Causality and supervised machine learning

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Introduction

 \boldsymbol{x}

What is the objective of empirical policy research?

- 1. causation: what is the effect of a particular variable on an outcome?
- 2. prediction: find some function that provides a good prediction of \boldsymbol{y} as a function of

Intution

$$y = \alpha + \beta x + \varepsilon$$

- causation: interested in \hat{eta}
- ullet prediction: interested in \hat{y}

Preparation

```
In [37]: import matplotlib.pyplot as plt
import numpy as np
import pandas as pd
import seaborn as sns
import statsmodels.formula.api as smf # module for various regression models
sns.set()
%matplotlib inline
```

Causal Inference

Introduction

Most statistical methods in social science theory is focused on estimating causal effects

Causal effect: how does the factor A affect B?

Examples of causal questions:

- what is the effect of being assigned to a shared group on communication?
- what is the effect of sterotypical names on job interview success?

Intuition

Variable of interest (often called *treatment*): D_i

Outcome of interest: Y_i

Potential outcome framework

$$Y_i = \left\{egin{array}{ll} Y_{1i} & ext{if } D_i = 1, \ Y_{0i} & ext{if } D_i = 0. \end{array}
ight.$$

The observed outcome Y_i can be written in terms of potential outcomes as

$$Y_i = Y_{0i} + (Y_{1i} - Y_{0i})D_i$$

 $Y_{1i} - Y_{0i}$ is the *causal* effect of D_i on Y_i .

But we never observe the same individual i in both states. This is the **fundamental problem of causal inference**.

Selection Bias I

We need some way of estimating the state we do not observe (the *counterfactual*)

Usually, our sample contains individuals from both states - treated and untreated.

So why not do a naive comparison of averages by treatment status? i.e.

$$E[Y_i|D_i = 1] - E[Y_i|D_i = 0]$$

Selection Bias II

We can rewrite into: $\left[Y_i|D_i=1\right] - E[Y_i|D_i=1] - E[Y_i|D_i=1] + \left[Y_i|D_i=1\right] - E[Y_i|D_i=1] + \left[Y_i|D_i=1\right] - E[Y_i|D_i=1] - E[Y_i|D_i=$

The decomposition:

- $ullet E[Y_{1i}|D_i=1]-E[Y_{0i}|D_i=1]=E[Y_{1i}-Y_{0i}|D_i=1]$: the average causal effect of D_i on Y.
- $E[Y_{0i}|D_i=1]-E[Y_{0i}|D_i=0]$: difference in average Y_{0i} between the two groups. Likely to be different from 0 when individuals are allowed to self-select into treatment. Often referred to as **selection bias**.

Random assignment solves the problem

Random assignment of \mathcal{D}_i solves the problem because random assignment makes \mathcal{D}_i independent of potential outcomes

That means that $E[Y_{0i}|D_i=1]=E[Y_{0i}|D_i=0]$ and thus that the selection bias term is zero

Intuition: with random assignment, non-treated individuals can be used as counterfactuals for treated (what would have happened to individual i had he not received the treatment?)

This allows us to overcome the fundamental problem of causal inference

Randomization

Holland and Rubin (1986)

no causation without manipulation

As mentioned, we need to worry when individuals are allowed to self-select
This means that a lot of thought has to go into the *randomization phase*Randomization into treatment groups has to be manipulated by someone
But what about effect of *immutable characteristics* such as race, gender, etc.?

Quasi Experiments

Quasi-experiments: randomization happens by "accident"

- Differences in Differences
- Regression Discontinuity Design
- Instrumental variables

Randomized Controlled Trials

Randomized controlled trials (RCT): randomization done by researcher

- Survey experiments
- Field experiments

Note: difficult to say one is strictly better than the other. Randomization can be impractical and/or unethical.

External & internal validity

Internal validity: Refers to the validity of causal conclusions

External validity: Refers to the extent to which the conclusions of a particular study can be generalized beyond a particular setting

RCTs - external and internal validity

- Kosuke Imai (2016): There is tradeoff.
- Cyrus Samii (2016): No such tradeoff.

Observational study

In many cases, social scientists are unable to randomize treatment assignment for ethical or logistic reasons

Observational study: No random manipulation of treatment

Strategy: Statistical control (control variables, fixed effects, matching, etc)

Risks: selection & confounding bias and endogeneity.

Case: Racial Discrimination in the Labor Market

Does racial discrimination exist in the labor market?

Experiment: In response to newspaper ads, researchers send out resumes of fictitious job candidates, varying only the names of the job applicants while leaving all other information in the resumes unchanges

Names were randomized between stereotypically black- and white-sounding names (Lakisha, Jamal, Emily, Greg, etc.)

Case: Racial Discrimination in the Labor Market (2)

```
In [38]: gh_raw = "https://raw.githubusercontent.com/"
    user = "kosukeimai/"
    repo = 'qss/'
    branch = "master/"
    filepath = "CAUSALITY/resume.csv"
    url = gh_raw + user + repo + branch + filepath

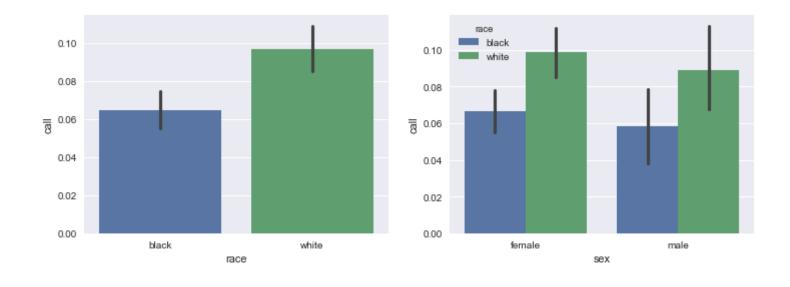
df = pd.read_csv(url,dtype={'race':'category','sex':'category'})
```

Case: Racial Discrimination in the Labor Market (3)

Can we use a boxplot? No boxplot not good for binary data.

```
In [3]: f, ax = plt.subplots(1,2,figsize=(12,4))
    sns.barplot(x='race', y='call', data=df, ax=ax[0])
    sns.barplot(x='sex', hue='race', y='call', data=df, ax=ax[1])
```

Out[3]: <matplotlib.axes._subplots.AxesSubplot at 0x1d1e56a24e0>



Case: Racial Discrimination in the Labor Market (4)

```
In [39]: model = smf.ols(formula='call~race*sex', data=df)
    results = model.fit()
    results.summary()
```

Out[39]: OLS Regression Results

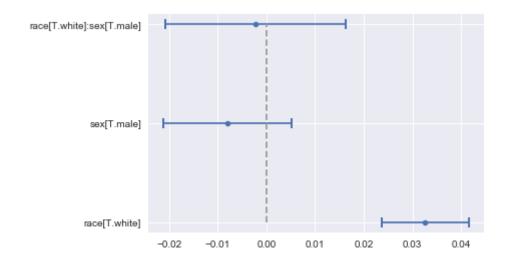
Dep. Variable:	call	R-squared:	0.004
Model:	OLS	Adj. R-squared:	0.003
Method:	Least Squares	F-statistic:	5.973
Date:	Mon, 14 Aug 2017	Prob (F-statistic):	0.000464
Time:	09:40:34	Log-Likelihood:	-561.75
No. Observations:	4870	AIC:	1131.
Df Residuals:	4866	BIC:	1157.
Df Model:	3		
Covariance Type:	nonrobust		

	coef	std err	t	P> t	[0.025	0.975]
Intercept	0.0663	0.006	10.595	0.000	0.054	0.079
race[T.white]	0.0326	0.009	3.677	0.000	0.015	0.050
sex[T.male]	-0.0080	0.013	-0.606	0.544	-0.034	0.018
race[T.white]:sex[T.male]	-0.0022	0.018	-0.121	0.904	-0.038	0.034

Omnibus:	2968.362	Durbin-Watson:	1.441
----------	----------	----------------	-------

Case: Racial Discrimination in the Labor Market (5)

Out[5]: [<matplotlib.lines.Line2D at 0x1d1e65c9c50>]



Machine learning

Topics in machine learning

Supervised Learning: Models designed to infer a relationship between input and labeled training data. These models are used for **prediction**. Examples: OLS, logistic reg.

Unsupervised Learning: Models designed to infer a relationship from **unlabeled** training data. This may involve clustering, dimensionality reduction and more.

Supervised machine learning

Prediction

Many policy problems are not about causality but rather about prediction

Sometimes called *prediction policy problems*

- How many people will sign up for Obamacare?
- Who will win the U.S general election in November?
- Who should the Department of Economics hire in the future?

Who predicts?

- Local governments -> crime, childcare usage, pension payments etc.
- FB/GOOG/AMZN/NTFL/etc. > estimating 'preferences' to improve customer experience / sales
 - ads, status updates, music, movies, news
- Insurance companies -> what your risk of death is
- Stock traders > to trade
- Robots -> understanding their environment (e.g. self-driving cars)
- You? -> will Social Data Science be a fun/rewarding/interesting course to follow?

Why predict? Glory!



The Netflix Contest

Competition started in October 2006. Training data is ratings for 18K movies by 400K Netflix customers, each rating between 1 and 5

Training data is very sparse - about 98% missing

Objective is to predict the rating for a set of 1 million customer-movie pairs that are missing in the training data

Winner: Averaged 800 models

Why predict? Riches!



Improve Healthcare, Win \$3,000,000.

http://www.heritagehealthprize.com/c/hhp (http://www.heritagehealthprize.com/c/hhp)

Prediction problem types

Predicition problems are often described in terms of the data types they are predicting.

- The first is **regression** which uses numeric (continuous) variables.
- The second is **classification** which uses categorical (discrete) variables.

Examples?

Case: Predicting gender from body measures

What type of prediction problem is this? Classification.

• Classification!

Case: Predicting gender from body measures (2)

```
In [43]: | print(body.head())
          Gender Height
                                 Weight Male
            Male 189.048364 109.819678 1.0
         1 Male 176.081674 73.688955 1.0
         2 Male 189.721870 96.584348 1.0
         3 Male 183.631305 99.899282 1.0
         4 Male 178.897397 93.682809
                                          1.0
In [40]:
         gh_raw = "https://raw.githubusercontent.com/"
         user = "johnmyleswhite/"
         repo = 'ML for Hackers/'
         branch = "master/"
         filepath = "02-Exploration/data/01 heights weights genders.csv"
         url = gh raw + user + repo + branch + filepath
         body = pd.read csv(url)
         body['Male'] = (body.Gender=='Male').astype(float) # Binary variable
         body.Height = body.Height*2.56 # convert inches to cm
         body.Weight = body.Weight*0.454 # convert pounds to kg
```

Case: Predicting gender from body measures (3)

Do we already know any machine learning models?

```
In [7]: from sklearn.linear_model import LogisticRegression

X = body[['Weight', 'Height']] # features
y = body.Male # labels

# make classifier and fit model
clf = LogisticRegression().fit(X, y)

# parameter estimates
pd.Series(clf.coef_[0], index=['Weight', 'Height'])
Out[7]: Weight  0.433517
```

Out[7]: Weight 0.433517 Height -0.186886 dtype: float64

Case: Predicting gender from body measures (4)

Logit estimates

$$P(Y_i=1|X_i=x_i)=rac{1}{1+e^{-x_ieta}}$$

This probability is .5 when $x_i\beta=0$. Thus we can classify predicted gender based on height and weight with the following rule:

$$\hat{y} = egin{cases} 1 & ext{if } x_i eta \geq 0, \ 0 & ext{otherwise} \end{cases}$$

Classifier threshold:

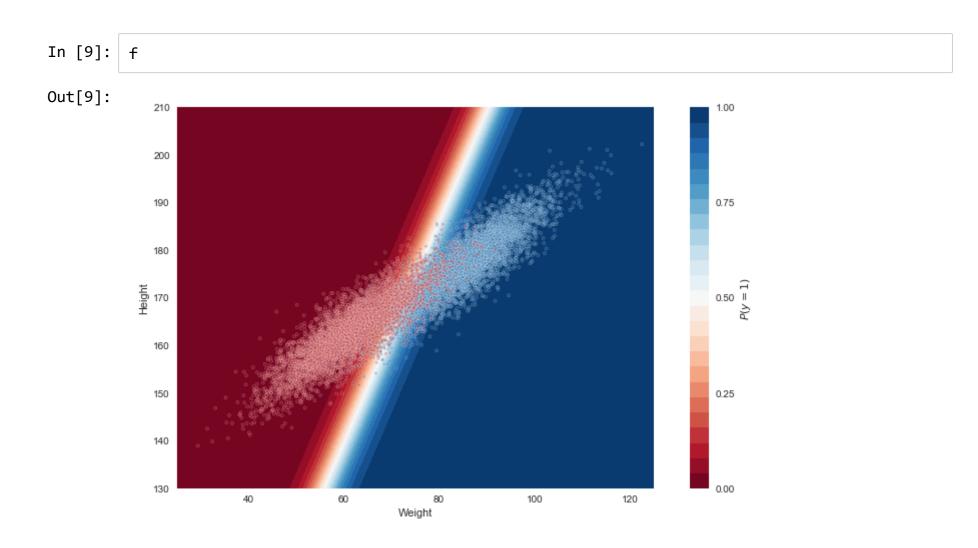
$$H = rac{-lpha - eta_W W}{eta_H}$$

Case: Predicting gender from body measures (5)

AttributeError: 'numpy.ndarray' object has no attribute 'iloc'

Case: Predicting gender from body measures (6)

Decision boundary



Case: Predicting gender from body measures (7)

Another model: nearest neighbor

```
In [45]: from sklearn.ensemble import RandomForestClassifier
from sklearn.neighbors import KNeighborsClassifier

X = body[['Weight', 'Height']]
y = body.Male

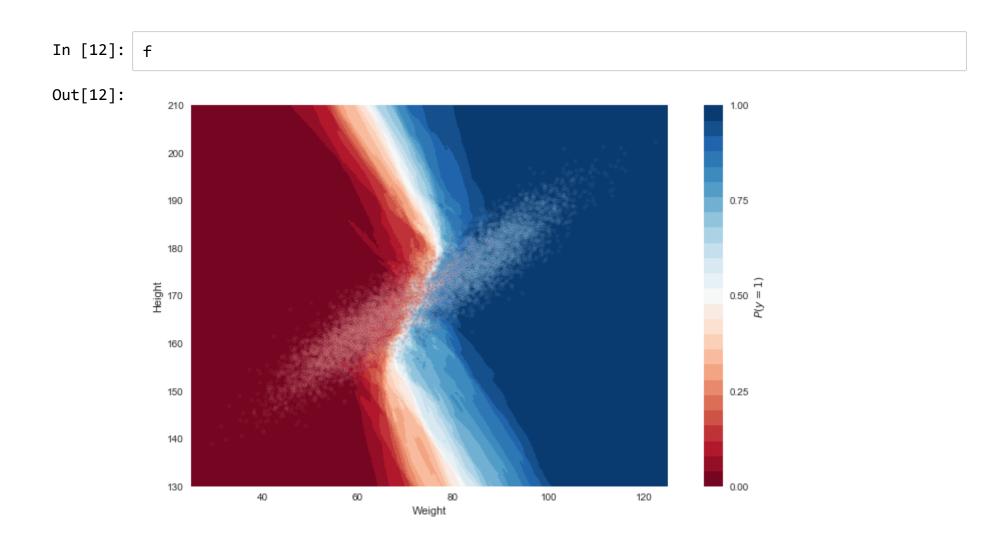
# make model on data - fifty nearest neighbors
clf = KNeighborsClassifier(n_neighbors=50).fit(X, y)
```

Case: Predicting gender from body measures (8)

Computing nearest neighbor decision boundary

Case: Predicting gender from body measures (9)

Decision boundary: non-linear



Bias and variance

Are OLS and logistic regression good for prediction?

The bias-variance tradeoff

OLS is designed to minimize *in sample error*: the error rate you get on the same data set you used to build your predictor.

$$rg\min_{eta} \sum_{i=1}^n (y_i - \hat{y}_i)^2 = rg\min_{eta} (V(\hat{f}\left(x_0
ight)) + \sigma^2)$$

But for prediction we are interested in minimizing *out of sample error*: the error rate you get on a new data set

Prediction

Too see this, consider a prediction at a new point (out-of-sample), x_0 . Our prediction for y_0 is then $\hat{f}\left(x_0\right)$ and the mean squared error (MSE) can be decomposed as

$$\mathbb{E}[(y_0 - \hat{f}(x_0))^2] = \underbrace{\mathbb{E}[\hat{f}(x_0) - f(x_0)]}_{Bias(\hat{f}(x))}^2 + \underbrace{\mathbb{E}[\hat{f}(x_0)^2] - \mathbb{E}[\hat{f}(x_0)]^2}_{Var(\hat{f}(x))} + \sigma^2$$

By ensuring zero bias within sample, OLS picks a solution which not be optimal for prediction

• in many cases we can lower variance while increasing bias a little.

Bias and variance

What do we mean by the variance and bias of an estimator?

- ullet Bias: Comes from using erroneous model assumptions, e.g. fitting non-linear fct. f with linear fct. \hat{f} .
 - Can lead to missing relevant patterns in data, i.e. underfitting.
- Variance: Refers to model complexity. If the model is too complex then small changes to the data will cause the solution to change a lot.
 - Can lead to finding spurious patterns in data, i.e. overfitting.

Machine learning techniques were developed specifically to maximize prediction performance by providing an empirical way to make this bias-variance trade off

Bias and variance (2)

So why do we care about bias?

- By not modelling bias: allows inference, i.e. testing hypotheses! (model parameters converge to true parameters) ~ interested in $\hat{\beta}$
- By modelling bias: allows better predictive models as they trade off bias and variance. Interested in \hat{y}

Out-of-sample measures

Key concepts

- Training data: where we estimate our model
- Test data: where we evaluate the model's accuracy

Error

Statistical learning models are designed to minimize *out of sample error*: the error rate you get on a new data set

Key ideas

- Out of sample error is what you care about
- In sample error < out of sample error
- The reason is overfitting (matching your algorithm to the data you have)

Error measures (continuous variables)

Mean absolute error (MAE):

$$MAE = rac{1}{n}\sum_{i=1}^n |\hat{y}_i - y_i|$$

Mean squared error (MSE):

$$MSE = rac{1}{n} \sum_{i=1}^n (\hat{y}_i - y_i)^2$$

Root mean squared error (RMSE):

$$\sqrt{MSE}$$

Question: what is the difference?

Case: Longevity

```
In [14]: gh_raw = "https://raw.githubusercontent.com/"
    user = "johnmyleswhite/"
    repo = "ML_for_Hackers/"
    branch = "master/"
    filepath = "05-Regression/data/longevity.csv"
    url = gh_raw + user + repo + branch + filepath
    longevity = pd.read_csv(url)
    print(longevity.head())
```

	Smokes	AgeAtDeath
0	1	75
1	1	72
2	1	66
3	1	74
4	1	69

Case: Longevity (2)

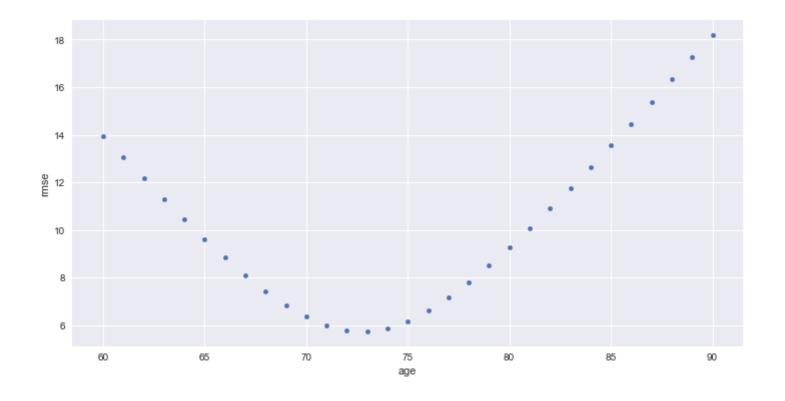
```
In [59]: y true = longevity.AgeAtDeath
          def rmse_year(y):
              Takes as input: year (y)
              Outputs: root mean squared of quessing y
             y pred = [y]*len(longevity)
              return np.sqrt(mse(y_true, y_pred))
          # normal for loop
          rmse_years = []
          for y in range(60,91):
              rmse years.append((y, rmse year(y)))
          # list comprehenseion:
          rmse_years = [(y, rmse_year(y)) for y in range(60,91)]
          rmse data = pd.DataFrame(data = rmse_years,
                                   columns = ['age', 'rmse'])
          # print ('Best guess:', rmse_data.set_index('year').rmse.idxmin())
          #rmse data.plot.scatter('age', 'rmse')
```

Case: Longevity (3)

```
In [58]: f,ax = plt.subplots(figsize=(12,6))
    print ('Best guess:', rmse_data.set_index('age').rmse.idxmin())
    rmse_data.plot.scatter('age', 'rmse', ax=ax)
```

Best guess: 73

Out[58]: <matplotlib.axes._subplots.AxesSubplot at 0x1d182a17be0>



Cross validation (CV)

Test and training data

Accuracy on the training set (resubstitution accuracy) does not capture bias and therefore is optimistic. A better estimate comes from an independent set (test set accuracy). Strategy:

- Use share of observations for training
- Use other of observations for testing model (out-of-sample)

So we estimate the test data accuracy with the model calibrated on training data.

Data split

Why not just divide data randomly the data into a test and training set?

Two drawbacks

- 1. RMSE is very sensitive to which observations are used for test and training.
- 2. RMSE is artificially large as not all observations are used for training model (model becomes more accurate for more observations)

One very useful refinement of the test-training data approach is *cross-validation* use multiple splits.

K-fold Cross Validation

- 1. Divide the data into k roughly equal subsets and label them $s=1,\ldots,k$.
- 2. Fit your model using the k-1 subsets other than subset s
- 3. Predict for subset s and calculate RMSE
- 4. Stop if s=k, otherwise increment s by 1 and continue

The k fold CV estimate is computed by averaging the mean squared errors ($ext{MSE}_1, \dots, ext{MSE}_k$)

$$ext{CV}_k = rac{1}{k} \sum_{i=1}^k ext{MSE}_i.$$

Common choices for k are 3, 5 and 10.

CV can (and should) be used both to decide hyperparameters and to report goodness-of-fit measures.

K-fold Cross Validation (2)

<img src="http://sebastianraschka.com/images/faq/evaluate-a-model/k-fold.png
(http://sebastianraschka.com/images/faq/evaluate-a-model/k-fold.png)", width="1000" >

Fitting polynomial

Polyonomial: $f(x) = 2 + 8 * x^4$

Try models of higher and higher polynomials. Iteration n: $y = \sum_{k=0}^n (eta_k \cdot x^k) + arepsilon$.

Fitting polynomial (2)

Compute within sample error for OLS

order 1 order 2 order 3

1

```
In [84]: from sklearn.linear_model import LinearRegression

X_s = {}
    rmse_in_sample = []

for i in range(1,10): # for each order 1-9
        X_s['order '+str(i)]= x_range**i # add polynomial of order i
        X = pd.concat(X_s,axis=1) # concatename polynomials of order 1,..,i

        model = LinearRegression().fit(X,y) # fit linear regression model
        y_pred = model.predict(X) # make predictions within-sample
        rmse_in_sample.append(np.sqrt(mse(y, y_pred)))

print(X.iloc[:,:5].head(2))
```

order 4

0.00 0.0000 0.000000 0.000000e+00 0.000000e+00 0.02 0.0004 0.000008 1.600000e-07 3.200000e-09

order 5

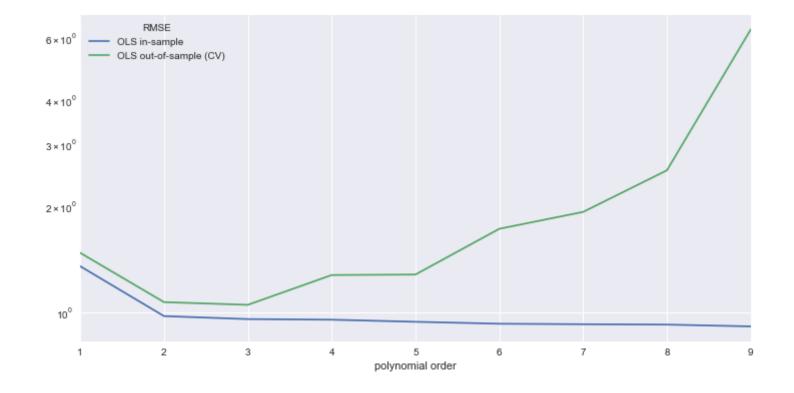
Fitting polynomial (3)

Compute out-of-sample errors for OLS

```
In [109]: | from sklearn.model_selection import KFold
          kf = KFold(n splits=10, random state=123)
          X s = \{\}
          rmse CV = []
           coef CV = []
           for i in range(1,10):
              X s['order '+str(i)] = x range**i
              X = pd.concat(X s, axis=1)
               rmse fold = []
               coef fold = []
               # cross validation loop
               for train index, test index in kf.split(X):
                  X train, X test = X.iloc[train index], X.iloc[test index]
                  y train, y test = y.iloc[train index], y.iloc[test index]
                   model = LinearRegression().fit(X train,y train)
                  y_pred = model.predict(X test)
                   rmse = np.sqrt(mse(y test, y pred))
                   rmse fold.append(rmse)
                   coef fold.append(pd.Series(model.coef , index=range(1,i+1)))
               rmse CV.append(np.mean(rmse fold))
               coef CV.append(pd.concat(coef fold,1).T.mean().rename(i))
```

Fitting polynomial (4)

How does in-sample and out-of-sample estimates of RMSE diverse?



Fitting polynomial (5)

Why does in-sample and out-of-sample estimates of RMSE diverse? Well, the coefficient of OLS are increasingly mis-estimated for higher and higher number of variables.

In [111]: pd.concat(coef_CV,1).T

Out[111]:

	1	2	3	4	
1	6.234355	NaN	NaN	NaN	NaN
2	-6.146667	12.590554	NaN	NaN	NaN
3	-0.781354	-1.104807	9.249710	NaN	NaN
4	-6.394433	22.107885	-25.078074	16.501495	NaN
5	7.678056	-73.795322	227.908655	-266.336210	112.593443
6	-24.034620	197.092328	-785.577926	1574.624054	-1482.858265
7	-26.234597	139.009441	-235.967168	-318.984810	1647.278049
8	-2.480596	-149.025175	1496.517741	-6011.772182	12283.632851
9	-174.311112	2248.717158	-16219.517439	69637.464867	-182832.8811

Regularization

Why do we regularize?

• To avoid overfitting and thus have better predictions

How do we regularize?

We make models which are less complex by reducing the number and/or size of the coefficients.

Regularization (2)

What does regularization look like?

We add a penalty term our optimization procedure:

$$rg\min_{eta} \underbrace{E[(y_0 - \hat{f}(x_0))^2]}_{ ext{MSE}} + \underbrace{\lambda \cdot R(eta)}_{ ext{penalty}}$$

Introduction of penalties implies that increased model complexity has to be met with high increases precision of estimates.

Regularization (3)

What are some used penalty functions?

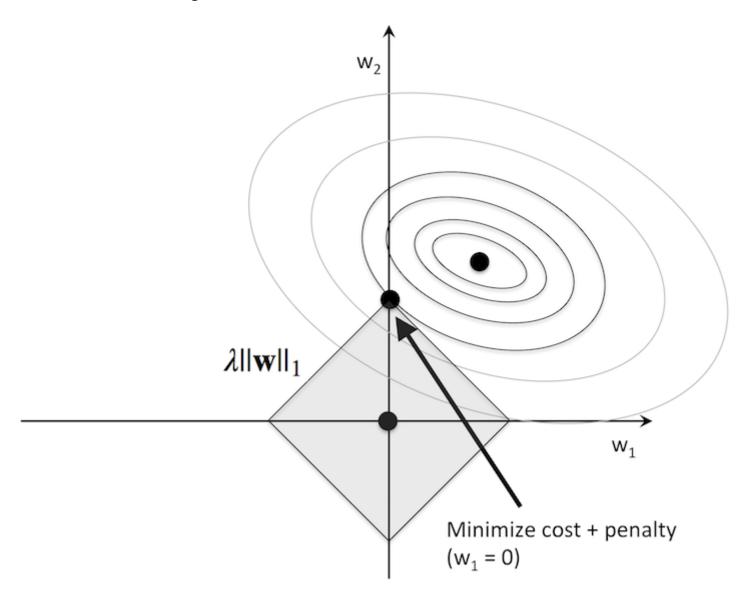
The two most common penalty functions are L1 and L2 regularization.

- L1 regularization (*Lasso*): $R(eta) = \sum_{j=1}^p |eta_j|$
 - \blacksquare Makes coefficients sparse, i.e. selects variables by removing some (if λ is high)
- L2 regularization (*Ridge*): $R(\beta) = \sum_{j=1}^p \beta_j^2$
 - Reduce coefficient size
 - Fast due to analytical solution

To note: The Elastic Net uses a combination of L1 and L2 regularization.

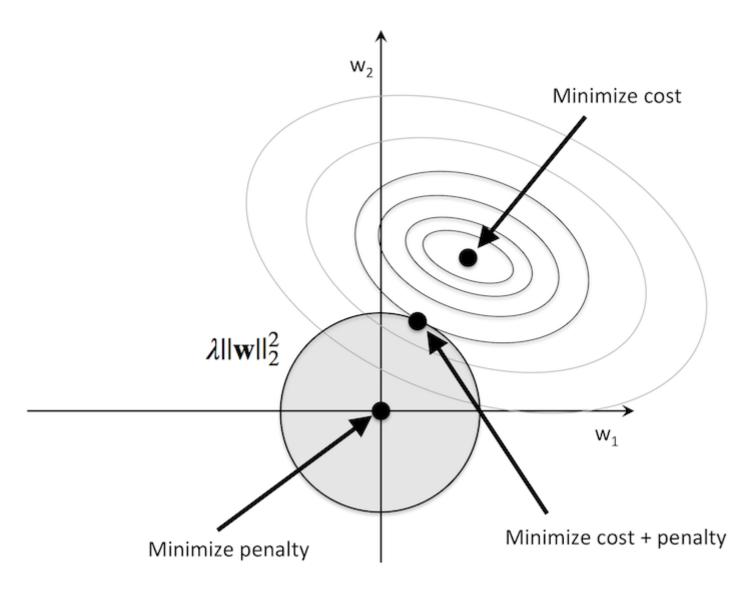
Regularization (4)

How the Lasso (L1 reg.) deviates from OLS



Regularization (5)

How the Ridge regression (L2 reg.) deviates from OLS



Models for supervised machine learning

Model overview

Parametric models

- regression models
 - unbiased: OLS
 - biased: *Lasso* (L1), *Ridge* (L2) (regulariation)
- classifier
 - unbiased: logistic

Other models

- random forest
- nearest neighbor
- neural networks

Fitting polynomial (6)

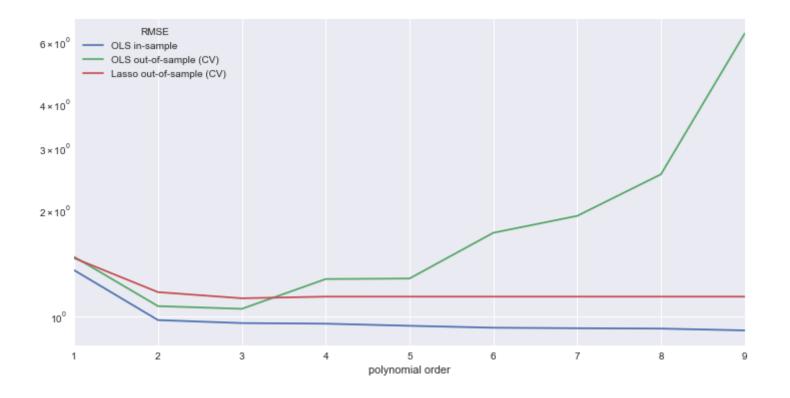
Training the model with Lasso

```
In [87]: | from sklearn.model_selection import KFold
         from sklearn.linear_model import Lasso
         kf = KFold(n splits=10, random state=123)
         X s = \{\}
         rmse_CV_L = []
         for i in range(1,10):
             X s['order '+str(i)] = x range**i
             X = pd.concat(X s, axis=1)
              rmse fold = []
              # cross validation loop
              for train index, test index in kf.split(X):
                 X train, X test = X.iloc[train index], X.iloc[test index]
                 y train, y test = y.iloc[train index], y.iloc[test index]
                 # use Lasso with Lambda = .05
                 y pred = Lasso(alpha=0.05)
                              .fit(X train, y train)
                              .predict(X test)
                  rmse = np.sqrt(mse(y_test, y_pred))
                  rmse fold.append(rmse)
              rmse CV L.append(np.mean(rmse fold))
```

Fitting polynomial (7)

Lasso vs OLS performance

```
In [75]: f,ax = plt.subplots(figsize=(12,6))
    rmse_df['Lasso out-of-sample (CV)'] = rmse_CV_L
    rmse_df.plot(ax=ax)
    ax.set_yscale('log')
```



Fitting polynomial (8)

Tuning The Lasso

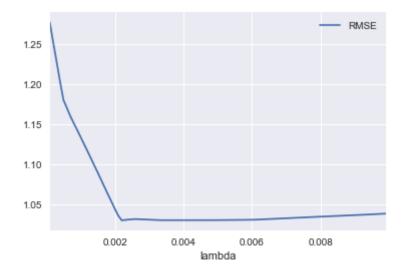
```
In []: X = pd.concat(X s, axis=1)
         rmse CV lambda = []
         coef CV lambda = []
         for 1 in np.arange(.0001,.01,.0001): # loop over different values of lambda
             rmse fold = []
             for train index, test index in kf.split(X):
                 X train, X test = X.iloc[train index], X.iloc[test index]
                 y train, y test = y.iloc[train index], y.iloc[test index]
                 model = Lasso(alpha=1).fit(X train,y train)
                 y pred = model.predict(X test)
                 rmse = np.sqrt(mse(y test, y pred))
                 rmse fold.append(rmse)
             coef CV lambda.append(model.coef )
             rmse CV lambda.append([1, np.mean(rmse fold)])
```

Fitting polynomial (9)

We search the λ grid : 0.0001-0.01 to find the optimal λ parameter

```
In [89]: rmse_lambda_df = pd.DataFrame(rmse_CV_lambda,columns=['lambda', 'RMSE']).set_index('lambda')
    rmse_lambda_df.plot()
```

Out[89]: <matplotlib.axes._subplots.AxesSubplot at 0x1d1801e5470>



Fitting polynomial (10)

Model for optimal lambda

```
In [34]: lambda_opt = rmse_lambda_df.idxmin()
lambda_opt

Out[34]: RMSE    0.0022
dtype: float64
```

Parameters for optimal lambda

```
In [78]: coefs =
   pd.DataFrame(coef_CV_lambda,columns=range(1,10),index=np.arange(.0001,.01,.0001))
   print(coefs.loc[lambda_opt])
1 2 3 4 5 6 7 8 9
```

0.0022 -0.077694 0.0 6.793418 0.0 0.0 -0.0 -0.0 -0.0 -0.0

Summary causality

Selection bias: Issue for observational studies where treatment is correlated with baseline outcome.

Randomization: Enactment of treatments that are assigned randomly and thus do not suff selection biases.

Summary supervised learning

Prediction/postdiction: Application of model to estimate response/output associated with input.

Bias-variance tradeoff: There exist models beside OLS which can improve better at out-of-sample predictions, however, they have biased parameter estimates.

Prediction types:

- when the response is numeric (continuous) the problem is called *regression*
- when response is categorical (discrete) the problem is called classification

MAE/RMSE: measures of prediction accuracy for regression problems

Cross validation: Split data in test and training data. Train model on training data, test it on test data.

Regularization: A technique used to model bias in an attempt to solve overfitting problems