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SESSION ID: CRYPT-W03 - Secure Multiparty Computation

Hybrid Publicly Verifiable Computation

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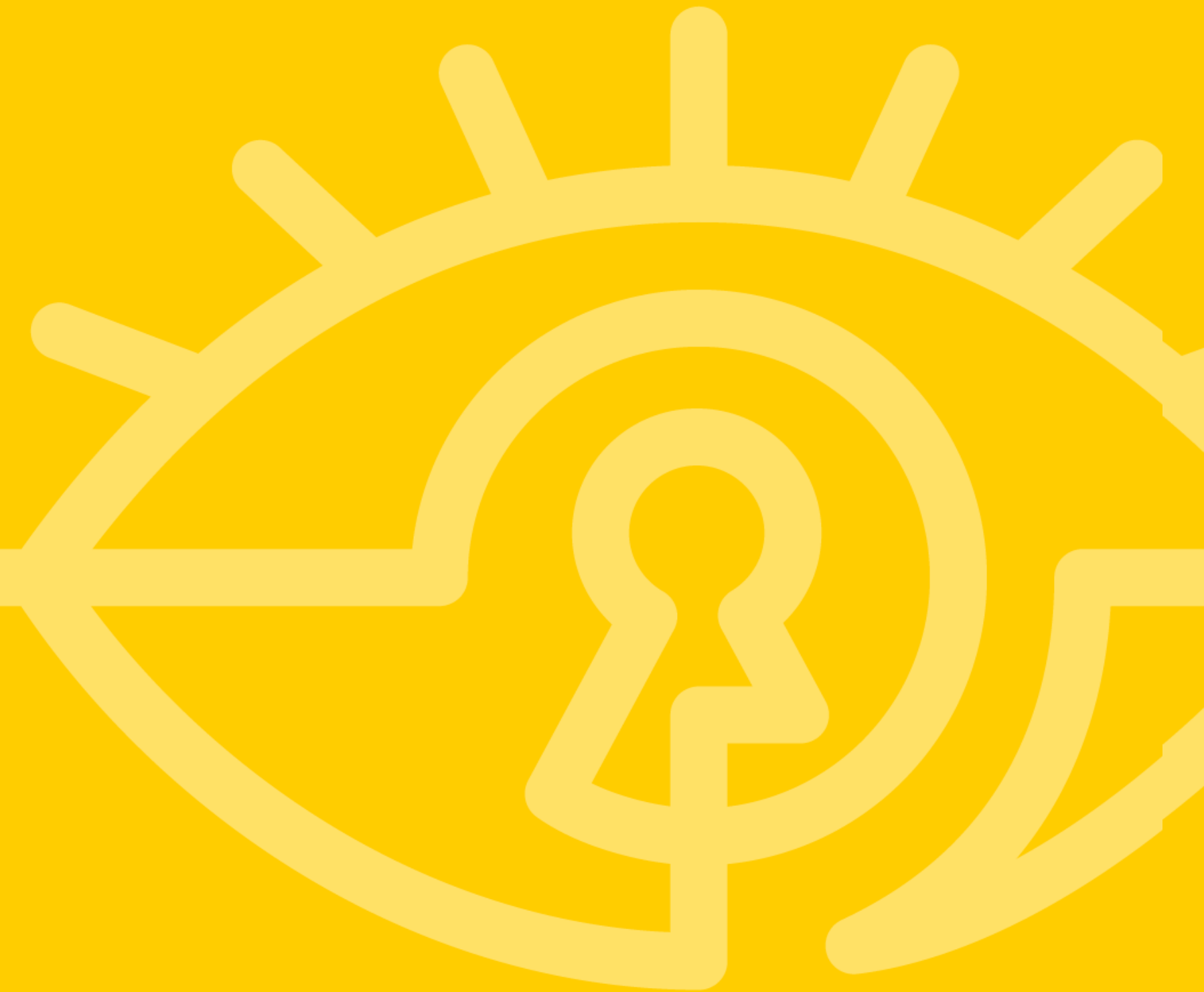
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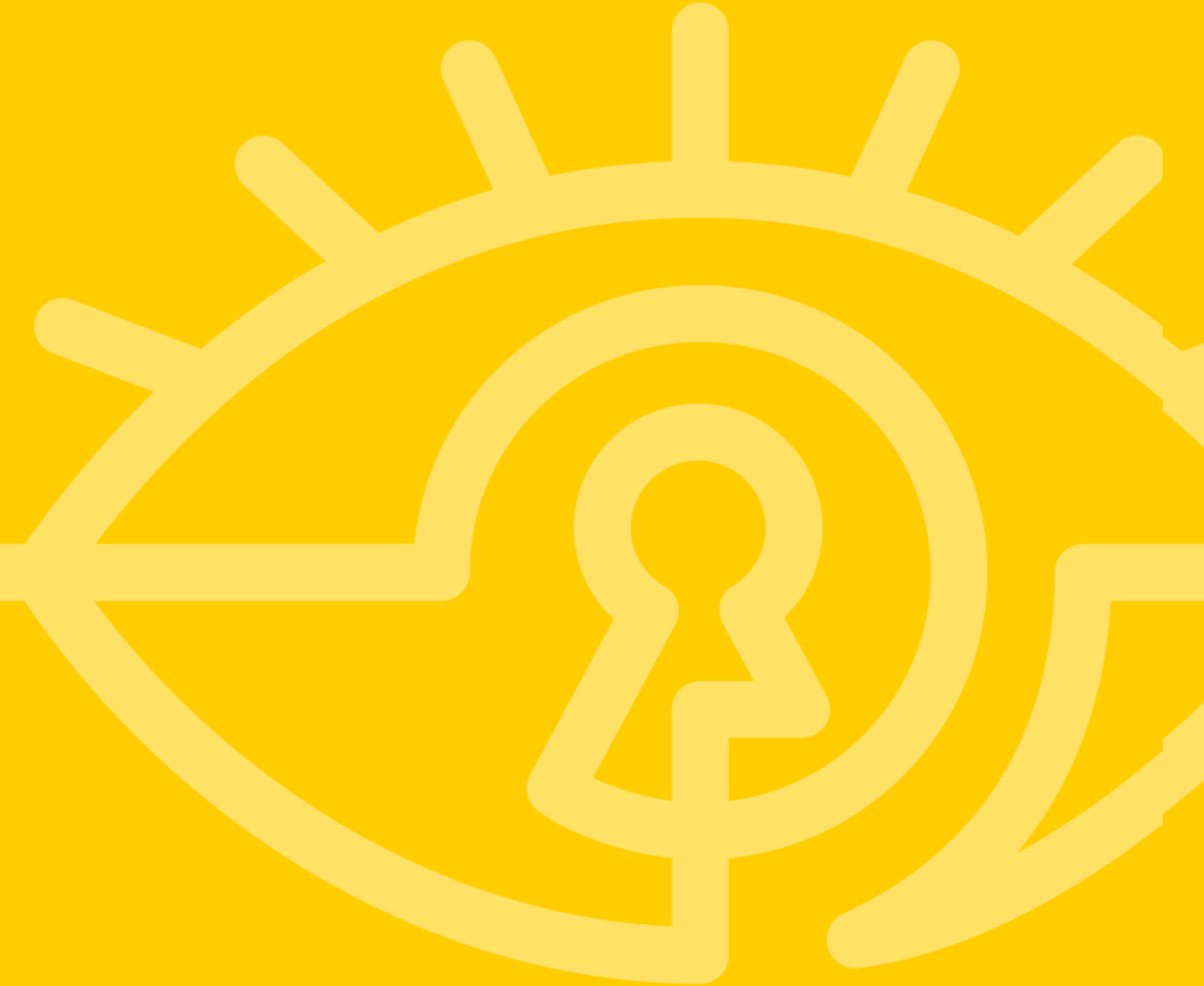
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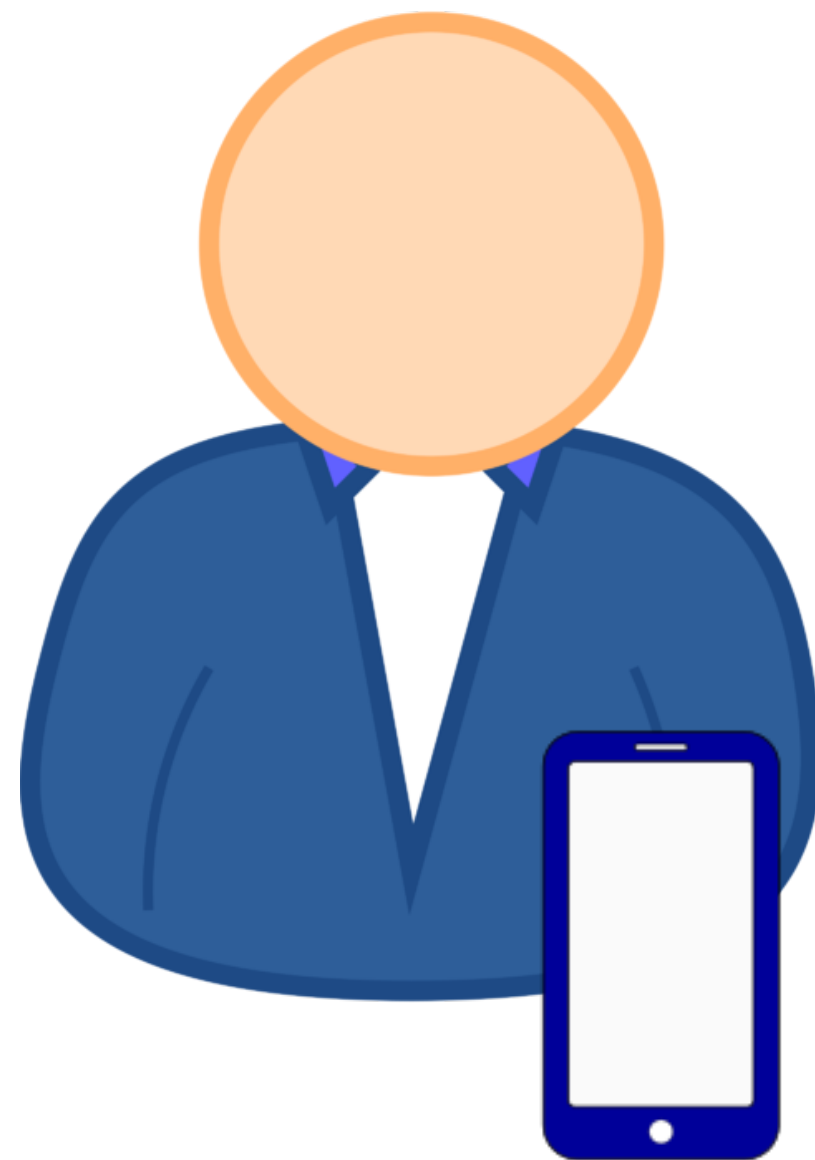




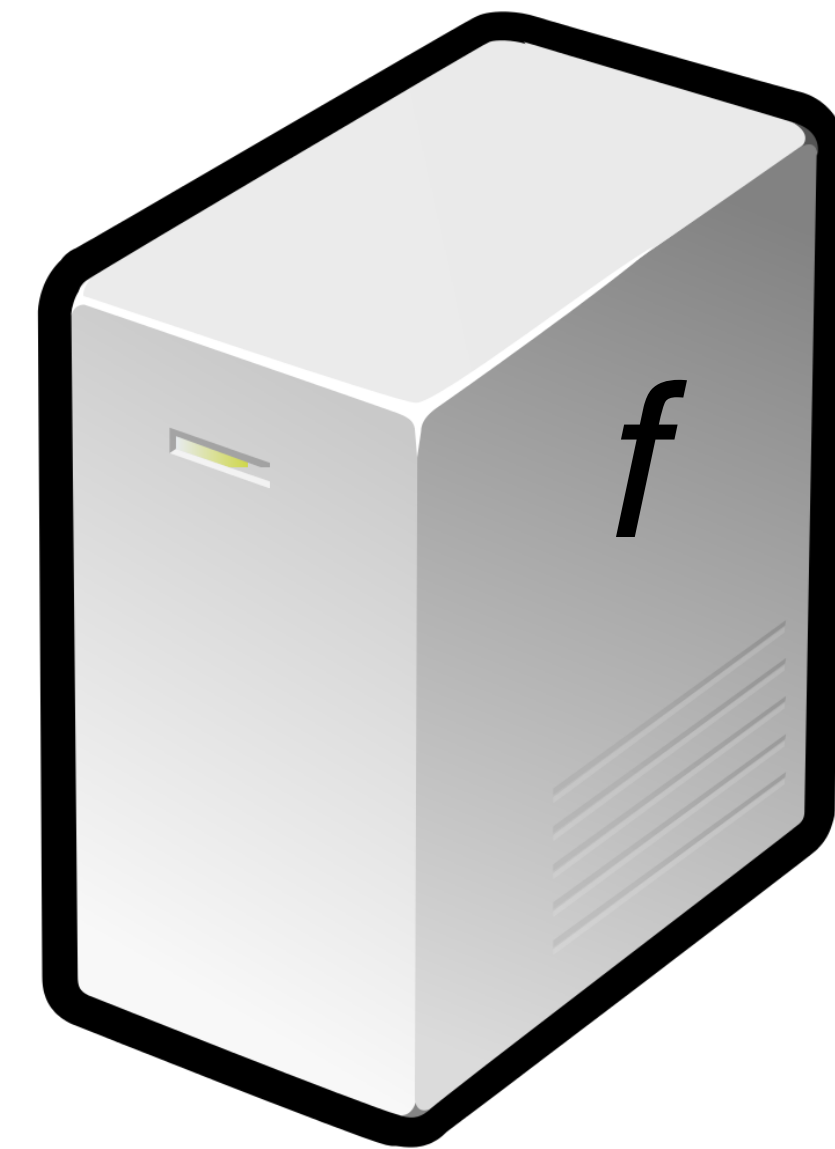
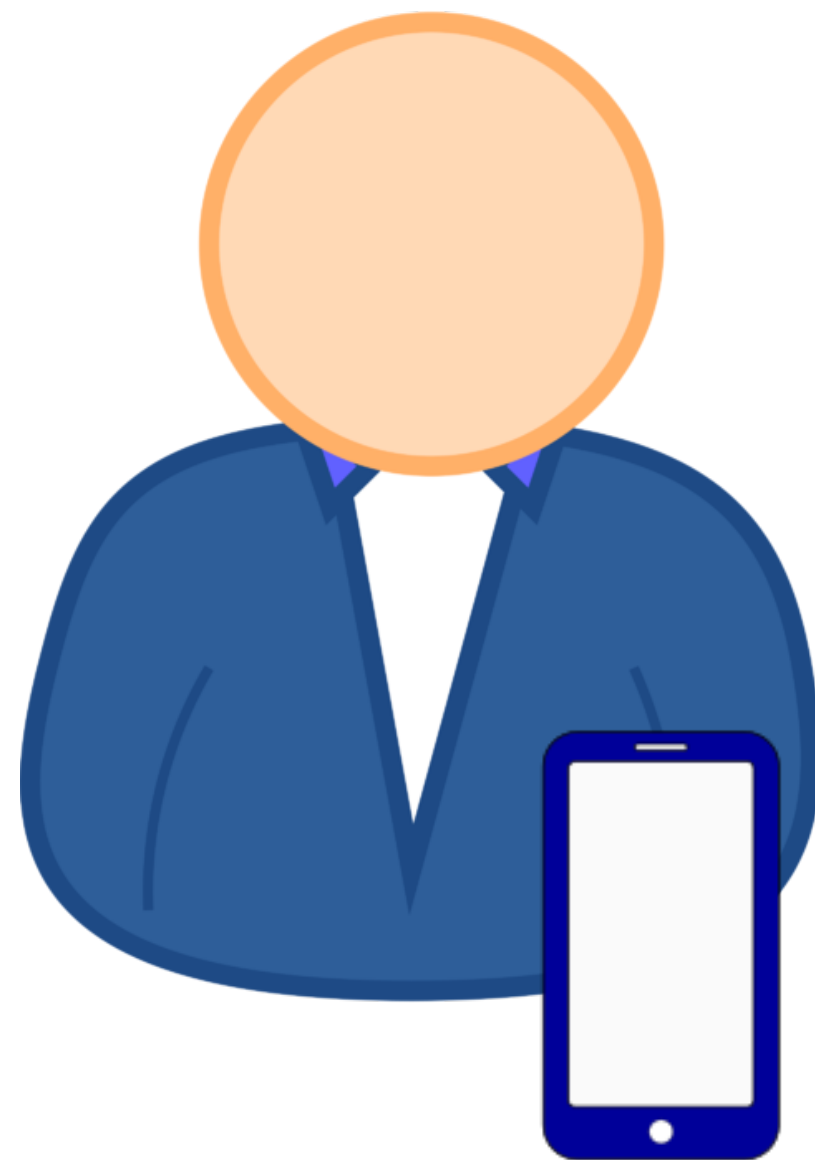
Background



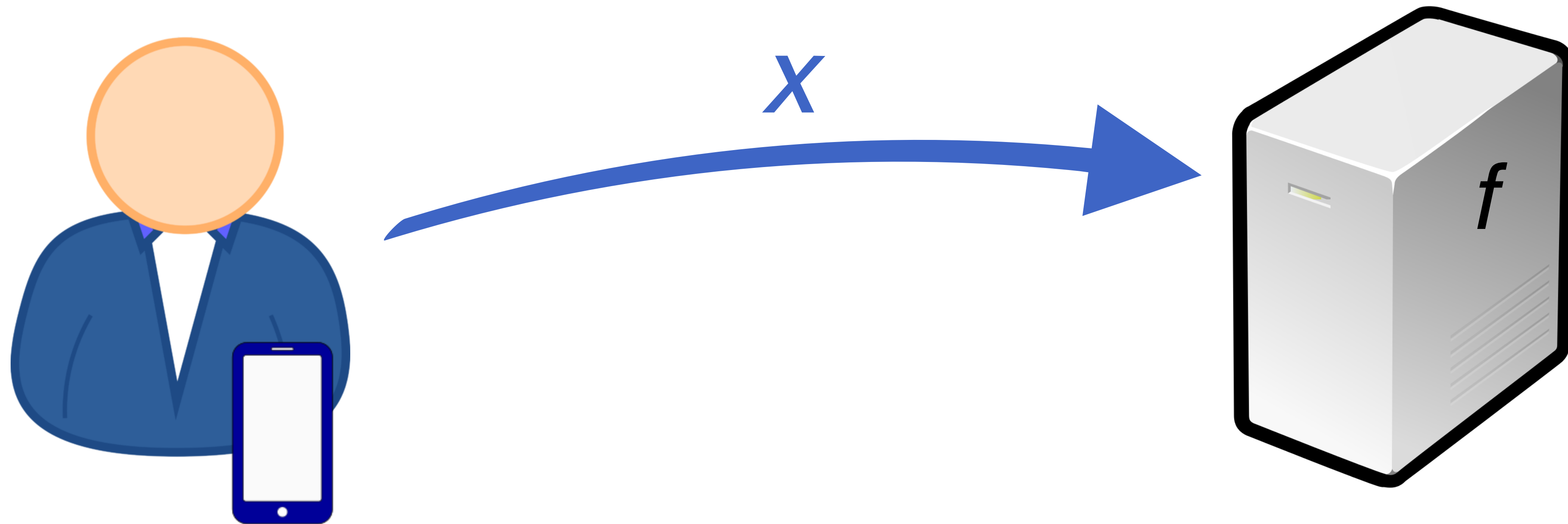
Verifiable Outsourced Computation



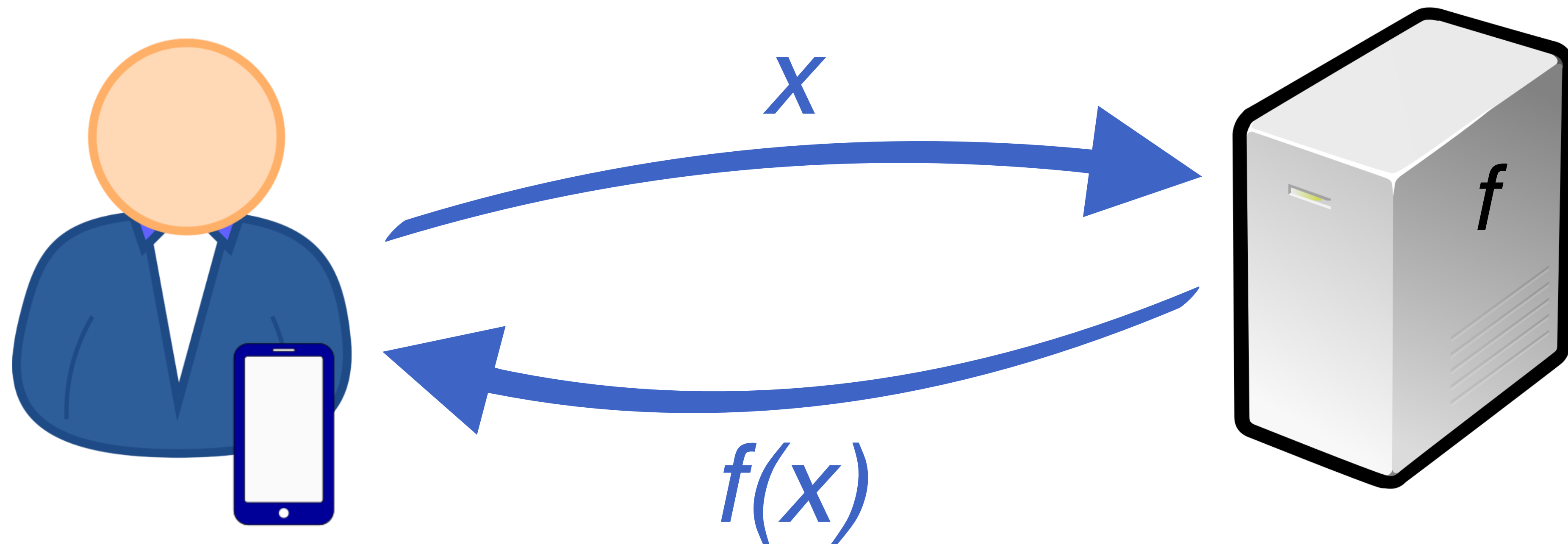
Verifiable Outsourced Computation



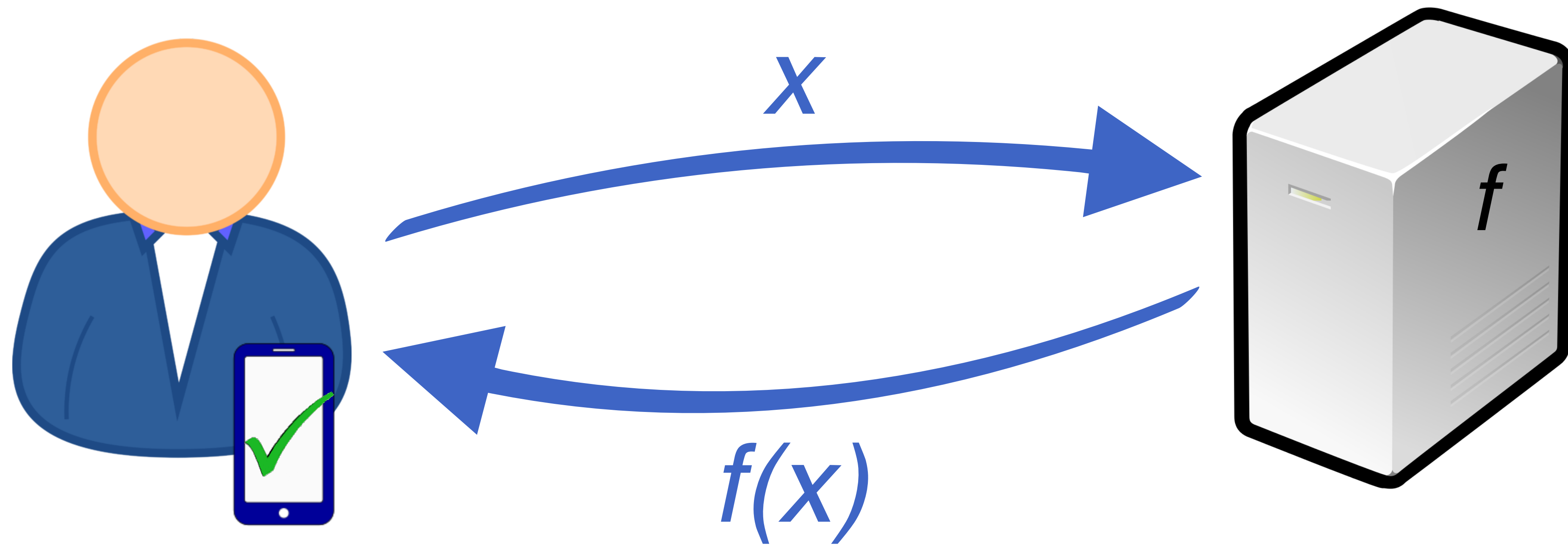
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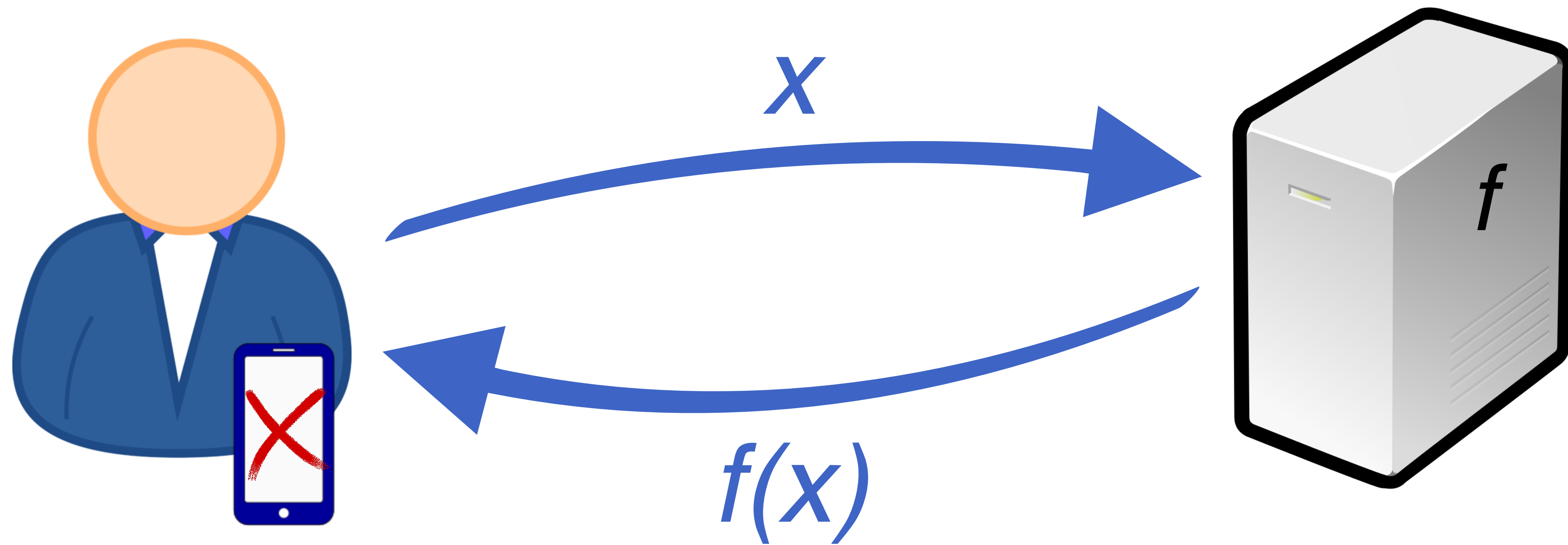
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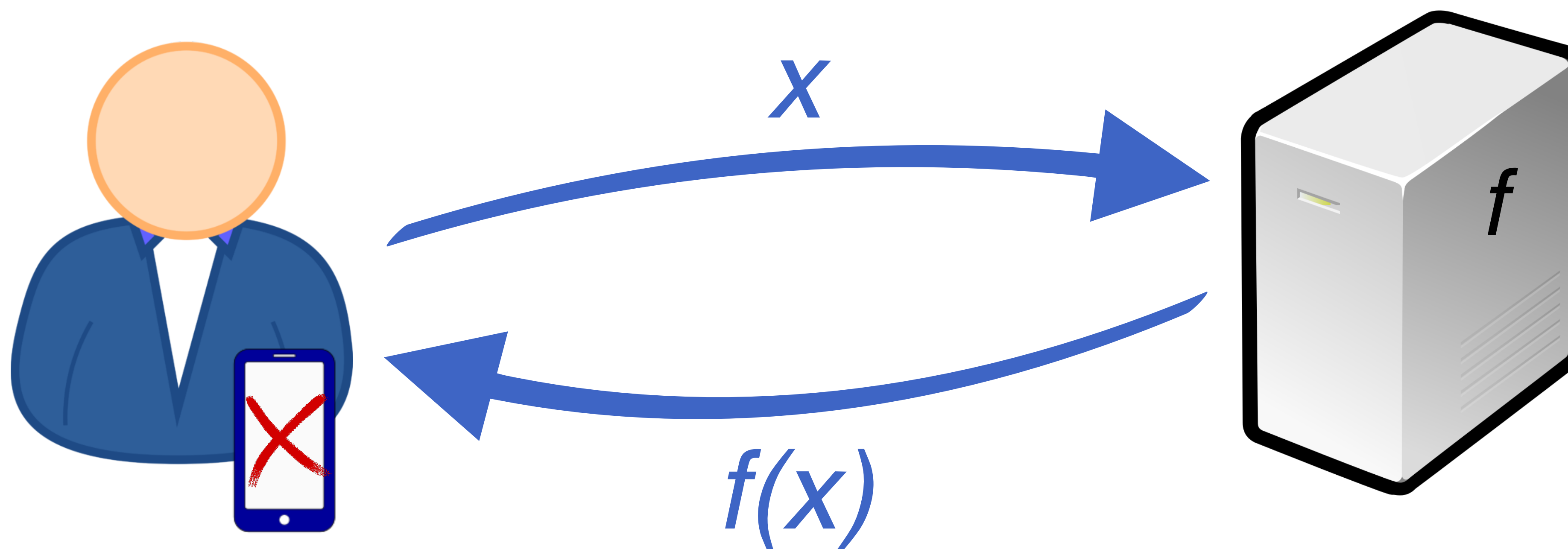
Verifiable Outsourced Computation



Verifiable Outsourced Computation

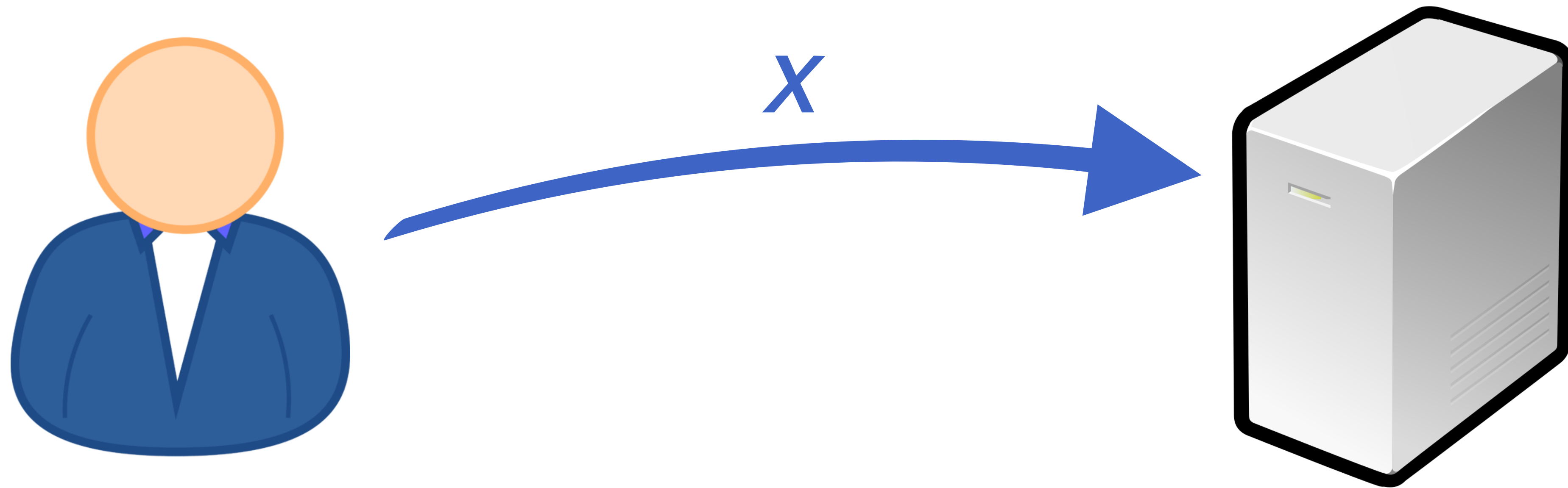


Verifiable Outsourced Computation

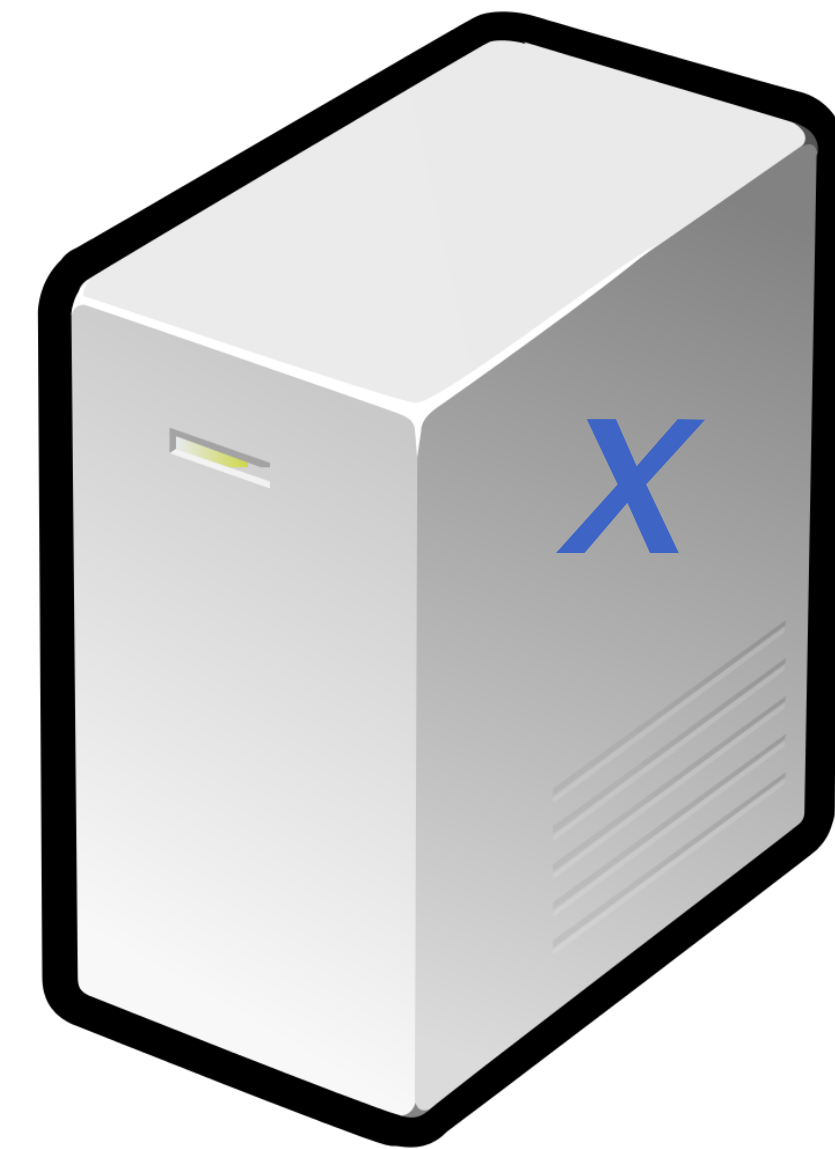
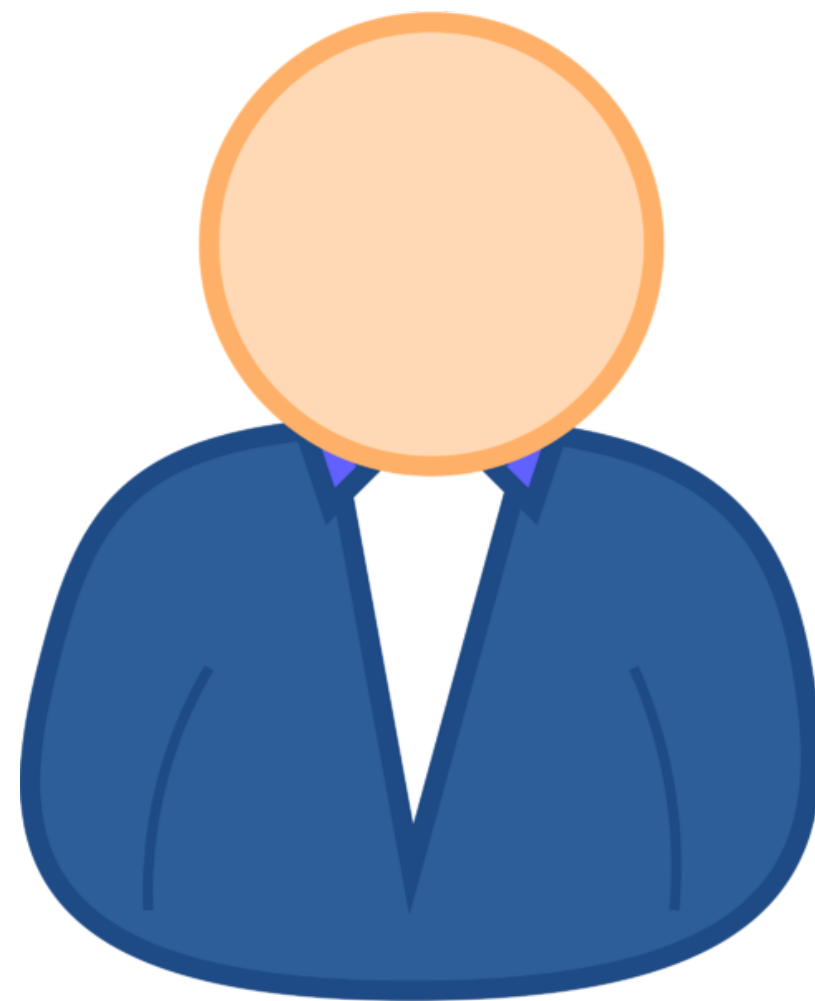


Outsourcing and verifying must be cheaper than computing $f(x)$ locally

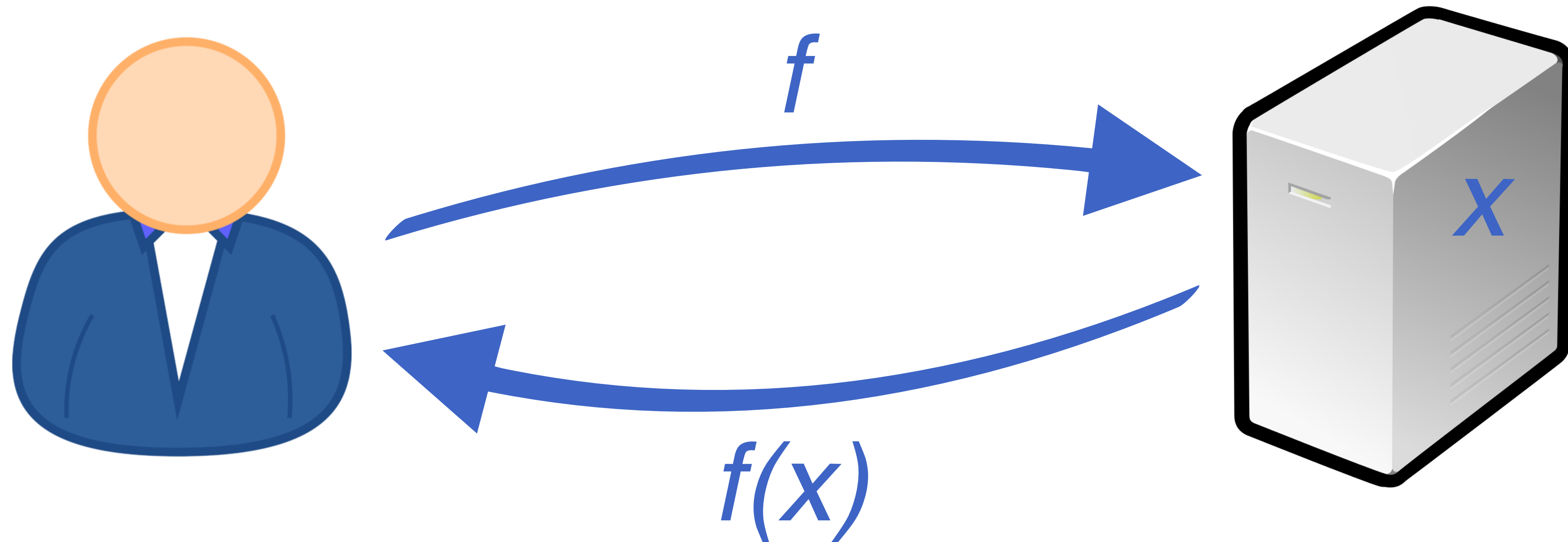
Searchable Encryption/Memory Delegation



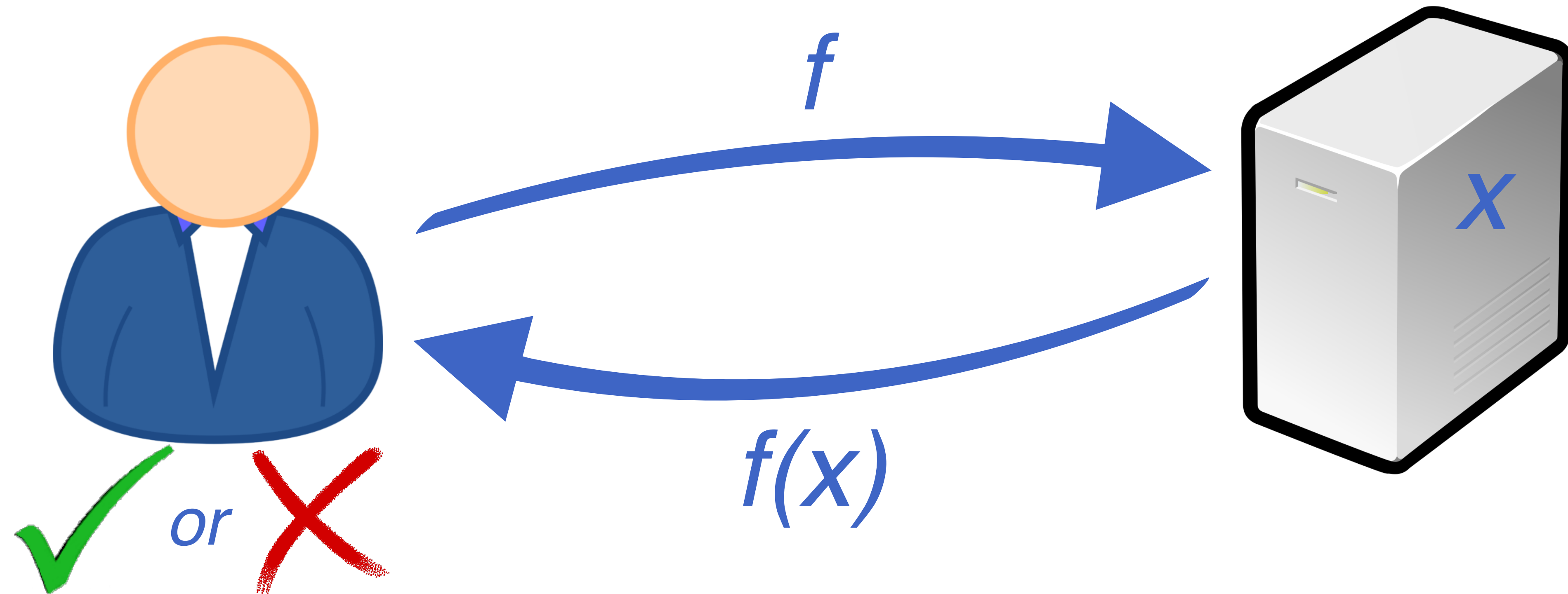
Searchable Encryption/Memory Delegation



Searchable Encryption/Memory Delegation



Searchable Encryption/Memory Delegation





Our work



Our work - a hybrid system



- Entities can act as both servers and clients as required
- Can sell spare resources to perform computations for others, or request computations when resources run low
- Data to be processed may be provided by the client or stored at the server
- Can restrict which servers can perform a given computation

Modes of Operation



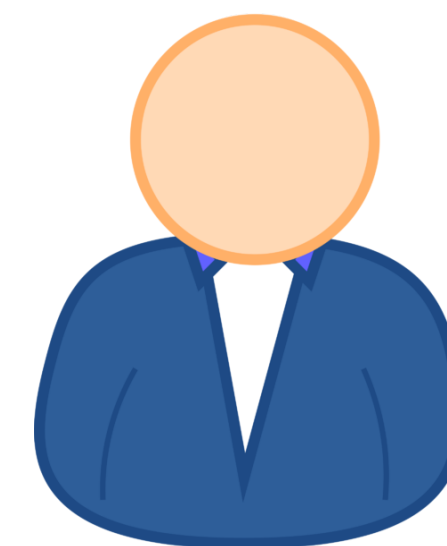
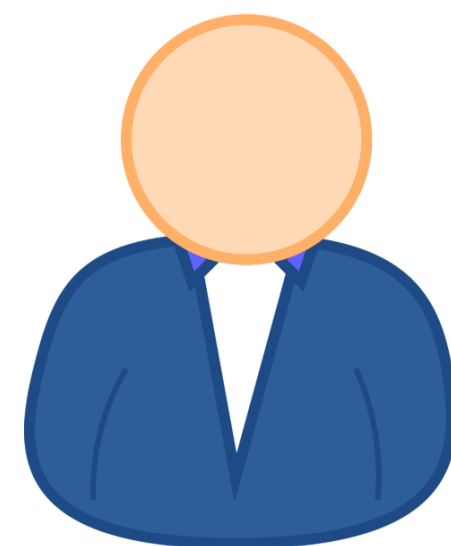
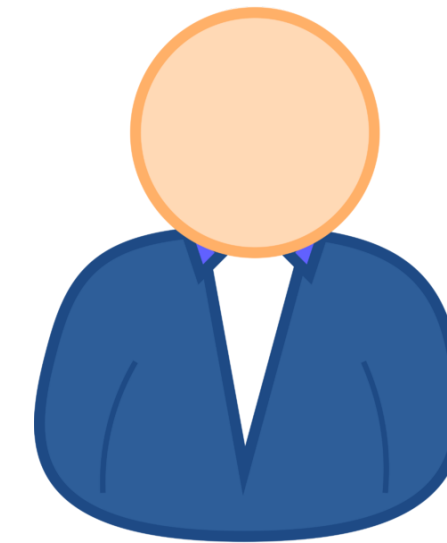
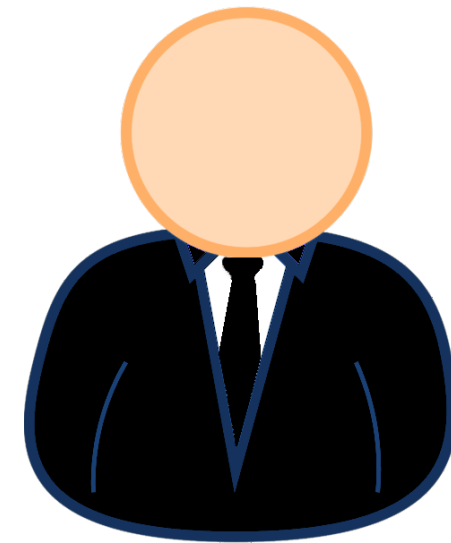
- We allow three modes of operation:
 - **Revocable Publicly Verifiable Computation (RPVC)**: client provides data, anybody can verify correctness, misbehaving servers can be revoked
 - **Revocable Publicly Verifiable Computation with access control (RPVC-AC)**: as above, but can restrict the servers that may compute on a given input
 - **Verifiable Delegable Computation (VDC)**: server holds data, clients request computations using public labels of the data, anybody can verify correctness

Definition

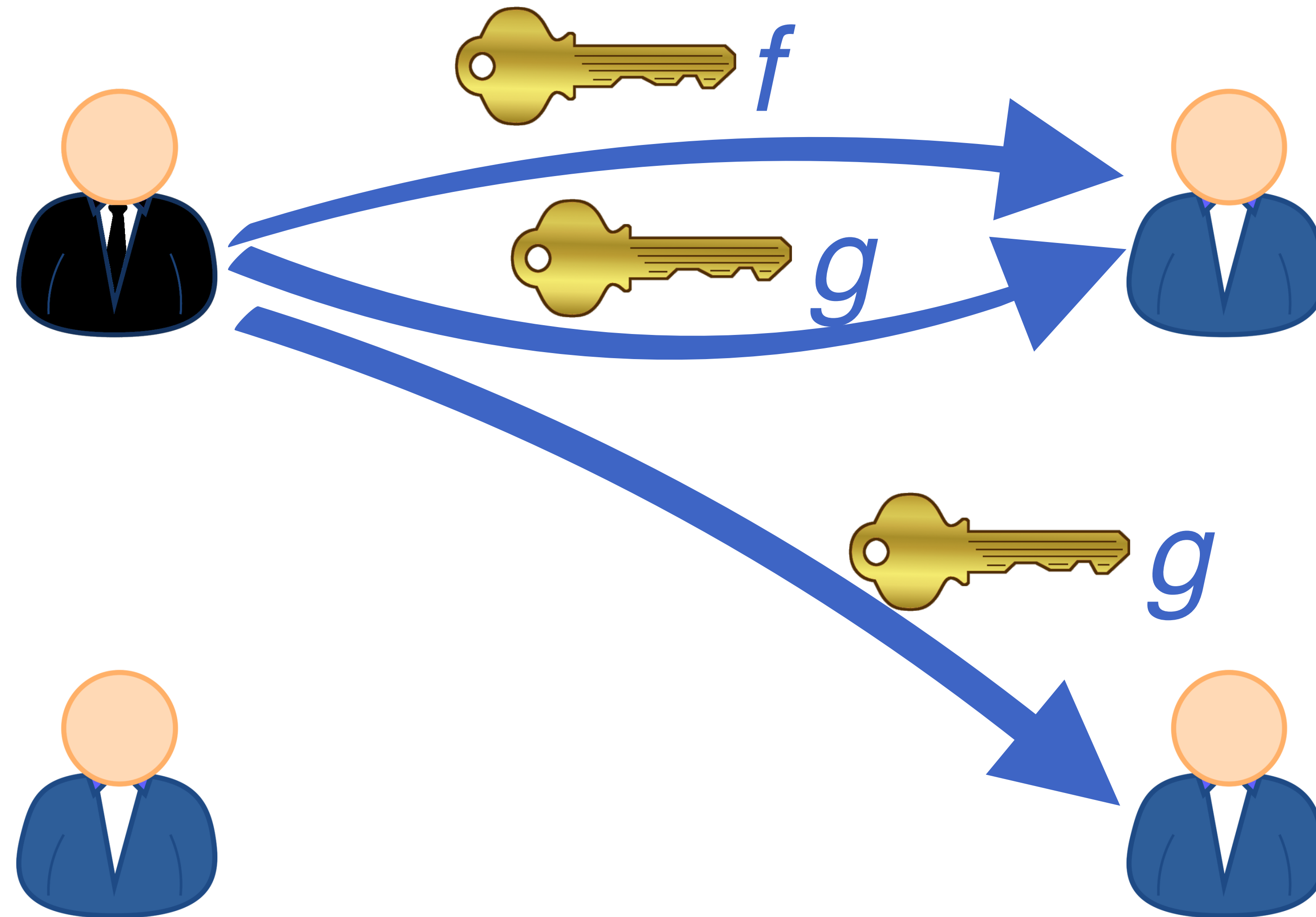


- $(PP, MK) \leftarrow \mathbf{Setup}(1^k, F)$
- $PK_F \leftarrow \mathbf{FnInit}(F, MK, PP)$
- $SK_S \leftarrow \mathbf{Register}(S, MK, PP)$
- $EK_{(\mathbf{O}, \boldsymbol{\psi}), S} \leftarrow \mathbf{Certify}(\text{mode}, S, (\mathbf{O}, \boldsymbol{\psi}), L_i, F_i, MK, PP)$
- $(\sigma_{F, X}, VK_{F, X}) \leftarrow \mathbf{ProbGen}(\text{mode}, (\boldsymbol{\omega}, \mathbf{S}), L_{F, X}, PK_F, PP)$
- $\theta_{F(X)} \leftarrow \mathbf{Compute}(\text{mode}, \sigma_{F, X}, EK_{(\mathbf{O}, \boldsymbol{\psi}), S}, SK_S, PP)$
- $(y, \tau_{F(X)}) \leftarrow \mathbf{Verify}(\theta_{F(X)}, VK_{F, X}, PP)$
- $UM \leftarrow \mathbf{Revoke}(\tau_{F(X)}, MK, PP)$

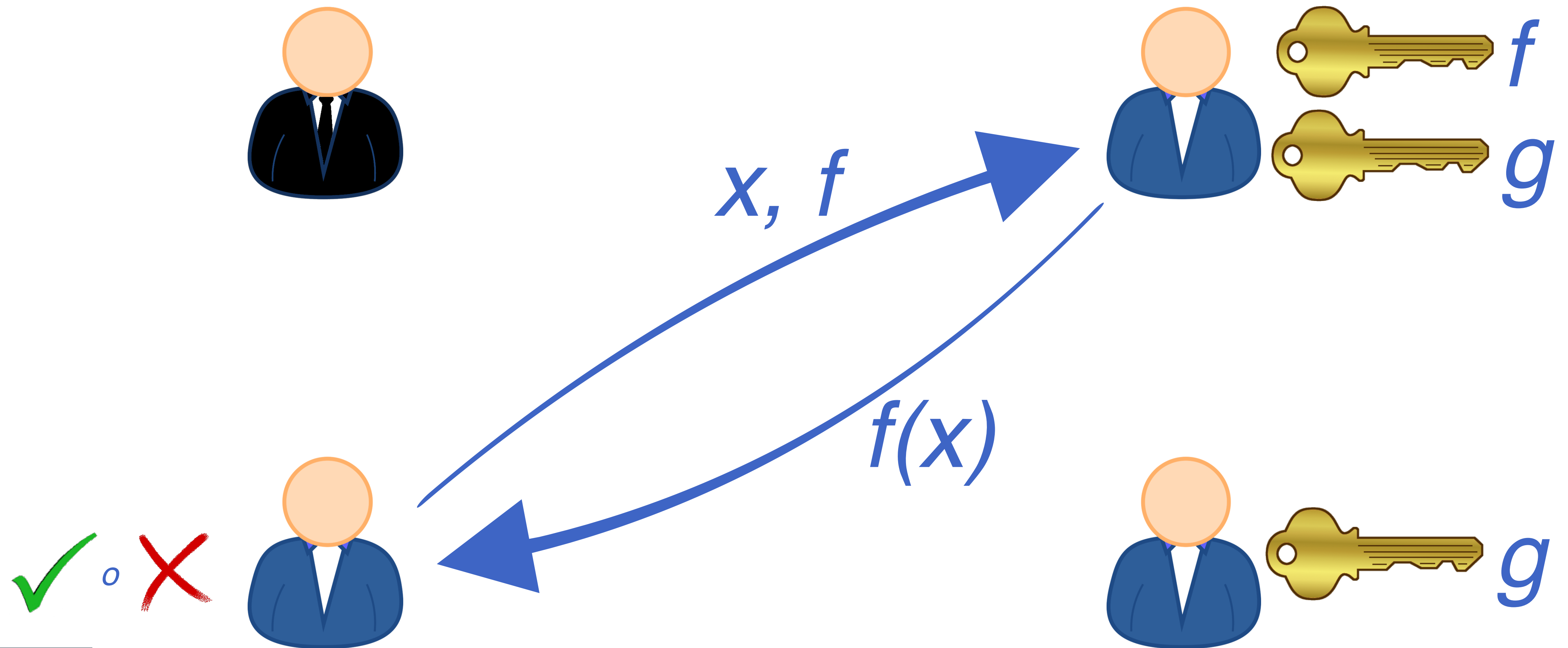
Our model



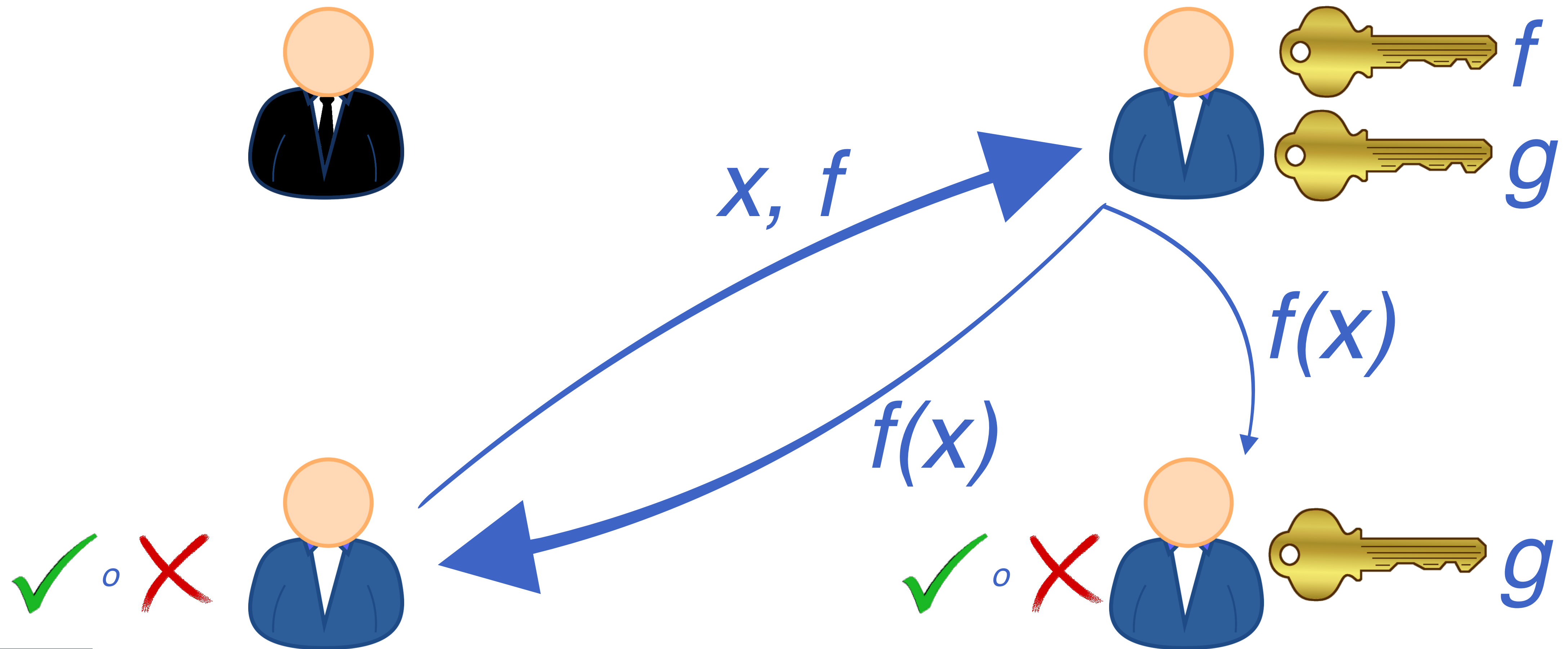
Our model - certifying servers



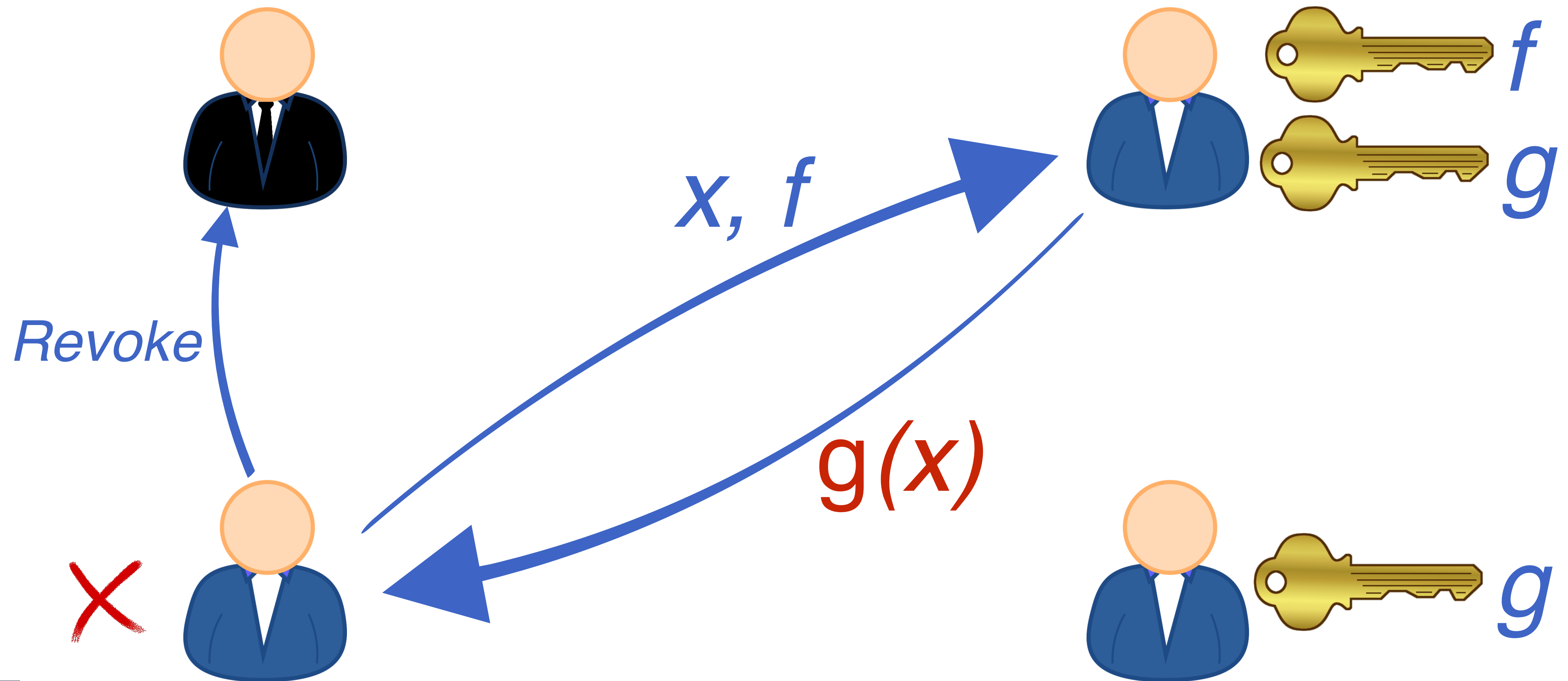
Our model - RPVC



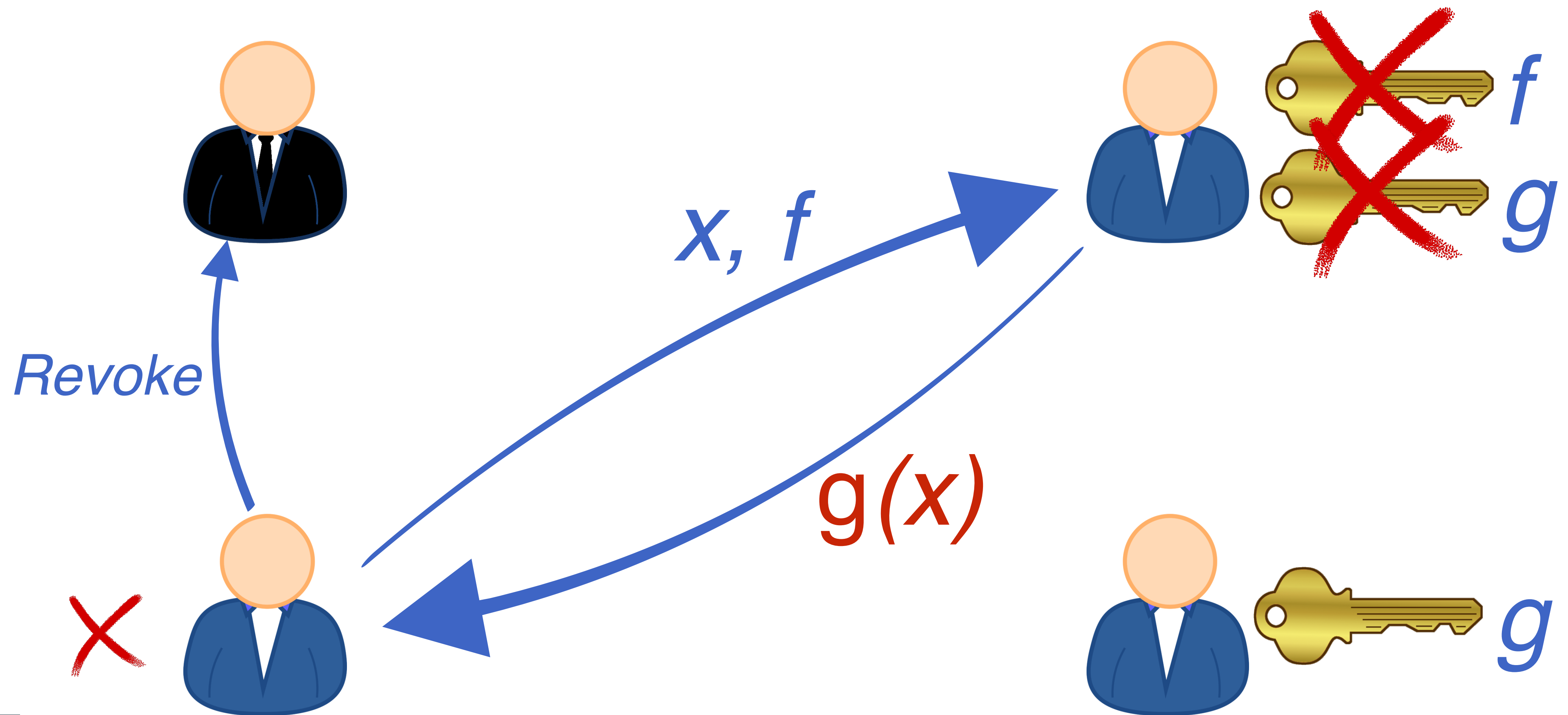
Our model - public verifiability



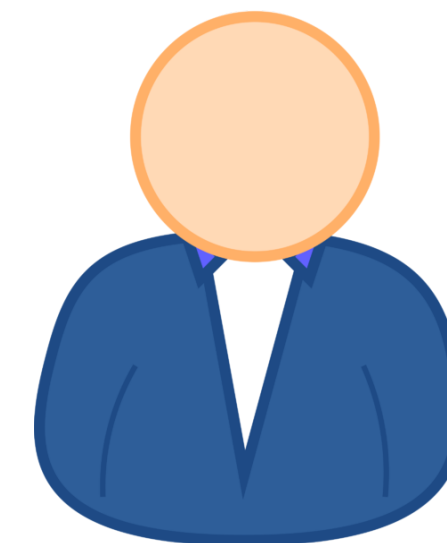
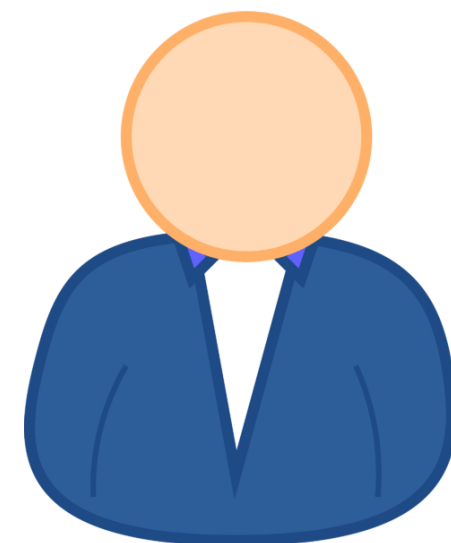
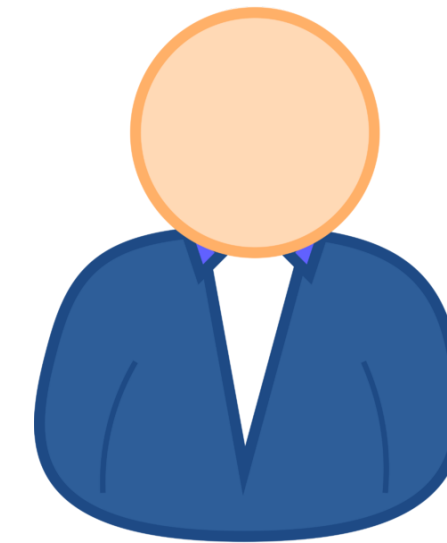
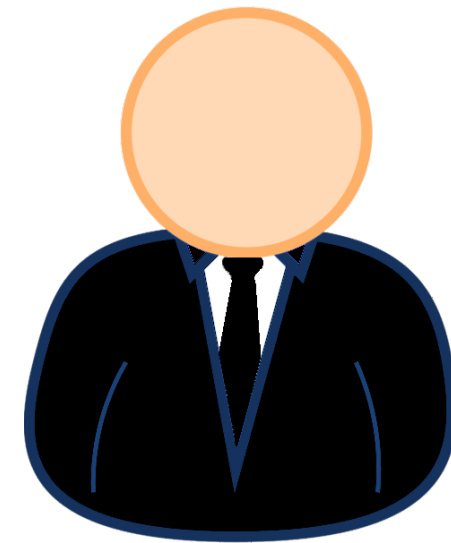
Our model - revocation



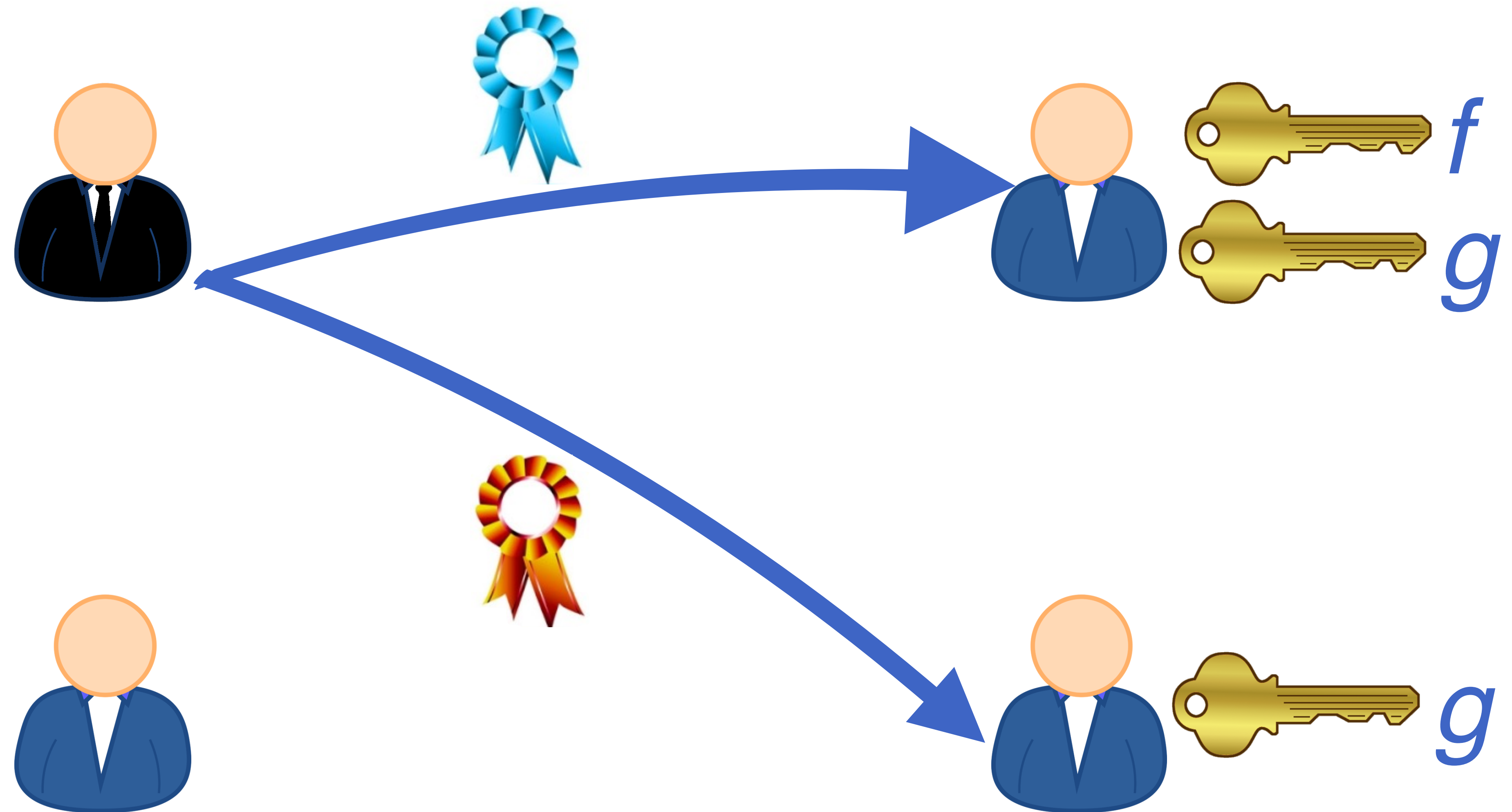
Our model - revocation



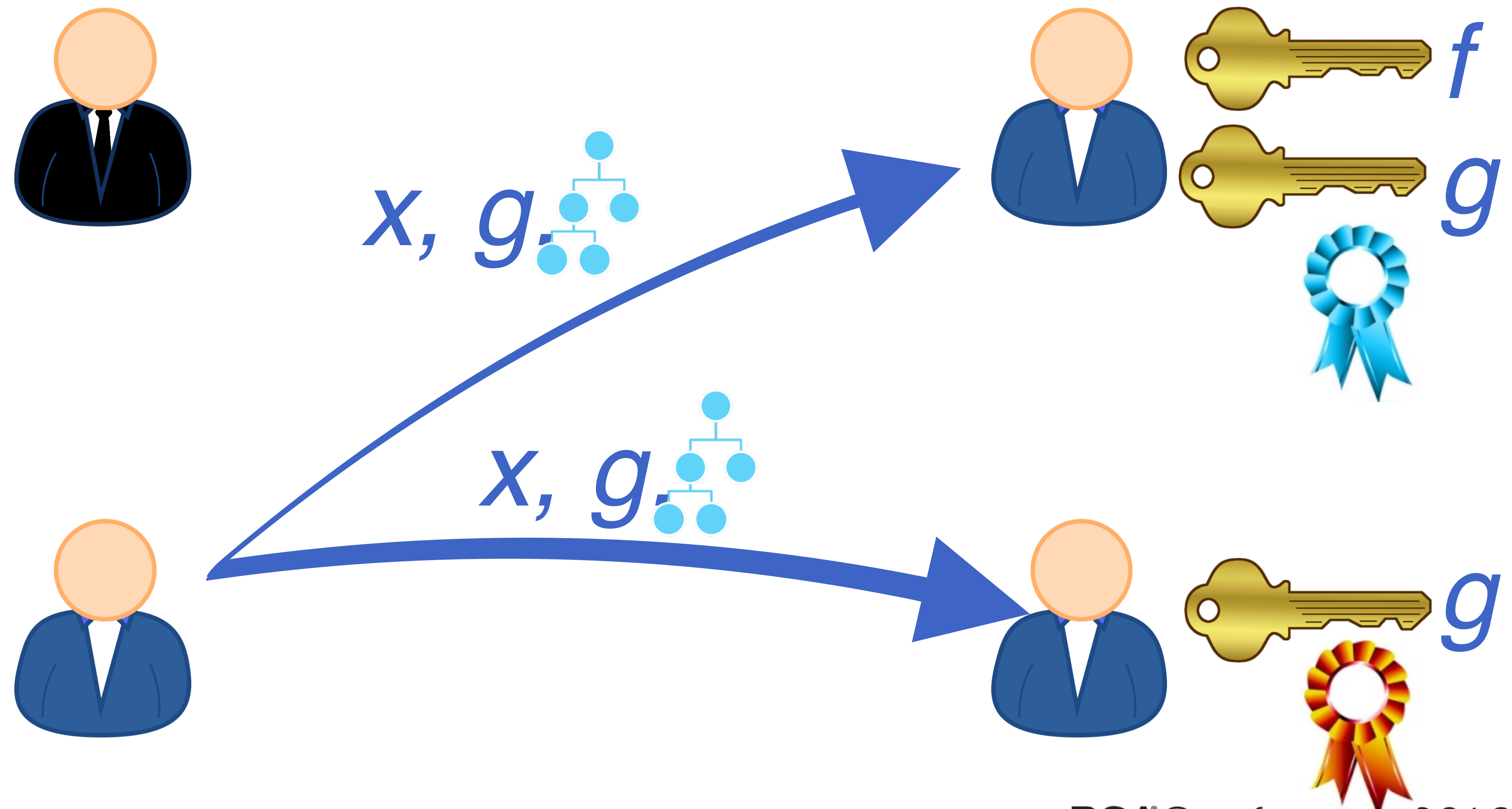
Our model - RPVC with Access Control



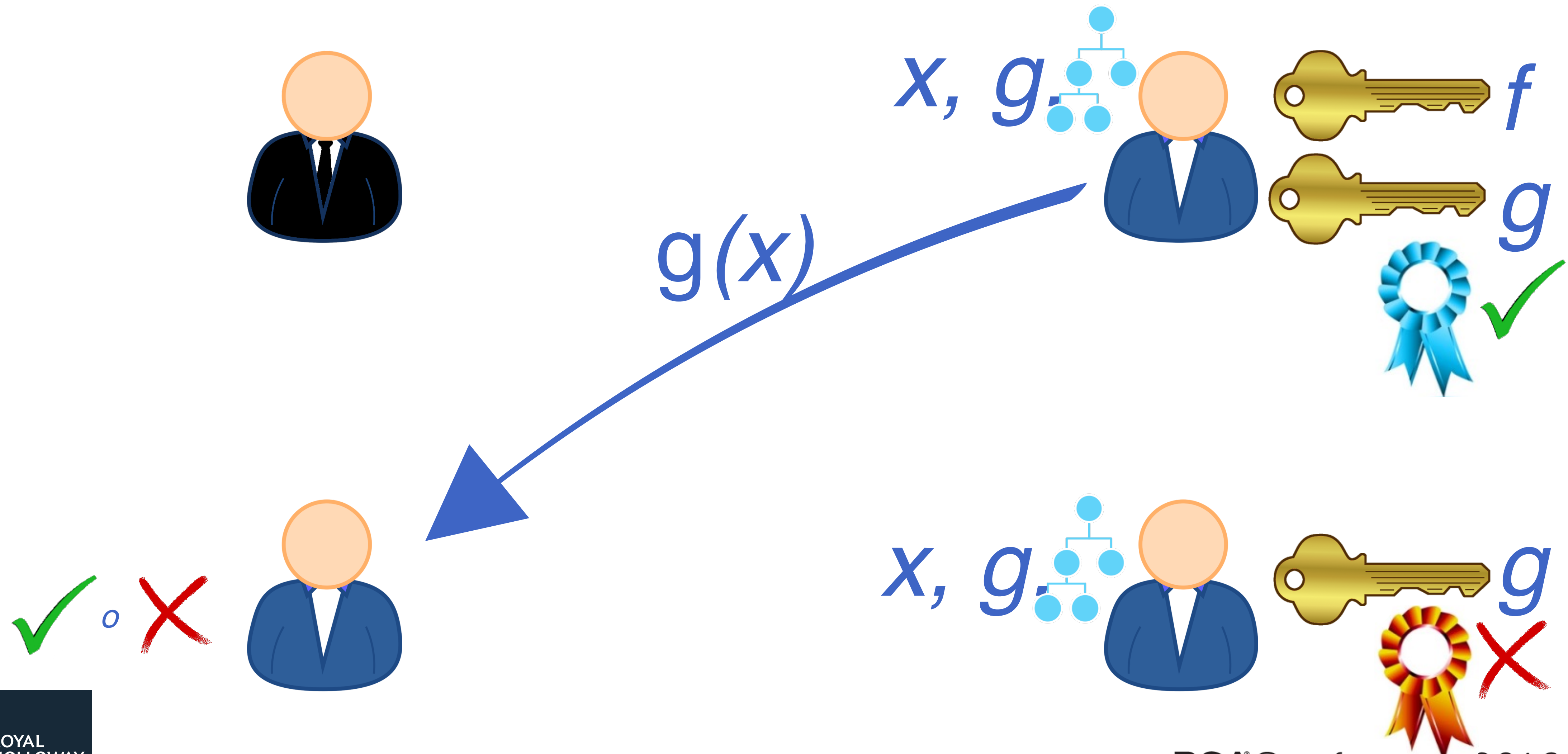
Our model - RPVC with Access Control



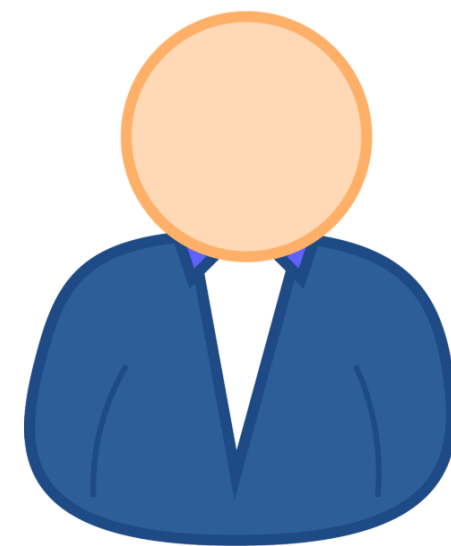
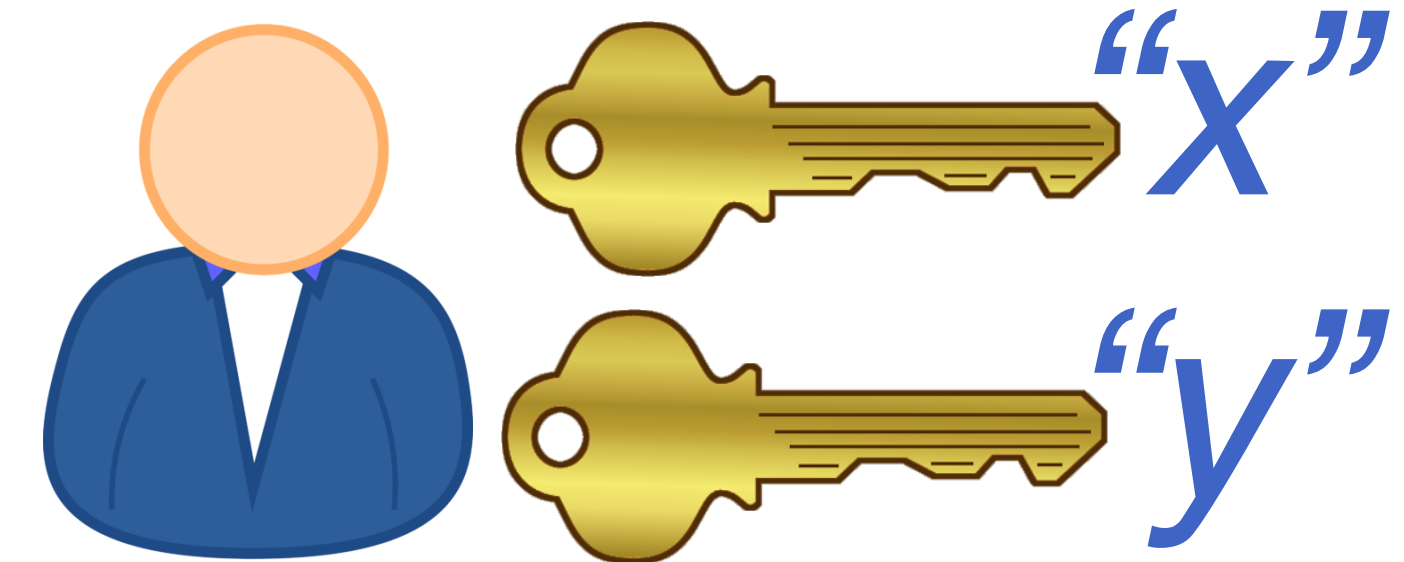
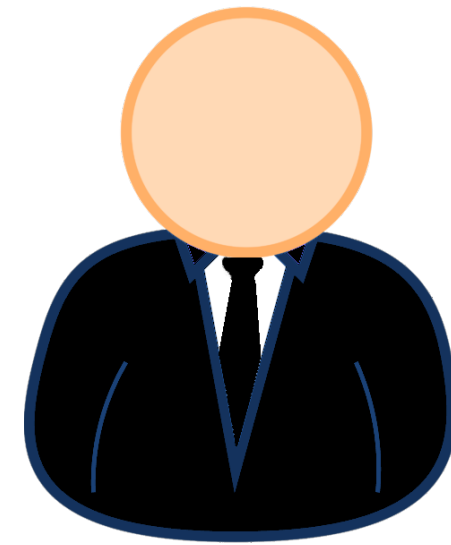
Our model - RPVC with Access Control



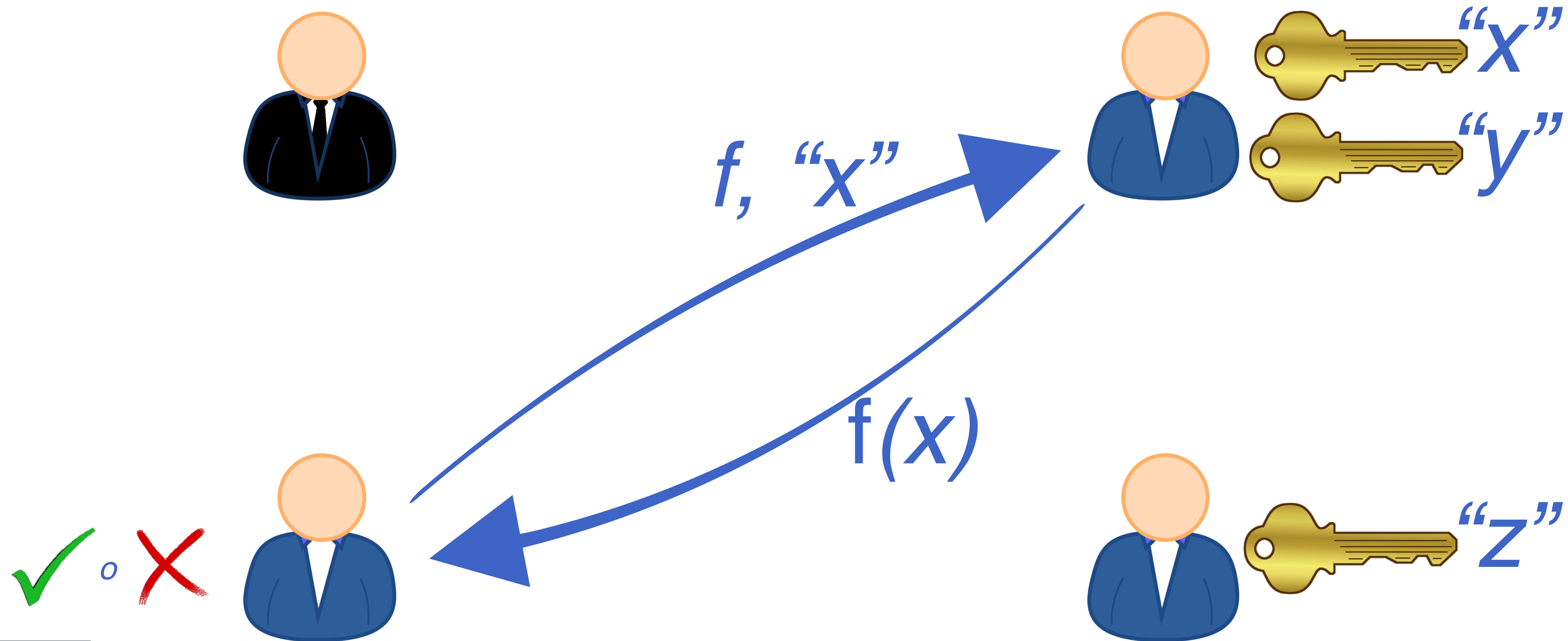
Our model - RPVC with Access Control



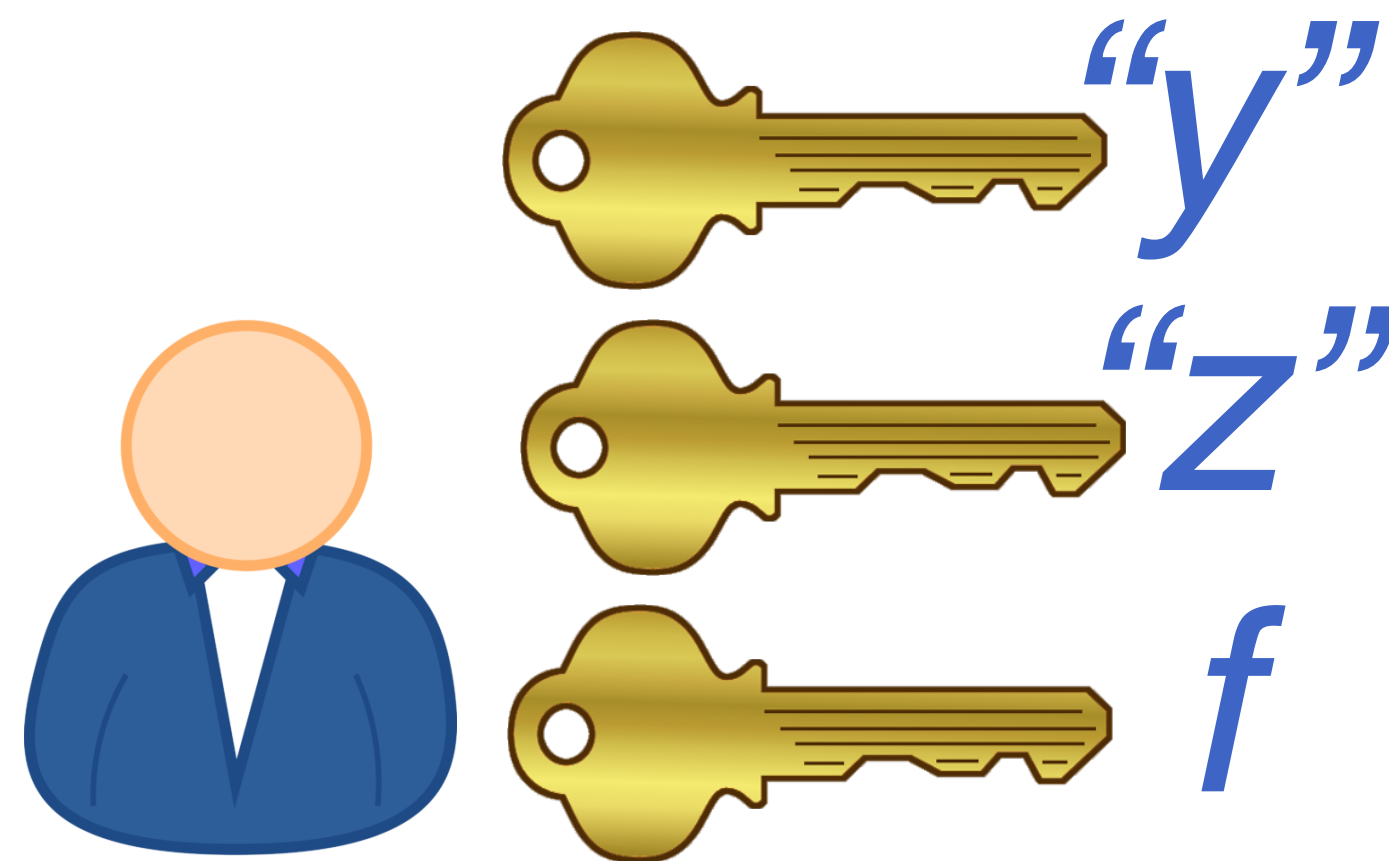
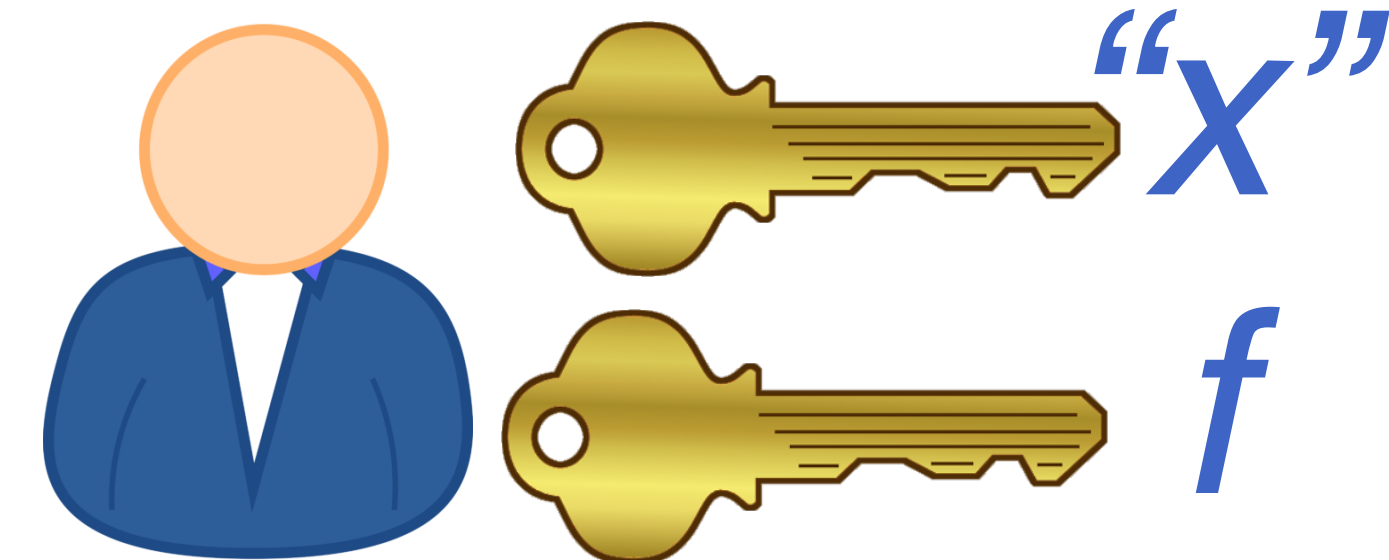
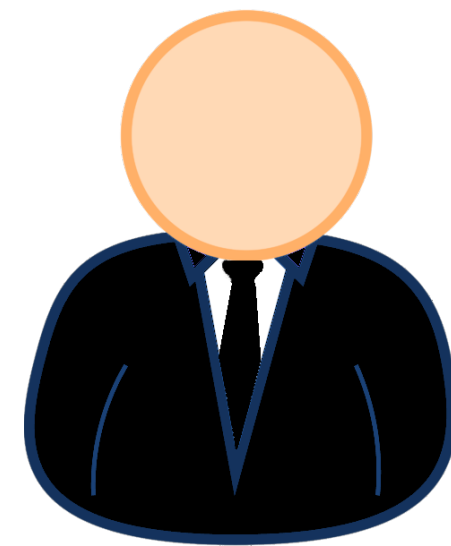
Our model - VDC



Our model - VDC

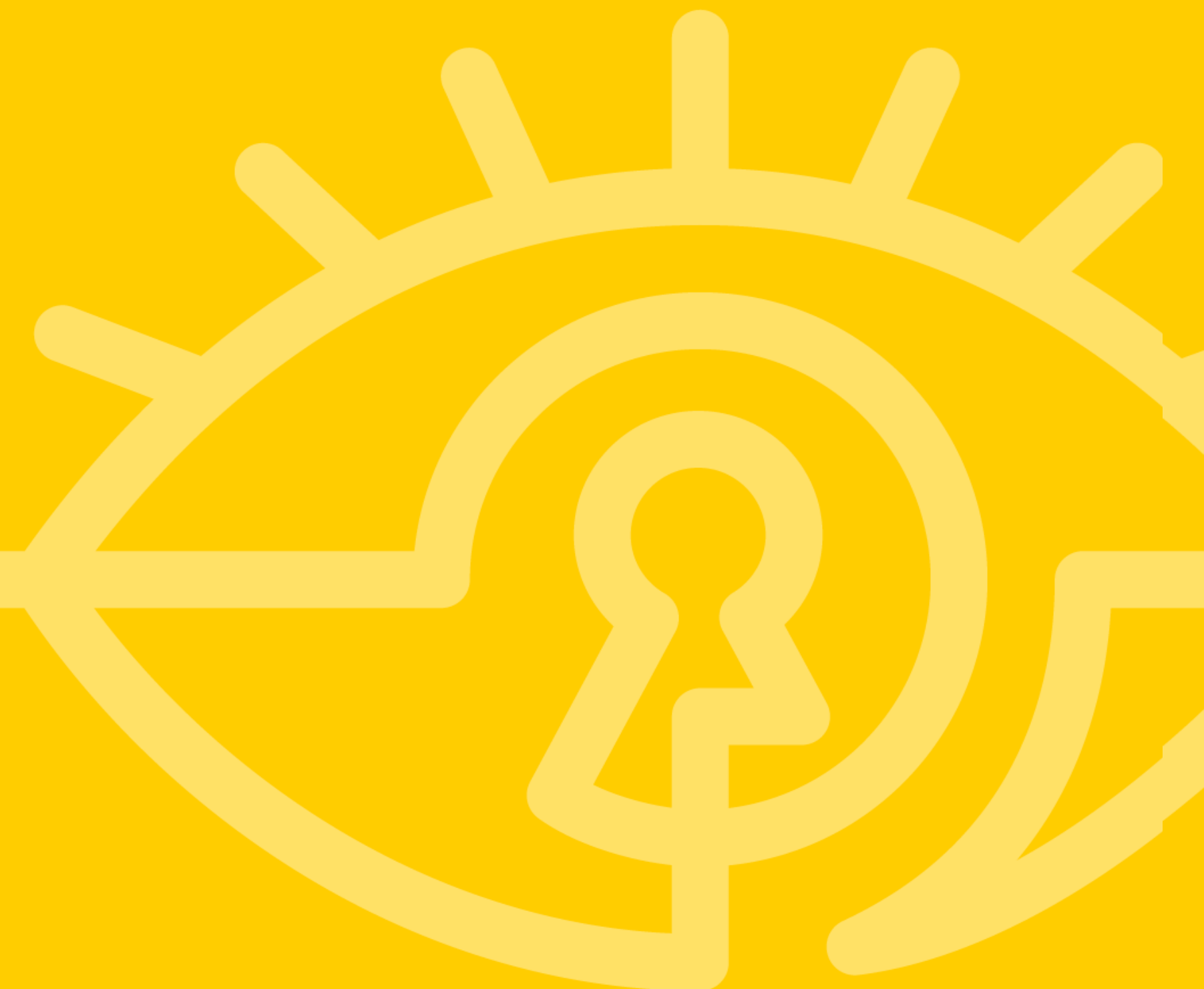


Our model - hybrid





Technical Details



Our approach



- Our approach extends the key-policy attribute-based encryption scheme of Parno et al. [TCC '12] for Boolean functions
- Functions are encoded as attribute-based policies
- Input data is encoded as attributes
- Outsourced computations are encryptions of random messages under the input attributes
- Successful decryption \Rightarrow Policy satisfied \Rightarrow Function evaluates to 1 on input. Repeat for the compliment function

Our approach



- We introduce Revocable-Key Dual-policy Attribute-based Encryption
- DP-ABE combines key-policy and ciphertext-policy attribute-based encryption
- RPVC mode uses KP-ABE (functions in server evaluation keys)
- VDC mode uses CP-ABE (data in server evaluation keys)
- RPVC with access control mode uses both — server key comprises function and authorisation attributes, ciphertext comprises input data and authorisation policy

Revocable-key DP-ABE



- $(PP, MK) \leftarrow \mathbf{Setup}(1^k, U)$
- $CT_{(\omega, \mathbf{S}), t} \leftarrow \mathbf{Encrypt}(m, (\omega, \mathbf{S}), t, PP)$
- $SK_{(\mathbf{O}, \psi), ID} \leftarrow \mathbf{KeyGen}(ID, (\mathbf{O}, \psi), MK, PP)$
- $UK_{R, t} \leftarrow \mathbf{KeyUpdate}(R, t, MK, PP)$
- $m \leftarrow \mathbf{Decrypt}(CT_{(\omega, \mathbf{S}), t}, (\omega, \mathbf{S}), SK_{(\mathbf{O}, \psi), ID}, (\mathbf{O}, \psi), UK_{R, t}, PP)$
 - if and only if $\omega \in \mathbf{O}$ and $\psi \in \mathbf{S}$
 - if and only if $\mathbf{O}(\omega) = 1$ and $\mathbf{S}(\psi) = 1$

\mathbf{S}, \mathbf{O} policies
 ψ, ω attribute sets

Definition



Recall:

- $(PP, MK) \leftarrow \mathbf{Setup}(1^k, F)$
- $PK_F \leftarrow \mathbf{FnInit}(F, MK, PP)$
- $SK_S \leftarrow \mathbf{Register}(S, MK, PP)$
- $EK_{(\mathbf{O}, \boldsymbol{\psi}), S} \leftarrow \mathbf{Certify}(\text{mode}, S, (\mathbf{O}, \boldsymbol{\psi}), L_i, F_i, MK, PP)$
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- $\theta_{F(X)} \leftarrow \mathbf{Compute}(\text{mode}, \sigma_{F, X}, EK_{(\mathbf{O}, \boldsymbol{\psi}), S}, SK_S, PP)$
- $(y, \tau_{F(X)}) \leftarrow \mathbf{Verify}(\theta_{F(X)}, VK_{F, X}, PP)$
- $UM \leftarrow \mathbf{Revoke}(\tau_{F(X)}, MK, PP)$

Parameter Choices



- Recall: key has policy \mathcal{O} and attributes ψ
- Ciphertext has policy \mathcal{S} and attributes ω

Mode	\mathcal{O}	ψ	ω	\mathcal{S}	label	F_i
RPVC	F	$\{T_o\}$	x	$\{\{T_s\}\}$	"F"	F
RPVC-AC	F	p	x	\mathcal{P}	"F"	F
VDC	$\{\{T_o\}\}$	x	$\{T_o\}$	F	"x"	F_1, F_2, \dots, F_n

\mathcal{S}, \mathcal{O} policies
 ψ, ω attribute sets
 T_o, T_s dummy attributes
 p authorisation attributes
 \mathcal{P} authorisation policy

b authorisation policy
 b authorisation attributes



- **Public Verifiability** — cheating servers are detected, servers can't use evaluation keys for different functions
- **Revocation** — revoked servers can't produce acceptable outputs
- **Authorised Computation** — only servers that satisfy the authorisation policy can produce acceptable outputs
- **Indistinguishability against selective-target with semi-static query attack (IND-sHRSS)** — security model for revocable-key DP-ABE

Summary



- We introduce a hybrid framework for flexible outsourcing of computations
 - RPVC - revocable outsourcing on local data
 - RPVC-AC - RPVC with access control policies detailing which servers can perform the computation
 - VDC - verifiable querying on remote data
- We introduce Revocable-Key Dual-policy Attribute-based Encryption to enable revocation of misbehaving entities



Thank you

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