

# Homework 6

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## 8.1

A decomposition  $\{R_1, R_2\}$  is a lossless-join decomposition if  $R_1 \cap R_2 \rightarrow R_1$  or  $R_1 \cap R_2 \rightarrow R_2$ . Let  $R_1 = (A, B, C)$ ,  $R_2 = (A, D, E)$ , and  $R_1 \cap R_2 = A$ . Since  $A$  is a candidate key, Therefore  $R_1 \cap R_2 \rightarrow R_1$ .

## 8.13

The dependency  $B \rightarrow D$  is not preserved.  $F_1$  contains no dependencies with  $D$  on the right side of the arrow.  $F_2$  contains no dependencies with  $B$  on the left side of the arrow. Therefore for  $B \rightarrow D$  to be preserved there must be an FD  $B \rightarrow a$  in  $F_1$  and  $a \rightarrow D$  in  $F_2$  (so  $B \rightarrow D$  would follow by transitivity). Since the intersection of the two schemes is  $A$ ,  $a = A$ . Observe that  $B \rightarrow A$  is not in  $F_1$  since  $B^+ = BD$ .

## 8.19

From Exercise 8.6, we know that  $B \rightarrow D$  is nontrivial and the left hand side is not a superkey. By the algorithm of Figure 8.11 we

derive the relations  $\{(A, B, C, E), (B, D)\}$ . This is in BCNF.

## 8.20

First we note that the dependencies given in Practice Exercise 8.1 form a canonical cover. Generating the schema from the algorithm of Figure 8.12 we get  $R' = \{(A, B, C), (C, D, E), (B, D), (E, A)\}$ . Schema  $(A, B, C)$  contains a candidate key. Therefore  $R'$  is a 3NF dependency-preserving lossless-join decomposition. Note that the original schema  $R = (A, B, C, D, E)$  is already in 3NF. Thus, it was not necessary to apply the algorithm as we have done above. The single original schema is trivially a lossless join, dependency-preserving decomposition.

## 8.28

$(A, B, C, D, E)$

A	B	C	D	E
a1	b1	c1	d1	e1
a2	b2	c2	d2	e2
a3	b3	c3	d3	e3

$(A, B, C)$

A	B	C
a1	b1	c1

a2	b2	c2
a3	b3	c3

(C, D, E)

C	D	E
c1	d1	e1
c2	d2	e2
c3	d3	e3

The decomposition is not a lossless-join decomposition.