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Hogeschool Rotterdam Rotterdam, Netherlands



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#### Lecture topics

- Beyond type equality
- Defining our own subtypes
- Lists and state machines



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# Beyond type equality



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#### Introduction

- $\bullet$  In the previous lecture we have seen that Java/C# have a static type system
- Programs that make no sense are outright refused by the compiler
- "Make no sense" means calling methods or making assignments with the wrong types



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So far, we defined a type to be wrong if it is not exactly the same as what we expected.

If we expected an int, but got a Person, then clearly something was off and we expect<sup>a</sup> a compiler error.

<sup>a</sup>welcome, actually



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#### Wrong types

The two most important typing rules for these violations are those of variable assignment and method call.



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When assigning a variable, we expect the type of the expression and that of the variable to be exactly the same: T=D[x]

$$\frac{\langle \mathbf{e}, D \rangle \to \langle T, D \rangle \wedge \ T = D[x]}{\langle \mathbf{x} = \mathbf{e}, D \rangle \to \langle D[\mathtt{void}], D \rangle}$$



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When calling a method, we expect the type of the parameters and those of the arguments to be exactly the same:  $P_i = P_i'$ 

$$\frac{\langle \mathtt{c}, D \rangle \to \langle \mathtt{C}, D \rangle \wedge \ \langle \mathtt{m}, C \rangle \to \langle (\mathtt{P}_1 \times \mathtt{P}_2 \times \dots \times \mathtt{P}_n \to \mathtt{R}), C \rangle \wedge \ \langle \mathtt{p}_i, D \rangle \to \langle \mathtt{P}_i', D \rangle \wedge \ \mathtt{P}_i = \mathtt{P}_i'}{\langle (\mathtt{c}.\mathtt{m}(...\mathtt{p}_i..)), D \rangle \to \langle \mathtt{R}, D \rangle}$$



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For example, the program below violates typing rules:

```
int x = 5;
x = "uh!?";
```



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For example, the program below violates typing rules:

```
class Counter {
  private int cnt;
  public Counter() {
    this.cnt = 0;
  }
  public void Incr(int diff) {
    this.cnt = (this.cnt + diff);
  }
}
Counter c = new Counter();
c.Incr(c);
```



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int x = 5.5; makes no sense

This will also give a compiler error.



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Conclusion

#### Always wrong?

- What about a similar expression, such as float x = 10;?
- x is a float
- 10 is an int
- float  $\neq$  int, so we should get a type error.



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float x = 10; makes sense, even though it violates the strictest typing rules described so far.

Floating point numbers "contain" integers, so converting the integer  $10\ \text{to}\ 10.0$  loses no information



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#### Subtyping

This means that the typing rules as seen so far are **too restrictive**: we should be able to accept an assignment from a more specific data type (such as int) to a less specific data type (such as float).



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Consider any two data types, T and S

We say that S <: T, read "S is a subtype of T", to mean that any value of type S can be safely used where a value of type T is expected.

We also say that, when S <: T, T generalizes S.



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Conclusion

#### More and less specific data types

For example, int <: float, because any value of type int can be safely used where a value of type float is expected (as the conversion loses no data, and thus can be inserted by the compiler itself).



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Conclusion

#### More and less specific data types

We can now amend many of our typing rules: instead of type equality, we can use subtyping to preserve safety, but achieve more flexibility.



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Conclusion

When assigning a variable, we expect the type of the expression **to be a subtype** of that of the variable.

$$\frac{\langle \mathbf{e}, D \rangle \to \langle T, D \rangle \wedge \ T <: D[x]}{\langle \mathbf{x} = \mathbf{e}, D \rangle \to \langle D[\mathtt{void}], D \rangle}$$



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When calling a method, we expect the type of the parameters **to be subtypes** of the types of the arguments.

$$\frac{\langle \mathtt{c}, D \rangle \to \langle \mathtt{C}, D \rangle \wedge \ \langle \mathtt{m}, C \rangle \to \langle (\mathtt{P}_1 \times \mathtt{P}_2 \times \dots \times \mathtt{P}_n \to \mathtt{R}), C \rangle \wedge \ \langle \mathtt{p}_1, D \rangle \to \langle \mathtt{P}_i', D \rangle \wedge \ \mathtt{P}_i :> \mathtt{P}_i'}{\langle (\mathtt{c}.\mathtt{m}(..\mathtt{p}_i..)), D \rangle \to \langle \mathtt{R}, D \rangle}$$



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# **Defining our own subtypes**



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Remember that we can define our own classes to extend the data types of the language when they are insufficient for our domain.

We can make use of subtyping for those custom classes.

This makes it possible to capture **generalization relationships** between our own data types.



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Can you think of a few examples of classes that generalize each other?



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Can you think of a few examples of classes that generalize each other?

Person generalizes Student.

LightEmitter generalizes Lamp.

Animal generalizes Dog.



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Which generalizes which?

Mercedes vs CarBrand?



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Which generalizes which?

Mercedes vs CarBrand? CarBrand :> Mercedes



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LivingSpace vs Apartment?



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Mercedes vs CarBrand? CarBrand :> Mercedes

LivingSpace vs Apartment? LivingSpace :> Apartment

Cat vs Bird? Neither.



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Cat vs Bird? Neither.

Person vs Employee?



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Cat vs Bird? Neither.

Person vs Employee? Person :> Employee



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Cat vs Bird? Neither.

Person vs Employee? Person :> Employee

Student vs Person?



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```
Which generalizes which?
```

Mercedes vs CarBrand? CarBrand :> Mercedes

LivingSpace vs Apartment? LivingSpace :> Apartment

Cat vs Bird? Neither.

Person vs Employee? Person :> Employee

Student vs Person? Person :> Student.



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Cat vs Bird? Neither.

Person vs Employee? Person :> Employee

Student vs Person? Person :> Student.

Student vs Employee?



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Cat vs Bird? Neither.

Person vs Employee? Person :> Employee

Student vs Person? Person :> Student.

Student vs Employee? Neither.



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Cat vs Bird? Neither.

Person vs Employee? Person :> Employee

Student vs Person? Person :> Student.

Student vs Employee? Neither.



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Consider, in particular, the following relationships:

Person :> Employee

Person :> Student



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Conclusion

Consider, in particular, the following relationships:

Person :> Employee

Person :> Student

We could imagine that Person, Employee, and Student are all classes

Moreover, Person and Employee are somehow related

Similarly, Person and Student are related in the same way



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#### Class inheritance

- This relationships is modeled, in Java/C#, with class inheritance.
- A class such as Employee will therefore inherit from class Person
- This means that Employee will automatically have all fields and methods of Person



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When we use inheritance, for example of Person from Employee, then the language automatically infers that Person :> Employee

This means therefore that anywhere in the language (a variable, a parameter, etc.) where we expected a Person, we can give an Employee.

This provides polymorphism, as the same data type (in this case Person) can have multiple shapes: a Person, an Employee, a Student, etc.



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Inheritance requires very little code: in C#, a colon (:) suffices with the name of the inherited class next to that of the defined class.

In Java, we use the keyword extends instead of the colon.

It is possible to inherit at most one class.



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#### The program below works: why?

```
class A {
  public int M(int x) {
    return (x + x);
  }
}
class B : A {
  public int N(int y) {
    return (y * 10);
  }
}
A b = new B();
Console.WriteLine(b.M(5));
```



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The program below works: why?

```
class A {
  public int M(int x) {
    return (x + x);
class B : A f
  public int N(int v) {
    return (v * 10);
A b = new B():
Console.WriteLine(b.M(5));
```

Because the declaration of b specifies A as the type, but whenever we expect an A we can use a B thanks to inheritance.



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#### Which in Java then becomes:

```
class A {
  public int M(int x) {
    return (x + x);
  }
}
class B extends A {
  public int N(int y) {
    return (y * 10);
  }
}
A b = new B();
System.out.println(b.M(5));
```



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```
class A {
  public A() {
  public int M(int x) {
    return (x + x):
class B : A {
  public B() {
  public int N(int y) {
    return (y * 10);
A b = new B();
Console.WriteLine(b.M(5));
```

```
Declarations:
```



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```
class A {
   public A() {
   }
   public int M(int x) {
      return (x + x);
   }
} class B : A {
   public B() {
   }
   public int N(int y) {
      return (y * 10);
   }
} A b = new B();
Console.WriteLine(b.M(5));
```

```
 \begin{array}{c} \text{Declarations:} & \begin{array}{c} PC \\ \hline 7 \\ \end{array} \\ \text{Classes:} & \begin{array}{c} A \\ A = A \rightarrow A \\ M = (A \times \text{int}) \rightarrow \text{int} \end{array}
```



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```
class A {
  public A() {
  public int M(int x) {
    return (x + x):
class B : A {
  public B() {
  public int N(int y) {
    return (y * 10);
A b = new B();
Console.WriteLine(b.M(5));
```

```
Declarations:
```

А	В
$\begin{array}{c} A{=}A \to A \\ M{=}(A{\times}int) \to int \end{array}$	$\begin{array}{c} B {=} B \to B \\ M {=} (A {\times} int) \to int \\ N {=} (B {\times} int) \to int \end{array}$



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```
class A {
   public A() {
   }
   public int M(int x) {
      return (x + x);
   }
}
class B: A {
   public B() {
   }
   public int N(int y) {
      return (y * 10);
   }
}
A b = new B();
Console.WriteLine(b.M(5));
```

```
Declarations: PC b 16 A
```

Α	В
$\begin{array}{c} A{=}A \to A \\ M{=}(A{\times}int) \to int \end{array}$	$\begin{array}{c} B {=} B \to B \\ M {=} (A {\times} int) \to int \\ N {=} (B {\times} int) \to int \end{array}$



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```
Conclusion
```

```
class A {
  public A() {
  public int M(int x) {
    return (x + x):
class B : A {
  public B() {
  public int N(int y) {
    return (y * 10);
A b = new B();
Console.WriteLine(b.M(5));
```

Declarations:	b		PC	ret	$arg_1$	this
Deciarations.	Α		16	null	int	Α
						Ъ

A	В
$\begin{array}{c} A{=}A \to A \\ M{=}(A{\times}int) \to int \end{array}$	$\begin{array}{c} B {=} B \to B \\ M {=} (A {\times} int) \to int \\ N {=} (B {\times} int) \to int \end{array}$



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```
class A {
  public A() {
  public int M(int x) {
    return (x + x):
class B : A {
  public B() {
  public int N(int y) {
    return (y * 10);
A b = new B():
Console.WriteLine(b.M(5));
```

 $N=(B\times int) \rightarrow int$ 

Declarati	one.						01		
Declarations:		Α		16	int	t	int	Α	
	А							В	
Classes:	$A=A \rightarrow A$						_	$B \rightarrow B$ $\langle int \rangle \rightarrow$	int
	$M=(A \times int) \rightarrow int$					M (D)			

PC ret



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```
Conclusion
```

```
class A {
  public A() {
  public int M(int x) {
    return (x + x):
class B : A {
  public B() {
  public int N(int y) {
    return (y * 10);
A b = new B();
Console.WriteLine(b.M(5));
```

```
Declarations:
```

A	В
$\begin{array}{c} A{=}A \to A \\ M{=}(A{\times}int) \to int \end{array}$	$\begin{array}{c} B {=} B \to B \\ M {=} (A {\times} int) \to int \\ N {=} (B {\times} int) \to int \end{array}$



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```
class A {
  public A() {
  }
  public int M(int x) {
    return (x + x);
  }
}
class B : A {
  public B() {
  }
  public int N(int y) {
    return (y * 10);
  }
}
A b = new B();
Console WriteLine(b.M(5));
```

```
Stack: PC 1
```



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```
class A {
  public A() {
  public int M(int x) {
    return (x + x);
class B : A {
  public B() {
  public int N(int y) {
    return (v * 10);
A b = new B();
Console.WriteLine(b.M(5));
```

```
Stack:
Heap:
```



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```
class A {
   public A() {
   }
   public int M(int x) {
      return (x + x);
   }
}
class B : A {
   public B() {
   }
   public int N(int y) {
      return (y * 10);
   }
}
A b = new B();
Console.WriteLine(b.M(5));
```

Stack:	PC		PC	ret	this
Stack.	15		10	null	ref 1
Heap:	1				



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```
class A {
  public A() {
  }
  public int M(int x) {
    return (x + x);
  }
}
class B : A {
  public B() {
  }
  public int N(int y) {
    return (y * 10);
  }
}
A b = new B();
Console.WriteLine(b.M(5));
```

```
        PC
        ...
        PC
        ret

        15
        ...
        10
        ref 1

        Heap:
        1
```



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```
Conclusion
```

```
class A {
   public A() {
   }
   public int M(int x) {
      return (x + x);
   }
}
class B : A {
   public B() {
   }
   public int N(int y) {
      return (y * 10);
   }
}
A b = new B();
Console.WriteLine(b.M(5));
```

```
        PC
        b

        16
        ref 1
```



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class A {
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    }
   public int M(int x) {
      return (x + x);
   }
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class B : A {
   public B() {
   }
   public int N(int y) {
      return (y * 10);
   }
}
A b = new B();
Console.WriteLine(b.M(5));
```

Stack:	PC		PC	ret	this	х
Stack:	16		5	null	ref 1	5
Heap:	1					



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```
class A {
  public A() {
  public int M(int x) {
    return (x + x);
class B : A {
  public B() {
  public int N(int y) {
    return (v * 10);
A b = new B();
Console.WriteLine(b.M(5));
```

Stack:	PC		PC	ret
Stack:	16		5	10
Hean:	1			



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```
class A {
  public A() {
  }
  public int M(int x) {
    return (x + x);
  }
}
class B : A {
  public B() {
  }
  public int N(int y) {
    return (y * 10);
  }
}
A b = new B();
Console.WriteLine(b.M(5));
```

```
Stack: PC b 17 ref 1

Heap: 1

Output: 10
```



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#### Class inheritance

Similarly, given a method that expects a parameter of type A could accept a parameter of type C.



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Conclusion

Inheritance does not make all combinations possible. For example, the program below does not work: why?

```
class A {
  public int M(int x) {
    return (x + x);
  }
}
class B : A {
  public int N(int y) {
    return (y * 10);
  }
}
class C : A {
  public int O(int z) {
    return (z - 1);
  }
}
B b = new C();
Console.WriteLine(b.M(5));
```



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Conclusion

Inheritance does not make all combinations possible. For example, the program below does not work: why?

```
class A {
   public int M(int x) {
      return (x + x);
   }
}
class B : A {
   public int N(int y) {
      return (y * 10);
   }
}
class C : A {
   public int O(int z) {
      return (z - 1);
   }
}
B b = new C();
Console.WriteLine(b.M(5));
```

There is no inheritance relationship between B and C!



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Conclusion

#### Which in Java then becomes:

```
class A {
   public int M(int x) {
      return (x + x);
   }
}
class B extends A {
   public int N(int y) {
      return (y * 10);
   }
}
class C extends A {
   public int O(int z) {
      return (z - 1);
   }
}
B b = new C();
System.out.println(b.M(5));
```



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Conclusion

#### Class inheritance

The subtyping relationship is transitive. This means that given  $X_i$ :  $Y_i$  and  $Y_i$ :  $Z_i$ , implies  $X_i$ :  $Z_i$ .



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Conclusion

#### Inheritance can also perform multiple conversion steps:

```
class A {
   public int M(int x) {
      return (x + x);
   }
}
class B : A {
   public int N(int y) {
      return (y * 10);
   }
}
class C : B {
   public int O(int z) {
      return (z - 1);
   }
}
A a = new C();
Console.WriteLine(a.M(5));
```



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Conclusion

#### Which in Java then becomes:

```
class A {
    public int M(int x) {
        return (x + x);
    }
}
class B extends A {
    public int N(int y) {
        return (y * 10);
    }
}
class C extends B {
    public int 0(int z) {
        return (z - 1);
    }
}
A a = new C();
System.out.println(a.M(5));
```



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```
node.
```

```
class A {
  public int M(int x) {
    return (x + x);
class B : A {
  public int N(int y) {
    return (y * 10);
class C : B {
  public int O(int z) {
    return (z - 1);
A = new C();
Console.WriteLine(a.M(5)):
```

```
Declarations:
```



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```
class A {
   public int M(int x) {
      return (x + x);
   }
}
class B : A {
   public int N(int y) {
      return (y * 10);
   }
}
class C : B {
   public int O(int z) {
      return (z - 1);
   }
}
A a = new C();
Console.WriteLine(a.M(5));
```

```
\begin{array}{c|c} \text{Declarations:} & \hline PC \\ \hline 5 \\ \\ \text{Classes:} & \hline A \\ \hline M = (A \times \text{int}) \rightarrow \text{int} \\ \end{array}
```



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```
class A {
  public int M(int x) {
    return (x + x);
class B : A f
  public int N(int y) {
    return (y * 10);
class C : B {
  public int O(int z) {
    return (z - 1);
A = new C();
Console.WriteLine(a.M(5));
```

```
Declarations:
                                                                          В
                                                             M=(A \times int) \rightarrow int
Classes:
                   M=(A \times int) \rightarrow int
                                                             N=(B\times int) \rightarrow int
```



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```
class A {
  public int M(int x) {
    return (x + x):
class B : A f
  public int N(int y) {
    return (v * 10);
class C : B {
  public int O(int z) {
    return (z - 1):
A = new C();
Console.WriteLine(a.M(5)):
```

```
Declarations:
                                                                                                                        C.
                                                                             В
                                                                                                           M=(A \times int) \rightarrow int
Classes:
                                                               M=(A \times int) \rightarrow int
                    M=(A \times int) \rightarrow int
                                                                                                           N=(B\times int) \rightarrow int
                                                                N=(B\times int) \rightarrow int
                                                                                                           O=(C\times int) \rightarrow int
```



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```
class A {
  public int M(int x) {
    return (x + x):
class B : A f
  public int N(int y) {
    return (v * 10);
class C : B {
  public int O(int z) {
    return (z - 1):
A = new C();
Console.WriteLine(a.M(5)):
```

```
Declarations: PC a
```

A	В	С
$M=(A \times int) \rightarrow int$	$\begin{array}{c} M{=}(A{\times}int)\toint\\ N{=}(B{\times}int)\toint \end{array}$	$\begin{array}{c} M{=}(A{\times}int) \to int \\ N{=}(B{\times}int) \to int \\ O{=}(C{\times}int) \to int \end{array}$



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Classes:

```
class A {
  public int M(int x) {
    return (x + x):
class B : A f
  public int N(int y) {
    return (v * 10);
class C : B {
  public int O(int z) {
    return (z - 1):
A = new C();
Console.WriteLine(a.M(5)):
```

Declarations:	а	PC	ret	$arg_1$	this
Deciarations.	Α	17	null	int	Α

Α	В	С
$M=(A \times int) \rightarrow int$	$M=(A \times int) \rightarrow int$ $N=(B \times int) \rightarrow int$	$\begin{array}{c} M{=}(A{\times}int) \to int \\ N{=}(B{\times}int) \to int \\ O{=}(C{\times}int) \to int \end{array}$



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```
class A {
  public int M(int x) {
    return (x + x):
class B : A f
  public int N(int y) {
    return (v * 10);
class C : B {
  public int O(int z) {
    return (z - 1):
A = new C();
Console.WriteLine(a.M(5)):
```

Declaratio	ne.	а		PC	ret	arg <sub>1</sub>	this		
Deciaratio	"13. [	Α		17	int	int	Α	]	
		A				В			
Classes:						M=(A	$\times$ int) $\rightarrow$	int	M=(A)

$M{=}(A{\times}int)\to int$	$M=(A \times int) \rightarrow int$ $N=(B \times int) \rightarrow int$	$ \begin{array}{c} M{=}(A{\times}int) \to int \\ N{=}(B{\times}int) \to int \\ O{=}(C{\times}int) \to int \end{array} $



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```
class A {
  public int M(int x) {
    return (x + x):
class B : A f
  public int N(int y) {
    return (v * 10);
class C : B {
  public int O(int z) {
    return (z - 1):
A = new C();
Console.WriteLine(a.M(5)):
```

```
Declarations: PC a
```

Classes:

A	В	С
M=(A  imes int)  o int	$\begin{array}{c} M{=}(A{\times}int) \to int \\ N{=}(B{\times}int) \to int \end{array}$	$\begin{array}{c} M{=}(A{\times}int) \to int \\ N{=}(B{\times}int) \to int \\ O{=}(C{\times}int) \to int \end{array}$



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Stack:

```
class A {
  public int M(int x) {
    return (x + x):
class B : A {
  public int N(int y) {
    return (v * 10);
class C : B {
  public C() {
  public int O(int z) {
    return (z - 1):
A = new C();
Console.WriteLine(a.M(5)):
```



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Stack:

Heap:

```
class A {
  public int M(int x) {
    return (x + x);
class B : A f
  public int N(int y) {
    return (y * 10);
class C : B {
  public C() {
  public int O(int z) {
    return (z - 1):
A a = new C():
Console.WriteLine(a.M(5));
```



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```
Conclusion
```

```
class A {
  public int M(int x) {
    return (x + x);
class B : A f
  public int N(int y) {
    return (y * 10);
class C : B {
  public C() {
  public int O(int z) {
    return (z - 1):
A a = new C():
Console.WriteLine(a.M(5));
```

Stack:	PC		PC	ret	this
Juack.	18		13	null	ref 1
Неар:	1				



PC

13

ret

ref 1

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Stack:

Heap:

18

```
Conclusion
```

```
class A {
  public int M(int x) {
    return (x + x);
class B : A f
  public int N(int y) {
    return (y * 10);
class C : B {
  public C() {
  public int O(int z) {
    return (z - 1):
A = new C():
Console.WriteLine(a.M(5));
```



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Stack:

Heap:

19

ref 1

```
Conclusion
```

```
class A {
  public int M(int x) {
    return (x + x);
class B : A f
  public int N(int y) {
    return (y * 10);
class C : B {
  public C() {
  public int O(int z) {
    return (z - 1):
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Console.WriteLine(a.M(5));
```



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```
node.
```

```
class A {
  public int M(int x) {
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    return (y * 10);
class C : B {
  public C() {
  public int O(int z) {
    return (z - 1):
A = new C();
Console.WriteLine(a.M(5));
```

Stack:	PC		PC	ret	this	×
Stack.	19		3	null	ref 1	5
Heap:	1					



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```
class A {
  public int M(int x) {
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  public int N(int y) {
    return (y * 10);
class C : B {
  public C() {
  public int O(int z) {
    return (z - 1):
A a = new C():
Console.WriteLine(a.M(5));
```

Stack:	PC		PC	ret
Stack.	19		3	10
Неар:	1			



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```
onclusio
```

```
class A {
  public int M(int x) {
    return (x + x):
class B : A {
  public int N(int y) {
    return (v * 10);
class C : B {
  public C() {
  public int O(int z) {
    return (z - 1);
A = new C();
Console.WriteLine(a.M(5));
```

```
Stack: PC a 20 ref 1

Heap: 1

Output: 10
```



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Of course, when inheriting, we can still use all methods available given a variable type.

The code below does indeed work. Why?

```
class A {
  public int M(int x) {
    return (x + x):
class B : A f
  public int N(int y) {
    return (v * 10);
class C : B {
  public int O(int z) {
    return (z - 1);
B b = new C():
Console.WriteLine(b.M(5)):
Console.WriteLine(b.N(5)):
```



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Of course, when inheriting, we can still use all methods available given a variable type.

The code below does indeed work. Why?

```
class A {
  public int M(int x) {
    return (x + x):
class B : A f
  public int N(int y) {
    return (v * 10);
class C : B {
  public int O(int z) {
    return (z - 1);
B b = new C();
Console.WriteLine(b.M(5)):
Console.WriteLine(b.N(5)):
```

It is possible to call both methods M and N on an instance of B.



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#### Which in Java then becomes:

```
class A {
  public int M(int x) {
    return (x + x);
class B extends A {
  public int N(int y) {
    return (y * 10);
class C extends B {
  public int O(int z) {
    return (z - 1);
B b = new C();
System.out.println(b.M(5));
System.out.println(b.N(5));
```



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```
class A {
  public int M(int x) {
    return (x + x):
class B : A {
  public int N(int y) {
    return (v * 10);
class C : B {
  public int O(int z) {
    return (z - 1):
B b = new C():
Console.WriteLine(b.M(5)):
Console.WriteLine(b.N(5));
```

```
Declarations: PC 1
```



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```
Conclusion
```

```
class A {
  public int M(int x) {
    return (x + x);
class B : A f
  public int N(int y) {
    return (y * 10);
class C : B {
  public int O(int z) {
    return (z - 1);
B b = new C():
Console.WriteLine(b.M(5)):
Console.WriteLine(b.N(5)):
```

```
Declarations:
Classes:
                 M=(A \times int) \rightarrow int
```



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Conclusion

```
class A {
  public int M(int x) {
    return (x + x):
class B : A f
  public int N(int y) {
    return (v * 10);
class C : B {
  public int O(int z) {
    return (z - 1):
B b = new C();
Console.WriteLine(b.M(5)):
Console.WriteLine(b.N(5));
```

```
Declarations:
                                                                          B
Classes:
                                                             M=(A \times int) \rightarrow int
                   M=(A\times int) \rightarrow int
                                                             N=(B\times int) \rightarrow int
```

PC



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```
class A {
  public int M(int x) {
    return (x + x):
class B : A {
  public int N(int y) {
    return (v * 10);
class C : B {
  public int O(int z) {
    return (z - 1):
B b = new C():
Console.WriteLine(b.M(5));
Console.WriteLine(b.N(5));
```

```
Declarations:
                                                                             В
                                 A
                                                                                                          M=(A \times int) \rightarrow int
                                                               M=(A \times int) \rightarrow int
Classes:
                    M=(A\times int) \rightarrow int
                                                                                                           N=(B\times int) \rightarrow int
                                                               N=(B\times int) \rightarrow int
                                                                                                          O=(C\times int) \rightarrow int
```



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```
class A {
   public int M(int x) {
      return (x + x);
   }
}
class B : A {
   public int N(int y) {
      return (y * 10);
   }
}
class C : B {
   public int O(int z) {
      return (z - 1);
   }
}
b = new C();
Console.WriteLine(b.M(5));
Console.WriteLine(b.N(5));
```



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```
class A {
  public int M(int x) {
    return (x + x):
class B : A {
  public int N(int y) {
    return (v * 10);
class C : B {
  public int O(int z) {
    return (z - 1):
B b = new C():
Console.WriteLine(b.M(5));
Console.WriteLine(b.N(5));
```

В

Declarations:	Ь	PC	ret	$arg_1$	this
Deciarations.	В	17	null	int	В

A

Classes:  $M=(A \times int) \rightarrow int$  $M=(A\times int) \rightarrow int$ 



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```
class A {
  public int M(int x) {
    return (x + x):
class B : A {
  public int N(int y) {
    return (v * 10);
class C : B {
  public int O(int z) {
    return (z - 1):
B b = new C():
Console.WriteLine(b.M(5));
Console.WriteLine(b.N(5));
```

Declarations:	Ь	PC	ret	$arg_1$	this
Deciarations.	В	17	int	int	В

В A  $M=(A \times int) \rightarrow int$ Classes:  $M=(A \times int) \rightarrow int$  $M=(A\times int) \rightarrow int$  $N=(B\times int) \rightarrow int$  $N=(B\times int) \rightarrow int$  $O=(C\times int) \rightarrow int$ 



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Console.WriteLine(b.N(5));
```

```
Declarations:
                         18
                                    В
                                                                            В
                                                                                                         M=(A \times int) \rightarrow int
                                                              M=(A \times int) \rightarrow int
Classes:
                    M=(A\times int) \rightarrow int
                                                                                                          N=(B\times int) \rightarrow int
                                                               N=(B\times int) \rightarrow int
                                                                                                         O=(C\times int) \rightarrow int
```



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  public int O(int z) {
    return (z - 1):
B b = new C():
Console.WriteLine(b.M(5));
Console.WriteLine(b.N(5));
```

Declarations:	Ь	PC	ret	$arg_1$	this
Deciarations.	В	18	null	int	В

$M{=}(A{\times}int) \rightarrow int \qquad M{=}(A{\times}int) \rightarrow int \\ N{=}(B{\times}int) \rightarrow int \qquad M{=}(A{\times}int) \rightarrow int \\ N{=}(B{\times}int) \rightarrow int \\ O{=}(C{\times}int) \rightarrow int $	A	В	C
	$M=(A \times int) \rightarrow int$		$N=(B\times int) \rightarrow int$



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class C : B {
  public int O(int z) {
    return (z - 1):
B b = new C():
Console.WriteLine(b.M(5));
Console.WriteLine(b.N(5));
```

	B   18   Int	Int B			
	Α	В	C		
5:	M=(A  imes int)  o int	$\begin{array}{c} M{=}(A{\times}int) \to int \\ N{=}(B{\times}int) \to int \end{array}$	$M=(A \times int) \rightarrow int$ $N=(B \times int) \rightarrow int$ $O=(C \times int) \rightarrow int$		

this

ret

 $arg_1$ 



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    return (z - 1):
B b = new C():
Console.WriteLine(b.M(5));
Console.WriteLine(b.N(5));
```

```
Declarations:
                                                   В
```

$M{=}(A{\times}int)\to int$	$\begin{array}{c} M{=}(A{\times}int) \to int \\ N{=}(B{\times}int) \to int \end{array}$	$\begin{array}{c} M{=}(A{\times}int) \to int \\ N{=}(B{\times}int) \to int \\ O{=}(C{\times}int) \to int \end{array}$



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```
class A {
  public int M(int x) {
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B b = new C():
Console.WriteLine(b.M(5));
Console.WriteLine(b.N(5));
```

```
Stack: PC 1
```



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```
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```

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  public C() {
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B b = new C();
Console.WriteLine(b.M(5));
Console.WriteLine(b.N(5)):
```

```
Stack:
         18
Heap:
```



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  public int O(int z) {
    return (z - 1);
B b = new C();
Console.WriteLine(b.M(5));
Console.WriteLine(b.N(5)):
```

Stack:	PC		PC	ret	this
Juack.	18		13	null	ref 1
Heap:	1				



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```
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```

```
class A {
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  public int O(int z) {
    return (z - 1);
B b = new C();
Console.WriteLine(b.M(5));
Console.WriteLine(b.N(5)):
```

Stack:	PC		PC	ret
Stack.	18		13	ref 1
Неар:	1			
псар.				



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```
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```

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    return (z - 1);
B b = new C();
Console.WriteLine(b.M(5));
Console.WriteLine(b.N(5)):
```

```
Stack:
          19
                 ref 1
Heap:
```



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PC

19

Stack:

Heap:

PC

3

ret

null

demo: list. empty, and node.

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```
class A {
  public int M(int x) {
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class B : A f
  public int N(int y) {
    return (v * 10);
class C : B {
  public C() {
  public int O(int z) {
    return (z - 1);
B b = new C();
Console.WriteLine(b.M(5));
Console.WriteLine(b.N(5)):
```

this

ref 1

х



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    return (z - 1);
B b = new C();
Console.WriteLine(b.M(5));
Console.WriteLine(b.N(5)):
```

Stack:	PC		PC	ret
Stack.	19		3	10
Неар:	1			



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```
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```

```
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  public C() {
  public int O(int z) {
    return (z - 1):
B b = new C();
Console.WriteLine(b.M(5)):
Console.WriteLine(b.N(5));
```

```
        PC
        b

        20
        ref 1

Heap: 1
Output: 10
```



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```
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  public C() {
  public int O(int z) {
    return (z - 1):
B b = new C();
Console.WriteLine(b.M(5)):
Console.WriteLine(b.N(5));
```

Stack:	PC			PC	ret	this	у	
Stack:	20			8	null	ref 1	5	
Heap: 1								
Output	: 10							



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```
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```

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  public C() {
  public int O(int z) {
    return (z - 1):
B b = new C();
Console.WriteLine(b.M(5)):
Console.WriteLine(b.N(5));
```

```
PC.
                            PC.
                                   ret
Stack:
         20
                             8
                                   50
Heap:
Output:
```



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```
class A {
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class B : A {
  public int N(int y) {
    return (v * 10);
class C : B {
  public C() {
  public int O(int z) {
    return (z - 1):
B b = new C();
Console.WriteLine(b.M(5)):
Console.WriteLine(b.N(5));
```

```
Stack:
         21
                ref 1
Heap:
Output:
```



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A major difference with Python is that, even if the instance may allow calling some methods, subtyping might disallow it.

The code below does not work. Why?

```
class A {
  public int M(int x) {
     return (x + x);
  }
}
class B : A {
  public int N(int y) {
     return (y * 10);
  }
}
class C : B {
  public int O(int z) {
     return (z - 1);
  }
}
B b = new C();
Console.WriteLine(b.O(5));
```



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The code below does not work. Why?

```
class A {
  public int M(int x) {
    return (x + x);
  }
}
class B : A {
  public int N(int y) {
    return (y * 10);
  }
}
class C : B {
  public int O(int z) {
    return (z - 1);
  }
}
B b = new C();
Console.WriteLine(b.O(5));
```

b is declared with type B, which has no method 0.



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#### Which in Java then becomes:

```
class A {
   public int M(int x) {
     return (x + x);
   }
}
class B extends A {
   public int N(int y) {
     return (y * 10);
   }
}
class C extends B {
   public int O(int z) {
     return (z - 1);
   }
}
B b = new C();
System.out.println(b.0(5));
```



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#### Zero-level data types

- The subtyping relationship can start from a data type so general that it has no concrete implementation.
- This data type is called an interface.
- Interfaces are classes defined with the keyword interface. They have no fields, and no implementation of their methods.
- We say that a class implements, not inherits from, one or more interfaces.



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#### Zero-level data types

- Interfaces are especially useful to specify what requirements a data type must satisfy to be used in a context.
- With interfaces we are not bound to also giving a "default" implementation.



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Implementing interfaces requires very little code: in C#, a colon (:) suffices with the name of the implemented interface next to that of the defined class.

In Java, we use the keyword implements instead of the colon.

It is possible to implement multiple interfaces from the same class.



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The program below works: why?

```
interface A {
   int M(int x);
}
class B : A {
   public int M(int x) {
     return (x + x);
   }
}
A b = new B();
Console.WriteLine(b.M(5));
```



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The program below works: why?

```
interface A {
  int M(int x);
}
class B : A {
  public int M(int x) {
    return (x + x);
  }
}
A b = new B();
Console.WriteLine(b.M(5));
```

Because the declaration of b specifies A as the type, but whenever we expect an A we can use a B thanks to the subtyping of implemented interfaces.



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#### Which in Java then becomes:

```
interface A {
   int M(int x);
}
class B implements A {
   public int M(int x) {
     return (x + x);
   }
}
A b = new B();
System.out.println(b.M(5));
```



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```
The program below does not work: why?
```

```
interface A {
  int M(int x);
}
A a = new A();
Console.WriteLine(a.M(5));
```



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The program below does not work: why?

```
interface A {
  int M(int x);
}
A a = new A();
Console.WriteLine(a.M(5));
```

Because A has no implementation and so cannot be instantiated: what code could we possibly execute for method M?



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#### Which in Java then becomes:

```
interface A {
   int M(int x);
}
A a = new A();
System.out.println(a.M(5));
```



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#### Zero-level data types

Polymorphism can be used in a lot of contexts, as long as the conversion we expect of the language is provably safe.



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The program below works: why?

```
interface A {
   A M(A x);
}
class B : A {
   public A M(A x) {
     return this;
   }
}
A b = new B();
Console.WriteLine(b.M(new B()));
```



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The program below works: why?

```
interface A {
   A M(A x);
}
class B : A {
   public A M(A x) {
      return this;
   }
}
A b = new B();
Console.WriteLine(b.M(new B()));
```

Because the argument to M, which should be an A, can safely accept a B as well.



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#### Which in Java then becomes:

```
interface A {
   A M(A x);
}
class B implements A {
   public A M(A x) {
      return this;
   }
}
A b = new B();
System.out.println(b.M(new B()));
```



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#### Looking back

- Polymorphism makes it possible to pass different data types to other contexts, as long as the conversion is safe
- Inheritance is the basic mechanism of polymorphism
- Interfaces make this even more powerful by allowing the use of polymorphism without a concrete data type



#### This is it!

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# The best of luck, and thanks for the attention!