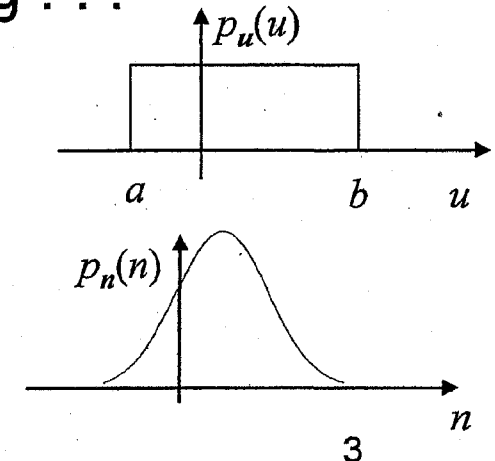


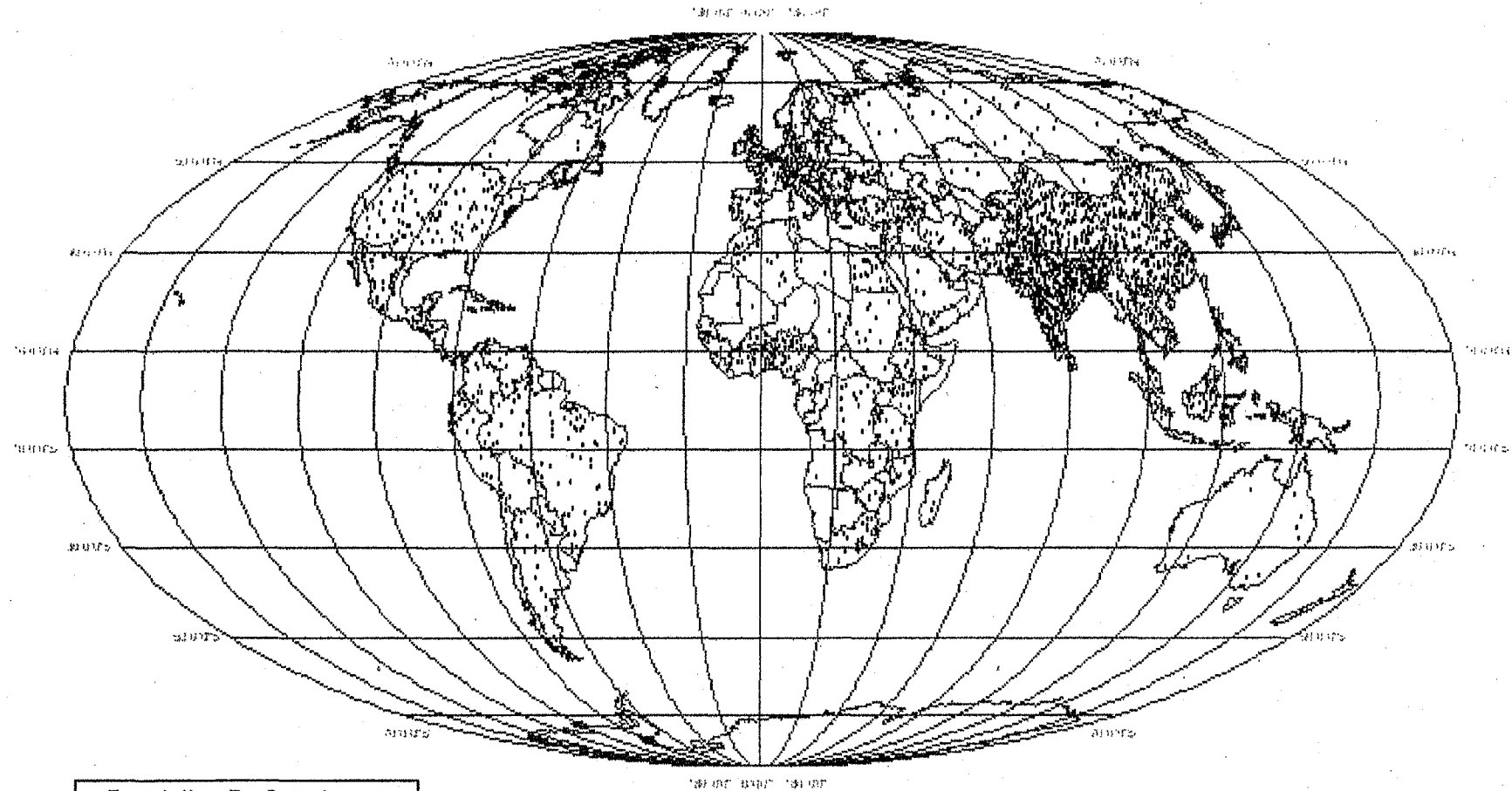
# How to generate a population density map?

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- Given: population density  $d(\theta, \varphi)$  in people per km<sup>2</sup>  
 where  $\theta$  – longitude [0 ... 360 degree]  
 $\varphi$  – latitude [-90 ... 90 degree]
- **Devise an algorithm that generates random number pairs  $(\theta, \varphi)$  in accordance with the population density  $d(\theta, \varphi)$**
- You can generate random numbers by using . . .
  - . . . a function  $u(a, b)$  that generates random numbers uniformly distributed between  $a$  and  $b$
  - . . . a function  $n(\mu, \sigma)$  that generates Gaussian random numbers with mean  $\mu$  and variance  $\sigma^2$



## World Population Density - 1994



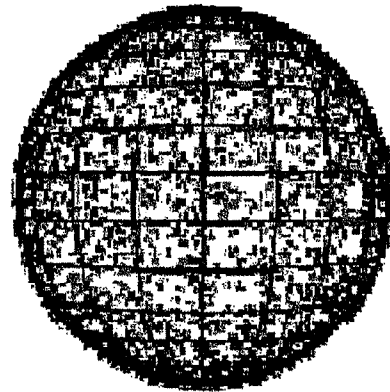
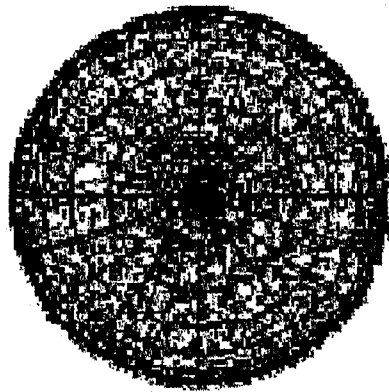
Population By Country

1 Dot = 2,000,000 people

Mapmaker: Mibi Comstock  
Date Created: April 13, 2005  
Source: ESRI, 1994  
Projection: Mollweide

*top view*

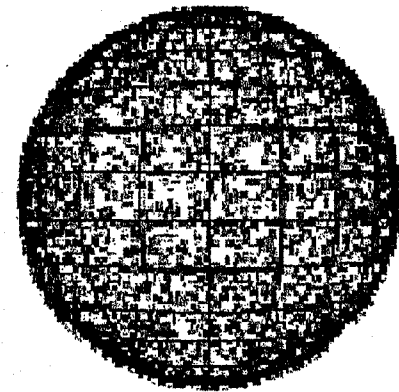
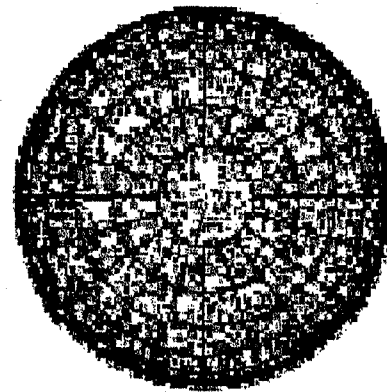
*side view*



*incorrectly distributed points*

*top view*

*side view*



*correctly distributed points*

Birds independently land on an infinitely long telegraph wire at random positions. Each bird has a right neighbor and a left neighbor. The distance  $\Delta$  between neighboring birds is exponentially distributed according to the pdf  $f_{\Delta}(\Delta) = e^{-\Delta}$  for  $\Delta \geq 0$ .

- (a) What is the pdf of the distance between a bird and its nearest neighbor?
- (b) If bird  $B'$  is the nearest neighbor of  $B$ , what is the probability that  $B$  is also the nearest neighbor of  $B'$ ?
- (c) Paint the interval between  $B$  and its nearest neighbor  $B'$  yellow. If we do this for each bird  $B$ , what fraction of the real line will be painted yellow?



You are giving  $N = 2$  identical fuses. Their rating is the same; it is one of the following values:

0.5 mA, 1 mA, 2 mA, 5 mA, 10 mA, 20 mA, 50 mA, 100 mA, 200 mA, 500 mA, 1 A

Since the fuses are not marked, you test them repeatedly with different currents to determine the unknown rating. When the current exceeds the rating, the fuse is irreversibly destroyed.

Devise a strategy that minimizes the maximum number of tests to reliably determine the fuses' current rating.

How many tests  $T$  are required to distinguish  $R$  different ratings, if you have  $N$  fuses?

Note: All  $N$  fuses may be destroyed in the process.