

Software Paradigms SS 2015 4

| Nachname | Vorname | Matrikelnummer |
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| LORENZ | Peter | |
| ZIKO | Haris | |

Exercise 1**1.**

$$t = p(Y, f(X), a), t' = p(X, f(b), X)$$

$$\theta = \{X/Y\}$$

$$t = p(Y, f(Y), a); t' = p(Y, f(b), Y)$$

$$\theta = \theta \cup \{Y/b\}$$

$$t = p(b, f(b), a); t' = p(b, f(b), b)$$

Not unifiable, see rule 2a from Slides 7 - S17. There are different values, and no Variables.

2.

$$t = q(f(a), g(f(a)), Y), t' = q(X, g(X), f(g(a)))$$

$$\Theta = \{X/f(a)\}$$

$$t = q(f(a), g(f(a)), Y), t' = q(f(a), g(f(a)), f(g(a)))$$

$$\Theta = \Theta \cup \{Y/f(g(a))\}$$

$$t = q(f(a), g(f(a)), f(g(a))), t' = q(f(a), g(f(a)), f(g(a)))$$

□

$$MGU = \{X/f(a), Y/f(g(a))\}$$

3.

$$t = r(b, f(g(X)), Z) \text{ und } t' = r(X, Z, f(g(a)))$$

$$\Theta = \{X/b\}$$

$$r(b, f(g(b)), Z); r(b, Z, f(g(a)))$$

$$\Theta = \{Z/f(g(b))\}$$

$$r(b, f(g(b)), f(g(b))); r(b, f(g(b)), f(g(a)))$$

$$MGU = \{X/b, Z/f(g(b))\}$$

Not unifiable. Slides 7 - S17. It exists a difference correspondig to 2.a, but there are not any variables. The algorithm stops, because there is a difference between t and t'.

4.

$$t = s(X, c, Y), t' = s(g(a, b), Z, f(Y))$$

$$\Theta = \{X/g(a,b)\}$$

$$t = s(g(a,b),c,Y), t' = s(g(a,b),Z,f(Y))$$

Not unifiable, see rule 2b from Slides 7 - S17. It is not possible to unify Y with $f(Y)$.

5.

$$t = u(f(Z,g(X)),Z), t' = u(f(g(a),g(Z)), X)$$

$$\Theta = \{Z/g(a)\}$$

$$t = u(f(g(a),g(X)),g(a)), t' = u(f(g(a),g(g(a))), X)$$

$$\Theta = \Theta \cup \{X/g(a)\}$$

$$t = u(f(g(a),g(g(a))),g(a)), t' = u(f(g(a),g(g(a))), g(a))$$

□

$$MGU = \{Z/g(a), X/g(a)\}$$

Exercise 2

Predicate for greater(X,Y)

greater(s(_), 0) :=.

greater(s(X),s(Y)) := greater(X,Y)

show, if the next statement is true or false:

:=greater(s(s(s(0))), s(s(s(0))))

\neg greater(s(s(s(0))), s(s(s(0)))) \neg greater(X,Y) \vee greater(s(X),s(Y))
 $\{X \mid s(s(0)), Y \mid s(s(0))\}$

\neg greater(s(s(0)), s(s(0))) \neg greater(X,Y) \vee greater(s(X),s(Y))
 $\{X \mid s(0), Y \mid s(0)\}$

\neg greater(s(0), s(0)) \neg greater(X,Y) \vee greater(s(X),s(Y))
 $\{X \mid 0, Y \mid 0\}$

\neg greater(0, 0) \neg greater(X,Y) \vee greater(s(X),s(Y))

Not possible, because no MGU exists.

\neg greater(0, 0) \neg greater(s(_),0)

Not possible, because left side is not equal to right side.

Reject input =_ False

Exercise 3

1.

male(mannister).

male(lombard).

male(tytos).

female(genna).

male(jamballalia).

male(kevan).

male(lancel).

male(willem).

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female(janei).
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male(tywin).
male(jaime).
female(cersei).
male(tyrion).
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```
parent(mannister, lombard).
parent(mannister, tytos).
parent(mannister, jamballalia).
```

```
parent(tytos, genna).
parent(tytos, tywin).
parent(tytos, kevan).
```

```
parent(kevan, lancel).
parent(kevan, willem).
parent(kevan, janei).
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```
parent(tywin, jaime).
parent(tywin, cersei).
parent(tywin, tyrion).
```

2.

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grandp(X,Y) :- parent(X, P), parent(P, Y).
sibling(X,Y) :- parent(P,X), parent(P,Y), X\=Y.
cousin(X,Y) :- parent(A,X), parent(B,Y), sibling(A,B), male(X).
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c1 = grandp(X,Y) ∨ ¬parent(X, P) ∨ ¬parent(P, Y).
c2 = sibling(X,Y) ∨ ¬parent(P,X) ∨ ¬parent(P,Y) ∨ ¬X̄Ȳ.
c3 = cousin(X,Y) ∨ ¬male(X) ∨ ¬parent(A,X) ∨ ¬parent(B,Y) ∨ ¬sibling(A,B).
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:= cousin(willem, jaime).
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| Program | MGU | Rule |
|---|---|---|
| $\neg\text{cousin}(\text{willem}, \text{jaimie})$ | $\theta = \{X/\text{willem}, Y/\text{jaimie}\}$ | $\text{cousin}(X,Y) \vee \neg \text{male}(X) \vee \neg\text{parent}(A,X) \vee \neg\text{parent}(B,Y) \vee \neg \text{sibling}(A,B)$ |
| $\neg \text{male}(\text{willem}) \vee \neg\text{parent}(A,\text{willem}) \vee \neg\text{parent}(B,\text{jaimie}) \vee \neg \text{sibling}(A,B)$ | | $\text{male}(\text{willem})$ |
| $\neg\text{parent}(A,\text{willem}) \vee \neg\text{parent}(B,\text{jaimie}) \vee \neg \text{sibling}(A,B)$ | $\theta = \{A/\text{kevan}, B/\text{tywin}\}$ | $\text{parent}(\text{kevan}, \text{willem})$ and $\text{parent}(\text{tywin}, \text{jaimie})$ |
| $\text{sibling}(\text{kevan}, \text{tywin})$ | $\theta = \{X/\text{kevan}, B/\text{tywin}\}$ | $\text{sibling}(X,Y) \vee \neg\text{parent}(P,X) \vee \neg\text{parent}(P,Y) \vee \neg X\bar{Y}$ |
| $\neg\text{parent}(P,X) \vee \neg\text{parent}(P,Y) \vee \neg X\bar{Y}$ | $\theta = \{P/\text{tytos}\}$ | $\text{parent}(\text{tytos}, \text{kevan})$ and $\text{parent}(\text{tytos}, \text{tywan})$ |
| \square | | |

3.

$\text{granddaughter}(X,Y) :- \text{grandp}(Y,X), \text{female}(X).$

| Program | MGU | Rule |
|--|-------------------------------|---|
| $:= \text{granddaughter}(X,\text{tytos})$ | $\theta = \{Y/\text{tytos}\}$ | $\text{granddaughter}(X,Y) \vee \neg\text{grandp}(Y,X) \vee \text{female}(X)$ |
| $\neg\text{grandp}(\text{tytos},X) \vee \neg\text{female}(X)$ | $\theta = \{X/\text{tytos}\}$ | $\text{grandp}(X,Y) \vee \neg\text{parent}(X,P) \vee \neg\text{parent}(P,Y)$ |
| $\neg\text{parent}(\text{tytos}, P) \vee \neg\text{p}(P,Y)$ | $\theta = \{P/\text{kevan}\}$ | $\text{parents}(\text{tytos}, \text{kevan}).$ |
| $\neg\text{parents}(\text{tytos}, \text{kevan}) \vee \neg\text{parents}(\text{kevan},Y)$ | $\theta = \{Y/\text{janei}\}$ | $\text{p}(\text{kevan}, \text{janei})$ |
| $\text{parents}(\text{kevan}, \text{janei})$ | | |
| \square | | |

Exercise 4

1.

$\text{edge}(a, b, s(s(s(0)))).$
 $\text{edge}(a, c, s(0)).$
 $\text{edge}(c, d, s(s(0))).$
 $\text{edge}(b, d, s(s(0))).$

$\text{add}(0,Y,Y). \text{add}(s(X),Y,s(Z)) := \text{add}(X,Y,Z). \text{greaterequ}(X,0).$
 $\text{greaterequ}(s(X), s(Y)) := \text{greaterequ}(X,Y).$

$\text{path}(S,E,M) := \text{find}(S,E,N), \text{greaterrequ}(M,N).$

$\text{find}(S,E,L) := \text{edge}(S,E,L).$

$\text{find}(S,E,N) := \text{edge}(S,X,L), \text{find}(X,E,N1), \text{add}(N1,L,N).$

2.

c1: $\text{edge}(a, b, s(s(s(0))))$.

c2: $\text{edge}(a, c, s(0))$.

c3: $\text{edge}(c, d, s(s(0)))$.

c4: $\text{edge}(b, d, s(s(0)))$.

c5: $\text{add}(0, Y, Y)$. c6: $\text{add}(s(X), Y, s(Z)) \vee \neg \text{add}(X, Y, Z)$. c7: $\text{greaterrequ}(X, 0)$.

c8: $\text{greaterrequ}(s(X), s(Y)) \vee \neg \text{greaterrequ}(X, Y)$.

c9: $\text{path}(S, E, M) \vee \neg \text{find}(S, E, N) \vee \neg \text{greaterrequ}(M, N)$.

c10: $\text{find}(S, E, L) \vee \neg \text{edge}(S, E, L)$.

c11: $\text{find}(S, E, N) \vee \neg \text{edge}(S, X, L) \vee \neg \text{find}(X, E, N1) \vee \neg \text{add}(N1, L, N)$

| Program | MGU | Rule |
|--|---------------------------------|--|
| $\neg \text{path}(a, d, s(s(s(s(0)))))$ | $\{S/a, E/d, M/s(s(s(s(0))))\}$ | c9: $\text{path}(S, E, M)$ $\vee \neg \text{find}(S, E, N)$ $\vee \neg \text{greaterrequ}(M, N)$ |
| $\neg \text{find}(a, d, N) \vee$ $\neg \text{greaterrequ}(s(s(s(s(0))))) , N$ | $\{S/a, E/d\}$ | c11: $\text{find}(S, E, N)$ $\vee \neg \text{edge}(S, X, L)$ $\vee \neg \text{find}(X, E, N1)$ $\vee \neg \text{add}(N1, L, N)$ |
| $\neg \text{edge}(a, X, L) \vee$ $\neg \text{find}(X, d, N1) \vee$ $\neg \text{add}(N1, L, N)$ $\neg \text{greaterrequ}(s(s(s(s(0))))) , N$ | $\{X/c, L/s(0)\}$ | c2: $\text{edge}(a, c, s(0))$ |
| $\neg \text{find}(c, d, N1) \vee$ $\neg \text{add}(N1, s(0), N)$ $\neg \text{greaterrequ}(s(s(s(s(0))))) , N$ | $\{S/c, E/d, L/N1\}$ | c10: $\text{find}(S, E, L)$ $\vee \neg \text{edge}(S, E, L)$ |
| $\neg \text{edge}(c, d, N1) \vee$ $\neg \text{add}(N1, s(0), N)$ $\neg \text{greaterrequ}(s(s(s(s(0))))) , N$ | $\{N1/s(s(0))\}$ | c3: $\text{edge}(c, d, s(s(0)))$ |
| $\neg \text{add}(s(s(0)), s(0), N) \vee$ $\neg \text{greaterrequ}(s(s(s(s(0))))) , N$ | $\{X/s(0), Y/s(0), N/s(Z)\}$ | c6: $\text{add}(s(X), Y, s(Z))$ $\vee \neg \text{add}(X, Y, Z)$ |
| $\neg \text{add}(s(0), s(0), s(Z)) \vee$ $\neg \text{greaterrequ}(s(s(s(s(0))))) , s(Z)$ | $\{X'/s(0), Y'/s(0), Z/s(Z')\}$ | c6: $\text{add}(s(X'), Y', s(Z'))$ $\vee \neg \text{add}(X', Y', Z')$ |
| $\neg \text{add}(0, s(0), s(s(Z'))) \vee$ $\neg \text{greaterrequ}(s(s(s(s(0))))) , s(s(Z'))$ | $\{Y''/s(0), Z'/Y''\}$ | c5: $\text{add}(0, Y'', Y'')$ |
| $\neg \text{greaterrequ}(s(s(s(s(0))))) , s(s(0))$ | $\{X/s(s(0)), Y/s(s(0))\}$ | c8: $\text{greaterrequ}(s(X), s(Y))$ $\vee \neg \text{greaterrequ}(X, Y)$ |
| $\neg \text{greaterrequ}(s(s(s(0))), s(s(0)))$ | $\{X'/s(s(0)), Y'/s(s(0))\}$ | c8: $\text{greaterrequ}(s(X'), s(Y'))$ $\vee \neg \text{greaterrequ}(X', Y')$ |
| $\neg \text{greaterrequ}(s(s(0)), s(0))$ | $\{X''/s(0), Y''/s(0)\}$ | c8: $\text{greaterrequ}(s(X''), s(Y''))$ $\vee \neg \text{greaterrequ}(X'', Y'')$ |
| $\neg \text{greaterrequ}(s(0), 0)$ | $\{X'''/s(0)\}$ | c7: $\text{greaterrequ}(X''', 0)$ |
| \square | | |

We can say, that the input

Exercise 5**1.**

$$\text{less}(0, s(Y)).$$

$$\text{less}(s(X), s(Y)) := \text{less}(X, Y).$$

$$\text{union}(\text{null}, \text{null}, \text{null}).$$

$$\text{union}(\text{null}, Y, Y).$$

$$\text{union}(X, \text{null}, X).$$

$$\text{union}(\text{build}(X, Xs), \text{null}, \text{build}(X, Zs)) := \text{union}(Xs, \text{null}, Zs).$$

$$\text{union}(\text{null}, \text{build}(Y, Ys), \text{build}(Y, Zs)) := \text{union}(\text{null}, Ys, Zs).$$

$$\text{union}(\text{build}(Z, Xs), \text{build}(Z, Ys), \text{build}(Z, Zs)) := \text{union}(Xs, Ys, Zs).$$

$$\text{union}(\text{build}(X, Xs), \text{build}(Y, Ys), \text{build}(X, Zs)) := \text{less}(X, Y), \text{union}(Xs, \text{build}(Y, Ys), Zs).$$

$$\text{union}(\text{build}(X, Xs), \text{build}(Y, Ys), \text{build}(Y, Zs)) := \text{less}(Y, X), \text{union}(\text{build}(X, Xs), Ys, Zs).$$
2.

| | Resolution for Example 5 Nr. 2 |
|---------|---|
| Program | $:= \text{union}(\text{build}(0, \text{build}(s(s(0)), \text{null})), \text{build}(s(0), \text{null}), \text{build}(0, \text{build}(s(0), \text{build}(s(s(0)), \text{null})))$ |
| Rule | $\text{union}(\text{build}(X, Xs), \text{build}(Y, Ys), \text{build}(X, Zs)) := \text{less}(X, Y), \text{union}(Xs, \text{build}(Y, Ys), Zs).$ |
| MGU | $\{X/0, Xs/\text{build}(s(s(0)), \text{null}), Y/s(0), Ys/\text{null}, Zs/\text{build}(s(0), \text{build}(s(s(0)), \text{null}))\}$ |
| Program | $:= \text{less}(0, s(0)), \text{union}(\text{build}(s(s(0)), \text{null}), \text{build}(s(0), \text{null}), \text{build}(s(0), \text{build}(s(s(0)), \text{null})))$ |
| Rule | $\text{less}(0, s(Y)).$ |
| MGU | $\{Y/0\}$ |
| Program | $:= \text{union}(\text{build}(s(s(0)), \text{null}), \text{build}(s(0), \text{null}), \text{build}(s(0), \text{build}(s(s(0)), \text{null})))$ |
| Rule | $\text{union}(\text{build}(X, Xs), \text{build}(Y, Ys), \text{build}(Y, Zs)) := \text{less}(Y, X), \text{union}(\text{build}(X, Xs), Ys, Zs).$ |
| MGU | $\{X/s(s(0)), Xs/\text{null}, Y/s(0), Ys/\text{null}, Zs/\text{build}(s(s(0)), \text{null})\}$ |
| Program | $:= \text{less}(s(0), s(s(0))), \text{union}(\text{build}(s(s(0)), \text{null}), \text{null}, \text{build}(s(s(0)), \text{null})).$ |
| Rule | $\text{less}(s(X), s(Y)) := \text{less}(X, Y).$ |
| MGU | $\{X/0, Y/s(0)\}$ |
| Program | $:= \text{less}(0, s(0)), \text{union}(\text{build}(s(s(0)), \text{null}), \text{null}, \text{build}(s(s(0)), \text{null})).$ |
| Rule | $\text{less}(0, s(Y)).$ |
| MGU | $\{Y/0\}$ |
| Program | $:= \text{union}(\text{build}(s(s(0)), \text{null}), \text{null}, \text{build}(s(s(0)), \text{null})).$ |
| Rule | $\text{union}(\text{build}(X, Xs), \text{null}, \text{build}(X, Zs)) := \text{union}(Xs, \text{null}, Zs).$ |
| MGU | $\{X/s(s(0)), Xs/\text{null}, Zs/\text{null}\}$ |
| Program | $:= \text{union}(\text{null}, \text{null}, \text{null}).$ |
| Rule | $\text{union}(\text{null}, \text{null}, \text{null}).$ |
| MGU | $\{\}$ |
| Program | \square |