Ph.D. Qualifying Examination

Problem 1. The circumference of a circle is colored a% in red such that a<100/3. Prove that it is always possible to inscribe an equilateral triangle into the circle such that all three vertices avoid the red, irrespective of how the coloring is done.

