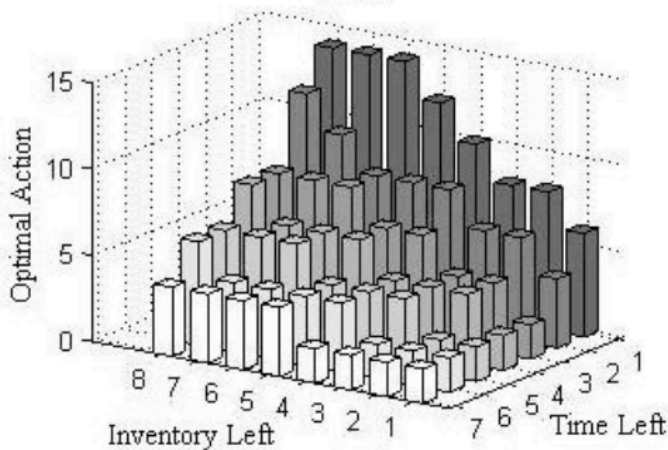


# Trade Execution Optimization

Theoretical computer science:  
*One-way trading problem*



Nevmyvaka, Yuriy, Yi Feng, and Michael Kearns.  
"Reinforcement learning for optimized trade execution."  
Proceedings of the 23rd international conference on Machine learning. ACM, 2006.

"How can we buy (respectively sell)  $V$  shares within a time horizon  $T$ , in a manner that minimizes the capital spent (respectively, maximizes the revenue received)?"

## Private Variables:

- Remaining Inventory  $i$
- Remaining time left  $t$
- (Maker/taker fees)

## Market Variables:

- Drawn from order book that evolves over time
- E.g. market volume, liquidity, volatility
- More advanced features: technical analysis
- Examination of their performance impact

Order book

Sell Orders

Buy Orders

5734.00

5733.20

5731.50

5731.00

5730.10

5730.00

5729.00

5728.30

5728.00

5726.80

5726.20

5725.90

5725.00

5.378

0.023

0.003

1.000

0.088

8.117

0.873

0.002

2.308

0.255

0.008

0.009

0.424

18.488

13.110

13.087

13.084

12.084

11.996

3.879

3.006

3.004

0.696

0.441

0.433

0.424

5721.20 EUR

5721.00

5720.10

5720.00

5718.90

5716.80

5715.60

5715.20

5714.30

5711.10

5711.00

5706.00

5697.40

5686.70

10.790

14.420

7.447

3.210

3.090

1.448

6.890

0.050

0.438

0.013

2.175

0.260

0.050

10.790

25.210

32.657

35.867

38.957

40.405

47.295

47.345

47.783

47.796

49.971

50.231

50.281

5738.00

5737.70

5737.00

5736.00

5735.00

5734.20

5734.00

5733.40

5733.20

5731.50

5731.00

5730.10

5730.00

1.037

0.070

1.000

0.009

0.382

0.018

5.378

0.100

0.296

0.003

1.000

0.088

6.927

16.308

15.271

15.201

14.201

14.192

13.810

13.792

8.414

8.314

8.018

8.015

7.015

6.927

5730.00 EUR

5729.70

5728.60

5726.80

5725.00

5721.50

5721.40

5721.10

5721.00

5720.20

5720.00

5715.60

5714.30

5711.10

0.014

0.015

2.063

0.066

0.093

0.710

6.740

0.484

2.550

105.047

1.448

0.050

0.438

0.014

0.029

2.092

2.158

2.251

2.961

9.701

10.185

12.735

117.782

119.230

119.280

119.718

State at:  $t$

State at:  $t+1$

## Reinforcement Learning

Action  $a$ : placing a limit order at price  $ask$   
 $= 0 \rightarrow ask\ price$   
 $> 0 \rightarrow buyer\ side\ of\ book$   
 $< 0 \rightarrow sell\ side\ of\ book$

## Other approaches:

Online Learning  
 Neural Nets  
 Genetic algorithm

Detecting market specific patterns  
 Detecting buy/sell walls

## Evaluation

Commonly compared against mid-spread price:  $(ask+bid) / 2$

Outlook: evolve into *market maker*, seeking to profit from the difference between the buy and sell price of an asset