

Dr. Giuseppo Maggiore

Reasoning on programs

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Introduction

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Lecture topics

- We introduce conditional expressions
- We show how to verify properties on complex expressions



Conditional expressions

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Conditional expressions

- Sometimes we can make decisions within an expression
- ullet The general form is VALUE if CONDITION else VALUE' $(if_{VCV'})$
- If the condition is true, then we return VALUE, otherwise VALUE,

$$\begin{cases} \left(PC,S\right) \overset{if_{V} \subseteq V'}{\to} V & when & \left(PC,S\right) \overset{C}{\to} TRUE \\ \left(PC,S\right) \overset{if_{V} \subseteq V'}{\to} V' & when & \left(PC,S\right) \overset{C}{\to} FALSE \end{cases}$$



Conditional expressions

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Conditional expressions

- "adult" if age >= 18 else "minor" = ?
- Can you guess the results for age = 18 and age = 16?



Conditional expressions

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Conditional expressions

- "adult" if age >= 18 else "minor" = ?
- Can you guess the results for age = 18 and age = 16?
- age = 16: "minor"
- age = 18: "adult"



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- Sometimes we do not know exactly the values of all variables at all times
- The program may be too complex to allow it



Dr. Giuseppe Maggiore Consider a throttle control system.

The throttle may never go under 1000RPM, or the engine stops and everybody dies.

The temperature must be kept under control, or the engine blows up and everybody dies.

```
throttle = throttle - 1000 if (temp > 350.0) & (
throttle > 2500) else throttle
```

The question thus is: **could the code above cause everyone to die?**



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throttle	temp
100010000	-20.0400.0



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throttle	temp
100010000	-20.0400.0

1

throttle	temp
?!?!?	-20.0400.0



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- We cannot list all possible combinations of variable values
- We cannot just "hope it works"



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- We cannot list all possible combinations of variable values
- We cannot just "hope it works"
- We can reason in terms of conditions on variables



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- We partition the state based on the conditional
- (temp > 350.0) & (throttle > 2500) generates four states
 - temp > 350 and throttle > 2500
 - temp <= 350 and throttle > 2500
 - temp > 350 and throttle <= 2500
 - temp <= 350 and throttle <= 2500
- We study the semantics on each of these four states



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temp > 350 and throttle > 2500

throttle	temp
>2500.0 10000	>350.0400.0



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temp > 350 and throttle > 2500

throttle	temp
>2500.0 10000	>350.0400.0

throttle	temp
>1500.09000.0	>350.0400.0



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temp
$$\leq$$
 350 and throttle $>$ 2500

throttle	temp
>2500.010000	-20.0350.0

```
throttle = throttle - 1000 if (temp > 350.0) & (
throttle > 2500) else throttle
```



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temp <=
$$350$$
 and throttle > 2500

throttle	temp
>2500.010000	-20.0350.0

```
throttle = throttle - 1000 if (temp > 350.0) & (
throttle > 2500) else throttle
```

throttle	temp
>2500.010000.0	-20.0350.0



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temp > 350 and throttle <= 2500

throttle	temp
1000>2500.0	>350400.0



Maggiore

temp > 350 and throttle <= 2500

throttle	temp
1000>2500.0	>350400.0

throttle	temp
1000>2500.0	>350400.0



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temp
$$<=$$
 350 and throttle $<=$ 2500

throttle	temp
1000>2500.0	-20.0350.0

```
throttle = throttle - 1000 if (temp > 350.0) & (
throttle > 2500) else throttle
```



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temp \leq 350 and throttle \leq 2500

throttle	temp
1000>2500.0	-20.0350.0

throttle	temp
1000>2500.0	-20.0350.0



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- Each of the four states has a result
- We now merge the results



Dr. Giuseppe Maggiore We now merge these states, knowing that each of them may actually happen:

throttle	temp
>1500.09000.0	>350.0400.0
>2500.010000.0	-20.0350.0
1000.0>2500.0	>350400.0
1000.0>2500.0	-20.0350.0



Dr. Giuseppe Maggiore We now merge these states, knowing that each of them may actually happen:

throttle	temp
>1500.09000.0	>350.0400.0
>2500.010000.0	-20.0350.0
1000.0>2500.0	>350400.0
1000.0>2500.0	-20.0350.0

throttle	temp
1000.010000.0	-20.0400.0

We know that the throttle will never go below 1500RPM, and we also know that if the temperature is above 350 degrees then maximum throttle is never above 9000RPM.



Conclusion?

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Nobody dies:)



This is it!

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The best of luck, and thanks for the attention!