

# **Value Iteration for Dynamic Programming**

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# Bellman Equations

## Bellman Expectation Equation

$$v_{\pi}(s) = E_{\pi}[R_{t+1} + \gamma v_{\pi}(s_{t+1}) | S_t = s]$$

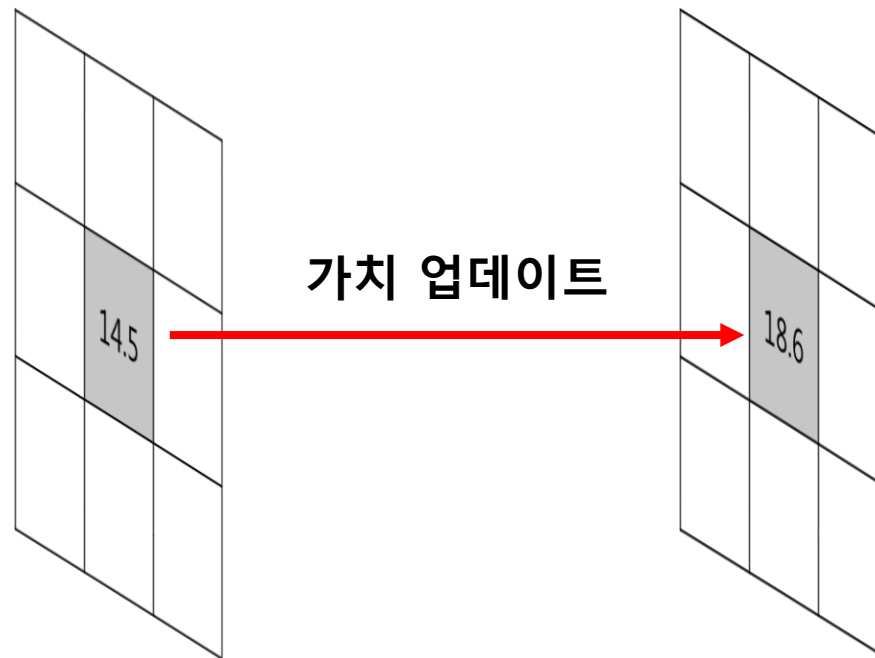


최적의 정책을 찾은 후  
이를 통해 계산된  
최적 Value function

## Bellman Optimality Equation

$$v_{*}(s) = \max_a E_{\pi}[R_{t+1} + \gamma v_{*}(s_{t+1}) | S_t = s, A_t = a]$$

## (Remind)



현재 (땅의) 가치

보다 그럴듯한 (땅의) 가치

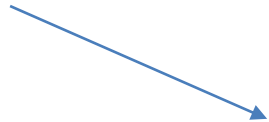
- 최초에는 땅의 가치를 모르기 때문에(동등, uniform)
- 목표점까지 갈 수 있는 땅들이 높은 값을 가질 수 있게
- 가치를 업데이트 할 수 있는 방법이 필요하다.

# Value Iteration

[Insight]

$$v'(s) = \max_{a \in A} (R_s^a + \gamma v(s'))$$

Random Value Function



Slightly improved Random Value Function



Slightly improved Random Value Function



...



Optimal Value Function

Coding

# VALUE ITERATION METHOD

# Implementation

- Implement
  - `def update_value(self)`
  - `def get_action(self, state)`
- Useful Methods

| Method or Variables                                     | Description                                  |
|---|--|
| <code>self.env.possible_actions()</code>                | return all possible actions in current state |
| <code>self.env.state_after_action(state, action)</code> | retrieve next state                          |
| <code>self.get_value(state)</code>                      | return value of the state                    |
| <code>self.discount_factor</code>                       | discount factor                              |
| <code>self.env.get_reward(state, action)</code>         | get reward                                   |

**Download code**

<https://bit.ly/2m7jdEM>