

Looping and
iteration

The INFDEV
Team @ HR

Introduction

Repeated
behaviors

Repeating
behaviors in
Python

Reasoning
about `while`

Termination
(or lack
thereof)

Exponential
explosion of
potential
control-paths

Assignment

Looping and iteration

The INFDEV Team @ HR

Hogeschool Rotterdam
Rotterdam, Netherlands

Looping and
iteration

The INFDEV
Team @ HR

Introduction

Repeated
behaviors

Repeating
behaviors in
Python

Reasoning
about `while`

Termination
(or lack
thereof)

Exponential
explosion of
potential
control-paths

Assignment

Introduction

Looping and
iteration

The INFDEV
Team @ HR

Introduction

Repeated
behaviors

Repeating
behaviors in
Python

Reasoning
about `while`

Termination
(or lack
thereof)

Exponential
explosion of
potential
control-paths

Assignment

Lecture topics

- Repeated behaviors
- `while` statements and their semantics
- Expressive power of `while`
- Termination and infinite iteration
- Explosion of states with `while`

Looping and
iteration

The INFDEV
Team @ HR

Introduction

Repeated
behaviors

Repeating
behaviors in
Python

Reasoning
about `while`

Termination
(or lack
thereof)

Exponential
explosion of
potential
control-paths

Assignment

Repeated behaviors

Looping and
iteration

The INFDEV
Team @ HR

Introduction

Repeated
behaviors

Repeating
behaviors in
Python

Reasoning
about *while*

Termination
(or lack
thereof)

Exponential
explosion of
potential
control-paths

Assignment

Repeated behaviors

- Sometimes running code just once is not enough
- We can *loop* execution of a block of code until some *condition* is met
- Extreme increase in expressive power

Looping and
iteration

The INFDEV
Team @ HR

Introduction

Repeated
behaviors

Repeating
behaviors in
Python

Reasoning
about while

Termination
(or lack
thereof)

Exponential
explosion of
potential
control-paths

Assignment

Repeated behaviors

- While *there are hostile aliens*
- Do *attack an alien*

Looping and iteration

The INFDEV
Team @ HR

Introduction

Repeated
behaviors

Repeating
behaviors in
Python

Reasoning
about while

Termination
(or lack
thereof)

Exponential
explosion of
potential
control-paths

Assignment

Repeated behaviors

- Loops can solve very big problems
- Each step of the loop removes a part of the problem
- We typically stop when all parts of the problem have been removed

Looping and
iteration

The INFDEV
Team @ HR

Introduction

Repeated
behaviors

Repeating
behaviors in
Python

Reasoning
about while

Termination
(or lack
thereof)

Exponential
explosion of
potential
control-paths

Assignment

Breaking problems up

- Problem: **kill all aliens**
- Problem piece: **a single alien to be killed**
- Solution piece: **attack a single alien**
- Termination condition: **there are no more aliens**

Looping and
iteration

The INFDEV
Team @ HR

Introduction

Repeated
behaviors

Repeating
behaviors in
Python

Reasoning
about while

Termination
(or lack
thereof)

Exponential
explosion of
potential
control-paths

Assignment

Breaking problems up

- Of course loops can be combined with each other
- This means that we can *cascade* repetition
- This is the building block of *intelligent decisions* in our programs

Looping and
iteration

The INFDEV
Team @ HR

Introduction

Repeated
behaviors

Repeating
behaviors in
Python

Reasoning
about while

Termination
(or lack
thereof)

Exponential
explosion of
potential
control-paths

Assignment

Breaking problems up

- While *there are hostile alien armies*
 - Do *pick an alien army*
 - While *there are aliens in the army*
 - Do *attack an alien*

Looping and
iteration

The INFDEV
Team @ HR

Introduction

Repeated
behaviors

Repeating
behaviors in
Python

Reasoning
about `while`

Termination
(or lack
thereof)

Exponential
explosion of
potential
control-paths

Assignment

Repeating behaviors in Python

Repeating behaviors in Python

Looping and
iteration

The INFDEV
Team @ HR

Introduction

Repeated
behaviors

Repeating
behaviors in
Python

Reasoning
about while

Termination
(or lack
thereof)

Exponential
explosion of
potential
control-paths

Assignment

while

- Python offers built-in facilities for repetition
- `while` statement
- We can repeat execution of a block of code

Repeating behaviors in Python

Looping and
iteration

The INFDEV
Team @ HR

Introduction

Repeated
behaviors

Repeating
behaviors in
Python

Reasoning
about while

Termination
(or lack
thereof)

Exponential
explosion of
potential
control-paths

Assignment

while

- The general form is `while CONDITION: BODY` (w_{CB})
- If the condition is true, then we jump to the beginning of BODY, otherwise we jump to the end of the whole while

$$\left\{ \begin{array}{ll} (PC, S) \xrightarrow{w_{CB}} (firstLine(B), S) & \text{when } (PC, S) \xrightarrow{C} TRUE \\ (PC, S) \xrightarrow{w_{CB}} (skipAfter(B), S) & \text{when } (PC, S) \xrightarrow{C} FALSE \end{array} \right.$$

Repeating behaviors in Python

Looping and
iteration

The INFDEV
Team @ HR

Introduction

Repeated
behaviors

Repeating
behaviors in
Python

Reasoning
about while

Termination
(or lack
thereof)

Exponential
explosion of
potential
control-paths

Assignment

while

- Remember that Python is *indentation*-based
- White-spaces go at the beginning of some lines
- A more indented line is *within* a less indented line above

Repeating behaviors in Python

Looping and
iteration

The INFDEV
Team @ HR

Introduction

Repeated
behaviors

Repeating
behaviors in
Python

Reasoning
about while

Termination
(or lack
thereof)

Exponential
explosion of
potential
control-paths

Assignment

while

- Indentation specifies where the body begins and ends
- The general form of a `while` is thus:
 - `while COND:`
 - `newline`
 - **indentation**
 - `code of body`
 - **de-indentation**

A correct example

Looping and
iteration

The INFDEV
Team @ HR

Introduction

Repeated
behaviors

Repeating
behaviors in
Python

Reasoning
about while

Termination
(or lack
thereof)

Exponential
explosion of
potential
control-paths

Assignment

```
1 n = 64
2 i = 0
3 while n > 1:
4     n = n / 2
5     i = i + 1
```


An incorrect example

Looping and
iteration

The INFDEV
Team @ HR

Introduction

Repeated
behaviors

Repeating
behaviors in
Python

Reasoning
about while

Termination
(or lack
thereof)

Exponential
explosion of
potential
control-paths

Assignment

```
1 n = 64
2 i = 0
3 while n > 1:
4     n = n / 2
5     i = i + 1
```

Repeating behaviors in Python

Looping and
iteration

The INFDEV
Team @ HR

Introduction

Repeated
behaviors

Repeating
behaviors in
Python

Reasoning
about while

Termination
(or lack
thereof)

Exponential
explosion of
potential
control-paths

Assignment

while

- while statements eventually terminate (hopefully)
- if the condition evaluates to False, then we skip after the end of the while

After a while

Looping and
iteration

The INFDEV
Team @ HR

Introduction

Repeated
behaviors

Repeating
behaviors in
Python

Reasoning
about while

Termination
(or lack
thereof)

Exponential
explosion of
potential
control-paths

Assignment

```
1 n = 64
2 i = 0
3 while n > 1:
4     n = n / 2
5     i = i + 1
6 print(i)
```

After a while?

Looping and
iteration

The INFDEV
Team @ HR

Introduction

Repeated
behaviors

Repeating
behaviors in
Python

Reasoning
about while

Termination
(or lack
thereof)

Exponential
explosion of
potential
control-paths

Assignment

Without indentation, this:

```
1 n = 64
2 i = 0
3 while n > 1:
4     n = n / 2
5     i = i + 1
6 print(i)
```

would be indistinguishable from both:

1	n = 64	1	n = 64
2	i = 0	2	i = 0
3	while n > 1:	3	while n > 1:
4	n = n / 2	4	n = n / 2
5	i = i + 1	5	i = i + 1
6	print(i)	6	print(i)

Looping and
iteration

The INFDEV
Team @ HR

Introduction

Repeated
behaviors

Repeating
behaviors in
Python

Reasoning
about `while`

Termination
(or lack
thereof)

Exponential
explosion of
potential
control-paths

Assignment

Reasoning about `while`

Reasoning about while

Looping and
iteration

The INFDEV
Team @ HR

Introduction

Repeated
behaviors

Repeating
behaviors in
Python

Reasoning
about while

Termination
(or lack
thereof)

Exponential
explosion of
potential
control-paths

Assignment

while

- while effectively rewrites the code to become as long as the problem needs
- Until run-time, we are not really sure how long the code will become

Example while's

Looping and
iteration

The INFDEV
Team @ HR

Introduction

Repeated
behaviors

Repeating
behaviors in
Python

Reasoning
about while

Termination
(or lack
thereof)

Exponential
explosion of
potential
control-paths

Assignment

What values of `n` will we print?

```
1 i = 0
2 j = 1
3 n = 0
4 while i < 10:
5     i = i + 1
6     n = n + j
7     print(n),
```

Example while's

Looping and
iteration

The INFDEV
Team @ HR

Introduction

Repeated
behaviors

Repeating
behaviors in
Python

Reasoning
about while

Termination
(or lack
thereof)

Exponential
explosion of
potential
control-paths

Assignment

What values of `n` will we print?

```
1 i = 0
2 j = 1
3 n = 0
4 while i < 10:
5     i = i + 1
6     n = n + j
7     print(n),
```

1 2 3 4 5 6 7 8 9 10

Example while's

Looping and
iteration

The INFDEV
Team @ HR

Introduction

Repeated
behaviors

Repeating
behaviors in
Python

Reasoning
about while

Termination
(or lack
thereof)

Exponential
explosion of
potential
control-paths

Assignment

What values of `n` will we print?

```
1 i = 0
2 j = 2
3 n = 0
4 while i < 10:
5     i = i + 1
6     n = n + j
7     print(n),
```

Example while's

Looping and
iteration

The INFDEV
Team @ HR

Introduction

Repeated
behaviors

Repeating
behaviors in
Python

Reasoning
about while

Termination
(or lack
thereof)

Exponential
explosion of
potential
control-paths

Assignment

What values of `n` will we print?

```
1 i = 0
2 j = 2
3 n = 0
4 while i < 10:
5     i = i + 1
6     n = n + j
7     print(n),
```

2 4 6 8 10 12 14 16 18 20

Reasoning about while

Looping and
iteration

The INFDEV
Team @ HR

Introduction

Repeated
behaviors

Repeating
behaviors in
Python

Reasoning
about while

Termination
(or lack
thereof)

Exponential
explosion of
potential
control-paths

Assignment

while

- Each iteration produces new values of the variables
- These new values are then fed back into the next iteration
- Eventually these cause the condition to become false
 - Or the program runs forever and never produces a result

Reasoning about while

Looping and
iteration

The INFDEV
Team @ HR

Introduction

Repeated
behaviors

Repeating
behaviors in
Python

Reasoning
about while

Termination
(or lack
thereof)

Exponential
explosion of
potential
control-paths

Assignment

while

- Each iteration produces new values of the variables
- These new values are then fed back into the next iteration
- Eventually these cause the condition to become false
 - Or the program runs forever and never produces a result
 - We'd rather not have this one

Example while's

Looping and
iteration

The INFDEV
Team @ HR

Introduction

Repeated
behaviors

Repeating
behaviors in
Python

Reasoning
about while

Termination
(or lack
thereof)

Exponential
explosion of
potential
control-paths

Assignment

i	j	n
0	2	0

```
1 while i < 10:  
2     i = i + 1  
3     n = n + j  
4     print(n),
```

Example while's

Looping and
iteration

The INFDEV
Team @ HR

Introduction

Repeated
behaviors

Repeating
behaviors in
Python

Reasoning
about while

Termination
(or lack
thereof)

Exponential
explosion of
potential
control-paths

Assignment

i	j	n
0	2	0

```
1 while i < 10:  
2     i = i + 1  
3     n = n + j  
4     print(n),
```

i	j	n
1	2	2

Example while's

Looping and
iteration

The INFDEV
Team @ HR

Introduction

Repeated
behaviors

Repeating
behaviors in
Python

Reasoning
about while

Termination
(or lack
thereof)

Exponential
explosion of
potential
control-paths

Assignment

i	j	n
1	2	2

```
1 while i < 10:  
2     i = i + 1  
3     n = n + j  
4     print(n),
```

Example while's

Looping and
iteration

The INFDEV
Team @ HR

Introduction

Repeated
behaviors

Repeating
behaviors in
Python

Reasoning
about while

Termination
(or lack
thereof)

Exponential
explosion of
potential
control-paths

Assignment

i	j	n
1	2	2

```
1 while i < 10:  
2     i = i + 1  
3     n = n + j  
4     print(n),
```

i	j	n
2	2	4

Example while's

Looping and
iteration

The INFDEV
Team @ HR

Introduction

Repeated
behaviors

Repeating
behaviors in
Python

Reasoning
about while

Termination
(or lack
thereof)

Exponential
explosion of
potential
control-paths

Assignment

i	j	n
2	2	4

```
1 while i < 10:  
2     i = i + 1  
3     n = n + j  
4     print(n),
```

Example while's

Looping and
iteration

The INFDEV
Team @ HR

Introduction

Repeated
behaviors

Repeating
behaviors in
Python

Reasoning
about while

Termination
(or lack
thereof)

Exponential
explosion of
potential
control-paths

Assignment

i	j	n
2	2	4

```
1 while i < 10:  
2     i = i + 1  
3     n = n + j  
4     print(n),
```

i	j	n
3	2	6

Example while's

Looping and
iteration

The INFDEV
Team @ HR

Introduction

Repeated
behaviors

Repeating
behaviors in
Python

Reasoning
about while

Termination
(or lack
thereof)

Exponential
explosion of
potential
control-paths

Assignment

After k iterations (for $k < 10$):

i	j	n
k	2	$2 * k$

```
1 while i < 10:  
2     i = i + 1  
3     n = n + j  
4     print(n),
```

Example while's

Looping and iteration

The INFDEV
Team @ HR

Introduction

Repeated behaviors

Repeating behaviors in Python

Reasoning about while

Termination (or lack thereof)

Exponential explosion of potential control-paths

Assignment

After k iterations (for $k < 10$):

i	j	n
k	2	$2 * k$

```
1 while i < 10:
2     i = i + 1
3     n = n + j
4     print(n),
```

i	j	n
$k+1$	2	$2 * k + 2$

Example while's

Looping and
iteration

The INFDEV
Team @ HR

Introduction

Repeated
behaviors

Repeating
behaviors in
Python

Reasoning
about while

Termination
(or lack
thereof)

Exponential
explosion of
potential
control-paths

Assignment

After k iterations (for $k = 10$):

i	j	n
10	2	20

```
1 while i < 10:  
2     i = i + 1  
3     n = n + j  
4     print(n),
```

Example while's

Looping and
iteration

The INFDEV
Team @ HR

Introduction

Repeated
behaviors

Repeating
behaviors in
Python

Reasoning
about while

Termination
(or lack
thereof)

Exponential
explosion of
potential
control-paths

Assignment

After k iterations (for $k = 10$):

i	j	n
10	2	20

```
1 while i < 10:  
2     i = i + 1  
3     n = n + j  
4     print(n),
```

We jump to the first instruction **after** the while loop, and do not touch the state further.

i	j	n
10	2	20

Looping and iteration

The INFDEV
Team @ HR

Introduction

Repeated behaviors

Repeating behaviors in Python

Reasoning about while

Termination (or lack thereof)

Exponential explosion of potential control-paths

Assignment

Readability and termination

- The loop above is *well designed*
- All iterations produce a new piece of a logical series
 - (The j -th row of the table of multiplication)

Looping and
iteration

The INFDEV
Team @ HR

Introduction

Repeated
behaviors

Repeating
behaviors in
Python

Reasoning
about while

Termination
(or lack
thereof)

Exponential
explosion of
potential
control-paths

Assignment

Readability and termination

- After each iteration we know that we have i elements correctly computed
- After each iteration we know that we have $10-i$ elements still to compute
- When $i=10$ then we have $10-10$ elements still to compute
 - This is the **termination condition**
 - Since i keeps growing, we know that eventually the termination condition will be met

Reasoning about while

Looping and
iteration

The INFDEV
Team @ HR

Introduction

Repeated
behaviors

Repeating
behaviors in
Python

Reasoning
about while

Termination
(or lack
thereof)

Exponential
explosion of
potential
control-paths

Assignment

Nesting

- Loops can be nested
- A loop can be inside a loop (which can further be inside other loops)
- This makes it slightly harder to reason

Example nested while's

Looping and
iteration

The INFDEV
Team @ HR

Introduction

Repeated
behaviors

Repeating
behaviors in
Python

Reasoning
about while

Termination
(or lack
thereof)

Exponential
explosion of
potential
control-paths

Assignment

```
1 j = 1
2 while j <= 10:
3     i = 0
4     n = 0
5     while i < 10:
6         i = i + 1
7         n = n + j
8         print(n),
9         print("\t"),
10    j = j + 1
11    print("")
```

Example nested while's

We now know that the semantics of the inner loop is **print the j-th row of the table of multiplication**, so instead of reasoning on:

```
1 j = 1
2 while j <= 10:
3     i = 0
4     n = 0
5     while i < 10:
6         i = i + 1
7         n = n + j
8         print(n),
9         print("\t"),
10        j = j + 1
11        print("")
```

we reason on:

```
1 j = 1
2 while j <= 10:
3     print the j-th row of the table of multiplication
4     j = j + 1
5     print("")
```

Looping and
iteration

The INFDEV
Team @ HR

Introduction

Repeated
behaviors

Repeating
behaviors in
Python

Reasoning
about while

Termination
(or lack
thereof)

Exponential
explosion of
potential
control-paths

Assignment

Example nested while's

Looping and
iteration

The INFDEV
Team @ HR

Introduction

Repeated
behaviors

Repeating
behaviors in
Python

Reasoning
about while

Termination
(or lack
thereof)

Exponential
explosion of
potential
control-paths

Assignment

j	output
1	nothing

```
1 while j <= 10:  
2     print the j-th row of the table of multiplication  
3     j = j + 1  
4     print("")
```

Example nested while's

Looping and
iteration

The INFDEV
Team @ HR

Introduction

Repeated
behaviors

Repeating
behaviors in
Python

Reasoning
about while

Termination
(or lack
thereof)

Exponential
explosion of
potential
control-paths

Assignment

j	output
1	nothing

```
1 while j <= 10:  
2     print the j-th row of the table of multiplication  
3     j = j + 1  
4     print("")
```

j	output
2	1st row of table

Example nested while's

Looping and
iteration

The INFDEV
Team @ HR

Introduction

Repeated
behaviors

Repeating
behaviors in
Python

Reasoning
about while

Termination
(or lack
thereof)

Exponential
explosion of
potential
control-paths

Assignment

j	output
2	1st row of table

```
1 while j <= 10:  
2     print the j-th row of the table of multiplication  
3     j = j + 1  
4     print("")
```

Example nested while's

Looping and
iteration

The INFDEV
Team @ HR

Introduction

Repeated
behaviors

Repeating
behaviors in
Python

Reasoning
about while

Termination
(or lack
thereof)

Exponential
explosion of
potential
control-paths

Assignment

j	output
2	1st row of table

```
1 while j <= 10:  
2     print the j-th row of the table of multiplication  
3     j = j + 1  
4     print("")
```

j	output
3	1st and 2nd rows of table

Example nested while's

Looping and
iteration

The INFDEV
Team @ HR

Introduction

Repeated
behaviors

Repeating
behaviors in
Python

Reasoning
about while

Termination
(or lack
thereof)

Exponential
explosion of
potential
control-paths

Assignment

...

Example nested while's

Looping and
iteration

The INFDEV
Team @ HR

Introduction

Repeated
behaviors

Repeating
behaviors in
Python

Reasoning
about while

Termination
(or lack
thereof)

Exponential
explosion of
potential
control-paths

Assignment

Thus for all k 's such that $k \leq 10$:

j	output
k	first $k-1$ rows of table

```
1 while j <= 10:  
2     print the j-th row of the table of multiplication  
3     j = j + 1  
4     print("")
```

Example nested while's

Looping and
iteration

The INFDEV
Team @ HR

Introduction

Repeated
behaviors

Repeating
behaviors in
Python

Reasoning
about while

Termination
(or lack
thereof)

Exponential
explosion of
potential
control-paths

Assignment

Thus for all k 's such that $k \leq 10$:

j	output
k	first $k-1$ rows of table

```
1 while j <= 10:  
2     print the j-th row of the table of multiplication  
3     j = j + 1  
4     print("")
```

j	output
$k+1$	first k rows of table

Example nested while's

Eventually we get $j = 11$:

j	output	PC
11	first 10 rows of table	1

```
while j <= 10:
    print the j-th row of the table of multiplication
    j = j + 1
    print("")
...
```

1
2
3
4
5

Looping and
iteration

The INFDEV
Team @ HR

Introduction

Repeated
behaviors

Repeating
behaviors in
Python

Reasoning
about while

Termination
(or lack
thereof)

Exponential
explosion of
potential
control-paths

Assignment

Example nested while's

Looping and
iteration

The INFDEV
Team @ HR

Introduction

Repeated
behaviors

Repeating
behaviors in
Python

Reasoning
about while

Termination
(or lack
thereof)

Exponential
explosion of
potential
control-paths

Assignment

Eventually we get $j = 11$:

j	output	PC
11	first 10 rows of table	1

```
while j <= 10:
    print the j-th row of the table of multiplication
    j = j + 1
    print("")
...
```

j	output	PC
11	first 10 rows of table	5

Looping and
iteration

The INFDEV
Team @ HR

Introduction

Repeated
behaviors

Repeating
behaviors in
Python

Reasoning
about while

Termination
(or lack
thereof)

Exponential
explosion of
potential
control-paths

Assignment

Termination (or lack thereof)

Termination (or lack thereof)

Looping and
iteration

The INFDEV
Team @ HR

Introduction

Repeated
behaviors

Repeating
behaviors in
Python

Reasoning
about while

Termination
(or lack
thereof)

Exponential
explosion of
potential
control-paths

Assignment

Wait! It gets worse!

- It is not guaranteed that a loop will terminate
- A loop that does not terminate gets the program stuck forever
- It is a bit sad for the machine
- Care when designing loops is needed to prevent this

Termination (or lack thereof)

Looping and
iteration

The INFDEV
Team @ HR

Introduction

Repeated
behaviors

Repeating
behaviors in
Python

Reasoning
about while

Termination
(or lack
thereof)

Exponential
explosion of
potential
control-paths

Assignment

Care in the design

- A loop changes the state of the program many times
- A **good** loop changes the state in one **direction**
- Every step should bring us closer to the **final state**
- The condition defines the aspects of the final state

Example non terminating while

Looping and
iteration

The INFDEV
Team @ HR

Introduction

Repeated
behaviors

Repeating
behaviors in
Python

Reasoning
about while

Termination
(or lack
thereof)

Exponential
explosion of
potential
control-paths

Assignment

```
1 i = 1
2 while i > 0:
3     i = i + 1
4     print(i)
```

What is the issue here?

Example non terminating while

Looping and
iteration

The INFDEV
Team @ HR

Introduction

Repeated
behaviors

Repeating
behaviors in
Python

Reasoning
about while

Termination
(or lack
thereof)

Exponential
explosion of
potential
control-paths

Assignment

```
1 i = 1
2 while i > 0:
3     i = i + 1
4     print(i)
```

What is the issue here?

Iterations do not go **towards** the condition, but **away** from it.

Example non terminating while

Looping and
iteration

The INFDEV
Team @ HR

Introduction

Repeated
behaviors

Repeating
behaviors in
Python

Reasoning
about while

Termination
(or lack
thereof)

Exponential
explosion of
potential
control-paths

Assignment

This is not a duplicated slide.

```
1 i = 1
2 while i < 10:
3     i = i + 1
4     print(i)
```

What is the issue here?

Example non terminating while

Looping and
iteration

The INFDEV
Team @ HR

Introduction

Repeated
behaviors

Repeating
behaviors in
Python

Reasoning
about while

Termination
(or lack
thereof)

Exponential
explosion of
potential
control-paths

Assignment

This is not a duplicated slide.

```
1 i = 1
2 while i < 10:
3     i = i + 1
4     print(i)
```

What is the issue here?

Iterations are **orthogonal (unrelated)** to the condition.

No iteration changes elements tested in the condition.

Looping and
iteration

The INFDEV
Team @ HR

Introduction

Repeated
behaviors

Repeating
behaviors in
Python

Reasoning
about while

Termination
(or lack
thereof)

Exponential
explosion of
potential
control-paths

Assignment

Exponential explosion of potential control-paths

Looping and
iteration

The INFDEV
Team @ HR

Introduction

Repeated
behaviors

Repeating
behaviors in
Python

Reasoning
about while

Termination
(or lack
thereof)

Exponential
explosion of
potential
control-paths

Assignment

Exponential explosion of potential control-paths

- How many things can happen in a `while` loop?
- Depends on its content

Looping and
iteration

The INFDEV
Team @ HR

Introduction

Repeated
behaviors

Repeating
behaviors in
Python

Reasoning
about while

Termination
(or lack
thereof)

Exponential
explosion of
potential
control-paths

Assignment

Exponential explosion of potential control-paths

- The more we nest loops and conditionals within a loop...

Looping and
iteration

The INFDEV
Team @ HR

Introduction

Repeated
behaviors

Repeating
behaviors in
Python

Reasoning
about while

Termination
(or lack
thereof)

Exponential
explosion of
potential
control-paths

Assignment

Exponential explosion of potential control-paths

- The more we nest loops and conditionals within a loop...
- ...the more things may happen at run-time

Loops with nested if's

Looping and
iteration

The INFDEV
Team @ HR

Introduction

Repeated
behaviors

Repeating
behaviors in
Python

Reasoning
about while

Termination
(or lack
thereof)

Exponential
explosion of
potential
control-paths

Assignment

```
1 while C0:  
2     if C1:  
3         A1  
4     else:  
5         B1
```

How many execution paths per **N** iterations of the loop?

Loops with nested if's

Looping and
iteration

The INFDEV
Team @ HR

Introduction

Repeated
behaviors

Repeating
behaviors in
Python

Reasoning
about while

Termination
(or lack
thereof)

Exponential
explosion of
potential
control-paths

Assignment

```
1 while C0:  
2     if C1:  
3         A1  
4     else:  
5         B1
```

How many execution paths per **N** iterations of the loop?

2 execution paths per iteration

2^N execution paths per N iterations

Loops with nested if's

Looping and
iteration

The INFDEV
Team @ HR

Introduction

Repeated
behaviors

Repeating
behaviors in
Python

Reasoning
about while

Termination
(or lack
thereof)

Exponential
explosion of
potential
control-paths

Assignment

```
1 while C0:  
2     if C1:  
3         A1  
4     else:  
5         B1
```

Example: execution paths per **3** iterations of the loop.

A1 A1 A1

A1 A1 B1

A1 B1 A1

A1 B1 B1

B1 A1 A1

B1 A1 B1

B1 B1 A1

B1 B1 B1

Exponential explosion of potential control-paths

Looping and
iteration

The INFDEV
Team @ HR

Introduction

Repeated
behaviors

Repeating
behaviors in
Python

Reasoning
about while

Termination
(or lack
thereof)

Exponential
explosion of
potential
control-paths

Assignment

Exponential explosion of potential control-paths

- Consider a loop that performs m iterations
- With n if's inside
- Each iteration can have 2^n possible execution paths
- The whole loop can have $2^{n \times m}$ possible execution paths^a

$$^a 2^{2 \times 10} = 1048576$$

Looping and iteration

The INFDEV
Team @ HR

Introduction

Repeated
behaviors

Repeating
behaviors in
Python

Reasoning
about while

Termination
(or lack
thereof)

Exponential
explosion of
potential
control-paths

Assignment

Exponential explosion of potential control-paths

- Each path can alter the state in a different way
- After a `while` with many billions possible paths
 - We have many billions possible resulting states

Exponential explosion of potential control-paths

Looping and iteration

The INFDEV
Team @ HR

Introduction

Repeated behaviors

Repeating behaviors in Python

Reasoning about while

Termination (or lack thereof)

Exponential explosion of potential control-paths

Assignment

Exponential explosion of potential control-paths

- The more nested the code inside a `while`
- The more complex its behavior
- *The harder it is to reason about it!*

Looping and
iteration

The INFDEV
Team @ HR

Introduction

Repeated
behaviors

Repeating
behaviors in
Python

Reasoning
about while

Termination
(or lack
thereof)

Exponential
explosion of
potential
control-paths

Assignment

The value of reasoning

- **Always keep in mind:**
- You have the power to make your own life a living Hell...

Exponential explosion of potential control-paths

Looping and iteration

The INFDEV
Team @ HR

Introduction

Repeated behaviors

Repeating behaviors in Python

Reasoning about while

Termination (or lack thereof)

Exponential explosion of potential control-paths

Assignment

The value of reasoning

- **Always keep in mind:**
- You have the power to make your own life a living Hell...
- ...unless you reason first and then structure code logically

Looping and
iteration

The INFDEV
Team @ HR

Introduction

Repeated
behaviors

Repeating
behaviors in
Python

Reasoning
about `while`

Termination
(or lack
thereof)

Exponential
explosion of
potential
control-paths

Assignment

Assignment

Looping and
iteration

The INFDEV
Team @ HR

Introduction

Repeated
behaviors

Repeating
behaviors in
Python

Reasoning
about while

Termination
(or lack
thereof)

Exponential
explosion of
potential
control-paths

Assignment

Drawing with loops!

- Exclusively with `while`-loops
- Reading the appropriate parameters from the command line (figure height, width, etc.)
- Draw the following figures on the console:
 - A full square
 - The border of a square
 - A rectangle triangle
 - A centered, isosceles triangle
 - A circle
 - A smiley face
- **See assignment description online for examples and better details**

Looping and
iteration

The INFDEV
Team @ HR

Introduction

Repeated
behaviors

Repeating
behaviors in
Python

Reasoning
about while

Termination
(or lack
thereof)

Exponential
explosion of
potential
control-paths

Assignment

The best of luck, and thanks for the
attention!