

# CONTENT-BASED IMAGE RETRIEVAL

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Multimedia Databases SS 23 (Exercises)

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# Task 1: CBR

## ➤ What is CBR?

- A content-based retrieval system processes the information contained in data and creates an abstraction of its content in terms of attributes.
- **E.g.:** Online clothes shopping might allow users to search by traditional categories (brand, price range) and also in terms of visual attributes (color, texture)
- Steps:
  - Feature Extraction: The first step in the process is extracting image features to a distinguishable extent.
  - Matching: The second step involves matching these features to yield a result that is visually similar.



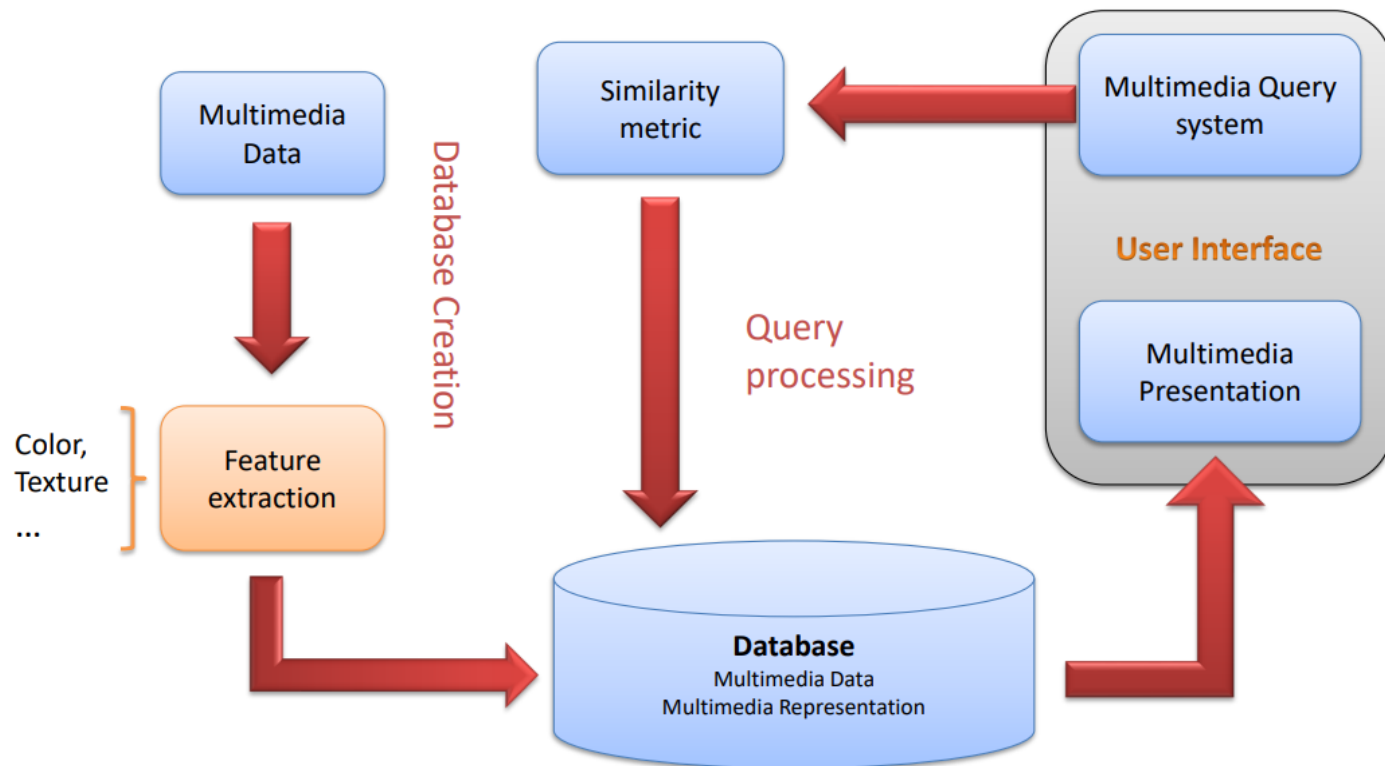
# CBR

- **Compared to each other, what are the benefits and limitations of ABIR and CBIR?**
- ❑ **Limitations of ABIR compared to CBIR**
  - Problem of Image annotations [Brahmi et al. 2004]
    - Large volumes of DB: manual image annotation is time-consuming and therefore costly.
    - The annotation is language dependent.
  - Problem with human perception [Brahmi et al. 2004]
    - Human annotation is **subjective**
    - The accuracy and quality of the annotations are of the responsibility of the annotator and end-user.
  - Problem in annotating images with words [Sclaroff et al. 1999]
    - Some images could not be annotated as it is difficult to describe their content with words.
- ❑ **Limitations of CBIR compared to ABIR**
  - Problem of Semantic Gap [Inoue et al. 2004, Brahmi et al. 2004]
    - Visual features cannot fully represent concepts.
  - Problem of the availability of the image query [Inoue et al. 2004]
    - Users must have an example image in their hands

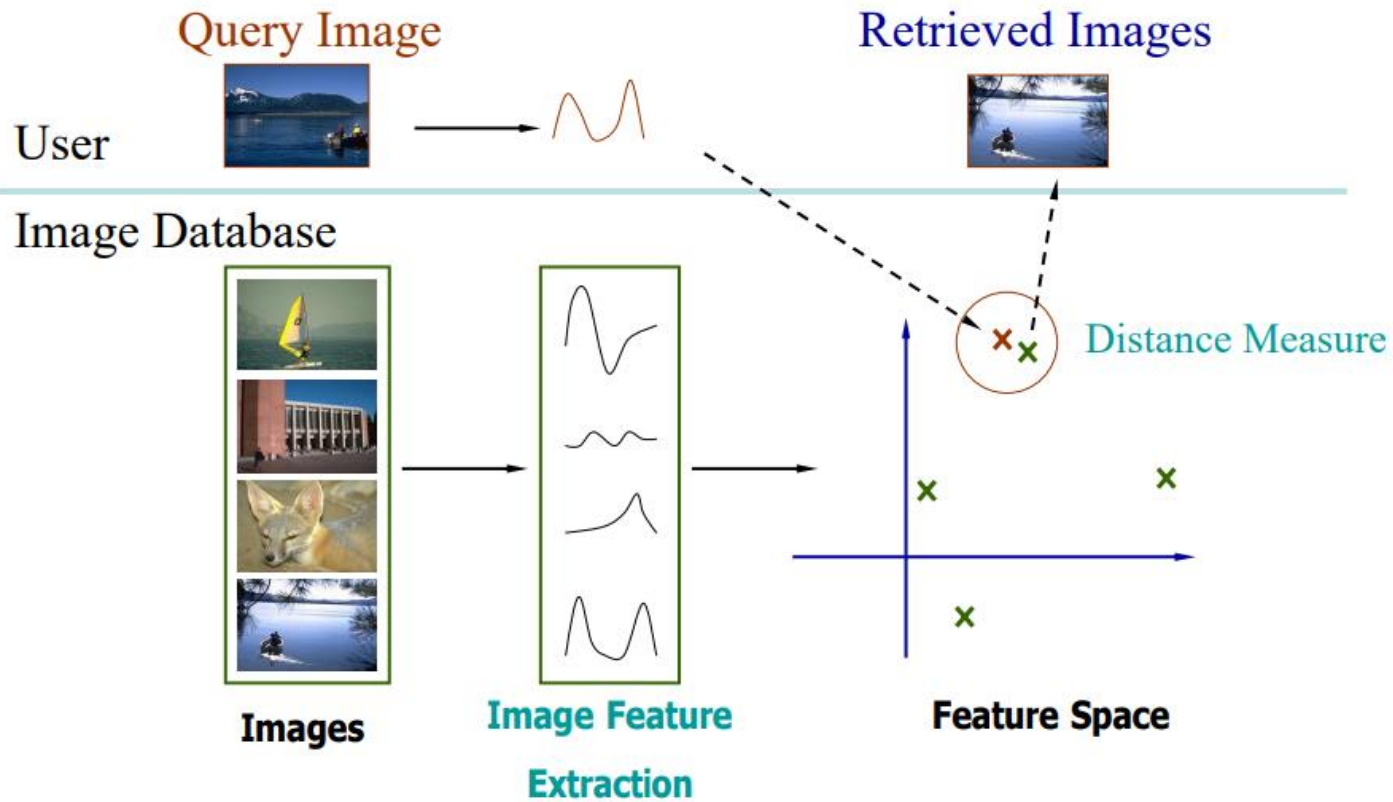


# Task 1: CBR

- What are the components of a CBIR architecture?  
Explain the basic principle of each component using an example?



# Task 1: CBR



# Task 1: CBR

## ➤ What is a feature vector?

- Numerical representation of object **features** in an n-dimensional **vector**
- E.g. feature = avg color, fv = (255,0,0)

## ➤ Which problem arise when indexing features vector?

- ‘The query performance of access methods decreases , if the dimensionality of the underlying data set becomes high.’  
by Berchtold et al.
- A large number of features diminishes the distinguishing power of each feature and the indexing structures.

## ➤ How to avoid the ‘Curse of Dimensionality’?

- Development of specific index structures that are specialized for high-dimensional data
- Reduction of the vector dimension:
  - Feature selection
  - Feature extraction



# Task 2: CBR Definitions

## 1. Dominant Color

- The Dominant Color Descriptor allows specification of a small number of dominant color values + statistical properties like distribution and variance.
- In contrast to histogram color, only the representative colors are selected from each region or image.
- Its purpose is to provide an effective, compact and intuitive representation of colors present in a region or image.

# Task 2: CBR Definitions

- **Dominant Color**

- The dominant color descriptor is defined by :

$$F = \{(c_i, p_i, v_i), s\}, (i = 1 \dots N)$$

- N is the total number of color clusters (= bins in the histogram) in the image region, such that  $1 \leq N \leq 8$
- $c_i$  is the dominant color vector (3d RGB vector),
- $p_i$  is the percentage for each dominant color, such that
  - $P_i \in [0,1]$  and their sum is equal to 1,
- $v_i$  is its color variance,
- s is a scalar that represents the overall spatial coherency of the dominant colors in the image.



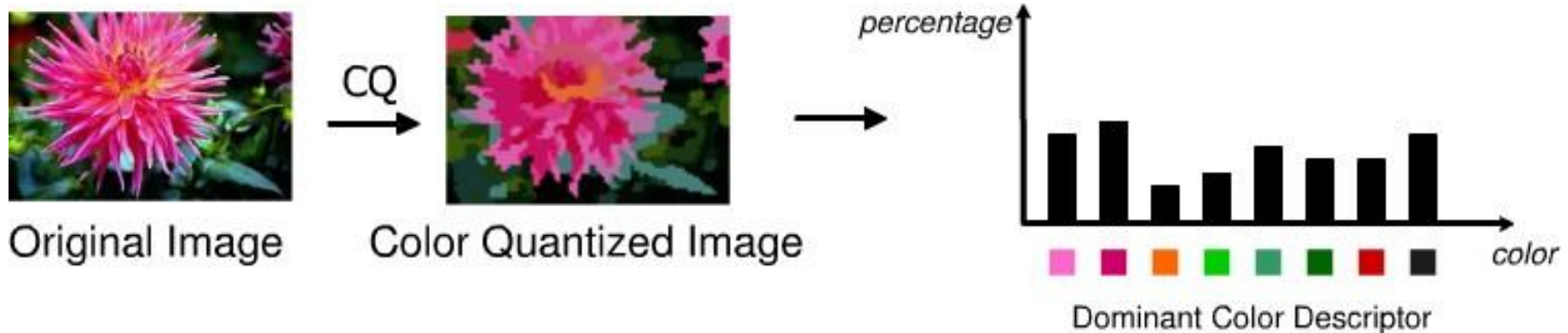


# Task 2: CBR Definitions

- **Dominant Color**

- Often, the color variance  $v$  and spatial coherency  $s$  are not considered, which simplifies the definition of the dominant color descriptor to:

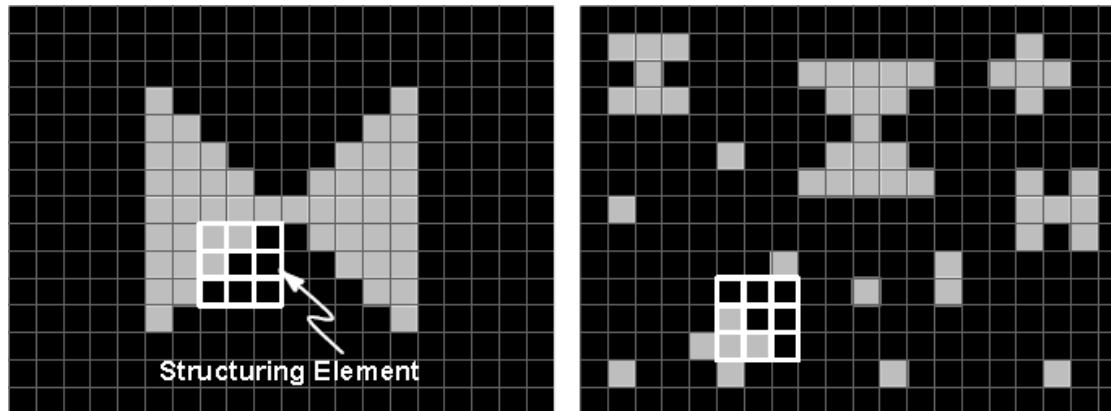
$$F = \{(c_i, p_i)\}, (i = 1...N)$$



# Task 2: CBR Definitions

## 2. Spatial Coherency

- The spatial coherency of a given dominant color is measured with **the normalized average number of connected pixels of this color**. It is computed using a 3x3 mask
- The overall spatial coherency is a linear combination of the individual spatial coherencies weighted with the corresponding percentages  $p_i$ .



**Note:** these two images have the same colors but the distribution of the colors is not the same.



# Task 2: CBR Definitions

## 3. Distance metrics

- Degree of similarity between two points is measured by distance in data space. Several metrics have been established, i.e. euclidian distance.

## 4. Curse of Dimensionality

- CBR performs worse when dimensionality of the FVs increases.

## 5. Types of content-based queries

- **Point Query:** Retrieve all points with identical feature vector
- **Range Query:** Retrieve all points with a maximum distance from query point.
- **K-Nearest Neighbor Query:** Returns the k most similar results



# Task 3: CBIR System

- What are the necessary conditions that must be fulfilled in order to be able to issue the following query to a CBIR system:
  - *Give me all images which contain a red car!*
- What are the problems that can occur?

# Task 3: CBIR System

- **What are the necessary conditions that must be fulfilled in order to be able to issue the following query to a CBIR system:**
  - **Give me all images which contain a red car!**

To resolve this question using a "query by feature", we could:

1. Define the set of colors that correspond to the concept of "red"
2. Define a set of contours (shape descriptors), which correspond to the shape of a car.
3. Perform a query by features based on these two features.

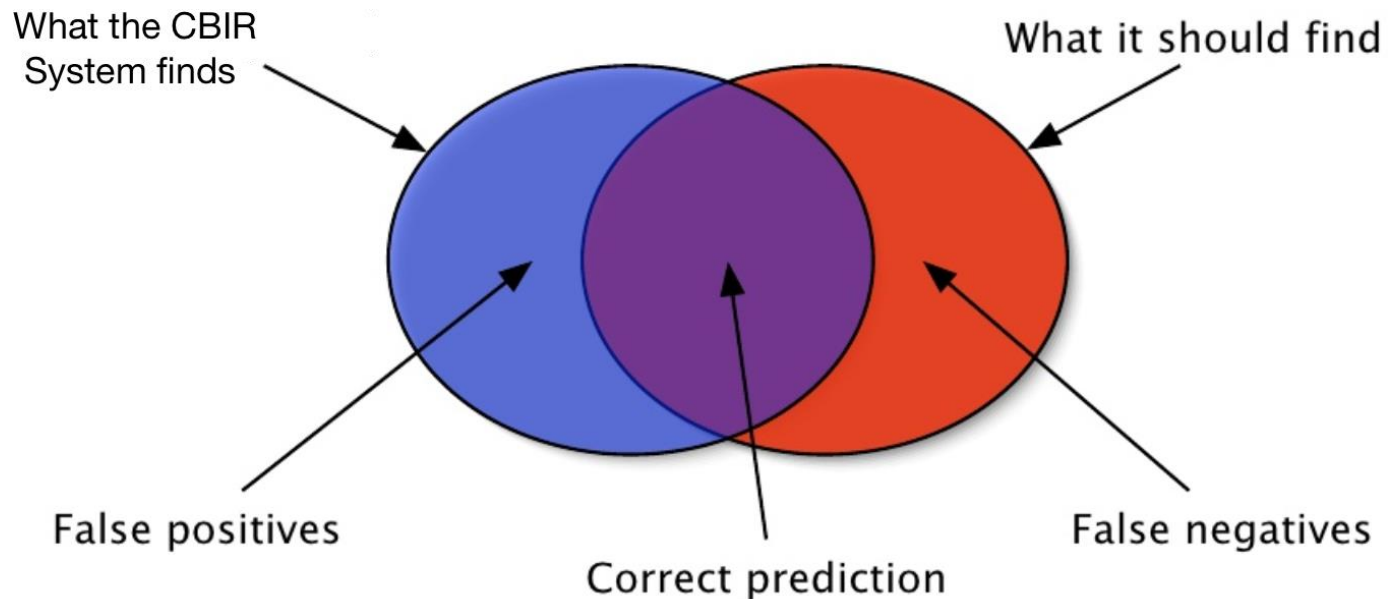
# Task 3: CBIR System

- **What are the problems that can occur?**
- In the QBF-solution, the difficulty lies in the definition of the shape, as cars can have very different contours (e.g. formula 1 cars, BMW cars, etc.).
- **To which extent the definition of the shape should be precise?**
  - precise definition will lead to a good precision but a bad recall.
  - less precise definition will provide bad precision (false positives) but a better recall.
- Thus, the appropriate strategy depends on the exact goals of the query.
  - **But, it is very difficult to get this information from the user.**



# Task 3: CBIR System

- How good is the result?



**Precision** How many of the returned entities are relevant?

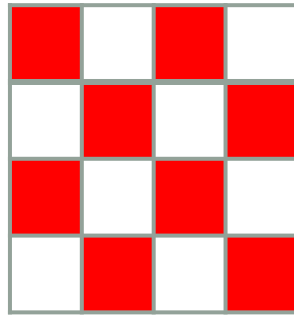
*High precision = few false positives*

**Recall** How many relevant entities are returned?

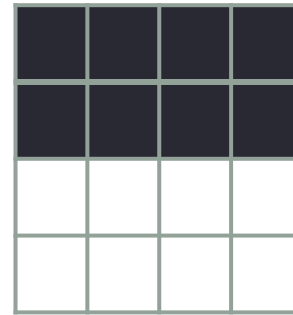
*High recall = few false negatives*

# Task 4: Image Indexing by Colours

- Apply a uniform colour quantization of 8 bins.
- Which quantization area (range) do the colours in the two images belong to?



**Image 1**

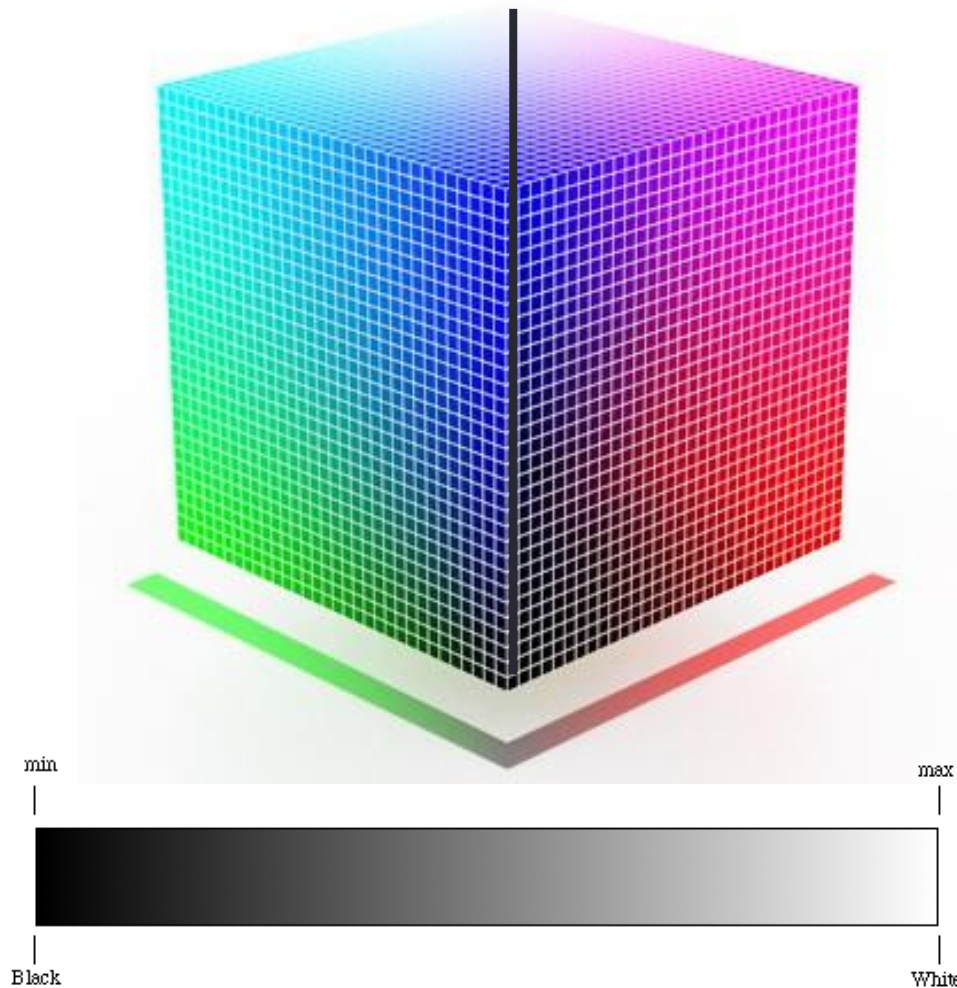
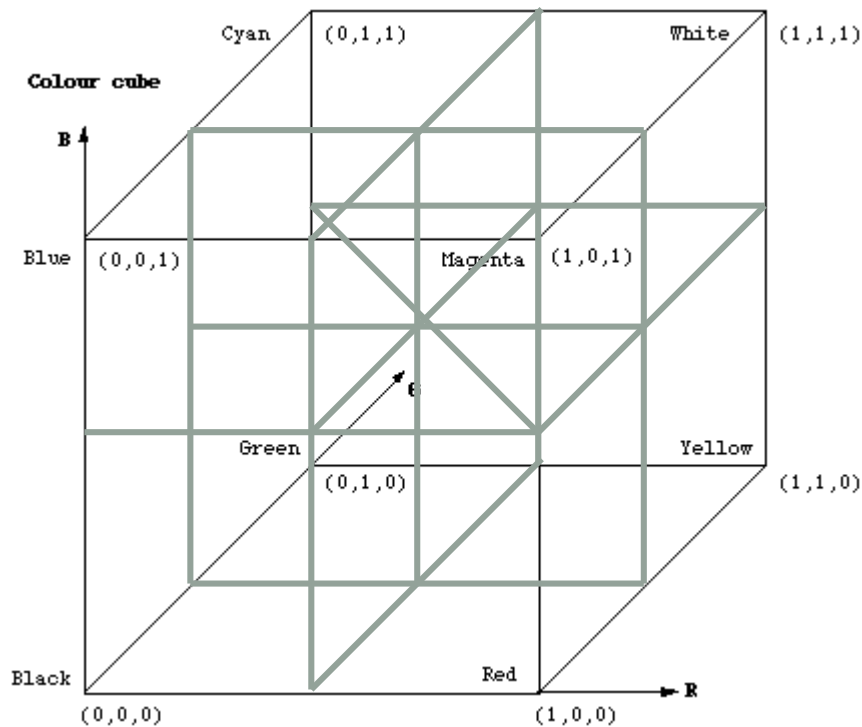


**Image 2**



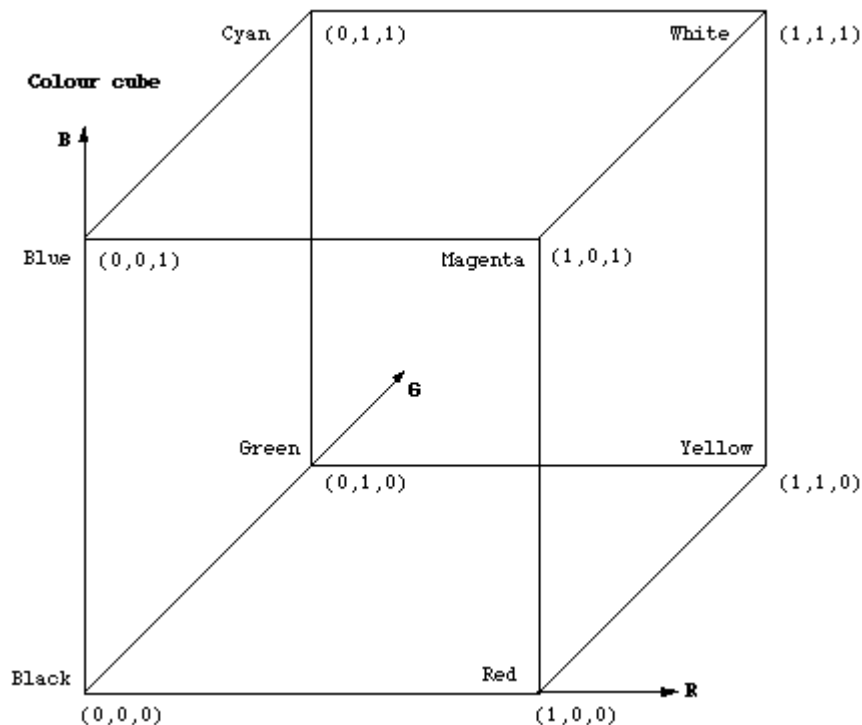
# Task 4: Image Indexing by Colours

- Apply a uniform colour quantization of 8 bins.



# Task 4: Image Indexing by Colours

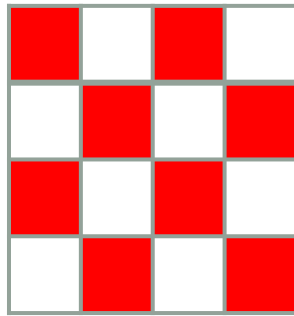
- Apply a uniform colour quantization of 8 bins.



- |           |           |
|-----------|-----------|
| ▪ (0,0,0) | ▪ (1,0,0) |
| ▪ (0,0,1) | ▪ (1,0,1) |
| ▪ (0,1,0) | ▪ (1,1,0) |
| ▪ (0,1,1) | ▪ (1,1,1) |

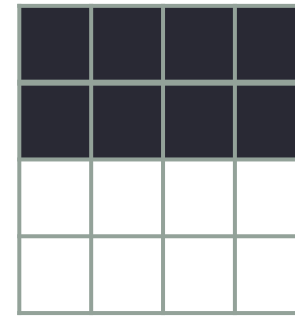
# Task 4: Image Indexing by Colours

- Which quantization area (range) do the colours in the two images belong to?



**Image 1**

- Red pixels are part of the (1,0,0) bin
- White pixels are part of the (1,1,1) bin

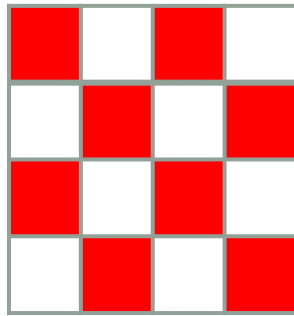


**Image 2**

- Black pixels are part of the (0,0,0) bin
- White pixels are part of the (1,1,1) bin

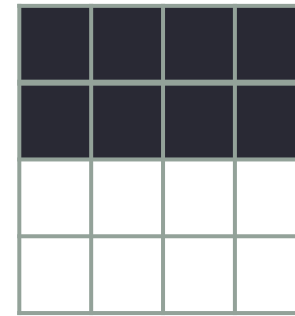
# Task 4: Image Indexing by Colours

- Create a color histogram for both images



**Image 1**

▪  $H_1 = (0,0,0,0,8,0,0,8)$

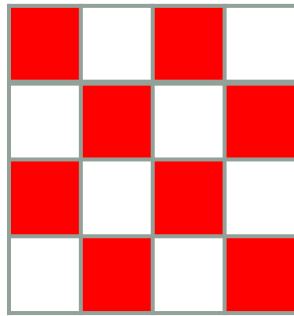


**Image 2**

▪  $H_2 = (8,0,0,0,0,0,0,8)$

# Task 4: Image Indexing by Colours

- Apply a uniform bin quantization for 2 bits.



**Image 1**

$$\blacksquare H_1 = (0,0,0,0,8,0,0,8)$$

$$\Rightarrow H_1 = (0,0,0,0,2,0,0,2)$$



**Image 2**

$$\blacksquare H_2 = (8,0,0,0,0,0,0,8)$$

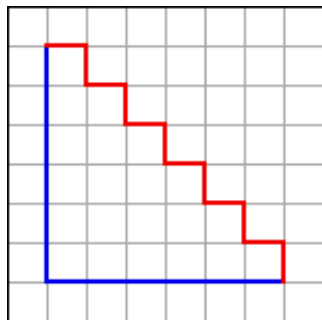
$$\Rightarrow H_2 = (2,0,0,0,0,0,0,2)$$

# Task 5: Similarity of images because of colour distribution

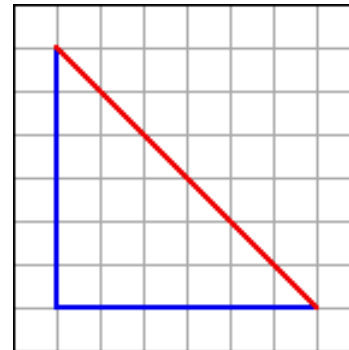
- **Minkowski Distances**

Use the two images of exercise 4 and the results of exercise 4.b (without bin quantification). Determine the similarity of the images with the help of Minkowski distances:

- $L_1$ : Manhattan distance
- $L_2$ : Euclidian distance
- $L_\infty$ : Maximal distance (also called Tschebyschow distance)



Manhattan Distance



Euclidean Distance

# Task 5: Similarity of images because of colour distribution

- **Minkowski Distances**

Starting with  $P = (x_1, x_2, \dots, x_n)$  and  $Q = (y_1, y_2, \dots, y_n) \in R^n$

$$L_p(P, Q) = \left( \sum_{i=1}^n |x_i - y_i|^p \right)^{1/p}$$

▪  $H_1 = (0, 0, 0, 0, 8, 0, 0, 8)$

▪  $H_2 = (8, 0, 0, 0, 0, 0, 0, 8)$

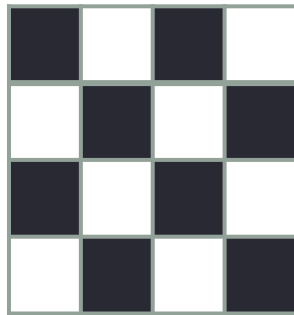
$$L_1(H_1, H_2) = |0-8| + |0-0| + |0-0| + |0-0| + |8-0| + |0-0| + |0-0| + |8-8| = 8+8 = 16$$

$$L_2(H_1, H_2) = \sqrt{(0-8)^2 + \dots + (8-0)^2 + \dots + (8-8)^2} = \sqrt{128} \approx 11,3$$

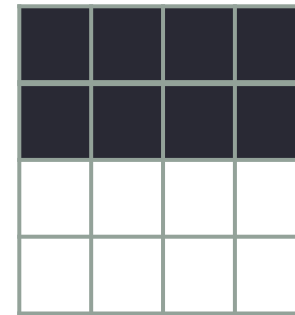
$$L_\infty(H_1, H_2) = \max_i |x_i - y_i| = 8$$

# Task 5: Similarity of images because of colour distribution

- Which result would you obtain if the red colour in the left image was black? Which conclusions do you draw?



**Image 1**



**Image 2**

Spatial Distribution of colors ignored!



# Task 5: Similarity of images because of colour distribution

- **Statistical Distances**

*Starting with the following colour distribution:  $H_1 = (4, 4, 4, 4)$  and  $H_2 = (8, 3, 4, 5)$*

*Non-parametrical distances:*

*Calculate the distances between  $H_1$  and  $H_2$  with the help of the following functions: Kolgomorov-Smirnov Distance, Chi-squared Distance.*

*Kolgomorov-Smirnov Distance:*

$$KS(P, Q) = \max_i |F^r(i; P) - F^r(i; Q)|$$

$F^r(i; P)$  is equivalent to *cumulative histogram* of P in place i.

- Cumulative  $H_1 = (4, 8, 12, 16)$  and Cumulative  $H_2 = (8, 11, 15, 20)$   
 $\Rightarrow KS(H_1, H_2) = 4$



# Task 5: Similarity of images because of colour distribution

- **Chi-squared Distance**

$$H_1 = (4, 4, 4, 4) \text{ and } H_2 = (8, 3, 4, 5)$$

$$D_{\chi}(P, Q) = \sum_i \frac{(x_i - f'(i))^2}{f'(i)}$$

$$f'(i) = \frac{x_i + y_i}{2}$$

$$f'(i_1) = 6, f'(i_2) = \frac{7}{2}, f'(i_3) = 4, f'(i_4) = \frac{9}{2}$$
$$D_{\chi}(H_1, H_2) = \frac{(4 - 6)^2}{6} + \frac{(4 - \frac{7}{2})^2}{\frac{7}{2}} + 0 + \frac{(4 - \frac{9}{2})^2}{\frac{9}{2}} = \frac{4}{6} + \frac{\frac{1}{4}}{\frac{7}{2}} + \frac{\frac{1}{4}}{\frac{9}{2}}$$

$$D_{\chi}(H_1, H_2) = \frac{2}{3} + \frac{1}{14} + \frac{1}{18} = \frac{50}{63}$$

$$D_{\chi}(H_1, H_2) \approx 0,794$$



# Task 5: Similarity of images because of colour distribution

- **Parametrical Distance Function**
- Calculate the distance between H1 and H2. Use Weighted-mean-variance and the following training data:
  - $V_1 (8,8,4,12)$ ,  $V_2 (4,0,0,16)$ ,  $V_3 (2,3,8,7)$ ,  $V_4 (4,4,6,10)$

*Weighted-mean-variance:*

$$WMV(P, Q) = \frac{|\mu(P) - \mu(Q)|}{|\sigma(\mu(Ref))|} + \frac{|\sigma(P) - \sigma(Q)|}{|\sigma(\sigma(Ref))|}$$

$\mu$ : Average

$\sigma$ : Standard deviation

$\mu(Ref)$ : Average calculated from training data

$\sigma(Ref)$ : Standard deviation calculated from training data



# Task 5: Similarity of images because of colour distribution

- **Parametrical Distance Function**

- $V_1 (8,8,4,12), V_2 (4,0,0,16), V_3 (2,3,8,7), V_4 (4,4,6,10)$

$$WMV(P, Q) = \frac{|\mu(P) - \mu(Q)|}{|\sigma(\mu(Ref))|} + \frac{|\sigma(P) - \sigma(Q)|}{|\sigma(\sigma(Ref))|}$$

- **How to calculate it?**

$$H_1 = (4, 4, 4, 4) \text{ and } H_2 = (8, 3, 4, 5)$$

- Numerator:
  - Mean values of  $\mu(H_1), \mu(H_2)$
  - Standard deviation:  $\sigma(H_1), \sigma(H_2)$

$$\sigma(P) = \sqrt{\frac{\sum_{i=1}^n (x_i - \mu(P))^2}{n}}$$



# Task 5: Similarity of images because of colour distribution

- **Parametrical Distance Function**

- $V_1 (8,8,4,12), V_2 (4,0,0,16), V_3 (2,3,8,7), V_4 (4,4,6,10)$
- $Ref = \{V_1, V_2, V_3, V_4\}$

$$WMV(P, Q) = \frac{|\mu(P) - \mu(Q)|}{|\sigma(\mu(Ref))|} + \frac{|\sigma(P) - \sigma(Q)|}{|\sigma(\sigma(Ref))|}$$

- **How to calculate it?**

- Denominator:  $\sigma(\mu(Ref)) \approx 1,224$ 
  - $\mu(Ref) = (\mu(V_{d1}), \mu(V_{d2}), \mu(V_{d3}), \mu(V_{d4}))$
  - $\sigma(Ref) = (\sigma(V_{d1}), \sigma(V_{d2}), \sigma(V_{d3}), \sigma(V_{d4}))$

$$\sigma(P) = \sqrt{\frac{\sum_{i=1}^n (x_i - \mu(P))^2}{n}}$$



# Task 5: Similarity of images because of colour distribution

- **Parametrical Distance Function**

- $V_1 (8,8,4,12), V_2 (4,0,0,16), V_3 (2,3,8,7), V_4 (4,4,6,10)$

$$WMV(P, Q) = \frac{|\mu(P) - \mu(Q)|}{|\sigma(\mu(Ref))|} + \frac{|\sigma(P) - \sigma(Q)|}{|\sigma(\sigma(Ref))|}$$

- **How to calculate it?**

- Denominator:  $\sigma(\sigma(Ref)) \approx 1,716$ 
  - Mean value of  $\mu(\sigma(Ref))$

$$\sigma(P) = \sqrt{\frac{\sum_{i=1}^n (x_i - \mu(P))^2}{n}}$$

- **Result:**  $WMV(H_1, H_2) \approx 1,907$

