Non-Metric Space Library Manual

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Abstract. This document describes a library for similarity searching. Even though the library contains a variety of metric-space access methods, our main focus is on search methods for non-metric spaces. Because there are fewer exact solutions for non-metric spaces, many of our methods give only approximate answers. Thus, the methods are evaluated in terms of efficiency-effectiveness trade-offs rather than merely in terms of their efficiency. Our goal is, therefore, to provide not only state-of-theart approximate search methods for both non-metric and metric spaces, but also the tools to measure search quality. We concentrate on technical details, i.e., how to compile the code, run the benchmarks, evaluate results, and use our code in other applications. Additionally, we explain how to extend the code by adding new search methods and spaces.

1 Introduction

1.1 Motivation

The Non-Metric Space Library is a collection of similarity search methods and a toolkit for their evaluation. Our software suit can also be used as a standalone search library on Linux and Windows. Most search methods were implemented by Bileg(saikhan) Naidan and Leo(nid) Boytsov.³ Additional contributors are listed on the GitHub page.

The code written by Bileg and Leo is distributed under the business-friendly Apache License. Some contributions are licensed differently. For more information regarding licensing and acknowledging the use of the library resource, please refer to \S 9.

³ Leo(nid) Boytsov is a maintainer.

The design of the library was influenced by and superficially resembles the design of the Metric Spaces Library [18]. Yet our approach is different in many ways:

- We focus on approximate⁴ search methods and non-metric spaces.
- We simplify experimentation, in particular, through automatically measuring and aggregating important parameters related to speed and accuracy. In addition, we provide capabilities for testing in both single- and multi-threaded modes to ensure that implemented solutions scale well with the number of available CPUs.
- We care about overall efficiency and aim to implement methods that have runtime comparable to an optimized production system.

Search methods for non-metric spaces are especially interesting. This domain does not provide sufficiently generic exact search methods. We may know very little about analytical properties of the distance or the analytical representation may not be available at all (e.g., if the distance is computed by a black-box device [29]). In many cases it is not possible to search exactly and instead one has to resort to approximate search procedures.

This is why methods are evaluated in terms of efficiency-effectiveness tradeoffs rather than merely in terms of their efficiency. We believe that there is no "one-size-fits-all" search method. Hence, it is important to being able to evaluate the "goodness of fit" for a particular domain.

Our commitment to efficiency affected several design decisions:

- The library is implemented in C++;
- We focus on in-memory indices and, thus, do not require our methods to materialize a disk-based version of an index (this also reduces programming effort).
- We provide efficient implementations of many distance functions, which rely on Single Instruction Multiple Data (SIMD) CPU commands and/or approximation of computationally intensive mathematical operations (see § 7).

It is often possible to demonstrate a substantial reduction in the number of distance computations compared to sequential searching. However, such reductions entail additional computations (i.e., extra book-keeping) and do not always lead to improved overall performance [3]. To eliminate situations where book-keeping costs are "masked" by inefficiencies of the distance function, we pay special attention to distance function efficiency.

1.2 Problem Formulation

Similarity search is an essential part of many applications, which include, among others, content-based retrieval of multimedia and statistical machine learning.

⁴ An approximate method may not return a true nearest-neighbor or all the points within a given query ball.

The search is carried out on a finite database of objects $\{o_i\}$ (we also used a term data point or simply point), using a search query q and a dissimilarity measure. The dissimilarity measure is typically represented by a distance function $d(o_i, q)$. The ultimate goal is to answer a query by retrieving a subset of database objects sufficiently similar to the query q. These objects will be called **answers**. Note that we use the terms **distance** and the **distance** function in a broader sense than usually: We do not assume that the distance is a true metric distance. The distance can be asymmetric and is not constrained to be metric (i.e., it may not satisfy the triangle inequality).

Two retrieval tasks are typically considered: a nearest neighbor and a range search. The nearest neighbor search aims to find the least dissimilar object, i.e., the object at the smallest distance from the query. Its direct generalization is the k-nearest neighbor search (the k-NN search), which looks for the k most closest objects. Given a radius r, the range query retrieves all objects within a query ball (centered at the query object q) with the radius r, or, formally, all the objects $\{o_i\}$ such that $d(o_i,q) \leq r$. In generic spaces, the distance is not necessarily symmetric. Thus, two types of queries can be considered. In a left query, the object is the left argument of the distance function, while the query is the right argument. In a right query, q is the first argument and the object is the second, i.e., the right, argument.

The queries can be answered either exactly, i.e., by returning a complete result set that does not contain erroneous elements, or, approximately, e.g., by finding only some answers. Thus, the methods are evaluated in terms of efficiency-effectiveness trade-offs rather than merely in terms of their efficiency. One common effectiveness metric is recall. In the case of the nearest neighbor search, it is computed as an average fraction of true neighbors returned by the method. If ground-truth judgements (produced by humans) are available, it is possible to compute an accuracy of a k-NN based classification (see § 3.5.2).

In the current release, we focus on vector-space implementations, i.e., all the distance functions are defined over real-valued vectors. Note that this is not a principal limitation, because most methods do not access data objects directly. Instead, they rely only on distance values. In the future, we plan to add more complex spaces, in particular, string-based.

2 Getting Started

2.1 Prerequisites

The Non-Metric Space Library was developed and tested on 64-bit Linux. Yet, almost all the code (except LSHKIT) can be built and run on 64-bit Windows. Building the code requires a modern C++ compiler that supports C++11. Currently, we support GNU C++ (≥ 4.7), Intel compiler (≥ 14), Clang ($\geq 4.2.1$), and Visual Studio (≥ 12 ; note that you can use the free express version). Under Linux, the build process relies on CMake. Under Windows, one should use Visual Studio projects stored in the repository.

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Note, however, that we do not have a portable code to measure memory consumption: This part will work only for Linux (with PROCFS) and Windows. More specifically, for Linux we require:

- 1. A **64-bit** distributive (Ubuntu **LTS** is recommended);
- 2. GNU C++ (≥ 4.7), Intel Compiler (≥ 14), Clang ($\geq 4.2.1$);
- 3. Cmake (GNU make is also required);
- Boost (dev version ≥ 48, Ubuntu package libboost1.48-all-dev);
- 5. GNU scientific library (dev version, Ubuntu package libgsl0-dev).

For Windows, we require:

- 1. A **64-bit** distributive (we tested on Windows 8);
- 2. Visual Studio Express (or Professional) version 12 or later;
- 3. Boost is not required to build the core library and test utilities, but it is needed by the main testing binary experiment.exe (see § 3.2).

Efficient implementations of many distance functions (see § 7) rely on SIMD instructions, which operate on small vectors of integer or floating point numbers. These instructions are available on most modern processors, but we support only SIMD instructions available on recent Intel and AMD processors. Each distance function has a pure C++ implementation, which can be less efficient than an optimized SIMD-based implementation. On Linux, SIMD-based implementations are activated automatically for all sufficiently recent CPUs. On Windows, it is necessary to update project settings manually (see §3.2).

Scripts to generate and process data sets are written in Python. We also provide the Python script to plot performance graphs: genplot.py (see § 3.7). In addition to Python, this plotting script requires Latex and PGF.

2.2Installing C++11 Compilers

Installing C++11 compilers can be tricky, because they are not always provided as a standard package. This is why we briefly review the installation process here.

It is, perhaps, the easiest to obtain Visual Studio 12 by simply downloading it from the Microsoft web-page. We were able to build and run the 64-bit code using the free distributive of Visual Studio Express 12 (also called Express 2013). The professional (and expensive) version of Visual Studio is not required.

To install GNU C++ version 4.7 on some Linux distributions with the Debian package management system, one can simply type:

```
sudo apt-get install gcc-4.7 g++-4.7
```

However, it did not work for us and we needed to use an experimental repository as follows:

```
sudo add-apt-repository ppa:ubuntu-toolchain-r/test
sudo apt-get update
sudo apt-get install gcc-4.7 g++-4.7
```

If the script add-apt-repository is missing, it can be installed as follows:

```
sudo apt-get install python-software-properties
```

More details can be found on the AskUbuntu web-site.

Similarly to the GNU C++ compiler, to install a C++11 version of Clang, one may need to add a non-standard repository. For Debian and Ubuntu distributions, it is easiest to add repositories from the LLVM web-site. For example, if you have Ubuntu 12 (Precise), you need to add repositories as follows:⁵

Then, Clang 3.4 (and LLDB debugger) can be installed by typing:

```
sudo apt-get install clang-3.4 lldb-3.4
```

The Intel compiler can be freely used for non-commerical purposes. It is a part of C++ Composer XE for Linux and can be obtained from the Intel web site. After downloading and running an installation script, one needs to set environment variables. If the compiler is installed to the folder <code>/opt/intel</code>, environment variables are set by a script as follows:

```
/opt/intel/bin/compilervars.sh intel64
```

One pitfall on Linux is that installing compilers does not necessarily make them default compilers. One way to fix this is to set environment variables CXX and CC. For the GNU 4.7 compiler:

```
export CXX=g++-4.7 CC=gcc-4.7

For the Clang compiler:

export CXX=clang++ CC=clang

For the Intel compiler:

export CXX=icc CC=icc
```

⁵ Do not forget to remove deb-src for source repositories. See the discussion here for more details.

2.3 Quick Start on Linux

To build the project, go to the directory similarity_search and type:

cmake .

This creates several binaries in the directory similarity_search/release, most importantly, a benchmarking utility experiment, which carries out experiments, and testing utilities bunit, test_integer, and bench_distfunc. Examples of using this benchmarking utility can be found in the directory sample_scripts. Please, check the script sample_run.sh.

A more detailed description of the build process on Linux is given in § 3.1.

2.4 Quick Start on Windows

Building on Windows is straightforward: One can simply use the provided Visual Studio solution file. The solution file references several project (*.vcxproj) files: NonMetricSpaceLib.vcxproj is the main project file that is used to build the library itself. The output is stored in the folder similarity_search\x64. Note that the core library, the test utilities, as well as examples of the standalone applications (projects sample_standalone_app1 and sample_standalone_app2) can be built without installing Boost.

A more detailed description of the build process on Windows is given in § 3.2.

3 Building and running the code (in detail)

A build process creates several important binaries, which include:

- The Non-Metric Space Library library (on Linux libNonMetricSpaceLib.a), which can be used in external applications;
- The main benchmarking utility experiment (experiment.exe on Windows) that carries out experiments and saves evaluation results;
- A tuning utility tune_vptree (tune_vptree.exe on Windows) that finds optimal VP-tree parameters (see § 5.1.1 and our paper for details [4]);
- A semi unit test utility bunit (bunit.exe on Windows);
- A utility bench_distfunc that carries out integration tests (bench_distfunc.exe on Windows);

A build process is different under Linux and Windows. In the following sections, we consider these differences in more detail.

3.1 Building under Linux

Implementation of similarity search methods is in the directory similarity_search. The code is built using a cmake, which works on top of the GNU make. Before creating the makefiles, we need to ensure that a right compiler is used. This is done by setting two environment variables: CXX and CC. In the case of GNU C++ (version 4.7), you need to type:

```
export CCX=g++-4.7 CC=gcc-4.7
```

In the case of the Intel compiler, you need to type:

```
export CXX=icc CC=icc
```

To create makefiles for a release version of the code, type:

```
cmake -DCMAKE_BUILD_TYPE=Release .
```

If you did not create any makefiles before, you can shortcut by typing:

cmake .

To create makefiles for a debug version of the code, type:

```
cmake -DCMAKE_BUILD_TYPE=Debug .
```

When makefiles are created, just type:

make

If cmake complains about the wrong version of the GCC, it is most likely that you forgot to set the environment variables CXX and CC (as described above). If this is the case, make these variables point to the correction version of the compiler. Important note: do not forget to delete the cmake cache file, before recreating the makefiles:

```
rm CMakeCache.txt
```

Also note that, for some reason, cmake may ignore environmental variables CXX and CC. Then, you can specify the compiler directly through cmake arguments. For example, in the case of the GNU C++ and the Release build, this can be done as follows:

```
cmake -DCMAKE_BUILD_TYPE=Release -DCMAKE_CXX_COMPILER=g++-4.7 \
-DCMAKE_GCC_COMPILER=gcc-4.7 CMAKE_CC_COMPILER=gcc-4.7 .
```

The build process creates several binaries. Most importantly, the main benchmarking utility experiment. The directory similarity_search/release contains release versions of these binaries. Debug versions are placed into the folder similarity_search/debug.

Important note: a shortcut command:

cmake

(re)-creates makefiles for the previously created build. When you type cmake . for the first time, it creates release makefiles. However, if you create debug makefiles and then type cmake ., this will not lead to creation of release makefiles!

To use the library in external applications, which do not belong to the library repository, one needs to install the library first. Assume that an installation location is the folder NonMetrLibRelease in the home directory. Then, the following commands do the trick:

```
cmake \
    -DCMAKE_INSTALL_PREFIX=$HOME/NonMetrLibRelease \
    -DCMAKE_BUILD_TYPE=Release .
make install
```

A directory sample_standalone_app contains two sample programs (see files sample_standalone_app1.cc and sample_standalone_app2.cc) that use the Non-Metric Space Library installed in the folder \$HOME/NonMetrLibRelease.

3.1.1 Developing and Debugging on Linux There are several debuggers that can be employed. Among them, some of the most popular are: gdb (a command line tool) and a ddd (a GUI wrapper for gdb). For users who prefer IDEs, one good option is Eclipse IDE for C/C++ developers. It is not the same as Eclipse for Java and one needs to download this version of Eclipse separately.

After downloading and decompressing, e.g. as follows:

```
tar -zxvf eclipse-cpp-europa-winter-linux-gtk-x86_64.tar.gz
```

one can simply run the binary eclipse (in a newly created directory eclipse). On the first start, Eclipse will ask you select a repository location. This would be the place to store the project metadata and (optionally) actual project source files

After selecting the workspace, the user can import the Eclipse project stored in the GitHub repository. Go to the menu File, sub-menu Import, category General and choose to import an existing project into the workspace as shown in Fig. 1. After that select a root directory. To this end, go to the directory where you checked out the contents of the GitHub repository and enter a sub-directory similarity_search. You should now be able to see the project Non-Metric-Space-Library as shown in Fig 2. You can now finalize the import by pressing the button Finish.

Next, we need to set some useful settings. Most importantly, we need to enable indexing of source files. This would allow us to browse class hierarchies, as well as find declarations of variables or classes. To this end, go to the menu Window, sub-menu Preferences and select a category C++/indexing (see Fig. 3). Then, check the box Index all files. Eclipse will start indexing your files with the progress being shown in the status bar (right down corner).

The user can also change the editor settings. We would strongly encourage to disable the use of tabs. Again, go the menu Window, sub-menu Preferences

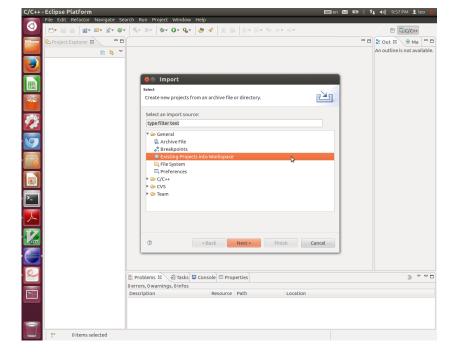


Fig. 1: Selecting an existing project to import

and select a category General/Editors/Text Editors. Then, check the box Insert spaces for tabs. In the same menu, you can also change the fonts (use the category General/Appearance/Colors and Fonts).

It is possible to build the project from Eclipse (see the menu Project). However, one first needs to generate makefiles as described in § 3.1. The current limitation is that you can build either release or the debug version at a time. Moreover, to switch from one version to another, you need to recreate the makefiles from the command line.

After building you can debug the project. To do this, you need to create a debug configuration. As an example, one configuration can be found in the project folder launches. Right click on the item sample.launch, choose the option Debug as (in the drop-down menu), and click on sample (in the pop-up menu). Note that you may need to edit command line arguments.

After switching to a debug perspective, the Eclipse may stop the debugger in the file dl-debug.c as shown in Fig. 5. If this happened, simply, press the continue icon a couple of times until the debugger enters the code belonging to the library.

Additional configurations can be created by right clicking on the project name (left pane), selecting Properties in the pop-up menu and clicking on Run/Debug settings. The respective screenshot is shown in Fig. 4.

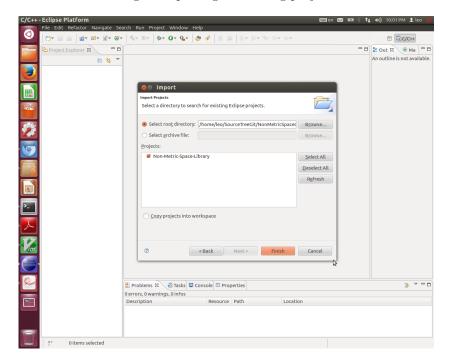


Fig. 2: Importing an existing project

Note that this manual contains only a basic introduction to Eclipse. If the user is new to Eclipse, we recommend reading additional documentation available online.

3.2 Building under Windows

It is straightforward to build the project using the provided Visual Studio solution file. The solution file references several (sub)-project (*.vcxproj) files, which can be built either separately or all together.

The main sub-project is NonMetricSpaceLib that is built before any other sub-projects. Two sub-projects: sample_standalone_app1, sample_standalone_app2 are examples of using the library in a standalone mode. Unlike building under Linux, we provide no installation procedure yet. In a nutshell, the installation consists in copying the library binary as well as the directory with header files.

There are three possible configurations for the binaries: Release, Debug, and RelWithDebInfo (release with debug information). The corresponding output files are placed into the subdirectories:

```
similarity_search\x64\Release,
similarity_search\x64\Debug,
similarity_search\x64\RelWithDebInfo.
```

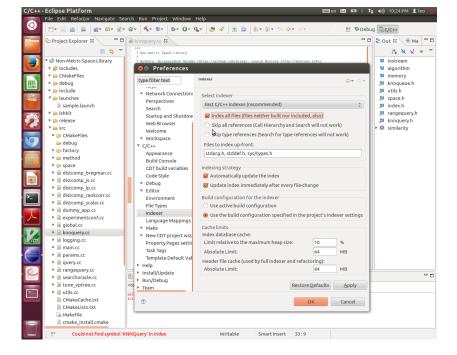


Fig. 3: Enabling indexing of the source code

If the user's CPU supports AVX extensions, it is recommended to modify code generation settings as shown in the screenshot in Fig. 6. This should be done for all sub-projects. Unlike other compilers, there seems to be no way to detect the CPU type in the Visual Studio automatically.⁶

The core library, the semi unit test binary as well as examples of the standalone applications can be built without installing Boost. However, Boost libraries are required for the binaries experiment and tune_vptree. The installer of the Boost libraries can be downloaded from this page. Note that one needs 64-bit binaries compiled with the same version of the Visual Studio as the Non-Metric Space Library binaries. For Visual Studio 12, one can use the following download link.

We recommend installing Boost into the folder c:\local\boost_1_55_0.64. Then, no modifications of the project settings are required. Should you install into a different folder, the location of Boost binaries and header file need to be specified in the project settings for all three build configurations (Release, Debug, RelWithDebInfo). An example of specifying the location of Boost libraries (binaries) is given in Fig. 7.

 $^{^{6}}$ It is not also possible to opt for using only SSE4.

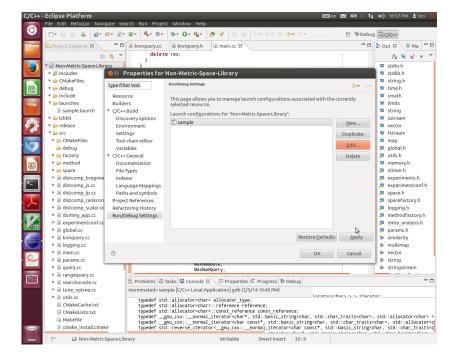


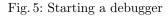
Fig. 4: Creating a debug/run configuration

3.3 Testing the Correctness of Implementations

We have two main testing utilities bunit and test_integr (experiment.exe and test_integr.exe on Windows). Both utilities accept the single optional argument: the name of the log file. If the log file is not specified, a lot of informational messages are printed to the screen.

The bunit verifies some basic functitionality akin to unit testing. In particular, it checks that an optimized version of, e.g., the Eucledian, distance returns results that are very similar to the results returned by unoptimized and simpler version. The utility bunit is expected to always run without errors.

The utility test_integr runs complete implementations of many methods and checks if several effectiveness and efficiency characteristics meet the expectations. The expectations are encoded as an array of instances of the class MethodTestCase (see the code here). For example, we expect that the recall (see § 3.5.2) fall in a certain pre-recorded range. Because almost all our methods are randomized, there is a great deal of variance in the observed performance characteristics. Thus, some tests may fail infrequently, if e.g., the actual recall value is slightly lower or higher than an expected minimum or maximum. From an error message, it should be clear if the discrepancy is substantial, i.e., something went wrong, or not, i.e., we observe an unlikely outcome due to randomization. The exact search method, however, should always have an almost perfect recall.



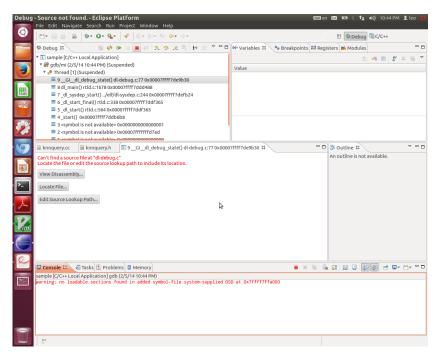
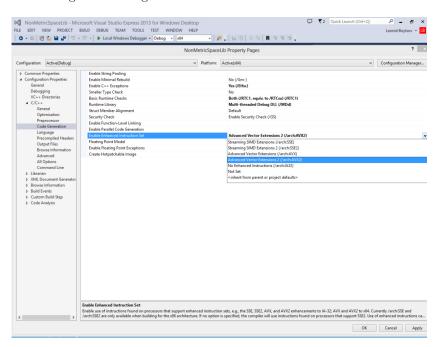


Fig. 6: Enabling SIMD Instructions in the Visual Studio



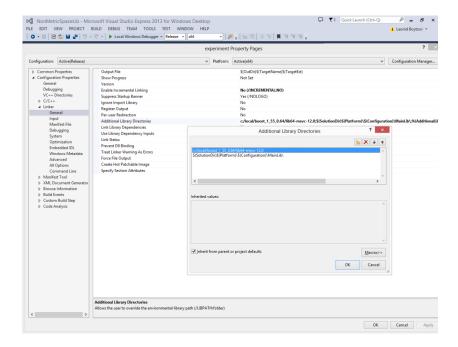


Fig. 7: Specifying Location of Boost libraries

3.4 Running Benchmarks

There are no major differences in benchmarking on Linux and Windows. There is a single benchmarking utility experiment (experiment.exe on Windows) that includes implementation of all methods. It has multiple options, which specify, among others, a space, a data set, a type of search, and a list of methods to test (with parameters). These options and their use cases are described in the following subsections.

3.4.1 Space and distance value type A distance function can return an integer (int), a single-precision (float), or a double-precision (double) real value. A type of the distance and its value is specified as follows:

```
-s [ --spaceType ] arg space type, e.g., 11, 12, lp:p=0.25 distance value type: int, float, double
```

A description of a space may contain parameters (parameters may not contain whitespaces). In this case, there is colon after the space mnemonic name followed by a comma-separated (not spaces) list of parameters in the format: $\operatorname{parameter}$ name>= $\operatorname{parameter}$ value>. Currently, this is used only for L_p spaces. For instance, 1p:0.5 denotes the space $L_{0.5}$. A detailed list of possible spaces and respective distance functions is given in Table 2 in \S 4.

For real-valued distance functions, one can use either single- or double-precision type. Single-precision is a recommended default.⁷ We do not have a space with integer-valued distance function yet, but we plan to implement an edit distance in the nearest future.

3.4.2 Input Data/Test Set There are three options that define the data to be indexed:

```
-i [ --dataFile ] arg input data file
--maxNumData arg (=0) if non-zero, only the first
maxNumData elements are used
-d [ --dimension ] arg (=0) optional dimensionality
```

The input file can be indexed either completely, or partially. In the latter case, the user can create the index using only the first --maxNumData elements. In the case of vector-space data, the dimensionality is determined by the number of columns in the data file. The user may choose to restrict the dimensionality and use only the first --dimension columns.

For testing, the user can use a separate test set. It is, again, possible to limit the number of queries:

If a separate test set is not available, it can be simulated by bootstrapping. To this, end the --maxNumData elements of the original data set are randomly divided into testing and indexable sets. The number of queries in this case is defined by the option --maxNumQuery. A number of bootstrap iterations is specified through an option:

```
-b [ --testSetQty ] arg (=0) # of sets created by bootstrapping;
```

Benchmarking can be carried out in either a single- or a multi-threaded mode. The number of test threads are specified as follows:

```
--threadTestQty arg (=1) # of threads
```

3.4.3 Query Type Our framework supports the k-NN and the range search. The user can request to run both types of queries:

```
-k [ --knn ] arg comma-separated values of k for the k-NN search comma-separated radii for range search
```

⁷ It is not clear yet, if having double-precision distance functions is essential. Yet, we decided to keep them. Thanks to C++ templates, it requires very little additional effort.

For example, by specifying the options

```
--knn 1,10 --range 0.01,0.1,1
```

the user requests to run queries of five different types: 1-NN, 10-NN, as well three range queries with radii 0.01, 0.1, and 1.

3.4.4 Methods The following is an option to specify search methods:

```
-m [ --method ] arg list of method(s) with parameters
```

Methods, similar to spaces, accept parameters (parameters may not contain whitespaces). In this case, the name of the method is followed by a colon and a comma-separated list (no-spaces) of parameters in the format: cparameter name>=cparameter value>. For a detailed list of methods and their parameters, please, refer to § 5.

3.4.5 Saving and Processing Benchmark Results The benchmarking utility outputs a detailed report (including all the log entries) to the screen (we plan to improve logging in the nearest future). To save benchmarking results to a file, on needs to specify a parameter:

```
-o [ --outFilePrefix ] arg output file prefix
```

In fact, we create two files: a human-readable report (suffix .rep) and a tabseparated data file (suffix .data). By default, the benchmarking utility creates files from scratch. The following option can be used to make it work in the append mode:

```
--appendToResFile arg (=0) append mode flag
```

For information on processing and interpreting results see \S 3.5. A description of the plotting utility is given in \S 3.7.

Finally, one can redirect the output of the benchmarking utility to a log-file:

The default behavior is to send all messages to the standard error stream.

3.4.6 Efficiency of Testing Except for measuring methods' performance, two expensive operations are computing ground truth answers and indexing. Currently, we recompute ground truth data every time we benchmark, which may take long time. However, substantial time savings can be achieved by benchmarking several methods using a single invocation of the binary experiment. In this case, ground truth data is computed once for all tested methods. To do this one simply needs to provide several arguments --method with different method names and/or parameters.

The disadvantage, of course, is that the test binary experiment will use more memory (as it has to keep several indices), which limits the size of the data set that can be tested. In future versions, we plan to address this issue and to compute ground truth data before any experimentation begins (and save it to a file).

Additional time savings can be achieved by testing copies of the same method that differ only in one or more *query time* parameter. In this case, we do not need to recreate the index before each new test, but rather just change query time parameters.

There are couple of gotchas here. First, all method descriptions (parameter --method) that correspond to the same method should be adjacent in the command line. Second, one needs to explicitly specify all default values. Currently, (though this needs to be fixed in the future) the main benchmarking utility knows nothing about the default parameter values and cannot, therefore, set them. If a default parameter is omitted, the system simply uses an arbitrary explicitly specified value of the parameter.

In particular, for the list of clusters method § 5.1.4, specifying the default value (2147483647) for the parameter maxLeavesToVisit is especially important as the method uses a different (a special exact search algorithm) when maxLeavesToVisit is equal to the default value.

3.5 Measuring Performance and Interpreting Results

3.5.1 Efficiency Three types of efficiency indicators are used: query runtime, the number of distance computations, and the amount of memory used by the index and the data. We also measure the improvement in runtime (improvement in efficiency) with respect to a single-thread sequential search (i.e., brute force) approach as well as an improvement in the number of distance computations. A good method should carry out fewer distance computations and be faster than the brute-force search, which compares all the objects directly with the query.

The amount of memory consumed by a search method is measured indirectly: We record the overall memory usage of a benchmarking process before and after creation of the index. Then, we add the amount of memory used by the data. On Linux, we query a special file /dev/cess id>/status, which might not work for all Linux distributives. Under Windows, we retrieve the working set size using the function GetProcessMemoryInfo. Note that we do not have a truly portable code to measure memory consumption of a process.

3.5.2 Effectiveness In the following description, we assume that a method returns a set of points/objects $\{o_i\}$. The value of $pos(o_i)$ represents a positional distance from o_i to the query, i.e., the number of database objects closer to the query than o_i plus one. Among objects with identical distances to the query, the object with the smallest index is considered to be the closest. Note that $pos(o_i) \geq i$.

Several effectiveness metrics are computed by the benchmarking utility:

- A number of points closer to the query than the nearest returned point. This metric is equal $pos(o_1)$ minus one. If o_1 is always the true nearest object, its positional distance is one and, thus, the number of points closer is always equal to zero.
- A relative position error for point o_i is equal to $pos(o_i)/i$, an aggregate value is obtained by computing the geometric mean over all returned o_i ;
- Recall, which is is equal to the fraction of all correct answers retrieved.
- Classification accuracy, which is equal to the fraction of labels correctly predicted by a k-NN based classification procedure.

The first two metrics represent a so-called rank (approximation) error. The closer the returned objects are to the query object, the better is the quality of the search response and the lower is the rank approximation error.

Recall is a classic metric. It was argued, however, that recall does not account for position information of returned objects and is, therefore, inferior to rank approximation error metrics [1,7].

If we specify ground-truth object classes (see \S 8 for the description of data set formats), it is possible to compute an accuracy of a k-NN based classification procedure. The label of an element is selected as the most frequent class label among k closest objects returned by the method (in the case of ties the class label with the smallest id is chosen).

If we had ground-truth queries and relevance judgements from human assessors, we could in principle compute other realistic effectiveness metrics such as the mean average precision, or the normalized discounted cumulative gain. This remains for the future work.

Note that it is pointless to compute the mean average precision when human judgments are not available, as the mean average precision is identical to the recall in this case.

Table 1: An example of a human-readable report

```
_____
vptree: triangle inequality
alphaLeft=2.0,alphaRight=2.0
_____
# of points: 9900
# of queries: 100
              0.954 \rightarrow [0.95 \ 0.96]
Recall:
ClassAccuracy: 0
                   -> [0 0]
RelPosError:
             1.05 -> [1.05 1.06]
NumCloser:
             0.11 \rightarrow [0.09 \ 0.12]
_____
QueryTime:
              0.2
                   -> [0.19 0.21]
DistComp:
              2991 -> [2827 3155]
ImprEfficiency: 2.37 -> [2.32 2.42]
ImprDistComp: 3.32 \rightarrow [3.32 \ 3.39]
Memory Usage:
             5.8 MB
```

Note: confidence intervals are in brackets

3.6 Interpreting and Processing Benchmark Results

If the user specifies the option —outFilePrefix, the benchmarking results are stored to the file system. A prefix of result files is defined by the parameter —outFilePrefix while the suffix is defined by a type of the search procedure (the k-NN or the range search) as well as by search parameters (e.g., the range search radius). For each type of search, two files are generated: a report in a human-readable format, and a tab-separated data file intended for automatic processing. The data file contains only the average values, which can be used to, e.g., produce efficiency-effectiveness plots as described in § 3.7.

An example of human readable report (confidence intervals are in square brackets) is given in Table 1. In addition to averages, the human-readable report provides 95% confidence intervals. In the case of bootstrapping, statistics collected for several splits of the data set are aggregated. For the retrieval time and the number of distance computations, this is done via a classic fixed-effect model adopted in meta analysis [20]. When dealing with other performance metrics, we employ a simplistic approach of averaging split-specific values and computing the sample variance over spit-specific averages. Note for all metrics, except relative position error, an average is computed using an arithmetic mean. For the relative error, however, we use the geometric mean [22].

3.7 Plotting results

We provide the Python script to generate performance graphs from tab-separated data file produced by the benchmarking utility experiment. The plotting script is genplot.py. In addition to Python, it requires Latex and PGF. This script is supposed to run only on Linux.

Consider the following example of using genplot.py:

```
../sample_scripts/genplot.py \
    -i result_K\=1.dat -o plot_1nn \
    -x 1~norm~Recall \
    -y 1~log~ImprEfficiency \
    -1 "2~(0.96,-.2)" \
    -t "ImprEfficiency vs Recall"
```

It aims to process the tab-separated data file result_K=1.dat, which was generated for 1-NN search, and save the plot to the file plot_1nn.pdf. Note that one should not explicitly specify the extension of the output file (as .pdf is always implied).

Parameters -x and -y define X and Y axis. Parameter values have the same format. Each parameter has three tilda-separated values. The first should be 0 or 1. Specify 0, only if you do not want to print the axis label. The second value is

⁸ The distribution of many metric values is not normal. There are approaches to resolve this issue (e.g., apply a transformation), but an additional investigation is needed to understand which approaches work best.

either norm or log, which stands for a normal or logarithmic scale, respectively. The last value defines a metric that we want to visualize: The metric should be one of the names that appear in the header row of the output data file. The title of the plot is defind by -t (specify -t "" if you do not want to print the title).

The parameter -1 defines a plot legend. It is either a string none (to hide the legend) or it contains two tilda-separated values. The first value gives the number of columns in the legend, while the second value defines a position of the legend. The position can be either absolute or relative. An absolute position is defined by a pair of coordinates (in round brackets). A relative position is defined by one of the following descriptors (quotes are for clarity only): "north west", "north east", "south west", "south east". If the relative position is specified, the legend is printed inside the main plotting area, e.g.:

```
../sample_scripts/genplot.py \
    -i result_K\=1.dat -o plot_1nn \
    -x 1~norm~Recall \
    -y 1~log~ImprEfficiency \
    -l "2~north west" \
    -t "ImprEfficiency vs Recall"
```

4 Spaces

Currently we provide implementations only for vector spaces, but this is not a principal limitation. The input files can come in either regular, i.e., dense, or sparse variant (see § 8).

A detailed list of spaces, their parameters, and performance characteristics is given in Table 2. The mnemonic name of the space is passed to the benchmarking utility (see \S 3.4). There can be more than one version of a distance function, which have different space-performance trade-off. In particular, for distances that require computation of logarithms we can achieve an order of magnitude improvement (e.g., for the GNU C++ and Clang) by pre-computing logarithms at index time. This comes at a price of extra storage. In the case of Jensen-Shannon distance functions, we can pre-compute some of the logarithms and accurately approximate those we cannot pre-compute. The details are explained in \S 4.1-4.4.

Straightforward slow implementations of the distance functions may have the substring slow in their names, while faster versions contain the substring fast. Fast functions that involve approximate computations contain additionally the substring approx. For non-symmetric distance function, a space may have two variants: one variant is for left queries (the data object is the first, i.e., left, argument of the distance function while the query object is the second argument) and another is for right queries (the data object is the second argument and the query object is the first argument). In the latter case the name of the space ends on rq. Separating spaces by query types, might not be the best approach. Yet, it seems to be unavoidable, because, in many cases, we need separate indices to support left and right queries [7].

Distance computation efficiency was evaluated on a Core i7 laptop (3.4 Ghz peak frequency) in a single-threaded mode (by the utility bench_distfunc). It is measured in millions of computations per second for single-precision floating pointer numbers (double precision computations are, of course, more costly). The code was compiled using the GNU compiler. Somewhat higher efficiency numbers can be obtained by using the Intel compiler or the Visual Studio (Clang seems to be equally efficient). In fact, performance is much better for distances relying on "heavy" math functions: slow versions of KL- and Jensen-Shannon divergences and Jensen-Shannon metrics, as well as for L_p spaces, where $p \notin \{1, 2, \infty\}$.

In the efficiency test, all dense vectors have 128 elements. For all dense-vector distances except the Jensen-Shannon divergence, their elements were generated randomly and uniformly. For the Jensen-Shannon divergence, we first generate elements randomly, and next we randomly select elements that are set to zero (approximately half). Additionally, for KL-divergences and the JS-divergence, we normalize vector elements so that they correspond a true discrete probability distribution.

Sparse space distances were tested using sparse vectors from two sample files in the sample_data directory. Sparse vectors in the first and the second file on average contain about 100 and 600 non-zero elements, respectively.

4.1 L_p -norms

The L_p distance between vectors x and y are given by the formula:

$$L_p(x,y) = \left(\sum_{i=1}^n |x_i - y_i|^p\right)^{1/p} \tag{1}$$

In the limit $(p \to \infty)$, the L_p distance becomes the Maximum metric, also known as the Chebyshev distance:

$$L_{\infty}(x,y) = \max_{i=1}^{n} |x_i - y_i| \tag{2}$$

 L_{∞} and all spaces L_p for $p \geq 1$ are true metrics. They are symmetric, equal to zero only for identical elements, and, most importantly, satisfy the triangle inequality. However, the L_p norm is not a metric if p < 1.

In the case of dense vectors, we have reasonably efficient implementations for L_p distances where p is either integer or infinity. The most efficient implementations are for L_1 (Manhattan), L_2 (Euclidean), and L_{∞} (Chebyshev). As explained in the author's blog, we compute exponents through square rooting. This works best when the number of digits (after the binary digit) is small, e.g., if p = 0.125.

Any L_p space can have a dense and a sparse variant. Sparse vector spaces have their own mnemonic names, which are different from dense-space mnemonic names in that they contain a suffix $_$ sparse (see also Table 2). For instance 11 and 11 $_$ sparse are both L_1 spaces, but the former is dense and the latter is

Table 2: Description of implemented spaces

| Space | Mnemonic Name & Formula | Efficiency (million op/sec) |
|----------------------------|---|-----------------------------|
| | Metric Spaces | |
| Hamming | bit_hamming $\sum_{i=1}^n x_i-y_i $ | 240 |
| L_1 | 11, 11_sparse $\sum_{i=1}^n x_i-y_i $ | 35, 1.6 |
| L_2 | 12, 12_sparse $\sqrt{\sum_{i=1}^n x_i-y_i ^2}$ | 30, 1.6 |
| L_{∞} | $	ext{linf}, 	ext{linf_sparse} \ 	ext{max}_{i=1}^n x_i - y_i $ | 34 , 1.6 |
| L_p (generic $p \ge 1$) | $	ext{lp:p=, lp_sparse:p=} \ \left(\sum_{i=1}^n x_i-y_i ^p ight)^{1/p}$ | 0.1-3, 0.1-1.2 |
| Angular distance | angulardist, angulardist_sparse, angulardist_sparse_fast $\arccos\left(1-\frac{\sum_{i=1}^n x_i y_i}{\sqrt{\sum_{i=1}^n x_i^2}\sqrt{\sum_{i=1}^n y_i^2}}\right)$ | 13, 1.4, 3.5 |
| Jensen-Shan. metr. | jsmetrslow, jsmetrfast, jsmetrfastapprox $\sqrt{\frac{1}{2}\sum_{i=1}^{n}\left[x_{i}\log x_{i}+y_{i}\log y_{i}-(x_{i}+y_{i})\log\frac{x_{i}+y_{i}}{2}\right]}$ | 0.3, 1.9, 4.8 |
| | Non-metric spaces (symmetric distance) | |
| L_p (generic $p < 1$) | lp:p=, lp_sparse:p= $\left(\sum_{i=1}^n x_i-y_i ^p\right)^{1/p}$ | 0.1-3, 0.1-1 |
| Jensen-Shan. div. | jsdivslow, jsdivfast, jsdivfastapprox $rac{1}{2}\sum_{i=1}^n \left[x_i\log x_i + y_i\log y_i - (x_i+y_i)\lograc{x_i+y_i}{2} ight]$ | 0.3, 1.9, 4.8 |
| Cosine similarity | $ \begin{array}{l} \text{cosinesimil, cosinesimil_sparse, cosinesimil_sparse_fast} \\ 1 - \frac{\sum_{i=1}^n x_i y_i}{\sqrt{\sum_{i=1}^n x_i^2} \sqrt{\sum_{i=1}^n y_i^2}} \end{array} $ | 13, 1.4, 3.5 |
| | Non-metric spaces (non-symmetric distance) | |
| Regular KL-div. | left queries: kldivfast right queries: kldivfastrq $\sum_{i=1}^n x_i \log \frac{x_i}{y_i}$ | 0.5, 27 |
| Generalized KL-div. | left queries: kldivgenslow, kldivgenfast right queries: kldivgenfastrq $\sum_{i=1}^{n} \left[x_i \log \frac{x_i}{y_i} - x_i + y_i \right]$ | 0.5, 27 27 |
| Itakura-Saito | left queries: itakurasaitoslow, itakurasaitofast right queries: itakurasaitofastrq $\sum_{i=1}^n \left[\frac{x_i}{y_i} - \log \frac{x_i}{y_i} - 1\right]$ | 0.2, 3, 14 14 |

sparse. The mnemonic names of L_1 , L_2 , and L_{∞} spaces (passed to the benchmarking utility) are 11, 12, and linf, respectively. Other generic L_p have the name 1p, which is used in combination with a parameter. For instance, L_3 is denoted as 1p:p=3.

Distance functions for sparse-vector spaces are far less efficient, due to a costly, branch-heavy, operation of matching sparse vector indices (between two sparse vectors).

4.2 Scalar-product Related Distances

We have two distance function whose formulas include normalized scalar product. One is the cosine similarity, which is equal to:

$$d(x,y) = 1 - \frac{\sum_{i=1}^{n} x_i y_i}{\sqrt{\sum_{i=1}^{n} x_i^2} \sqrt{\sum_{i=1}^{n} y_i^2}}$$

The cosine similarity is not a true metric, but it can be converted into one by applying a monotonic transformation (i.e., taking an inverse cosine). The resulting distance function is a true metric that is called the angular distance. The angular distance is computed using the following formula:

$$d(x,y) = \arccos\left(1 - \frac{\sum_{i=1}^{n} x_i y_i}{\sqrt{\sum_{i=1}^{n} x_i^2} \sqrt{\sum_{i=1}^{n} y_i^2}}\right)$$

In the case of sparse spaces, to compute the scalar product, we need to obtain an intersection of vector element ids corresponding to non-zero elements. A classic text-book intersection algorithm (akin to a merge-sort) is not particularly efficient, apparently, due to frequent branching. For single-precision floating point vector elements, we provide a more efficient implementation that relies on the all-against-all comparison SIMD instruction <code>_mm_cmpistrm</code>. This implementation (inspired by the set intersection algorithm of Schlegel et al. [28]) is about 2.5-3 times faster than a pure C++ implementation based on the merge-sort approach.

4.3 Jensen-Shannon divergence

Jensen-Shannon divergence is a symmetrized and smoothed KL-divergence:

$$\frac{1}{2} \sum_{i=1}^{n} \left[x_i \log x_i + y_i \log y_i - (x_i + y_i) \log \frac{x_i + y_i}{2} \right]$$
 (3)

This divergence is symmetric, but it is not a metric function. However, the square root of the Jensen-Shannon divergence is a proper a metric [15], which we call the Jensen-Shannon metric.

A straightforward implementation of Eq. 3 is inefficient for two reasons (at least when one uses the GNU C++ compiler) (1) computation of logarithms is a

slow operation (2) the case of zero x_i and/or y_i requires conditional processing, i.e., costly branches.

A better method is to pre-compute logarithms of data at index time. It is also necessary to compute logarithms of a query vector. However, this operation has a little cost since it is carried out once for each nearest neighbor or range query. Pre-computation leads to a 3-10 fold improvement depending on the sparsity of vectors, albeit at the expense of requiring twice as much space. Unfortunately, it is not possible to avoid computation of the third logarithm: it needs to be computed in points that are not known until we see the query vector.

However, it is possible to approximate it with a very good precision, which should be sufficient for the purpose of approximate searching. Let us rewrite Equation 3 as follows:

$$\frac{1}{2} \sum_{i=1}^{n} \left[x_i \log x_i + y_i \log y_i - (x_i + y_i) \log \frac{x_i + y_i}{2} \right] =$$

$$= \frac{1}{2} \sum_{i=1}^{n} \left[x_i \log x_i + y_i \log y_i \right] - \sum_{i=1}^{n} \left[\frac{(x_i + y_i)}{2} \log \frac{x_i + y_i}{2} \right] =$$

$$= \frac{1}{2} \sum_{i=1}^{n} x_i \log x_i + y_i \log y_i -$$

$$\sum_{i=1}^{n} \frac{(x_i + y_i)}{2} \left[\log \frac{1}{2} + \log \max(x_i, y_i) + \log \left(1 + \frac{\min(x_i, y_i)}{\max(x_i, y_i)} \right) \right] \tag{4}$$

We can pre-compute all the logarithms in Eq. 4 except for $\log\left(1 + \frac{\min(x_i, y_i)}{\max(x_i, y_i)}\right)$. However, its argument value is in a small range: from one to two. We can discretize the range, compute logarithms in many intermediate points and save the computed values in a table. Finally, we employ the SIMD instructions to implement this approach. As our tests show, this is a very efficient approach, which results in a very little (around 10^{-6} on average) relative error for the value of the Jensen-Shannon divergence.

Another possible approach is use an efficient approximation for logarithm computation. However, as our tests show, this method is still relatively slow (it takes almost 20 CPU cycles per log), while the relative error is as high as $3 \cdot 10^{-4}$ for logarithm arguments smaller than 2.

4.4 Bregman Divergences

Bregman divergences are typically non-metric distance functions, which are equal to a difference between some convex differentiable function f and its first-order Taylor expansion [6,7]. More formally, given the convex and differentiable function f (of many variables), its corresponding Bregman divergence $d_f(x,y)$ is equal to:

$$d_f(x,y) = f(x) - f(y) - (f(y) \cdot (x - y))$$

where $x \cdot y$ denotes the scalar product of vectors x and y. In this library, we implement the generalized KL-divergence and the Itakura-Saito divergence, which correspond to functions $f = \sum x_i \log x_i - \sum x_i$ and $f = -\sum \log x_i$. The generalized KL-divergence is equal to:

$$\sum_{i=1}^{n} \left[x_i \log \frac{x_i}{y_i} - x_i + y_i \right],$$

while the Itakura-Saito divergence is equal to:

$$\sum_{i=1}^{n} \left[\frac{x_i}{y_i} - \log \frac{x_i}{y_i} - 1 \right].$$

If vectors x and y are proper probability distributions, $\sum x_i = \sum y_i = 1$. In this case, the generalized KL-divergence becomes a regular KL-divergence:

$$\sum_{i=1}^{n} \left[x_i \log \frac{x_i}{y_i} \right].$$

Computing logarithms is costly: We can considerably improve efficiency of Itakura-Saito divergence and KL-divergence by pre-computing logarithms at index time. The spaces that implement this functionality contain the substring fast in their mnemonic names (see also Table 2).

5 Search Methods

Implemented search methods can be broadly divided into the following categories:

- Space partitioning methods (including a specialized method bbtree for Bregman divergences) § 5.1;
- Locality Sensitive Hashing (LSH) methods § 5.2;
- Filtering methods based on permutations § 5.3;
- Miscellaneous methods \S 5.4, which also include a k-NN graph implementation \S 5.4.1;

In the following subsections (§ 5.1-5.4), we describe implemented methods, explain their parameters, and provide examples of their use via the benchmarking utility experiment (experiment.exe on Windows). Note that a few parameters are query time parameters, which means that they can be changed without rebuilding the index see § 3.4.6. For the description of the utility experiment see § 3.4.

5.1 Space Partitioning Methods

Parameters of space partitioning methods are summarized in Table 3. Most of these methods are hierarchical partitioning methods.

Hierarchical space partitioning methods create a hierarchical decomposition of the space (often in a recursive fashion), which is best represented by a tree (or a forest). There are two main partitioning approaches: pivoting and compact partitioning schemes [11].

Pivoting methods rely on embedding into a vector space where vector elements are distances from the object to pivots. Partitioning is based on how far (or close) the data points are located with respect to pivots. 9

Hierarchical partitions produced by pivoting methods lack locality: a single partition can contain not-so-close data points. In contrast, compact partitioning schemes exploit locality. They either divide the data into clusters or create, possibly approximate, Voronoi partitions. In the latter case, for example, we can select several centers/pivots π_i and associate data points with the closest center.

If the current partition contains fewer than bucketSize (a method parameter) elements, we stop partitioning of the space and place all elements belonging to the current partition into a single bucket. If, in addition, the value of the parameter chunkBucket is set to one, we allocate a new chunk of memory that contains a copy of all bucket vectors. This method often halves retrieval time at the expense of extra memory consumed by a testing utility (e.g., experiment) as it does not deallocate memory occupied by the original vectors. ¹⁰

Classic hierarchical space partitioning methods are exact. It is possible to make them approximate via an early termination technique, where we terminate the search after exploring a pre-specified number of partitions. To implement this strategy, we define an order of visiting partitions. In the case of clustering methods, we first visit partitions that are closer to a query point. In the case of hierarchical space partitioning methods such as the VP-tree, we greedily explore partitions containing the query.

In the Non-Metric Space Library, the early termination condition is defined in terms of the maximum number of buckets (parameter maxLeavesToVisit) to visit before terminating the search procedure. By default, the parameter maxLeavesToVisit is set to a large number (2147483647), which means that no early termination is employed.

5.1.1 VP-tree A VP-tree [32,34] (also known as a ball-tree) is a pivoting method. During indexing, a (random) pivot is selected and a set of data objects is divided into two parts based on the distance to the pivot. If the distance

⁹ If the original space is metric, mapping an object to a vector of distances to pivots defines the contractive embedding in the metric spaces with L_{∞} distance. That is, the L_{∞} distance in the target vector space is a lower bound for the original distance.

¹⁰ Keeping original vectors simplifies the testing workflow. However, this is not necessary for a real production system. Hence, storing bucket vectors at contiguous memory locations does not have to result in a larger memory footprint.

is smaller than the median distance, the objects are placed into one (inner) partition. If the distance is larger than the median, the objects are placed into the other (outer) partition. If the distance is exactly equal to the median, the placement can be arbitrary.

The VP-tree in metric spaces is an exact search method, which relies on the triangle inequality. It can be made approximate by applying the early termination strategy (as described in the previous subsection). Another approximate-search approach, which is currently implemented only for the VP-tree, is based on the relaxed version of the triangle inequality.

Assume that π is the pivot in the VP-tree, q is the query with the radius r, and R is the median distance from π to every other data point. Due to the triangle inequality, pruning is possible only if $r \leq |R - d(\pi, q)|$. If this latter condition is true, we visit only one partition that contains the query point. If $r > |R - d(\pi, q)|$, there is no guarantee that all answers are in the same partition as q. Thus, to guarantee retrieval of all answers, we need to visit both partitions.

The pruning condition based on the triangle inequality can be overly pessimistic. By selecting some $\alpha>1$ and opting to prune when $r\leq \alpha|R-d(\pi,q)|$, we can improve search performance at the expense of missing some valid answers. The efficiency-effectiveness trade-off is affected by the choice of α : Note that for some (especially low-dimensional) data sets, a modest loss in recall (e.g., by 1-5%) can lead to an order of magnitude faster retrieval. Not only the triangle inequality can be overly pessimistic in metric spaces, but it often fails to capture the geometry of non-metric spaces. As a result, if the metric space method is applied to a non-metric space, the recall can be too low or retrieval time can be too long.

Yet, in non-metric spaces, it is often possible to answer queries, when using α possibly smaller than one [4]. In this version, we would use different α for different partitions. More generally, we assume that there exists an unknown decision/pruning function $D(R,d(\pi,q))$ and that pruning is done when $r \leq D(R,d(\pi,q))$. The decision function D(), which can be learned from data, is called a search oracle. A pruning algorithm based on the triangle inequality is a special case of the search oracle described by the formula:

$$D_{\pi,R}(x) = \begin{cases} \alpha_{left}|x - R|, & \text{if } x \le R\\ \alpha_{right}|x - R|, & \text{if } x \ge R \end{cases}$$
 (5)

Optimal α_{left} and α_{right} are determined by the utility tune_vptree (via a grid search).¹¹ The user can specify values of α_{left} and α_{right} via parameters alphaLeft and alphaRight, respectively. It is possible to implement new search oracles and plug them into the implementation of the VP-tree.

The following is an example of testing the VP-tree with the benchmarking utility experiment:

release/experiment \

¹¹ To this end, we index a small subset of the data points and seek to obtain parameters that give the shortest retrieval time at a specified recall threshold.

```
--distType float --spaceType 12 --testSetQty 5 --maxNumQuery 100 \
--knn 1 --range 0.1 \
--dataFile ../sample_data/final8_10K.txt --outFilePrefix result \
--method vptree:alphaLeft=2.0,alphaRight=2.0,maxLeavesToVisit=500,\
bucketSize=10,chunkBucket=1
```

5.1.2 Multi-Vantage Point Tree It is possible to have more than one pivot per tree level. In the binary version of the multi-vantage point tree (MVP-tree), which is implemented in Non-Metric Space Library, there are two pivots. Thus, each partition divides the space into four parts, which are similar to partitions created by two levels of the VP-tree. The difference is that the VP-tree employs three pivots to divide the space into four parts, while in the MVP-tree two pivots are used.

In addition, in the MVP-tree we memorize distances between a data object and the first maxPathLen (method parameter) pivots on the path connecting the root and the leaf that stores this data object. Because mapping an object to a vector of distances (to maxPathLen pivots) defines the contractive embedding in the metric spaces with L_{∞} distance, these values can be used to improve the filtering capacity of the MVP-tree and, consequently to reduce the number of distance computations.

The following is an example of testing the MVP-tree with the benchmarking utility experiment:

Our implementation of the MVP-tree permits to answer queries both exactly and approximately (by specifying the parameter maxLeavesToVisit). Yet, this implementation should be used only with metric spaces.

5.1.3 GH-Tree A GH-tree [32] is a binary tree. In each node the data set is divided using two randomly selected pivots. Elements closer to one pivot are placed into a left subtree, while elements closer to the second pivot are placed into a right subtree.

The following is an example of testing the GH-tree with the benchmarking utility experiment:

Our implementation of the GH-tree permits to answer queries both exactly and approximately (by specifying the parameter maxLeavesToVisit). Yet, this implementation should be used only with metric spaces.

5.1.4 List of Clusters The list of clusters [10] is an exact search method for metric spaces, which relies on flat (i.e., non-hierarchical) clustering. Clusters are created sequentially starting by randomly selecting the first cluster center. Then, close points are assigned to the cluster and the clustering procedure is applied to the remaining points. Closeness is defined either in terms of the maximum radius, or in terms of the maximum number (bucketSize) of points closest to the center.

Next we select cluster centers according to one of the policies: random selection, a point closest to the previous center, a point farthest from the previous center, a point that minimizes the sum of distances to the previous center, and a point that maximizes the sum of distances to the previous center. In our experience, a random selection strategy (a default one) works well in most cases.

The search algorithm iterates over the constructed list of clusters and checks if answers can potentially belong to the currently selected cluster (using the triangle inequality). If the cluster can contain an answer, each cluster element is compared directly against the query. Next, we use the triangle inequality to verify if answers can be outside the current cluster. If this is not possible, the search is terminated.

We modified this exact algorithm by introducing an early termination condition. The clusters are visited in the order of increasing distance from the query to a cluster center. The search process stops after vising a maxLeavesToVisit clusters. Our version is supposed to work for metric spaces (and symmetric distance functions), but it can also be used with mildly-nonmetric symmetric distances such as the cosine similarity.

An example of testing the list of clusters using the bucketSize as a parameter to define the size of the cluster:

An example of testing the list of clusters using the radius as a parameter to define the size of the cluster:

5.1.5 SA-tree The Spatial Approximation tree (SA-tree) [27] aims to approximate the Voronoi partitioning. A data set is recursively divided by selecting several cluster centers in a greedy fashion. Then, all remaining data points are assigned to the closest cluster center.

A cluster-selection procedure first randomly chooses the main center point and arranges the remaining objects in the order of increasing distances to this center. It then iteratively fills the set of clusters as follows: We start from the empty cluster list. Then, we iterate over the set of data points and check if there is a cluster center that is closer to this point than the main center point. If no such cluster exists (i.e., the point is closer to the main center point than to any of the already selected cluster centers), the point becomes a new cluster center (and is added to the list of clusters). Otherwise, the point is added to the nearest cluster from the list.

After the cluster centers are selected, each of them is indexed recursively using the already described algorithm. Before this, however, we check if there are points that need to be reassigned to a different cluster. Indeed, because the list of clusters keeps growing, we may miss the nearest cluster not yet added to the list. To fix this, we need to compute distances among every cluster point and cluster centers that were not selected at the moment of the point's assignment to the cluster.

Currently, the SA-tree is an exact search method for metric spaces without any parameters. The following is an example of testing the SA-tree with the benchmarking utility experiment:

```
release/experiment \
  --distType float --spaceType 12 --testSetQty 5 --maxNumQuery 100 \
  --knn 1 --range 0.1 \
  --dataFile ../sample_data/final8_10K.txt --outFilePrefix result \
  --method satree
```

5.1.6 bbtree A Bregman ball tree (bbtree) is an exact search method for Bregman divergences [7]. The bbtree divides data into two clusters (each covered by a Bregman ball) and recursively repeats this procedure for each cluster until the number of data points in a cluster falls below **bucketSize**. Then, such clusters are stored as a single bucket.

At search time, the method relies on properties of Bregman divergences to compute the shortest distance to a covering ball. This is a rather expensive iterative procedure that may require several computations of direct and inverse gradients, as well as of several distances.

Additionally, Cayton [7] employed an early termination method: The algorithm can be told to stop after processing a maxLeavesToVisit buckets. The resulting method is an approximate search procedure.

Our implementation of the bbtree uses the same code to carry out the nearest-neighbor and the range searching. Such an implementation of the range searching is somewhat suboptimal and a better approach exists [8].

The following is an example of testing the bbtree with the benchmarking utility experiment:

```
release/experiment \
   --distType float --spaceType kldivgenfast \
   --testSetQty 5 --maxNumQuery 100 \
   --knn 1 --range 0.1 \
   --dataFile ../sample_data/final8_10K.txt --outFilePrefix result \
   --method bbtree:maxLeavesToVisit=20,bucketSize=10
```

5.2 Locality-sensitive Hashing Methods

Locality Sensitive Hashing (LSH) is a class of methods employing hash functions that tend to have the same hash values for close points and different hash values for distant points. It is a probabilistic method in which the probability of having the same hash value is a monotonically decreasing function of the distance between two points (that we compare). A hash function that possesses this property is called locality sensitive. The first LSH method was proposed by Indyk and Motwani in [21]. Our library embeds the LSHKIT which provides locality sensitive hash functions in L_1 and L_2 . It supports only the nearest-neighbor (but not the range) search. Parameters of LSH methods are summarized in Table 4.

Random projections is a common approach to design locality sensitive hash functions. These functions are composed from M binary hash functions $h_i(x)$. A concatenation of the binary hash function values, i.e., $h_1(x)h_2(x)\dots h_M(x)$, is interpreted as a binary representation of the hash function value h(x). Pointers to objects with equal hash values (modulo H) are stored in same cells of the hash table (of the size H). If we used only one hash table, the probability of collision for two similar objects would be too low. To increase the probability of finding a similar object multiple hash tables are used. In that, we use a separate (randomly selected) hash function for each hash table.

To generate binary hash functions we first select a parameter W (called a width). Next, for every binary hash function, we draw a value a_i from a p-stable distribution [12], and a value b_i from the uniform distribution with the support [0, W]. Finally, we define $h_i(x)$ as:

$$h_i(x) = \left| \frac{x \cdot v_i + a_i}{W} \right|,$$

where $\lfloor x \rfloor$ is the **floor** function and $x \cdot y$ denotes the scalar product of x and y. For the L_2 a standard Guassian distribution is p-stable, while for L_1 distance one can generate hash functions using a Cauchy distribution [12]. For L_1 , the LSHKIT defines another ("thresholding") approach based on sampling. It is supposed to work best for data points enclosed in a cube $[a, b]^d$. We omit the description here and refer the reader to the papers that introduced this method [33,24].

One serious drawback of the LSH is that it is memory-greedy. To reduce the number of hash tables while keeping the collision probability for similar objects sufficiently high, it was proposed to "multi-probe" the same hash table more than once. When we obtain the hash value h(x), we check (i.e., probe) not only the contents of the hash table cell h(x) mod H, but also contents of cells

whose binary codes are "close" to h(x) (i.e, they may differ by a small number of bits). The LSHKIT, which is embedded in our library, contains a state-of-the-art implementation of the multi-probe LSH that can automatically select optimal values for parameters M and W to achieve a desired recall (remaining parameters still need to be chosen manually).

The following is an example of testing the multi-probe LSH with the benchmarking utility experiment. We aim to achieve the recall value 0.25 (parameter desiredRecall) for the 1-NN search (parameter tuneK):

The classic version of the LSH for L_2 can be tested as follows:

```
release/experiment \
   --distType float --spaceType 12 --testSetQty 5 --maxNumQuery 100 \
   --knn 1 \
   --dataFile ../sample_data/final8_10K.txt --outFilePrefix result \
   --method lsh_gaussian:W=2,L=5,M=40,H=16535
```

There are two ways to use LSH for L_1 . First, we can invoke the implementation based on the Cauchy distribution:

```
release/experiment \
  --distType float --spaceType 11 --testSetQty 5 --maxNumQuery 100 \
  --knn 1 \
  --dataFile ../sample_data/final8_10K.txt --outFilePrefix result \
  --method lsh_cauchy:W=2,L=5,M=10,H=16535
```

Second, we can use L_1 implementation based on thresholding. Note that it does not use the width parameter W:

```
release/experiment \
   --distType float --spaceType l1 --testSetQty 5 --maxNumQuery 100 \
   --knn 1 \
   --dataFile ../sample_data/final8_10K.txt --outFilePrefix result \
   --method lsh_threshold:L=5,M=60,H=16535
```

5.3 Permutation-based Filtering Methods

Rather than relying on distance values directly, we can assess similarity of objects based on their relative distances to reference points (i.e., pivots). For each data point x, we can arrange pivots π in the order of increasing distances from x (for simplicity we assume that there are no ties). This arrangement is called a *permutation*. The permutation is essentially a vector whose i-th element keeps an (ordinal) position of the i-th pivot (in the set of pivots sorted by a distance from x).

Computation of the permutation is a mapping from a source vector space with real coordinates to a target vector space with integer coordinates. In our library, the distance between permutations is defined as either L_1 or L_2 . Values of the distance in the source space often correlates well with the distance in the target space of permutations. This property is exploited in permutation methods. An advantage of permutation methods is that they are not relying on metric properties of the original distance and can be successfully applied to non-metric spaces [4].

Note that there is no simple relationship between the distance in the target space and the distance in the source space. In particular, the distance in the target space is neither a lower nor an upper bound for the distance in the source space. Thus, methods based on indexing permutations are filtering methods that allow us to obtain only approximate solutions. In the first step, we retrieve a certain number of candidate points whose permutations are sufficiently close to the permutation of the query vector. For these candidate data points, we compute an actual distance to the query, using the original distance function. For almost all implemented permutation methods, the number of candidate records can be controlled by a parameter dbScanFrac or minCandidate.

Permutation methods differ in how they index and process permutations. In the following subsections, we briefly review implemented variants. Parameters of these methods are summarized in Tables 5-6.

5.3.1 Sequential permutation search In the sequential search (i.e., bruteforce) approach, we scan the list of permutation methods and compute the distance between the permutation of the query and a permutation of every data point. Then, we sort all data points in the order of increasing distance to the query permutation. A fraction (dbScanFrac) of data points is compared directly against the query. The mnemonic code of this method is permutation. Instead of computing the complete ordering of permutations, one can resort to incremental sorting [19]. The mnemonic code of this (faster) modification is perm_incsort.

The following is an example of testing the incremental-sort permutation method with the benchmarking utility experiment:

```
release/experiment \
   --distType float --spaceType 12 --testSetQty 5 --maxNumQuery 100 \
   --knn 1 --range 0.1 \
   --dataFile ../sample_data/final8_10K.txt --outFilePrefix result \
   --method perm_incsort:numPivot=4,dbScanFrac=0.2
```

5.3.2 Permutation Prefix Index (PP-Index) In a permutation prefix index (PP-index), permutation are stored in a prefix tree of limited depth [16]. A parameter prefixLength defines the depth. The filtering phase aims to find minCandidate candidate data points. To this end, it first retrieves the data points whose permutation prefix is exactly the same as that of the query. If we do not get enough candidate records, we shorten the prefix and repeat the pro-

cedure until we get a sufficient number of candidate entries. Note that we do not the use the parameter dbScanFrac here.

The following is an example of testing the PP-index with the benchmarking utility experiment.

```
release/experiment \
   --distType float --spaceType 12 --testSetQty 5 --maxNumQuery 100 \
   --knn 1 --range 0.1 \
   --dataFile ../sample_data/final8_10K.txt --outFilePrefix result \
   --method perm_prefix:numPivot=4,prefixLength=4,minCandidate=100
```

5.3.3 VP-tree index over permutations We can use a VP-tree to index permutations. This approach is similar to that of Figueroa and Fredriksson [17]. We, however, rely on the approximate version of the VP-tree described in § 5.1.1, while Figueroa and Fredriksson use an exact one. The "sloppiness" of the VP-tree search is governed by the stretching coefficients alphaLeft and alphaRight in Equation (5).

The following is an example of testing the VP-tree index over permutations with the benchmarking utility experiment.

```
release/experiment \
   --distType float --spaceType 12 --testSetQty 5 --maxNumQuery 100 \
   --knn 1 --range 0.1 \
   --dataFile ../sample_data/final8_10K.txt --outFilePrefix result \
   --method perm_vptree:numPivot=4,alphaLeft=2,alphaRight=2,dbScanFrac=0.05
```

5.3.4 Inverted index over permutations Another approach relies on the inverted index over permutations [2]. We select (a potentially large) subset of pivots (parameter numPivot). Using these pivots, we compute a permutation for every data point. Then, numPivotIndex most closest pivots are memorized in a data file. If a pivot number i is the pos-th most distant pivot for the object x, we add the pair (pos, x) to the posting list number i. All posting lists are kept sorted in the order of the increasing first element (equal to the ordinal position of the pivot in a permutation).

During searching, we compute the permutation of the query and select posting lists corresponding to numPivotSearch most closest pivots. These posting lists are processed as follows: Imagine that we selected posting list i and the position of pivot i in the permutation of the query is pos. Then, using the posting list i, we retrieve all candidate records for which the position of the pivot i in their respective permutations is from $pos - \max PosDiff$ to $pos + \max PosDiff$. This allows us to update the estimate for the L_1 distance between retrieved candidate records' permutations and the permutation of the query (see [2] for more details).

Finally, we select at most dbScanFrac $\cdot N$ objects (N is the total number of indexed objects) with the smallest estimates for the L_1 between their permutations and the permutation of the query. These objects are compared directly against the query.

An example of testing this method using the utility experiment is as follows:

5.3.5 Pivot neighborhood index Recently it was proposed to index pivot neighborhoods: For each data point, we select $numPrefix \ll numPivot$ pivots that are closest to the data point. Then, we associate these numPrefix closest pivots with the data point via an inverted file [31]. One can hope that for similar points two pivot neighborhoods will have a non-zero intersection.

To exploit this observation, our implementation of the pivot neighborhood indexing method retrieves all points that share at least minTimes nearest neighbor pivots (using an inverted file). Then, these candidates points are compared directly against the query.

Note that our implementation is different from that of Tellez [31] in several ways. First, we do not use a succinct inverted index. Second, we use a simple posting merging algorithm based on counting (a ScanCount algorithm). Before a query is processed, we zero-initialize an array that keeps one counter for every data point. As we traverse a posting list and encounter an entry corresponding to object i, we increment a counter number i. The ScanCount is known to be efficient [23].

We also divide the index in chunks each accounting for at most chunkIndexSize data points. The search algorithm processes one chunk at a time. The idea is to make a chunk sufficiently small so that counters fit into L1 or L2 cache.

An example of testing this method using the utility experiment is as follows:

5.3.6 Binarized permutation methods Instead of computing the L_2 distance between two permutations, we can binarize permutations and computed the Hamming distance between binarized permutations. To this end, we select an adhoc binarization threshold binThreshold. All integer values smaller than binThreshold become zeros, and values larger than or equal to binThreshold become ones.

On a plus side, the Hamming distance between binarized permutations can be computed much faster than L_2 or L_1 (see Table 2). This comes at a cost though, as the Hamming distance appears to be a worse proxy for the original distance than L_2 or L_1 .

The binarized permutation can be search sequentially. An example of testing such a method using the utility experiment is as follows:

Alternatively, binarized permutations can be indexed using the VP-tree. This approach is usually more efficient than searching binarized permutations sequentially, but one needs to tune additional parameters. An example of testing such a method using the utility experiment is as follows:

5.4 Miscellaneous Methods

Parameters of miscellaneous methods are summarized in Table 7.

5.4.1 k-NN graph One efficient and effective approach relies on a graph, where objects are graph nodes and edges connect sufficiently close objects. When edges connect mostly near neighbors, such graph is called a *k*-NN graph (or a nearest neighbor graph). This method implements only the nearest-neighbor, but not the range search.

A search process is a series of sub-searches with (the number of sub-searches is defined by the parameter <code>initSearchAttempts</code>). A sub-search starts at a random node and proceeds to expanding the set of traversed nodes by following neighboring links. The sub-search stops when we cannot find points that are closer than already found NN nearest points (NN is a search parameter). Note that the greedy search is only approximate and does not necessarily return all NN nearest neighbors.

Indexing is a bottom-up procedure that relies on the previously described greedy search algorithm. The number of restarts, though, is defined by a different parameter, i.e., initIndexAttempts. We add points one by one. For each data point, we find NN closest points using an already constructed index. Then, we create an edge between a new graph node (representing a new point) and nodes that represent NN closest points found by the greedy search. Empirically, it was shown that this method often creates a navigable small world graph, where most nodes are separated by only a few edges (roughly logarithmic in terms of the overall number of objects) [26].

The indexing algorithm is rather expensive and we accelerate it by running parallel searches in multiple threads. The number of threads is defined by the parameter <code>indexThreadQty</code>. The graph updates are synchronized: If a thread needs to add edges to a node or obtain the list of node edges, it first locks a node-specific mutex. Because different threads rarely update and/or access the same node simultaneously, such synchronization creates little contention and, consequently, our parallelization approach is efficient. It is also necessary to synchronize updates for the list of graph nodes, but this operation takes little time compared to searching for NN neighboring points.

An example of testing this method using the utility experiment is as follows:

5.4.2 Sequential searching The improvement in efficiency is measured with respect to a single-thread sequential search method. To verify how the speed of sequential searching scales with the number of threads, we provide a reference implementation of the sequential searching.

For example, to benchmark sequential searching using two threads, one can type the following command:

```
release/experiment \
   --distType float --spaceType 12 --testSetQty 5 --maxNumQuery 100 \
   --knn 1 \
   --dataFile ../sample_data/final8_10K.txt --outFilePrefix result \
   --method seq_search --threadTestQty 2
```

5.4.3 Several copies of the same index type It is possible to generate several copies of the same index using a meta method mult_indx. This makes sense for randomized indexing methods, e.g., for the VP-tree or the PP-index. ¹²

```
release/experiment \
  --distType float --spaceType 12 --testSetQty 5 --maxNumQuery 100 \
  --knn 1 \
  --dataFile ../sample_data/final8_10K.txt --outFilePrefix result \
  --method mult_index:methodName=vptree,indexQty=5,maxLeavesToVisit=2
```

¹² In fact, all of the methods except for the sequential, i.e., brute force, search are randomized.

6 Extending the code

It is possible to add new spaces and search methods. This is done in three steps, which we only outline here. A more detailed description can be found in \S 6.2 and \S 6.3.

In the first step, the user writes the code that implements a functionality of a method or a space. In the second step, the user writes a special helper file containing methods that creates a class or a method. In this helper file, it is normally necessary to include the method/space header. Please, use the **angle brackets** in this include-directive here.

Because we tend to give the helper file the same name as the name of header for a specific method/space, we should not include method/space headers using quotes. Such code fails to compile under the Visual Studio. Here is an example of a proper include-directive:

#include <method/vptree.h>

In the third step, the user adds the registration code to either the file init_spaces.h (for spaces) or to the file init_methods.h (for methods). This step has two sub-steps. First, the user includes the previously created helper file into either init_spaces.h or init_methods.h. Finally the function initMethods or initSpaces are extended by adding a macro call that actually registers the space or method in a factory class. No modification of makefiles (or other configuration files) is required.

Is is noteworthy that all implementations of methods and spaces are mostly template classes parameterized by the distance value type. Recall that the distance function can return an integer (int), a single-precision (float), or a double-precision (double) real value. The user may choose to provide specializations for all possible distance values or decide to focus, e.g., only on integer-valued distances.

The user can also add new applications, which are meant to be a part of the testing framework/library. However, adding new applications does require minor editing of the meta-makefile CMakeLists.txt (and re-running cmake § 3.1). It is also possible to create standalone applications that use the library. Please, see § 3.1 and § 3.2 for details.

In the following subsections, we consider extension tasks in more detail. For illustrative purposes, we created a zero-functionality space (DummySpace), method (DummyMethod), and application (dummy_app). These dummy classes can also be used as starting points to develop fully functional code.

6.1 Test Workflow

The main benchmarking utility **experiment** parses command line parameters. Then, it creates a space and all required search methods using the space and the method factories. Thus, when we create a class representing a search method, the constructor of this class has to create an index in the memory. Both search

method and spaces can have parameters, which are passed to the method/space in an instance of the class AnyParams. We consider this in detail in \S 6.2 and \S 6.3.

Depending on parameters, two test scenarios are possible. In the first scenario, the user specifies separate data and test files. In the second scenario, a test file is created by bootstrapping: The data set is randomly divided into training and a test set. Then, we call the function RunAll and subsequently Execute for all possible test sets.

The function Execute is a main workhorse, which creates queries, runs searches, produces ground truth data, and collects execution statistics. There are two types of queries: nearest-neighbor and range queries, which are represented by (template) classes RangeQuery and KNNQuery. Both classes inherit from the class Query. Similar to spaces, these template classes are parameterized by the type of the distance value.

Both types of queries are similar in that they implement the Radius function and the functions CheckAndAddToResult. In the case of the range query, the radius of a query is constant. However, in the case of the nearest-neighbor query, the radius typically decreases as we compare the query with previously unseen data objects (by calling the function CheckAndAddToResult). In both cases, the value of the function Radius is used to prune unpromising partitions and data points.

This commonality between the RangeQuery and KNNQuery allows us in many cases to carry out a nearest-neighbor query using an algorithm designed to answer range queries. Thus, only a single implementation of a search method—that answers queries of both types—can be used in many cases.

A query object proxies distance computations during the testing phase. Namely, the distance function is accessible through the function IndexTimeDistance, which is defined in the class Space. During the testing phase, a search method can compute a distance only by accessing functions Distance, DistanceObjLeft (for left queries) and DistanceObjRight for right queries, which are member functions of the class Query. The function Distance accepts two parameters (i.e., object pointers) and can be used to compare two arbitrary objects. The functions DistanceObjLeft and DistanceObjRight are used to compare data objects with the query. Note that it is a query object memorizes the number of distance computations. This allows us to compute the variance in the number of distance evaluations and, consequently, a respective confidence interval.

6.2 Creating a space

A space is a collection of data objects. In our library, objects are represented by instances of the class Object. The functionality of this class is limited to creating new objects and/or their copies as well providing access to the raw (i.e., unstructured) representation of the data (through functions data and datalength). We would re-iterate that currently (though this may change in the future releases), Object is a very basic class that only keeps a blob of data and blob's size. For example, the Object can store an array of single-precision floating point numbers,

but it has no function to obtain the number of elements. These are the spaces that are responsible for reading objects from files, interpreting the structure of the data blobs (stored in the Object), and computing a distance between two objects.

For dense vector spaces the easiest way to create a new space, is to create a functor (function object class) that computes a distance. Then, this function should be used to instantiate a template VectorSpaceGen. A sample implementation of this approach can be found in sample_standalone_app1.cc.

To further illustrate the process of developing a new space, we created a sample zero-functionality space <code>DummySpace</code>. It is represented by the header file space_dummy.h and the source file space_dummy.cc. The user is encouraged to study these files and read the comments. Here we focus only on the main aspects of creating a new space.

The sample files describe a template class DummySpace, which is declared and defined in the namespace similarity. It is a direct ancestor of the class Space:

It is possible to provide the complete implementation of the DummySpace in the header file. However, this would make compilation slower. Instead, we recommend to use the mechanism of explicit template instantiation. To this end, the user should instantiate the template in the source file for all possible combination of parameters. In our case, the <code>source</code> file space_dummy.cc contains the following lines:

```
template class SpaceDummy<int>;
template class SpaceDummy<float>;
template class SpaceDummy<double>;
```

Most importantly, the user needs to implement the function ReadDataset, which reads objects from a file, and the function HiddenDistance, which computes the distance between objects. For a sample implementation of ReadDataset, please, see the file space_bit_hamming.cc. Note that ReadDataset is supposed to read at most MaxNumObjects from the file. If the file has more objects, only the first maxNumData should be retrieved. The space is responsible for following this convention, the library does not enforce this behavior.

Remember that the function HiddenDistance should not be directly accessible by classes that are not friends of the Space. As explained in § 6.1, during the indexing phase, HiddenDistance is accessible through the function Space::IndexTimeDistance. During the testing phase, a search method can compute a distance only by accessing functions Distance, DistanceObjLeft, or DistanceObjRight, which are member functions of the Query.

Finally, we need to "tell" the library about the space, by registering the space in the space factory. At runtime, the space is created through a helper function. In our case, it is called CreateDummy. The function, accepts only one parameter, which is a reference to an object of the type AllParams:

```
template <typename dist_t>
Space<dist_t>* CreateDummy(const AnyParams& AllParams) {
   AnyParamManager pmgr(AllParams);
   int param1, param2;
   pmgr.GetParamRequired("param1", param1);
   pmgr.GetParamRequired("param2", param2);
   return new SpaceDummy<dist_t>(param1, param2);
}
```

To extract parameters, the user needs an instance of the class AnyParamManager (see the above example). In most cases, it is sufficient to call two functions: GetParamOptional and GetParamRequired. Parameter values specified in the commands line are interpreted as strings. The GetParam* functions can convert these string values to integer or floating-point numbers if necessary. A conversion occurs, if the type of a receiving variable (passed as a second parameter to the functions GetParam*) is different from a string. It is possible to use boolean variables as parameters. In that, in the command line, one has to specify 1 (for true) or 0 (for false). Note that the function GetParamRequired raises an error, if the request parameter was not supplied in the command line.

The function CreateDummy is registered in the space factory using a special macro. This macro should be used for all possible values of the distance function, for which our space is defined. For example, if the space is defined only for integer-valued distance function, this macro should be used only once. However, in our case the space CreateDummy is defined for integers, single- and double-precision floating pointer numbers. Thus, we use this macro three times as follows:

```
REGISTER_SPACE_CREATOR(int, SPACE_DUMMY, CreateDummy)
REGISTER_SPACE_CREATOR(float, SPACE_DUMMY, CreateDummy)
REGISTER_SPACE_CREATOR(double, SPACE_DUMMY, CreateDummy)
```

This macro should be placed into the function <code>initSpaces</code> in the file init_spaces.h. Last, but not least we need to include the helper function, which creates the class into file <code>init_spaces.h</code> as follows:

#include "factory/space/space_dummy.h"

6.3 Creating a method

To explain the basics of developing a new search method, we created a sample zero-functionality method <code>DummyMethod</code>. It is represented by the header file dummy.h and the source file dummy.cc. The user is encouraged to study these files and read the comments. Here we would omit certain minor details.

Similar to the space and query classes, a search method is implemented using a template class, which is parameterized by the distance function value:

```
template <typename dist_t>
class DummyMethod : public Index<dist_t> {
 public:
  DummyMethod(const Space<dist_t>* space,
              const ObjectVector& data,
              AnyParamManager& pmgr)
              : data_(data) {
    pmgr.GetParamOptional("doSeqSearch",
                                           bDoSeqSearch_);
    SetQueryTimeParamsInternal(pmgr);
  }
  ~DummyMethod(){};
  const std::string ToString() const;
  void Search(RangeQuery<dist_t>* query);
  void Search(KNNQuery<dist_t>* query);
  virtual vector<string> GetQueryTimeParamNames() const;
 private:
  virtual void SetQueryTimeParamsInternal(AnyParamManager& );
  const ObjectVector&
                          data_;
  // disable copy and assign
  DISABLE_COPY_AND_ASSIGN(DummyMethod);
};
```

Note that it is the constructor that creates a search index (or calls a function to create it)! Here it accepts the pointer to a space, a reference to an array of data objects, and an additional parameter. When this parameter is true, our dummy method will carry out a sequential search. Otherwise, it does nothing useful.

The space object is typically used to compute the distance by calling the function IndexTimeDistance. Note again that IndexTimeDistance should not be used in a function Search. If the user attempts to invoke IndexTimeDistance during the test phase, the program will terminate. ¹³

As noted previously, we want to compute the number of times the distance was computed for each query. This allows us to estimate the variance. Hence, during the testing phase, the distance function should be invoked only through a query object.

A method can have query time parameters, which can be changed without rebuilding the index. The function <code>GetQueryTimeParamNames</code> returns the list of names of such parameters. If this list is non-empty and the method is supposed to support query time modification of some parameters, these modifications are carried out inside the function <code>SetQueryTimeParamsInternal</code>.

Finally, we need to "tell" the library about the method, by registering the method in the method factory, similarly to registering a space. At runtime, the method is created through a helper function, which accepts several parameters. One parameter is a reference to an object of the type AllParams. In our case, the function name is CreateDummy:

There is an include-directive preceding the creation function, which uses angle brackets. As explained previously, if you opt to using quotes (in the include-directive), the code may not compile under the Visual Studio.

Note that, similarly to the dummy space example, we use a parameter extraction class AnyParamManager. The only difference, is that we retrieve an optional parameter doSeqSearch. If this parameter is not present in the command line, the code uses an old value of the variable bDoSeqSearch (which was set to false before we called GetParamOptional). An example of such function for the method MethodDummy is given in the file dummy.h.

Again, similarly to the case of the space, the method-creating function CreateDummy needs to be registered in the method factory in two steps. First, we need to include dummy.h into the file init_methods.h as follows:

```
#include "factory/method/dummy.h"
```

Then, this file is further modified by adding the following lines to the function initMethods:

```
REGISTER_METHOD_CREATOR(float, METH_DUMMY, CreateDummy)
REGISTER_METHOD_CREATOR(double, METH_DUMMY, CreateDummy)
REGISTER_METHOD_CREATOR(int, METH_DUMMY, CreateDummy)
```

If we want our method to work only with integer-valued distances, we only need the following line:

```
REGISTER_METHOD_CREATOR(int, METH_DUMMY, CreateDummy)
```

When adding the method, please, consider expanding the test utility test_integr. This is especially important if for some combination of parameters the method is expected to return all answers (and will have a perfect recall). Then, if we break the code in the future, this will be detected by test_integr.

To create a test case, the user needs to add one or more test cases to the file test_integr. A test case is an instance of the class MethodTestCase. It encodes the range of plausible values for the following performance parameters: the recall, the number of points closer to the query than the nearest returned point, and the improvement in the number of distance computations.

If you are using the script genplot.py (see § 3.7) to plot performances graphs, you will need to modify it as well. The function methodNameAndStyle in this script defines a mapping from the method name to plot marker. Currently, we provide markers for all the implemented methods. Yet, if you add a new one, you need to provide the mapping yourself (by modifying methodNameAndStyle). Note the name of the method is returned by the class member ToString.

6.4 Creating an application (inside the framework)

First, we create a hello-world source file dummy_app.cc:

```
#include <iostream>
using namespace std;
int main(void) {
  cout << "Hello world!" << endl;
}</pre>
```

Now we need to modify the meta-makefile similarity_search/src/CMakeLists.txt and re-run cmake as described in § 3.1.

More specifically, we do the following:

- by default, all source files in the similarity_search/src/ directory are included into the library. To prevent dummy_app.cc from being included into the library, we use the following command:

```
list(REMOVE_ITEM SRC_FILES ${PROJECT_SOURCE_DIR}/src/dummy_app.cc)
```

- tell cmake to build an additional executable:

```
add_executable (dummy_app dummy_app.cc ${SRC_FACTORY_FILES})
```

- specify the necessary libraries:

7 Notes on Efficiency

7.1 Efficiency of Distance Functions

Note that improvement in efficiency and in the number of distance computations obtained with slow distance functions can be overly optimistic. That is, when a slow distance function is replaced with a more efficient version, the improvements over sequential search may become far less impressive. In some cases, the search method can become even slower than the brute-force comparison against every data point. This is why we believe that optimizing computation of a distance function is equally important (and sometimes even more important) than designing better search methods.

In this library, we optimized several distance functions, especially non-metric functions that involve computations of logarithms. An order of magnitude improvement can be achieved by pre-computing logarithms at index time and by approximating those logarithms that are not possible to pre-compute (see \S 4.3 and \S 4.4 for more details). Yet, this doubles the size of an index.

The Intel compiler has a powerful math library, which allows one to efficiently compute several hard distance functions such as the KL-divergence, the Jensen-Shanon divergence/metric, and the L_p spaces for non-integer values of p more efficiently than in the case of GNU C++ and Clang. In the Visual Studio's fast math mode (which is enabled in the provided project files) it is also possible to compute some hard distances several times faster compared to GNU C++ and Clang. Yet, our custom implementations seems to be always twice as fast. For example, in the case of the Intel compiler, the custom implementation of the KL-divergence is 10 times faster than the standard one while the custom implementation of the JS-divergence is 7 times as fast as the standard one, while the custom JS-divergence is 10 times faster. Therefore, doubling the size of the data set by storing pre-computed logarithms seems to be worthwhile.

Efficient implementations of some other distance functions rely on SIMD instructions. These instructions, available on most modern Intel and AMD processors, operate on small vectors. Some C++ implementations can be efficiently vectorized by both the GNU and Intel compilers. That is, instead of the scalar operations the compiler would generate more efficient SIMD instructions. Yet, the code is not always vectorized by the Clang. And even the Intel compiler, fails to efficiently vectorize computation of the KL-divergence (with pre-computed logarithms).

There are also situations when we efficient automatic vectorization is hardly possible. For instance, we provide an efficient implementation of the scalar product for sparse *single-precision* floating point vectors. It relies on the all-against-all comparison SIMD instruction <code>_mm_cmpistrm</code>. However, it requires keeping the data in a special format, which makes automatic vectorization nearly impossible.

Intel SSE extensions that provide SIMD instructions are automatically detected by compilers but the Visual Studio. If these SSE extensions are not available, the compilation process will produce warnings like the following one:

LInfNormSIMD: SSE2 is not available, defaulting to pure C++ implementation!

Because we do not know a good way to create/modify Visual Studio project files that enable SSE extensions automatically (depending on whether hardware supports them), the user need to enable these extensions manually. For the instructions, the user is referred to \S 3.2.

7.2 Cache-friendly Data Layout

In our previous report [3], we underestimated a cost of a random memory access. A more careful analysis showed that, on a recent laptop (Core i7, DDR3), a truly random access "costs" about 200 CPU cycles, which may be 2-3 times longer than a computation of a cheap distance such as L_2 .

Many implemented methods use some form of bucketing. For example, in the VP-tree or bbtree we recursively decompose the space until a partition contains at most bucketSize elements. The buckets are searched sequentially, which could be done much faster, if bucket objects were stored in contiguous memory regions. Thus, to check elements in a bucket we would need only one random memory access.

A number of methods support this optimized storage model. It is activated by setting a parameter chunkBucket to 1. If chunkBucket is set to 1, indexing is carried out in two stages. At the first stage, a method creates unoptimized buckets, each of which is an array of pointers to data objects. Thus, objects are not necessarily contiguous in memory. In the second stage, the method iterates over buckets, allocates a contiguous chunk of memory, which is sufficiently large to keep all bucket objects, and copies bucket objects to this new chunk.

Important note: Note that currently we do not delete old objects and do not deallocate the memory they occupy. Thus, if chunkBucket is set to 1, the memory usage is overestimated. In the future, we plan to address this issue.

8 Data Sets

Currently we provide only vector space data sets that come in either dense or sparse format. For simplicity, these are textual formats where each row of the file contains a single vector. If a row starts with a prefix in the form: label:non-negative integer value < white-space>, the integer value is interpreted as the identifier of a class. These identifiers can be used to compute the accuracy of <math>k-NN based classification procedure.

Aside from the prefix, the sparse and dense vectors are stored in a different format. In the dense-vector format, each row contains the same number of vector elements, one per each dimension. The values can be separated by spaces or commas/columns. In the sparse format, each vector element is preceded by a zero-based vector element id. The ids can be unsorted, but they should not repeat. For example, the following line describes a vector with three explicitly specified values, which represent vector elements 0, 25, and 257:

0 1.234 25 0.03 257 -3.4

The vectors are sparse and most values are not specified. It is up to a designer of the space to decide on the default value for an unspecified vector element. All existing implementations use *zero* as the default value. Again, elements can be separated by spaces or commas/columns instead of spaces.

In addition, the directory sample_scripts contains the full set of scripts that can be used to re-produce our NIPS'13 and SISAP'13 results [3,4]. This includes the software to generate plots (see also § 3.7). Additionally, to reproduce our previous results, one needs to obtain a data set using the script data/get_data_nips2013.sh. To get all data set sets available, please, use the script data/get_all_data.sh.

The complete set contains the following:

- The data set created by Lawrence Cayton. To download, use the script data/download_cayton.sh;
- The Colors data set, which comes with the Metric Spaces Library[18]. To download, use the script data/download_colors.sh;
- The Wikipedia tf-idf vectors in the sparse format. To download, use the script data/download_wikipedia_sparse.sh;
- The Wikipedia dense 128-element vectors obtained from sparse vectors. Dimensionality is reduced via the singular value decomposition (SVD). To download, use the script data/download_wikipedia_lsi128.sh;
- A synthetic, randomly generated, 64-dimensional data set, where each coordinate is a real number sampled independently from U[0,1]: data/genunif.py -d 64 -n 500000 -o unif64.txt

Note that all data sets, except the Wikipedia tf-idf (sparse) vectors, are vectors in the dense format (see § 4). If we use any of them, please consider citing the sources (see Section 9) for details. Also note that, the data will be downloaded in the **compressed** form. You would need the standard **gunzip** to uncompress all the data except the Wikipedia (sparse and dense) vectors. The Wikipedia data is compressed using 7z, which provides superior compression ratios.

9 Licensing and Acknowledging the Use of Library Resources

The code that was written entirely by the authors is distributed under the business-friendly Apache License. The best way to acknowledge the use of this code in a scientific publication is to provide the URL of the GitHub repository¹⁴ and to cite our engineering paper:

¹⁴ https://github.com/searchivarius/NonMetricSpaceLib

```
@incollection{Boytsov_and_Bilegsaikhan:sisap2013,
  year={2013},
  isbn={978-3-642-41061-1},
 booktitle={Similarity Search and Applications},
  volume={8199},
  series={Lecture Notes in Computer Science},
  editor={Brisaboa, Nieves and Pedreira, Oscar and Zezula, Pavel},
  doi=\{10.1007/978-3-642-41062-8_28\},
  title={Engineering Efficient and Effective
         \mbox{Non-Metric Space Library}},
  url={http://dx.doi.org/10.1007/978-3-642-41062-8_28},
  publisher={Springer Berlin Heidelberg},
  keywords={benchmarks; (non)-metric spaces; Bregman divergences},
  author={Boytsov, Leonid and Naidan, Bilegsaikhan},
  pages={280-293}
}
  Most provided data sets are created by Lawrence Cayton. Our implemen-
tation of the bbtree, an exact search method for Bregman divergences, is also
based on the code of Cayton. If you use any of these, please, consider citing:
@inproceedings{cayton2008,
  title=
             {Fast nearest neighbor retrieval for bregman divergences},
  author=
             {Cayton, Lawrence},
 booktitle= {Proceedings of the 25th international conference on
             Machine learning},
  pages=
             {112--119},
  year=
             {2008},
  organization={ACM}
}
  The Colors data set originally belongs to the Metric Spaces Library:
@misc{LibMetricSpace,
  Author =
              {K.~Figueroa and G.{}~Navarro and E.~Ch\'avez},
  Keywords = {Metric Spaces, similarity searching},
  Lastchecked = {August 18, 2012},
 Note = {Available at
         {\url{http://www.sisap.org/Metric\_Space\_Library.html}}},
  Title = {\mbox{Metric Spaces Library}},
  Year = \{2007\}
}
  The Wikipedia data sets were created with a help of the gensim library:
@inproceedings{rehurek_lrec,
  title = {{Software Framework for Topic Modelling
            with Large Corpora}},
```

Last, but not least, our library incorporates the efficient LSHKIT library. Note that is is distributed under a different license: GNU General Public License version 3 or later.

If you (re)-use it, please, consider citing the authors:

```
@inproceedings{Dong_et_al:2008,
                {Dong, Wei and Wang, Zhe and Josephson, William
 author =
                  and Charikar, Moses and Li, Kai},
                {Modeling LSH for performance tuning},
 title =
 booktitle =
                {Proceedings of the 17th ACM conference on Information
                 and knowledge management},
                {CIKM '08},
 series =
 year =
                {2008},
                {978-1-59593-991-3},
 isbn =
 location =
                {Napa Valley, California, USA},
                {669--678},
 pages =
 numpages =
                {10},
 url =
                {http://doi.acm.org/10.1145/1458082.1458172},
 doi =
                {10.1145/1458082.1458172},
 acmid =
                {1458172},
 publisher =
                {ACM},
 address =
                {New York, NY, USA},
keywords = {locality sensitive hashing, similarity search},
```

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Table 3: Parameters of space partitioning methods

| | Common parameters |
|------------------|---|
| bucketSize | A maximum number of elements in a bucket/leaf. |
| chunkBucket | Indicates if bucket elements should be stored contiguously in memory (1 by default). |
| maxLeavesToVisit | An early termination parameter equal to the maximum number of buckets (tree leaves) visited by a search algorithm (2147483647 by default). |
| | VP-tree (vptree) [32,34] |
| | Common parameters bucketSize, chunkBucket, and maxLeavesToVisit |
| alphaLeft | A stretching coefficient α_{left} in Equation (5) |
| alphaRight | A stretching coefficient α_{right} in Equation (5) |
| | Multi-Vantage Point Tree (mvptree) [5] |
| | Common parameters bucketSize, chunkBucket, and maxLeavesToVisit |
| maxPathLen | the maximum number of top-level pivots for which we memorize distances to data objects in the leaves $$ |
| | GH-tree (ghtree) [32] |
| | Common parameters bucketSize, chunkBucket, and maxLeavesToVisit |
| | List of clusters (list_clusters) [10] |
| | Common parameters bucketSize, chunkBucket, and maxLeavesToVisit. Note maxLeavesToVisit is a query time parameter. |
| useBucketSize | If equal to one, we use the parameter bucketSize to determine the number of points in the cluster. Otherwise, the size of the cluster is defined by the parameter radius. |
| radius | The maximum radius of a cluster (used when ${\tt useBucketSize}$ is set to zero). |
| strategy | A cluster selection strategy. It is one of the following: random, closestPrevCenter, farthestPrevCenter, minSumDistPrevCenters, maxSumDistPrevCenters. |
| | SA-tree (satree) [27] |
| | No parameters |
| | bbtree (bbtree) [7] |
| | Common parameters bucketSize, chunkBucket, and maxLeavesToVisit |

Table 4: Parameters of LSH methods

| | Table 4: Parameters of LSH methods | |
|--|--|--|
| Common parameters | | |
| W | A width of the window [13]. | |
| M | A number of atomic (binary hash functions), which are concatenated to produce an integer hash value. | |
| Н | A size of the hash table. | |
| L | The number hash tables. | |
| Multiprobe LSH: only for L_2 (1sh_multiprobe) [25,14,13] | | |
| | Common parameters W, M, H, and L | |
| Т | a number of probes | |
| desiredRecall | a desired recall | |
| tuneK | find optimal parameter for $k\text{-NN}$, search where k is defined by this parameter | |
| L | SH Gaussian: only for L_2 (lsh_gaussian) [9] | |
| | Common parameters W, M, H, and L | |
| | LSH Cauchy: only for L_1 (1sh_cauchy) [9] | |
| | Common parameters W, M, H, and L | |
| LSH | thresholding: only for L_1 (lsh_threshold) [33,24] | |
| | Common parameters M, H, and L (W is not used) | |
| | | |

Table 5: Parameters of permutation-based filtering methods

| Table | 5: Parameters of permutation-based filtering methods |
|------------------------|--|
| | Common parameters |
| numPivot | A number of pivots. |
| dbScanFrac | A number of candidate records obtained during the filtering step. It is specified as a <i>fraction</i> (not a percentage!) of the total number of data points in the data set. |
| binThreshold | Binarization threshold. If a value of an original permutation vector is below this threshold, it becomes 0 in the binarized permutation. If the value is above, the value is converted to 1. |
| В | rute-force permutation search (permutation) [19] |
| | Common parameters numPivot and dbScanFrac. |
| Brute-force pe | rmutation search with incremental sorting (perm_incsort) [19] |
| | Common parameters numPivot and dbScanFrac. Note that dbScanFrac is a query time parameter. |
| | PP-index (perm_prefix) [16] |
| numPivot | A number of pivots. |
| minCandidate | a minimum number of candidates to retrieve (note that we do not use dbScanFrac here. |
| prefixLength | a maximum length of the tree prefix that is used to retrieve candidate records. |
| chunkBucket | 1 if we want to store vectors having the same permutation prefix in the same memory chunk (i.e., contiguously in memory) |
| Inv | verted index over permutations (perm_inv_indx) [2] |
| | Common parameters numPivot and dbScanFrac. |
| numPivotIndex | a number of (closest) pivots to index |
| ${\tt numPivotSearch}$ | a number of (closest) pivots to use during searching |
| maxPosDiff | the maximum position difference permitted for searching in the inverted file |
| Inverted in | ndex over pivot neighborhoods (pivot_neighb_invindx) [31] |
| | Common parameter numPivot. |
| invProcAlg | An algorithm to merge posting lists. In practice, only scan worked well. |
| chunkIndexSize | A number of documents in one index chunk. Select a small value (in the order of several thousands) for better cache utilization. |
| ${\tt indexThreadQty}$ | A number of indexhing threads. |
| minPrefix | A number of most closest pivots to be indexed. |
| minTimes | A candidate entry should share this number of pivots with the query. This is a query time parameter. |
| - | |

Table 6: Parameters of permutation-based filtering methods (continued)

Brute-force search with incremental sorting for binarized permutations (perm_incsort_bin) [30]

Common parameters numPivot, dbScanFrac, binThreshold.

VP-tree index over binarized permutations (perm_bin_vptree)

Similar to [30], but uses an approximate search in the VP-tree.

Common parameters numPivot, dbScanFrac, binThreshold.

VP-tree index over permutations (perm_vptree)

Similar to [17], but uses an approximate search in the VP-tree.

Common parameters numPivot and dbScanFrac. Note that dbScanFrac is a query time parameter.

alphaLeft A stretching coefficient α_{left} in Equation (5)

alphaRight A stretching coefficient α_{right} in Equation (5)

Note: mnemonic method names are given in round brackets.

Table 7: Parameters of miscellaneous methods

| $k\text{-NN}$ graph (bottom-up and greedy index creation) (small_world_rand) [26] | | |
|---|--|--|
| NN | A number of close entries returned by one sub-search. | |
| $\verb"initSearchAttempts"$ | A number of sub-searches to answer one query. This is a query time parameter. | |
| $\verb"initIndexAttempts"$ | A number of sub-searches to add one data point during indexing. | |
| ${\tt indexThreadQty}$ | A number of indexing threads. | |
| Severa | l copies of the same index type (mult_index) | |
| indexQty | A number of copies | |
| methodName | A mnemonic method name | |
| | Any other parameter that the method accepts. For instance, if we create several copies of the VP-tree, we can specify the parameters alphaLeft, alphaRight, maxLeavesToVisit, and so on. | |
| Ex | chaustive/sequential search (seq_search) | |
| | No parameters. | |
| | | |