Consider a causal LTI system with frequency response $H(j\omega)$. Only the real part of the frequency response is known:

$$\operatorname{Re}\left\{H(j\omega)\right\} = 1 + \cos\omega$$

Show that the system possesses a linear-phase frequency response.