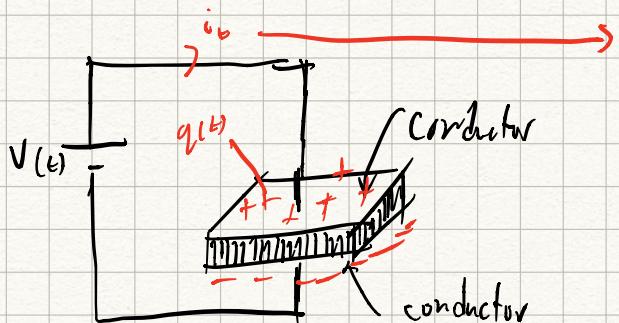
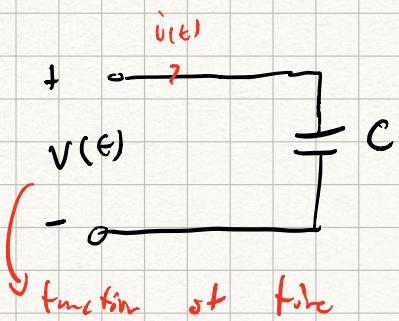


# CAPACITOR



there is no current between conductors, but  
there is always current;

## ideal linear capacitor



$$q(t) = C V(t)$$

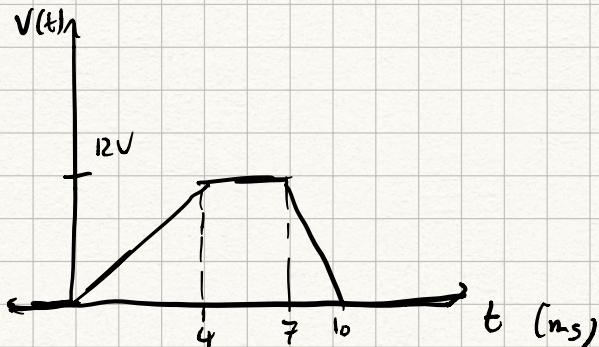
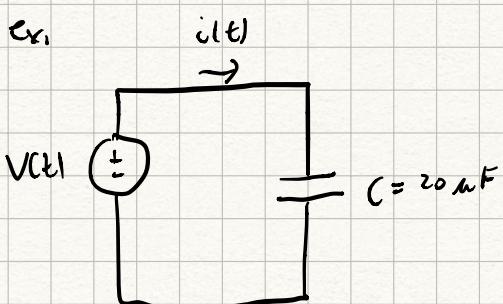
capacitance  $\frac{\text{Coulomb}}{\text{volt}} = \text{Farad (F)}$

→ how do we compute charge?

$$i(t) = C \frac{dV(t)}{dt}$$

! if  $V(t) = \text{constant}$ ,  $i(t) = 0$ .  
↳ open circuit!!!!

!  $V(t)$  cannot have a jump  
→ must be continuous 😊  
→ derivative not defined  
→ physically, can't instantly transfer charge

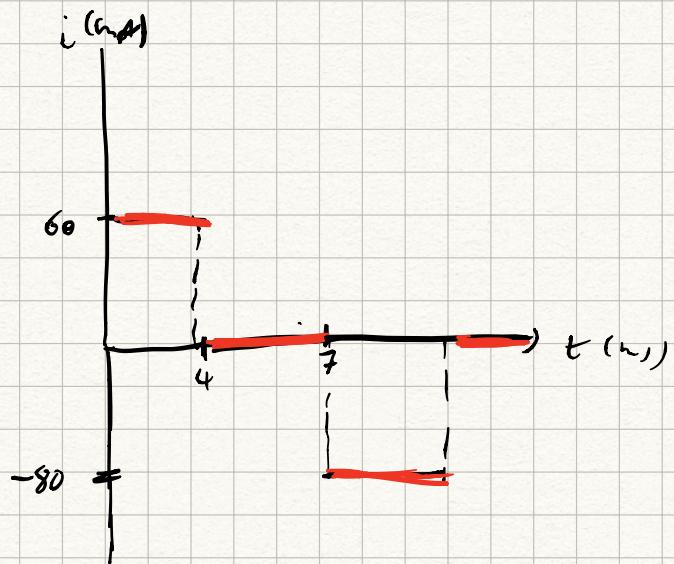


For  $0 < t < 4$  ms

$$i = (20 \times 10^{-6}) \left( \frac{12}{4 \times 10^{-3}} \right) = 60 \text{ mA}$$

For  $4 \leq t < 7$  ms

$$i = 0$$

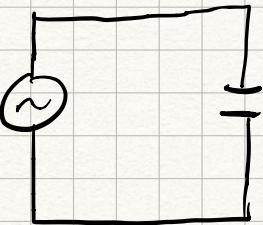


For  $7 \leq t < 10$  ms:

$$i = (20 \times 10^{-6}) \left( \frac{-12}{3 \times 10^{-3}} \right) = -80 \text{ mA}$$

$$V(t) = V(t_0) + \frac{1}{C} \int_{t_0}^t i(t) dt$$

# CAPACITORS IN AC



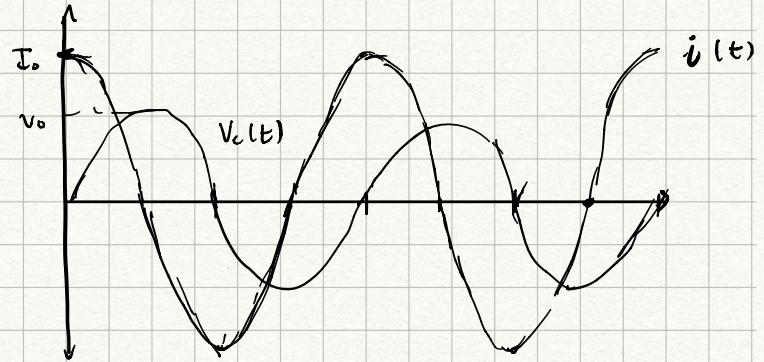
$$V(t) = V_0 \sin(\omega t) \quad (\text{Voltage across capacitor})$$

$$V_c(t) = V_0 \sin(\omega t) \quad (\text{Voltage across cap.})$$

how to find current across capacitor?

$$i = \frac{dQ}{dt} \quad \text{and} \quad Q = CV$$

$$i(t) = C \frac{dV}{dt} = C V_0 \omega \cos(\omega t)$$



$$\phi_I - \phi_v = 0 - \left(-\frac{\pi}{2}\right) = \frac{\pi}{2}$$

$\Rightarrow \cos$  and  $\sin$  always off by  $\frac{\pi}{2}$ , regardless of  $\omega$ .

## Capacitive Reactance

$$\text{Since } I_0 = CV_0 \omega$$

$$V_0 = \frac{1}{C\omega} I_0$$

$X_C$  = Capacitive reactance (equiv. to resistance,  $\Omega$ ).

When  $\omega \downarrow$ , open circuit. When  $\omega \uparrow$ , short circuit.

