

Data Structures (in C++)

- List and Iterator ADTs -



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List and Iterator ADTs

Vector

- **List or Sequence**

- A collection S of n elements stored in a certain linear order
- Each element e in S can be uniquely referred using an integer in the range $[0, n-1]$
- **index**
 - the number of elements that are before e in S
 - A simple yet powerful notion, since it can be used to specify where to insert a new element into a list or where to remove an old element


index

- **Vector**

- A sequence that supports access to its elements by their indices

Vector ADT

- The vectors(also called an array list) ADT supports the following fundamental functions
 - the index parameter i is assumed to be in the range $0 \leq i \leq \text{size}() - 1$

$\text{at}(i)$: Return the element of V with index i ; an error condition occurs if i is out of range.

$\text{set}(i, e)$: Replace the element at index i with e ; an error condition occurs if i is out of range.

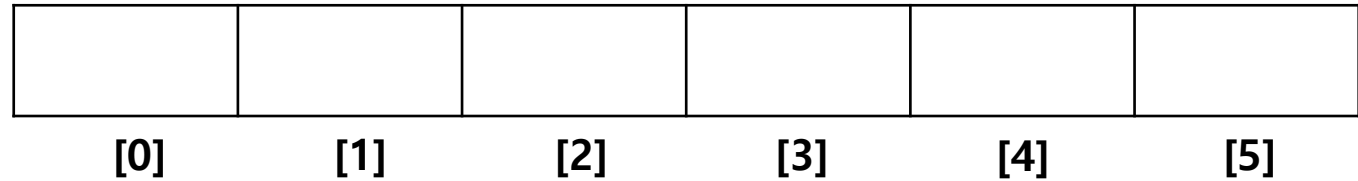
$\text{insert}(i, e)$: Insert a new element e into V to have index i ; an error condition occurs if i is out of range.

$\text{erase}(i)$: Remove from V the element at index i ; an error condition occurs if i is out of range.

- The **index** definition offers us a way to refer to the “place” where an element is stored in a sequence
- However, the index of an element may change when the sequence is updated

Vector Example

<i>Operation</i>	<i>Output</i>	<i>V</i>
insert(0,7)	—	(7)
insert(0,4)	—	(4,7)
at(1)	7	(4,7)
insert(2,2)	—	(4,7,2)
at(3)	“error”	(4,7,2)
erase(1)	—	(4,2)
insert(1,5)	—	(4,5,2)
insert(1,3)	—	(4,3,5,2)
insert(4,9)	—	(4,3,5,2,9)
at(2)	5	(4,3,5,2,9)
set(3,8)	—	(4,3,5,8,9)



Simple Array-Based Implementation

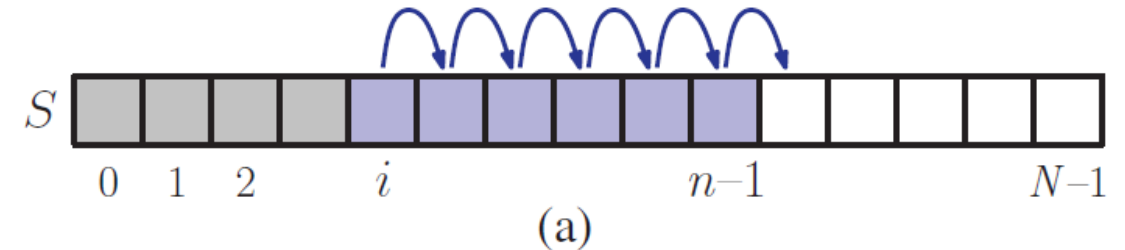
- Use a fixed size array A , where $A[i]$ stores the element at index i
 - The sufficiently large size N of array A
 - the number $n < N$ of elements in the vector in a member variable.
 - $at(i)$ operation just return $A[i]$.

Operation	Time
size()	$O(1)$
empty()	$O(1)$
at(i)	$O(1)$
set(i, e)	$O(1)$
insert(i, e)	$O(n)$
erase(i)	$O(n)$

Algorithm insert(i, e):

```

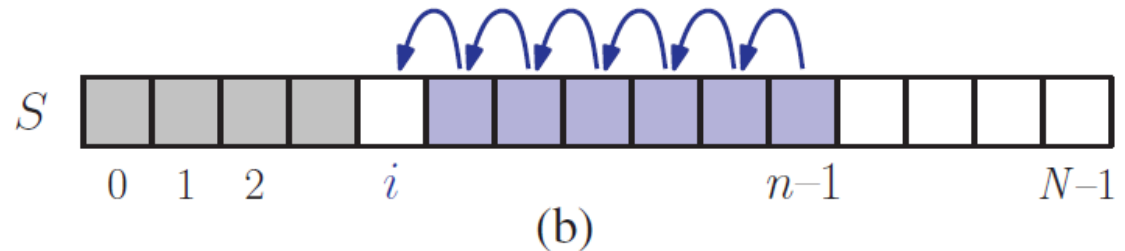
for  $j = n - 1, n - 2, \dots, i$  do
     $A[j + 1] \leftarrow A[j]$     {make room for the new element}
 $A[i] \leftarrow e$ 
 $n \leftarrow n + 1$ 
    
```



Algorithm erase(i):

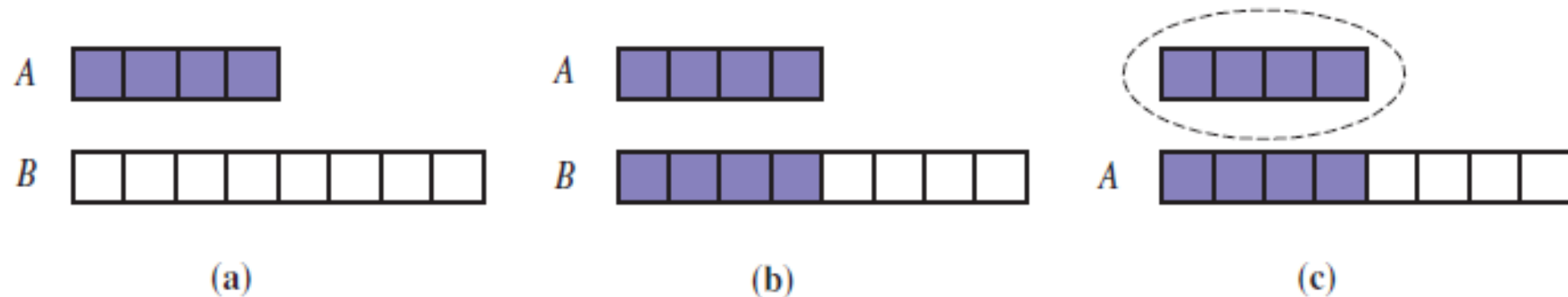
```

for  $j = i + 1, i + 2, \dots, n - 1$  do
     $A[j - 1] \leftarrow A[j]$     {fill in for the removed element}
 $n \leftarrow n - 1$ 
    
```



Extendable Array Implementation

- A major weakness of the simple array implementation for the vector ADT
 - It requires advance specification of a fixed capacity N
- Array replacement strategy (**Extendable Array**)
 - when an overflow occurs, that is, when $n=N$ and function insert is called
 - 1. Allocate a new array B of capacity $2N$
 - 2. Copy $A[i]$ to $B[i]$, for $i = 0, \dots, N-1$
 - 3. Deallocate A and reassign A to point to the new array B



Extendable Array Implementation

- Vector implementation using an extendable array
 - Two means for accessing individual elements of the vector
 - ***at()*** function performs a range test
 - There is no need to explicitly define a ***set*** function
 - $v.set(i, 5)$ could be implemented either as $v[i] = 5$ or, more safely, as $v.at(i) = 5$.

```
typedef int Elem;           // base element type

class ArrayVector {
public:
    ArrayVector();           // constructor
    int size() const;        // number of elements
    bool empty() const;      // is vector empty?
    Elem& operator[](int i);  // element at index
    Elem& at(int i) throw(IndexOutOfBounds); // element at index
    void erase(int i);        // remove element at index
    void insert(int i, const Elem& e); // insert element at index
    void reserve(int N);      // reserve at least N spots
    // ... (housekeeping functions omitted)

private:
    int capacity;            // current array size
    int n;                   // number of elements in vector
    Elem* A;                 // array storing the elements
};

ArrayVector::ArrayVector() // constructor
    : capacity(0), n(0), A(NULL) { }

int ArrayVector::size() const // number of elements
{ return n; }

bool ArrayVector::empty() const // is vector empty?
{ return size() == 0; }

Elem& ArrayVector::operator[](int i) // element at index
{ return A[i]; }

Elem& ArrayVector::at(int i) throw(IndexOutOfBounds) // element at index (safe)
{
    if (i < 0 || i >= n)
        throw IndexOutOfBounds("illegal index in function at()");
    return A[i];
}
```


Extendable Array Implementation

- Vector implementation using an extendable array

```
void ArrayVector::erase(int i) {  
    for (int j = i+1; j < n; j++)  
        A[j - 1] = A[j];  
    n--;  
}
```

```
// remove element at index  
void ArrayVector::reserve(int N) {  
    if (capacity >= N) return;  
    Elem* B = new Elem[N];  
    for (int j = 0; j < n; j++)  
        B[j] = A[j];  
    if (A != NULL) delete [] A;  
    A = B;  
    capacity = N;  
}  
void ArrayVector::insert(int i, const Elem& e) {  
    if (n >= capacity)  
        reserve(max(1, 2 * capacity));  
    for (int j = n - 1; j >= i; j--)  
        A[j+1] = A[j];  
    A[i] = e;  
    n++;  
}
```

// reserve at least N spots
// already big enough
// allocate bigger array
// copy contents to new array

// discard old array
// make B the new array
// set new capacity

// overflow?
// double array size
// shift elements up


// put in empty slot
// one more element

STL Vectors

- The class vector is perhaps the most basic example of an STL container class
- Like standard C++ arrays, but they provide many additional features.
 - Elements can also be accessed by a member function called *at*
 - STL vectors can be dynamically resized
 - When an STL vector of class objects is destroyed, it automatically invokes the destructor for each of its elements
 - A number of useful functions

```
#include <vector>           // provides definition of vector
using std::vector;         // make vector accessible

vector<int> myVector(100);  // a vector with 100 integers
```

 **base type**

STL Vectors

- Member functions of STL vector

`vector(n)`: Construct a vector with space for *n* elements; if no argument is given, create an empty vector.

`size()`: Return the number of elements in *V*.

`empty()`: Return true if *V* is empty and false otherwise.

`resize(n)`: Resize *V*, so that it has space for *n* elements.

`reserve(n)`: Request that the allocated storage space be large enough to hold *n* elements.

`operator[]`: Return a reference to the *i*th element of *V*.

`at(i)`: Same as *V*[*i*], but throw an `out_of_range` exception if *i* is out of bounds, that is, if $i < 0$ or $i \geq V.size()$.

`front()`: Return a reference to the first element of *V*.

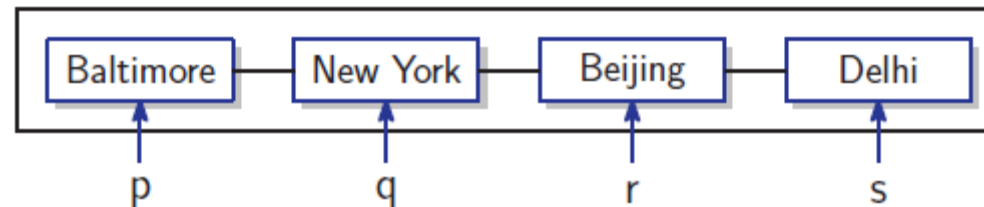
`back()`: Return a reference to the last element of *V*.

`push_back(e)`: Append a copy of the element *e* to the end of *V*, thus increasing its size by one.

`pop_back()`: Remove the last element of *V*, thus reducing its size by one.

Node-Based Operations and Iterators

- If we have a list L implemented with a (singly or doubly) linked list
 - more natural and efficient to use a node instead of an index
 - Node-based operations
 - Speedups over index-based functions
 - Finding the index of an element in a linked list requires searching through the list incrementally
 - **Position**
 - data type that abstracts the notion of the relative **position** or place of an element within a list
- `element()`: Return a reference to the element stored at this position.
- given a position variable p , the associated element can be accessed by $*p$
 - A position q , which is associated with some element e in a container, does not change, even if the index of e changes in the container



Iterators

- An iterator is an extension of a position
 - it also provides the ability to navigate forwards (and possibly backwards) through the container
- There are a number of ways in which to define an ADT for an iterator object
 - `p.next()`
 - `++p`
- Two special iterator values, `begin` and `end`



List ADT

- List ADT supports the following functions

`begin()`: Return an iterator referring to the first element of L ; same as `end()` if L is empty.

`end()`: Return an iterator referring to an imaginary element just after the last element of L .

`insertFront(e)`: Insert a new element e into L as the first element. ← `insert(L.begin(), e)`

`insertBack(e)`: Insert a new element e into L as the last element. ← `insert(L.end(), e)`

`insert(p , e)`: Insert a new element e into L before position p in L .

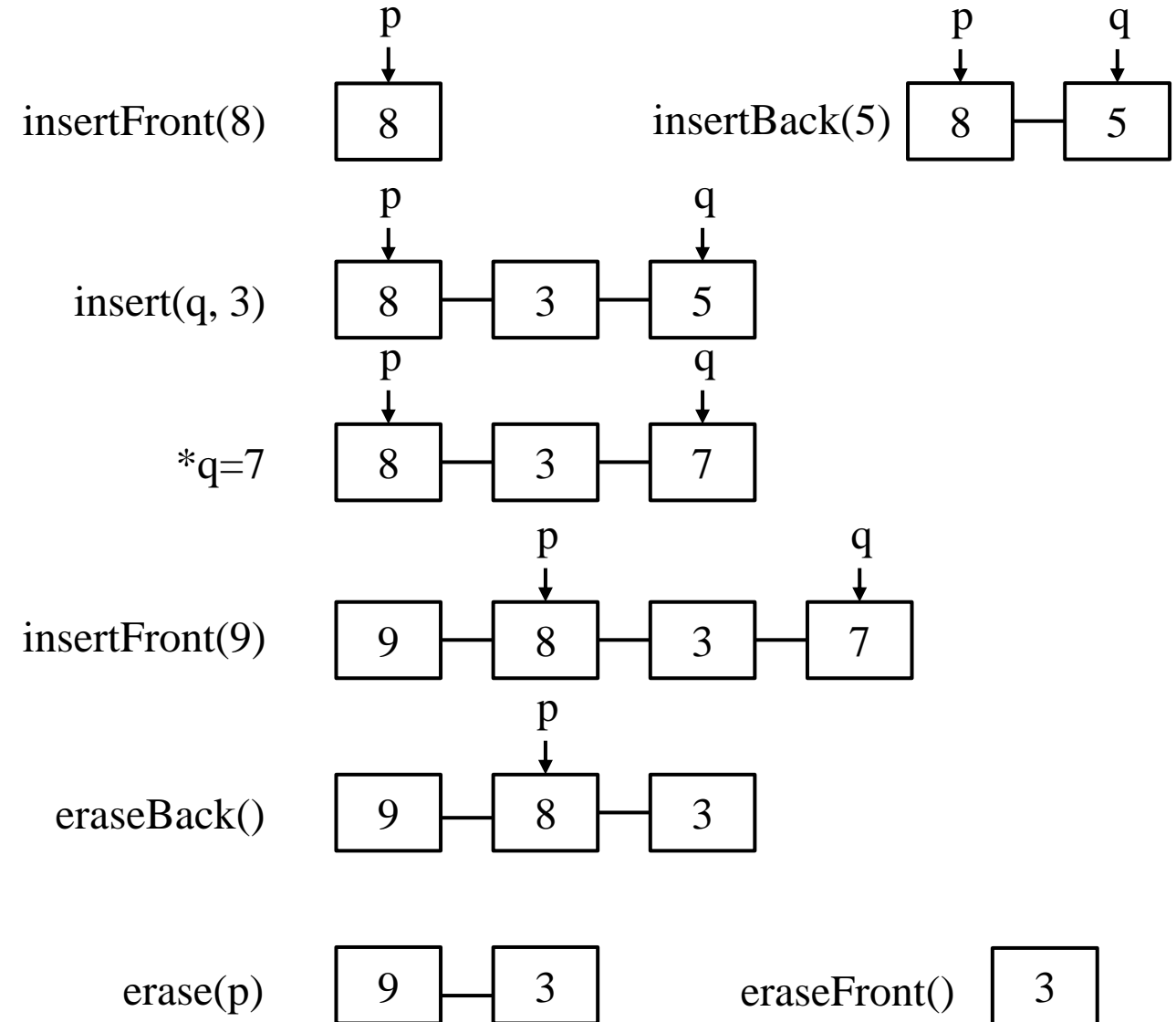
`eraseFront()`: Remove the first element of L .

`eraseBack()`: Remove the last element of L .

`erase(p)`: Remove from L the element at position p ; invalidates p as a position.

List ADT

Operation	Output	L
insertFront(8)	—	(8)
$p = \text{begin}()$	$p : (8)$	(8)
insertBack(5)	—	(8, 5)
$q = p; ++q$	$q : (5)$	(8, 5)
$p == \text{begin}()$	true	(8, 5)
insert($q, 3$)	—	(8, 3, 5)
$*q = 7$	—	(8, 3, 7)
insertFront(9)	—	(9, 8, 3, 7)
eraseBack()	—	(9, 8, 3)
erase(p)	—	(9, 3)
eraseFront()	—	(3)



List Implementation: Doubly Linked List

```
struct Node {  
    Elem elem;  
    Node* prev;  
    Node* next;  
};  
  
class Iterator {  
public:  
    Elem& operator*();  
    bool operator==(const Iterator& p) const;  
    bool operator!=(const Iterator& p) const;  
    Iterator& operator++();  
    Iterator& operator--();  
    friend class NodeList;  
private:  
    Node* v;  
    Iterator(Node* u);  
};
```

```
// a node of the list  
// element value  
// previous in list  
// next in list
```

```
// an iterator for the list  
  
// reference to the element  
// compare positions  
  
// move to next position  
// move to previous position  
// give NodeList access
```

```
// pointer to the node  
// create from node
```

nested class Iterator

```
NodeList::Iterator::Iterator(Node* u) // constructor from Node*  
{ v = u; }  
  
Elem& NodeList::Iterator::operator*() // reference to the element  
{ return v->elem; }  
  
// compare positions  
bool NodeList::Iterator::operator==(const Iterator& p) const  
{ return v == p.v; }  
  
bool NodeList::Iterator::operator!=(const Iterator& p) const  
{ return v != p.v; }  
  
// move to next position  
NodeList::Iterator& NodeList::Iterator::operator++()  
{ v = v->next; return *this; }  
  
// move to previous position  
NodeList::Iterator& NodeList::Iterator::operator--()  
{ v = v->prev; return *this; }
```

This makes it possible to use the result of the increment operation, as in "q = ++p"

List Implementation: Doubly Linked List

```
typedef int Elem;           // list base element type
class NodeList {           // node-based list
private:
    // insert Node declaration here...
public:
    // insert Iterator declaration here...
public:
    NodeList();             // default constructor
    int size() const;       // list size
    bool empty() const;     // is the list empty?
    Iterator begin() const; // beginning position
    Iterator end() const;   // (just beyond) last position
    void insertFront(const Elem& e); // insert at front
    void insertBack(const Elem& e);  // insert at rear
    void insert(const Iterator& p, const Elem& e); // insert e before p
    void eraseFront();       // remove first
    void eraseBack();        // remove last
    void erase(const Iterator& p); // remove p
    // housekeeping functions omitted...
private:
    // data members
    int n;                  // number of items
    Node* header;           // head-of-list sentinel
    Node* trailer;          // tail-of-list sentinel
};
```

List Implementation: Doubly Linked List

```
NodeList::NodeList() {           // constructor
    n = 0;                       // initially empty
    header = new Node;           // create sentinels
    trailer = new Node;
    header->next = trailer;       // have them point to each other
    trailer->prev = header;
}

int NodeList::size() const       // list size
{ return n; }

bool NodeList::empty() const     // is the list empty?
{ return (n == 0); }

NodeList::Iterator NodeList::begin() const // begin position is first item
{ return Iterator(header->next); }

NodeList::Iterator NodeList::end() const   // end position is just beyond last
{ return Iterator(trailer); }
```

List Implementation: Doubly Linked List

```

// insert e before p
void NodeList::insert(const NodeList::Iterator& p, const Elem& e) {
    Node* w = p.v;           // p's node
    Node* u = w->prev;        // p's predecessor
    Node* v = new Node;      // new node to insert
    v->elem = e;
    v->next = w; w->prev = v;  // link in v before w
    v->prev = u; u->next = v;  // link in v after u
    n++;
}

void NodeList::insertFront(const Elem& e) // insert at front
{ insert(begin(), e); }

void NodeList::insertBack(const Elem& e) // insert at rear
{ insert(end(), e); }

// remove p
// node to remove
// successor
// predecessor
// unlink p
// delete this node
// one fewer element
void NodeList::erase(const Iterator& p) {
    Node* v = p.v;
    Node* w = v->next;
    Node* u = v->prev;
    u->next = w; w->prev = u;
    delete v;
    n--;
}

// remove first
void NodeList::eraseFront()
{ erase(begin()); }

// remove last
void NodeList::eraseBack()
{ erase(--end()); }
```

why we chose to define the iterator function end to return an imaginary position that lies just beyond the end of the list?

STL List

- The STL list is implemented as a doubly linked list.

```
#include <list>
using std::list;           // make list accessible
list<float> myList;        // an empty list of floats
```

`list(n)`: Construct a list with *n* elements; if no argument list is given, an empty list is created.

`size()`: Return the number of elements in *L*.

`empty()`: Return true if *L* is empty and false otherwise.

`front()`: Return a reference to the first element of *L*.

`back()`: Return a reference to the last element of *L*.

`push_front(e)`: Insert a copy of *e* at the beginning of *L*. ← **insertFront**

`push_back(e)`: Insert a copy of *e* at the end of *L*. ← **insertBack**

`pop_front()`: Remove the first element of *L*. ← **eraseFront**

`pop_back()`: Remove the last element of *L*. ← **eraseBack**

STL Containers and Iterators

- The STL provides a variety of different container classes
 - A container is a data structure that stores a collection of elements
- STL iterators provide a relatively **uniform method for accessing and enumerating the elements** stored in containers.

<i>STL Container</i>	<i>Description</i>
vector	Vector
deque	Double ended queue
list	List
stack	Last-in, first-out stack
queue	First-in, first-out queue
priority_queue	Priority queue
set (and multiset)	Set (and multiset)
map (and multimap)	Map (and multi-key map)

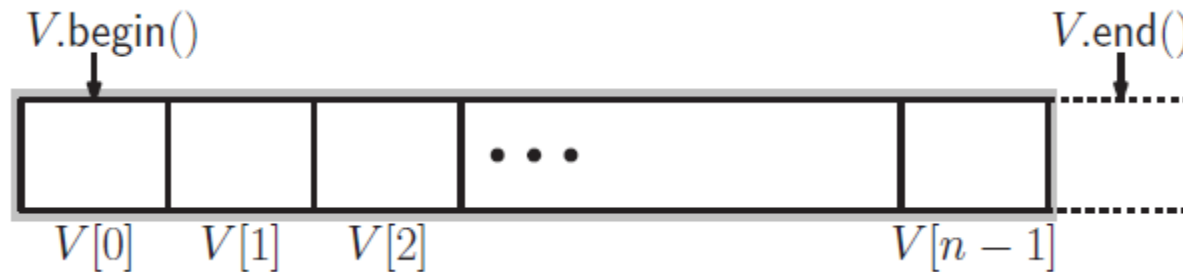
```
int vectorSum1(const vector<int>& V) {  
    int sum = 0;  
    for (int i = 0; i < V.size(); i++)  
        sum += V[i];  
    return sum;  
}
```

Unfortunately, this method would not be applicable to other types of containers

because it relies on the fact that the elements of a vector can be accessed efficiently through indexing.

STL Iterators

- Every STL container class defines a special associated class called an iterator
- Iterator is an object that specifies a position within a container
- If p is an iterator
 - $*p$ yields a reference to the associated element.
 - either $++p$ or $p++$ advances p to point to the next element of the container



```
int vectorSum2(vector<int> V) {  
    typedef vector<int>::iterator Iterator;           // iterator type  
    int sum = 0;  
    for (Iterator p = V.begin(); p != V.end(); ++p)  
        sum += *p;  
    return sum;  
}
```

This approach can be applied to any STL container class, not just vectors

STL Iterators

- Const Iterators
 - it is possible to read the values of the container by dereferencing the iterator
 - it is not possible to modify the container's values

```
int vectorSum3(const vector<int>& V) {  
    typedef vector<int>::const_iterator ConstIterator; // iterator type  
    int sum = 0;  
    for (ConstIterator p = V.begin(); p != V.end(); ++p)  
        sum += *p;  
    return sum;  
}
```

STL Iterators

- STL Iterator-Based Container Functions
 - The member functions of the STL vector class that use iterators as arguments.
 - The above functions are also defined for the STL list and the STL deque
 - These three STL containers (vector, list, and deque) are called **sequence containers**

`vector(p,q)`: Construct a vector by iterating between p and q , copying each of these elements into the new vector.

`assign(p,q)`: Delete the contents of V , and assigns its new contents by iterating between p and q and copying each of these elements into V .

`insert(p,e)`: Insert a copy of e just prior to the position given by iterator p and shifts the subsequent elements one position to the right.

`erase(p)`: Remove and destroy the element of V at the position given by p and shifts the subsequent elements one position to the left.

`erase(p,q)`: Iterate between p and q , removing and destroying all these elements and shifting subsequent elements to the left to fill the gap.

`clear()`: Delete all these elements of V .

the iterator range is understood to start with p and end just prior to q , $[p,q)$

Note that the vector member functions insert and erase **move elements around in the vector**. They can be quite slow.

STL Iterators

- STL Vectors and Algorithms
 - the STL also provides a number of algorithms that operate on containers
 - `#include <algorithm>`

`sort(p,q)`: Sort the elements in the range from p to q in ascending order. It is assumed that less-than operator (“<”) is defined for the base type.

`random_shuffle(p,q)`: Rearrange the elements in the range from p to q in random order.

`reverse(p,q)`: Reverse the elements in the range from p to q .

`find(p,q,e)`: Return an iterator to the first element in the range from p to q that is equal to e ; if e is not found, q is returned.

`min_element(p,q)`: Return an iterator to the minimum element in the range from p to q .

`max_element(p,q)`: Return an iterator to the maximum element in the range from p to q .

`for_each(p,q,f)`: Apply the function f the elements in the range from p to q .

For example, to sort an entire vector V , we would use `sort(V.begin(),V.end())`.

STL Iterators

STL Vectors and Algorithms

```
#include <cstdlib>           // provides EXIT_SUCCESS
#include <iostream>          // I/O definitions
#include <vector>             // provides vector
#include <algorithm>          // for sort, random_shuffle

using namespace std;        // make std:: accessible

int main () {
    int a[] = {17, 12, 33, 15, 62, 45};
    vector<int> v(a, a + 6); // v: 17 12 33 15 62 45
    cout << v.size() << endl; // outputs: 6
    v.pop_back();            // v: 17 12 33 15 62
    cout << v.size() << endl; // outputs: 5
    v.push_back(19);         // v: 17 12 33 15 62 19
    cout << v.front() << " " << v.back() << endl; // outputs: 17 19
    sort(v.begin(), v.begin() + 4); // v: (12 15 17 33) 62 19
    v.erase(v.end() - 4, v.end() - 2); // v: 12 15 62 19
    cout << v.size() << endl; // outputs: 4

    char b[] = {'b', 'r', 'a', 'v', 'o'};
    vector<char> w(b, b + 5); // w: b r a v o
    random_shuffle(w.begin(), w.end()); // w: o v r a b
    w.insert(w.begin(), 's'); // w: s o v r a b

    for (vector<char>::iterator p = w.begin(); p != w.end(); ++p)
        cout << *p << " "; // outputs: s o v r a b
    cout << endl;
    return EXIT_SUCCESS;
}
```

random_shuffle to permute the elements
of the vector randomly

Sequence

- Sequence
 - An abstract data type that generalizes the vector and list ADTs
 - A sequence is an ADT that supports all the functions of the list ADT
 - It also provides functions for accessing elements by their index, as we did in the vector ADT
 - Provides the following two “bridging” functions

$\text{atIndex}(i)$: Return the position of the element at index i .

$\text{indexOf}(p)$: Return the index of the element at position p .

Sequence Implementation: Doubly Linked List

- Sequence

```
class NodeSequence : public NodeList {
public:
    Iterator atIndex(int i) const;           // get position from index
    int indexOf(const Iterator& p) const;    // get index from position
};

// get position from index
NodeSequence::Iterator NodeSequence::atIndex(int i) const {
    Iterator p = begin();
    for (int j = 0; j < i; j++) ++p;
    return p;
}

// get index from position
int NodeSequence::indexOf(const Iterator& p) const {
    Iterator q = begin();
    int j = 0;
    while (q != p) {
        ++q; ++j;
    }
    return j;
}
```

Sequence Implementation: Doubly Linked List vs. Array

<i>Operations</i>	<i>Circular Array</i>	<i>List</i>
size, empty	$O(1)$	$O(1)$
atIndex, indexOf	$O(1)$	$O(n)$
begin, end	$O(1)$	$O(1)$
$*p, ++p, --p$	$O(1)$	$O(1)$
insertFront, insertBack	$O(1)$	$O(1)$
insert, erase	$O(n)$	$O(1)$