Given the LPP with the objective function:

MAX.
$$Z = 2x_1 + 5x_2$$

subject to the list of constraints

$$x_1 + 4x_2 \le 24$$

$$3 x_1 + x_2 \le 21$$

$$x_1 + x_2 \le 9$$

```
%Matrices are directly derived from the Question
%cost matrix
z = [2;5];
%Coefficient matrix
A = [1 \ 4;3 \ 1;1 \ 1];
%b vector
b = [24;21;9];
%introducing slack variables
I = eye(size(A,1));
%we take slack vars as basic vars
Basic_vars = [3;4;5];
                      % 1 -> x1 ; 2 -> x2 ; 3 -> s1 ; 4 -> s2 ; 5
-> s3
*here all the constraint are having less than inequality so coeff. of I
will be +1 only
Table_1 = [A,I];
Z_{row} = [transpose(-z) 0 0 0 0];
%Append the Zj - Cj row in the table
Table_1 = [Table_1,b];
Table_1 = [Z_row; Table_1];
know we have to decide the exiting variable and the entering variable
%-----%
[min_ele,idx] = min(Z_row,[],'all');
%Checking whether the element is negative or not
if (min_ele >= 0)
   %the table is already the optimal table
   Table 1
```

```
opti_ans = answer(Table_1,Basic_vars);
   Optimal_Value = opti_ans(1,1)
   x1 = opti_ans(2,1)
   x2 = opti_ans(3,1)
end
%find mrv of idx column
mrv = find_mrv(Table_1,b,idx);
%-----%
%finding the minimum MRV
[min_mrv,idx_mrv] = min(mrv,[],'all');
%the pivot row and pivot element
pivot_ele = Table_1(idx_mrv+1,idx);
pivot_row = idx_mrv + 1;
%updating the basic variables
Basic_vars(pivot_row - 1,1) = idx;
%Creating new table
Table_2 = change_table(Table_1,pivot_ele,pivot_row,idx);
Now doing the same procedure for to make table 3
[min_ele,idx] = min(Table_2(1),[],'all');
%Checking whether the element is negative or not
if (min_ele >= 0)
   %the table is already the optimal table
   Table_1
   Table_2
   opti_ans = answer(Table_2, Basic_vars);
   Optimal_Value = opti_ans(1,1)
   x1 = opti_ans(2,1)
   x2 = opti_ans(3,1)
end
%finding the mrvs to find the exiting variable
mrv_2 = find_mrv(Table_2,b,idx);
[min_mrv,idx_mrv] = min(mrv_2,[],'all');
pivot_ele = Table_2(idx_mrv+1,idx);
pivot_row = idx_mrv+1;
%updating the basic variables
Basic_vars(pivot_row - 1,1) = idx;
```

```
%creating the third table
Table_3 = change_table(Table_2,pivot_ele,pivot_row,idx);
% Now doing the same procedure for to make table 4
[\min_{e} = \min_{e} \max_{i} \max_{j} \max_{i} \max_{j} \max_{i} \max_{j} \max_{j} \min_{e} \max_{j} \min_{i} \max_{j} \min_{j} \min_{e} \min_{j} \min_{e} \min_{j} \min_{e} \min_{e} \min_{j} \min_{e} \min
%Checking whether the element is negative or not
if (min_ele >= 0)
              %the table is already the optimal table
             Table 1
             Table_2
             Table 3
             opti_ans = answer(Table_3, Basic_vars);
             Optimal_Value = opti_ans(1,1)
             x1 = opti_ans(2,1)
             x2 = opti_ans(3,1)
end
Table_1 = 4 \times 6
           -2 -5
                                       0 0 0
                                                                                               0
                                                                0
                             4
                                              1
             1
                                                                                 0
                                                                                                 24
                            1
                                              0
                                                               1
              3
                                                                                 0 21
                                           0
                                                            0
                                                                              1
                                                                                               9
             1
                            1
Table_2 = 4x6
          -0.7500 0 1.2500 0
0.2500 1.0000 0.2500 0
                                                                                                                                       0 30.0000
       -0.7500
                                                                                                                                         0 6.0000
          2.7500
                                         0 -0.2500 1.0000
                                                                                                                                         0 15.0000
          0.7500
                                                  0 -0.2500
                                                                                                   0 1.0000
                                                                                                                                                       3.0000
Table_3 = 4 \times 6
                                                                                                 0 1.0000 33.0000
0 -0.3333 5.0000
                                                 0 1.0000
                       0
                                     1.0000 0.3333
                        0
                                         0 0.6667 1.0000 -3.6667
                        0
                                                                                                                                                        4.0000
                                                  0 -0.3333
           1.0000
                                                                                                   0
                                                                                                                          1.3333
                                                                                                                                                   4.0000
Optimal_Value = 33
x1 = 4
x2 = 5
function output = find_mrv(Table_1,b,idx)
              %taking i+1 as the first row is cost row(Zj - Cj)
              mrv = zeros([1 size(b,1)]);
              for i=1:size(b,1)
                           mrv(i) = Table_1(i+1,6)/Table_1(i+1,idx);
              end
              output = transpose(mrv);
end
function new_table = change_table(table, pivot_ele,pivot_row,idx)
```

%Changing Pivot row

```
for i=1:size(table,2)
         new_table(pivot_row,i) = table(pivot_row,i)/pivot_ele;
    end
   for i=1:size(table,1)
        if(i == pivot_row)
            continue
        else
            for j=1:size(table,2)
                new_table(i,j) = table(i,j) -
table(i,idx)*new_table(pivot_row,j);
            end
        end
    end
end
function output = answer(table,basic_vars)
    %Find the indices of 1 and 2 in basic vars vector
   x1_idx = find(basic_vars==1) + 1;
   x2_idx = find(basic_vars==2) + 1;
    %Final Answer
    output(1,1) = table(1,size(table,2));
    output(2,1) = table(x1_idx ,size(table,2));
    output(3,1) = table(x2_idx ,size(table,2));
end
```