

# Classic Models

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# Review

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- Query & Information Need
- Relevance
- Information Retrieval & Data Retrieval

# IR Modeling

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- Modeling in IR is a complex process aimed at producing a ranking function
  - Ranking function is a function that assigns scores to documents with regard to a given query
- This process consists of two main tasks
  - The conception of a logical framework for representing documents and queries
    - Representation
  - The definition of a ranking function that allows quantifying the similarities among documents and queries
    - Ranking

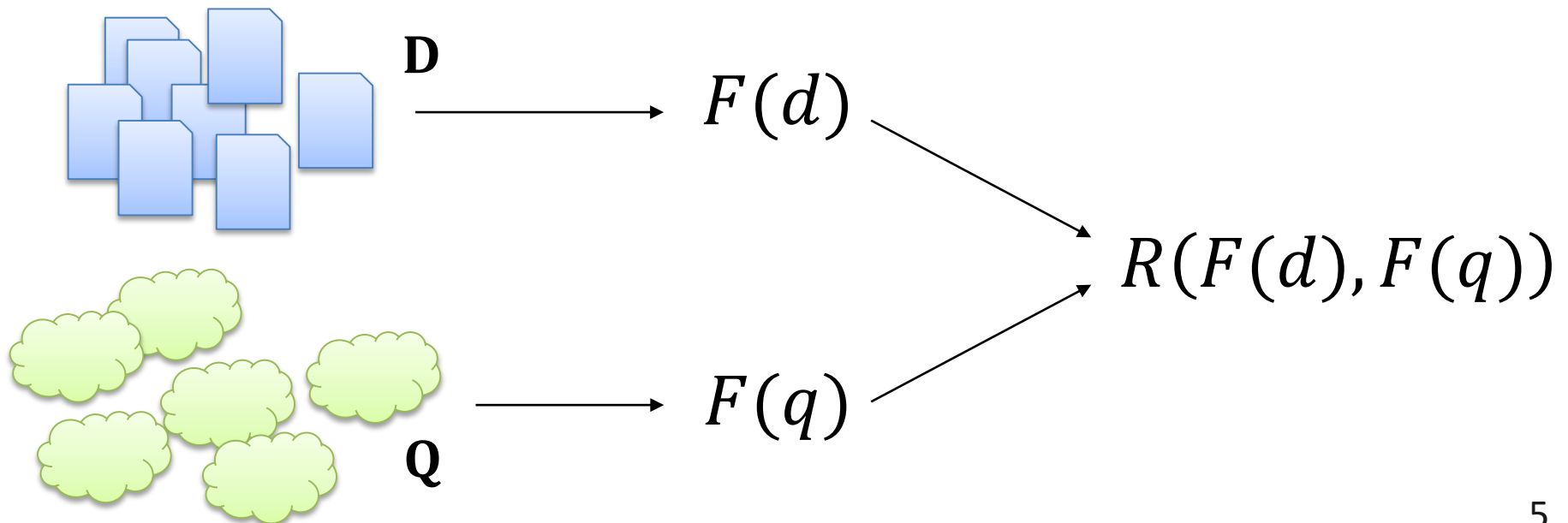
# Ranking

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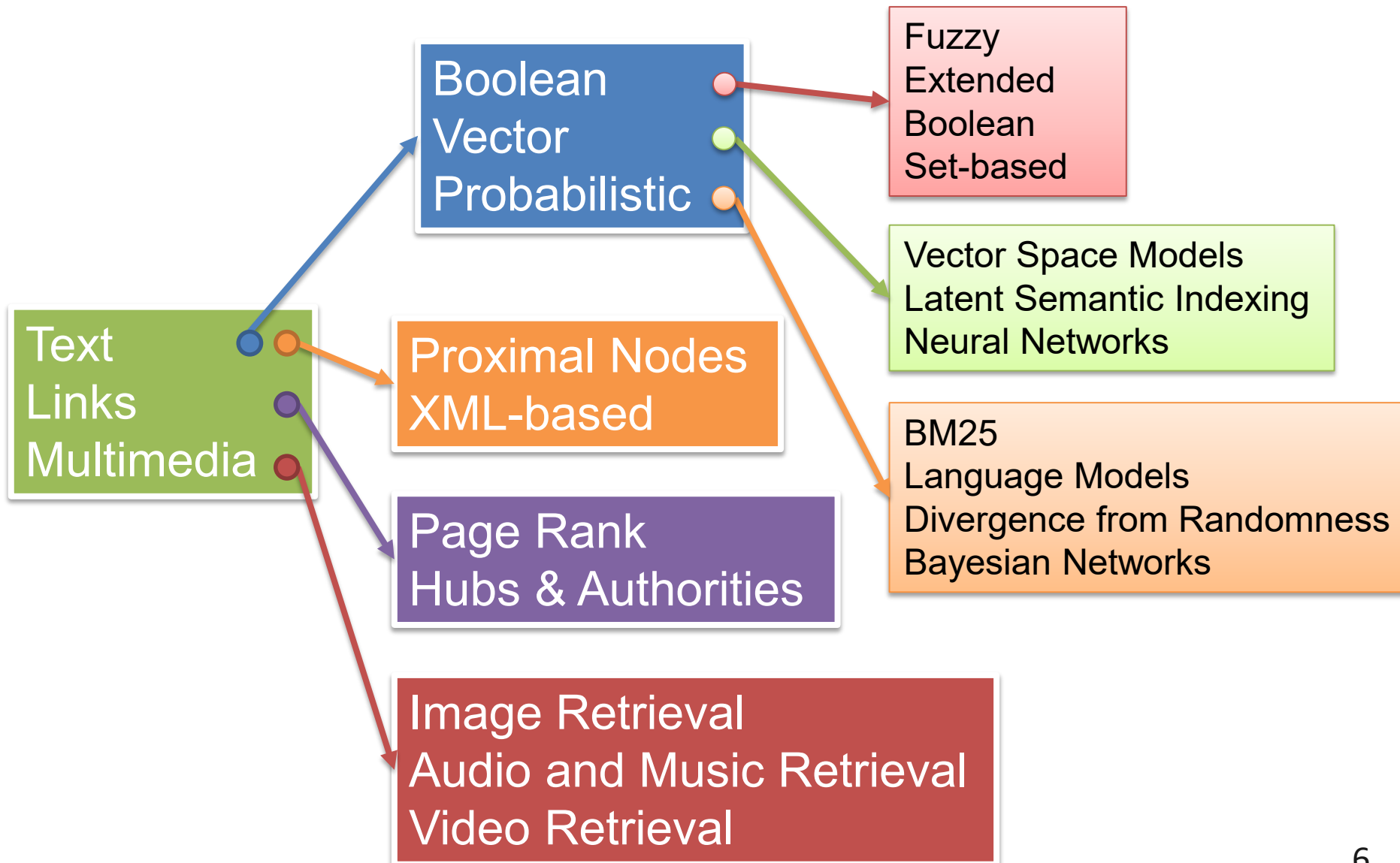
- A ranking is an ordering of the documents that reflects their relevance to a user query
- Any IR system has to deal with the problem of predicting which documents the users will find relevant
- This problem naturally embodies a degree of uncertainty, or vagueness
  - **Relevance!**

# Formal Expression

- An IR model is a **quadruple**  $[D, Q, F, R]$ 
  - $D$  is a set of documents in the collection  $D = \{d_1, \dots, d_{|D|}\}$
  - $Q$  is a set of user queries  $Q = \{q_1, \dots, q_{|Q|}\}$
  - $F$  is a function that translates the queries and documents into a sort of representations
  - $R$  is a ranking function



# Taxonomy of Classic IR Models



# Index Term

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- Each document is represented by a set of representative keywords or index terms
  - An index term is **a word or group of consecutive words** in a document
- A pre-selected set of index terms can be used to summarize the document contents
- However, it might be interesting to assume that **all words are index terms** (full text representation)

# **Boolean Model**



# Boolean Model – 1

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- Boolean model is a simple model, which based on **set theory** and **Boolean algebra**
- Documents are represented by a term-document incidence matrix
  - Terms are units
- Queries specified as Boolean expressions
  - quite intuitive and precise semantics
  - neat formalism

# Boolean Model – 2

- For documents
  - $d_1$  = The way to avoid linearly scanning is to index the documents in advance
  - $d_2$  = The model views each document as just a set of words
  - $d_3$  = We will discuss and model these size assumption

		$d_1$	$d_2$	$d_3$
Vocabulary / Lexicon	⋮			
	way	1	0	0
	document	1	1	0
	model	0	1	1
	avoid	1	0	0
	view	0	1	0
	discuss	0	0	1
	advance	1	0	0
	⋮			

# Boolean Model – 3

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- For term-document matrix
  - Each row associates with a term, which shows the documents it appears in
  - Each column associates with a document, which reveals the terms that occur in it

	$d_1$	$d_2$	$d_3$
⋮			
way	1	0	0
document	1	1	0
model	0	1	1
avoid	1	0	0
view	0	1	0
discuss	0	0	1
advance	1	0	0
⋮			

# Boolean Model – 4

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- Let's query “way”

$$\text{way} = [1 \ 0 \ 0]$$

$$\therefore \text{answer} = d_1$$

	$d_1$	$d_2$	$d_3$
⋮			
way	1	0	0
document	1	1	0
model	0	1	1
avoid	1	0	0
view	0	1	0
discuss	0	0	1
advance	1	0	0
⋮			

# Boolean Model – 5

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- Let's query non-“way”

$$\neg \text{way} = \neg [1 \ 0 \ 0] = [0 \ 1 \ 1]$$

$$\therefore \text{answer} = d_2 \ \& \ d_3$$

	$d_1$	$d_2$	$d_3$
⋮			
way	1	0	0
document	1	1	0
model	0	1	1
avoid	1	0	0
view	0	1	0
discuss	0	0	1
advance	1	0	0
⋮			

# Boolean Model – 6

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- Let's query “document” and “model”

$$\text{document} \wedge \text{model} = [1 \ 1 \ 0] \wedge [0 \ 1 \ 1] = [0 \ 1 \ 0]$$

$$\therefore \text{answer} = d_2$$

	$d_1$	$d_2$	$d_3$
⋮			
way	1	0	0
document	1	1	0
model	0	1	1
avoid	1	0	0
view	0	1	0
discuss	0	0	1
advance	1	0	0
⋮			

# Boolean Model – 7

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- Let's query “avoid” or “view”

$$\text{avoid} \vee \text{view} = [1 \ 0 \ 0] \vee [0 \ 1 \ 0] = [1 \ 1 \ 0]$$

$$\therefore \text{answer} = d_1 \& d_2$$

	$d_1$	$d_2$	$d_3$
⋮			
way	1	0	0
document	1	1	0
model	0	1	1
avoid	1	0	0
view	0	1	0
discuss	0	0	1
advance	1	0	0
⋮			

# Boolean Model – 8

- Let's query “avoid” and (“view” or non-”model”)

$$\text{avoid} \wedge (\text{view} \vee \neg \text{model}) = [1 \ 0 \ 0] \wedge ([0 \ 1 \ 0] \vee \neg[0 \ 0 \ 1])$$

$$[1 \ 0 \ 0] \wedge ([0 \ 1 \ 0] \vee [1 \ 1 \ 0])$$

$$[1 \ 0 \ 0] \wedge [1 \ 1 \ 0]$$

$$[1 \ 0 \ 0]$$

$$\therefore \text{answer} = d_1$$

	$d_1$	$d_2$	$d_3$
⋮			
way	1	0	0
document	1	1	0
model	0	1	1
avoid	1	0	0
view	0	1	0
discuss	0	0	1
advance	1	0	0
⋮			



# Boolean Model – Drawbacks

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- Retrieval based on binary decision criteria with **no notion of partial matching**
  - Data retrieval?
- **No ranking** of the documents is provided (absence of a grading scale)
- Information need has to be translated into a Boolean expression, which most users find awkward
  - The Boolean queries formulated by the users are most often too simplistic
- The model frequently returns either too few or too many documents in response to a user query

# Probabilistic Model

# The Probabilistic Model

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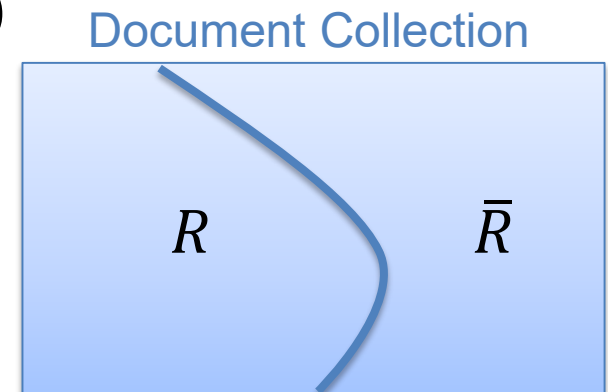
- The probabilistic model captures the IR problem using a **probabilistic framework**
  - Tries to estimate the **probability** that a document will be relevant to a user query
    - $P(R_q|d_j)$
  - Assumes that this probability depends on the query and document representations only
    - Hyper-links and other information
  - The **ideal answer set**, referred to as  $R$ , should maximize the probability of relevance

# Formal Expression

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- $R_q$  be the set of relevant documents to a given query  $q$
- $\bar{R}_q$  be the set of non-relevant documents to query  $q$
- $P(R_q|d_j)$  be the probability that  $d_j$  is relevant to the query  $q$
- $P(\bar{R}_q|d_j)$  be the probability that  $d_j$  is non-relevant to  $q$
- The relevance degree can be defined as

$$\text{sim}(d_j, q) = \frac{P(R_q|d_j)}{P(\bar{R}_q|d_j)}$$



# Derivation

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- By using Bayes' rule

$$\begin{aligned} \text{sim}(d_j, q) &= \frac{P(R_q | d_j)}{P(\bar{R}_q | d_j)} = \frac{\frac{P(R_q, d_j)}{P(d_j)}}{\frac{P(\bar{R}_q, d_j)}{P(d_j)}} = \frac{P(R_q, d_j)}{P(\bar{R}_q, d_j)} \\ &= \frac{\frac{P(R_q, d_j)}{P(\bar{R}_q, d_j)} P(R_q)}{\frac{P(\bar{R}_q, d_j)}{P(\bar{R}_q)} P(\bar{R}_q)} = \frac{P(d_j | R_q) P(R_q)}{P(d_j | \bar{R}_q) P(\bar{R}_q)} \propto \frac{P(d_j | R_q)}{P(d_j | \bar{R}_q)} \end{aligned}$$

**Constant for the given query  $q$**

# Probabilistic Model – 1

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- The probabilistic model can be computed by

$$\text{sim}(d_j, q) = \frac{P(d_j|R_q)P(R_q)}{P(d_j|\bar{R}_q)P(\bar{R}_q)} \propto \frac{P(d_j|R_q)}{P(d_j|\bar{R}_q)}$$

- $P(d_j|R_q)$  probability of randomly selecting the document  $d_j$  from the set  $R_q$
- $P(R_q)$  probability that a document randomly selected from the entire collection is relevant to query
- $P(d_j|\bar{R}_q)$  and  $P(\bar{R}_q)$  are analogous and complementary

# Probabilistic Model – 2

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- We make the Naive Bayes conditional independence assumption that the presence or absence of a word in a document is independent of the presence or absence of any other word

$$\text{sim}(d_j, q) \approx \frac{P(d_j | R_q)}{P(d_j | \bar{R}_q)} = \frac{\left( \prod_{w_i \in d_j} P(w_i | R_q) \right) \left( \prod_{w_i \notin d_j} P(\bar{w}_i | R_q) \right)}{\left( \prod_{w_i \in d_j} P(w_i | \bar{R}_q) \right) \left( \prod_{w_i \notin d_j} P(\bar{w}_i | \bar{R}_q) \right)}$$

- $P(w_i | R_q)$  is the probability that the term  $w_i$  is present in a document randomly selected from  $R_q$
- $P(\bar{w}_i | R_q)$  is the probability that  $w_i$  is not present in a document randomly selected from the set  $R_q$
- probabilities with  $\bar{R}_q$ : analogous to the ones just described

$$\begin{aligned} P(w_i | R_q) + P(\bar{w}_i | R_q) &= 1 \\ P(w_i | \bar{R}_q) + P(\bar{w}_i | \bar{R}_q) &= 1 \end{aligned}$$

# Probabilistic Model – 3

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- Since we assume index terms follow the Bernoulli distributions

$$\begin{aligned}P(w_i|R_q) + P(\bar{w}_i|R_q) &= 1 \\P(w_i|\bar{R}_q) + P(\bar{w}_i|\bar{R}_q) &= 1\end{aligned}$$

- The probabilistic model can be translated to:

$$\begin{aligned}sim(d_j, q) &\approx \frac{\left(\prod_{w_i \in d_j} P(w_i|R_q)\right) \left(\prod_{w_i \notin d_j} P(\bar{w}_i|R_q)\right)}{\left(\prod_{w_i \in d_j} P(w_i|\bar{R}_q)\right) \left(\prod_{w_i \notin d_j} P(\bar{w}_i|\bar{R}_q)\right)} \\&= \frac{\left(\prod_{w_i \in d_j} P(w_i|R_q)\right) \left(\prod_{w_i \notin d_j} (1 - P(w_i|R_q))\right)}{\left(\prod_{w_i \in d_j} P(w_i|\bar{R}_q)\right) \left(\prod_{w_i \notin d_j} (1 - P(w_i|\bar{R}_q))\right)}\end{aligned}$$



# Probabilistic Model – 4

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- Then, we take logarithms:

$$\begin{aligned} \text{sim}(d_j, q) &\approx \frac{\left(\prod_{w_i \in d_j} P(w_i | R_q)\right) \left(\prod_{w_i \notin d_j} (1 - P(w_i | R_q))\right)}{\left(\prod_{w_i \in d_j} P(w_i | \bar{R}_q)\right) \left(\prod_{w_i \notin d_j} (1 - P(w_i | \bar{R}_q))\right)} \\ &\propto \log \prod_{w_i \in d_j} P(w_i | R_q) + \log \prod_{w_i \notin d_j} (1 - P(w_i | R_q)) \\ &\quad - \log \prod_{w_i \in d_j} P(w_i | \bar{R}_q) - \log \prod_{w_i \notin d_j} (1 - P(w_i | \bar{R}_q)) \end{aligned}$$

# Probabilistic Model – 5

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- By using a trick

$$\begin{aligned} & \text{sim}(d_j, q) \\ & \propto \log \prod_{w_i \in d_j} P(w_i | R_q) + \log \prod_{w_i \notin d_j} (1 - P(w_i | R_q)) \\ & + \log \prod_{w_i \in d_j} (1 - P(w_i | R_q)) - \log \prod_{w_i \in d_j} (1 - P(w_i | R_q)) \\ & - \log \prod_{w_i \in d_j} P(w_i | \bar{R}_q) - \log \prod_{w_i \notin d_j} (1 - P(w_i | \bar{R}_q)) \\ & + \log \prod_{w_i \in d_j} (1 - P(w_i | \bar{R}_q)) - \log \prod_{w_i \in d_j} (1 - P(w_i | \bar{R}_q)) \end{aligned}$$

# Probabilistic Model – 6

- Consequently, we can obtain

$$\begin{aligned} \text{sim}(d_j, q) &\propto \log \prod_{w_i \in d_j} P(w_i | R_q) + \log \prod_{w_i \notin d_j} (1 - P(w_i | R_q)) + \log \prod_{w_i \in d_j} (1 - P(w_i | \bar{R}_q)) - \log \prod_{w_i \in d_j} (1 - P(w_i | R_q)) \\ &\quad - \log \prod_{w_i \in d_j} P(w_i | \bar{R}_q) - \log \prod_{w_i \notin d_j} (1 - P(w_i | \bar{R}_q)) + \log \prod_{w_i \in d_j} (1 - P(w_i | \bar{R}_q)) - \log \prod_{w_i \in d_j} (1 - P(w_i | \bar{R}_q)) \\ &= \log \prod_{w_i \in d_j} \frac{P(w_i | R_q)}{1 - P(w_i | R_q)} + \log \prod_{w_i} (1 - P(w_i | R_q)) + \log \prod_{w_i \in d_j} \frac{1 - P(w_i | \bar{R}_q)}{P(w_i | \bar{R}_q)} - \log \prod_{w_i} (1 - P(w_i | \bar{R}_q)) \end{aligned}$$

Constant for the given query  $q$   
and document  $d_j$

# Probabilistic Model – 7

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- So, we have

$$\text{sim}(d_j, q) \propto \log \prod_{w_i \in d_j} \frac{P(w_i | R_q)}{1 - P(w_i | R_q)} + \log \prod_{w_i \in d_j} \frac{1 - P(w_i | \bar{R}_q)}{P(w_i | \bar{R}_q)}$$

- Further, let's make an additional simplifying assumption that we **only consider terms that occurring in the query**
  - This is a key expression for ranking computation in the probabilistic model

$$\text{sim}(d_j, q) \propto \sum_{w_i \in d_j \& w_i \in q} \log \frac{P(w_i | R_q)}{1 - P(w_i | R_q)} + \log \frac{1 - P(w_i | \bar{R}_q)}{P(w_i | \bar{R}_q)}$$

# How to Estimate? – 1

- For a given query, if we have
  - $N$  be the number of documents in the collection
  - $n_i$  be the number of documents that contain term  $w_i$
  - $R_q$  be the total number of relevant documents to query  $q$
  - $r_i$  be the number of relevant documents that contain term  $w_i$

	Relevant	Non-relevant	All Documents
Documents that contain $w_i$	$r_i$	$n_i - r_i$	$n_i$
Documents that do not contain $w_i$	$R_q - r_i$	$N - n_i - (R_q - r_i)$	$N - n_i$
All documents	$R_q$	$N - R_q$	$N$

# How to Estimate? – 2

- The probabilities can be estimated by:

$$P(w_i|R_q) = \frac{r_i}{R_q}$$

$$P(w_i|\bar{R}_q) = \frac{n_i - r_i}{N - R_q}$$

	Relevant	Non-relevant	All Documents
Documents that contain $w_i$	$r_i$	$n_i - r_i$	$n_i$
Documents that do not contain $w_i$	$R_q - r_i$	$N - n_i - (R_q - r_i)$	$N - n_i$
All documents	$R_q$	$N - R_q$	$N$

- Then, the equation for ranking computation in the probabilistic model could be rewritten as

$$\begin{aligned}
 \text{sim}(d_j, q) &\propto \sum_{w_i \in d_j \& w_i \in q} \log \frac{P(w_i|R_q)}{1 - P(w_i|R_q)} + \log \frac{1 - P(w_i|\bar{R}_q)}{P(w_i|\bar{R}_q)} \\
 &= \sum_{w_i \in d_j \& w_i \in q} \log \frac{\frac{r_i}{R_q}}{1 - \frac{r_i}{R_q}} + \log \frac{1 - \frac{n_i - r_i}{N - R_q}}{\frac{n_i - r_i}{N - R_q}} \\
 &= \sum_{w_i \in d_j \& w_i \in q} \log \left( \frac{r_i}{R_q - r_i} \cdot \frac{N - R_q - n_i + r_i}{n_i - r_i} \right)
 \end{aligned}$$

# In Practice – 1

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- For handling small values of  $r_i$ , we add 0.5 to each of the terms in the formula

$$\text{sim}(d_j, q) \propto \sum_{w_i \in d_j \& w_i \in q} \log \left( \frac{r_i + 0.5}{R_q - r_i + 0.5} \cdot \frac{N - R_q - n_i + r_i + 0.5}{n_i - r_i + 0.5} \right)$$

Robertson-Sparck Jones Equation

## In Practice – 2

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- In real case, it is hard to obtain the statistics of  $R_q$  and  $r_i$ 
  - Ground truth?
  - A simplest way is to assume they are zero!

$$\text{sim}(d_j, q)$$

$$\propto \sum_{w_i \in d_j \& w_i \in q} \log \left( \frac{r_i + 0.5}{R_q - r_i + 0.5} \cdot \frac{N - R_q - n_i + r_i + 0.5}{n_i - r_i + 0.5} \right)$$

$$\approx \sum_{w_i \in d_j \& w_i \in q} \log \left( \frac{N - n_i + 0.5}{n_i + 0.5} \right)$$



# Pros and Cons

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- Advantages:
  - Docs ranked in decreasing order of probability of relevance
- Disadvantages:
  - need to estimate  $P(w_i|R_q)$
  - method does not take “frequency” into account
  - the lack of document length normalization
    - The longer the document, the larger the score?

# Overlap Score Model

# Term Weighting – 1

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- The terms of a document are not equally useful for describing the document contents
  - There are index terms which are **vaguer**
- There are (occurrence) properties of an index term which are useful for evaluating the importance of the term in a document
  - For instance, a word which appears in all documents of a collection is completely useless for retrieval tasks
  - However, deciding on the importance of a term for summarizing the contents of a document is not a trivial issue

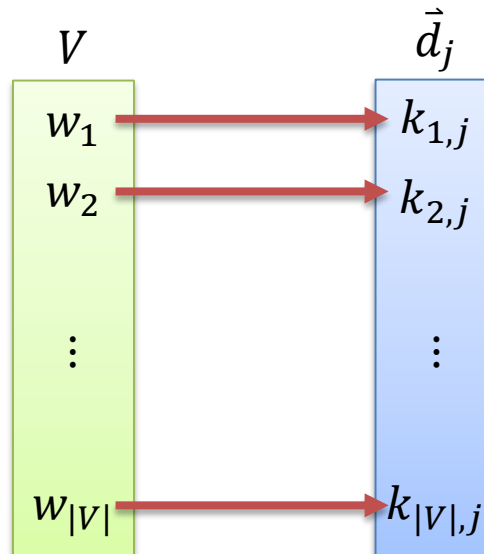
# Term Weighting – 2

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- To characterize term importance, we associate a weight  $k_{i,j} > 0$  with each term  $w_i$  that occurs in the document  $d_j$ 
  - If  $w_i$  that does not appear in the document  $d_j$ , then  $k_{i,j} = 0$
- The weight  $k_{i,j}$  **quantifies the importance** of the index term  $w_i$  for describing the contents of document  $d_j$
- These weights are useful to **compute a rank** for each document in the collection with regard to a given query

# Formal Expression

- $w_i$  be an index term and  $d_j$  be a document
- $V = \{w_1, \dots, w_{|V|}\}$  be the set of all index terms
- $k_{i,j} > 0$  be the weight associated with  $w_i$  and  $d_j$
- We can define a  $|V|$ -dimensional weighted vector  $\vec{d}_j$  that contains the weight of each index term  $w_i \in V$  in the document  $d_j$



# Term Frequency – 1

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- The value of  $k_{i,j}$  is proportional to the term frequency
  - **Luhn Assumption**
  - The weights  $k_{i,j}$  can be computed using the **frequencies of occurrence** of the term within the document

$$k_{i,j} = tf_{i,j}$$

- This is based on the observation that high frequency terms are important for describing documents
  - The more often a term occurs in the text of the document, the higher its weight

# Term Frequency – 2

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- Several variants of  $tf$  weight have been proposed

Binary	$\{0, 1\}$
Raw Frequency	$tf_{i,j}$
Log Normalization	$1 + \log_2(tf_{i,j})$
Double Normalization 0.5	$0.5 + 0.5 \frac{tf_{i,j}}{\max_j tf_{i,j}}$
Double Normalization $\sigma$	$\sigma + (1 - \sigma) \frac{tf_{i,j}}{\max_j tf_{i,j}}$

# Term Frequency – 3

- Take “Log Normalization” for example

$$\bar{tf}_{i,j} = \begin{cases} 1 + \log_2(tf_{i,j}) & \text{if } tf_{i,j} > 0 \\ 0 & \text{otherwise} \end{cases}$$

To do is to be.  
To be is to do.

$d_1$

To be or not to be.  
I am what I am.

$d_2$

I think therefore I am.  
Do be do be do.

$d_3$

Do do do, da da da.  
Let it be, let it be.

$d_4$

Vocabulary		$tf_{i,1}$	$tf_{i,2}$	$tf_{i,3}$	$tf_{i,4}$
1	to	3	2	-	-
2	do	2	-	2.585	2.585
3	is	2	-	-	-
4	be	2	2	2	2
5	or	-	1	-	-
6	not	-	1	-	-
7	I	-	2	2	-
8	am	-	2	1	-
9	what	-	1	-	-
10	think	-	-	1	-
11	therefore	-	-	1	-
12	da	-	-	-	2.585
13	let	-	-	-	2
14	it	-	-	-	2



# Inverse Document Frequency – 1

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- Raw term frequency as above suffers from a critical problem
  - All terms are considered equally important when it comes to assessing relevancy on a query
  - In fact certain terms have little or no discriminating power in determining relevance
- An immediate idea is to scale down the term weights by leveraging the document frequency of each term
  - Document Frequency  $df_i$ : the number of documents in the collection that contain the term  $w_i$

# Inverse Document Frequency – 2

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- Denoting as usual the total number of documents in a collection by  $N$ , we define the *inverse document frequency* of a term  $w_i$  as follows

$$idf_i = \log \frac{N}{df_i}$$

- The *idf* of a rare term is high, whereas the *idf* of a frequent term is likely to be low
- *idf* is used to reveal the **term specificity**

# Inverse Document Frequency – 3

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- Five distinct variants of *idf* weight

Unary	1
Inverse Frequency	$\log \frac{N}{n_i}$
Inverse Frequency Smooth	$\log \left( 1 + \frac{N}{n_i} \right)$
Inverse Frequency Max	$\log \left( 1 + \frac{\max_i(n_i)}{n_i} \right)$
Probabilistic Inverse Frequency	$\log \frac{N - n_i}{n_i}$

# TF-IDF

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- We now combine the definitions of term frequency and inverse document frequency, to produce a composite weight for each term in each document

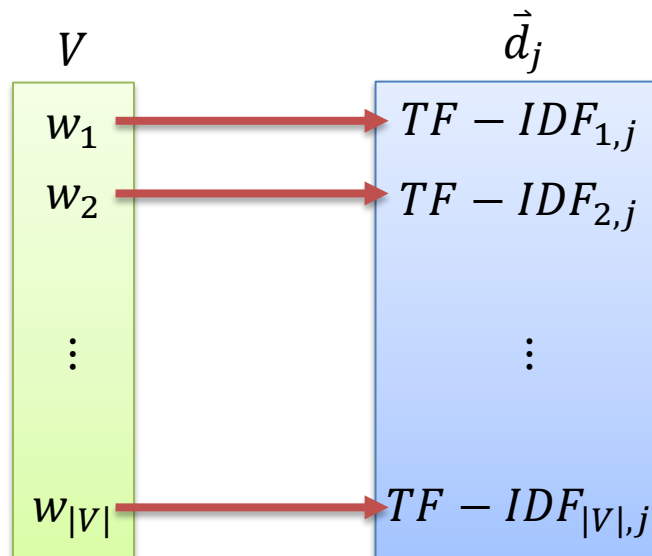
$$TF - IDF_{i,j} = tf_{i,j} \times idf_i$$

- $TF - IDF_{i,j}$  assigns to term  $w_i$  a weight in document  $d_j$ 
  - $TF - IDF_{i,j}$  will be higher when  $w_i$  occurs many times within a small number of documents
  - It will be lower when the term occurs fewer times in a document, or occurs in many documents
  - It will be the lowest when the term occurs in virtually all documents ( $idf_i = 0$ )

# Overlap Score Model – 1

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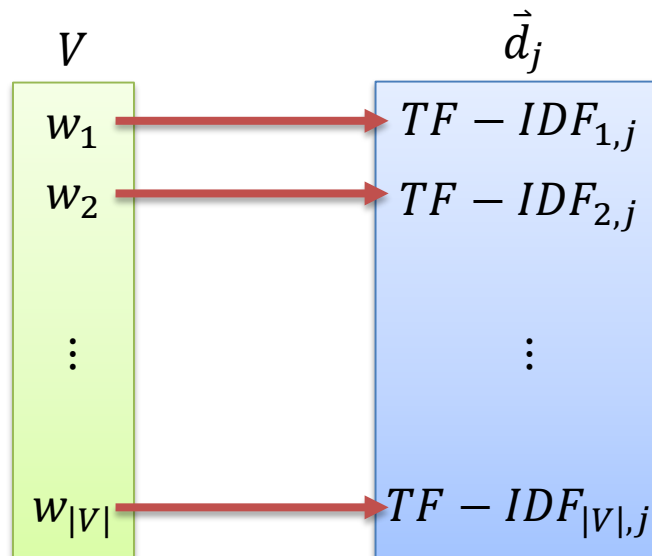
- At this point, we may view each document as a vector with one component corresponding to each term in the dictionary
  - The weight for each component is determined by its  $TF - IDF_{i,j}$
  - For dictionary terms that do not occur in the document, this weight is zero



# Overlap Score Model – 2

- The score of a document  $d_j$  is the sum, over all query terms, of the  $TF - IDF_{i,j}$  weight of the query terms occurs in  $d_j$

$$sim(q, d_j) = \sum_{w_i \in q} TF - IDF_{i,j}$$



# **Vector Space Model**

# The Vector Space Model – 1

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- Opposite to the overlap score model, we now present queries as vectors in the same vector space as the document collection
  - In other word, documents and queries are all vectors, and the weight for each component is determined by its *TF – IDF*
- The relevance degree between a given query and a document can be computed by referring to the cosine similarity measure

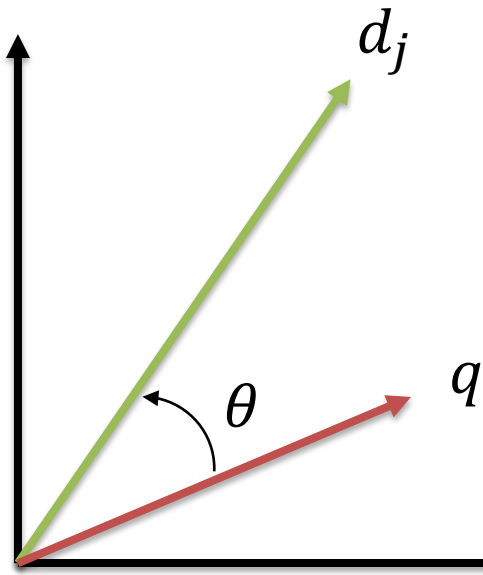
$$sim(q, d_j) = \frac{\vec{q} \cdot \vec{d_j}}{|\vec{q}| |\vec{d_j}|}$$



# The Vector Space Model – 2

- Similarity between a document  $d_j$  and a query  $q$ 
  - Since  $w_{i,q} > 0$  and  $w_{i,j} > 0$ , we have  $0 \leq \text{sim}(q, d_j) \leq 1$

$$\text{sim}(q, d_j) = \cos(\theta) = \frac{\vec{q} \cdot \vec{d_j}}{|\vec{q}| |\vec{d_j}|} = \frac{\sum_{w_i \in V} w_{i,q} \times w_{i,j}}{\sqrt{\sum_{w_i \in V} w_{i,q}^2} \times \sqrt{\sum_{w_i \in V} w_{i,j}^2}}$$



Why cosine similarity measure?  
Why not Euclidean distance?

# The Vector Space Model – 2

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- Recommended TF-IDF weighting schemes

Scheme	Document Term Weight	Query Term Weight
1	$tf_{i,j} \times \log \frac{N}{n_i}$	$\left(0.5 + 0.5 \frac{tf_{i,q}}{\max_i(tf_{i,q})}\right) \times \log \frac{N}{n_i}$
2	$1 + tf_{i,j}$	$\log \left(1 + \frac{N}{n_i}\right)$
3	$(1 + tf_{i,j}) \times \log \frac{N}{n_i}$	$(1 + tf_{i,q}) \times \log \frac{N}{n_i}$

# Pros & Cons

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- Advantages
  - Term-weighting improves quality of the answer set
  - Partial matching is somewhat allowed
  - Cosine ranking formula sorts documents according to a degree of similarity to the query
  - Document length normalization is naturally built-in into the ranking
- Disadvantages
  - It assumes independence of index terms

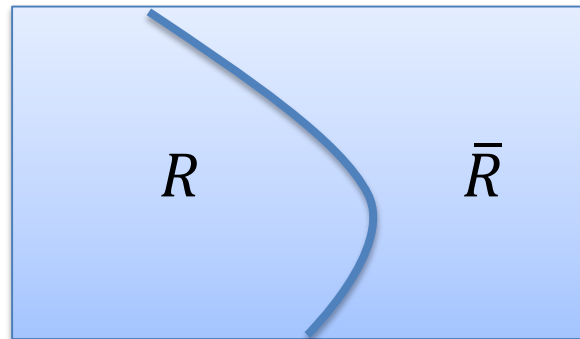
# **Discussion & Comparison**

# TF vs. IDF

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- The role of index terms

IR as a binary clustering  
Relevance vs. Non-relevance



- Which index terms (features) better describe the relevant class
  - Intra-cluster similarity (TF-factor)
  - Inter-cluster dissimilarity (IDF-factor)

# Comparisons

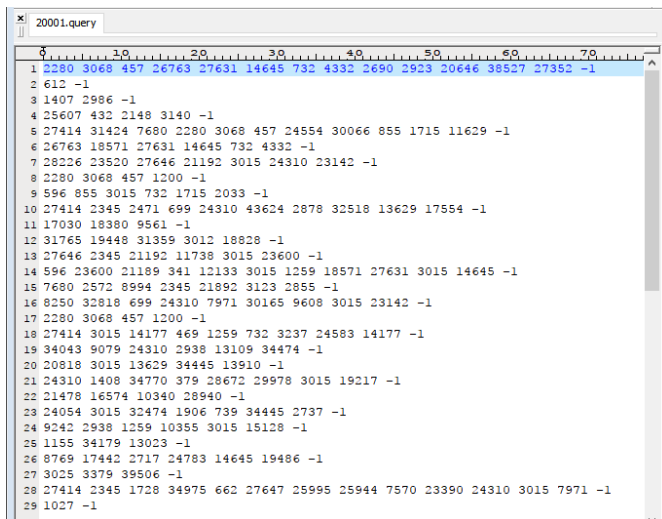
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- Boolean model does not provide for partial matches and is considered to be the weakest classic model
- There is some controversy as to whether the **probabilistic model outperforms the vector model**
  - Croft suggested that the probabilistic model provides a better retrieval performance
- However, Salton ~~XXXX~~ showed that the **vector model outperforms probabilistic model** with general collections

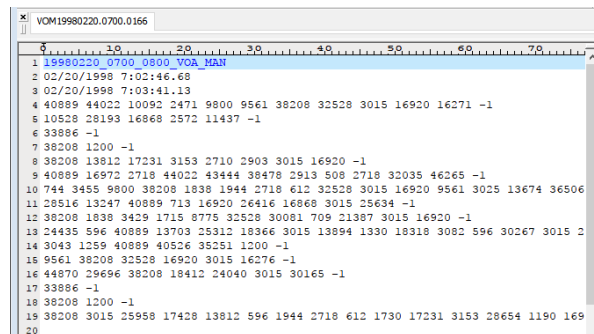
# **Homework 1 – Retrieval Model**

# Homework 1

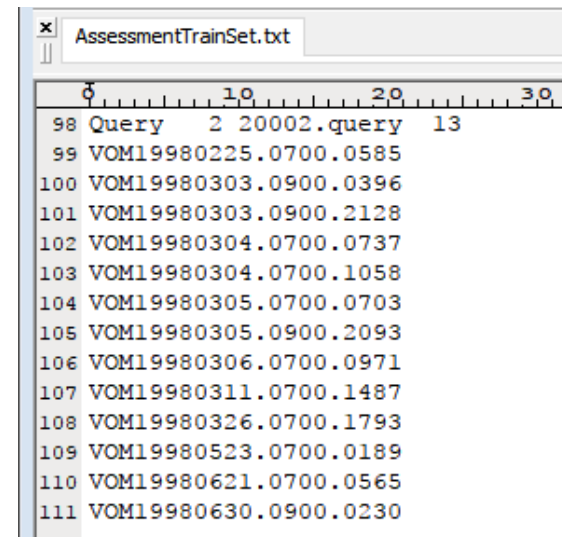
- In this project, you will have a set of queries (16 queries) and a collection of documents (2265 documents)
  - Each words/terms is represented as a number except that the number “-1” is a delimiter
- Our goal is to implement a vector space model, and print out the ranking results for all of the queries



```
20001.query
1 2280 3068 457 26763 27631 14645 732 4332 2690 2923 20646 38527 27352 -1
2 612 -1
3 1407 2986 -1
4 25607 432 2148 3140 -1
5 27414 31424 7680 2280 3068 457 24554 30066 855 1715 11629 -1
6 26763 18571 27631 14645 732 4332 -1
7 28226 23520 27646 21192 3015 24310 23142 -1
8 2280 3068 457 1200 -1
9 596 855 3015 732 1715 2033 -1
10 27414 2345 2471 699 24310 43624 2878 32518 13629 17554 -1
11 17030 18380 9561 -1
12 31765 19448 31359 3012 18928 -1
13 27646 2345 21192 11738 3015 23600 -1
14 596 23600 21189 341 12133 3015 1259 18571 27631 3015 14645 -1
15 7680 2572 8994 2345 21892 3123 2855 -1
16 8250 32818 699 24310 7971 30165 9608 3015 23142 -1
17 2280 3068 457 1200 -1
18 27414 3015 14177 469 1259 732 3237 24583 14177 -1
19 34043 9079 24310 2938 13109 34474 -1
20 20818 3015 13629 34445 13910 -1
21 24310 1408 34770 379 28672 29978 3015 19217 -1
22 21478 16574 10340 28940 -1
23 24054 3015 32474 1906 739 34445 2737 -1
24 9242 2938 1259 10355 3015 15128 -1
25 1155 34179 13023 -1
26 8769 17442 2717 24783 14645 19486 -1
27 3025 3379 39506 -1
28 27414 2345 1728 34975 662 27647 25995 25944 7570 23390 24310 3015 7971 -1
29 1027 -1
```



```
VOM19980220.0700.0166
1 19980220.0700.0800_VOM_MAN
2 02/20/1998 7:02:46.66
3 02/20/1998 7:03:41.13
4 40889 44022 10092 2471 9800 9561 38208 32528 3015 16920 16271 -1
5 10528 28193 16968 2572 11437 -1
6 33886 -1
7 38208 1200 -1
8 38208 13812 17231 3153 2710 2903 3015 16920 -1
9 40889 16972 2718 44022 43444 38478 2913 508 2718 32035 46265 -1
10 744 3455 9800 38208 1838 1944 2718 612 32528 3015 16920 9561 3025 13674 36506
11 28516 13247 40889 713 16920 26416 16868 3015 25634 -1
12 38208 1838 3429 1715 8775 32528 30081 709 21387 3015 16920 -1
13 24435 596 40889 13703 25312 18366 3015 13894 1330 18318 3082 596 30267 3015 2
14 3043 1259 40889 40526 35251 1200 -1
15 9561 38208 32528 16920 3015 16276 -1
16 44870 29696 38208 18412 24040 3015 30165 -1
17 33886 -1
18 38208 1200 -1
19 38208 3015 25958 17428 13812 596 1944 2718 612 1730 17231 3153 28654 1190 169
20
```



```
AssessmentTrainSet.txt
98 Query 2 20002.query 13
99 VOM19980225.0700.0585
100 VOM19980303.0900.0396
101 VOM19980303.0900.2128
102 VOM19980304.0700.0737
103 VOM19980304.0700.1058
104 VOM19980305.0700.0703
105 VOM19980305.0900.2093
106 VOM19980306.0700.0971
107 VOM19980311.0700.1487
108 VOM19980326.0700.1793
109 VOM19980523.0700.0189
110 VOM19980621.0700.0565
111 VOM19980630.0900.0230
```



# Questions?

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