

The INFDEV Team @ HR

Introduction

## Concrete model of computation

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Hogeschool Rotterdam Rotterdam, Netherlands



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Introduction

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#### Lecture topics

- We discuss a formal way to define computation
  - We discuss the fundamental elements of a concrete computer
  - We bridge what we have seen in the previous lecture with concrete descriptions



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#### **Semantics**

- Any language has semantics
- **Semantics** describe the *meaning* of sentences in the language
- Programming languages have formal semantics
- Formal semantics are expressed in a very logical, unambiguous format



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Consider this program from the previous lecture:

take 3 steps forward sit on the chair turn left slide 3 steps forward

What do you implicitly assume by performing each of the instructions? **Try to guess and discuss!** 



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#### Semantics of stdNt

- We start with a current instruction and a student state:
  - The current instruction (often called instruction pointer (IP) or program counter (PC)) is just the index of the current instruction;
  - the student state (usually just called *state*, or S, or  $\sigma$ ) is whatever relevant attributes we track about the student (for example, his position and orientation in the room and whether or not he is sitting).
- Each instruction changes the PC and the S.



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PC	S.Pose	S.Orientation	S.Position
1	Standing	Forward	(0,0)

2 3 4 take 3 steps forward sit on the chair turn left slide 3 steps forward



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Introduction

PC	S.Pose	S.Orientation	S.Position
2	Standing	Forward	(0, 3)

take 3 steps forward sit on the chair turn left slide 3 steps forward



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PC	S.Pose	S.Orientation	S.Position
3	Sitting	Forward	(0,3)

2 3 4 take 3 steps forward sit on the chair turn left slide 3 steps forward



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PC	S.Pose	S.Orientation	S.Position
4	Sitting	Left	(0,3)

take 3 steps forward sit on the chair turn left slide 3 steps forward



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PC	S.Pose	S.Orientation	S.Position
END	Sitting	Left	( -3 ,3)

take 3 steps forward
sit on the chair
turn left
slide 3 steps forward

what do we do now? Try to guess and discuss!



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### A slight formalization

 We say that an instruction I is a function that, given a pair of PC and S, returns a new pair of PC and S



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- We say that an instruction I is a function that, given a pair of PC and S, returns a new pair of PC and S
- Do not panic now, math..y symbols incoming!



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- We say that an instruction I is a function that, given a pair of PC and S, returns a new pair of PC and S
- Do not panic now, math..y symbols incoming!
- $\bullet (PC,S) \stackrel{Instr}{\to} (PC',S')$



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- Consider instruction sit on the chair (we will shorten it to sit)
- How do we change the current instruction?
- How do we change the position of the resulting state depending on the orientation of the input state?



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- Consider instruction sit on the chair (we will shorten it to sit)
  - $(PC, S) \stackrel{sit}{\rightarrow} (PC + 1, S[Pose \mapsto Sitting])$
- We increment the current instruction index by one
- We change the pose of the resulting state independent on the input state
  - $S[Pose \mapsto Sitting]$  is read as "S, where pose is sitting"



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- Consider instruction stand up (we will shorten it to stand)
- How do we change the current instruction?
- How do we change the position of the resulting state depending on the orientation of the input state?



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### A slight formalization

 Consider instruction stand up (we will shorten it to stand)



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- Consider instruction stand up (we will shorten it to stand)
  - $(PC, S) \stackrel{stand}{\rightarrow} (PC + 1, S[Pose \mapsto Standing])$
- We increment the current instruction index by one
- We change the pose of the resulting state independent on the input state



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- Consider instruction take 3 steps forward (we will shorten it to fwd 3)
- How do we determine the next instruction index?
- How do we change the position of the resulting state?
  - Are there dependencies from the input state?



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PC	S.Pose	S.Orientation	S.Position
104	Standing	Left	(10,20)

**10**3

**10**4

take 3 steps forward

PC	S.Pose	S.Orientation	S.Position
105	Standing	Left	(7,20)



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PC	S.Pose	S.Orientation	S.Position
104	Standing	Right	(10,20)

103

104

take 3 steps forward

**10**5

PC	S.Pose	S.Orientation	S.Position
105	Standing	Right	( 13 ,20)





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#### A slight formalization

 Consider instruction take 3 steps forward (we will shorten it to fwd 3)

```
 \begin{array}{l} (PC,S) \overset{f \, wd3}{\rightarrow} (PC+1,S[Position \mapsto S.Position+(0,3)]) \\ when \, S.Orientation = Forward \\ (PC,S) \overset{f \, wd3}{\rightarrow} (PC+1,S[Position \mapsto S.Position-(0,3)]) \\ when \, S.Orientation = Backward \\ (PC,S) \overset{f \, wd3}{\rightarrow} (PC+1,S[Position \mapsto S.Position+(3,0)]) \\ when \, S.Orientation = Right \\ (PC,S) \overset{f \, wd3}{\rightarrow} (PC+1,S[Position \mapsto S.Position-(3,0)]) \\ when \, S.Orientation = Left \end{array}
```

- We always increment the instruction by one
- We change the position of the resulting state depending on the orientation of the input state



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- Consider instruction if A then B else C
- How do we determine the next instruction index?
- How do we change the state?



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```
PC S.Pose S.Orientation S.Position
24 Standing Right (10,20)
```

if A is ''black'' then
 turn left by 90 \* B degrees
otherwise
 turn left by 90 \* C degrees

PC	S.Pose	S.Orientation	S.Position
$25^{1}$	Standing	Right	(10,20)

<sup>&</sup>lt;sup>1</sup>Assuming student's shirt is black



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```
PC S.Pose S.Orientation S.Position
24 Standing Right (10,20)
```

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if A is ''black'' then
 turn left by 90 \* B degrees
otherwise
 turn left by 90 \* C degrees

		S.Orientation	S.Position
27 <sup>2</sup>	Standing	Right	(10,20)

<sup>&</sup>lt;sup>2</sup>Assuming student's shirt is not black



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Introduction

#### A slight formalization

ullet Consider instruction if A then B else C (shortened by as  $if_{ABC}$ )



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- ullet Consider instruction if A then B else C (shortened by as  $if_{ABC}$ )
- We jump to the first instruction of the B block if the condition evaluates to TRUE



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- ullet Consider instruction if A then B else C (shortened by as  $if_{ABC}$ )
- We jump to the first instruction of the B block if the condition evaluates to TRUE
- We jump to the first instruction of the C block if the condition evaluates to FALSE



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- ullet Consider instruction if A then B else C (shortened by as  $if_{ABC}$ )
- We jump to the first instruction of the B block if the condition evaluates to TRUE
- We jump to the first instruction of the C block if the condition evaluates to FALSE
- We leave the state unchanged



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- Consider instruction if A then B else C (shortened by as  $if_{ABC}$ )
- We jump to the first instruction of the B block if the condition evaluates to TRUE
- We jump to the first instruction of the C block if the condition evaluates to FALSE
- We leave the state unchanged

$$\begin{cases} (PC,S) \overset{if_{ABC}}{\rightarrow} (loc(B),S) & when & (PC,S) \overset{A}{\rightarrow} \text{TRUE} \\ (PC,S) \overset{if_{ABC}}{\rightarrow} (loc(C),S) & when & (PC,S) \overset{A}{\rightarrow} \text{FALSE} \end{cases}$$



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- Consider instruction while A do B
- How do we determine the next instruction index?
- How do we change the state?



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PC	S.Pose	S.Orientation	S.Position
24	Standing	Right	(10,20)

while A is ''sunny'' do
order another beer
enjoy the day for another hour
go back to work

\_\_\_\_

		S.Orientation	S.Position
$25^{3}$	Standing	Right	(10,20)



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Introduction

PC	S.Pose	S.Orientation	S.Position
24	Standing	Right	(10,20)

while A is 'sunny' do
order another beer
enjoy the day for another hour
go back to work

PC	S.Pose	S.Orientation	S.Position
27 <sup>4</sup>	Standing	Right	(10,20)



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Introduction

## A slight formalization

ullet Consider instruction while A do B (shortened by as  $while_{AB})$ 



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- ullet Consider instruction while A do B (shortened by as  $while_{AB})$
- We jump to the first instruction of the B block if the condition evaluates to TRUE



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- ullet Consider instruction while A do B (shortened by as  $while_{AB})$
- We jump to the first instruction of the B block if the condition evaluates to TRUE
- We jump to after the last instruction of the B block if the condition evaluates to FALSE



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Introduction

- ullet Consider instruction while A do B (shortened by as  $while_{AB})$
- We jump to the first instruction of the B block if the condition evaluates to TRUE
- We jump to after the last instruction of the B block if the condition evaluates to FALSE
- We leave the state unchanged



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Introduction

- ullet Consider instruction while A do B (shortened by as  $while_{AB})$
- We jump to the first instruction of the B block if the condition evaluates to TRUE
- We jump to after the last instruction of the B block if the condition evaluates to FALSE
- We leave the state unchanged

$$\left\{ \begin{array}{c} (PC,S) \overset{while}{\rightarrow} ^{AB} \ (loc(B),S) \ when \ (PC,S) \overset{A}{\rightarrow} \text{TRUE} \\ (PC,S) \overset{while}{\rightarrow} ^{AB} \ (lastloc(B)+1,S) \ when \ (PC,S) \overset{A}{\rightarrow} \text{FALSE} \end{array} \right.$$



## This is it!

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# The best of luck, and thanks for the attention!