EE Qualifying Exam January 2007

An important property of linear, time-invariant systems is that complex exponentials are eigenfunctions.

What about the converse? That is, suppose L is a linear system and the complex exponentials $e^{2\pi i\nu x}$ are eigenfunctions of L for all $\nu \in \mathbf{R}$. Is L necessarily a time-invariant system?