# Sweet.js - Hygienic Macros for JavaScript

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# 1. Introduction

Sweet.js is a new hygienic macro system for JavaScript.

Macros systems have a long history in the design of extensible programming languages going back at least to lisp as a tool to provide programmers syntactic flexibility.

While powerful macro systems have been used extensively in lisp derived languages there has been considerable less movement for macros systems for languages with an expression based syntax such as JavaScript. This is due to a variety of technical reasons that have held back macro systems in expression based languages which we address in this paper.

Recently the Honu project has shown how to overcome some of the existing challenges in developing a macro system for expression based language. The Honu technique was designed for an idealized JavaScript like language. In this paper we show how to extend the ideas of Honu for full JavaScript and present additional techniques that target expression based languages.

The design of sweet.js attempts to overcome the following technical challenges:

- a correct implementation of read that structures the token stream before expansion begins
- parser class annotation (e.g. :expr) in patterns to allow macro authors easier declaration of a macro shape
- · operator overloading
- · infix macros
- the invoke primitive to allow custom parser classes and more powerful matching

# 2. Overview

TODO: syntax, main features etc...

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## 3. Read

The syntax of JavaScript presents a challenge to correctly implement the critical read function. This challenge is not present in Honu because their language is an idealized syntax that misses the problematic interaction of delimiters and regular expression literals.

TODO: motivate read with examples etc.

## 3.1 Proof of read

We first define a simplified grammar that captures just the essential complexity we want to address, namely the interaction between the division symbol / and the regular expression literal /x/.

$$\begin{array}{ccc} \textit{Token} & ::= & x \mid / \\ \textit{TokenTree} & ::= & x \mid / \mid /x/ \end{array}$$

We also define Expr' with the same productions as Expr but defined over  $TokenTree^*$  instead of  $Token^*$ . So the terminal /x/ in the second production of Expr is three distinct tokens (/, x, and /) while it is a single token in Expr'.

We define the grammar of a  $Program_e$  as a function from Token to Expr.

$$Program_e :: Token \rightarrow Expr$$

Theorem 1 (Read is correct).

$$\forall s \in Token.s \in Expr_e \text{ iff } t = read(s, p, 0), t \in Expr'_e.$$

Proof.

By showing set inclusion. Details in the appendix.

The grammar we present is a simplified version of the grammar specified in the ES5 specification. The simplification we are making do not affect the read algorithm, and only serve to shorten its presentation. In particular, functions can only have a single parameter, function bodies are not allowed to be empty and a few other minor changes. We only address the = assignment operator and only the / and + binary operators.

Figure 1: Simplified ES Grammar

```
PrimaryExpression<sub>x</sub>
                                                 ::=
                                                        х
PrimaryExpression<sub>/x/</sub>
                                                 ::=
                                                        / · x · /
PrimaryExpression_{\{x:e\}}
                                                         {x: AssignmentExpression<sub>e</sub>}
                                                 ::=
PrimaryExpression (e)
                                                 ::=
                                                          (AssignmentExpression<sub>e</sub>)
MemberExpression<sub>e</sub>
                                                         PrimaryExpression ..
                                                 ::=
{\it MemberExpression}_e
                                                 ::=
                                                          FunctionExpression<sub>e</sub>
MemberExpression_{e.x}
                                                         MemberExpression_e. x
                                                 ::=
CallExpression_{e (e')}
                                                          MemberExpression_e (AssignmentExpression<sub>e'</sub>)
                                                 ::=
CallExpression_{e (e')}
                                                 ::=
                                                         CallExpression<sub>e</sub> (AssignmentExpression<sub>e'</sub>)
CallExpression_{e.x}
                                                         CallExpression_e . x
                                                 ::=
BinaryExpression<sub>e</sub>
                                                 ::=
                                                          CallExpression<sub>e</sub>
BinaryExpression_{e / e'}
                                                          BinaryExpression<sub>e</sub> / BinaryExpression<sub>e</sub>
                                                 ::=
BinaryExpression_{e+e'}
                                                         BinaryExpression + BinaryExpression
                                                 ::=
                                                         {\it BinaryExpression}_e
AssignmentExpression<sub>e</sub>
                                                 ::=
AssignmentExpression_{e=e'}
                                                 ::=
                                                          CallExpression_e = AssignmentExpression_{e'}
ExpressionStatement<sub>e</sub>
                                                 ::=
                                                         AssignmentExpression<sub>e</sub>;
                                                          where lookahead \neq { or function
ReturnStatement_return;
ReturnStatement_{\mathtt{return}\ e}
                                                         return [no line terminator here] AssignmentExpression_e
                                                 ::=
Block_{\{e\}}
                                                          {StatementList<sub>e</sub>}
                                                 ::=
StatementList_e
                                                          Statement<sub>e</sub>
                                                 ::=
StatementList<sub>e,e'</sub>
                                                          StatementList<sub>e</sub> Statement<sub>e'</sub>
                                                 ::=
LabelledStatementx: e
                                                          x : Statement_e
                                                 ::=
\mathit{IfStatement}_{\mathtt{if}\ (e)\ e'\ \mathtt{else}\ e''}
                                                          if (AssignmentExpression<sub>e</sub>) Statement<sub>e''</sub> else Statement<sub>e''</sub>
                                                 ::=
Statement<sub>e</sub>
                                                 ::=
                                                          Block_e
                                                         Expression Statement_{\rho}
Statement_e
                                                 ::=
                                                         \underline{\mathit{IfS}tatement}_e
Statement<sub>e</sub>
                                                 ::=
Statement_e
                                                          ReturnStatement<sub>e</sub>
                                                         LabelledStatement_e
Statement_e
                                                 ::=
FunctionDeclaration_{function x (x) \{e\}}
                                                          function x (x) \{SourceElements_e\}
                                                 ::=
FunctionExpression<sub>function x (x) {e}</sub>
                                                          function x (x) \{SourceElements_e\}
                                                 ::=
SourceElement_e
                                                          Statement<sub>e</sub>
                                                 ::=
SourceElement_e
                                                          FunctionDeclaration_e
                                                 ::=
SourceElements<sub>e</sub>.
                                                 ::=
                                                          SourceElement<sub>e</sub>
SourceElements<sub>e.e.</sub>
                                                 ::=
                                                          SourceElements<sub>e</sub> SourceElement<sub>e</sub>,
Program<sub>e</sub>
                                                 ::=
                                                          SourceElements_e
Program
                                                 ::=
```

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```
Punctuator
                                                                                 / | + | : | ; | = | .
                                            Keyword
                                                                        ::=
                                                                                 return | function | if | else
                                           ExpressionPrefix
                                                                        ::=
                                                                                  = | / | + | return
                                           DeclarationPrefix
                                                                        ::=
                                                                                 x | /x / | else | ;
                                                                                         /x/\cdot \mathtt{read}(s,\ /x/,\ b)
read(/\cdot x \cdot /\cdot s, \epsilon, b)
read(/\cdot x \cdot /\cdot s, p \cdot p', b)
                                                                                         /x/\cdot \mathtt{read}(s, p \cdot p' \cdot /x/, b)
                                                                                             if p' \in Punctuator or Keyword
read(/\cdot x \cdot /\cdot s, p \cdot if \cdot (p'), b)
                                                                                         /x/\cdot \mathtt{read}(s,\ p\cdot \mathtt{if}\cdot (p')\cdot /x/,\ b)
read(/\cdot x \cdot /\cdot s, p \cdot p' \cdot function \cdot x \cdot (q) \cdot \{q'\}, b)
                                                                                         /x/\cdot \mathtt{read}(s,\ p\cdot p'\cdot \mathtt{function}\cdot \mathtt{x}\cdot (q)\cdot \{q'\}\cdot /x/,\ b)
                                                                                             if p' \in DeclarationPrefix
read(/\cdot x \cdot /\cdot s, p \cdot \{q\}^l, b)
                                                                                         /x/\cdot \mathtt{read}(s, p \cdot \{q\}^l \cdot /x/, b)
                                                                                            where true = isBlockPrefix(p, b, l)
read(/\cdot s, p \cdot x, b)
                                                                                         /\cdot \mathtt{read}(s,\ p\cdot x\cdot/,\ b)
read(/\cdot s, p \cdot /x/, b)
                                                                                         /\cdot \mathtt{read}(s, p \cdot /x/\cdot /, b)
read(/\cdot s, p \cdot (p'), b)
                                                                                          /\cdot \mathtt{read}(s, p \cdot (p') \cdot /, b)
read(/\cdot s, p \cdot p' \cdot function \cdot x \cdot (q) \cdot \{q'\}, b)
                                                                                         /\cdot \mathtt{read}(s,\ p\cdot p'\cdot \mathtt{function}\cdot \mathtt{x}\cdot (q)\cdot \{q'\}\cdot /,\ b)
                                                                                             if p' \in ExpressionPrefix
read(/\cdot s, p \cdot \{q'\}^l, b)
                                                                                          /\cdot \mathtt{read}(s,\ p\cdot \{q'\}^l\cdot /,\ b)
                                                                                             where false = isBlockPrefix(p, b, l)
read((\cdot s \cdot) \cdot s', p, b)
                                                                                         (t) \cdot \text{read}(s', p \cdot (t), b)
   where s contains no unmatched )
                                                                                             where t = read(s, \epsilon, false)
read(\{^l \cdot s \cdot \} \cdot s', p, b)
                                                                                         \{t\}^l \cdot \operatorname{read}(s', p \cdot \{t\}^l, b)
                                                                                         \textit{where } t = \mathtt{read}(s, \; \epsilon, \; \mathtt{isBlockPrefix}(p, \; b, \; l))
   where s contains no unmatched }
read(x \cdot s, p, b)
                                                                                         x \cdot \text{read}(s, p \cdot x, b)
\operatorname{read}(\epsilon, p, b)
                                           isBlockPrefix(\epsilon, false, l)
                                                                                                   =
                                                                                                         false
                                                                                                         false
                                          isBlockPrefix(p \cdot /, b, l)
                                                                                                   =
                                           isBlockPrefix(p \cdot +, b, l)
                                                                                                         false
                                          {\tt isBlockPrefix}(p\cdot:,\ b,\ l)
                                                                                                   _
                                                                                                          h
                                          isBlockPrefix(p \cdot return^l, b, l')
                                                                                                                    if l \neq l'
                                                                                                   =
                                                                                                         true
                                           isBlockPrefix(p \cdot return^l, b, l')
                                                                                                                    if l = l'
                                                                                                         false
                                                                                                   =
                                           isBlockPrefix(p, b, l)
                                                                                                          true
```

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#### 4. Enforestation

The core algorithm introduced by Honu is called *enforestation* which is basically responsible for expanding macros and building a partial syntax tree with enough structure to match on parse classes. Sweet.js implements this algorithm mostly as described with some additions to provide infix macros and invoke pattern classes described below.

### 4.1 Infix Macros

The macros we have described so far must all be prefixed by the macro identifier and syntax after the macro name is matched. This is sufficient for many kinds of macros but some syntax forms require the macro identifier to sit between patterns.

Honu addresses this need in a limited way by providing a way to define new binary and unary operators which during expansion can manipulate their operators. However, those operators must be fully expanded and must match as an expression.

Sweet.js provides *infix macros* which allows a macro identifier to match syntax before it. For example, the following implements ES6-style arrow functions via infix macros:

```
macro (=>) {
    rule infix {
        ($params ...) | { $body ... }
    } => {
        function ($params ...) {
          $body ...
     }
    }
}
var id = (x) => { return x; }
```

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This is accomplished by simply providing the state of previously expanded syntax to macro transformers. Macros may then consume from either ends as needed, yielding new previous and subsequent syntax. At first glance, this can appear brittle:

```
var foo = bar(x) => { return x; }
```

We've juxtaposed the => macro next to a function call, which we did not intend to be valid syntax. A naive expansion results in unparsable code:

```
var foo = bar function(x) { return x; }
```

In more subtle cases, a naive expansion can result in parsable code with incorrect semantics. [Example needed?] To preserve the integrity of previously expanded syntax, we verify that an infix macro only matches previous syntax on boundaries delimited by the partial syntax tree we've built. The syntax tree would show bar(x) as a complete function call term. Consuming the parentheses would result in a split term and is disallowed, failing the rule. In practice, this has proven to be an intuitive restriction. [Elaborate?]

The primary limitation of infix macros is they do not obey precedence and associativity. They stand as a complement to Honu operators, not as a replacement, for when an infix form does not adhere to operator semantics, much like the => macro. Its left-hand-side and right-hand-side are not arbitrary expressions but must match a specific form. Additionally, it would need a precedence of infinity so as to always bind tighter than other operators.

#### 4.2 Invoke and Pattern Classes

[Something about default pattern classes and ':expr'...]

Pattern classes are extensible via the invoke class which is parameterized by a macro name.

```
macro color {
```

```
rule { red } => { red }
rule { green } => { green }
rule { blue } => { blue }
}
macro colors_options {
rule { ($opt:invoke(color) ...) } => { ... }
}
```

The macro is essentially inserted into the token stream. If the expansion succeeds, the result will be loaded into the pattern variable, otherwise the rule will fail. We've added sugar so that any non-primitive pattern classes are interpretted as invoke parameterized by the custom class. We've also added identity rules to shorten definitions of simple custom classes.

```
macro color {
  rule { red }
  rule { green }
  rule { blue }
}
macro colors_options {
  rule { ($opt:color (,) ...) } => { ... }
}
```

These macros may return an optional pattern environment which will be scoped and loaded into the invoking macro's pattern environment. This lets us define Honu-style pattern classes as simple macro-generating macros.

```
macro color {
    ...
}
macro number {
    ...
}
// 'pattern' is just a macro-generating macro
pattern color_value { $color:color $num:number }

macro color_options {
    rule { ($opt:color_value (,) ...) } => {
        var cols = [$opt$color (,) ...];
        var nums = [$opt$num (,) ...];
    }
}
...?
```

# 5. Hygiene

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Mostly straightforward implementation from scheme with some details to handle var.

# 6. Implementation

Sweet.js is written in JavaScript and runs in the major JS environments (i.e. the brower and node.js). This is in contrast

to Honu which translates its code to Racket code and reuses the hygienic expansion machinery already built in Racket. While this simplifies the implementation of Honu it also requires an installation of Racket which in some cases is not feasible (e.g. sweet.js is able to run in mobile device browsers).

# 7. Related Work

- Scheme/Racket
- Honu
- Template Haskell
- Nemerle
- Scala
- Closure

# 8. Conclusion

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# A. Read Proof

Theorem 2 (Read Program).

 $\forall s.s \in Program_e \Leftrightarrow read(s, \epsilon, b) \in Program'_e$ 

*Proof.* For the if direction, there are two cases:

- $s \in Program_e ::= \epsilon$ . The result is immediate.
- $s \in Program_e ::= SourceElements_e$  this holds by Lemma 1.

A similar argument holds for the only if direction.

# Lemma 1 (Read SourceElements).

 $\forall s.s \in SourceElements_e \Leftrightarrow read(s, p, b) \in SourceElements'_e$ 

*Proof.* For the if direction, there are two cases:

- $s \in SourceElements_e ::= SourceElement_e$ . This holds by Lemma 2.
- $s \in SourceElements_{e \ e'} ::= SourceElements_{e} SourceElement_{e'}$ . We have  $s = s' \cdot s''$  where  $s' \in SourceElements_{e}$  and  $s'' \in SourceElement_{e'}$ .

$$\begin{array}{lll} t & = & \mathtt{read}(s' \cdot s'', \ p, \ b) \\ & = & \mathtt{read}(s', \ p, \ b) \cdot \mathtt{read}(s'', \ p \cdot \mathtt{read}(s', \ p, \ b), \ b) \end{array}$$

(TODO: need to say something about reading the prefix) By induction  $\operatorname{read}(s', p, b) \in \mathit{SourceElements'}_e$  and by Lemma 2,  $\operatorname{read}(s'', p \cdot \operatorname{read}(s', p, b), b) \in \mathit{SourceElement'}_{e'}$ . Thus  $t \in \mathit{SourceElements'}_{e \in e'}$ .

The argument is similar for the only if direction.

### Lemma 2 (Read SourceElement).

 $\forall s.s \in SourceElement_e \Leftrightarrow read(s, p, b) \in SourceElement'_e$ 

*Proof.* For the if direction there are two cases:

- $s \in SourceElement_e ::= Statement_e$ . This holds by Lemma 4.
- $s \in SourceElement_e ::= FunctionDeclaration_e$ . This holds by Lemma 3.

### Lemma 3 (Read FunctionDeclaration).

 $\forall s.s \in \mathit{FunctionDeclaration}_e \ \Leftrightarrow \ \mathit{read}(s, \ p, \ b) \in \mathit{FunctionDeclaration'}_e$ 

*Proof.* For the if direction we only have a single case:

 $s \in FunctionDeclaration_{function x (x) \{e\}} ::= function x (x) \{SourceElements_e\}$ 

We have  $s = \text{function } \mathbf{x} \ (\mathbf{x}) \ \{s'\} \text{ where } s' \in SourceElements_e so:}$ 

 $t = \text{read}(\text{function x (x) } \{s'\}, p, b)$ = function x (x)  $\{t'\}$ 

where  $t' = \text{read}(s', \epsilon, true)$ . **TODO:** explain why **b** = **true**. Since by Lemma 1,  $t' \in SourceElements'_e$  we have  $t \in FunctionDeclaration'_{function x (x) \{e\}}$ .

#### Lemma 4 (Read Statement).

 $\forall s.s \in Statement_e \Leftrightarrow read(s, p, b) \in Statement'_e$ 

*Proof.* For the if direction we have several cases:

- $s \in Statement_e ::= Block_e$ . This holds by Lemma 8.
- $s \in \mathit{Statement}_e ::= \mathit{ExpressionStatement}_e.$  This holds by Lemma 10.
- $s \in Statement_e ::= IfStatement_e$ . This holds by Lemma 5.
- $s \in Statement_e ::= ReturnStatement_e$ . This holds by Lemma 7.
- $s \in \mathit{Statement}_e ::= \mathit{LabelledStatement}_e$ . This holds by Lemma 6.

Lemma 5 (Read IfStatement).

 $\forall s.s \in \mathit{IfStatement}_e \Leftrightarrow \mathit{read}(s, p, b) \in \mathit{IfStatement}'_e$ 

*Proof.* For the if direction we have:

 $s \in \mathit{IfStatement}_{\mathtt{if}\ (e)\ e'\ \mathtt{else}\ e''} ::=$  if  $(\mathit{AssignmentExpression}_e)\ \mathit{Statement}_{e'}\ \mathtt{else}\ \mathit{Statement}_{e''}$ 

We have  $s=\text{if}\cdot(s')\cdot s''\cdot \text{else}\cdot s'''$  where  $s'\in AssignmentExpression_e,\ s''\in Statement_{e''},\ \text{and}\ s'''\in Statement_{e''}.$ 

$$t = read(if \cdot (s') \cdot s'' \cdot else \cdot s''', p, b)$$
$$= if \cdot (t') \cdot t'' \cdot else \cdot t'''$$

where

$$\begin{array}{lcl} t' & = & \mathtt{read}(s',\,\epsilon,\,b) \\ t'' & = & \mathtt{read}(s'',\,p\cdot\mathtt{if}\cdot(t'),\,b) \\ t''' & = & \mathtt{read}(s''',\,p\cdot\mathtt{if}\cdot(t')\cdot t''\cdot\mathtt{else},\,b) \end{array}$$

By Lemma 11  $t' \in AssignmentExpression'_e$ . By Lemma 4,  $t'' \in Statement'_{e'}$  and  $t''' \in Statement'_{e''}$ . Thus  $t \in IfStatement'_{if}(e) e' else e''$ .

#### Lemma 6 (Read LabelledStatement).

 $\forall s.s \in \textit{LabelledStatement}_e \; \Leftrightarrow \; \textit{read}(s, \; p, \; b) \; \in \textit{LabelledStatement'}_e$ 

*Proof.* For the if direction we have a single case:  $s \in LabelledStatement_{\mathtt{x}:\ e} ::= \mathtt{x}: Statement_{e}.$  We have  $s = \mathtt{x} \cdot : \cdot s'$  where  $s' \in Statement_{e}$ . Then:

$$t = \text{read}(\mathbf{x} \cdot : \cdot s', p, b)$$
  
=  $\mathbf{x} \cdot : \cdot \text{read}(s', p \cdot \mathbf{x} \cdot :, b)$ 

By Lemma 4,  $\operatorname{read}(s', p \cdot \mathbf{x} \cdot :, b) \in \mathit{Statement'}_e$  so  $t \in \mathit{LabelledStatement'}_{\mathbf{x} : e}$ . TODO: need to take into account b and the prefix.

#### Lemma 7 (Read ReturnStatement).

 $\forall s.s \in \textit{ReturnStatement}_e \Leftrightarrow \textit{read}(s, p, b) \in \textit{ReturnStatement'}_e$ 

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```
read(/\cdot s, p \cdot x, b)
                                                                                               /\cdot \mathtt{read}(s, p \cdot x \cdot /, b)
read(/\cdot s, p \cdot /x/, b)
                                                                                               /\cdot \mathtt{read}(s, p \cdot /x/\cdot /, b)
read(/\cdot s, p \cdot function \cdot (q) \cdot \{q'\}, b)
                                                                                              /\cdot \mathtt{read}(s, p \cdot \mathtt{function} \cdot (q) \cdot \{q'\} \cdot /, b)
\texttt{read}(/\cdot s,\ p\cdot p'\cdot \texttt{function}\cdot \texttt{x}\cdot (q)\cdot \{q'\},\ b)
                                                                                                 /\cdot \mathtt{read}(s,\ p\cdot p'\cdot \mathtt{function}\cdot \mathtt{x}\cdot (q)\cdot \{q'\}\cdot /,\ b)
                                                                                                    if p' \in ExpressionPrefix
                                                                                                 /\cdot \operatorname{read}(s, p \cdot \{q'\}^l \cdot /, b)
read(/\cdot s, p \cdot \{q'\}^l, b)
                                                                                                    where false = isBlockPrefix(p, b, l)
\begin{split} & \mathtt{read}(/\cdot x \cdot / \cdot s, \, \epsilon, \, b) \\ & \mathtt{read}(/\cdot x \cdot / \cdot s, \, p \cdot p', \, b) \\ & \mathtt{read}(/\cdot x \cdot / \cdot s, \, p \cdot \mathtt{if} \cdot (p'), \, b) \end{split}
                                                                                                /x/\cdot \mathtt{read}(s,\ /x/,\ b)
                                                                                                /x/\cdot \mathtt{read}(s,\ p\cdot p'\cdot /x/,\ b) if p'\in Punctuator\ or\ Keyword
                                                                                                /x/\cdot \mathtt{read}(s,\ p\cdot \mathtt{if}\cdot (p')\cdot /x/,\ b)
\mathtt{read}(/\cdot x\cdot/\cdot s,\; p\cdot\mathtt{for}\cdot(p'),\; b)
                                                                                               /x/\cdot \mathtt{read}(s,\ p\cdot \mathtt{for}\cdot (p')\cdot /x/,\ b)
read(/\cdot x \cdot /\cdot s, p \cdot while \cdot (p'), b)
                                                                                        = /x/\cdot \mathtt{read}(s, p \cdot \mathtt{while} \cdot (p') \cdot /x/, b)
                                                                                        = /x/\cdot read(s, p \cdot with \cdot (p') \cdot /x/, b)
read(/\cdot x \cdot / \cdot s, p \cdot with \cdot (p'), b)
read(/\cdot x \cdot /\cdot s, p \cdot p' \cdot function \cdot x \cdot (q) \cdot \{q'\}, b)
                                                                                                /x/\cdot \text{read}(s, p \cdot p' \cdot \text{function} \cdot x \cdot (q) \cdot \{q'\} \cdot /x/, b)
                                                                                                    if p' \in DeclarationPrefix
read(/\cdot x \cdot /\cdot s, p \cdot \{q\}^l, b)
                                                                                                /x/\cdot \operatorname{read}(s, p \cdot \{q\}^l \cdot /x/, b)
                                                                                                    where true = isBlockPrefix(p, b, l)
read((\cdot s \cdot) \cdot s', p, b)
                                                                                                (t) \cdot \text{read}(s', p \cdot (t), b)
    where s contains no unmatched)
                                                                                                    where t = read(s, \epsilon, false)
\operatorname{read}(\{^l \cdot s \cdot \} \cdot s', p, b)
                                                                                                \{t\}^l \cdot \operatorname{read}(s', p \cdot \{t\}^l, b)
    where s contains no unmatched }
                                                                                                where t = read(s, \epsilon, isBlockPrefix(p, b, l))
read(x \cdot s, p, b)
                                                                                                x \cdot \text{read}(s, p \cdot x, b)
read(\epsilon, p, b)
                                                  isBlockPrefix(\epsilon, false, l)
                                                  {\tt isBlockPrefix}(p\cdot /,\ b,\ l)
                                                                                                                    false
                                                                                                              =
                                                  isBlockPrefix(p \cdot +, b, l)
                                                                                                              =
                                                                                                                      false
                                                  isBlockPrefix(p \cdot :, b, l)
                                                                                                              =
                                                                                                                      b
                                                  isBlockPrefix(p \cdot return^l, b, l')
                                                                                                             =
                                                                                                                     true
                                                                                                                                 if l \neq l'
                                                                                                                                 if l = l'
                                                  isBlockPrefix(p \cdot return^l, b, l')
                                                                                                                    false
                                                  {\tt isBlockPrefix}(p \cdot {\tt void}, \ b, \ l)
                                                                                                               = false
                                                  isBlockPrefix(p \cdot typeof, b, l)
                                                                                                                     false
                                                  isBlockPrefix(p \cdot in, b, l)
                                                                                                                     false
                                                  isBlockPrefix(p \cdot case, b, l)
                                                                                                                     false
                                                  isBlockPrefix(p \cdot delete, b, l)
                                                                                                                     false
                                                  isBlockPrefix(p, b, l)
                                                                                                                      true
```

*Proof.* To show the if direction there are two cases:

*Proof.* For the if direction we have:

```
• s \in ReturnStatement_{return}; ::= return ;. Since s \in Block_{\{e\}} ::= \{StatementList_e\} s = return; and read(s, p, q) = return \cdot; \in ReturnStatement'_{return}; we have our result directly. So s = \{s'\} where s' \in StatementList_e.

• s \in ReturnStatement_{return} e ::= return AssignmentExpression_e. We have s = return \cdot s' where s' \in AssignmentExpression_e. t = read(\{s'\}, p, b) Then:

t = read(return \cdot s', p, b) \qquad where \ t' = read(s', \epsilon, true). \text{ By Lemma 9, } t' \in statementList'_e \text{ so } t \in Block'_{\{e\}}.
```

By Lemma 11,  $\operatorname{read}(s', p \cdot \operatorname{return}, b) \in \operatorname{AssignmentExpressionLemma 9}$  (Read StatementList). thus  $t \in \operatorname{ReturnStatement'}_{\operatorname{return}} e$ .  $\forall s.s \in \operatorname{StatementList}_e \Leftrightarrow \operatorname{read}(s, p, b) \in \operatorname{StatementList'}_e$ 

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 $\square$  *Proof.* For the if direction we have two cases:

```
Lemma 8 (Read Block). \forall s.s \in Block_e \Leftrightarrow read(s, p, b) \in Block'_e
```

•  $s \in StatementList_e ::= Statement_e$ . This follows by Lemma 4.

•  $s \in StatementList_{e \ e'} ::= StatementList_e \ Statement_{e'}.$ So  $s = s' \cdot s''$  where  $s' \in StatementList_e$  and  $s'' \in Statement_{e'}.$  Then,

$$t = read(s' \cdot s'', p, b)$$
  
= read(s', p, b) \cdot read(s'', p \cdot read(s', p, b), b)

By induction  $\operatorname{read}(s', p, b) \in \operatorname{\it StatementList'}_e$  and by Lemma 4,  $\operatorname{read}(s'', p \cdot \operatorname{read}(s', p, b), b) \in \operatorname{\it Statement'}_{e'}$ . Thus,  $t \in \operatorname{\it StatementList'}_{e e'}$ .

# Lemma 10 (Read ExpressionStatement).

 $\forall s.s \in \textit{ExpressionStatement}_e \Leftrightarrow \textit{read}(s, p, b) \in \textit{ExpressionStatement'}_e$ 

*Proof.* For the if direction we have  $s \in ExpressionStatement_e ::= AssignmentExpression_e$ ; so  $s = s' \cdot$ ; where  $s' \in AssignmentExpression_e$ . Then:

$$\begin{array}{lll} t & = & \mathtt{read}(s' \cdot \texttt{;}, \ p, \ b) \\ & = & \mathtt{read}(s', \ p, \ b) \cdot \texttt{;} \end{array}$$

Since by Lemma 11,  $read(s', p, b) \in AssignmentExpression'_e$  we have  $t \in ExpressionStatement'_e$ .

# Lemma 11 (Read AssignmentExpression).

 $\forall s.s \in \textit{AssignmentExpression}_e \Leftrightarrow \textit{read}(s, \ p, \ b) \in \textit{AssignmentExpression'}_e$ 

*Proof.* For the if direction we have two cases:

- $s \in AssignmentExpression_e ::= BinaryExpression_e$ . This holds by Lemma 12.
- $s \in AssignmentExpression_{e=e'}$  by

 $CallExpression_e = AssignmentExpression_{e'}$ 

Then  $s = s' \cdot = \cdot s''$  where  $s' \in CallExpression_e$  and  $s'' \in AssignmentExpression_{e'}$ . Then:

$$\begin{array}{lll} t & = & \mathtt{read}(s' \cdot \texttt{=} \cdot s'', \ p, \ b) \\ & = & \mathtt{read}(s', \ p, \ b) \cdot \texttt{=} \cdot \mathtt{read}(s'', \ p \cdot \mathtt{read}(s', \ p, \ b) \cdot \texttt{=}, \ b) \end{array}$$

By Lemma 13,  $\operatorname{read}(s', p, b) \in \operatorname{CallExpression'}_e$  and by induction  $\operatorname{read}(s'', p \cdot \operatorname{read}(s', p, b) \cdot =, b) \in \operatorname{AssignmentExpression'}_{e'}$  so  $t \in \operatorname{AssignmentExpression'}_{e = e'}$ .

## Lemma 12 (Read BinaryExpression).

 $\forall s.s \in \mathit{BinaryExpression}_e \Leftrightarrow \mathit{read}(s, p, b) \in \mathit{BinaryExpression}_e$ 

*Proof.* To show the if direction we have three cases:

•  $s \in BinaryExpression_e ::= CallExpression_e$ . This holds by Lemma 13.

•  $s \in BinaryExpression_{e/e'}$  by

BinaryExpression<sub>e</sub> / BinaryExpression<sub>e</sub>,

We have  $s = s' \cdot / \cdot s''$  where  $s' \in BinaryExpression_e$  and  $s'' \in BinaryExpression_{e'}$ . Then:

$$t = read(s' \cdot / \cdot s'', p, b)$$
  
= read(s', p, b) \cdot / \cdot read(s'', p \cdot read(s', p, b) \cdot /, b)

**TODO:** since reasons. By induction  $read(s', p, b) \in BinaryExpression'_e$  and  $read(s'', p \cdot read(s', p, b) \cdot /, b) \in BinaryExpression'_{e'}$  thus  $t \in BinaryExpression'_{e'} \cdot e'$ .

•  $s \in BinaryExpression_{e+e'}$  by

BinaryExpression<sub>e</sub> + BinaryExpression<sub>e</sub>,

We have  $s = s' \cdot + \cdot s''$  where  $s' \in BinaryExpression_e$  and  $s'' \in BinaryExpression_{e'}$ . Then:

$$\begin{array}{lll} t & = & \mathtt{read}(s' \cdot + \cdot s'', \ p, \ b) \\ & = & \mathtt{read}(s', \ p, \ b) \cdot + \cdot \mathtt{read}(s'', \ p \cdot \mathtt{read}(s', \ p, \ b) \cdot +, \ b) \end{array}$$

**TODO:** since reasons. By induction  $read(s', p, b) \in BinaryExpression'_e$  and  $read(s'', p \cdot read(s', p, b) \cdot +, b) \in BinaryExpression'_{e'}$  thus  $t \in BinaryExpression'_{e + e'}$ .

Lemma 13 (Read CallExpression).

 $\forall s.s \in CallExpression_e \Leftrightarrow read(s, p, b) \in CallExpression'_e$ 

*Proof.* For the if direction we have three cases:

•  $s \in CallExpression_{e(e')}$  by

MemberExpression<sub>e</sub> (AssignmentExpression'<sub>e'</sub>)

We have  $s = s' \cdot (s'')$  where  $s' \in MemberExpression_e$  and  $s'' \in AssignmentExpression_{e'}$ . Then

$$\begin{array}{lll} t & = & \mathtt{read}(s' \cdot (s''), \; p, \; b) \\ & = & \mathtt{read}(s', \; p, \; b) \cdot \mathtt{read}((s''), \; p \cdot \mathtt{read}(s', \; p, \; b), \; b) \end{array}$$

By Lemma 14 we have  $\operatorname{read}(s', p, b) \in MemberExpression'_e$  and my Lemma 11 we have  $\operatorname{read}(s'', \epsilon, false) \in AssignmentExpression'_{e'}$  thus  $t \in CallExpression'_{e'}(e')$ .

•  $s \in CallExpression_{e.x} ::= CallExpression_e$  . x. Then  $s = s' \cdot ... \times where s' \in CallExpression_e$ . Then

$$\begin{array}{lll} t & = & \mathtt{read}(s' \cdot \ldots \mathtt{x}, \; p, \; b) \\ & = & \mathtt{read}(s', \; p, \; b) \cdot \ldots \mathtt{x} \end{array}$$

By induction  $\operatorname{read}(s', p, b) \in \operatorname{CallExpression'}_e$ . Thus  $t \in \operatorname{CallExpression'}_{e, \mathbf{x}}$ .

Lemma 14 (Read MemberExpression).

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 $\forall s.s \in \mathit{MemberExpression}_e \Leftrightarrow \mathit{read}(s, p, b) \in \mathit{MemberExpression}_e$ 

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*Proof.* For the if direction we have three cases:

- $s \in MemberExpression_e ::= PrimaryExpression_e$ . This follows from Lemma 15.
- $s \in MemberExpression_e ::= FunctionExpression_e$ . This follows from Lemma  $\ref{lem:eq:lem$
- $s \in MemberExpression_{e.x} ::= MemberExpression_e$  . x. We have  $s = s' \cdot .x$  where  $s \in MemberExpression_e$ . Then

$$t = read(s' \cdot ... x, p, b)$$
$$= read(s', p, b) \cdot ... x$$

By induction  $read(s', p, b) \in MemberExpression'_e$  thus  $t \in MemberExpression'_{e, \mathbf{x}}$ .

*Proof.* By cases of  $Expr_e$ :

• Case  $Expr_{e/e'} ::= Expr_e / Expr_{e'}$ . From this  $s = s' \cdot / \cdot s''$  where  $s' \in Expr_e$  and  $s'' \in Expr_{e'}$ . So

$$\begin{array}{lll} t &=& \mathtt{read}(s'\cdot /\cdot s'',\; p,\; b) \\ &=& \mathtt{read}(s',\; p,\; b) \cdot \mathtt{read}(/\cdot s'',\; p \cdot \mathtt{read}(s',\; p,\; b),\; b) \\ && (\mathtt{by}\; \mathtt{Lemma}\; 16\; \mathtt{since}\; s' \in \mathit{ReadUnit}) \end{array}$$

$$= \operatorname{read}(s', p, b) \cdot / \cdot \operatorname{read}(s'', p \cdot \operatorname{read}(s', p, b) \cdot /, b)$$
(since by Lemma 17,  $\operatorname{read}(s', p, b) \in \operatorname{DivPrefix}$ )

By induction  $\operatorname{read}(s', p, b) \in \operatorname{Expr'}_e$  and  $\operatorname{read}(s'', p \cdot \operatorname{read}(s', p, b) \cdot /, b) \in \operatorname{Expr'}_{e'}$  so  $t \in \operatorname{Expr'}_{e' \cdot e'}$ .

Lemma 15 (Read PrimaryExpression).

 $\forall s, p \in RePrefix.$ 

 $s \in PrimaryExpression_e \Leftrightarrow read(s, p, b) \in PrimaryExpression'_e$ 

*Proof.* For the if direction we have several cases:

- $s \in PrimaryExpression_x ::= x$ . Then s = x and  $read(x, p, b) \in PrimaryExpression'_x$  directly.
- $s \in PrimaryExpression_{/x/} ::= / \cdot x \cdot /.$  Then  $s = / \cdot x \cdot /.$  and  $read(/ \cdot x \cdot /, p, b) = /x/ \in PrimaryExpression'_{/x/}$  since  $p \in RePrefix$ .
- $s \in PrimaryExpression_{\{\mathtt{x}\,:\,e\}} ::= \{\mathtt{x}\,:\,AssignmentExpression_e\}.$  Then  $s = \mathtt{x}\,\cdot\,:\,\cdot\,\{s'\}$  where  $s' \in AssignmentExpression_e.$  Then:

$$\begin{array}{lll} t & = & \operatorname{read}(\mathbf{x} \cdot \colon \cdot \: \{s'\}, \: p, \: b) \\ & = & \mathbf{x} \cdot \colon \cdot \: \{t'\} \end{array}$$

where  $t' = \text{read}(s', \epsilon, false)$ . By Lemma 11,  $t' \in AssignmentExpression'_{e}$  and thus  $t \in PrimaryExpression'_{\{x:e\}}$ .

•  $s \in PrimaryExpression_{(e)} ::= (AssignmentExpression_e)$ . Then s = (s') where  $s' \in AssignmentExpression_e$ . So,

$$\begin{array}{ll} t & = & \mathtt{read}(\texttt{(}s'\texttt{)},\ p,\ b) \\ & = & (t'\texttt{)} \end{array}$$

where  $t' = \operatorname{read}(s', \epsilon, false)$ . By Lemma 11  $t' \in AssignmentExpression'_{e}$ . So,  $t \in PrimaryExpression'_{(e)}$ .

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Lemma 16 (Reading a Unit).

 $s \in ReadUnit \Rightarrow$ 

 $read(s \cdot s', p, b) = read(s, p, b) \cdot read(s', p \cdot read(s, p, b), b)$ 

Lemma 17 (Reading the end of an expr).

$$s \in Expr_e \Rightarrow p \cdot read(s, p, b) \in DivPrefix$$

**Lemma 18.**  $s \in Expr_e \Rightarrow s \in ReadUnit$ 

Lemma 19 (Read Expr).

$$\forall s, p. p \notin DivPrefix$$
  
 $s \in Expr_e \Leftrightarrow read(s, p, b) \in Expr'_e$