

Type systems

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# Type systems

The INFDEV team

Hogeschool Rotterdam  
Rotterdam, Netherlands

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## Lecture topics

- Issues with Python
- Issues with Python and possible solutions
- Static typing

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# Issues with Python

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## Lack of...

- Lack of constraints: how can we specify that a function only takes integers as input
- Lack of structure: how can we specify that a variable will certainly support some methods
- Lack of assurances: how can we guarantee that programs with evident errors are not run

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*What is wrong with this?*

```
1 def f(x):  
2     return (x * 2)  
3 f("nonsense")
```

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*What is wrong with this?*

```
1 def f(x):  
2     return (x * 2)  
3 f("nonsense")
```

The function clearly works with integers, but is given a string

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*What is wrong with this?*

```
1 x = input()
2 if (x > 100):
3     print("dumb")
4 else:
5     print("dumber")
```



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*What is wrong with this?*

```
1 x = input()
2 if (x > 100):
3     print("dumb")
4 else:
5     print("dumber")
```

The comparison is nonsensical if  $x$  is not a number

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```
1 def g(car):  
2     return car.drive(2)  
3 g(-1)
```

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*What is wrong with this?*

```
1 def g(car):  
2     return car.drive(2)  
3 g(-1)
```

We expect something with a drive method, but get an integer instead

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# Possible solutions

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## Testing?

- Testing the program should be enough

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## Testing?

- Testing the program should be enough
- Right?

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## Testing?

- Testing the program should be enough
- Right?
- No. The number of possible execution paths is immense (order of billions), and each test only takes one.
- Testing can only guarantee presence of bugs, but not their absence!

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*How many times would we need to test to be sure there is no error?*

```
1 if (randint(0,100000) > 99999):  
2     g(-1)  
3 else:  
4     g(mercedesSL500)
```



# Possible solutions

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*How many times would we need to test to be sure there is no error?*

```
1 if (randint(0,100000) > 99999):  
2     g(-1)  
3 else:  
4     g(mercedesSL500)
```

$\geq 100000$

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## Testing?

- We want our programming languages to perform checks for us
- Clearly nonsensical programs should be rejected before we can even run them
- It is safer and easier to spend more time “talking” with the IDE than hoping to find all errors with tests

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# Static typing

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## Introduction

- The language verifies<sup>a</sup>, before running code, that all variables are correctly used
- "Correctly used" means that they are guaranteed to support all operations used on them
- This is by far and large the most typical solution to increase safety and productivity

---

<sup>a</sup>By means of the **compiler**.

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## What is static typing?

- When declaring a variable, we also specify what sort of data it will contain
- The **sort** of data contained is called **TYPE** of the variable
- Types can be either primitives (int, string, etc.), custom (classes), or compositions (functions, list of elements of a given type, etc.)

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## What is static typing?

- Especially in mainstream languages, the specification of the type of a variable is done by hand by the programmer
- In other languages (mostly functional languages like F#, Haskell, etc.) the type of variables is automatically 'guessed' by the compiler
- In our case our programs will become a bit more verbose but better specified
- Still, static typing is not necessarily connected with verbosity

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A variable declaration in C# or Java is prefixed by the type of the variable

- `int x;` declares an integer variable
- `string s;` declares a string variable
- `float f;` declares a floating point variable
- ...

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```
1 def f(x):  
2     return (x * 2)
```

Becomes, typed:

```
1 int f(int x) {  
2     return (x * 2);  
3 }
```

*What has improved and why?*



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```
1 def f(x):  
2     return (x * 2)
```

Becomes, typed:

```
1 int f(int x) {  
2     return (x * 2);  
3 }
```

*What has improved and why?*

The second definition encodes information about what goes in and what comes out of the function

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*Is this still possible to write (as it was in Python)?*

```
1  int f(int x) {  
2      return (x * 2);  
3  }  
4  f("nonsense");
```

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*Is this still possible to write (as it was in Python)?*

```
1  int f(int x) {  
2      return (x * 2);  
3  }  
4  f("nonsense");
```

No: we get a compiler error because a string cannot be used where a number is expected

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```
1 x = input()
2 if (x > 100):
3     print("dumb")
4 else:
5     print("dumber")
```

Becomes, typed:

```
1 int x = Int32.Parse(Console.ReadLine());
2 if (x > 100) {
3     Console.WriteLine("safe");
4 } else {
5     Console.WriteLine("safer");
6 }
```

*What has improved and why?*

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```
1 x = input()
2 if (x > 100):
3     print("dumb")
4 else:
5     print("dumber")
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Becomes, typed:

```
1 int x = Int32.Parse(Console.ReadLine());
2 if (x > 100) {
3     Console.WriteLine("safe");
4 } else {
5     Console.WriteLine("safer");
6 }
```

*What has improved and why?*

The variable declaration specifies what is allowed (and what is not) inside the variable.

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```
1 def g(car):  
2     return car.drive(2)  
3 g(-1)
```

Becomes, typed:

```
1 int g(Car car) {  
2     return car.drive(2);  
3 }  
4 g(-1);
```

*What has improved and why?*

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```
1 def g(car):  
2     return car.drive(2)  
3 g(-1)
```

Becomes, typed:

```
1 int g(Car car) {  
2     return car.drive(2);  
3 }  
4 g(-1);
```

*What has improved and why?*

The function declaration specifies that `car` is an instance of the `Car` class. We will thus get a compiler error.

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# Typing rules and semantic rules



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## How do we describe them?

- How do we describe such relations clearly?
- We use the so-called **typing rules**, which specify what may be done and what not
- Typing rules are quite intuitive: they state that if one or more premises are true, then the conclusion is true as well

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$$\frac{A \wedge B}{C}$$

If A and B are true, then we can conclude C

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$$\frac{\text{I wish to buy a pretty car} \wedge \text{I have 120000 euros}}{\text{I buy a Mercedes SL500}}$$

*How do we read this rule?*

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$$\frac{\text{I wish to buy a pretty car} \wedge \text{I have 120000 euros}}{\text{I buy a Mercedes SL500}}$$

*How do we read this rule?*

If I have 120000 euros and I wish to buy a pretty car, then I buy a Mercedes SL500

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It is raining  $\wedge$  I have my umbrella with me  
I open my umbrella

*How do we read this rule?*

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It is raining  $\wedge$  I have my umbrella with me  
I open my umbrella

*How do we read this rule?*

If it is raining, and I have my umbrella with me, then I open my umbrella

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## Reading typing rules

Let us apply this machinery to programming languages

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## Reading typing rules

- Let us apply this machinery to programming languages
- We will effectively give the specification of a modern compiler
- This looks like a “broadly scoped” execution of the program, and it is indeed such
- This process is called type checking



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## Reading typing rules

- We want to specify this in the typing rule notation
- The typing rules manipulate a stack of declarations which we will call  $D$
- Each typing rule will add or remove variable declarations and return the type of the current expression
- Instead of coupling each variable with its value, we couple it with its type

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Conclusion

- The simplest typing rule is the one that finds a variable declaration
- A declaration adds to the declarations  $D$  the variable, connected with its type

$$\overline{\langle (T \text{ } v;), D \rangle \rightarrow \langle \text{void}, D[v \mapsto T] \rangle}$$

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1

```
int x;
```

Declarations:

PC
1

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```
int x;
```

Declarations:

PC	x
2	int

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Conclusion

- When we look the variable up, its type is whatever type was found connected to it in the declarations
- This does further nothing to the declarations
- Let's assume that  $x$  is a variable name

$$\overline{\langle x, D \rangle} \rightarrow \langle D[x], D \rangle$$

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```
1  int x = 10;  
2  x = (x + 5);
```

Declarations:

PC
1

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```
1  int x = 10;  
2  x = (x + 5);
```

Declarations:

PC	x
2	int

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```
1 int x = 10;  
2 x = (x + 5);
```

Declarations:

PC	x
3	int



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- Another simple typing rule is the one that types a constant value
- It does nothing to the declarations
- Let's assume that `i` is an integer constant

$$\overline{\langle i, D \rangle} \rightarrow \overline{\langle \text{int}, D \rangle}$$

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- Let's assume that `f` is a floating point constant

$$\overline{\langle f, D \rangle \rightarrow \langle \text{float}, D \rangle}$$

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- Let's assume that  $s$  is a string constant

$$\overline{\langle s, D \rangle \rightarrow \langle \text{string}, D \rangle}$$

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- Let's assume that  $b$  is a boolean constant

$$\overline{\langle b, D \rangle} \rightarrow \langle \text{bool}, D \rangle$$

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## Reading typing rules

More complex typing rules compose together the types of different statements

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- The typing rule for operators such as `+` requires the operands to be compatible
- The type of both operands is often the same, for example `int` or `float`
- The resulting type is then the type of both operands
- Operands do not modify the current declarations

$$\frac{\langle a, D \rangle \rightarrow \langle \text{int}, D \rangle \wedge \langle b, D \rangle \rightarrow \langle \text{int}, D \rangle}{\langle (a + b), D \rangle \rightarrow \langle \text{int}, D \rangle}$$

$$\frac{\langle a, D \rangle \rightarrow \langle \text{float}, D \rangle \wedge \langle b, D \rangle \rightarrow \langle \text{float}, D \rangle}{\langle (a + b), D \rangle \rightarrow \langle \text{float}, D \rangle}$$

$$\frac{\langle a, D \rangle \rightarrow \langle \text{string}, D \rangle \wedge \langle b, D \rangle \rightarrow \langle \text{string}, D \rangle}{\langle (a + b), D \rangle \rightarrow \langle \text{string}, D \rangle}$$

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- The type of both operands could differ, but still be compatible (for example adding an `int` and a `float`)
- The resulting type is then the most generic type of the operands
- Operands do not modify the current declarations

$$\frac{\langle a, D \rangle \rightarrow \langle \text{int}, D \rangle \wedge \langle b, D \rangle \rightarrow \langle \text{float}, D \rangle}{\langle (a + b), D \rangle \rightarrow \langle \text{float}, D \rangle}$$
$$\frac{\langle a, D \rangle \rightarrow \langle \text{float}, D \rangle \wedge \langle b, D \rangle \rightarrow \langle \text{int}, D \rangle}{\langle (a + b), D \rangle \rightarrow \langle \text{float}, D \rangle}$$

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- Statements in a sequence both modify, top-to-bottom, the declarations
- Usually we expect the statements to simply return nothing, that is `void`
- Further we cannot say anything about what they each do

$$\frac{\langle a, D \rangle \rightarrow \langle \text{void}, D_1 \rangle \wedge \langle b, D_1 \rangle \rightarrow \langle \text{void}, D_2 \rangle}{\langle (a; b), D \rangle \rightarrow \langle \text{void}, D_2 \rangle}$$



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```
1  int x = 10;  
2  int y = 20;  
3  x = (x + y);
```

Declarations:

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1

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```
1  int x = 10;  
2  int y = 20;  
3  x = (x + y);
```

Declarations:

PC	x
2	int

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```
1 int x = 10;  
2 int y = 20;  
3 x = (x + y);
```

Declarations:

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3	int	int

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```
1 int x = 10;  
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3 x = (x + y);
```

Declarations:

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4	int	int

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- The typing rule for an if-then-else requires the condition to be a boolean expression, and assumes the type of both the then and the else bodies
- The type of both the then and the else bodies must be the same (usually void, something else in case of function returns)
- It does not add anything to the declarations, even though the bodies of the then and the else might declare local variables

$$\frac{\langle c, D \rangle \rightarrow \langle \text{bool}, D \rangle \wedge \langle A, D \rangle \rightarrow \langle T, D' \rangle \wedge \langle B, D \rangle \rightarrow \langle U, D' \rangle \wedge T = U}{\langle (\text{if } c \{ A \} \text{else} \{ B \}), D \rangle \rightarrow \langle T, D \rangle}$$

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```
1 int x = 10;  
2 int y = 20;  
3 if (x > y) {  
4     string z = "x";  
5     Console.WriteLine(z);  
6 } else {  
7     string z = "y";  
8     Console.WriteLine(z);  
9 }
```

Declarations:

PC
1

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```
1 int x = 10;  
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4     string z = "x";  
5     Console.WriteLine(z);  
6 } else {  
7     string z = "y";  
8     Console.WriteLine(z);  
9 }
```

Declarations:

PC	x
2	int

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```
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3 if (x > y) {
4     string z = "x";
5     Console.WriteLine(z);
6 } else {
7     string z = "y";
8     Console.WriteLine(z);
9 }
```

Declarations:

PC	x	y
3	int	int



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```
1 int x = 10;
2 int y = 20;
3 if (x > y) {
4     string z = "x";
5     Console.WriteLine(z);
6 } else {
7     string z = "y";
8     Console.WriteLine(z);
9 }
```

Declarations:

x	y		PC
int	int		4

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```
1 int x = 10;
2 int y = 20;
3 if (x > y) {
4     string z = "x";
5     Console.WriteLine(z);
6 } else {
7     string z = "y";
8     Console.WriteLine(z);
9 }
```

Declarations:

x	y		PC	z
int	int		5	string

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7     string z = "y";
8     Console.WriteLine(z);
9 }
```

Declarations:

PC	x	y
6	int	int

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```

Declarations:

x	y		PC
int	int		7

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8     Console.WriteLine(z);  
9 }
```

Declarations:

x	y		PC	z
int	int		8	string

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8     Console.WriteLine(z);
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```

Declarations:

PC	x	y
9	int	int

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- The typing rule for a `while` loop requires the condition to be a boolean expression, and assumes the type of the body
- The type of the body can be anything (usually `void`, something else in case of function returns)
- It does not add anything to the declarations, even though the body might declare local variables

$$\frac{\langle c, D \rangle \rightarrow \langle \text{bool}, D \rangle \wedge \langle B, D \rangle \rightarrow \langle T, D_1 \rangle}{\langle (\text{while } c \{ A \}), D \rangle \rightarrow \langle T, D \rangle}$$

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- The typing rule for a class declaration adds the class declaration to the declarations with all its fields and methods
- When adding the declaration of the class, we have to check that the types of the method bodies match their declarations
- Assume that  $C$  is the class name,  $f_i$  is the  $i$ -th field in the class (of type  $F_i$ ), and  $m_j$  is the  $j$ -th method in the class (with type  $M_j$ )

$$\frac{D_1 := D[C \mapsto [\dots f_i \mapsto F_i \dots m_j \mapsto M_j \dots]] \wedge \langle M_j m_j, D_1[\text{this} \mapsto C] \rangle \rightarrow \langle M_j^1, D_2 \rangle \wedge M_j = M_j^1}{\langle (\text{class } C \{ \dots F_i f_i \dots \dots M_j m_j \dots \}), D \rangle \rightarrow \langle T, D_1 \rangle}$$



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- When type checking a method declaration (within a class declaration we type check its body and compare the result with the type of the declaration
- Assume that  $C$  is the class name,  $p_i$  is the  $i$ -th parameter of the method (of type  $P_i$ ), and  $b$  is the method body
- The type of a method is of the form  $P_1 \times P_2 \times \dots \times P_n \rightarrow R$ , where  $P_l$  is the type of the  $l$ -th parameter and  $R$  is the return type

$$\frac{\langle (b), D[..p_l \mapsto P_l ..] \rangle \rightarrow \langle R, D_1 \rangle}{\langle (R \text{ m}(..P_1 \ p_1 ..)b), D \rangle \rightarrow \langle (P_1 \times P_2 \times \dots \times P_n \rightarrow R), D \rangle}$$

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1 class Counter {  
2     private int cnt;  
3     public Counter() {  
4         this.cnt = 0;  
5     }  
6     public void incr(int diff) {  
7         this.cnt = (this.cnt + diff);  
8     }  
9 }
```

Declarations:

PC
1

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6      public void incr(int diff) {
7          this.cnt = (this.cnt + diff);
8      }
9  }
```

Declarations:

PC	this
4	Counter

Classes:

Counter
Counter=Counter $\rightarrow$ Counter
cnt=int
incr=(Counter $\times$ int) $\rightarrow$ void

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Declarations:

PC	this
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```

Declarations:

PC	diff	this
7	int	Counter

Classes:

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Declarations:

PC	diff	this
8	int	Counter

Classes:

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7          this.cnt = (this.cnt + diff);
8      }
9  }
```

Declarations:

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Classes:

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Counter=Counter $\rightarrow$ Counter
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Conclusion

- When type checking a return statement, we typecheck its argument
- The type of the argument is also the type of the return statement
- There is no change to the declarations

$$\frac{\langle x, D \rangle \rightarrow \langle T, D \rangle}{\langle (\text{return } x), D \rangle \rightarrow \langle T, D \rangle}$$



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Conclusion

- Statements in a sequence might contain return statements
- In this case one of them might not return void
- Their sequence will assume the non-void type

$$\frac{\langle a, D \rangle \rightarrow \langle T, D_1 \rangle \wedge \langle b, D_1 \rangle \rightarrow \langle \text{void}, D_2 \rangle}{\langle (a; b), D \rangle \rightarrow \langle T, D_2 \rangle}$$

$$\frac{\langle a, D \rangle \rightarrow \langle \text{void}, D_1 \rangle \wedge \langle b, D_1 \rangle \rightarrow \langle T, D_2 \rangle}{\langle (a; b), D \rangle \rightarrow \langle T, D_2 \rangle}$$

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Conclusion

- Statements in a sequence might contain return statements
- They might both return a non-void type
- Their sequence will assume the non-void type of both, which must be the same

$$\frac{\langle a, D \rangle \rightarrow \langle T, D_1 \rangle \wedge \langle b, D_1 \rangle \rightarrow \langle U, D_2 \rangle \wedge T = U}{\langle (a; b), D \rangle \rightarrow \langle T, D_2 \rangle}$$

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2     private int cnt;  
3     public Counter() {  
4         this.cnt = 0;  
5     }  
6     public int incr(int diff) {  
7         this.cnt = (this.cnt + diff);  
8         return this.cnt;  
9     }  
10 }
```

Declarations:

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1

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```

1  class Counter {
2      private int cnt;
3      public Counter() {
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7          this.cnt = (this.cnt + diff);
8          return this.cnt;
9      }
10 }
```

Declarations:

PC	this
4	Counter

Classes:

Counter
Counter=Counter $\rightarrow$ Counter cnt=int incr=(Counter $\times$ int) $\rightarrow$ int

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```

1  class Counter {
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4          this.cnt = 0;
5      }
6      public int incr(int diff) {
7          this.cnt = (this.cnt + diff);
8          return this.cnt;
9      }
10 }
```

Declarations:

PC	this
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Classes:

Counter
Counter=Counter → Counter cnt=int incr=(Counter×int) → int

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2      private int cnt;
3      public Counter() {
4          this.cnt = 0;
5      }
6      public int incr(int diff) {
7          this.cnt = (this.cnt + diff);
8          return this.cnt;
9      }
10 }
```

Declarations:

PC	diff	this
7	int	Counter

Classes:

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4          this.cnt = 0;
5      }
6      public int incr(int diff) {
7          this.cnt = (this.cnt + diff);
8          return this.cnt;
9      }
10 }
```

Declarations:

PC	diff	this
8	int	Counter

Classes:

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1  class Counter {
2      private int cnt;
3      public Counter() {
4          this.cnt = 0;
5      }
6      public int incr(int diff) {
7          this.cnt = (this.cnt + diff);
8          return this.cnt;
9      }
10 }
```

Declarations:

PC	ret	diff	this
9	int	int	Counter

Classes:

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Counter=Counter $\rightarrow$ Counter cnt=int incr=(Counter $\times$ int) $\rightarrow$ int



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1  class Counter {
2      private int cnt;
3      public Counter() {
4          this.cnt = 0;
5      }
6      public int incr(int diff) {
7          this.cnt = (this.cnt + diff);
8          return this.cnt;
9      }
10 }
```

Declarations:

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Classes:

Counter
Counter=Counter $\rightarrow$ Counter cnt=int incr=(Counter $\times$ int) $\rightarrow$ int

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Conclusion

- Sometimes we may look a field  $f$  up from an instance  $x$  of a class
- This assumes the type of the field, which needs to be looked up in the class descriptor found in the declarations
- No declaration is further modified

$$\frac{\langle x, D \rangle \rightarrow \langle C, D \rangle \wedge \langle f, C \rangle \rightarrow \langle F, C \rangle \wedge T = U}{\langle \langle x.f \rangle, D \rangle \rightarrow \langle F, D \rangle}$$

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Conclusion

```
1 class Counter {  
2     public int cnt;  
3     public Counter() {  
4         this.cnt = 0;  
5     }  
6 }  
7 ICounter c = new Counter();  
8 int x = c.cnt;
```

Declarations:

PC
1

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1 class Counter {
2     public int cnt;
3     public Counter() {
4         this.cnt = 0;
5     }
6 }
7 ICounter c = new Counter();
8 int x = c.cnt;

```

Declarations:

PC	this
4	Counter

Classes:

Counter
Counter=Counter → Counter cnt=int

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7 ICounter c = new Counter();
8 int x = c.cnt;
```

Declarations:

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5	Counter

Classes:

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```

1  class Counter {
2      public int cnt;
3      public Counter() {
4          this.cnt = 0;
5      }
6  }
7  ICounter c = new Counter();
8  int x = c.cnt;
    
```

Declarations:

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Classes:

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Counter=Counter → Counter cnt=int

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```

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2     public int cnt;
3     public Counter() {
4         this.cnt = 0;
5     }
6 }
7 ICounter c = new Counter();
8 int x = c.cnt;
    
```

Declarations:

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Classes:

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```

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3      public Counter() {
4          this.cnt = 0;
5      }
6  }
7  ICounter c = new Counter();
8  int x = c.cnt;
    
```

Declarations:

PC	c	x
9	ICounter	int

Classes:

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Conclusion

- Sometimes we may call a method  $m$  up from an instance  $x$  of a class and with parameters  $p_i$
- This assumes the return type of the method, provided that all parameter types match the types expected by the method
- No declaration is further modified

$$\frac{\langle x, D \rangle \rightarrow \langle c, D \rangle \wedge \langle m, C \rangle \rightarrow \langle (P_1 \times P_2 \times \cdots \times P_n \rightarrow R), C \rangle \wedge \langle p_i, D \rangle \rightarrow \langle p'_i, D \rangle \wedge p_i = p'_i}{\langle (x.f(..p_1..)), D \rangle \rightarrow \langle R, D \rangle}$$

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1 class Counter {  
2     private int cnt;  
3     public Counter() {  
4         this.cnt = 0;  
5     }  
6     public void Incr(int diff) {  
7         this.cnt = (this.cnt + diff);  
8     }  
9 }  
10 Counter c = new Counter();  
11 c.Incr(5);
```

Declarations:

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8      }
9  }
10 Counter c = new Counter();
11 c.Incr(5);

```

Declarations:

PC	this
4	Counter

Classes:

Counter
Counter=Counter $\rightarrow$ Counter
Incr=(Counter $\times$ int) $\rightarrow$ void
cnt=int

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8      }
9  }
10 Counter c = new Counter();
11 c.Incr(5);

```

Declarations:

PC	diff	this
6	int	Counter

Classes:

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Incr=(Counter $\times$ int) $\rightarrow$ void
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```

Declarations:

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```

Declarations:

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Classes:

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7          this.cnt = (this.cnt + diff);
8      }
9  }
10 Counter c = new Counter();
11 c.Incr(5);

```

Declarations:

c		PC	ret	arg <sub>1</sub>	this
Counter		11	null	int	Counter

Classes:

Counter
Counter=Counter → Counter
Incr=(Counter×int) → void
cnt=int

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9  }
10 Counter c = new Counter();
11 c.Incr(5);

```

Declarations:

c		PC	ret	arg <sub>1</sub>	this
Counter		11	void	int	Counter

Classes:

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```

Declarations:

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Conclusion

- We may call a static method  $m$  from class  $C$  and with parameters  $p_i$
- This assumes the return type of the method, provided that all parameter types match the types expected by the method
- We do not need to look up the class because it is already specified in the call
- No declaration is further modified

$$\frac{\langle m, C \rangle \rightarrow \langle (P_1 \times P_2 \times \dots \times P_n \rightarrow R), C \rangle \wedge \langle p_i, D \rangle \rightarrow \langle P'_i, D \rangle \wedge P_i = P'_i}{\langle (C.f(..p_i..)), D \rangle \rightarrow \langle R, D \rangle}$$

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```
1 class Utils {  
2     static public int AddThree(int a,int b,int c) {  
3         return ((a + b) + c);  
4     }  
5 }  
6 int x = Utils.AddThree(10,20,30);
```

Declarations:

PC
1

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```

Declarations:

PC	a	b	c
3	int	int	int

Classes:

Utils
AddThree=(int×int×int) → int

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Declarations:

PC
6

Classes:

Utils
AddThree=( $\text{int} \times \text{int} \times \text{int}$ ) $\rightarrow$ int

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```

Declarations:

PC	x
7	int

Classes:

Utils
AddThree=(int×int×int) → int

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## Reading typing rules

- The constructor of a class is simply a specially named static method
- It has no further typing rules

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```
1 class CounterFrom {  
2     public int cnt;  
3     public CounterFrom(int cnt0) {  
4         this.cnt = cnt0;  
5     }  
6 }  
7 CounterFrom c = new CounterFrom(100);
```

Declarations:

PC
1



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6 }
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```

Declarations:

PC	cnt0	this
4	int	CounterFrom

Classes:

CounterFrom
CounterFrom=(CounterFrom $\times$ int) $\rightarrow$ CounterFrom cnt=int

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Declarations:

PC	cnt0	this
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Declarations:

PC
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Classes:

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5     }
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7 CounterFrom c = new CounterFrom(100);

```

Declarations:

PC	c
8	CounterFrom

Classes:

CounterFrom
CounterFrom=(CounterFrom $\times$ int) $\rightarrow$ CounterFrom cnt=int

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## Looking back

- Python is brittle and breaks easily
- Static typing is a way to run a coarse simulation of the program
- If type checking fails, then the program cannot be guaranteed to run correctly, and we get a compiler error
- Safer programming, but at the cost of being able to run less programs that might still be valid

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The best of luck, and thanks for the  
attention!