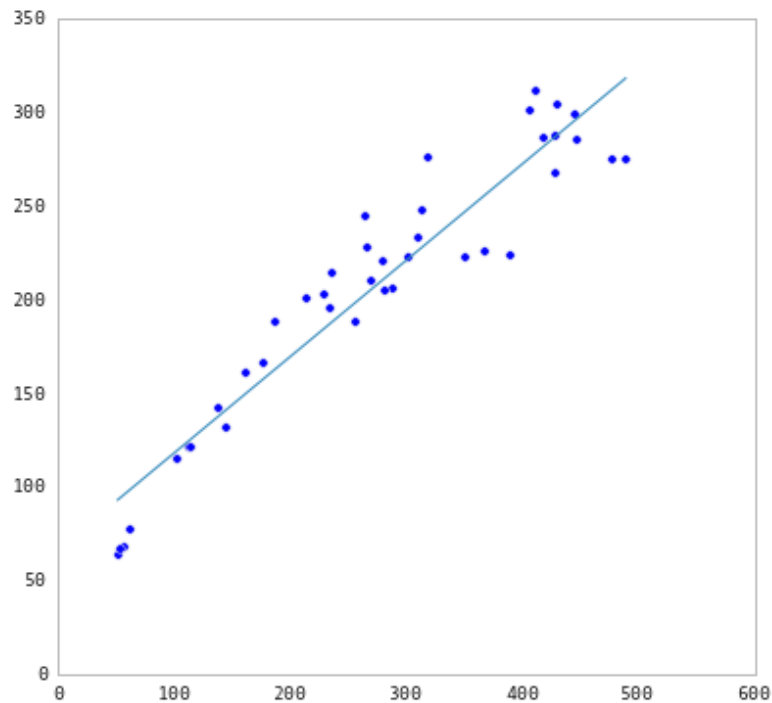
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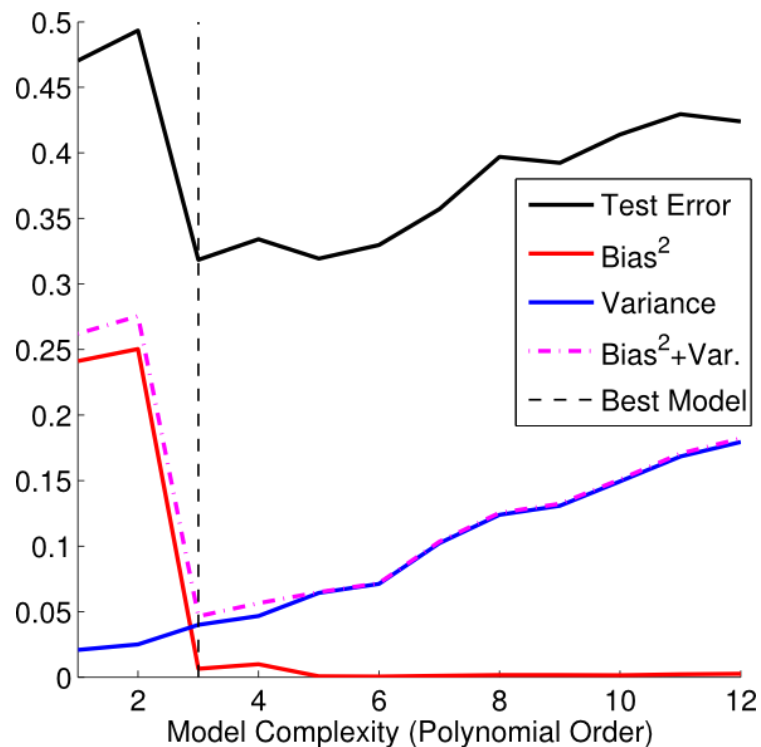
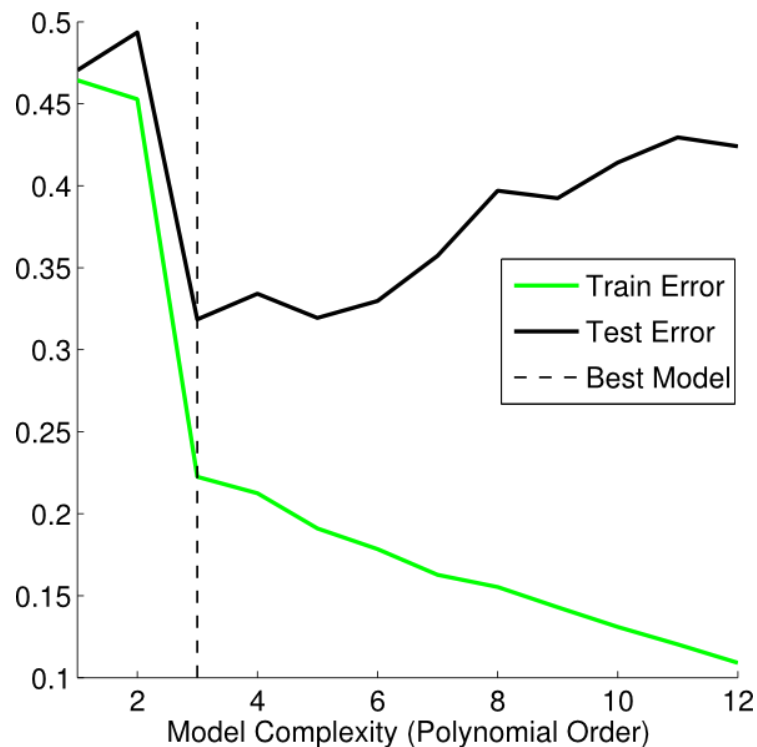
*A: Down to zero!*

### NOTE

This phenomenon is called *overfitting*.







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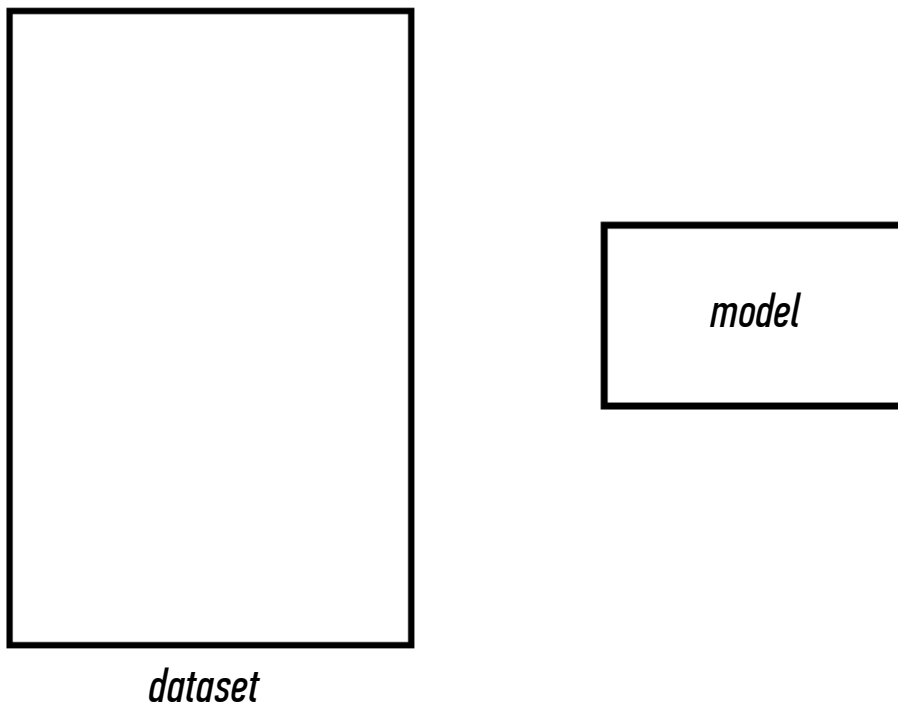
*A: Down to zero!*

**NOTE**

This phenomenon is called *overfitting*.

*A: Training error is not a good estimate of accuracy beyond training data.*

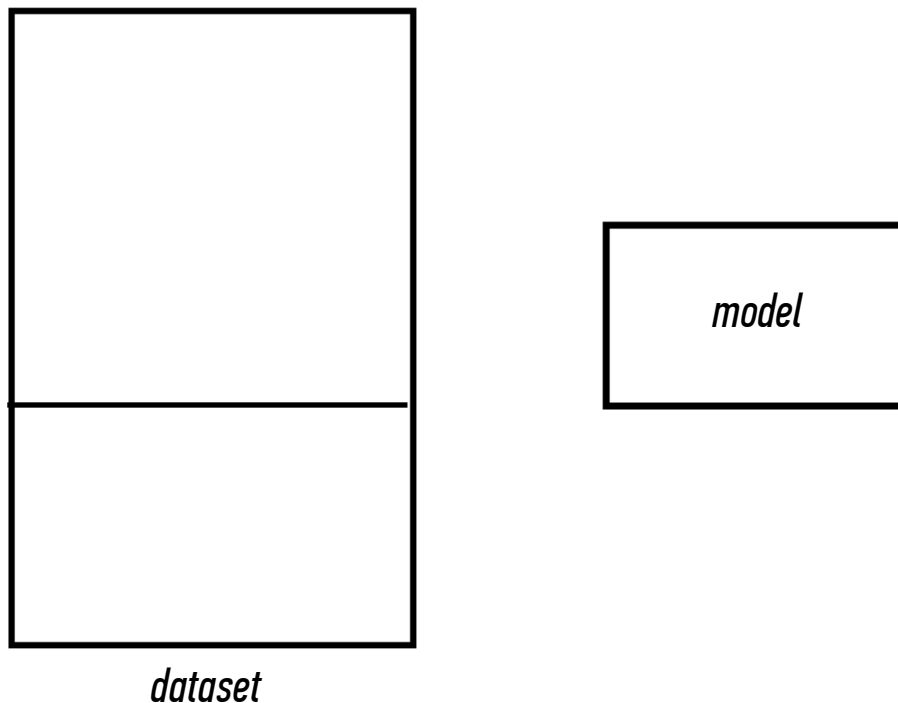
*Q: How can we make a model that generalizes well?*





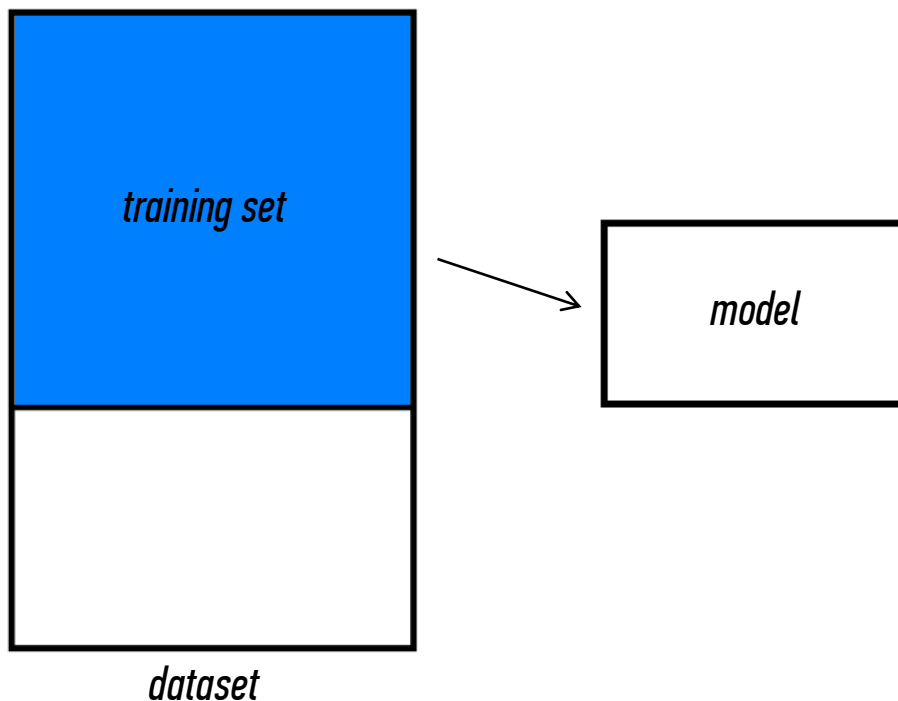
*Q: How can we make a model that generalizes well?*

*1) split dataset*



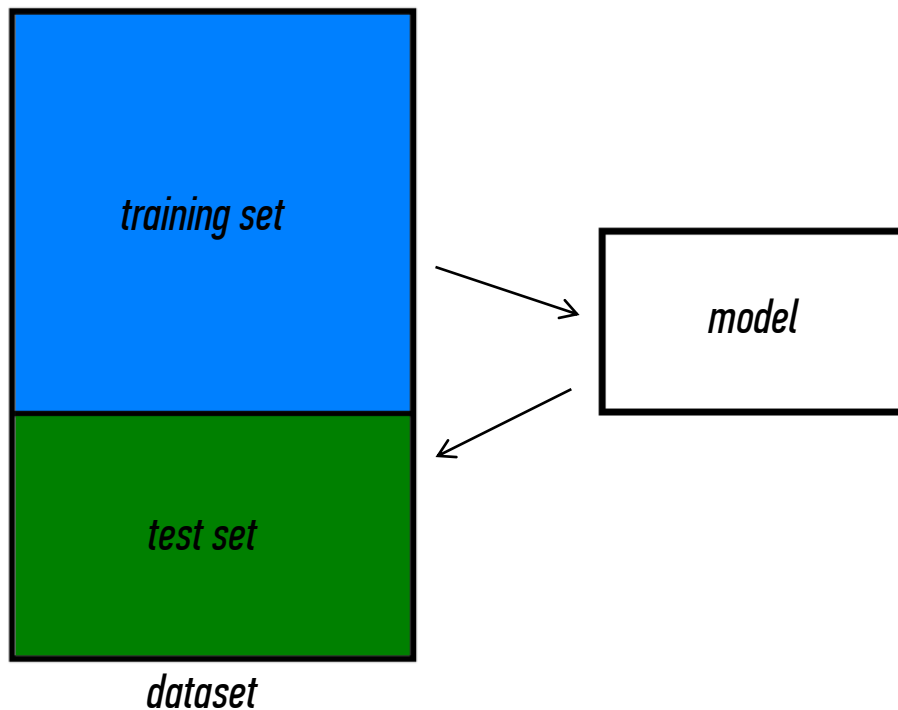
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- 1) split dataset*
- 2) train model*



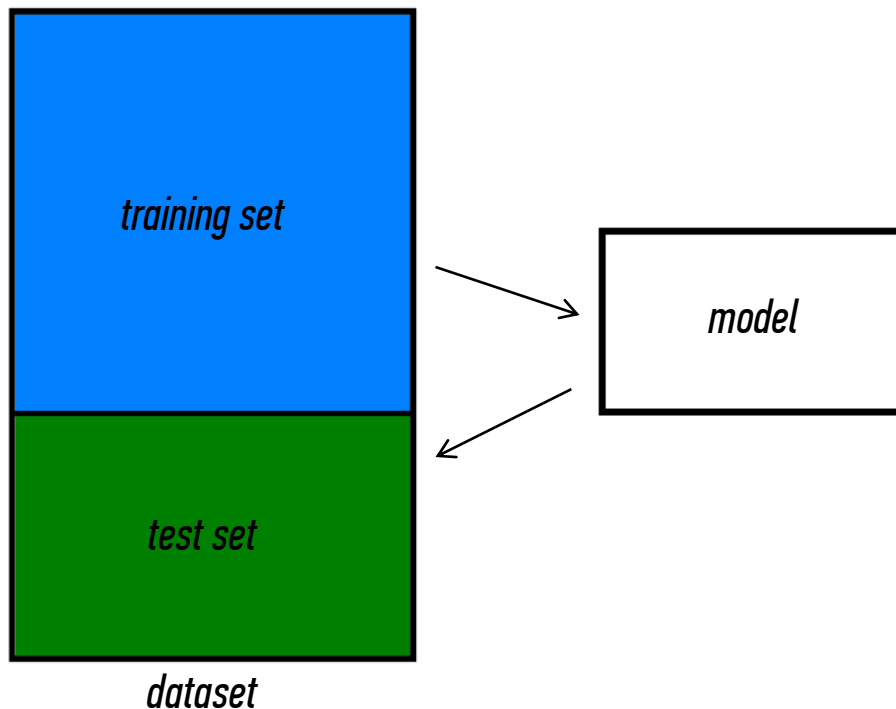
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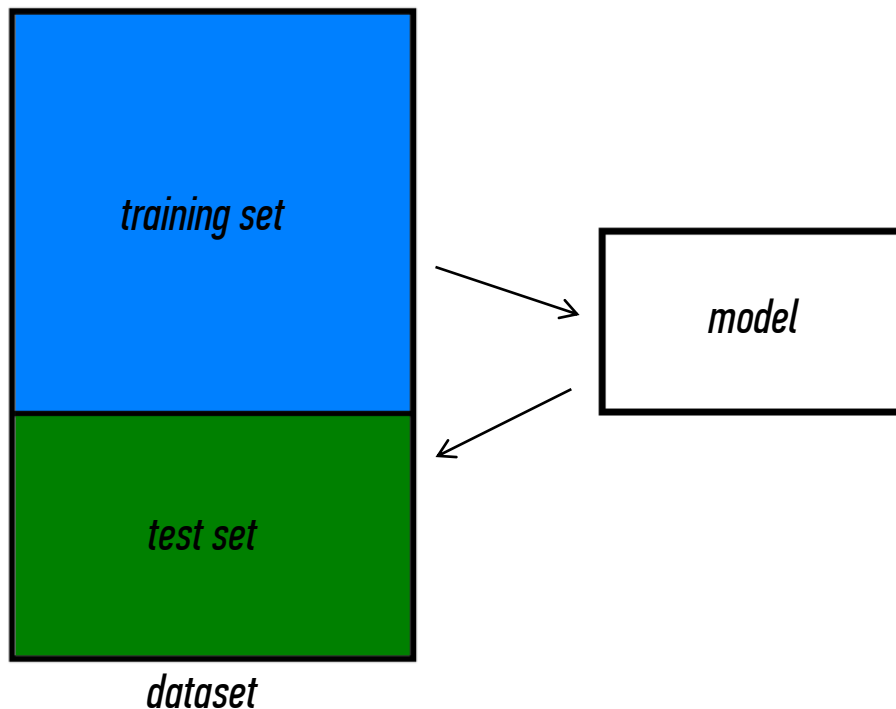
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- 1) split dataset*
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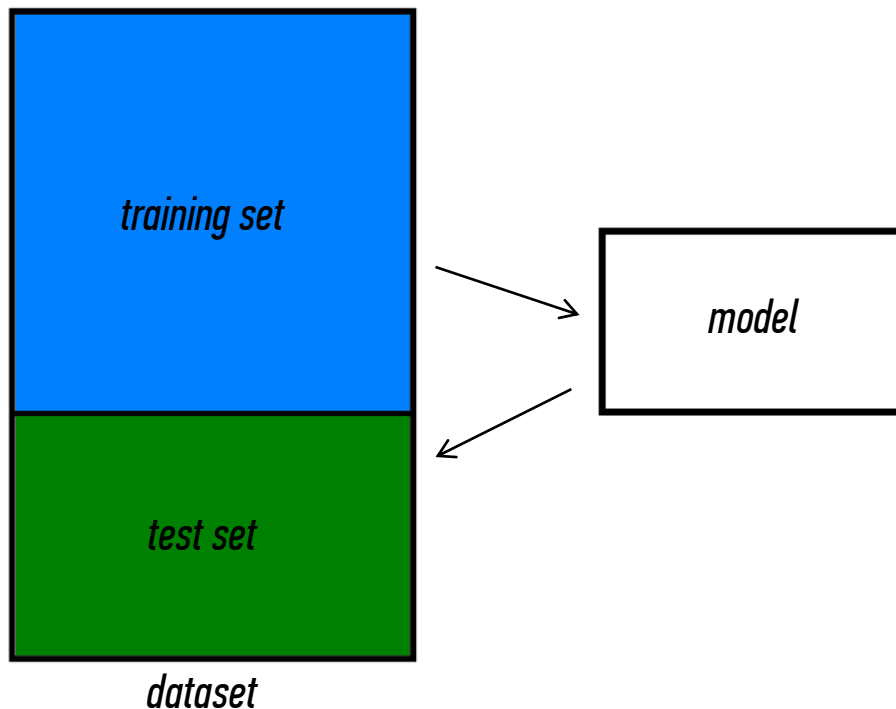
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- 5) choose best model*



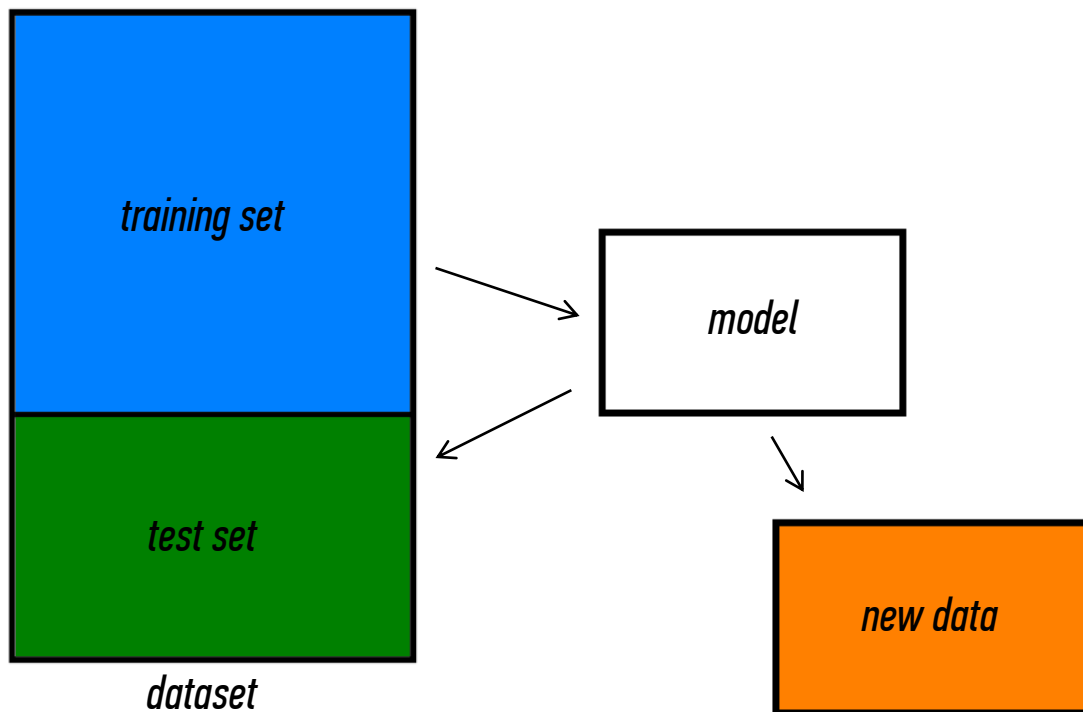
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- 6) train on **all** data*



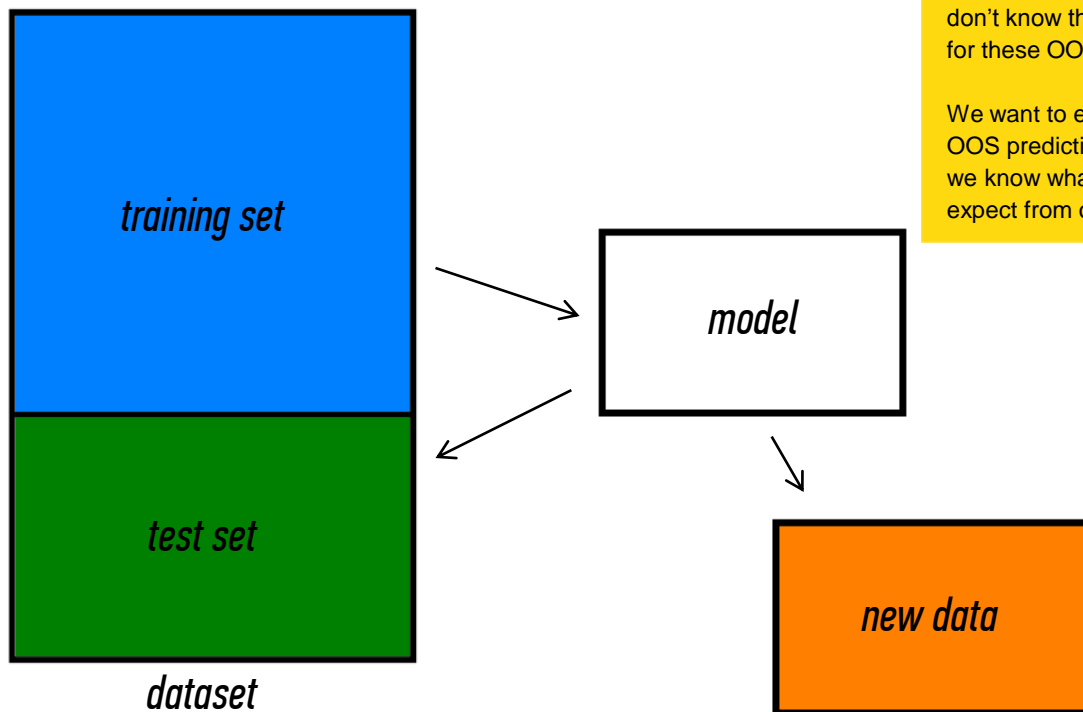
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- 7) make predictions  
on new data*



*Q: How can we make a model that generalizes well?*

- 1) *split dataset*
- 2) *train model*
- 3) *test model*
- 4) *parameter tuning*
- 5) *choose best model*
- 6) *train on **all** data*
- 7) *make predictions on new data*



## NOTE

This new data is called *out of sample* data. We don't know the labels for these OOS records!

We want to estimate OOS prediction error so we know what to expect from our model.



*Suppose we do the train/test split.*

*Q: How well does test set error predict OOS accuracy?*

*Thought experiment:*

*Suppose we had done a different train/test split.*

*Q: Would the test set error remain the same?*

*A: Of course not!*

*A: On its own, not very well.*

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*A: On its own, not very well.*

**NOTE**

The test set error gives a *high-variance estimate* of OOS accuracy.

*Something is still missing!*

*Q: How can we do better?*

*Thought experiment:*

*Different train/test splits will give us different test set errors.*

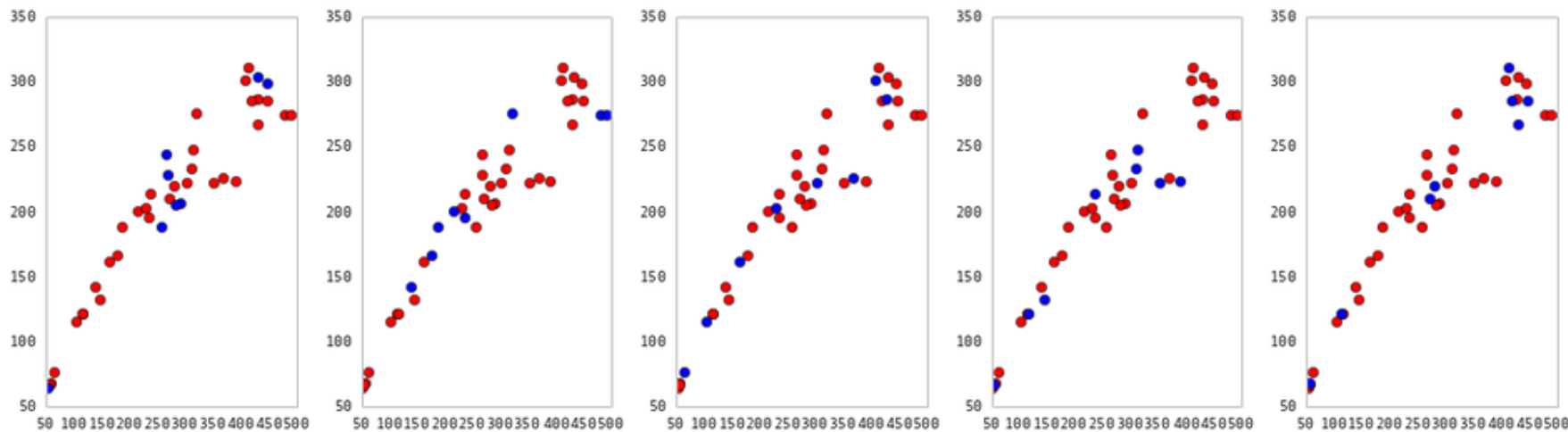
*Q: What if we did a bunch of these and took the average?*

*A: Now you're talking!*

*A: Cross-validation.*

### *Steps for K-fold cross-validation:*

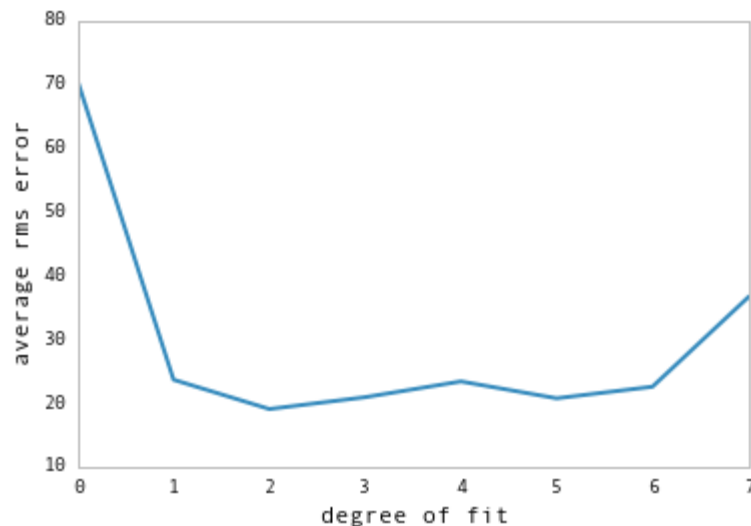
- 1) Randomly split the dataset into  $K$  equal partitions.*
- 2) Use partition 1 as test set & union of other partitions as training set.*
- 3) Calculate test set error.*
- 4) Repeat steps 2-3 using a different partition as the test set at each iteration.*
- 5) Take the average test set error as the estimate of OOS accuracy.*



*5-fold cross-validation: red = training folds, blue = test fold*

### *Features of K-fold cross-validation:*

- 1) *More accurate estimate of OOS prediction error.*
- 2) *More efficient use of data than single train/test split.*
  - *Each record in our dataset is used for both training and testing.*
- 3) *Presents tradeoff between efficiency and computational expense.*
  - *10-fold CV is 10x more expensive than a single train/test split*
- 4) *Can be used for parameter tuning and model selection.*



*Model selection using cross-validation:  
lowest predicted OOS error at degree = 2*

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