

The INFDEV Team @ HR

Introduction

# Concrete model of computation

The INFDEV Team @ HR

Hogeschool Rotterdam Rotterdam, Netherlands



Concrete model of computation

The INFDEV Team @ HR

Introduction

#### Lecture topics

- We discuss a formal way to define computation
- We discuss the fundamental elements of a concrete computer
- We bridge what we have seen in the previous lecture with concrete descriptions



Concrete model of computation

The INFDEV Team @ HR

Introduction

#### **Semantics**

- Any language has semantics
- **Semantics** describe the *meaning* of sentences in the language
- Programming languages have formal semantics
- Formal semantics are expressed in a very logical, unambiguous format



The INFDEV Team @ HR

Introduction

Consider this program from the previous lecture:

take 3 steps forward sit on the chair turn left slide 3 steps forward

What do you implicitly assume by performing each of the instructions? **Try to guess and discuss!** 



Concrete model of computation

The INFDEV Team @ HR

Introduction

#### Semantics of stdNt

- We start with a current instruction and a student state:
  - The current instruction (often called instruction pointer (IP) or program counter (PC)) is just the index of the current instruction:
  - the student state (usually just called *state*, or S, or  $\sigma$ ) is whatever relevant attributes we track about the student (for example, his position and orientation in the room and whether or not he is sitting).
- Each instruction changes the PC and the S.



The INFDEV Team @ HR

Introduction

| PC | S.Pose   | S.Orientation | S.Position |
|----|----------|---------------|------------|
| 1  | Standing | Forward       | (0,0)      |

2 3 4 take 3 steps forward sit on the chair turn left slide 3 steps forward



The INFDEV Team @ HR

Introduction

| PC | S.Pose   | S.Orientation | S.Position |
|----|----------|---------------|------------|
| 2  | Standing | Forward       | (0,3)      |

take 3 steps forward sit on the chair turn left slide 3 steps forward



The INFDEV Team @ HR

Introduction

| P | 7 | S.Pose  | S.Orientation | S.Position |
|---|---|---------|---------------|------------|
| 3 |   | Sitting | Forward       | (0,3)      |

2 3 4 take 3 steps forward sit on the chair turn left slide 3 steps forward



The INFDEV Team @ HR

Introduction

| PC | S.Pose  | S.Orientation | S.Position |
|----|---------|---------------|------------|
| 4  | Sitting | Left          | (0,3)      |

2 3 4 take 3 steps forward sit on the chair turn left slide 3 steps forward



Concrete model of

The INFDEV Team @ HR

Introduction

| PC  | S.Pose  | S.Orientation | S.Position |
|-----|---------|---------------|------------|
| END | Sitting | Left          | (-3,3)     |

take 3 steps forward sit on the chair turn left slide 3 steps forward

what do we do now? Try to guess and discuss!



Concrete model of computation

The INFDEV Team @ HR

Introduction

## A slight formalization

 We say that an instruction I is a function that, given a pair of PC and S, returns a new pair of PC and S



Concrete model of computation

The INFDEV Team @ HR

Introduction

- We say that an instruction I is a function that, given a pair of PC and S, returns a new pair of PC and S
- Do not panic now, math..y symbols incoming!



Concrete model of computation

The INFDEV Team @ HR

Introduction

- We say that an instruction I is a function that, given a pair of PC and S, returns a new pair of PC and S
- Do not panic now, math..y symbols incoming!
- $\bullet (PC,S) \stackrel{Instr}{\to} (PC',S')$



Concrete model of computation

The INFDEV Team @ HR

Introduction

- Consider instruction sit on the chair (we will shorten it to sit)
- How do we change the current instruction?
- How do we change the position of the resulting state depending on the orientation of the input state?



Concrete model of computation

The INFDEV Team @ HR

Introduction

- Consider instruction sit on the chair (we will shorten it to sit)
  - $(PC, S) \stackrel{sit}{\rightarrow} (PC + 1, S[Pose \mapsto Sitting])$
- We increment the current instruction index by one
- We change the pose of the resulting state independent on the input state
  - $S[Pose \mapsto Sitting]$  is read as "S, where pose is sitting"



Concrete model of computation

The INFDEV Team @ HR

Introduction

- Consider instruction stand up (we will shorten it to stand)
- How do we change the current instruction?
- How do we change the position of the resulting state depending on the orientation of the input state?



Concrete model of

The INFDEV Team @ HR

Introduction

# A slight formalization

• Consider instruction stand up (we will shorten it to stand)



Concrete model of computation

The INFDEV Team @ HR

Introduction

- Consider instruction stand up (we will shorten it to stand)
  - $(PC, S) \stackrel{stand}{\rightarrow} (PC + 1, S[Pose \mapsto Standing])$
- We increment the current instruction index by one
- We change the pose of the resulting state independent on the input state



Concrete model of computation

The INFDEV Team @ HR

Introduction

- Consider instruction take 3 steps forward (we will shorten it to fwd 3)
- How do we determine the next instruction index?
- How do we change the position of the resulting state?
  - Are there dependencies from the input state?



The INFDEV Team @ HR

Introduction

| PC  | S.Pose   | S.Orientation | S.Position |
|-----|----------|---------------|------------|
| 104 | Standing | Left          | (10,20)    |

**10**3

**10**4

take 3 steps forward

| PC  | S.Pose   | S.Orientation | S.Position |
|-----|----------|---------------|------------|
| 105 | Standing | Left          | (7,20)     |



The INFDEV Team @ HR

Introduction

| PC  | S.Pose   | S.Orientation | S.Position |
|-----|----------|---------------|------------|
| 104 | Standing | Right         | (10,20)    |

**10**3

**10**4

take 3 steps forward

**10**5 . .

| PC  | S.Pose   | S.Orientation | S.Position |
|-----|----------|---------------|------------|
| 105 | Standing | Right         | (13,20)    |



Concrete model of computation

The INFDEV Team @ HR

Introduction

#### A slight formalization

 Consider instruction take 3 steps forward (we will shorten it to fwd 3)

```
(PC,S) \overset{f \, wd3}{\rightarrow} (PC+1,S[Position \mapsto S.Position + (0,3)]) when S.Orientation = Forward (PC,S) \overset{f \, wd3}{\rightarrow} (PC+1,S[Position \mapsto S.Position - (0,3)]) when S.Orientation = Backward (PC,S) \overset{f \, wd3}{\rightarrow} (PC+1,S[Position \mapsto S.Position + (3,0)]) when S.Orientation = Right (PC,S) \overset{f \, wd3}{\rightarrow} (PC+1,S[Position \mapsto S.Position - (3,0)]) when S.Orientation = Left
```

- We always increment the instruction by one
- We change the position of the resulting state depending on the orientation of the input state



Concrete model of computation

The INFDEV Team @ HR

Introduction

- Consider instruction if A then B else C
- How do we determine the next instruction index?
- How do we change the state?



The INFDEV Team @ HR

Introduction

```
PC S.Pose S.Orientation S.Position
24 Standing Right (10,20)
```

23 ...
24 if A is ''black'' then
25 turn left by 90 \* B degrees
26 otherwise
27 turn left by 90 \* C degrees
28 ...

| PC              | S.Pose   | S.Orientation | S.Position |
|-----------------|----------|---------------|------------|
| 25 <sup>1</sup> | Standing | Right         | (10,20)    |

<sup>&</sup>lt;sup>1</sup>Assuming student's shirt is black



The INFDEV Team @ HR

Introduction

```
PC S.Pose S.Orientation S.Position
24 Standing Right (10,20)
```

232425262728

if A is ''black'' then
 turn left by 90 \* B degrees
otherwise
 turn left by 90 \* C degrees

| PC       | S.Pose   | S.Orientation | S.Position |
|----------|----------|---------------|------------|
| $27^{2}$ | Standing | Right         | (10,20)    |

<sup>&</sup>lt;sup>2</sup>Assuming student's shirt is not black



Concrete model of computation

The INFDEV Team @ HR

Introduction

#### A slight formalization

ullet Consider instruction if A then B else C (shortened by as  $if_{ABC}$ )



Concrete model of computation

The INFDEV Team @ HR

Introduction

- ullet Consider instruction if A then B else C (shortened by as  $if_{ABC}$ )
- We jump to the first instruction of the B block if the condition evaluates to TRUE



Concrete model of computation

The INFDEV Team @ HR

Introduction

- ullet Consider instruction if A then B else C (shortened by as  $if_{ABC}$ )
- We jump to the first instruction of the B block if the condition evaluates to TRUE
- We jump to the first instruction of the C block if the condition evaluates to FALSE



Concrete model of computation

The INFDEV Team @ HR

Introduction

- ullet Consider instruction if A then B else C (shortened by as  $if_{ABC}$ )
- We jump to the first instruction of the B block if the condition evaluates to TRUE
- We jump to the first instruction of the C block if the condition evaluates to FALSE
- We leave the state unchanged



Concrete model of computation

The INFDEV Team @ HR

Introduction

- ullet Consider instruction if A then B else C (shortened by as  $if_{ABC}$ )
- We jump to the first instruction of the B block if the condition evaluates to TRUE
- We jump to the first instruction of the C block if the condition evaluates to FALSE
- We leave the state unchanged

$$\begin{cases} (PC,S) \overset{if_{ABC}}{\rightarrow} (loc(B),S) & when & (PC,S) \overset{A}{\rightarrow} \text{TRUE} \\ (PC,S) \overset{if_{ABC}}{\rightarrow} (loc(C),S) & when & (PC,S) \overset{A}{\rightarrow} \text{FALSE} \end{cases}$$



Concrete model of computation

The INFDEV Team @ HR

Introduction

- Consider instruction while A do B
- How do we determine the next instruction index?
- How do we change the state?



The INFDEV Team @ HR

Introduction

| PC | S.Pose   | S.Orientation | S.Position |
|----|----------|---------------|------------|
| 24 | Standing | Right         | (10,20)    |

23 ...

24 while A is ''sunny'' do

25 order another beer

26 enjoy the day for another hour

27 go back to work

28 ...

| PC       | S.Pose   | S.Orientation | S.Position |
|----------|----------|---------------|------------|
| $25^{3}$ | Standing | Right         | (10,20)    |



The INFDEV Team @ HR

Introduction

| PC | S.Pose   | S.Orientation | S.Position |
|----|----------|---------------|------------|
| 24 | Standing | Right         | (10,20)    |

23 ...

24 while A is ''sunny'' do

25 order another beer

26 enjoy the day for another hour

27 go back to work

28 ...

| PC              | S.Pose   | S.Orientation | S.Position |
|-----------------|----------|---------------|------------|
| 27 <sup>4</sup> | Standing | Right         | (10,20)    |



Concrete model of computation

The INFDEV Team @ HR

Introduction

## A slight formalization

ullet Consider instruction while A do B (shortened by as  $while_{AB})$ 



Concrete model of computation

The INFDEV Team @ HR

Introduction

- ullet Consider instruction while A do B (shortened by as  $while_{AB})$
- We jump to the first instruction of the B block if the condition evaluates to TRUE



Concrete model of computation

The INFDEV Team @ HR

Introduction

- ullet Consider instruction while A do B (shortened by as  $while_{AB})$
- We jump to the first instruction of the B block if the condition evaluates to TRUE
- We jump to after the last instruction of the B block if the condition evaluates to FALSE



Concrete model of computation

The INFDEV Team @ HR

Introduction

- ullet Consider instruction while A do B (shortened by as  $while_{AB})$
- We jump to the first instruction of the B block if the condition evaluates to TRUE
- We jump to after the last instruction of the B block if the condition evaluates to FALSE
- We leave the state unchanged



Concrete model of computation

The INFDEV Team @ HR

Introduction

- Consider instruction while A do B (shortened by as  $while_{AB}$ )
- We jump to the first instruction of the B block if the condition evaluates to TRUE
- We jump to after the last instruction of the B block if the condition evaluates to FALSE
- We leave the state unchanged

$$\left\{ \begin{array}{c} (PC,S) \overset{while}{\rightarrow} ^{AB} \ (loc(B),S) \ when \ (PC,S) \overset{A}{\rightarrow} \text{TRUE} \\ (PC,S) \overset{while}{\rightarrow} ^{AB} \ (lastloc(B)+1,S) \ when \ (PC,S) \overset{A}{\rightarrow} \text{FALSE} \end{array} \right.$$



# This is it!

Concrete model of computation

The INFDEV Team @ HR

Introduction

# The best of luck, and thanks for the attention!