

# **RSA**®Conference2018

San Francisco | April 16 – 20 | Moscone Center

SESSION ID: CRYPT-W04

## **CRYPTOGRAPHIC PROTOCOLS: PRACTICAL REVOCATION AND KEY ROTATION**

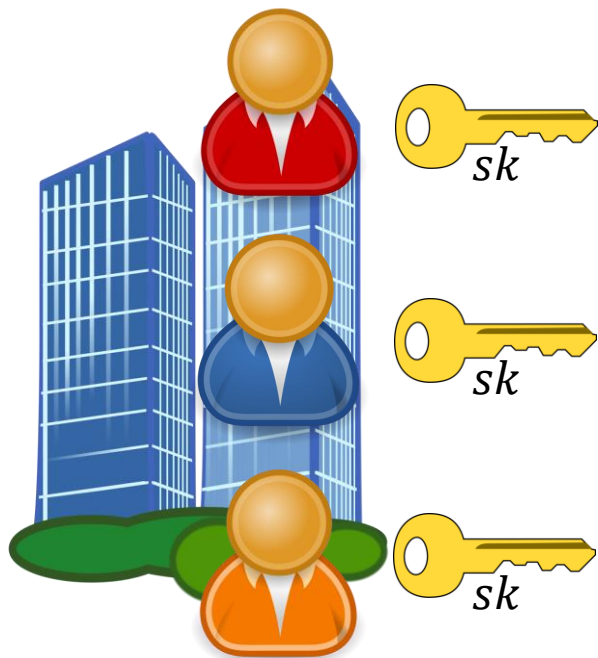
**Adam Shull**

Recent Ph.D. Graduate  
Indiana University



#RSAC

# Access revocation on the cloud

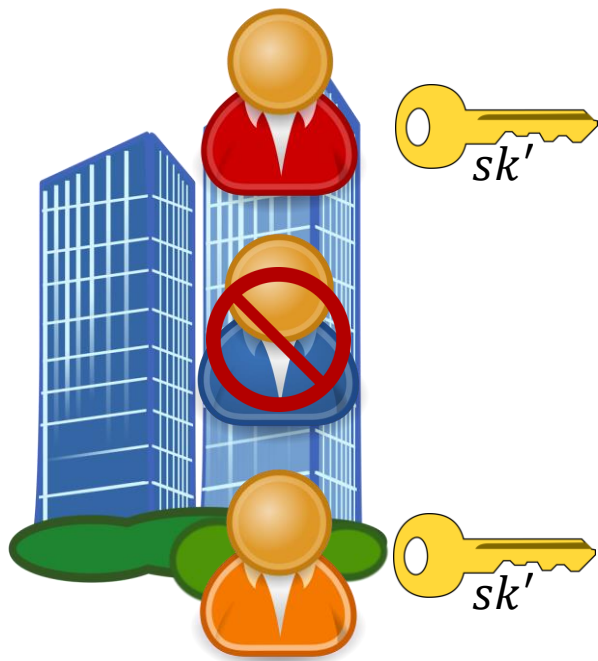


$(\text{Enc}_{pk}^{\text{Pub}}(k_1), \text{Enc}_{k_1}^{\text{Sym}}(f_1))$

$(\text{Enc}_{pk}^{\text{Pub}}(k_2), \text{Enc}_{k_2}^{\text{Sym}}(f_2))$

$(\text{Enc}_{pk}^{\text{Pub}}(k_3), \text{Enc}_{k_3}^{\text{Sym}}(f_3))$

# Access revocation on the cloud



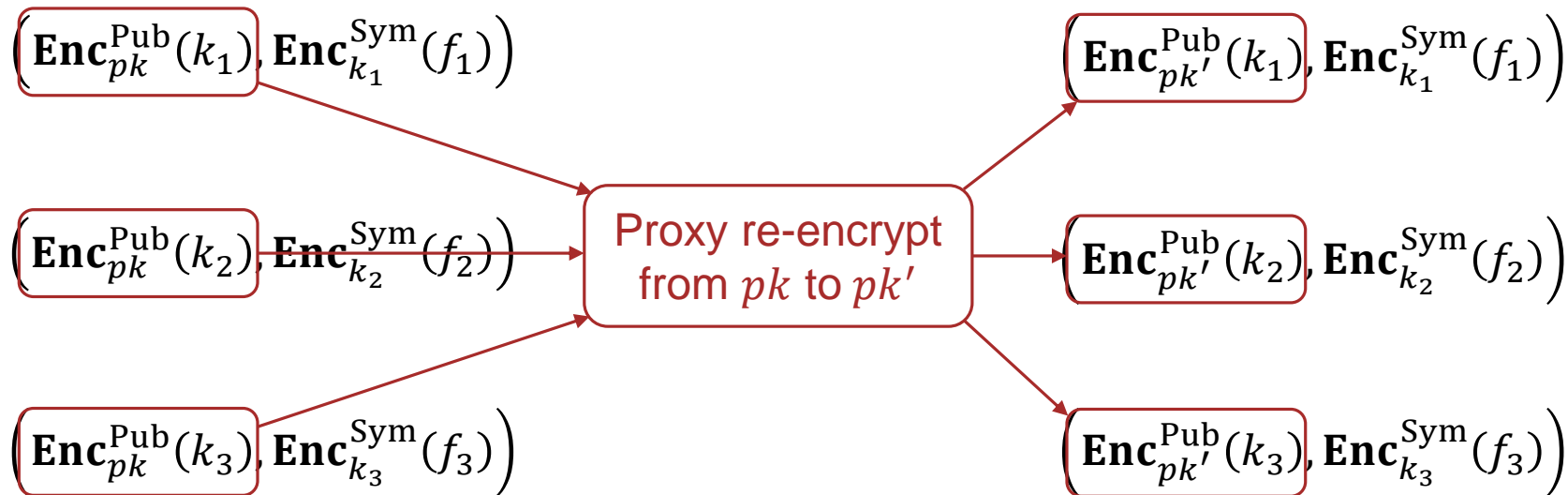
$(\text{Enc}_{pk}^{\text{Pub}}(k_1), \text{Enc}_{k_1}^{\text{Sym}}(f_1))$

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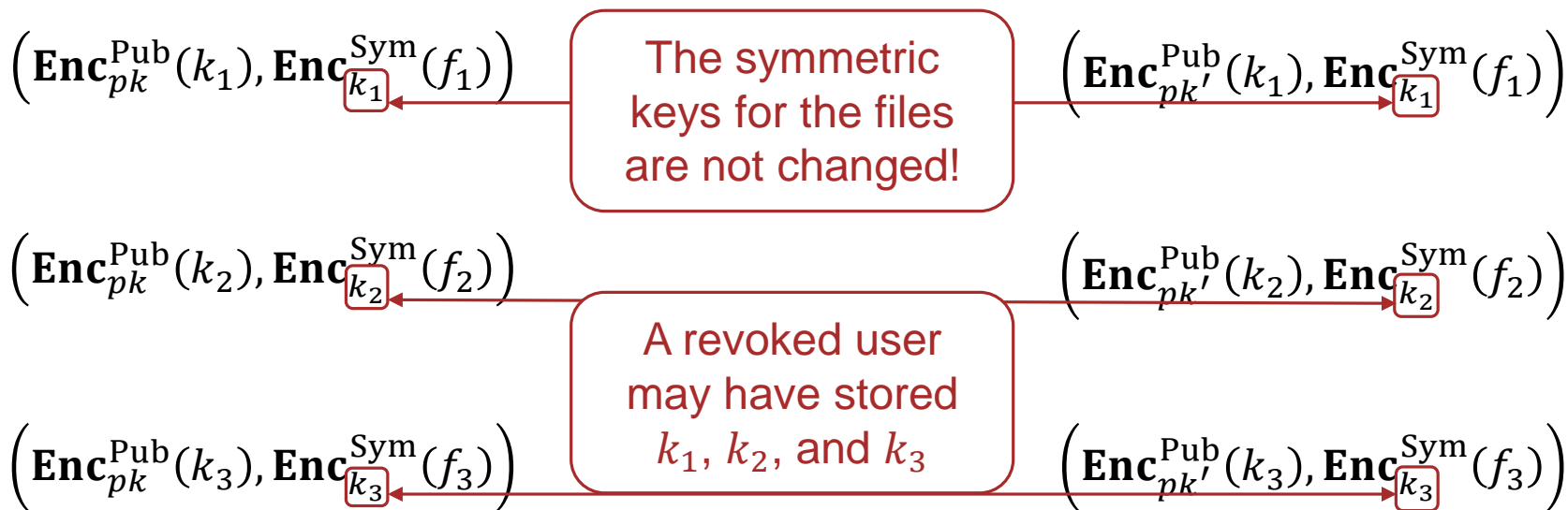
$(\text{Enc}_{pk}^{\text{Pub}}(k_3), \text{Enc}_{k_3}^{\text{Sym}}(f_3))$



# Revocation using proxy re-encryption



# Key-scraping attack



# The symmetric key must be changed!

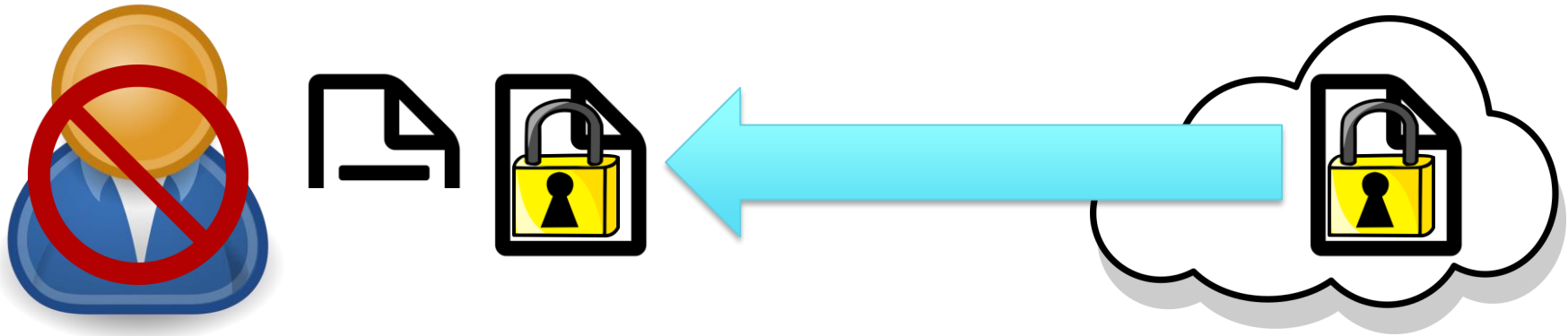


- Decrypt with old key, encrypt with new key
  - Requires trusted re-encryptor and takes two full passes for re-encryption
- Encrypt existing ciphertext with new key
  - Decryption takes one full pass for each previous re-encryption
- Key-homomorphic pseudorandom functions
  - Allow untrusted party to re-encrypt to fresh key
  - Existing key-homomorphic pseudorandom functions are extremely slow

# Security model



# Security model





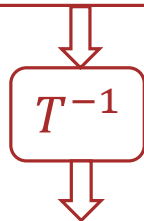
# All-or-nothing transform (AONT)



0111101100101111010010011100100011001110001111010100010010010111



101011000011111101001010101110100111011000101010001010100111000



0111101100101111010010011100100011001110001111010100010010010111

# All-or-nothing transform (AONT)



0111101100101111010010011100100011001110001111010100010010010111



$T$



1010110 001111 110100101010 11 10011101100010 01 0010101 0 11000



$T^{-1}$



?

0111101100101111010010011100100011001110001111010100010010010111



1010110000111111010010101011101001110110011000101010001010100111000

## XOR with a pseudorandom string

1010110100111101101001010101110100111011000101011001010100011000

# Security intuition



1010110000111111101001010101110100111011000101010001010100111000



10101100001111111010010101011101

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10101100001111111010010101011101

+

1010110100111101101001010101110100111011000101011001010100011000



1010110000111111101001010101110100111011000101011001010100011000

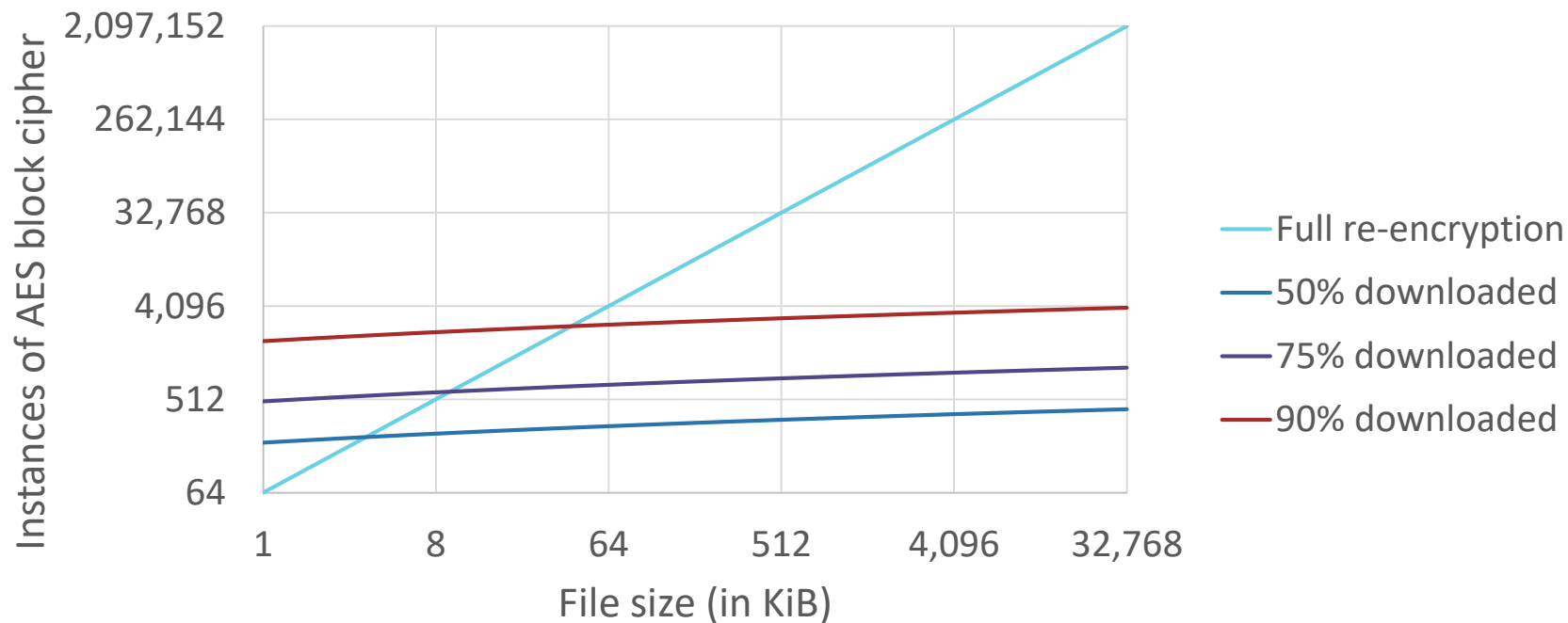


# Proxy re-encryption construction

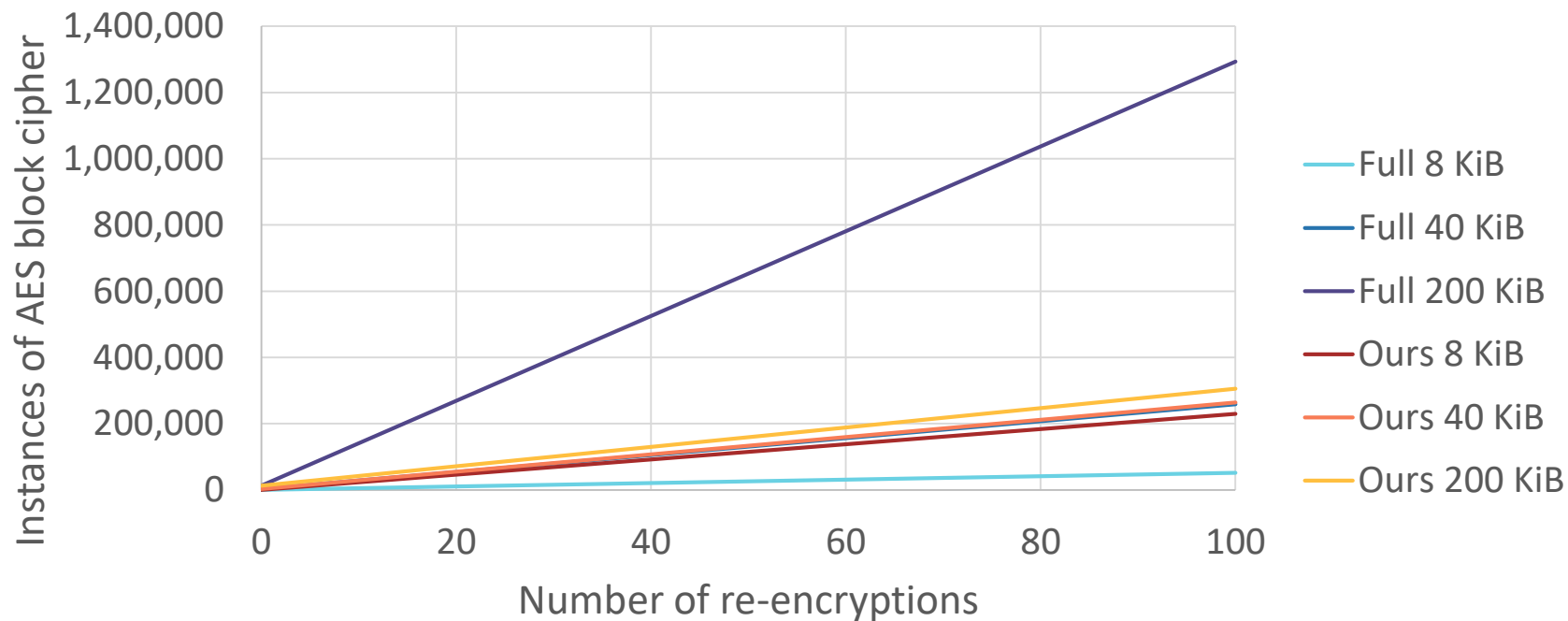


- Initial ciphertext:  $\left( \mathbf{Enc}_{pk}(k_0), T \left( \mathbf{Enc}_{k_0}^{\text{Sym}}(f) \right) \right)$
- Once re-encrypted ciphertext:  
$$\left( \mathbf{Enc}_{pk'}(k_0), [\mathbf{Enc}_{pk'}(s_1, k_1)], \left[ T \left( \mathbf{Enc}_{k_0}^{\text{Sym}}(f) \right) \right]_{\text{Ind}(s_1), \text{Ctr}(k_1)} \right)$$
- Twice re-encrypted ciphertext:  
$$\left( \mathbf{Enc}_{pk''}(k_0), [\mathbf{Enc}_{pk''}(s_1, k_1), \mathbf{Enc}_{pk''}(s_2, k_2)], \left[ \left[ T \left( \mathbf{Enc}_{k_0}^{\text{Sym}}(M) \right) \right]_{\text{Ind}(s_1), \text{Ctr}(k_1)} \right]_{\text{Ind}(s_2), \text{Ctr}(k_2)} \right)$$

# Result: Much faster re-encryption



# Result: Much faster decryption



# Summary



- In scenarios such as access revocation and key rotation, symmetric-key ciphertexts may need to be re-encrypted
- Existing solutions are either insecure or too slow to be used in practice
- Using an all-or-nothing transform, we can re-encrypt efficiently while achieving provable security under a reasonable model
- We provide constructions for updatable symmetric-key encryption, public-key and identity-based proxy re-encryption, and revocable-storage attribute-based encryption



# Apply What You Have Learned



- Realize the need to update the symmetric key
  - Many papers on public-key revocation don't consider hybrid encryption
  - Realistic security models must address key-scraping attacks
- Possible future work:
  - Produce a general theorem encompassing all uses of symmetric-key encryption
  - Assess tradeoffs between streaming efficiency and security
  - Provide a full implementation of the construction

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## ASYNCHRONOUS PROVABLY-SECURE HIDDEN SERVICES

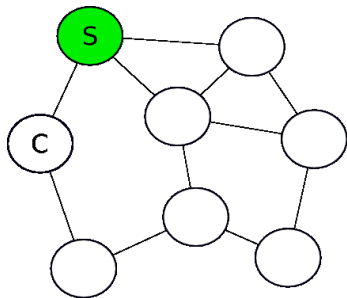


#RSAC

Fernando Krell   Philippe Camacho

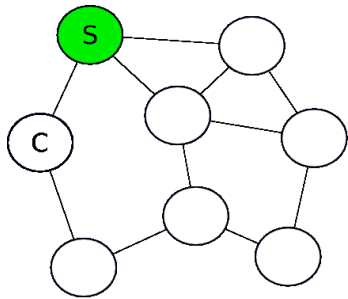


# Problem: how to hide the location of a server?

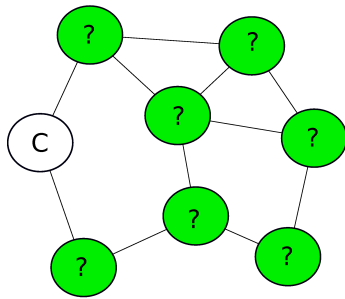


- Arbitrary network topology
- One node acts as a server
- Other nodes can be clients

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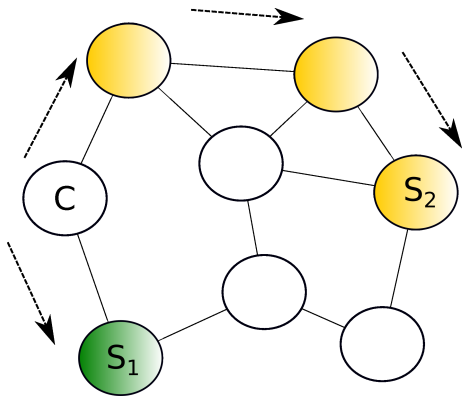
- Arbitrary network topology
- One node acts as a server
- Other nodes can be clients



- Avoid DoS
- Reduce attack surface
- Censorship resistance
- Traffic analysis



# Naive Solution: Recursive Multicast

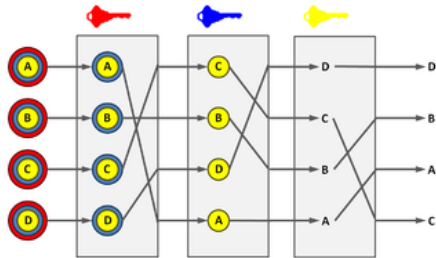


- If C contacts  $S_1$ , the response will arrive after  $\approx 2T$
- If C contacts  $S_2$ , the response will arrive after  $\approx 6T$

# Anonymity: Synchronous Solutions



## Mix-nets [Chaum '81]

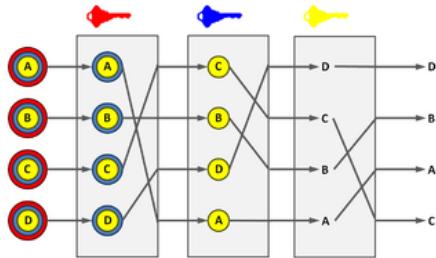


- Provably secure

# Anonymity: Synchronous Solutions

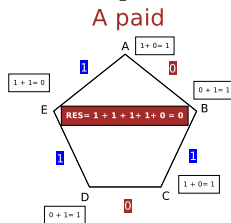


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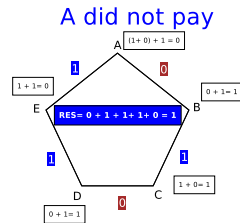


● Provably secure

## DC-nets [Chaum '88]



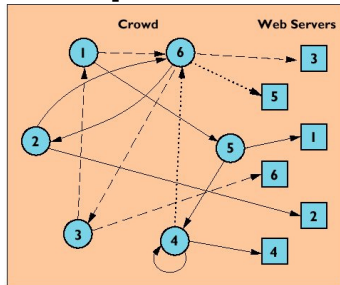
● Provably secure



# Anonymity: Asynchronous Alternatives



## Crowds [Reiter & Rubin '98]



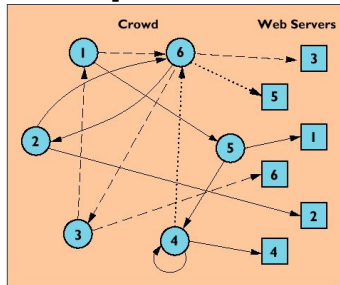
- Asynchronous
- Several attacks



# Anonymity: Asynchronous Alternatives

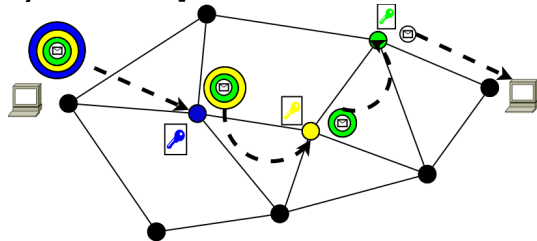


## Crowds [Reiter & Rubin '98]



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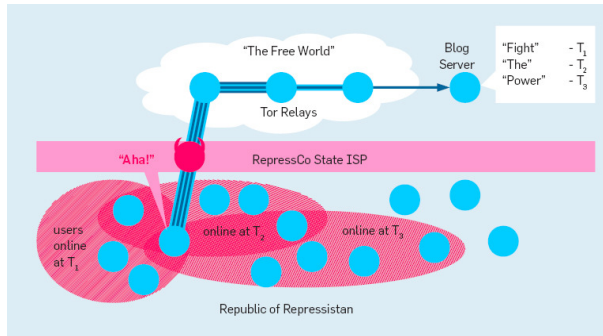
## Tor [Dingledine & Mathewson & Syverson '04]



- Asynchronous
- Several attacks
- Most popular

# Intersection attack

⇒ lower bound on communication



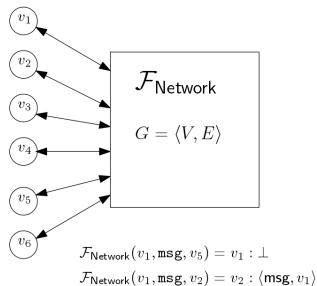
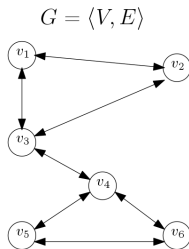
Thus all the nodes must participate in order to hide the server's location.

# Can we get the best of both worlds (Provably Secure and Asynchronous)?



	Asynchronous	Synchronous
<b>Provably Secure</b>	<a href="#">This work</a>	DC-nets/ mix-nets, DO'00
<b>Heuristic Security</b>	Tor,Crowds	Herbivore [GRPS '03]

- Simulation based security definition.
- Communication restricted to use  $\mathcal{F}_{\text{Network}}$ 
  - $P_i$  is allowed to send message to  $P_j$ , if they are directly connected.



# Overview of our solution



Participant's behavior is indistinguishable from server's.

- ① **Client.** Broadcast the request
- ② **Player  $P_i$ .** Upon seeing a request message, send a random value  $s_i$  to the server (broadcast)
- ③ **Player  $P_i$ .** Upon seeing everybody's values  $\{s_j\}$ :
  - **If  $P_i = \text{Server}$ .** Secret share response  $r$  using  $\{s_j\}$ .  
Send share  $r - \sum s_j$  to client.
  - **Else.** Submit  $s_i$  to client.
- ④ **Client.** Upon receiving all shares, reconstruct the server's response  $r$ .



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Naive implementation has  $O(n^2)$  communication complexity.

# Efficient Implementation



- Avoid recursive multicast on every message.
- Combine encrypted shares on intermediate nodes.

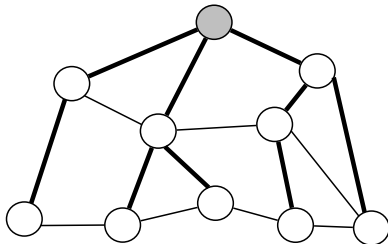
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Extra Tools:

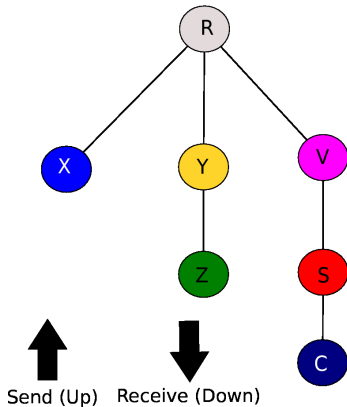
- **Homomorphic Encryption**
  - $\text{Enc}_{pk}(m_1) + \text{Enc}_{pk}(m_2) = \text{Enc}_{pk}(m_1 + m_2)$
- **Spanning Tree**



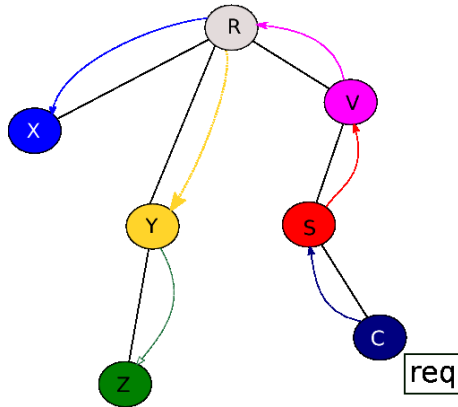
# Communication Pattern



Avoiding quadratic complexity:



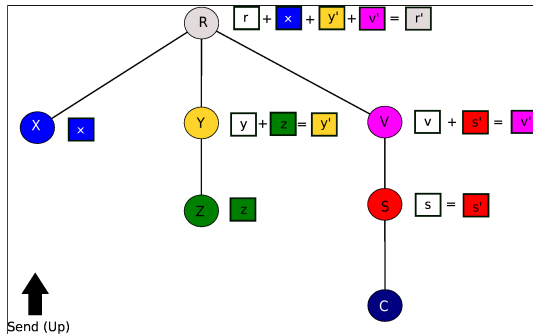
# Phase 1: Broadcast the Request



## Phase 2.a): Shares UP to root



Shares are encrypted for the server, and sent up the tree.

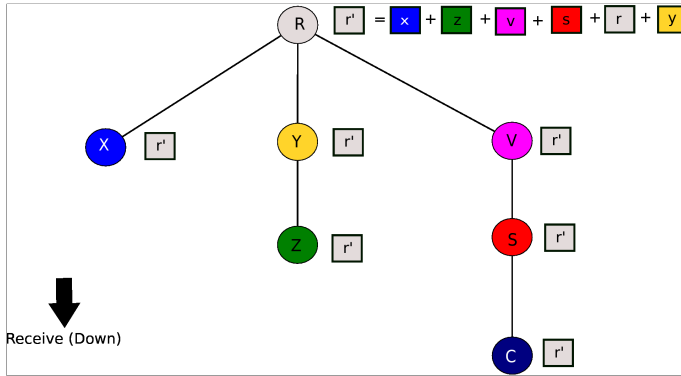


All shares are added using homomorphic encryption:

$$\text{Enc}_{\text{pk}^S}(\mathbf{y}) \cdot \text{Enc}_{\text{pk}^S}(\mathbf{z}) = \text{Enc}_{\text{pk}^S}(\mathbf{y} + \mathbf{z}) = \text{Enc}_{\text{pk}^S}(\mathbf{y}')$$



## Phase 2.b): Shares' sum DOWN to server



The encrypted sum  $\sum_{N_i \neq C} \text{share}_{N_i}$  is sent down the tree so that the server S can decrypt it.

## Phase 3: Server change its share



- The response to `req` is computed by the server  $S$ :

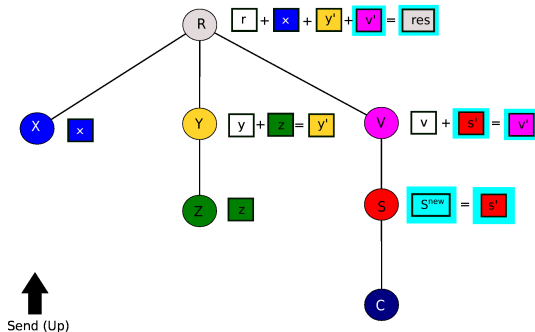
$$\text{res} := F(\text{req})$$

- The server recomputes its own share:

$$\text{share}_S^{\text{new}} := \text{res} - \left( \sum_{N_i \neq C} \text{share}_{N_i} - \text{share}_S^{\text{old}} \right)$$

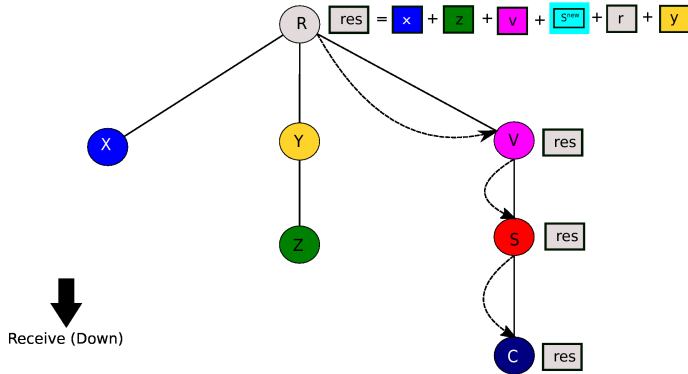
- The new share of the server and the share of the other nodes add up to `res`:

# Phase 4.a): Response shares sent to root



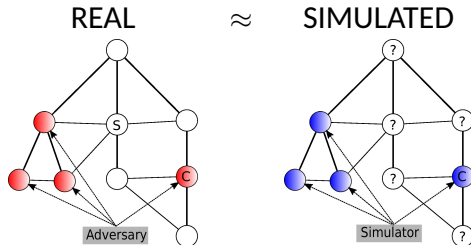
- All  $N_i \neq C$  (including S) send their share  $\text{share}_i$  to C.
- S will send  $\text{share}_S^{\text{new}}$  instead of  $\text{share}_S^{\text{old}}$ .
- All shares are added using homomorphic encryption (using C's public key):  $\text{Enc}_{\text{pk}C}(y) \cdot \text{Enc}_{\text{pk}C}(z) = \text{Enc}_{\text{pk}C}(y + z) = \text{Enc}_{\text{pk}C}(y')$

# Phase 4.b) Encrypted response sent to client



The encrypted response  $\text{res} = \sum_{N_i \neq C} \text{share}_{N_i}$  is sent down the tree so that the client **C** can decrypt it.

# Security based on simulation



- When client is not corrupted: just simulate protocol under fake messages.
- When client is corrupted:
  - Simulator  $S$  gets response from ideal functionality.
  - $S$  changes honest parties shares so that they reconstruct the correct response.

# Linear Complexity



- $O(1)$  messages per Spanning Tree Edge.
- $O(1)$  homomorphic encryption operations.

Although a node can have  $O(n)$  worst case complexity.



# Malicious Adversaries (Overview)



Adversary's strategies:

- Drop messages. DoS.
- Change shares. DoS.

New Protocol:

- Messages are signed.
- Use recursive multicast for all messages ( $O(n^2)$  Comm. complexity).
- Append zero-knowledge proof that ciphertexts encrypt same share. Allow identification of malicious players.

# Zero-knowledge proof



- Prove that two ciphertexts encrypt same message, except...

# Zero-knowledge proof



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- Server actually **changes** the share.
- Proof needs to convince that
  - [1] The two ciphertexts encrypt same message **OR**
  - [2] The issuer is the server

# Zero-knowledge proof



- Prove that two ciphertexts encrypt same message, except...
- Server actually **changes** the share.
- Proof needs to convince that
  - [1] The two ciphertexts encrypt same message **OR**
  - [2] The issuer is the server
- Do not reveal whether which of [1] , [2] is true.
- Reduces to simple  $\Sigma$ -protocol for relation

$$R_{g_1, g_2} = \underbrace{\{(A, B; r) : A = g_1^r \wedge B = g_2^r\}}_{[1]} \cup \underbrace{\{(D; s) : D = g^s\}}_{[2]}$$

# Future work



- Resilience. Protocol needs to succeed even if some players disappears
- Improve communication complexity of second protocol
- Empirical Study
- Find trade-offs to scale current solution
- Server anonymity

Questions?