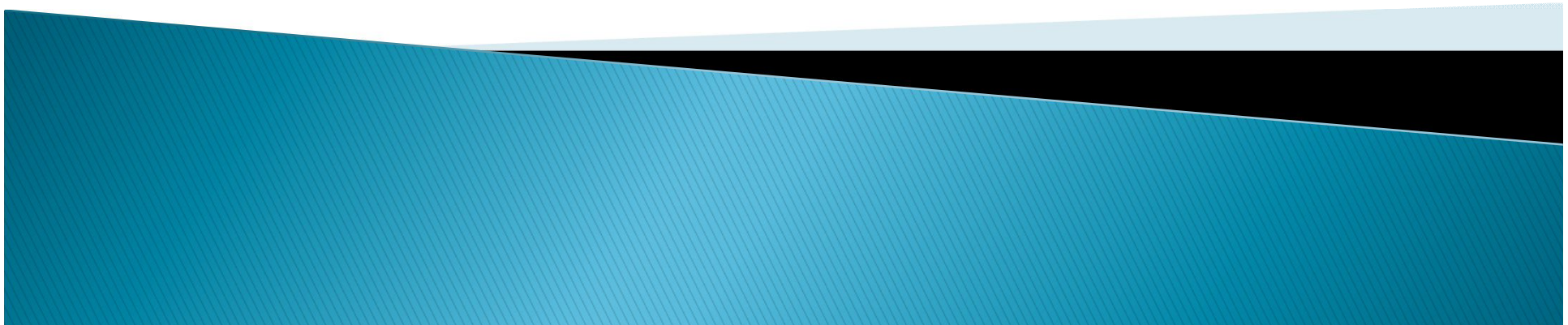


# Multimedia Databases

## The Image Medium

Prof. Dr. Michael Granitzer  
Prof. Dr. Harald Kosch

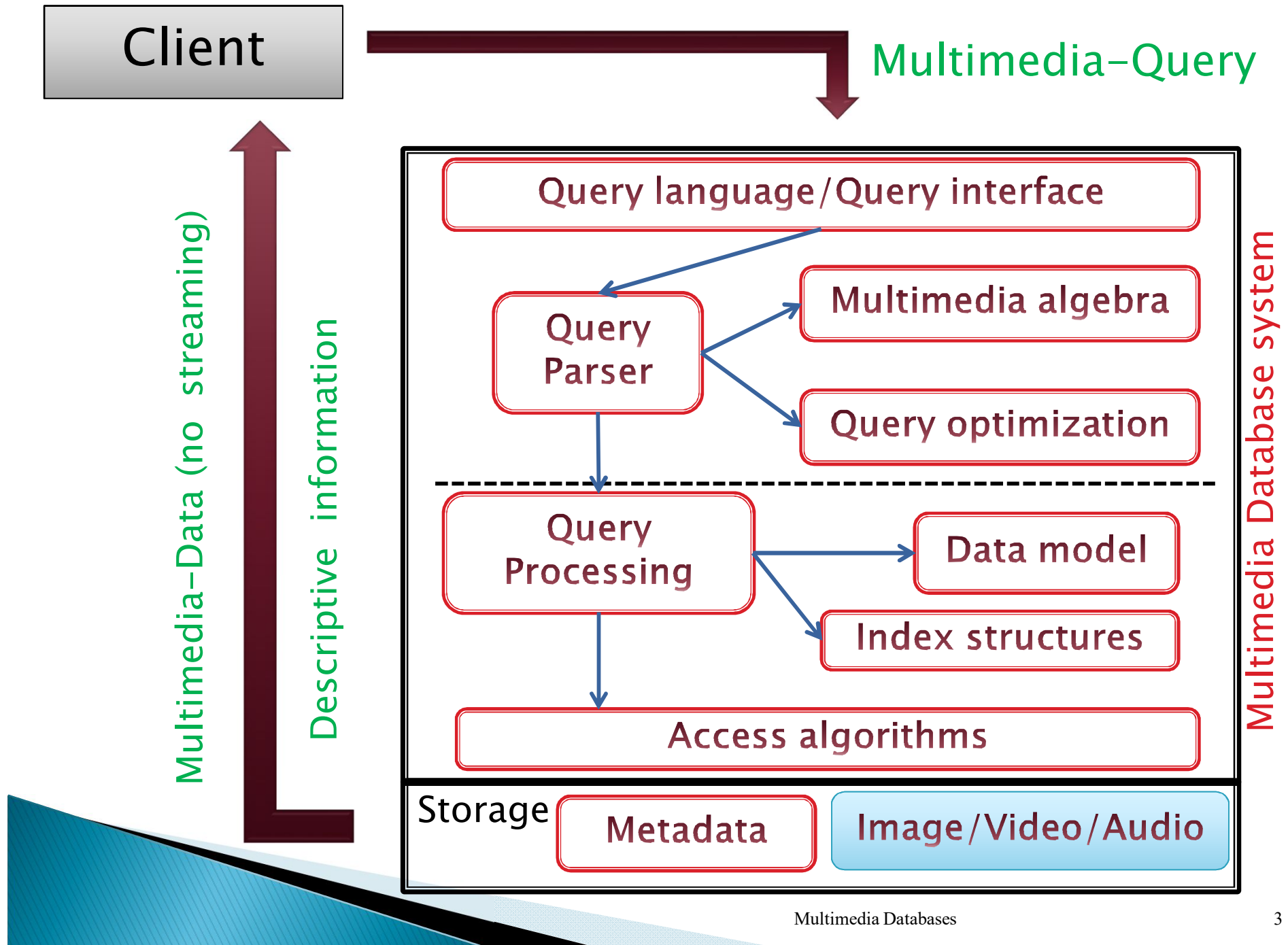


# Table of Contents

## Image

---

- 2      **Vector Graphics**
  - Bezier Curves
- 3      **Image Manipulation**
  - Image Point Operations
  - Filter
  - Geometric Operations



# Table of Contents

## Image

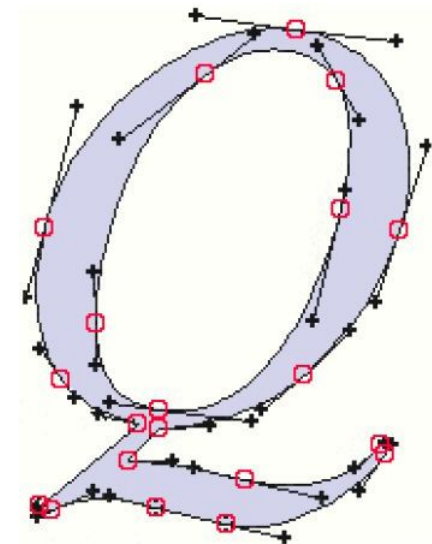
---

- 2      **Vector Graphics**
  - Bezier Curves
- 3      **Image Manipulation**
  - Image Point Operations
  - Filter

# Vector Graphics – Generalities I

Vector graphics are **mathematically** and **programmatically** defined **drawing instructions** within a **coordinate system**.

- ▶ Geometric transformations can be easily and exactly applied to vector graphics :
  - Scale, rotate, move
  - Single image elements can be separated:
    - Levels, groups, object
  - Attributes of image elements can be modified:
    - Color of an area, thickness of a line etc.



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# Vector graphics – Generalities II

---

- ▶ Vector graphics formats
  - PostScript (.ps, .eps). PDF
  - Windows Metafile (\*.wmf, \*.emf)
  - Corel Draw (\*.cdr)
  - Scalable Vector Graphics (\*.svg)
  - VRML (3D)
  - And more...
- ▶ **Drawbacks of** Vector Graphics: the images must be drawn in order to be visible:
  - Rendering (reproduction, interpretation)



# Representation of graphics

---

Computer generated Images  
based on models

## Mostly Geometric models

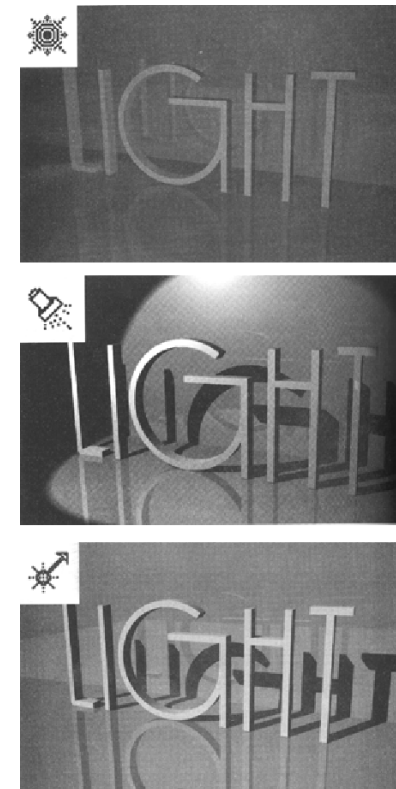
- Graphic libraries of 2D- and 3D- elementary objects (primitives)
- Associated functions, e.g.: rotation



# Operations for graphics

Highly dependent on the model

- ▶ **Editing**
  - Primitive and structures (spatial relations)
- ▶ **Shading**
  - Lighting effects on surfaces (mirroring etc.)
- ▶ **Mapping**
  - Textures
  - Irregularities of the surface, reflection
- ▶ **Lighting**
  - Position of light sources
- ▶ **Display**
  - 3D- to 2D-representation (model → screen)
- ▶ **Rendering**
  - Generation of an image based on the model and parameters (Resolution etc.)





# Scalable Vector Graphics (SVG)



- ▶ Language for **2D-Graphics** in XML
  - Can be combined with other Web standards
- ▶ Three types of graphical objects
  - Shapes (Paths of curves and straight lines)
  - Images (Raster graphics)
  - Text
- ▶ Graphical objects may be
  - grouped
  - „styled“ (CSS)
  - transformed
  - combined
- ▶ **Goodies:**
  - Global transformations
  - „Clipping paths“ (flexibly cut images)
  - Alpha masks (Objects transparency)
  - Filter effects
  - Object templates
- ▶ SVG drawings are potentially
  - interactive and
  - Dynamic

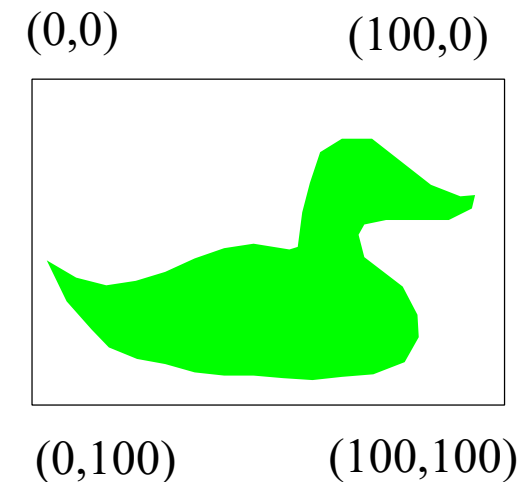
<https://wiki.selfhtml.org/wiki/SVG>



<http://www.w3.org/Graphics/SVG/>  
Current v2011

# SVG Coordinate System

- ▶ (0,0) is top left
- ▶ User Coordinate System default in screen-pixel units (e.g. 100 units in SVG are 100 pixel on screen)
- ▶ Units can be change

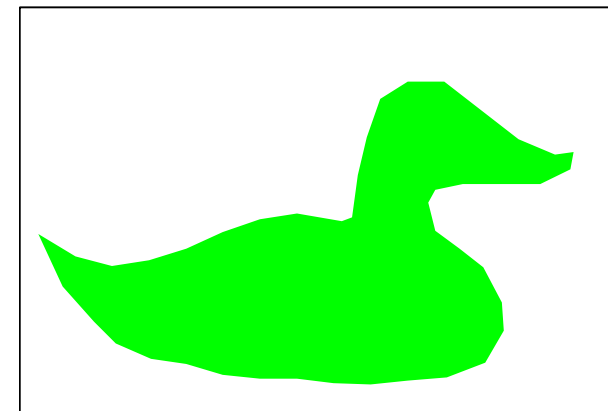


- ▶ Width / height / units defined in header:

```
<?xml version="1.0"?>
<!DOCTYPE svg PUBLIC "-//W3C//DTD SVG 1.1//EN"
"http://www.w3.org/Graphics/SVG/1.1/DTD/svg11.dtd">
<svg xmlns="http://www.w3.org/2000/svg"
      xmlns:xlink="http://www.w3.org/1999/xlink"
      width="320" height="220">
```

# SVG Example

```
<?xml version="1.0"?>
<!DOCTYPE svg PUBLIC "-//W3C//DTD SVG 1.1//EN"
"http://www.w3.org/Graphics/SVG/1.1/DTD/svg11.dtd">
<svg xmlns="http://www.w3.org/2000/svg"
      xmlns:xlink="http://www.w3.org/1999/xlink"
      width="320" height="220">
  <rect width="320" height="220" fill="white" stroke="black"/>
  <g transform="translate(10 10)">
    <g stroke="none" fill="lime">
      <path d="M 0 112 L 20 124 L 40 129 L 60 126 L 80 120
        L 100 111 L 120 104 L 140 101 L 164 105 L 170 103
        L 173 80 L 178 60 L 185 39 L 200 30 L 220 30
        L 260 61 L 280 69 L 290 68 L 288 77 L 272 85
        L 250 85 L 230 85 L 215 88 L 211 95 L 215 110
        L 228 120 L 241 130 L 251 149 L 252 164 L 242 181
        L 221 189 L 200 191 L 180 193 L 160 192 L 140 190
        L 120 190 L 100 188 L 80 182 L 61 179 L 42 171
        L 30 159 L 13 140 Z"/>
    </g> </g>
  </svg>
```



# Table of Contents

## Image

---

- 5      Vector Graphics
  - 5.1 Bezier Curves**
- 6      Image Manipulation
  - 6.1 Image Point Operations
  - 6.2 Filter



# Bezier Curves

# Properties of Parametric Curves

---

- ▶ Parametric curves are intended to provide the generality of polygons but with fewer parameters for smooth surfaces
  - Polygon have as many parameters as there are vertices (at least)
- ▶ Fewer parameters makes it faster to create a curve, and easier to edit an existing curve
- ▶ Parametric curves are easier to animate than polygon meshes



# Parametric Curves

---

- ▶ The parametric form for a line:

$$x = x_0t + (1-t)x_1$$

$$y = y_0t + (1-t)y_1$$

$$z = z_0t + (1-t)z_1$$

- ▶  $x$ ,  $y$  and  $z$  are each given by an equation that involves:
  - the parameter  $t$
  - Some user specified control points, like  $x_0$  and  $x_1$



# Hermite Spline (1)

---

- ▶ A *spline* is a parametric curve defined by *control points*
  - The term spline dates from engineering drawing, where a spline was a piece of flexible wood used to draw smooth curves
  - The control points are *adjusted by the user* to control the shape of the curve
- ▶ A *Hermite spline* is a curve for which the user provides:
  - The endpoints of the curve
  - The parametric derivatives of the curve at the endpoints
    - The parametric derivatives are  $dx/dt$ ,  $dy/dt$ ,  $dz/dt$





# Hermite Spline (2)

---

- ▶ Say the user provides

$$x_0, x_1, x'_0, x'_1$$

- ▶ A cubic spline has degree 3, and is of the form:

$$x = at^3 + bt^2 + ct + d$$

- ▶ We have constraints to determine a,b,c,d
  - The curve must pass through  $x_0$  when  $t=0$
  - The derivative must be  $x'_0$  when  $t=0$
  - The curve must pass through  $x_1$  when  $t=1$
  - The derivative must be  $x'_1$  when  $t=1$



# Hermite Spline (3)

---

- ▶ Solving for the unknowns gives:

$$a = -2x_1 + 2x_0 + x'_1 + x'_0$$

$$b = 3x_1 - 3x_0 - x'_1 - 2x'_0$$

$$c = x'_0$$

$$d = x_0$$



# Bezier Curves (1)

---

- ▶ Different choices of basis functions give different curves
  - In Hermite case, two control points define endpoints, and two more define parametric derivatives
- ▶ For Bezier curves, two control points define endpoints, and two control the tangents at the endpoints in a geometric way



# Bezier Curves (2)

---

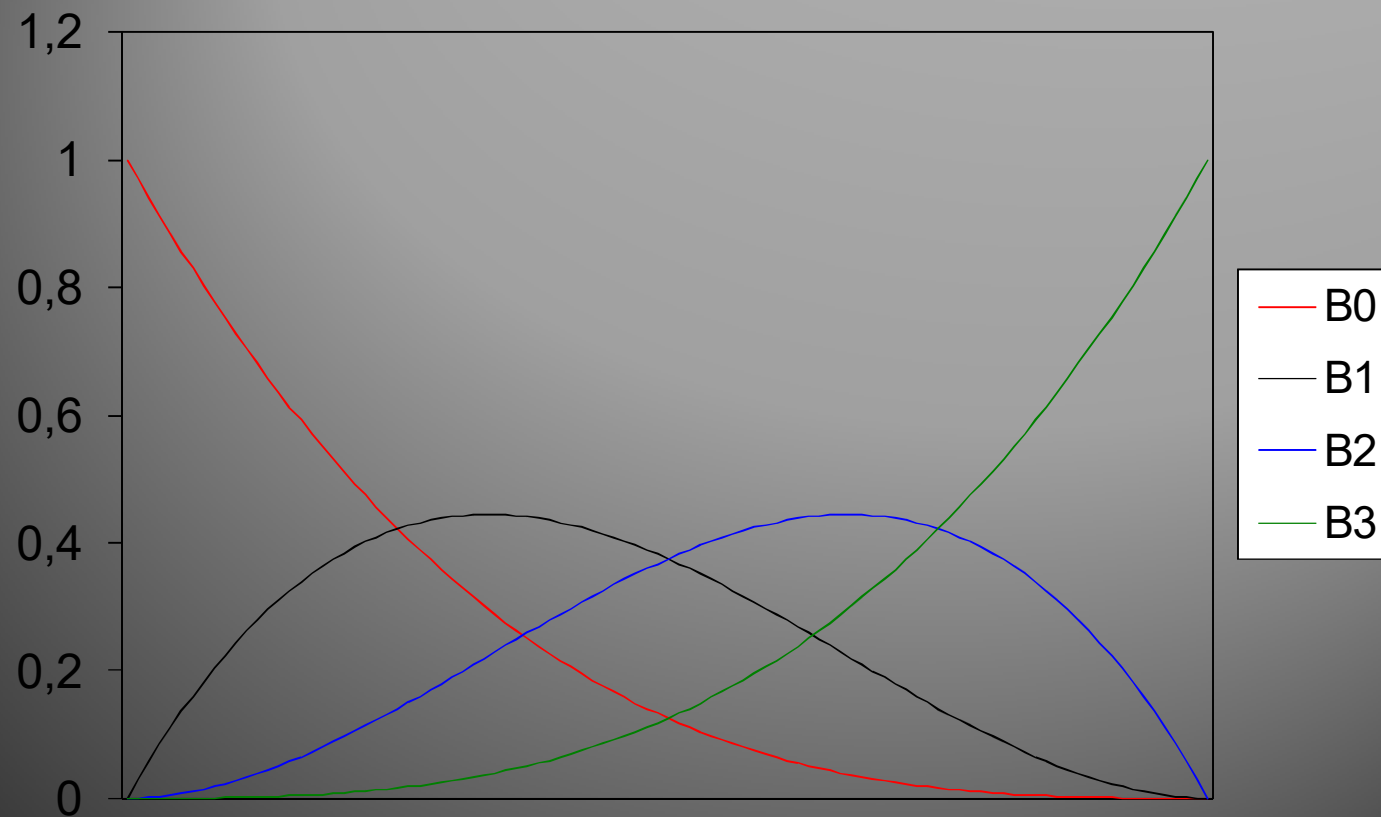
- ▶ The user supplies  $d$  control points,  $\mathbf{p}_i$
- ▶ Write the curve as:

$$\mathbf{x}(t) = \sum_{i=0}^d \mathbf{p}_i B_i^d(t) \qquad B_i^d(t) = \binom{d}{i} t^i (1-t)^{d-i}$$

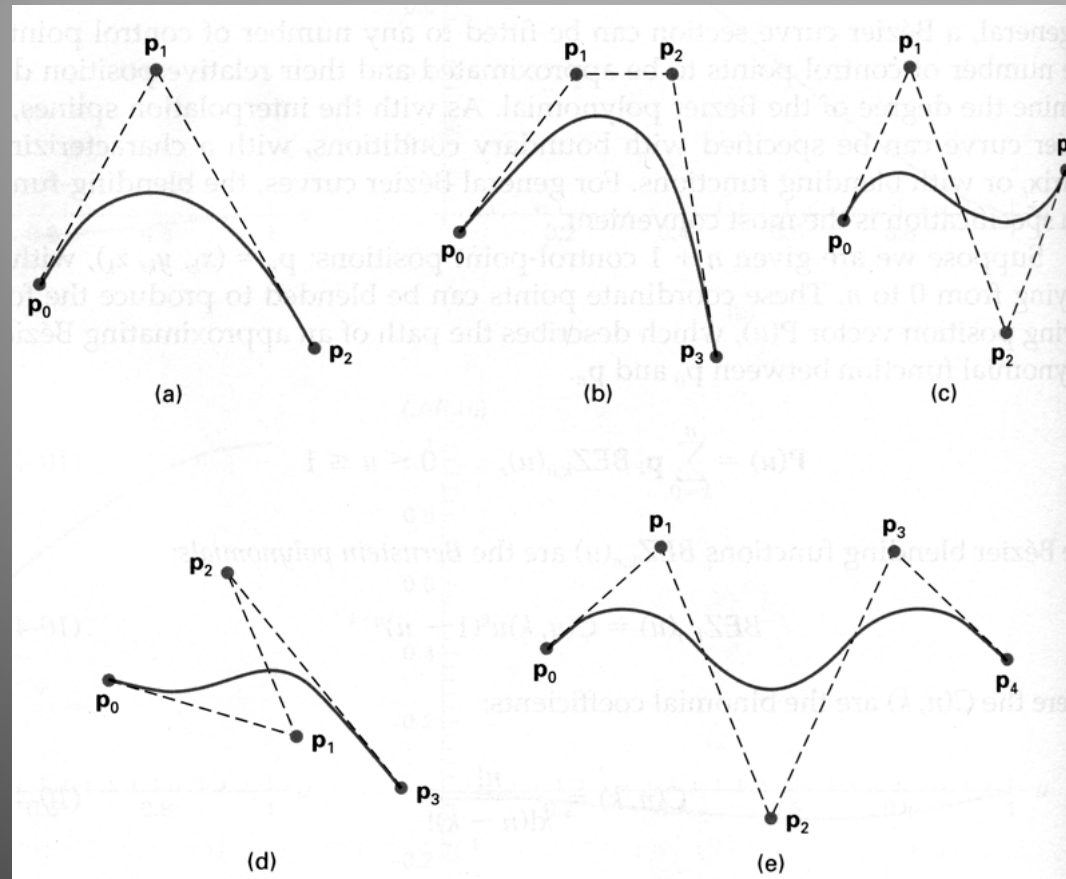
- ▶ The functions  $B_i^d$  are the *Bernstein polynomials* of degree  $d$



# Bezier Basis Functions for $d=3$



# Some Bezier Curves



# Bezier Curve Properties

---

- ▶ The first and last control points are interpolated
- ▶ The tangent to the curve at the first control point is along the line joining the first and second control points
- ▶ The tangent at the last control point is along the line joining the second last and last control points
- ▶ The curve lies entirely within the convex hull of its control points



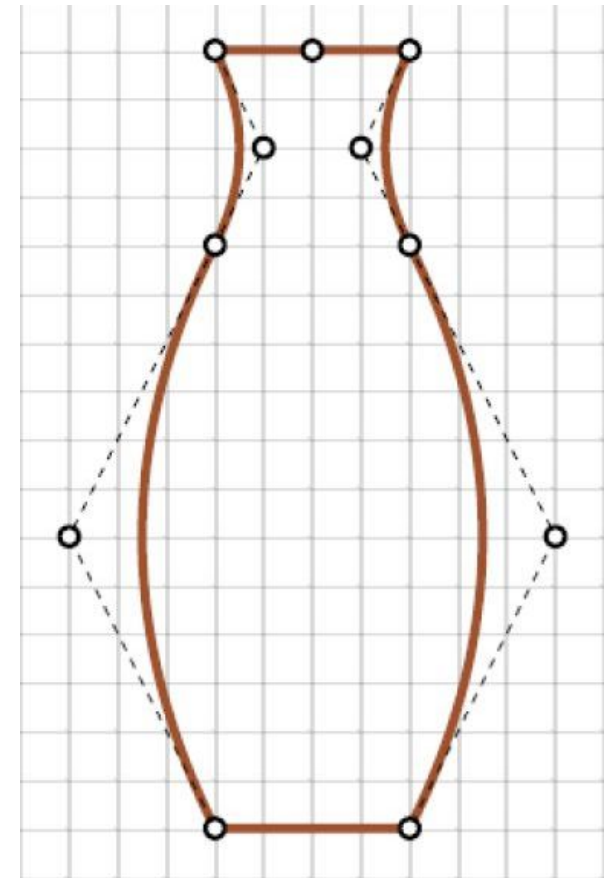
# SVG: Splines Example I

```
<?xml version="1.0" standalone="no"?>
<!DOCTYPE svg PUBLIC "-//W3C//DTD SVG 20010904//EN"
"http://www.w3.org/TR/2001/REC-SVG-
20010904/DTD/svg10.dtd">

<svg width="12cm" height="7.2cm"
  viewBox="0 0 1000 600"
  xmlns="http://www.w3.org/2000/svg" >

  <path stroke="sienna" stroke-width="2"
    fill="none"
    d="M 80,180
      Q 50,120 80,60
      Q 90, 40 80,20
      Q 100, 20 120,20
      Q 110, 40 120,60
      Q 150,120 120,180Z" />

</svg>
```



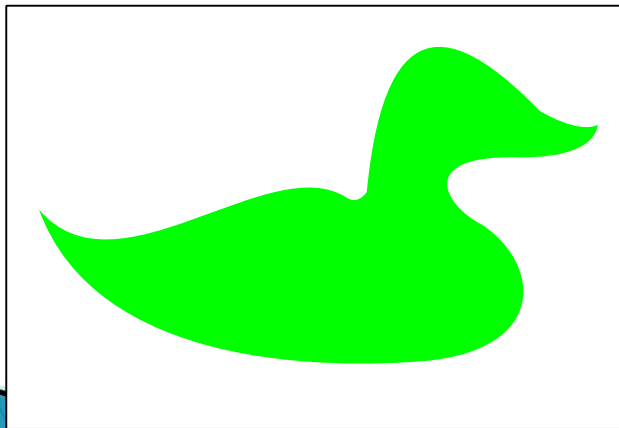
© Folien Medientechnik, Uni Koblenz



# SVG Example II – Bezier Paths

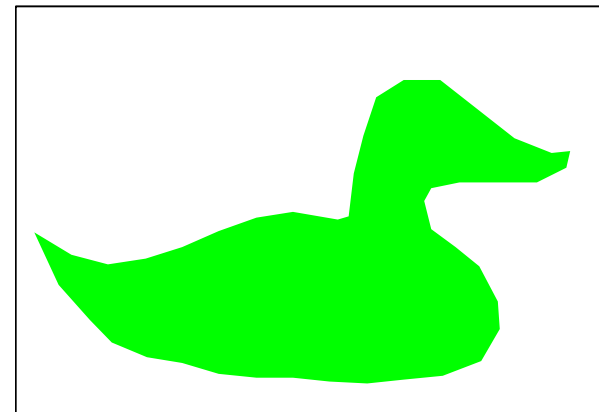
With Bezier curves

```
<path d="M 0 312  
C 40 360 120 280 160 306 C 160 306 165 310 170 303  
C 180 200 220 220 260 261 C 260 261 280 273 290 268  
C 288 280 272 285 250 285 C 195 283 210 310 230 320  
C 260 340 265 385 200 391 C 150 395 30 395 0 312 z"/>
```



Without Bezier curves

```
<path d="M 0 112 L 20 124 L 40 129 L 60 126 L 80 120  
L 100 111 L 120 104 L 140 101 L 164 105 L 170 103  
L 173 80 L 178 60 L 185 39 L 200 30 L 220 30  
L 260 61 L 280 69 L 290 68 L 288 77 L 272 85  
L 250 85 L 230 85 L 215 88 L 211 95 L 215 110  
L 228 120 L 241 130 L 251 149 L 252 164 L 242 181  
L 221 189 L 200 191 L 180 193 L 160 192 L 140 190  
L 120 190 L 100 188 L 80 182 L 61 179 L 42 171  
L 30 159 L 13 140 z"/>
```



# Table of Contents

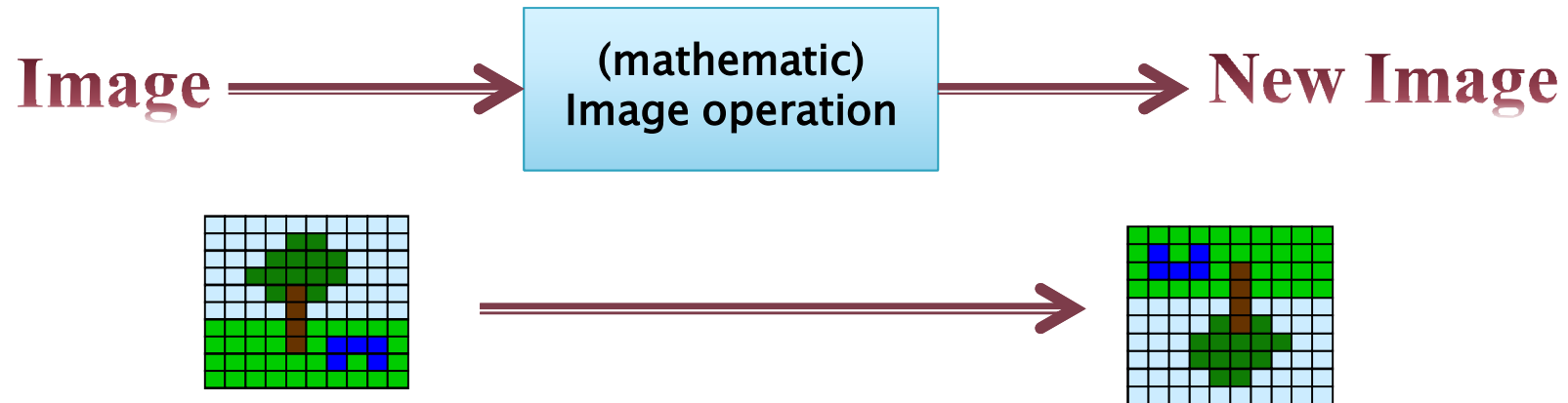
## Image

---

- 2      **Vector Graphics**
  - Bezier Curves
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# Types of Image Manipulation

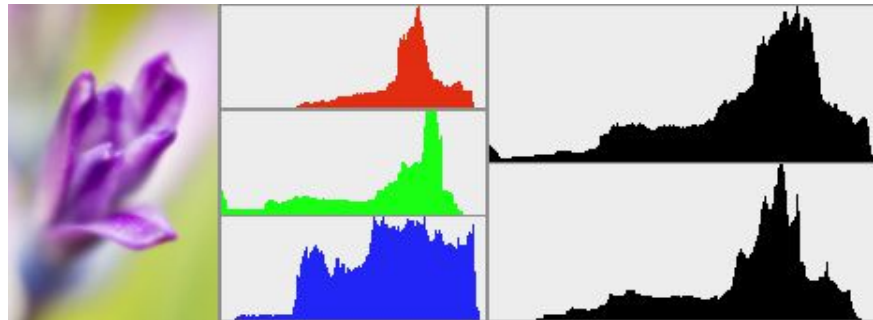
---



- ▶ Image Point Operations
  - Applied to an Image
- ▶ Neighborhood operations/Filter
- ▶ Geometric Operations

# Color-Histogram

- ▶  $h_c(i)$ : Number of Pixels with a particular color value  $i$  for a channel  $c$ 
  - Allows to identify basic properties of images (e.g. low contrast images)
  - Basis for point operations (e.g. contrast enhancements)

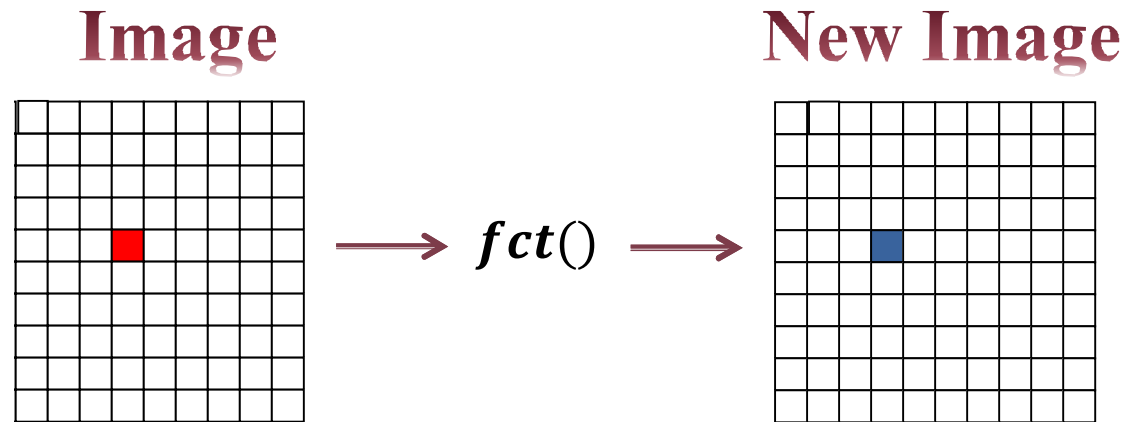


<http://blog.epicdis.com/2007/04/14/working-with-image-histograms/>

# Image Point Operations

# Image Point Operation

---



$$PixelNew(x, y) = fct(Pixel(x, y))$$

- ▶ Brightness and contrast adjustment
- ▶ Color corrections, tonal value corrections
- ▶ Image overlays, etc.

# Image Point Operation II

- ▶ Simple Example:  
Negative of a greyscale image

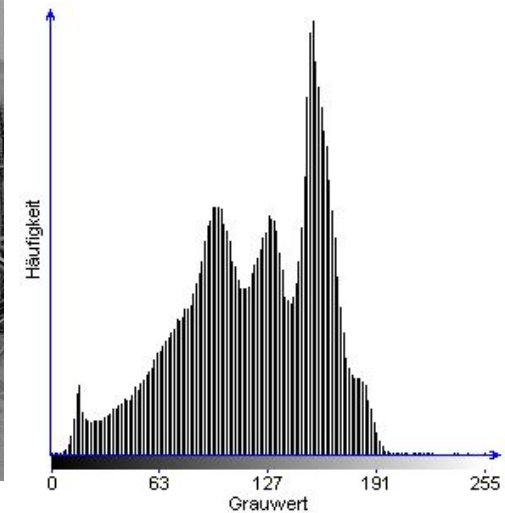
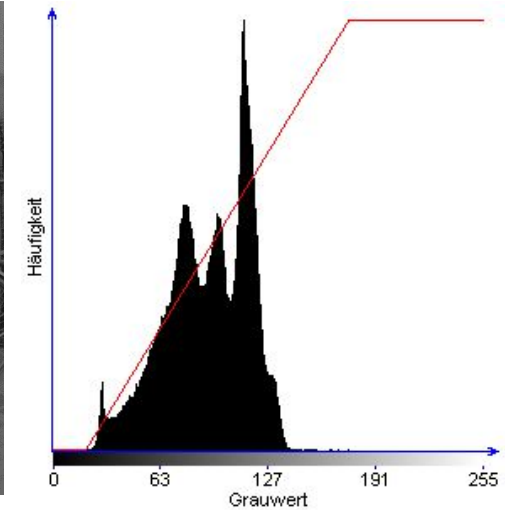
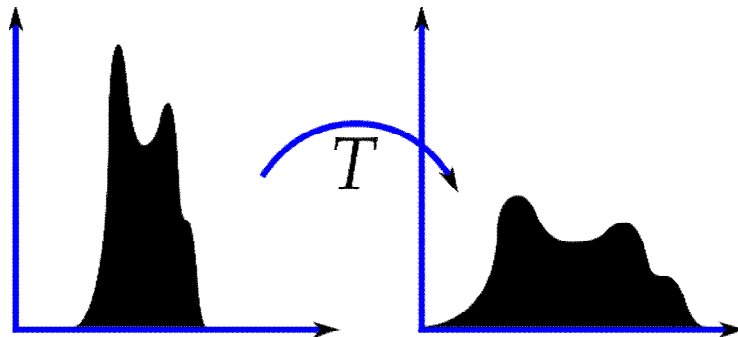
$$PixelNew(x, y) = 255 - Pixel(x, y)$$





# Histogram Spreading

New Histogramm  $h_c(i)$



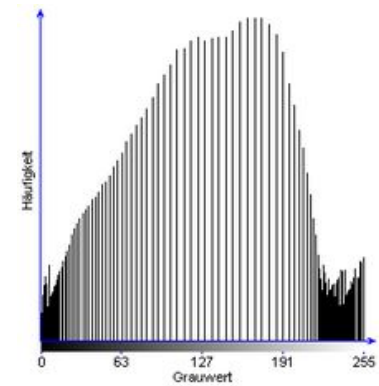
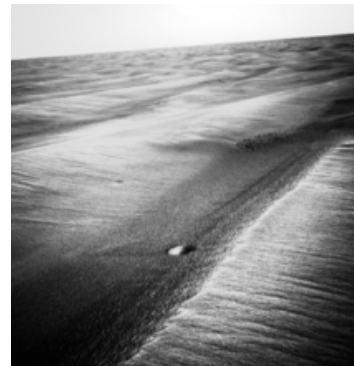
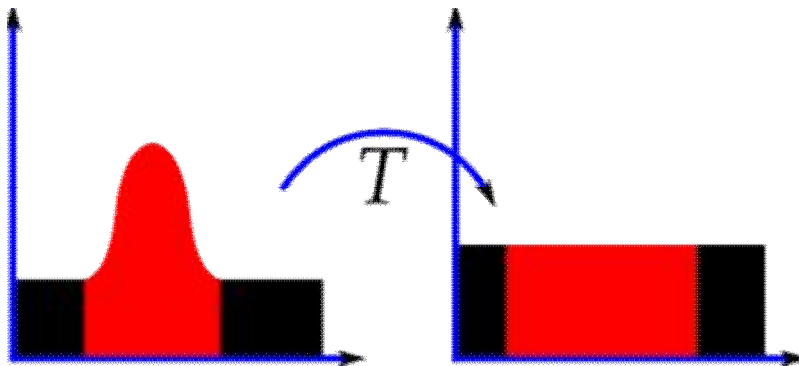
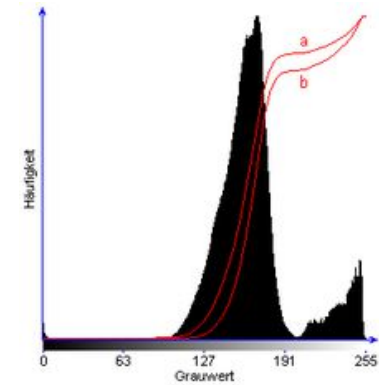


# Histogramm Equalization

- ▶ Cumulative Histogramm

$$H(i) = \sum_{j=0}^i h_c(j)$$

- ▶ New Histogramm

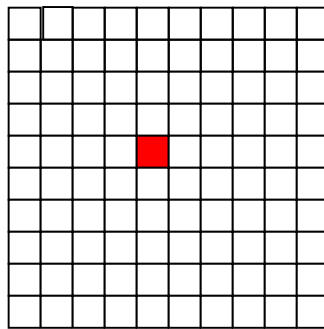


# Filter

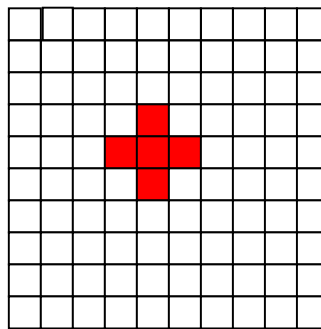
# Neighborhood operations/Filter

- ▶ Neighborhood is defined by the following formula:

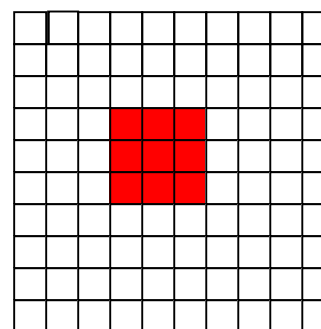
$$N_c(x, y) = \{(i, j): 0 < (i - x)^2 + (j - y)^2 \leq c\}$$



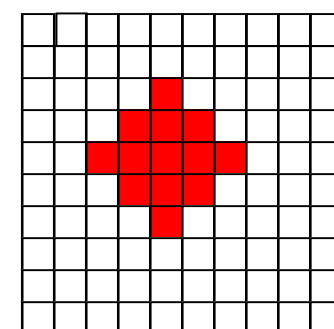
**c=0**



**c=1**



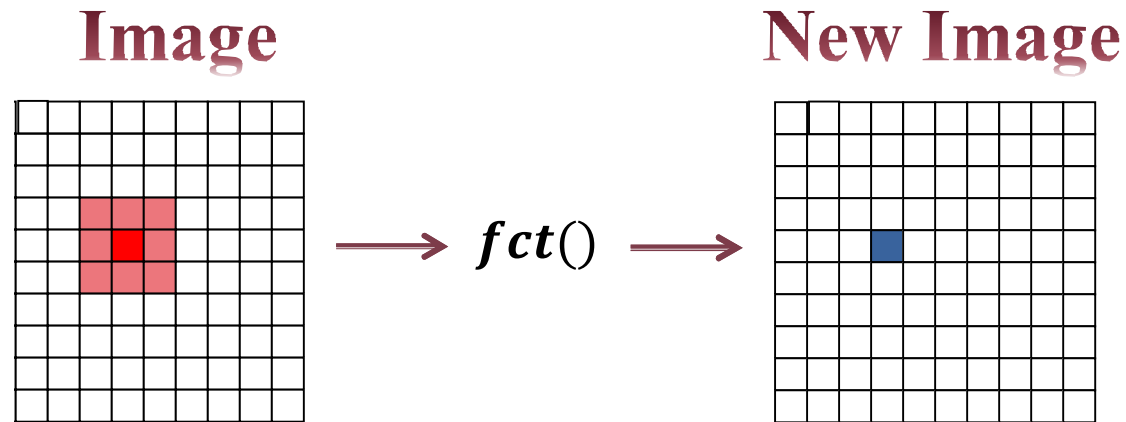
**c=2**



**c=3**

# Filter = Neighborhood operations

---



$$B^{\text{new}}(x, y) = fct(N_c(x, y))$$

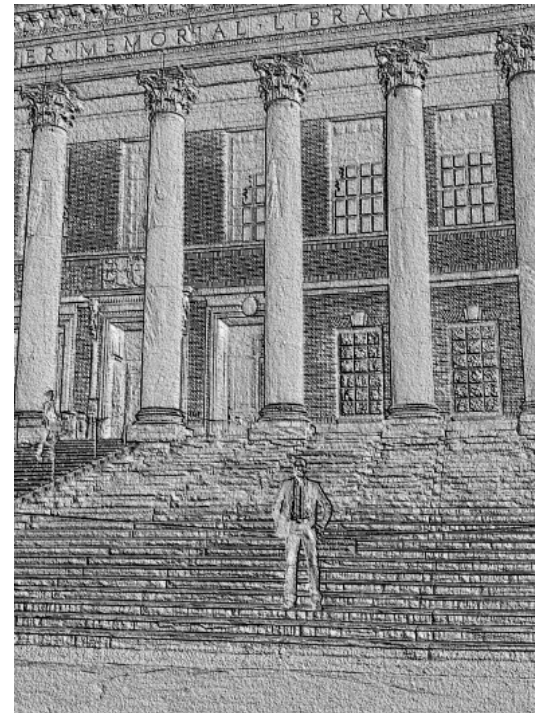
- ▶ Enhancement and blurring
- ▶ Denoising
- ▶ Edge detection

# Filter Example:

## Vertical relief generation

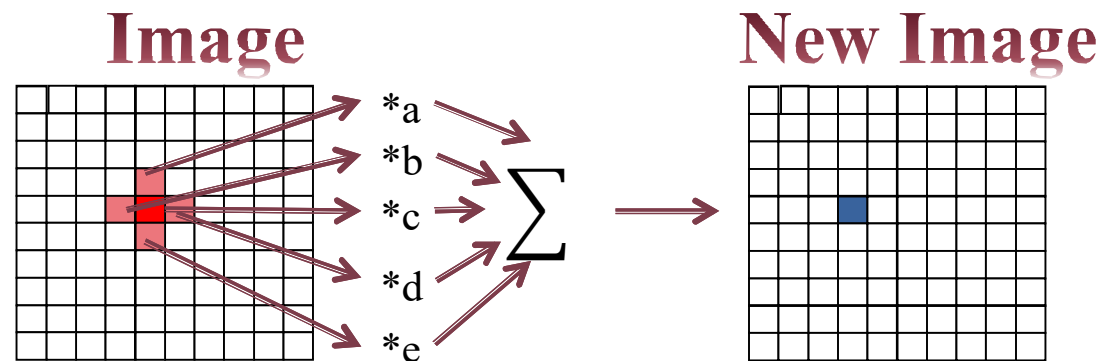
---

$$B^{\text{new}}(x, y) = 2 * B(x, y) - 2 * B(x, y - 1) + 128$$



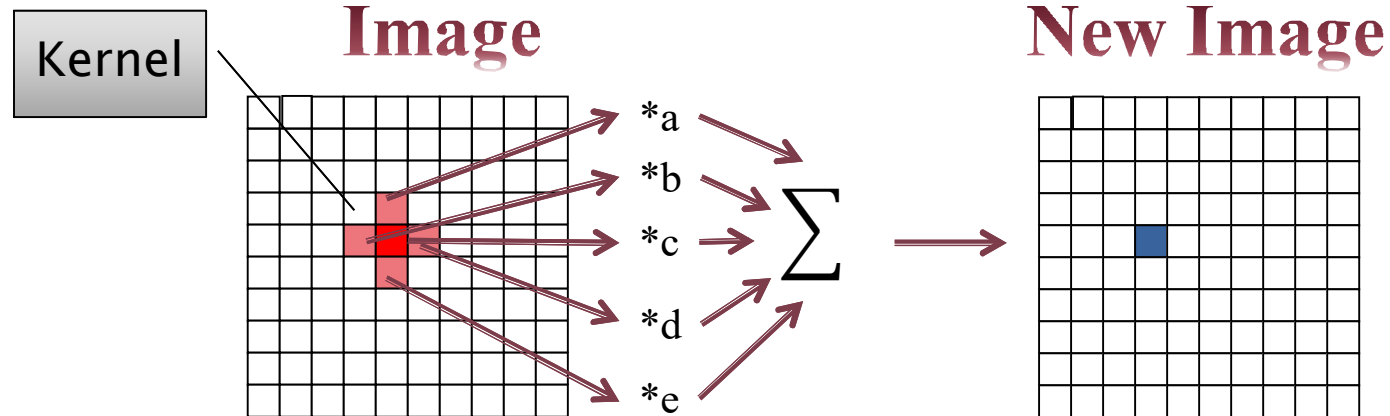
# Linear Filter = Convolution

- ▶ Linear Filter: Each (Pixel-)value is replaced by a linear weighted combination of the (Pixel-)values of its „neighborhood“ (the kernel region).





# Linear Filter



$$B^{\text{new}}(x, y) = a * B(x, y - 1) + b * B(x - 1, y) + c * B(x, y) + d * B(x + 1, y) + e * B(x, y + 1)$$

*M x N Kernel with Folding*

$$K = \begin{bmatrix} 0 & a & 0 \\ b & c & d \\ 0 & e & 0 \end{bmatrix}$$

$$B^{\text{new}}(x, y) = \mathbf{K} * \mathbf{B}(x, y) = \sum_{i=-M}^M \sum_{j=-N}^N K(i, j) \cdot B(x - i, y - j)$$

# Mode of operation of linear filters

---

- ▶ **Image point operations** (gradation curves,  $K=1 \times 1$ ) scale Pixel-(values) i.e. they modify the amplitude ratios
- ▶ **Linear neighborhood operators (Filter)** scale the spectral domains i.e. they modify the frequency ratios

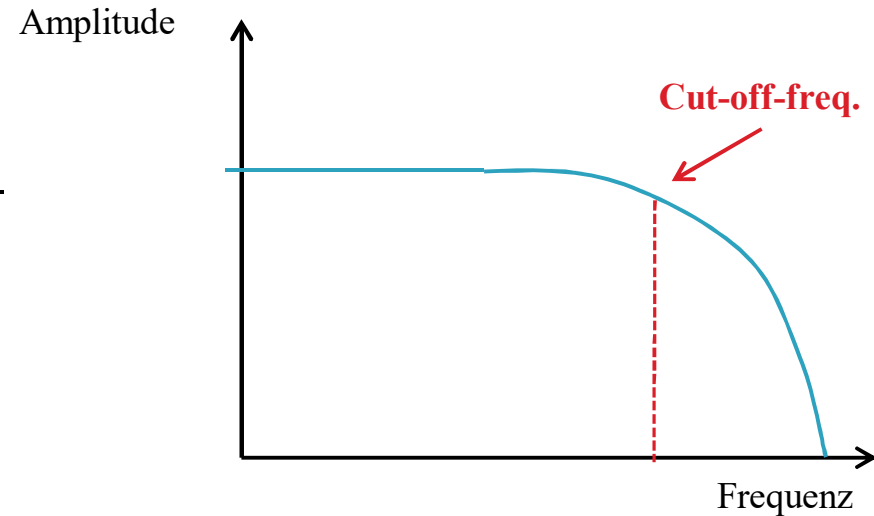




# Filter properties

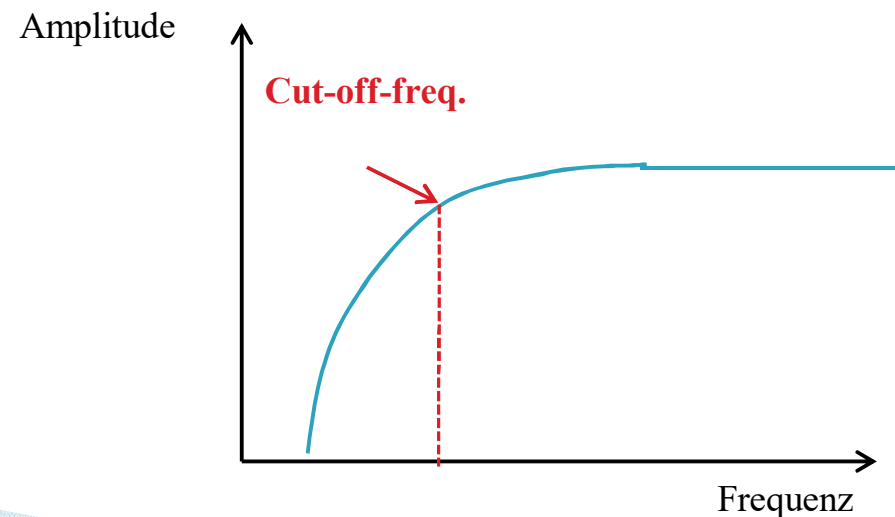
## ► Low-pass filter

- Frequencies above a specific one, the cut-off-frequency are reduced, whereas lower frequencies can „pass“



## ► High-pass-Filter

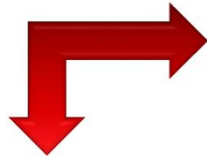
- Frequencies below the cut-off-frequency are reduced, the higher one can pass.



# Example

## Low- and high-pass filter

Low-pass filter



High-pass filter



The End

