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from random import randint
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def swap(arr, i, j):
  arr[i], arr[j] = arr[j], arr[i]
def partition(arr, lo, hi):
  pivot = randint(lo, hi)
  # swap last element in pivot element
  swap(arr, pivot, hi)
  i = lo
  # set j pointer to the last end of the scan
  j = hi - 1
  # when i pointer has greater index it has crossed the border of the j pointer
  while i <= j:
    # if i and j ptrs are < and >= to pivot swap then inc & dec
    if arr[i] >= arr[hi] > arr[j]:
       swap(arr, i, j)
      i += 1
      j -= 1
    # check if either of the two needs to be incremented or decremented or both
    elif arr[i] >= arr[hi] <= arr[j]:
      j -= 1
    elif arr[j] < arr[hi] > arr[i]:
      i += 1
    else:
      i += 1
      j -= 1
```

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# swap pivot element located in [hi] and swap with i
  swap(arr, i, hi)
  # return new position of fixed pivot element
  return i
def quicksort(arr,lo,hi):
  # if lo is greater than or equal hi, means array length reached 1
  if lo < hi:
    fixed = partition(arr, lo, hi)
    # process sorted left side of pivot
    quicksort(arr, lo, fixed - 1)
    # process sorted right side of pivot
    quicksort(arr, fixed + 1, hi)
def mergesort(arr, lo, hi):
  # lo and hi indeces at starting would be 0 to 9
  # if we had an array of 9 elements mid index would be
  \# (0 + 9) / 2 = 4 then plus 1, which is 5
  # this means we want to recursively pass the left most
  # elements of the array until the array becomes a single value
  # left most indeces in this first recursive iteration would be [0] to [4]
  # since 0 < 5 is exclusive we only get indeces from 0 to 4
  mid = int((lo + hi) / 2) + 1
  # range value or base case is when the array length reaches 1
  # because lo will be 0 and hi will be 0
  if lo >= hi:
```

```
# assign left most elements in mid in temp array, 0 < mid
  t_left = arr[:mid]
  # assign right most elements in mid in temp array, mid < length
  t right = arr[mid:]
  # process the left side first, pass in the arr that is already halved such that in recursive calls it gets
smaller everytime
  # in first recursive iteration arr would have length 9 and
  # lo and hi indeces will be 0 and 9, because of mid index 5
  # calculated from int((0 + 9) / 2) + 1, t_left will be of length
  # 5, since 0 to 5 exclusively will be the only elements it will take
  # and will only have indeces 0, 1, 2, 3, 4
  # in second recursive iteration arr would have length 5 and
  # lo and hi indeces will be 0 and 4, because of mid index 3
  # calculated from int((0 + 4) / 2) + 1, t_left will be of length
  #3, since 0 to 3 exclusively will be the only elements it will take
  # and will only have indeces 0, 1, 2
  # in third recursive iteration arr would have length 3 and
  # lo and hi indeces will be 0 and 2, because of mid index 2
  # calculated from int((0 + 2) / 2) + 1, t left will be of length
  # 1, since 0 to 2 exclusively will be the only elements it will take
  # and will only have indeces 0, 1
  # in fourth recursive iteration arr would have length 2 and
  # lo and hi indeces will be 0 and 1, because of mid index 1
  # calculated from int((0 + 1) / 2) + 1, t_left will be of length
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1, since 0 to 1 exclusively will be the only elements it will take

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# and will only have indeces 0
  mergesort(t_left, lo, mid - 1)
  # process right side second, pass the new lo and hi of each array
  mergesort(t_right, lo, hi - mid)
  i = j = k = 0
  while i != mid and j != (hi - mid + 1):
    # arr is only modified for the specific temp array passed
    if t_left[i] > t_right[j]:
       # note that real arr will not be modified until last recursive call has been executed
       arr[k] = t_right[j]
      j += 1
    else:
      arr[k] = t_left[i]
      i += 1
    k += 1
  # if j or i pointers have still elements left append those remaining elements
  if j != hi - mid + 1:
    for j in range(j, hi - mid + 1):
       arr[k] = t_right[j]
      k += 1
  else:
    for i in range(i, mid):
       arr[k] = t_left[i]
       k += 1
def bubblesort(arr):
  for i in range(len(arr) - 1, 0, -1):
    for j in range(i):
       if(arr[j] > arr[j + 1]):
```