



# Machine Learning #12

## ▼ 1. What is prior probability? Give an example.

Prior probability, in the context of Bayesian probability theory, **is the initial belief or probability assigned to an event before new evidence or data is taken into account.** It represents the subjective degree of belief in the occurrence of an event based on prior experience, knowledge, or other relevant information.

For example, let's say a doctor is trying to determine the probability that a patient has a certain disease based on the patient's symptoms. The doctor may assign an initial prior probability based on their prior experience with similar cases or knowledge about the prevalence of the disease in the population. This prior probability can be updated based on new evidence or test results to arrive at a more accurate estimate of the probability of the disease.

## ▼ 2. What is posterior probability? Give an example.

**Posterior probability is the probability of an event occurring based on the evidence or new information available after taking into account prior beliefs or assumptions. It is calculated using Bayes' theorem.**

For example, let's say a doctor wants to determine the probability of a patient having a particular disease. Based on previous research, the doctor has a prior belief that the disease occurs in 1 out of every 1000 patients. The doctor then conducts some tests on the patient and gets some new information, such as the patient's age, gender, and symptoms. Using this information, the doctor updates the prior belief and calculates the posterior probability of the patient having the disease.

## ▼ 3. What is likelihood probability? Give an example.

In Bayesian statistics, likelihood probability refers to **the probability of observing the data given a particular value of the parameter. It is the probability of the data conditioned on the parameter**, and it is often used in Bayesian inference to update the prior probability distribution of a parameter based on the observed data.

For example, suppose we have a coin that we believe is biased towards heads, and we want to estimate the probability of heads, denoted by  $p$ . We flip the coin 10 times and observe 7 heads and 3 tails. The likelihood function is given by the probability of observing 7 heads and 3 tails given a value of  $p$ :

$$L(p) = P(X = 7 \mid p) * P(X = 3 \mid 1 - p)$$

where  $X$  is the number of heads in 10 flips of the coin, and  $P(X = k \mid p)$  is the binomial probability mass function.

By using Bayes' theorem, we can update our prior belief about  $p$  based on the observed data to obtain the posterior probability distribution of  $p$ . The posterior distribution is proportional to the product of the prior distribution and the likelihood function:

$$P(p \mid X) \propto P(p) * L(p)$$

where  $P(p)$  is the prior probability distribution of  $p$  and  $P(p \mid X)$  is the posterior distribution of  $p$  given the observed data  $X$ .

#### ▼ 4. What is Naïve Bayes classifier? Why is it named so?

*Naïve Bayes classifier is a probabilistic algorithm used in machine learning for classification problems. It is based on the Bayes theorem of probability and is called "naïve" because it makes the assumption that the features (or variables) used for classification are independent of each other, which is a simplified assumption that may not be true in all cases.*

The Naïve Bayes classifier calculates the probability of each class (or category) for a given set of features, and selects the class with the highest probability as the predicted class. It requires a training dataset to learn the probability distribution of the features for each class, and uses this information to make predictions on new data.

Despite its simplistic assumptions, Naïve Bayes classifier is known to perform well in many real-world applications, especially in text classification tasks such as spam filtering and sentiment analysis. It is easy to implement and computationally efficient, making it a popular choice for many machine learning tasks.

#### ▼ 5. What is optimal Bayes classifier?

*The optimal Bayes classifier is a classification model that uses the Bayes theorem to classify data into different categories. It is considered optimal because it provides the highest accuracy rate among all classification algorithms.*

The optimal Bayes classifier is based on the Bayes theorem, which states that the probability of a hypothesis  $H$  given the evidence  $E$  is proportional to the product of the prior probability of  $H$  and the likelihood of  $E$  given  $H$ , divided by the marginal likelihood of  $E$ .

In the context of classification, the optimal Bayes classifier assigns a class label to a given input based on the class that has the highest posterior probability given the input features. This is done by calculating the posterior probability of each class for a given input, and then selecting the class with the highest probability as the predicted class.

The optimal Bayes classifier is sometimes also referred to as the Bayes optimal classifier, or the Bayes optimal decision rule.

#### ▼ 6. Write any two features of Bayesian learning methods.

Two features of Bayesian learning methods are:

1. Bayesian methods allow for the incorporation of prior knowledge or assumptions about the data, which can be useful in situations where the amount of available data is limited.
2. Bayesian methods provide a framework for handling uncertainty in the model parameters and predictions, which can be important in real-world applications where there is always some degree of uncertainty or noise in the data.

#### ▼ 7. Define the concept of consistent learners.

In machine learning, **a consistent learner is a model or algorithm that can perfectly fit the training data when given an infinite amount of it.** In other words, a consistent learner is guaranteed to converge to the true target function as the number of training examples increases without limit. This means that as **we feed more and more data to the model, its output becomes more and more accurate, and eventually, it will converge to the correct output.** The idea of consistency is important because it ensures that the model will eventually learn the true relationship between the inputs and the outputs and generalize well to unseen data.

#### ▼ 8. Write any two strengths of Bayes classifier.

Here are two strengths of Bayes classifier:

1. Naïve Bayes classifier is **very efficient** and **requires very little training data** compared to other classification algorithms.
2. It is **robust to irrelevant features**, meaning that it can still provide accurate predictions even if some of the input features are not relevant to the output.

## ▼ 9. Write any two weaknesses of Bayes classifier.

Here are two weaknesses of the Bayes classifier:

1. **Independence assumption:** *Naïve Bayes classifier assumes that the features are conditionally independent given the class, which may not hold true in real-world scenarios.* Violation of this assumption may lead to poor classification performance.
2. **Lack of expressiveness:** The model assumes a simple probabilistic model and therefore may not be expressive enough to capture complex relationships among features. As a result, *it may not perform well in scenarios where the data has complex dependencies.*

## ▼ 10. Explain how Naïve Bayes classifier is used for

1. Text classification
2. Spam filtering
3. Market sentiment analysis

Naïve Bayes classifier is a popular classification algorithm that works on the Bayesian theorem. It is used in various applications, including text classification, spam filtering, and market sentiment analysis.

1. **Text classification:** Naïve Bayes classifier is used in text classification to classify the text documents into different categories, such as news, sports, finance, politics, and so on. ***The classifier is trained on a set of labeled documents, and then it can predict the category of new, unseen documents based on the probability of the words in the document belonging to each category.*** This approach is widely used in email spam filtering, where the classifier can learn to recognize spam messages based on the words and phrases commonly used in such messages.
2. **Spam filtering:** Naïve Bayes classifier is a popular approach for spam filtering, which involves identifying unwanted or unsolicited messages. ***The classifier can be trained on a set of labeled messages, where spam and non-spam messages are labeled as positive and negative examples, respectively. The classifier then uses the probability of the words in the messages to predict whether a new message is spam or not.*** Naïve Bayes classifiers are fast and can handle large datasets, making them a popular choice for spam filtering.
3. **Market sentiment analysis:** Naïve Bayes classifier can also be used for market sentiment analysis, which involves predicting the sentiment of investors and traders in financial markets. ***The classifier can be trained on a set of labeled news articles, social media posts, and other sources of data, where the sentiment is labeled as positive, negative, or neutral. The classifier can then use the probability of the words and phrases in the data to predict the sentiment of the market.*** This approach is useful for investors and traders who want to make informed decisions based on the sentiment of the market.