

Sorts

Understanding Array Sorting Algorithms, Efficiency, Comparison and Implementation

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Runtime and Memory Complexity: Basics

- **Runtime Complexity**
 - Time an algorithm takes relative to input length.
- **Memory Complexity**
 - Memory needed by an algorithm relative to input size.
- Both are crucial for:
 - Comparing algorithm efficiency.
 - Choosing the right algorithm for the job.

Measuring Program Execution Time: Challenges

Types of Time Measurements

- **Time Measurement Issues**

- Real Time: Wall-clock time for program execution.
- User Time: CPU time for executing user program code.
 - Excludes system operations.
 - Reflects direct program execution time.
- System Time¹: CPU time for system operations for the program.
 - File operations, I/O tasks.
 - Essential for resource-intensive operations.

- Variability in measurements due to:

- System load, resources, hardware.
- Inconsistencies across environments.

¹See <https://stackoverflow.com/questions/556405/what-do-real-user-and-sys-mean-in-the-output-of-time1>

Measuring Program Execution Time: Theoretical Approach

Abstracting Time Measurements

- **Theoretical Approach**

- Approximate with **input size** (n) and **operation count**.
- $n \in \mathbb{N}^*$: Number of loops or iterations – main driver of complexity.
- $k \in \mathbb{N}^*$: Parameters affecting complexity, aside from input size.
 - Here intended as range of the non-negative key values
- Focus on growth trends rather than exact times.

- **Conclusion:**

- Theoretical focus helps identify scalability issues.
- Prioritizes relative efficiency over absolute timing.

Understanding Big O Notation

- **Big O Notation:** Describes the upper bound of complexity.
 - Focuses on worst-case scenario.
 - Ignores constant factors and lower order terms.
- **Basic Rules**
 - *Linear Terms:* $\mathcal{O}(\alpha n + \beta) = \mathcal{O}(n)$.
 - Constants α, β don't affect growth rate.
 - *Sum Rule:* $\mathcal{O}(f(n)) + \mathcal{O}(g(n)) = \mathcal{O}(\max(f(n), g(n)))$.
 - *Product Rule:* $\mathcal{O}(f(n)) \cdot \mathcal{O}(g(n)) = \mathcal{O}(f(n) \cdot g(n))$.
- **Implications**
 - Simplifies comparing algorithms.
 - Emphasizes dominant factors affecting growth.
- **Example**
 - $\mathcal{O}(3n^2 + 10n + 100) = \mathcal{O}(n^2)$.
 - n^2 term dominates as n grows.

Classic Sorting Algorithms and Their Complexities

Algo.	Best	Average	Worst	Mem.
Selection Sort	$\mathcal{O}(n^2)$	$\mathcal{O}(n^2)$	$\mathcal{O}(n^2)$	$\mathcal{O}(1)$
Insertion Sort	$\mathcal{O}(n)$	$\mathcal{O}(n^2)$	$\mathcal{O}(n^2)$	$\mathcal{O}(1)$
Bubble Sort	$\mathcal{O}(n)$	$\mathcal{O}(n^2)$	$\mathcal{O}(n^2)$	$\mathcal{O}(1)$
Merge Sort	$\mathcal{O}(n \log n)$	$\mathcal{O}(n \log n)$	$\mathcal{O}(n \log n)$	$\mathcal{O}(n)$
Quick Sort	$\mathcal{O}(n \log n)$	$\mathcal{O}(n \log n)$	$\mathcal{O}(n^2)$	$\mathcal{O}(\log n)$

More Algorithms and Their Complexities²

Algorithm	Best	Average	Worst	Memory
Selection Sort	$\Omega(n^2)$	$\Theta(n^2)$	$O(n^2)$	$O(1)$
Insertion Sort	$\Omega(n)$	$\Theta(n^2)$	$O(n^2)$	$O(1)$
Bubble Sort	$\Omega(n)$	$\Theta(n^2)$	$O(n^2)$	$O(1)$
Merge Sort	$\Omega(n \log n)$	$\Theta(n \log n)$	$O(n \log n)$	$O(n)$
Quick Sort	$\Omega(n \log n)$	$\Theta(n \log n)$	$O(n^2)$	$O(\log n)$
Timsort	$\Omega(n)$	$\Theta(n \log n)$	$O(n \log n)$	$O(n)$
Heapsort	$\Omega(n \log n)$	$\Theta(n \log n)$	$O(n \log n)$	$O(1)$
Tree Sort	$\Omega(n \log n)$	$\Theta(n \log n)$	$O(n^2)$	$O(n)$
Shell Sort	$\Omega(n \log n)$	$\Theta(n(\log n)^2)$	$O(n(\log n)^2)$	$O(1)$
Bucket Sort	$\Omega(n + k)$	$\Theta(n + k)$	$O(n^2)$	$O(n)$
Radix Sort	$\Omega(nk)$	$\Theta(nk)$	$O(nk)$	$O(n + k)$
Counting Sort	$\Omega(n + k)$	$\Theta(n + k)$	$O(n + k)$	$O(k)$
Cubesort	$\Omega(n)$	$\Theta(n \log n)$	$O(n \log n)$	$O(n)$

²See <https://www.bigocheatsheet.com/>

Selection Sort Algorithm

Simplicity in Action

- **How It Works**

- Iteratively selects the smallest element from the unsorted portion and swaps it with the element at the current position.
- Continues until the entire array is sorted.

```
def selection_sort(arr):  
    for i in range(len(arr)):  
        min_idx = i  
        for j in range(i+1, len(arr)):  
            if arr[j] < arr[min_idx]:  
                min_idx = j  
        arr[i], arr[min_idx] = arr[min_idx], arr[i]  
    return arr
```

Thank You for Your Attention!

Further Resources

- **Useful Links**

- Big O Cheat Sheet: <https://www.bigocheatsheet.com/>
 - A handy reference for complexity of common data structures and algorithms.
- Sorting Algorithms with Animations: <https://www.toptal.com/developers/sorting-algorithms/bubble-sort>
 - Explore how different sorting algorithms work with interactive animations.

- **Contact & Feedback**

- My GitHub: <https://github.com/onyr>
- This presentation: https://github.com/onyr/sorting_algorithms

Once again, thank you and have a great day!