

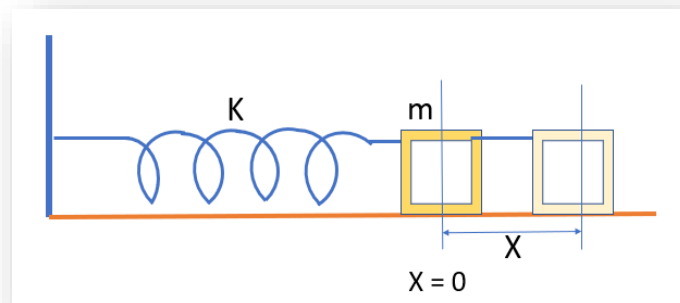
Mass-Spring System:

It consists of a block of mass m and a spring of spring constant k . It has two types:

- (i) Horizontal Mass-Spring System
- (ii) Vertical Mass-Spring System

(i) Horizontal Mass-Spring System:

Consider a horizontal mass-spring system of a block of mass m and a spring of spring constant k , as shown in the figure below.



Let the system be displaced through a distance X .

(Note: You are also free to use small letter 'x' for displacement for consistency through the chapter of SHM). Then a restoring force is developed such that the system has the tendency to come back to the mean position.

It is found that the **restoring force** is directly proportional to the **displacement** from the mean position and is **opposite** to it .

i.e. $F \propto X$

or, $F = -kX$, k being a constant of proportion, and is called the spring constant.

or, $ma = -kX$

Substituting the value of acceleration, we get

$$m \frac{d^2 X}{dt^2} + kX = 0$$

$$\boxed{\frac{d^2 X}{dt^2} + \omega^2 X = 0} \quad (1)$$

$$\text{where, } \omega = \sqrt{\frac{k}{m}}$$

(the angular frequency)

Equation (1) is the required **differential equation** of SHM. Hence the **motion** of the horizontal mass-spring system is simple harmonic.

To find the time period:

Since the time period is given by

$$T = \frac{2\pi}{\omega}$$

And from above, we have

$$\omega = \sqrt{\frac{k}{m}}$$

So,

$$T = 2\pi \sqrt{\frac{m}{k}}$$